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Compact Balanced Tries

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1 Introduction

Classical B –trees offer both fast direct addressing and easy sequential processing. The minimum storage utilization of a B –tree is 50%. Moreover it is always possible to shrink a B –tree to a minimum size as follows: scan the leaves in key increasing order; when reaching a leaf, transfer to it the keys of the next leaf with respect to the key order, until the leaf storage utilization is maximum, and delete the next leaf if it becomes empty; after such a shrinking, the B –tree has almost a 100% storage utilization. The segmented structure of B –trees makes them suitable for a multi-user environment. Their only drawback is their relative lack of compactness. A later version of the B –tree, the *Prefix B –tree* [1], improves upon this by substantial (about 50%) saving of storage utilization.

Other methods have been proposed in the last decade; they do not offer all the B –tree properties.

The *Bounding Disorder Method* [11] uses a mixing of hashing and tree indexing. The upper part of the index is tree ordered, while the lower part is hashed in multi-bucket nodes; this method provides good results for equi-join queries and for large range queries; however, sequential processing may result in weak performance and delicate overflow handling is necessary. Average storage utilization is about 80%.

Trie Hashing [10] uses an in-core trie directory. It allows sequential processing and the storage utilization is about 80%. However, the directory size is $O(n^{1+1/s})$ [4] (n being the number of records inserted and s the bucket size), which is superlinear in n , and the directory is not segmentable; this implies low parallelism for directory updating and limits the maximal data size. Moreover, unfavourable key distributions result in a large increase of the directory size.

The *Compact 0-complete Tree* [12] (section 2), also a B –tree descendant, produces very compact storage (4 bytes per key structure with 60% storage utilization), but no longer has the flexibility properties of the original B –tree.

The *Compact Trie* [8], [3] (section 3), based on a bit-map representation of the tries, is a simple, powerful, but not segmented structure.

We show (section 4) how it is possible to split Compact Tries in a segmented and flexible structure of B -tree type, keeping the compactness advantages of the Compact Tries and recovering all the important properties of B -trees. We call this new structure a *Compact Balanced Trie*. At the block-node level of the structure, binary search is not possible and only sequential processing is permitted; this is the price we must pay for the compression and this is not much of a drawback when considering that sequential-processing is only local and performed as in-core processing.

Experimental results are given in section 5.

2 Compact 0-complete Trees (C_0 -Trees)

The Compact 0-complete Trees, except the worst case splitting problem discussed in this chapter, have the best characteristics of an ordered index, and their architecture is similar to the architecture of a classical B -tree.

For random keys, they can represent 32 bytes long keys with only one byte; this result will be the point of comparison for the Compact-Balanced Tries.

2.1 Brief survey of the C_0 -Trees

2.1.1 0-complete trie

A 0-complete trie is a trie where each node has at-least a 0-node son; (a 0-node is a node accessed by a 0 bit in the trie).

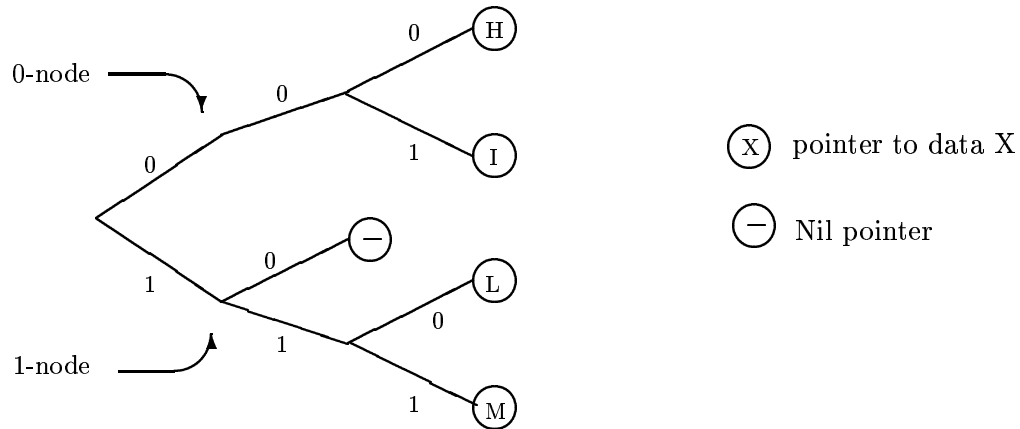


Figure 1: 0-complete trie

2.1.2 Bounding nodes

The following property holds for a 0-complete trie: each leaf node has a 1-node as a successor in the preorder traversal of the trie, which is called its bounding node; bounding nodes are represented with double circles in Figure 2.

