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Group velocity coupling and synchronization-like phenomenon of two light beams based on coherent population oscillations

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Abstract. We report on the control of the slow and fast light propagation velocity of two light beams (at 1550 nm and 980 nm) through an erbium doped fiber amplifier by means of coherent population oscillations. We modulate the amplitude of both beams with the same frequency so that the relative phase between both modulations allows us to control their group velocities. The same group velocity, in absolute value, is achieved when beams are modulated in phase or phase opposition. The experimental results are explained by a rate equation model.

1. Introduction

Slow light has recently become a subject of intense research due to its potential applications for tunable delay lines which can be used for data synchronization [1]. Thus, much research has been focused on the control of the speed of light in optical fibers since these devices would be compatible with fiber-optic communication systems (see review about slow light in optical fibers [2]). Song et al. [3] and Okawachi et al. [4] demonstrated slow and fast light in optical fibers for the first time. The underlying mechanism used on those works, stimulated Brillouin scattering, consists in the interaction of two propagating waves, a pump wave and a Stokes wave, which generates an acoustic wave at the frequency difference of the pump and the Stokes fields. The slow light resonance can be placed at the desired wavelength by changing the frequency of the pump field. A related process, stimulated Raman scattering, has also been used in optical fibers to demonstrate an ultrafast all-optical controllable delay [5]. Electromagnetically induced transparency (EIT), a pioneering technique to produce slow light propagation, has been recently demonstrated experimentally in hollow-core photonic-bandgap fibers filled with acetylene [6]. This technique creates a very deep transparency window in an atomic absorption profile with almost null absorption. However, EIT medium should preserve quantum coherence, therefore dephasing processes limit this technique.

Coherent population oscillations (CPO) have been shown to be another physical mechanism which allows for the variation of group velocity in optical fibers at room temperature. The periodic modulation of the ground-state population at the beat frequency between a control and a probe field sharing a common atomic transition produces scattered light from the control field into the probe field leading to a decrease in the absorption of the probe field. This give rise to a narrow hole in the absorption profile for the probe field leading to slow light propagation [7]. The hole linewidth is proportional to the inverse of the relaxation lifetime of the excited level [8]. Note that this technique is not affected by dephasing processes, in contrast to EIT. However, the transparency depth achieved in CPO is smaller than the one obtained with EIT. Therefore, CPO could be affected by the residual absorption. By means of an additional pump to populate upper levels, the CPO induces a dip in the gain spectrum, leading to anomalous dispersion and fast light (group velocities greater than c or even negative). A modification of group velocity by CPO in an erbium doped fiber (EDF) was reported for the first time by Schweinsberg et al [9], where an amplitude-modulated 1550 nm signal co-propagates with a 980 nm pump beam. They observed a change from sub- to superluminal propagation upon increasing pump power. The delay or advancement achieved saturates with both pump and signal powers, being this a limit in the delays and advancements obtained. Larger delays/advancements have been obtained for ultra-highly EDFs [10, 11, 12]. By using the same experimental system, fast light pulse propagation has been studied in more detail in [13, 14, 15]. Furthermore, a change from superluminal to subluminal propagation solely based upon increasing the beat frequency between the weak and the control field sharing a common atomic transition has been reported [16, 17]. This peculiar behavior is due to the interplay between pump absorption and pump-power broadening of the spectral hole induced by CPO.

Recently, Arrieta-Yáñez *et al* have developed a novel mechanism for enhancing the fractional delay and advancement obtained in EDFs by one order of magnitude [18]. They force the population oscillations by modulating with the same frequency

and simultaneously both, the 980 nm pump beam and the 1550 nm signal beam. The population oscillations are amplified by the pump modulation. Relative phase between both modulations was used as a knob for changing the propagation regime from ultraslow velocities to fast- or negative-velocities. The same physical mechanism was previously used by Stepanov *et al* [19] to control the phase shift of a modulated signal beam by modulating an additional beam simultaneously and with the same frequency. These two beams have different carrier frequencies, both within the fundamental absorption spectrum 1470-1570 nm of Er^{3+} ions.

Our aim in this work is to study the coupling of two light beams through the population oscillations and its effect in the propagation velocity of both beams. To this end, we induce a beat in both beams with the same frequency and analyze simultaneously the group velocity of both modulated beams. We use an EDF and the two light beams correspond to the usual signal (at 1550 nm) and pump (at 980 nm) beams. This method allows us to control the group velocity of both beams by means of the relative phase between both beats. We analyze under which conditions the coupling between the two beams makes that both propagate with the same group velocity, that is, the conditions that lead to a group velocity synchronization-like phenomenon.

The paper is organized as follows. The theoretical model used to study the propagation of two amplitude periodically-modulated beams through an EDF using CPO is described in section 2. The experimental setup is described in section 3. The experimental results and simulations are presented in section 4. The final conclusions are summarized in section 5.

2. Propagation equations

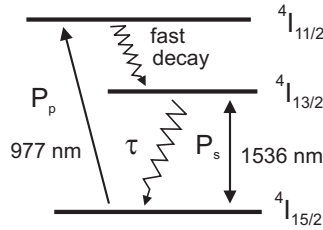


Figure 1. Three-level system for Er^{3+} ions. Wavelengths for the signal and pump beams.

The propagation of an amplitude periodically-modulated signal through an EDF has been modeled in previous works on CPO by using both semiclassical and rate equation procedures [7, 9]. We consider the erbium ions as three-level atomic systems interacting with a power-modulated 1536 nm signal which couples the transition ${}^4I_{15/2} \rightarrow {}^4I_{13/2}$ and a 977 nm pump laser which pump the ions onto the upper state ${}^4I_{11/2}$ (see figure 1). We also assume a fast decay from the upper state ${}^4I_{11/2}$ to the metastable state (${}^4I_{13/2}$). We obtain the rate equation for N_1 (the population of the ground state normalized to the total ion density ρ):

$$\frac{\partial N_1}{\partial t} = \frac{1}{\tau} \left[1 - N_1 + \frac{\beta_s}{1 + \beta_s} P_s (1 - N_1) - \frac{1}{1 + \beta_s} P_s N_1 - P_p N_1 \right], \quad (1)$$

where the four terms on the right hand side of the equation stand for the spontaneous emission from the metastable state, the stimulated emission from the metastable state, the absorption to the metastable state, and the absorption to the upper level, respectively. Here t is the time variable. P_s is the signal power normalized to the signal saturation power $P_s^{sat} \equiv \hbar\omega_s A_s / (\tau(\sigma_{21} + \sigma_{12}))$, where τ is the lifetime of the metastable state, σ_{21} is the emission cross section at the signal frequency ω_s , σ_{12} is the absorption cross section at the signal frequency ω_s , and A_s is the signal mode area. The ratio between the signal cross sections is $\beta_s \equiv \sigma_{21}/\sigma_{12}$. P_p is the pump power normalized to the pump saturation power $P_p^{sat} \equiv \hbar\omega_p A_p / (\tau\sigma_{13})$, where σ_{13} is the absorption cross section at the pump frequency ω_p , and A_p is the pump mode area. $\eta_s \equiv A_c/A_s$ is the ratio between the fiber core area and the signal mode area, and $\eta_p \equiv A_c/A_p$ is the ratio between the fiber core area and the pump mode area.

