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Estimating the gravity model without gravity using panel data

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Estimating the gravity model without gravity using panel data*

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Abstract

This paper examines the effects of zero trade on the estimation of the gravity model using both simulated and real data with a panel structure, which is different from the more conventional cross-sectional structure. We begin by showing that the usual log-linear estimation method can result in highly deceptive inference when some observations are zero. As an alternative approach, we suggest using the poisson fixed effects estimator. This approach eliminates the problems of zero trade, controls for heterogeneity across countries, and is shown to perform well in small samples.

JEL Classification: F10; F15; C15; C23.

Keywords: Gravity model of trade; Poisson regression model; Panel data; Monte Carlo simulation.

1 Introduction

The gravity model of trade has been widely used to estimate the impact of various policy issues, including preferential trade agreements, currency unions, and border effects. The model has a long tradition in social sciences where it has been used to model, for example, migration. In economics, the model has become very popular due to its success in explaining trade

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7 flows among countries. Some critique for the lack of theoretical underpinnings has emerged
8 but much progress has been made and now the gravity model rests on a solid theoretical
9 foundation. Instead, the focus has shifted towards the estimation techniques used.

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11 The gravity model has traditionally been estimated using cross-sectional data. However,
12 this has been shown to generate biased results since heterogeneity among the countries is
13 typically not controlled for in an appropriate way, see Cheng and Wall (2005), and Cheng
14 and Tsai (2008). To mitigate this problem, researchers have turned towards panel data,
15 which have the advantage that they permit more general types of heterogeneity. For example,
16 consider estimating the impact of currency unions on trade while controlling for country-pair
17 propensity to trade. For a single cross-section, these controls can only depend on observed
18 country-pair attributes such as common language, and estimates can thus be biased if there
19 is additionally an unobserved component to the propensity to trade. With panel data, such
20 unobserved heterogeneity can be readily controlled for by means of a country-pair fixed effects
21 model, which is more general than both the pooled cross-sectional and country specific fixed
22 effects panel data models.
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32 The single most popular approach to estimating the gravity model using panel data is
33 to first make it linear by taking logarithms and then to estimate the resulting log-linear
34 model by the fixed effects least squares (LS). However, although simple to implement, this
35 approach is problematic because the log-linearized model is not defined for observations with
36 zero trade. Moreover, even though the proportion of observations with zero trade may vary
37 somewhat depending on, among other things, the size of the sample, it is usually quite
38 significant, suggesting that the proper handling of these zeros is potentially very important.
39 Another problem is that the LS estimator of the log-linearized model may be both biased and
40 inefficient in the presence of heteroskedasticity.
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47 Two of the most common approaches to handle the presence of zero trade are to either
48 simply discarding the zeros from the sample, or to add a constant factor to each observation
49 on the dependent variable. The first strategy is correct as long as the zeros are randomly
50 distributed. However, if the zeros are not random, as is usually the case, then this induces
51 a selection bias. This problem is often ignored in applied work, but could be handled by
52 using sample selection correction. In a recent contribution, Helpman *et al.* (2008) propose
53 a theoretical model rationalizing the zero trade flows and suggest estimating the gravity
54 equation with a correction for the probability of countries to trade. To estimate the model
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7 they apply a two-step estimation technique similar to sample selection models. However,
8 in order to implement the new estimator, the researcher needs to find a suitable exclusion
9 restriction for identification of the second stage equation, which can be quite difficult. The
10 problem with bias and inefficiency in the presence of heteroskedasticity has been largely
11 ignored by applied researchers.
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15 In this paper, we explore and extend upon an idea first pointed out by Wooldridge (2002),
16 namely that the fixed effects panel poisson maximum likelihood (ML) estimator can be applied
17 also to continuous variables. We therefore propose estimating the gravity model directly from
18 its non-linear form by using the poisson ML estimator. Since this removes the need to
19 linearize the model by taking logarithms, the problem with zero trade disappears. A similar
20 approach has recently been proposed by Silva and Tenreyro (2006), who also use the poisson
21 ML estimator. However, they use cross-sectional data, and focus mainly on the issue of
22 heteroskedasticity. Our approach is more general in the sense that it permits one to get
23 rid of the problems of zero trade and heteroskedasticity while simultaneously taking care of
24 the bias caused by country specific heterogeneity, which cannot be accomplished when using
25 cross-sectional data.
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30 Our simulation results suggest that the new estimation method is superior to the conven-
31 tional approach of applying LS to the log-linearized model. In particular, it is shown that the
32 conventional approach is likely to result in severe bias and misleading inference even if the
33 fraction of observations with zero trade is very small. On the other hand, the poisson ML
34 estimator generally performs very well with only small bias and size distortion. Therefore,
35 since the poisson ML estimator is becoming increasingly available using standard statistical
36 software packages, these results suggest that it should be a valuable tool for econometric
37 analysis of the gravity model. As an empirical illustration, we consider the trade effects of
38 the 1995 European Union (EU) enlargement.
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43 The remainder of this paper is organized as follows. Section 2 briefly outlines the gravity
44 model and the problems of zero trade. Section 3 then presents the Monte Carlo simulations,
45 while Section 4 contains the application. Section 5 concludes.
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49 2 The problem of zero gravity