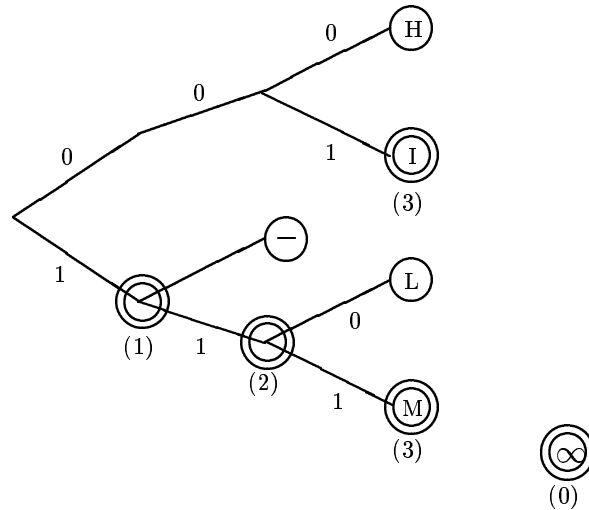


Figure 2: Bounding nodes

The depths of the bounding nodes are in parentheses in Figure 2; a special bounding node with depth 0 is added to bound the last leaf. With these preliminaries, Orlandic and Pfaltz produce an algorithm which provides the key of a leaf as a function of the depth of its bounding node and of the depths of all the preceding bounding nodes. This algorithm may be summarized as follows: scanning of the depths of the bounding nodes is sequentially processed; the starting key is null; set to 1 the bit with position equal to the current depth; set to 0 all the bits to the right of this bit.

Hence, we get the following table, corresponding to the trie of Figure 2:

depth	depths sequence	key	leaf
3	3	001	H
1	3, 1	100	I
2	3, 1, 2	110	—
3	3, 1, 2, 3	111	L
0	3, 1, 2, 3, 0	∞	M

Figure 3: Key construction

2.1.3 C_0 -node representation and C_0 -node splitting

A C_0 -node is a list of entries, each entry consisting of a bounding node depth and a data (or NIL) pointer; a node is a simple trie-node.

Node	
depth	data pointer
3	H
1	I
2	—
3	L
0	M

Figure 4: C_0 —compact node

The splitting rule for an overflowing C_0 —node is as follows: any entry may be chosen for the splitting, with the condition that no preceding entry in the C_0 —node has a depth inferior to the depth of this entry.

In case of Figure 4, the two possible splitting entries are entry 1 (depth 3), and entry 2 (depth 1). This rule, called minimal depth splitting rule, allows the handling of the upper parts of the C_0 —tree with the same algorithm as used for the leaves, but it does not insure, in worst cases, a good filling rate of the C_0 —nodes; the worst case is a kind of 1-comb which degenerates in a succession of 1-entry C_0 —nodes (Figure 5).

Moreover, the minimal depth splitting rule does not allow the transfer of entries at will between adjacent brother nodes, when this B —trees capability allows by a progressive scanning of the leaves to reach any desired filling rate.

For these reasons, we consider that the C_0 —compact trees do not offer the complete security required for standard indexes of B —tree type.