The behavior of the signal and pump powers along the fiber can be described by the following propagation equations:

$$\frac{\partial P_s}{\partial z} + \frac{n_{gs}}{c} \frac{\partial P_s}{\partial t} = \sigma_{12}\rho [\beta_s - (1 + \beta_s)N_1] \eta_s P_s, \quad (2)$$

$$\frac{\partial P_p}{\partial z} + \frac{n_{gp}}{c} \frac{\partial P_p}{\partial t} = -\sigma_{13}\rho N_1 \eta_p P_p, \quad (3)$$

where z is the distance along the fiber. Here n_{gs} and n_{gp} are the group indexes of the signal and pump in the fiber glass, respectively.

The signal is modulated as follows: $P_s = P_{s0} + P_{sm} \cos(2\pi f_m t)$, where P_{s0} is the average signal power, P_{sm} is the modulation amplitude (modulation depth P_{sm}/P_{s0}), and f_m is the modulation frequency. Due to this modulation, a periodic coherent oscillation of the population of the ground state occurs at this frequency ($N_1 = N_{1st} + N_{1c} \cos(2\pi f_m t) + N_{1s} \sin(2\pi f_m t)$) which produces a hole in the absorption spectrum for the modulated part of the signal. Thus, a slow light propagation of P_{sm} takes place. The presence of the pump beam allows to turn the delay into advancement (fast light), depending on the value of the pump power. However, the magnitude of the advancement obtained remains nearly constant when certain pump level has been achieved [7, 9, 10, 16, 20].

Here, we also modulate the pump beam with the same frequency as the signal beam, being the pump power made up of an average pump power P_{p0} , and a sinusoidal part with amplitude P_{pm} varying at frequency f_m , i.e., $P_p = P_{p0} + P_{pm} \cos(2\pi f_m t - \varphi)$. Note that the pump beam could be out of phase with the signal beam by a magnitude φ . Thus, the stationary part (N_{1st}) and the oscillating parts (N_{1c} and N_{1s}) of the population of the ground state will be given by:

$$N_{1st} = \frac{1}{w_c} \left(1 + \frac{\beta_s}{1 + \beta_s} P_{s0} \right), \quad (4)$$

$$N_{1c} = \frac{w_c P_{sm}}{w_c^2 + w_m^2} \left(\frac{\beta_s}{1 + \beta_s} - N_{1st} \right) - \frac{N_{1st} P_{pm}}{w_c^2 + w_m^2} (w_c \cos \varphi - w_m \sin \varphi), \quad (5)$$

$$N_{1s} = \frac{w_m P_{sm}}{w_c^2 + w_m^2} \left(\frac{\beta_s}{1 + \beta_s} - N_{1st} \right) - \frac{N_{1st} P_{pm}}{w_c^2 + w_m^2} (w_m \cos \varphi + w_c \sin \varphi), \quad (6)$$

where $w_m \equiv 2\pi f_m \tau$ is the dimensionless modulation frequency and $w_c \equiv 1 + P_{s0} + P_{p0}$ is a dimensionless frequency which determines the width of the transparency hole created in the absorption or gain spectrum by means of CPO. This magnitude roughly

measures the maximum modulation bandwidth that can experience the full slow or fast light effect [21] and it can be increased with the signal and pump powers. The expression obtained for the out of phase part of the population oscillation N_{1s} presents two terms: the first one, which is proportional to P_{sm} , is responsible of the delay/advancement experienced by the modulated part of the signal. The second term, which is proportional to P_{pm} , arises from the modulation imposed to the pump beam and incorporates explicitly the phase delay φ . We will show that by adjusting the value of φ , the delay and advancement experienced by the modulated part of the signal can be controlled.

Finally, we can obtain the propagation equations for the average powers and the amplitudes of the modulation of the signal and pump beams, and for the phase shift experienced by the periodic part of the signal and pump beams due to CPO:

$$\frac{dP_{s0}}{dz'} = \alpha_s P_{s0} [\beta_s - (1 + \beta_s) N_{1st}] , \quad (7)$$

$$\frac{dP_{p0}}{dz'} = -\alpha_p P_{p0} N_{1st} , \quad (8)$$

$$\frac{dP_{sm}}{dz'} = -\alpha_s (1 + \beta_s) P_{s0} N_{1c} + \alpha_s [\beta_s - (1 + \beta_s) N_{1st}] P_{sm} , \quad (9)$$

$$\frac{dP_{pm}}{dz'} = -\alpha_p P_{p0} (N_{1c} \cos \varphi + N_{1s} \sin \varphi) - \alpha_p P_{pm} N_{1st} , \quad (10)$$

$$\frac{d\phi_s}{dz'} = \alpha_s (1 + \beta_s) \frac{P_{s0}}{P_{sm}} N_{1s} , \quad (11)$$

$$\frac{d\phi_p}{dz'} = \alpha_p \frac{P_{p0}}{P_{pm}} (N_{1s} \cos \varphi - N_{1c} \sin \varphi) , \quad (12)$$

where the distance has been normalized to the fiber length L such that $z' \equiv z/L$. $\alpha_s \equiv L\sigma_{12}\rho\eta_s$ is the dimensionless signal absorption coefficient and $\alpha_p \equiv L\sigma_{13}\rho\eta_p$ is the dimensionless pump absorption coefficient. We neglect the term with the temporal derivative in equations (2) and (3). This term leads to a small delay (delay due to the fiber glass refractive index dispersion) compared to the delay due to CPO. The fractional delay of the signal (time delay normalized to the time duration of the signal) at the end of the fiber can be obtained from the signal phase shift at $z = L$, i.e., $F_s \equiv \phi_s(z = L)/(2\pi)$. While for the pump it will be $F_p \equiv \phi_p(z = L)/(2\pi)$.