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51 Let M_{ijt} denote the bilateral trade between countries $i = 1, \dots, n$ and $j = 1, \dots, n$ with $i \neq j$ at
52 time $t = 1, \dots, T$, as measured by the imports of country i from country j . For convenience,
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the total number of observations per time period, which is given by $n(n-1)$, is henceforth denoted by N .¹ A common empirical formulation of the gravity model for bilateral trade includes the GDP levels of the two countries, Y_{it} and Y_{jt} say, as well as D_{ijt} , a dummy variable representing for example some contiguity, common language or free-trade agreement effect. This formulation of the gravity equation can be written algebraically as

$$\lambda_{ijt} = E(M_{ijt}|Y_{it}, Y_{jt}, D_{ijt}) = \exp(\gamma D_{ijt}) Y_{it}^{\beta_1} Y_{jt}^{\beta_2}. \quad (1)$$

Because only a very limited amount of heterogeneity between the country pairs is allowed in the parametrization of the regression function, conventional cross-section estimates of the gravity model are generally biased. With panel data, on the other hand, we can easily permit for such heterogeneity by means of N country-pair specific effects, denoted α_{ij} . These effects may be different depending on the direction of trade and enters (1) multiplicatively in the following fashion

$$E(M_{ijt}|Y_{it}, Y_{jt}, D_{ijt}, \alpha_{ij}) = \exp(\alpha_{ij} + \gamma D_{ijt}) Y_{it}^{\beta_1} Y_{jt}^{\beta_2} = \exp(\alpha_{ij}) \lambda_{ijt}.$$

This implicitly defines the following regression

$$M_{ijt} = \exp(\alpha_{ij}) \lambda_{ijt} + e_{ijt},$$

which can be written equivalently as

$$M_{ijt} = \exp(\alpha_{ij}) \lambda_{ijt} v_{ijt}, \quad (2)$$

where e_{ijt} is a mean zero disturbance that is independent of the regressors, and where $v_{ijt} = 1 + e_{ijt}/\exp(\alpha_{ij})\lambda_{ijt}$ is a heteroskedastic disturbance term with $E(v_{ijt}|Y_{it}, Y_{jt}, D_{ijt}, \alpha_{ij}) = 1$. Moreover, since α_{ij} will generally be correlated with the explanatory variables, random effects estimation of (2) will be inconsistent. To circumvent this, it is common to treat α_{ij} as fixed.

Suppose for a moment that M_{ijt} is strictly positive. One of the most common approaches to estimate the regression in (2) is to first make it linear by taking logarithms, which yields

$$\ln(M_{ijt}) = \alpha_{ij} + \ln(\lambda_{ijt}) + \ln(v_{ijt}) = \alpha_{ij} + \gamma D_{ijt} + \beta_1 \ln(Y_{it}) + \beta_2 \ln(Y_{jt}) + \ln(v_{ijt}). \quad (3)$$

Since the model is now linear, it is readily estimable using LS. However, this is only possible as long as M_{ijt} is nonzero, which is not always the case. Indeed, a common feature of trade

¹Note that since each country is both an exporter and an importer in a bilateral trade relation, each country pair is observed twice. The number of observations is therefore twice the number of country pairs.

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data is that the bilateral trade can sometimes be zero. Although this poses no problem when estimating the gravity model based on its multiplicative form in (2), as the logarithm is defined only for positive outcomes, the log-linear regression in (3) is no longer admissible. A common solution to this problem is to drop all observations with zero trade, and then to estimate (3) based on the resulting truncated sample. However, although this approach certainly eliminates the zeros, it simultaneously induces a bias to the LS estimator, which is why truncating the sample should be avoided as a matter of practice.

A natural alternative approach in situations such as this, when the model cannot be log-linearized, is to estimate it from its multiplicative form directly. In so doing, note that the fixed effects conditional mean can be written as

$$\lambda_{ijt} = \exp(\alpha_{ij} + \gamma D_{ijt} + \beta_1 \ln(Y_{it}) + \beta_2 \ln(Y_{jt})), \quad (4)$$

which is known as the exponential regression function. This regression follows naturally from the multiplicative form of (1) and ensures that λ_{ijt} is nonnegative, which is very convenient as trade cannot be negative. Thus, the conventional additive regression in (3) is likely to be unsatisfactory here as it cannot ensure the nonnegativity of trade.