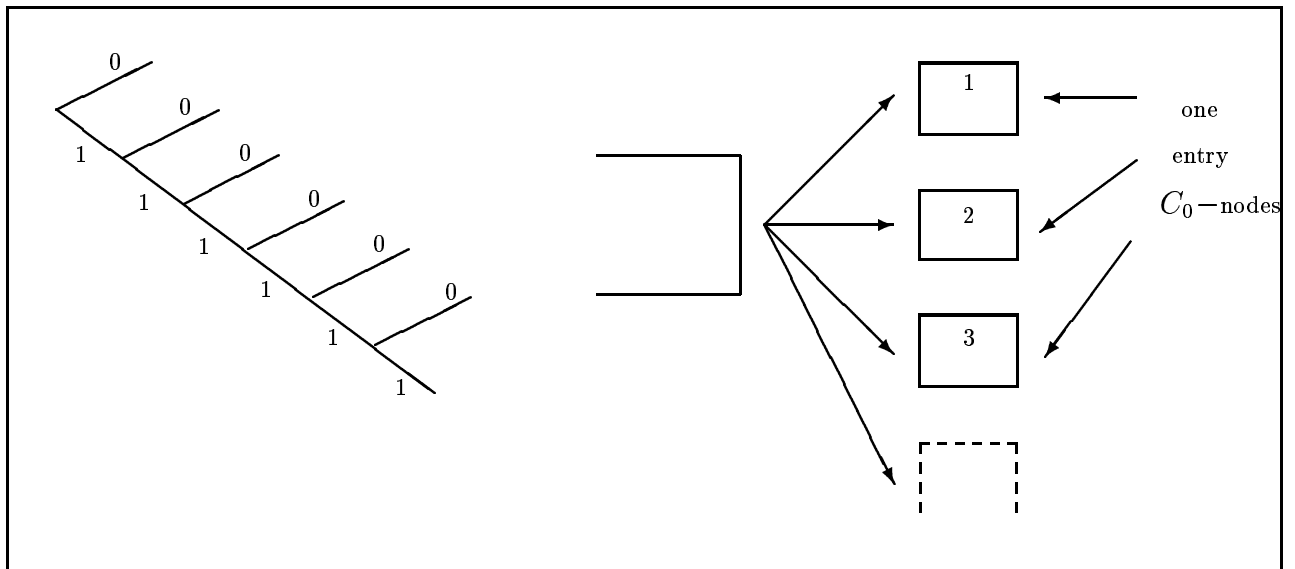


Figure 5: worst splitting case for the C_0 —Trees

3 Compact Trie

Jean Kouacou-Kouadio proposes a compact trie representation by bit-map, based on a scan along the nodes of the trie in respect with the preorder traversal [8].

W. de Jonge, A. S. Tanenbaum and R. P. van de Riet [3] propose a very similar representation; they call it linear representation. The Compact Balanced Trie we present in the next section is an extension of the Compact Trie, in terms of its ability to split the trie into subtries and to represent each of these in a compact way.

We present in this section the Compact Tries, and a data structure to handle them.

3.1 Compact-Trie Representation

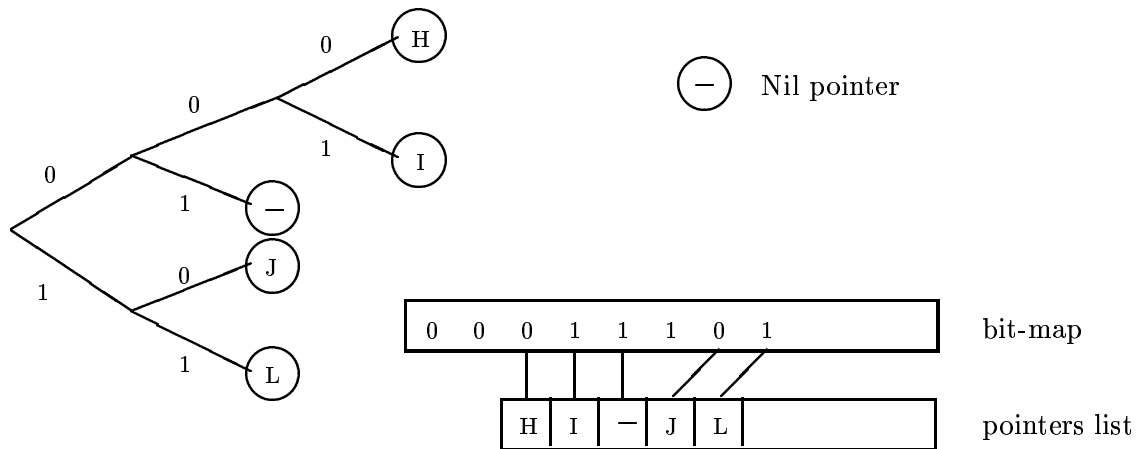


Figure 6: Compact-Trie Representation

The Compact Trie representation is composed of a bit-map and of a pointer-list. The 0 or 1 bit value of the trie corresponds to the digital values of the keys, data I beginning by 001 (Figure 6).

The bit-map is the sequence of 0 and 1 obtained by preorder traversal of the trie (Figure 6). The pointer list associates a pointer to each leaf of the trie.

A basic property of this representation is that any bit of the bit-map followed by a 1-bit represents a leaf node.