3. Experimental setup

The experimental setup is depicted in figure 2 and consists of an EDF in the forward-pumped configuration. The signal beam comes from a pigtailed distributed feedback laser diode operating at 1536 nm provided with a current and temperature controller which allows us to operate the laser at room temperature. This laser beam couples the transition between the erbium ground state $^4I_{15/2}$ and the metastable state $^4I_{13/2}$ (see figure 1). The signal beam is split into two beams: one part of the beam (1%) is sent directly to a switchable-gain amplified InGaAs photodetector, which is used as reference. The other part of the beam (99%) goes through the EDF under study and then to an identical photodetector. The EDF is pumped by a co-propagating beam coming from a pigtailed laser diode operating at 977 nm provided also with a current and temperature controller. This laser beam couples the erbium ground state with the fast decay upper pump level ($^4I_{11/2}$) (see figure 1). The pump beam is also split

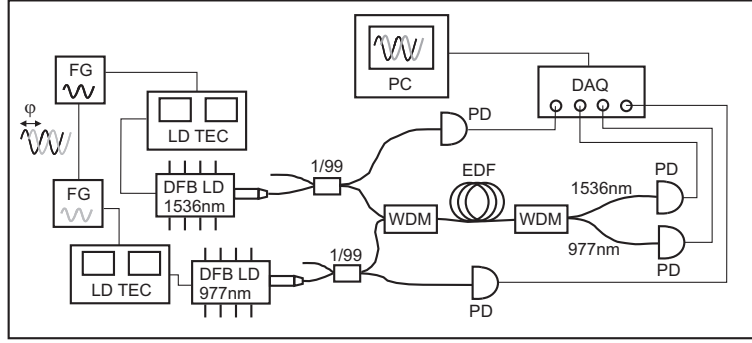


Figure 2. Experimental setup scheme. LD TEC: laser diode and temperature controller; FG: function generator; φ : relative phase between the pump modulation and the signal modulation; DFB LD: distributed feedback laser diode; WDM: wavelength division multiplexer; EDF: erbium doped fiber; PD: photodetector; DAQ: data acquisition card; PC: personal computer.

into two beams: one part of the beam (1%) is sent directly to a photodetector, which is used as reference. The other part of the beam (99%) goes through the EDF and then to an identical photodetector. The signal and pump beams are injected into the EDF through a wavelength division multiplexer. The pump and the signal beams at the output of the EDF are separated by means of an identical wavelength division multiplexer. Both laser powers are sinusoidally modulated with the same modulation frequency f_m by using two synchronized function generators which allow us to control the relative phase φ between both laser powers at the input of the fiber. Four signals (the reference signal, the signal propagated through the EDF, the reference pump, and the pump propagated through the EDF) are recorded with a fast data acquisition card and transferred to a computer for analysis. The experiment is controlled with a LabView program. We compute the time delay or advancement of the signal t_{ds} from the correlation of the reference signal and the signal propagated through the EDF. Similarly, we compute the time delay or advancement of the pump t_{dp} from the correlation of the reference pump and the pump propagated through the EDF. Then, the fractional delay/advancement of the signal is defined as $F_s \equiv t_{ds}f_m$, while the fractional delay/advancement of the pump is defined as $F_p \equiv t_{dp}f_m$. We used a 0.1 m-long single mode Al_2SiO_5 -glass-based fiber highly doped with Er^{3+} ions (ion density $\rho = 6.3 \times 10^{25} \text{ m}^{-3}$).

4. Experimental results and simulations

We have carried out two different set of experiments. In the first one, we analyze the enhancement of the slow and fast light propagation effects produced when forcing the population oscillations with a modulated pump. In the second one, we study the coupling of both modulated beams.

In order to theoretically reproduce the experimental results, we numerically solve the propagation equations (7)-(12). We have considered the following parameter values which are consistent with values previously used in other works [9, 22]: the signal cross section is $\sigma_{12} = \sigma_{21} = 5 \times 10^{-25} \text{ m}^2$, the pump cross section is $\sigma_{13} = 3 \times 10^{-25} \text{ m}^2$, the signal mode area is $A_s \simeq 33 \mu\text{m}^2$ (signal mode field diameter $6.5 \mu\text{m}$), the pump mode

area is $A_p \simeq 20 \mu\text{m}^2$ (pump mode field diameter $5.0 \mu\text{m}$), the fiber core area is $A_c \simeq 14 \mu\text{m}^2$ (fiber core diameter $4.2 \mu\text{m}$), the lifetime of the metastable state is $\tau \simeq 9$ ms. Using these parameters, the signal saturation power is $P_s^{sat} \simeq 0.5$ mW and the pump saturation power is $P_p^{sat} \simeq 1.5$ mW. The dimensionless signal absorption coefficient is $\alpha_s \simeq 1.35$, and the dimensionless pump absorption coefficient is $\alpha_p \simeq 1.33$. We used the insertion losses in the EDF as fitting parameters to reproduce the experimental curves. Thus, we considered an insertion losses of 0.8 for the signal beam and 0.65 for the pump beam. We are not considering changes in the refractive index due to nonlinear effects such as Kerr type nonlinearity since we are not working in a high power regimen.

4.1. Signal delay controlled by the modulated pump

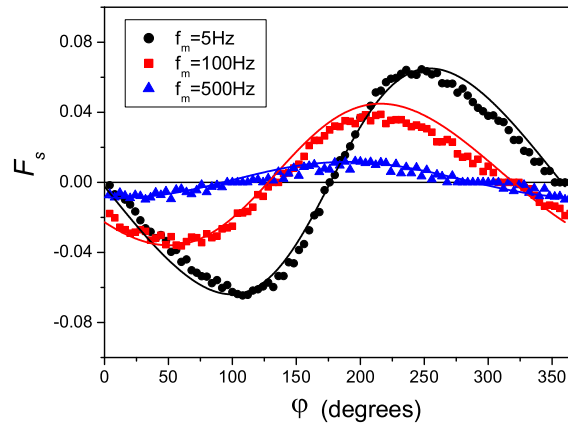


Figure 3. Fractional advancement of the signal as a function of the relative phase between the signal and pump modulated beams for three different modulation frequencies. Experiments (symbols) and simulations (lines). Signal power = 0.14 mW ($P_{s0} = 0.24$). Pump power = 10 mW ($P_{p0} = 4.3$). Modulation depths $P_{sm}/P_{s0} = P_{pm}/P_{p0} \simeq 0.5$.