The estimation of (4) has been studied by Hausman *et al.* (1984), who consider the special case when the data are measured in nonnegative integers. They propose using a version of the conventional poisson ML estimator, which is modified to account for the fixed effects. In so doing, the authors eliminate the fixed effects by conditioning on $\sum_{t=1}^T M_{ijt}$, a sufficient statistic for α_{ij} , which in our case yields the following log-likelihood function

$$\ln(L) = \sum_{i \neq j} \sum_{t=1}^T \Gamma(M_{ijt} + 1) - \sum_{i \neq j} \sum_{t=1}^T M_{ijt} \ln \left(\sum_{s=1}^T \frac{\lambda_{ijs}}{\lambda_{ijt}} \right),$$

where Γ is the gamma function. As noted by the authors, given that the regression in (4) is correctly specified, consistency of the resulting fixed effects poisson ML slope estimator follows directly by standard ML theory, see for example Gourieroux *et al.* (1984).² The Hausman *et al.* (1984) poisson conditional ML estimator is the same as the poisson ML estimator

²As long as (4) holds the poisson estimator works, see for example Wooldridge (2002) and Winkelmann (2008). In fact, neither (4) nor the maximization of the log-likelihood function require that the dependent variable is a count. It could be a binary variable or, as in our case, a nonnegative continuous variable. This property of the estimator has been used by Silva and Tenreyro (2006). The interpretation of the estimated coefficients is similar to the interpretation of the coefficients in the log-linear model. That is, the estimated coefficient reflects the elasticity of the dependent variable with respect to the relevant independent variable. In the case of an dummy variable, the estimated coefficient provides a reasonable approximation for small estimated values, see Winkelmann (2008) for a more elaborative discussion.

in a model with individual specific constants, which in turn is equivalent to the moment estimator in a model where the fixed effects are replaced by $\frac{1}{T} \sum_{t=1}^T M_{ijt} / \frac{1}{T} \sum_{t=1}^T \lambda_{ijt}$, the ratio of within group means. Alternative estimators of the fixed effects poisson model include the quasi-differenced generalized method of moments estimator and the pre-sample mean estimator that replaces the fixed effects by the pre-sample mean of the dependent variable, see for example Blundell *et al.* (2002) for a detailed discussion.³

Having estimated the slopes, an estimate of the fixed effects can be obtained by simply replacing λ_{ijt} in $\sum_{t=1}^T M_{ijt} / \sum_{t=1}^T \lambda_{ijt}$ by its ML estimate. Note that this gives an estimate of $\exp(\alpha_{ij})$, not of α_{ij} , which is unidentified in the fixed effects formulation of the model. In order to identify α_{ij} , a random effects assumption is needed. But such assumptions are generally not satisfied in practice, and so we only consider the fixed effects specification.

Although the poisson ML estimator is consistent, valid inference requires the correct specification of both the conditional mean and variance, which necessitates that

$$\lambda_{ijt} = \text{var}(M_{ijt} | Y_{it}, Y_{jt}, D_{ijt}). \quad (5)$$

However, note that the validity of (4) and (5) does not require the data to be poisson distributed. In fact, M_{ijt} does not have to be an integer at all. This suggests that we can use the fixed effects poisson ML to estimate the gravity model. Since this estimator does not require M_{ijt} to be nonzero, it is expected to produce better results than LS in panels where some trade flows are zero. Moreover, if it is consistency that we are interested in, then (5) does not have to hold either, so the data do not have to be equidispersed. In the next section, we elaborate on this point.

3 Monte Carlo study

In this section, we investigate the small-sample properties of the LS and ML estimators in the presence of zero observations through Monte Carlo simulations. The data generating process used for this purpose is given by

$$M_{ijt} = \exp(\alpha_{ij} + \gamma D_{ijt} + \beta Y_{ijt}) v_{ijt}, \quad (6)$$

³Another possibility is to use the zero inflated poisson (ZIP) model. But so far it seems that the estimation of this model with fixed effects has not yet been analyzed in the literature. In fact, Winkelmann (2008) points out that the properties of the fixed effects poisson ML estimator does not carry over to the ZIP model, and that the estimation of this model is still an open issue.

where $\alpha_{ij} = \gamma = \beta = 1$ for simplicity. Since Y_{ijt} is usually positive in applied work, we set $Y_{ijt} \sim U(0, 1)$. Moreover, if we let $\tau_{ij} \sim U(0, 1)$ denote the location of the break, then the dummy variable D_{ijt} , representing for example a preferential trade agreement, is such that $D_{ijt} = 1$ if $t > \tau_{ij}T$ and zero otherwise.

The disturbance v_{ijt} is key in this data generating process. In particular, it is assumed that v_{ijt} is a log-normally distributed variable with mean one and variance σ_{ij}^2 . We have two variance cases. In the case 1, $\sigma_{ij}^2 = 1$, which implies that

$$\text{var}(M_{ijt}|Y_{ijt}, D_{ijt}) = \exp(\alpha_{ij} + \gamma D_{ijt} + \beta Y_{ijt})^2,$$

while in case 2, $\sigma_{ij}^2 = 1/\exp(\alpha_{ij} + \gamma D_{ijt} + \beta Y_{ijt})$ so that

$$\text{var}(M_{ijt}|Y_{ijt}, D_{ijt}) = \exp(\alpha_{ij} + \gamma D_{ijt} + \beta Y_{ijt}).$$

Thus, we expect the LS estimator to perform relatively well in case 1, while we expect the poisson ML estimator to perform relatively well in case 2, as condition (5) is now satisfied.⁴ In both cases, we generate data by drawing 1,000 panels, each consisting of N observations on each of the T time series.