This property is true for a trie with a root and two leaves; note that replacing a leaf by a subtree with an interior node and two leaves corresponds to the insertion of a “01” bit sequence in the bit-map just after the bit representing the replaced leaf (Figure 7), and supposing the property true for any trie of $2n$ leaves, it is also true, by induction, for any trie of $2n + 2$ leaves.

3.2 Insertion

We suppose the key J has the value 10001001 and we want to insert a key K of value 10101111 in the trie of Figure 6; this will lead to the trie and the representation of Figure 7.

The insertion of another key X of value 10001000 will lead to Figure 8; in this figure, the presence of 4 new NIL-pointers is noticeable.

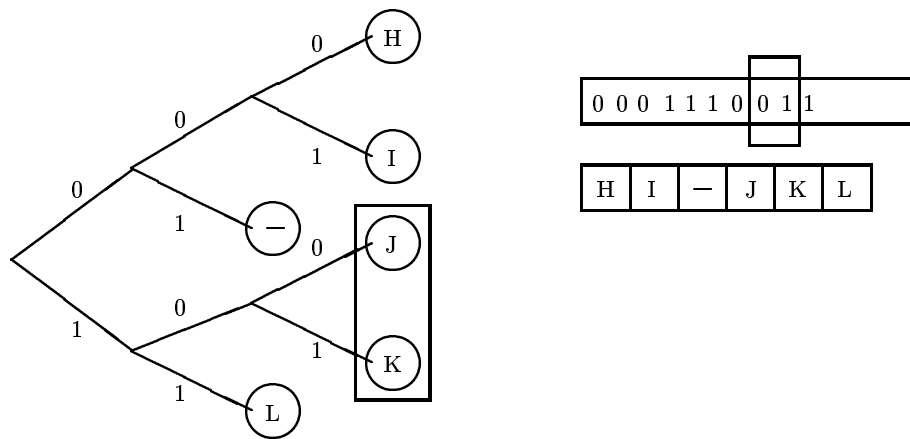


Figure 7: Insertion of key K (10101111)

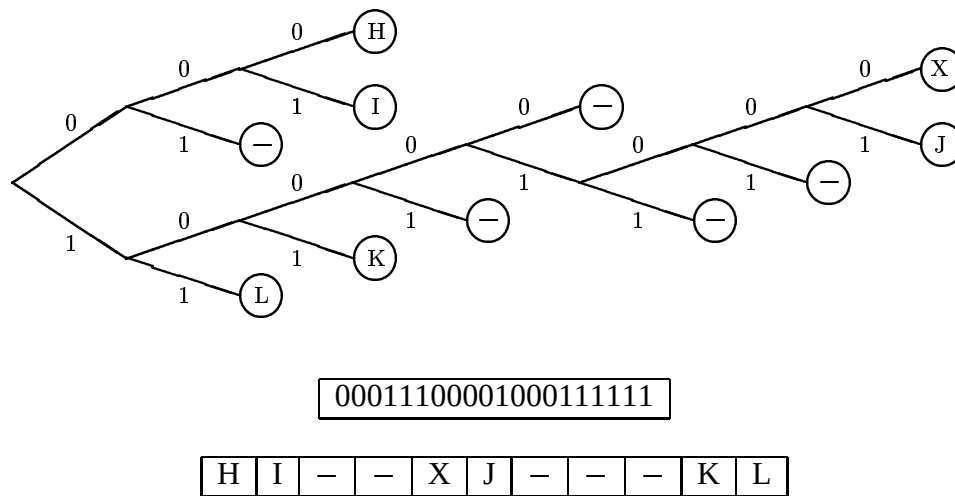


Figure 8: Insertion of key X (10001000)

3.3 Deletion

A key can be immediately deleted by setting to NIL the pointer to the suppressed key.

However it is useful to eliminate the unnecessary NIL-pointers; this is done by iteratively replacing the subtrees composed of an internal node, a data-leaf and a NIL-leaf, by a data-leaf, and by updating consequently the bit-map and the pointer list.

Deletion of key X in Figure 8 leads back to Figure 7.

3.4 Retrieval

The retrieval algorithm is based on a joint processing of the bit-map and of the pointers-list.

Each bit of the retrieval key is checked from left to right; for each 1-bit found, the corresponding 0-subtrie is skipped over.

Skipping over a subtrie is straightforward since in any subtrie the number of leaves exceeds by 1 the number of interior nodes.