First of all, we have analyzed the viability of controlling the propagation regime of the signal by means of the pump modulation. In figure 3 we show the dependence of the signal fractional delay F_s with the relative phase between the signal and pump modulated beams φ . We modulate the signal power (0.14 mW) and the pump power (10 mW) with the same modulation depth ($P_{sm}/P_{s0} = P_{pm}/P_{p0} \simeq 0.5$) and frequency. Different curves correspond to different modulation frequencies. The experimental results (symbols) have been plotted together with the simulated curves (lines) obtained by numerically solving the system of equations (7)-(12). We obtain ultra slow group velocities or very fast group velocities (even negatives) depending on the relative phase φ . It can be seen that the value of φ that leads to the maximum fractional delay or advancement shifts with the modulation frequency. For low frequencies, the maximum delay takes place around $\pi/2$ while the maximum advancement takes place around $3\pi/2$. As the modulation frequency increases, the position of the maximum delay shifts and tends to 0 while the position of the maximum advancement tends

to π . This behavior can be analytically explained by neglecting the attenuation or amplification of the signal and pump powers (undepleted solution) in equation (11). In this case, the phase shift of the signal is obtained by assuming implicitly the absence of z -dependence in the problem:

$$\phi_s(z = L) \simeq \frac{\alpha_s P_{s0}}{(w_c^2 + w_m^2) w_c} \left[w_m (\beta_s P_{p0} - 1) - \frac{P_{pm}}{P_{sm}} (1 + \beta_s + \beta_s P_{s0}) \sin[\varphi + \xi_m] \right], \quad (13)$$

where $\xi_m \equiv \arctan(w_m/w_c)$. By analyzing equation (13) we obtain that the maximum fractional advancement/delay takes place at $\varphi = (\pi/2) + n\pi - \xi_m$ (with $n = 0, 1$). Then, at low modulation frequencies ($w_m < w_c$), $\xi_m \simeq 0$, so the minimum and the maximum take place around $\pi/2$ and $3\pi/2$, respectively; whereas at high modulation frequencies ($w_m > w_c$), $\xi_m \simeq \pi/2$, so the minimum and the maximum take place around 0 and π , respectively, in agreement with the experimental results.

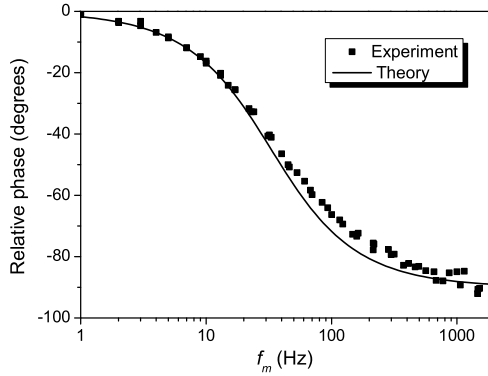


Figure 4. Phase between the signal and the pump beams as a function of the modulation frequency. Experiment (symbols) and theory (line). Signal power = 0.1 mW ($P_{s0} = 0.17$). Pump power = 1.5 mW ($P_{p0} = 0.66$). Pump modulation depth $P_{pm}/P_{p0} = 0.5$.

With the aim of better understanding the above results, we are going to take into account that the pump beam dominates the population oscillation since the pump power is much higher than the signal power, so its modulation amplitude is higher too. Thus, when only the pump beam is modulated, an oscillation will be induced in the signal beam due to the population oscillations. It is easy to analytically show that, in this particular case, the signal beam will oscillate with a phase shift of ξ_m with respect to the pump beam. In fact, this phase shift is the phase difference of the population oscillations with respect to the oscillation of the pump beam. In other words, the signal beam will oscillate in phase with the population oscillations which are induced by the modulated pump. In order to experimentally check this result, we have measured the phase shift between the signal and the pump beams when modulating a 1.5 mW pump beam with a constant signal beam of 0.1 mW. In figure 4 we plot the relative phase between the signal and pump beams as a function of the modulation frequency. We observe that for low modulation frequencies, the signal oscillates in phase with the pump beam, and for high modulation frequencies, the shift between

the pump beam and the signal beam is $\pi/2$. As expected, the relative phase between the signal and pump beams behaves as ξ_m , as can be seen in figure 4 (solid line).

So the oscillation that the pump induces in the signal has a phase shift of ξ_m with respect to the pump oscillation. When we modulate both beams simultaneously, as in figure 3, the signal oscillation will not affect to the population oscillations since the signal power and, thus, the signal modulation amplitude are smaller than the corresponding to the pump. Then, at low modulation frequencies ($\xi_m \simeq 0$), i.e., when the oscillations of the pump and the population are in phase, the maximum delay/advancement takes place when signal and pump are initially out of phase. However, at high modulation frequencies ($\xi_m \simeq \pi/2$), i.e., when the oscillations of the pump and the population are dephased by $\pi/2$, the signal will have a maximum delay or advancement when the signal oscillations are initially in phase with the pump oscillations. Thus, the maximum fractional delay (or advancement) occurs when the phase difference between the population and the signal beam is $\pi/2$ (or $3\pi/2$) for all modulation frequencies, i.e., $\varphi + \xi_m = \pi/2$ (or $3\pi/2$).

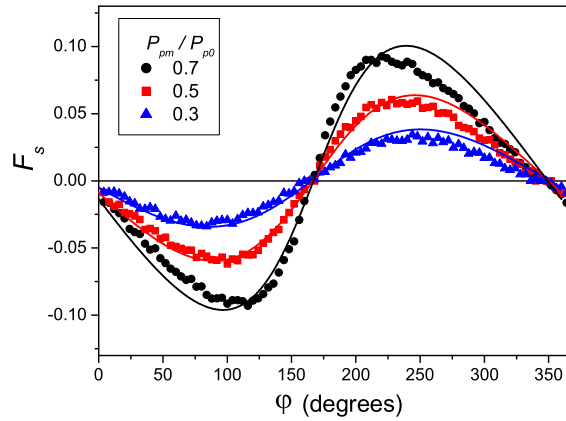


Figure 5. Fractional advancement of the signal as a function of the relative phase between the signal and pump modulated beams for three different pump modulation depths. Experiments (symbols) and simulations (lines). $f_m = 20$ Hz. The rest of parameters are the same than the ones used in figure 3.