The results are organized according to the two cases described above. In each case, we want to examine the effect of zero observations in the data. Both the LS and poisson ML estimators are considered.⁵ The former is implemented using both truncated data and $\ln(M_{ijt} + 1)$ as dependent variable. However, note that since $M_{ijt} > 0$ in this data generating process, the log-linear model is no longer inadmissible. Hence, to be able to study the effect of truncating the sample we use a positive truncation threshold parameter, which is such that the fraction of truncated observations is exactly δ . For brevity, we only report the mean bias and the size of a nominal 5% level t -test of the null hypothesis that the parameter of interest is equal to its true value versus the alternative that it is not.⁶

Besides the LS and poisson ML estimators, we also experimented with the negative binomial ML estimator of Hausman *et al.* (1984), which relaxes condition (5). But since the

⁴Other values of σ_{ij}^2 produced very similar results and are thus not reported.

⁵The poisson ML estimator is implemented using the GAUSS optimization library OPTMUM. We use the BFGS gradient algorithm with numerical derivatives. The standard errors of the estimated parameters are computed based on the conventional Hessian method, which generally worked best in the simulations. The truncated LS is used to start up the estimation.

⁶We also simulated the power of the t -tests. However, since the size of the LS based tests turned out to be heavily distorted, with rejection frequencies close to 100% in most experiments, power is not very interesting, and the results are therefore not reported.

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7 performance was so unsatisfactory, the results are not included here but are available from the
8 corresponding author upon request. The panel version of the quasi-ML estimator discussed
9 in *Gourieroux et al.* (1984) also performed very poorly, and was therefore removed.⁷ Another
10 possibility is to treat the zeros as a sample selection issue, and to estimate the model using
11 an estimator that eliminates the selectivity bias. We tried the Kyriazidou (1997) estimator,
12 which is a popular two-step procedure to difference out both the bias and fixed effects. How-
13 ever, as with the negative binomial and quasi-ML estimators, the results from this estimator
14 were very poor, and were therefore removed.⁸

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20 The results reported in Table 1 for the LS and poisson ML estimators can be summarized
21 as follows. First, as expected, LS estimation with $\ln(M_{ijt} + 1)$ as the dependent variable
22 generally produces very poor results. In particular, it is seen that the estimators of γ and β
23 both suffer from substantial downwards bias, which do not show any tendency to vanish as
24 the sample size increases. Moreover, the results of the size of the t -tests suggest that inference
25 based on this estimation method is likely to be highly deceptive. In fact, with this method,
26 we always end up rejecting the null hypothesis. Thus, based on these results, we recommend
27 not using LS estimation based on $\ln(M_{ijt} + 1)$.

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34 Second, the results on the truncated LS estimator are mixed. At one end of the scale, we
35 have case 1 when there is no truncation, in which the performance, both in terms of bias and
36 size accuracy, is very good. At the other end, we have the case when $\delta > 0$, in which Table
37 1 shows that the performance is poor, and that the problems with bias and size distortion
38 are highly potent, even for a truncation as small as 10%. Apparently, the truncation makes
39 the LS estimator both downwards biased and unfit for inference. Thus, from an empirical
40 point of view, it seems highly unlikely that the truncated LS is able to deliver any meaningful
41 results at all.

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47 In addition to the problems associated with truncating the data, Table 1 points to another
48 important shortcoming with the truncated LS estimator. In particular, it seems as that the
49 heteroskedasticity in case 2 induces both severe size distortions as well as a sizeable bias that
50 persists even in large panels.

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54 ⁷The quasi-ML estimator only requires that the conditional mean in (4) is correctly specified, and does not
55 make use of (5), see for example *Gourieroux et al.* (1984) and *Wooldridge* (2002).

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60 ⁸We used the $T = 2$ version of the Kyriazidou (1997) estimator, which is relatively easy to compute, but
preliminary results suggest that the poor performance extends also to the case when $T > 2$. Also, for this
experiment, the data generating process was adapted so as to fit the sample selection setting of Kyriazidou
(1997).

Although this may appear somewhat counterintuitive at first, as pointed out by Silva and Tenreyro (2006), it is actually a direct consequence of the well-known Jensen inequality. To appreciate this, consider the data generating process in (6) where $E(v_{ijt}|Y_{ijt}, D_{ijt}) = 1$. The LS estimator of the parameters in the log-linear model (3) are consistent only if $E(\ln(v_{ijt})|Y_{ijt}, D_{ijt}) = 0$. However, although $\ln(E(v_{ijt}|Y_{ijt}, D_{ijt})) = 0$, by the Jensen equality, $E(\ln(v_{ijt})|Y_{ijt}, D_{ijt}) \neq 0$. Indeed, since $E(v_{ijt}|Y_{ijt}, D_{ijt})^2 = 1$ in our case, by using the properties of the log-normal distribution, we have that

$$E(\ln(v_{ijt})|Y_{ijt}, D_{ijt}) = \ln\left(\frac{1}{1 + \sigma_{ij}^2}\right),$$

which is not equal to zero unless of course σ_{ij}^2 is zero too. As a result, the LS estimator in (3) will generally be biased.