We have also analyzed the behavior of F_s with the amplitude of the pump modulation P_{pm} . Figure 5 shows the experimental (symbols) and the simulated (lines) fractional advancement of the signal F_s versus φ when we modulate the pump and the signal powers at a low modulation frequency of $f_m = 20$ Hz. The simulated curves have been obtained by numerically solving the system of equations (7)-(12). Different curves correspond to different modulation depths of the pump beam. The rest of parameters are the same than the ones used in figure 3. We see how the maximum advancement and maximum delay increase linearly with the modulation amplitude, in agreement with the analytical expression (see equation (13)). Note that, for the largest pump modulation depth, the shape of the curve developed by $F_s(\varphi)$ slightly deviates from a sinusoidal profile (see circles in figure 5), i.e., from the prediction given by equation (13). This analytical expression was obtained by assuming implicitly the absence of z -dependence in the problem. However, the phase shift of the signal is

coupled to the amplitude of the signal modulation, in contrast to what occurs without pump modulation. Therefore, even in the undepleted case, for large amplitudes of the pump modulation we must take into account the spatial variation of the amplitude of the modulated part of the signal in order to accurately explain the behavior of the phase shift of the signal. In order to show this effect, let us consider that the spatial variation of the amplitude of the signal modulation P_{sm} is very small so that:

$$P_{sm}(z) \simeq P_{sm}(0) + \frac{z\alpha_s}{L} P_{pm} \cos \varphi \frac{P_{s0}(1 + \beta_s + \beta_s P_{s0})}{w_c^2}, \quad (14)$$

where we have considered a low modulation frequency, i.e., $w_m < w_c$. By using this expression we calculate the phase shift ϕ_s at the fiber output:

$$\phi_s(z=L) \propto -\sin \varphi \left[1 - P_{pm} \cos \varphi \frac{\alpha_s P_{s0}(1 + \beta_s + \beta_s P_{s0})}{2w_c^2 P_{sm}(0)} \right], \quad (15)$$

which shows a deviation from the sinusoidal profile. This correction leads to a shift of the position of the maximum delay towards larger values of φ whereas leads to a shift of the position of the maximum advancement in the opposite direction. The magnitude of this shift increases as the amplitude of the pump modulation increases, in agreement with the experimental results (see figure 5). This deviation of the $F_s(\varphi)$ curve from the sinusoidal profile is due to the coupling of the phase shift ϕ_s with the amplitude of signal modulation P_{sm} , which in fact, arises when modulating the pump.

Finally, we compare the magnitude of the signal fractional delay/advancement obtained in the presence or absence of modulation of the pump beam. To this aim, we have measured several curves of F_s versus f_m in the absence and in the presence of modulation of the pump beam. In the presence of modulation, we have also varied the values of the relative phase between the signal and pump modulated beams φ . These results are plotted in figure 6. When the pump is not modulated, the maximum fractional delay or advancement that can be achieved within the undepleted approximation is given by $\pm\alpha_s/(16\pi)$ which, for our experimental system, is close to ± 0.025 . Note that when this approximation is not valid (high optical densities) a more complex relation of the maximum fractional delay with the fiber length is obtained [17]. These two optimum cases have been measured when we modulate the signal with an amplitude of $P_{sm} = 0.3P_{s0}$. Optimum delay is achieved without pump, at the optimum modulation frequency $w_m \simeq w_c$, and an average signal power of 0.5 mW close to the signal saturation power $P_{s0} \simeq 1$ (see squares in figure 6 (a)). Maximum advancement is achieved increasing the signal power to 2 mW and applying a high pump power of 23 mW (see circles in figure 6 (a)). In order to analyze the effect of the periodic modulation of the pump beam, we consider similar parameters to the ones used without pump modulation while we periodically modulate the pump power such that $P_{pm} = 0.7P_{p0}$. Different curves shown in figure 6 (b)-(d) correspond to different values of the relative phase between the signal and pump modulated beams φ . The simulated curves have also been plotted in figure 6 (lines). We observe that the delay and advancement obtained when modulating the pump beam is around one order of magnitude larger than the one obtained without pump modulation. Furthermore, the behavior exhibited by the signal delay strongly depends on φ . We observe that for values of φ around $\pi/2$, delay is achieved for all values of f_m (see figure 6 (b)), whereas for values of φ around $3\pi/2$, advancement is achieved for all modulation frequencies (see figure 6 (d)). Note that for intermediate values of φ , around π , an increase in the