Third, except possibly for case 1 when there is no truncation, the results show that the poisson ML consistently outperforms the other estimators in terms of bias. In fact, by looking at Table 1, it would appear as that the bias is practically nonexistent even for as small panels as $T = 10$ and $N = 500$, which correspond approximately to 10 time series observations for 23 countries. We also see that the size is very close to the nominal 5% level in case 2 but that it is distorted in case 1, which is partly expected since condition (5) is not satisfied in this case.

One possibility to get rid of the distorted standard errors of the ML estimator is to use the bootstrap. This approach has become very popular in applied work, and it will therefore be used in this paper. The particular algorithm used is taken from Cameron and Trivedi (1998), who make a very simple proposal, in which the dependent and independent variables are resampled in pairs.⁹ Some simulations of the resulting bootstrapped t -statistic based on 100 bootstrap replications are reported in Table 2. As expected, we see that the size of the bootstrapped test generally lies much closer to the 5% level than the size of the asymptotic test. Also, the t -statistics appear to be well centered around zero.

In summary, we find that the poisson ML show smaller bias than the two LS estimators considered and, at the same time, maintain relatively good size properties in small samples. Since the poisson ML with bootstrapped standard errors is now readily available through existing software packages such as STATA, it should be considered a feasible alternative to estimation by LS.

⁹Another possibility is to use the wild bootstrap, see Cameron and Trivedi (1998) for a discussion.

4 An application to the 1995 EU enlargement

We have shown that log-linear LS estimation of the gravity model yields biased results. In this section, we demonstrate these findings by estimating the trade effects of the accession of Austria, Finland and Sweden to the EU in 1995. The sample that we use for this purpose covers the period 1992 to 2002 and consists of import data for EU and other developed countries from all trade partners except oil exporting countries and formerly planned economies in Central and Eastern Europe, as defined in Direction of Trade Statistics (International Monetary Fund, 2005). The GDP and population data comes from World Development Indicators (World Bank, 2005).

The estimated gravity equation can be written as

$$M_{ijt} = \exp(\alpha_{ij} + \mu_t + \gamma_1 D_{it} + \gamma_2 D_{jt} + \gamma_3 D_{ijt}) Y_{it}^{\beta_1} Y_{jt}^{\beta_2} N_{it}^{\beta_3} N_{jt}^{\beta_4} v_{ijt}, \quad (7)$$

or equivalently in its log-linear form

$$\begin{aligned} \ln(M_{ijt}) &= \alpha_{ij} + \mu_t + \gamma_1 D_{it} + \gamma_2 D_{jt} + \gamma_3 D_{ijt} + \beta_1 \ln(Y_{it}) + \beta_2 \ln(Y_{jt}) \\ &+ \beta_3 \ln(N_{it}) + \beta_4 \ln(N_{jt}) + \ln(v_{ijt}), \end{aligned} \quad (8)$$

where M_{ijt} denotes the nominal imports of country i from country j , Y_{it} and Y_{jt} denote the real GDP of the two countries, and N_{it} and N_{jt} denote their population. The fixed effects α_{ij} capture all types of unobserved country-pair specific heterogeneity that is constant over time, while the time effects μ_t capture all forms of time-varying heterogeneity that is shared among the country pairs.

The dummy variables D_{it} , D_{jt} and D_{ijt} are key in this model. The variable D_{it} equals one if country i is a member of the EU at time t while country j belongs to the rest of the world. The second dummy variable D_{jt} equals one if country j is a member of the EU while i belongs to the rest of the world. Similarly, D_{ijt} equals one if both i and j are members of the EU at time t . In other words, the three dummy variables take the value one for EU imports from the rest of the world, EU exports to the rest of the world and intra-EU trade, respectively.

The rest of the world is defined as all countries in the sample that are not members of the EU at any given time in the sample. This enables us to identify the effect of the enlargement on the trade of new EU members as opposed to the effect of changes in the size of the rest of the world. To appreciate this, note that if the rest of the world also included new members,

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7 the dummy variable D_{it} would capture not only the import effect on the new members but
8 also the effect of the change in the composition of the rest of the world, as the imports from
9 the new members to the old ones would no longer be classified as imports from the rest of
10 the world. A similar argument applies to the construction of D_{jt} .

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13 A consequence of this definition of the rest of the world is that, since fixed effects absorb
14 all heterogeneity that is constant over time, the trade effect for countries that have been
15 members of the EU for the whole sample period cannot be identified. Thus, the dummy
16 variables capture only the effect on countries that have changed their EU status at least one
17 time. That is, the dummy variables capture the effect of the Austrian, Finnish and Swedish
18 accession to the EU. Specifically, γ_1 measures the trade diversion or changes in EU imports
19 from the rest of the world. Similarly, γ_2 measures the effect on EU exports to the rest of the
20 world, sometimes called export diversion. Finally, γ_3 measures trade creation, resulting from
21 the increased intra-EU trade following the enlargement.