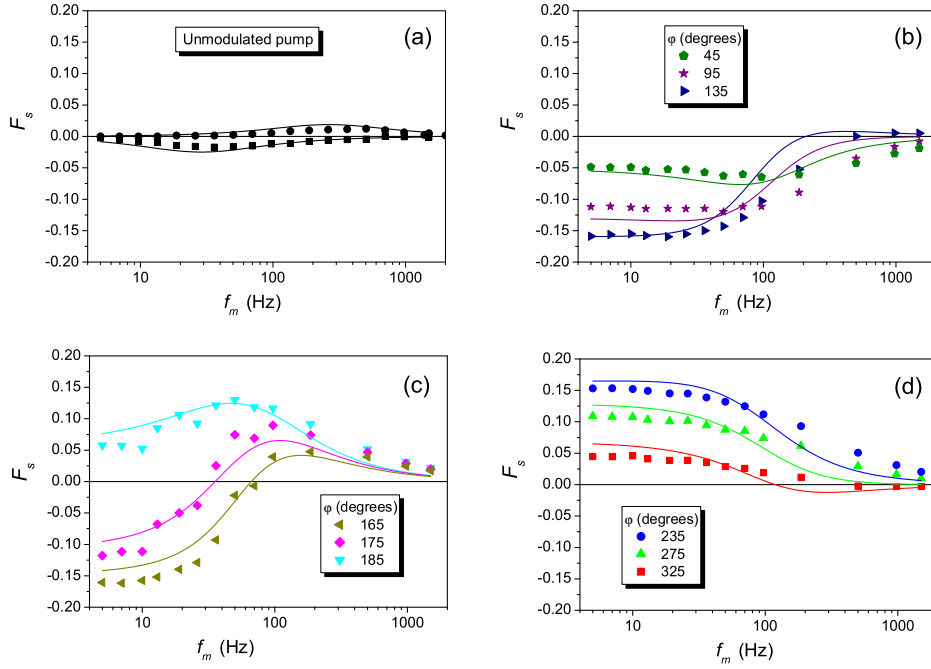


Figure 6. Fractional advancement of the signal as a function of the modulation frequency: (a) for the unmodulated pump case; and (b)-(d) when modulating the pump beam and for different relative phases between the signal and pump modulated beams φ . Experiments (symbols) and simulations (lines). (a) Optimum delay (squares): Signal power = 0.5 mW ($P_{s0} = 0.9$) with $P_{sm} = 0.3P_{s0}$, and pump power $P_{p0} = 0$ mW; Optimum advancement (circles): Signal power = 2 mW ($P_{s0} = 3.4$) with $P_{sm} = 0.3P_{s0}$, and pump power = 23 mW ($P_{p0} = 10$). (b)-(d) Signal power = 0.5 mW ($P_{s0} = 0.9$) with $P_{sm} = 0.4P_{s0}$, and pump power = 10 mW ($P_{p0} = 4.4$) with $P_{pm} = 0.7P_{p0}$.

modulation frequency switches from delay to advancement (see figure 6 (c)). These results have been reproduced by the simulations.

The signal fractional advancement can be related with the refractive index of the material at the probe field frequency which usually shows a dispersive-like profile. However, curves in figure 6 show a dispersive- or absorptive-like shape depending on the value of the relative phase between the signal and pump modulated beams. In order to clarify this behavior, we analyze theoretically the evolution of the fractional advancement and the modulation gain (the ratio of the output to input modulation depths) for the signal and the pump as a function of the modulation frequency. In figure 7 we plot that dependencies for four representative values of the relative phase between the signal and pump modulated beams and for the same parameters used in figure 6. As we said before, when the pump modulation amplitude is much higher than the signal modulation amplitude, the population oscillations are mainly due to

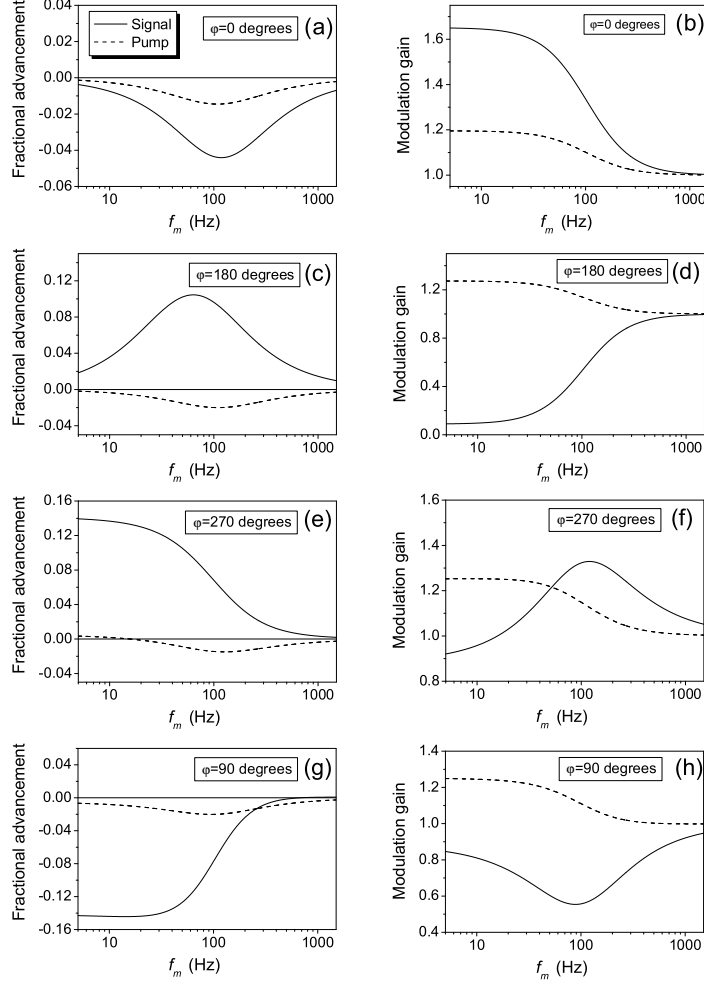


Figure 7. Simulated fractional advancement of the signal (solid line) and pump (dashed line) as a function of the modulation frequency for different relative phases between the signal and pump modulated beams: $\varphi = 0$ (a) $\varphi = \pi$ (c), $\varphi = 3\pi/2$ (e), and $\varphi = \pi/2$ (g). Simulated modulation gain for the signal $[(P_{sm}/P_{s0})_{out}/(P_{sm}/P_{s0})_{in}]$ (solid line) and pump (dashed line) as a function of the modulation frequency for $\varphi = 0$ (b) $\varphi = \pi$ (d), $\varphi = 3\pi/2$ (f), and $\varphi = \pi/2$ (h). $P_{s0} = 0.9$ with $P_{sm} = 0.4P_{s0}$, and $P_{p0} = 4.4$ with $P_{pm} = 0.7P_{p0}$.

the pump beam. In that case, the dependence of the pump phase shift with the modulation frequency is given by $\phi_p \propto -\omega_m/(\omega_c^2 + \omega_m^2)$ while the dependence of the pump modulation amplitude with ω_m is $P_{pm} \propto \omega_c/(\omega_c^2 + \omega_m^2)$. That is, ϕ_p shows the form of a dispersive-like curve while P_{pm} follows the form of an absorptive-like curve which shows the hole produced by the population oscillations in the pump absorption spectrum.