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Economic integration should increase trade between countries integrating. Thus, we expect the trade creation, as measured by γ_3 , to be positive. This effect can be separated into pure trade creation, or increased trade due to lower prices on imports from the other countries in the EU, and trade diversion, which implies a shift in imports from more efficient producers in the rest of the world to less efficient producers within the EU. A negative sign on γ_1 would thus indicate trade diversion. Similarly, export diversion occurs if exports to the rest of the world decreases as a result of the integration process, but exports could also increase. The expected sign of γ_2 is therefore ambiguous.

The empirical results are contained in Table 3. It is seen that the enlargement of the EU induced significant trade diversion but no trade creation. This absence of trade creation is, however, not surprising since the new members were part of a free trade area with the EU prior to the membership. When joining the EU, the new members implemented the Common External Tariff, which changed the tariffs on their imports from the rest of the world. Note that the trade diversion effect is rather large in comparison to the trade creation effect. Although counterintuitive at first, one should keep in mind that several countries with preferential access to the EU market, such as those that joined the EU in 2004, have been excluded from our sample, so trade might have been diverted away from suppliers on the world market to suppliers with preferential access to the EU market. Moreover, taken as a fraction of total trade, the diversion effect is probably quite small since the estimation results

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7 only capture the effect on imports to Austria, Sweden and Finland and not changes in the
8 total imports of the EU.
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10 Even though the number of zeros is comparatively small in our sample, only 10%, when
11 comparing the results obtained from the various estimators, we see that the difference can be
12 substantial. In particular, for the GDP and population variables, the poisson ML estimates
13 are typically larger than their LS counterparts. This finding is well in line with the Monte
14 Carlo evidence suggesting that both LS estimators are downwards biased. Moreover, while
15 the truncated LS estimator indicates that changes in GDP of importing countries does not
16 effect imports, the ML estimator gives a more plausible estimate close to unity.
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19 It should also be mentioned that the LS estimates of the GDP and population parameters
20 appear to be rather unstable, and to a large extent dependent on the time period used, which
21 is probably due to the fact that these variables seem to be quite highly correlated. On the
22 other hand, the corresponding LS estimates of the effects of trade liberalization appear to be
23 very robust, and show almost no variation between time periods. Similarly, all ML estimates
24 seem vary robust to changes in the time period.
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27 For the dummy variables, the differences are less marked. In particular, although the sign
28 and significance of the estimates do not differ much, the magnitude of the estimates varies
29 quite substantially. The LS estimator indicates that the trade diversion is twice as large as
30 implied by the ML estimator and, while the LS estimate of the trade creation effect is slightly
31 negative, it is positive for the ML estimator.
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34 In summary, the results presented in this section highlight the importance of using appro-
35 priate estimation techniques to be able to draw correct inference.
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38 5 Conclusions

39 The gravity model has become a standard tool for evaluating policies affecting trade and it
40 is widely used to assess the effects of preferential trade agreements and currency unions or to
41 calculate trade potential, among other things. It is well known that the gravity model should
42 be estimated by panel data to mitigate the bias due to failure to fully control for country
43 heterogeneity. A very popular way to accomplish this is to first linearize the model by taking
44 logarithms and then to apply the conventional fixed effects LS estimator.
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47 In this paper, we argue that this approach is likely to be very misleading with severely
48 biased estimates and t -statistics. There are two reasons for this. Firstly, since trade cannot
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7 be zero in the log-linearized model, all zeros must either be discarded or replaced by some
8 arbitrary positive value, which induces a sample selection bias. Secondly, the heteroskedas-
9 ticity inherent in the log-linear formulation of the gravity model can render the LS estimates
10 both biased and inefficient. By contrast, being based on the gravity model in its original
11 non-linear form, the fixed effects poisson ML estimator does not suffer from these weaknesses
12 and is therefore expected to yield more accurate results.
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17 Our assertion is verified by means of Monte Carlo simulations and illustrated via an
18 application to the 1995 EU enlargement. The simulations show that the performance of the
19 log-linear approach is likely to be so poor that it may not even be meaningful to interpret
20 the results. On the other hand, the poisson ML estimator performs well with only a very
21 small bias and good size accuracy in most cases. Still, in some data generating processes, the
22 results show that the estimated standard errors can be downward biased. To alleviate this, we
23 suggest using bootstrapped standard errors. The empirical application points to a significant
24 difference between the estimators with respect to both the main explanatory variables and
25 the trade effects of the 1995 EU enlargement, thus underlining the importance of using the
26 proper estimation technique.
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34 To conclude, we recommend not estimating the gravity model from its log-linear form.
35 Instead, we propose estimating the model directly from its non-linear form using the fixed
36 effects poisson ML estimator with bootstrapped standard error. Our proposal provide re-
37 searchers with a simple framework for analyzing the gravity model while at the same time
38 avoiding potential bias due to zero trade. This, together with the fact that the poisson ML
39 estimator can now be implemented using many standard statistical software packages such as
40 STATA, makes our proposal definitely seem worthwhile.
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Table 1: Simulated bias and tests size for the ML and LS estimators.