Both, the dispersive and absorptive phenomena that characterize ϕ_p and P_{pm} , contribute to the phase shift and also to the modulation amplitude of the signal beam through the relative phase φ . Thus, for $\varphi = 0$ or $\varphi = \pi$, ϕ_s follows a dispersive-like curve whereas P_{sm} develops an absorptive-like curve similarly to the behavior of ϕ_p and P_{pm} , respectively. In particular, for $\varphi = 0$, ϕ_s and P_{sm} behaves in the same way than ϕ_p and P_{pm} , respectively, as can be seen in figures 7 (a) and (b). As the signal modulation gain measures the ratio of the transmittance of the modulated part of the signal and the average signal power, we see in figure 7 (b) that the modulated part of the signal P_{sm} exhibits more gain than the average signal power P_{s0} . Thus, the signal delay can be explained as an antihole in the gain spectrum (gain increase) for P_{sm} generated by the population oscillations governed by the pump. For $\varphi = \pi$, ϕ_s and P_{sm} behaves in a similar manner although with opposite sign (see figures 7(c) and (d)). In this case, the signal advancement is due to the hole produced in the gain spectrum by the population oscillations. More complex behaviors are obtained for $\varphi = \pi/2$ or $\varphi = 3\pi/2$. In those particular cases, there is an interchange between the roles of ϕ_s and P_{sm} . That is, ϕ_s develops an absorptive-like curve following P_{pm} whereas P_{sm} develops a dispersive-like curve following ϕ_p . The case of $\varphi = 3\pi/2$ is shown in figures 7 (e) and (f). We see that ϕ_s resembles the spectral hole obtained for the pump whereas P_{sm} looks like the dispersive-like curve developed for the pump phase shift. In this case, the modulated part of the signal P_{sm} exhibits more gain than the average signal power P_{s0} and this phenomenon occurs for frequencies around ω_c (see figures 7 (e) and (f)). This shifted gain peak could be seen as a hole in the gain spectrum around $\omega_m = 0$, leading to signal advancement. For $\varphi = \pi/2$, a similar result is obtained (see figures 7 (g) and (h)). In this case, the modulated part of the signal P_{sm} exhibits less gain than the average signal power P_{s0} and this phenomenon occurs again for frequencies around ω_c (see figures 7 (g) and (h)). This shifted hole peak in the gain spectrum could be see as an antihole around $\omega_m = 0$. Thus, the signal delay could be explained in terms of this antihole. In summary, the behavior of the signal described above can be explained in terms of the interaction between the signal and the population oscillations generated by the pump. In some way, we could say that the pump intensity profile is imprinted onto the signal one through the population oscillations.

4.2. Signal and pump delay coupling

Now, let us analyze the interplay between the delay undergone by the signal beam and the one experienced by the pump beam, i.e., we study simultaneously the group velocity of both beams and the influence of the relative phase φ in those velocities. We analyze under which conditions the coupling between the two beams makes that both propagate with the same group velocity, that is, the conditions that lead to a synchronization-like phenomenon. To this end, let us first analyze in more detail the relation between the analytical expression of the signal phase shift derived in equation (13) and the expression derived for the pump phase shift following the same approach:

$$\phi_p(z = L) \simeq \frac{\alpha_p P_{p0}}{(w_c^2 + w_m^2) w_c (1 + \beta_s)} \left[-w_m (1 + \beta_s + \beta_s P_{s0}) + \frac{P_{sm}}{P_{pm}} (\beta_s P_{p0} - 1) \sin [\varphi - \xi_m] \right]. \quad (16)$$

We look for a condition which allows both beams to travel with the same group velocity independently of the average pump or signal powers (P_{p0} and P_{s0}). To this

end, we consider the case where the two beams are modulated in phase or in opposite phase, i.e., $\varphi = n\pi$ with $n = 0, 1$. Then, the signal and pump phase shifts remain:

$$\phi_s(z = L) \simeq \frac{\alpha_s P_{s0} w_m}{(w_c^2 + w_m^2) w_c} \left[(\beta_s P_{p0} - 1) - \frac{P_{pm}}{P_{sm}} (1 + \beta_s + \beta_s P_{s0}) (-1)^n \right], \quad (17)$$

$$\phi_p(z = L) \simeq \frac{\alpha_p P_{p0} w_m}{(w_c^2 + w_m^2) w_c (1 + \beta_s)} \left[\frac{P_{sm}}{P_{pm}} (\beta_s P_{p0} - 1) (-1)^n - (1 + \beta_s + \beta_s P_{s0}) \right] \quad (18)$$

An inspection of equations (17)-(18) reveals that both beams suffer the same delay (in absolute value) when the ratio of the modulation depths is:

$$\frac{P_{sm}/P_{s0}}{P_{pm}/P_{p0}} = \frac{\alpha_s (1 + \beta_s)}{\alpha_p}, \quad (19)$$

which for our experimental system is close to 2. Thus, $\phi_s = \phi_p$ at $\varphi = 0$ and $\phi_s = -\phi_p$ at $\varphi = \pi$. To experimentally observe these predictions, we have measured simultaneously F_s and F_p as a function of the modulation frequency f_m for different values of φ . We modulate the signal power (1.8 mW) with a modulation depth of $P_{sm}/P_{s0} \simeq 0.65$ and the pump power (2.2 mW) with a modulation depth of $P_{pm}/P_{p0} \simeq 0.3$ in such a way that the ratio between the modulation depths is close to the one given by equation (19). The experimental results (symbols) and the simulated ones (lines) are shown in figure 8. F_s and F_p are almost equal when both beams are modulated in phase, i.e., at $\varphi = 0$ (see figure 8 (a)), in agreement with the theoretical prediction. In this situation, the coupling of both beams leads to similar signal and pump group velocities for all modulation frequencies. That means that both beams propagate in phase along the fiber. On the contrary, when we modulate both beams in phase opposition, i.e., at $\varphi = \pi$, F_s and F_p take the same value but with different sign, in agreement with the theoretical prediction, that is, while the signal suffers advancement the pump suffers a delay of the same value being the optimum modulation frequency around 100 Hz (see figure 8 (c)). More complex behaviors are observed at other values of the phase difference between both modulations, as shown in figure 8 (b) and (d). For example, at $\varphi = \pi/2$, the pump beam suffers a transition from advancement to delay as the modulation frequency increases. Note that only the case of exactly equal velocities ($\varphi = 0$) is stable under propagation. However, for the other values of φ , within the undepleted approximation, the difference between the signal and pump phase shifts will depend linearly with the fiber length although this dependence is not relevant in our experiments due to the small values of F_s or F_p obtained.