| δ | Case | N | T | Mean bias | | | | | | Size of the t -test at the 5% level | | | | | | |
|----------|------|------|------|-----------------------|----------------------|-----------------------|----------------------|---------------------|--------------------|---------------------------------------|----------------------|---------------------|--------------------|-------|------|------|
| | | | | $\hat{\gamma}_{ls}^a$ | $\hat{\beta}_{ls}^a$ | $\hat{\gamma}_{ls}^b$ | $\hat{\beta}_{ls}^b$ | $\hat{\gamma}_{ml}$ | $\hat{\beta}_{ml}$ | $\hat{\gamma}_{ls}^a$ | $\hat{\beta}_{ls}^a$ | $\hat{\gamma}_{ml}$ | $\hat{\beta}_{ml}$ | | | |
| 0 | 1 | 500 | 10 | 0.1 | -0.1 | -36.4 | -36.9 | 0.1 | -0.1 | 7.3 | 5.8 | 100.0 | 100.0 | 24.6 | 31.8 | |
| | | 1000 | 10 | 0.0 | 0.0 | -36.5 | -36.8 | -0.1 | -0.1 | 6.6 | 5.8 | 100.0 | 100.0 | 25.6 | 32.2 | |
| | 2 | 500 | 20 | 0.1 | 0.1 | -36.5 | -36.7 | 0.1 | 0.2 | 6.2 | 6.1 | 100.0 | 100.0 | 24.1 | 33.4 | |
| | | 1000 | 20 | -0.1 | 0.0 | -36.5 | -36.8 | -0.1 | -0.2 | 5.9 | 6.2 | 100.0 | 100.0 | 26.5 | 31.9 | |
| | 0.1 | 1 | 500 | 10 | 13.8 | 14.1 | -25.8 | -26.6 | -0.1 | 0.0 | 100.0 | 99.8 | 100.0 | 100.0 | 5.0 | 6.3 |
| | | | 1000 | 10 | 13.8 | 14.2 | -25.8 | -26.5 | 0.1 | 0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 3.7 | 4.4 |
| 0.3 | 1 | 500 | 10 | 13.8 | 14.1 | -25.8 | -26.6 | 0.0 | 0.0 | 100.0 | 100.0 | 100.0 | 100.0 | 6.1 | 4.8 | |
| | | 1000 | 20 | 13.9 | 14.2 | -25.8 | -26.6 | 0.1 | 0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 4.9 | 5.3 | |
| | 2 | 500 | 10 | -21.8 | -21.8 | -36.5 | -36.8 | -0.1 | -0.1 | 100.0 | 99.9 | 100.0 | 100.0 | 25.3 | 29.6 | |
| | | 1000 | 10 | -21.9 | -21.8 | -36.6 | -36.8 | -0.1 | -0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 23.9 | 29.5 | |
| | 0.1 | 2 | 500 | 20 | -21.9 | -21.9 | -36.6 | -36.8 | -0.1 | -0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 27.1 | 31.3 |
| | | | 1000 | 20 | -21.8 | -21.9 | -36.5 | -36.8 | 0.0 | 0.0 | 100.0 | 100.0 | 100.0 | 100.0 | 25.3 | 32.2 |
| 0.3 | 1 | 500 | 10 | -9.4 | -13.4 | -25.7 | -26.6 | 0.1 | -0.1 | 99.8 | 99.8 | 100.0 | 100.0 | 4.7 | 4.9 | |
| | | 1000 | 10 | -9.5 | -13.5 | -25.8 | -26.6 | 0.0 | -0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 5.5 | 4.9 | |
| | 2 | 500 | 20 | -9.4 | -13.4 | -25.8 | -26.6 | 0.0 | -0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 5.6 | 4.5 | |
| | | 1000 | 20 | -9.5 | -13.3 | -25.8 | -26.5 | 0.0 | 0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 5.7 | 5.7 | |
| | 0.3 | 1 | 500 | 10 | -44.8 | -40.9 | -36.5 | -36.8 | -0.1 | -0.2 | 100.0 | 100.0 | 100.0 | 100.0 | 27.2 | 29.5 |
| | | | 1000 | 10 | -44.7 | -41.0 | -36.5 | -36.8 | 0.0 | -0.2 | 100.0 | 100.0 | 100.0 | 100.0 | 26.6 | 34.3 |
| 2 | 1 | 500 | 20 | -44.6 | -40.9 | -36.5 | -36.8 | 0.1 | 0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 28.8 | 33.2 | |
| | | 1000 | 20 | -44.8 | -41.0 | -36.6 | -36.8 | -0.1 | -0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 26.7 | 32.9 | |
| 0.3 | 2 | 500 | 10 | -41.4 | -29.0 | -25.9 | -26.6 | -0.1 | -0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 4.0 | 5.1 | |
| | | 1000 | 10 | -41.4 | -28.9 | -25.8 | -26.6 | 0.0 | 0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 6.1 | 3.9 | |
| 0.3 | 2 | 500 | 20 | -41.4 | -29.2 | -25.8 | -26.7 | 0.0 | -0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 5.3 | 5.5 | |
| | | 1000 | 20 | -41.4 | -29.1 | -25.8 | -26.6 | 0.0 | 0.1 | 100.0 | 100.0 | 100.0 | 100.0 | 5.0 | 5.2 | |