We have also experimentally corroborated that, when both beams are modulated in phase ($\varphi = 0$) or in opposite-phase ($\varphi = \pi$), they propagate with the same group velocity (in absolute value) independently of the average pump power. These results are shown in figure 9 where we plot the fractional advancement of the signal and pump as a function of the average pump power for these two relative phases φ and for a modulation frequency of $f_m = 50$ Hz. As in figure 8, we use again a signal power of 1.8 mW with a modulation depth of 0.65, and a modulation depth for the pump power of 0.3. We also plot the simulated fractional advancement of the signal (dashed line) and pump (solid line). As expected, the values of F_s and F_p are quite similar for each pump power when both beams are modulated in phase. Furthermore, when we modulate both beams in phase opposition, the fractional delay of the pump shows the same value than the fractional advancement of the signal and vice versa. As we

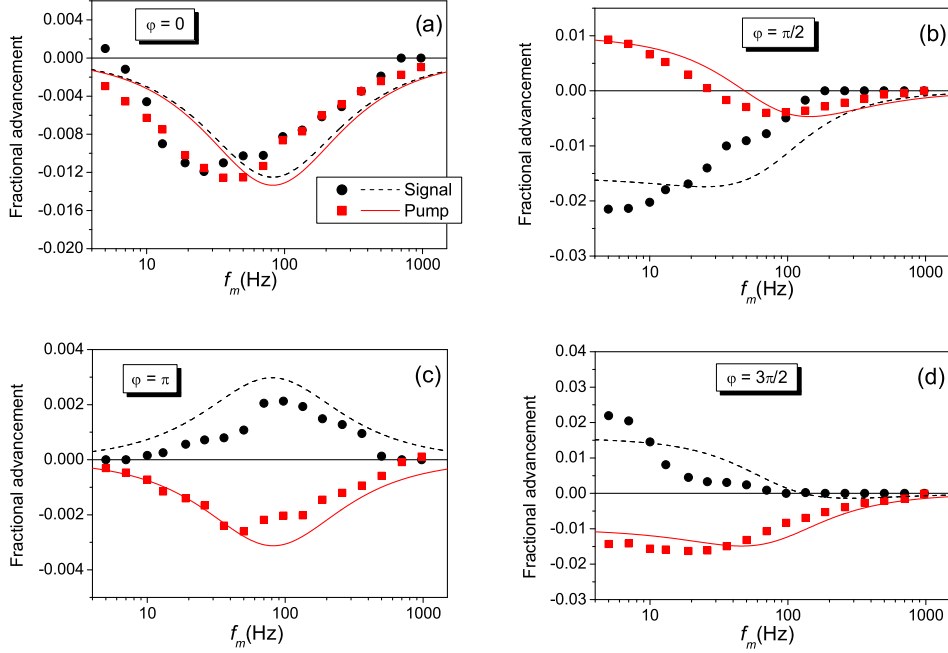


Figure 8. Fractional advancement of the signal (circles) and pump (squares) as a function of the modulation frequency for different relative phases between the signal and pump modulated beams φ . Simulated fractional advancement of the signal (dashed line) and pump (solid line). Signal power = 1.8 mW ($P_{s0} = 3$) with $P_{sm} = 0.65P_{s0}$, and pump power = 2.2 mW ($P_{p0} = 0.9$) with $P_{pm} = 0.3P_{p0}$.

have shown, the in-phase propagation of both beams is a general trend that does not depend on the modulation frequency or the average pump power, so it could be used for the propagation of pulses.

The group velocity synchronization-like phenomenon described in this work could be applied to a more interesting situation where we use two amplitude-modulated light beams, both with carrier frequencies within the optical communications C band (approximately from 1530 to 1565 nm). In fact, as we mention in section 1, Stepanov *et al* [19] controlled the phase shift of a 1526 nm probe beam in an EDF by using a 1568 nm saturating beam. Following the same analysis used in this section, we could achieve the same group velocity for both beams when the ratio of the modulation depths satisfy the following condition:

$$\frac{P_{sm}^{(1)}/P_{s0}^{(1)}}{P_{sm}^{(2)}/P_{s0}^{(2)}} = \frac{\alpha_s^{(1)}(1 + \beta_s^{(1)})}{\alpha_s^{(2)}(1 + \beta_s^{(2)})}, \quad (20)$$

where the superscripts (1) and (2) correspond to the different wavelengths.

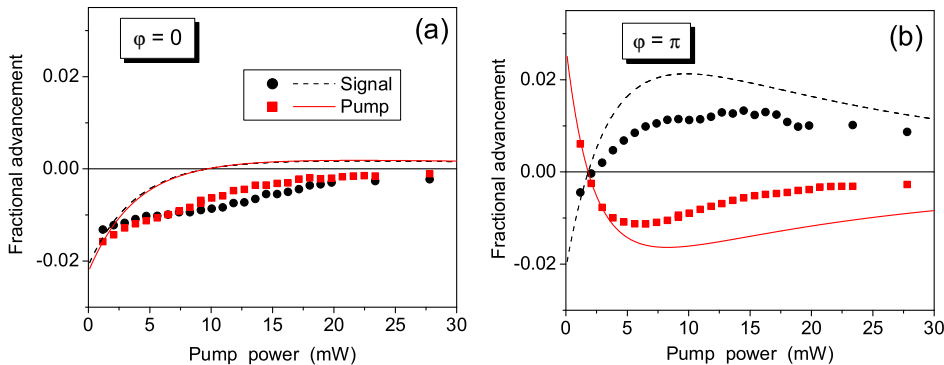


Figure 9. Fractional advancement of the signal (circles) and pump (squares) as a function of the average pump power for two different relative phases between the signal and pump modulated beams φ . Simulated fractional advancement of the signal (dashed line) and pump (solid line). Signal power = 1.8 mW ($P_{s0} = 3$) with $P_{sm} = 0.65P_{s0}$, and $P_{pm} = 0.3P_{p0}$. $f_m = 50$ Hz

5. Conclusions

In conclusion, we report the control of the slow and fast light propagation velocity of two amplitude-modulated light beams by means of CPO. These light beams correspond to the usual signal (at 1550 nm) and pump (at 980 nm) beams used in EDF amplifiers. To this end, we induce a simultaneous beat in both beams with the same frequency so that the relative phase between both beats allows us to control their group velocities. This condition could make difficult the application of the proposed mechanism for unpredictable signals, like a data stream. When the population oscillations are mainly governed by the modulated pump, an enhancement of the delay or advancement of the 1550 nm beam in one order of magnitude is observed. When the two modulated beams contribute similarly to the population oscillations, a synchronized propagation of both beams has been found. Thus, when both beams are modulated in phase, they propagate with the same group velocity along the fiber for each modulation frequency. This simultaneous propagation is obtained for all the average pump powers. Furthermore, when we modulate both beams in phase opposition, while signal suffers advancement, pump suffers delay, traveling both with the same absolute value of the group velocity. These results could be used in semiconductors which are good candidates for telecommunication applications due to their fast characteristic relaxation time scale (GHz). In fact, Antón et al [23] have shown that by modulating the injection current in a semiconductor optical amplifier to force the population oscillations they control and enhance the delay of the optical signal. These predictions have been experimentally proved in a very recent work [24].

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