Notes: The value δ refers to the fraction of truncated observations, $\hat{\gamma}_{ls}$ and $\hat{\beta}_{ls}$ refer to the LS estimates, and $\hat{\gamma}_{ml}$ and $\hat{\beta}_{ml}$ refer to the poisson ML estimates. Case 1 refers to the data generating process with $\sigma_{ij}^2 = 1$, while case 2 refers to the data generating process with $\text{var}(M_{ijt}|Y_{ijt}, D_{ijt}) = E(M_{ijt}|Y_{ijt}, D_{ijt})$. The reported bias results refer to the mean bias times 100.

^aThe LS estimator is based on truncating the sample.

^bThe LS estimator uses $\ln(M_{ijt} + 1)$ as the dependent variable

Table 2: Simulation results for the bootstrapped ML t -test.

| N | T | Case 1 | | | | Case 2 | | | |
|----------------------|-----|------------------------|-----------------------|--------------------------|-------------------------|------------------------|-----------------------|--------------------------|-------------------------|
| | | $t(\hat{\gamma}_{ml})$ | $t(\hat{\beta}_{ml})$ | $t^*(\hat{\gamma}_{ml})$ | $t^*(\hat{\beta}_{ml})$ | $t(\hat{\gamma}_{ml})$ | $t(\hat{\beta}_{ml})$ | $t^*(\hat{\gamma}_{ml})$ | $t^*(\hat{\beta}_{ml})$ |
| Size at the 5% level | | | | | | | | | |
| 500 | 10 | 23.8 | 33.4 | 9.2 | 10.0 | 5.8 | 4.0 | 10.2 | 7.4 |
| 1000 | 10 | 25.2 | 31.4 | 10.4 | 9.6 | 4.6 | 5.8 | 10.0 | 7.2 |
| 500 | 20 | 28.4 | 33.2 | 7.6 | 9.6 | 5.0 | 6.6 | 7.8 | 10.0 |
| 1000 | 20 | 26.4 | 39.4 | 8.4 | 10.6 | 6.4 | 4.8 | 8.2 | 6.6 |
| Mean | | | | | | | | | |
| 500 | 10 | 0.0 | -0.1 | 0.0 | -0.1 | 0.1 | 0.0 | 0.1 | 0.1 |
| 1000 | 10 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 500 | 20 | 0.0 | -0.1 | 0.0 | 0.0 | 0.1 | 0.0 | 0.1 | 0.0 |
| 1000 | 20 | 0.1 | 0.0 | 0.1 | 0.0 | 0.0 | -0.1 | 0.0 | -0.1 |
| Standard deviation | | | | | | | | | |
| 500 | 10 | 1.7 | 2.1 | 1.2 | 1.2 | 1.0 | 1.0 | 1.2 | 1.1 |
| 1000 | 10 | 1.8 | 1.9 | 1.2 | 1.2 | 1.0 | 1.0 | 1.2 | 1.1 |
| 500 | 20 | 1.8 | 2.1 | 1.1 | 1.2 | 1.0 | 1.1 | 1.1 | 1.1 |
| 1000 | 20 | 1.8 | 2.2 | 1.1 | 1.2 | 1.0 | 1.0 | 1.1 | 1.1 |

Notes: The values $t(\hat{\gamma}_{ml})$ and $t(\hat{\beta}_{ml})$ refer to the conventional asymptotic ML t -tests, while $t^*(\hat{\gamma}_{ml})$ and $t^*(\hat{\beta}_{ml})$ refer to their bootstrapped counterparts. See Table 1 for an explanation of the remaining features of the table.

Table 3: Empirical estimation results.

| Estimator | LS | LS | poisson ML |
|----------------------|----------------------|----------------------|----------------------|
| Dependent variable | $\ln(M_{ijt})$ | $\ln(M_{ijt} + 1)$ | M_{ijt} |
| β_1 | -0.091 (0.191) | 0.229*** (0.062) | 0.931*** (0.173) |
| β_2 | 1.438*** (0.084) | 0.820*** (0.039) | 1.483*** (0.110) |
| β_3 | 4.055*** (0.612) | 1.765*** (0.267) | 2.471*** (0.629) |
| β_4 | -1.275*** (0.190) | -0.979*** (0.074) | -0.580 (0.357) |
| γ_1 | -0.403*** (0.046) | -0.211*** (0.016) | -0.232*** (0.074) |
| γ_2 | 0.000 (0.032) | 0.102*** (0.023) | 0.041 (0.047) |
| γ_3 | -0.002 (0.025) | 0.033* (0.018) | 0.035 (0.034) |
| No. of country-pairs | 2719 | 2748 | 2719 |
| No. of observations | 32487 | 35600 | 35256 |

Notes: The numbers within the parantheses are the robust LS standard errors or the bootstrapped poisson ML standard errors. The superscripts (**), (*) and (*) denote significance at the 1%, 5% and 10% levels, respectively.

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