Therefore, the following retrieval algorithm stands:

```
int      bx;          /* index in the bit-map                */
int      bk;          /* bit being checked in the retrieved key */
int      px;          /* index in the pointers-list            */
int      nbbit;       /* number of bits in the bit-map        */

retrieve()
{
    for ( bk=1, bx=1, px=1;  bx <= nbbit;  bk++, bx++ ) {
        if ( bitkey(bk) == 0 )      skipstrie();
        if ( bitmap(bx+1) == 1 )    break;
    }
}

skipstrie()
{
    int      interior = 0;
    int      leaf     = 0;

    do {
        if ( bitmap(bx+1) == 1 )    { leaf++; px++; }
        else                        interior++;
        bx++;
    }
    while( leaf < interior + 1 );
}
```

3.5 Data Structure for Compact-Tries

We propose the structure of Figure 9 to handle a significant presence of NIL-pointers (other structures could be chosen, based upon a predicted amount of NIL-pointers).

The first byte of each pointer is only devoted to NIL-pointers; its value is the number of consecutive NIL-pointers at this point.

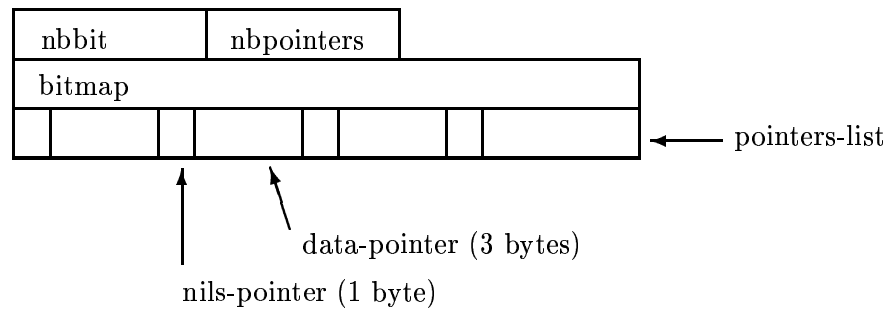


Figure 9: data structure for Compact-Tries

20		6			
00011110000100011111					
0	H	0	I	2	X
0	J	3	K	0	L

Figure 10: Compact Representation corresponding to the trie of figure 8

The drawback of this structure is that sequential processing all along the bit-map and the pointer-list is needed, which has two disadvantages: first, the processing time become very important as the number of keys increases; moreover, updating the structure implies locking the whole structure, which is a serious drawback for parallel processing.

These defaults will be corrected in the Compact-Balanced Tries we now present.

4 Compact-Balanced Tries (CB-Tries)

The Compact-Balanced Tries is a natural descendant of the Compact Trie of Jean Kouacou-Kouadio.

A trie is split into pieces and each piece is represented in a compact way by a node comparable to a B -tree node.

An edge key is generated at each trie or subtrie splitting and a corresponding starting depth is calculated. The edge key is the key value of the splitting point. The edge depth indicates the number of bits of the binary representation of the edge key to take in account before coming back to the ordinary processing of the bit-map. The edge handling modifies a part of the insertion, deletion and retrieval algorithm, but the global aspect of these algorithms is maintained.

The data structure exhibited to handle the Compact-Balanced Tries closely follows the one presented for handling the Compact Tries.

We will differentiate the trie-nodes or nodes from the Compact-Balanced CB-nodes containing trie-nodes.

4.1 Trie Splitting

We will split the trie T of Figure 6, assuming a 10001001 value for data J (Figure 11).

This key J is the edge key of the subtrie T_2 ; the associated edge-depth is 2; the subtrie T_1 is the beginning part (using preorder traversal) of the trie T ; hence it has no edge-depth; the only difference between such a beginning trie and an ordinary trie is that its last leaf may be missing.

The biggest part of Compact-Trie representation is the pointer-list; for this reason, the splitting point will be chosen at middle of the pointer-list, and the first leaf of a subtrie may be a 1-leaf, just as the last one may be a 0-leaf; therefore the subtrees generated may remain incomplete, at the beginning, or at the end, or at both extremities.

Insertion of two more keys Y (10100000) and Z (10110000) would produce a splitting of subtrie T_2 and of the corresponding CB-node N_2 (Figure 12); subtrie T_3 is beginning-incomplete.

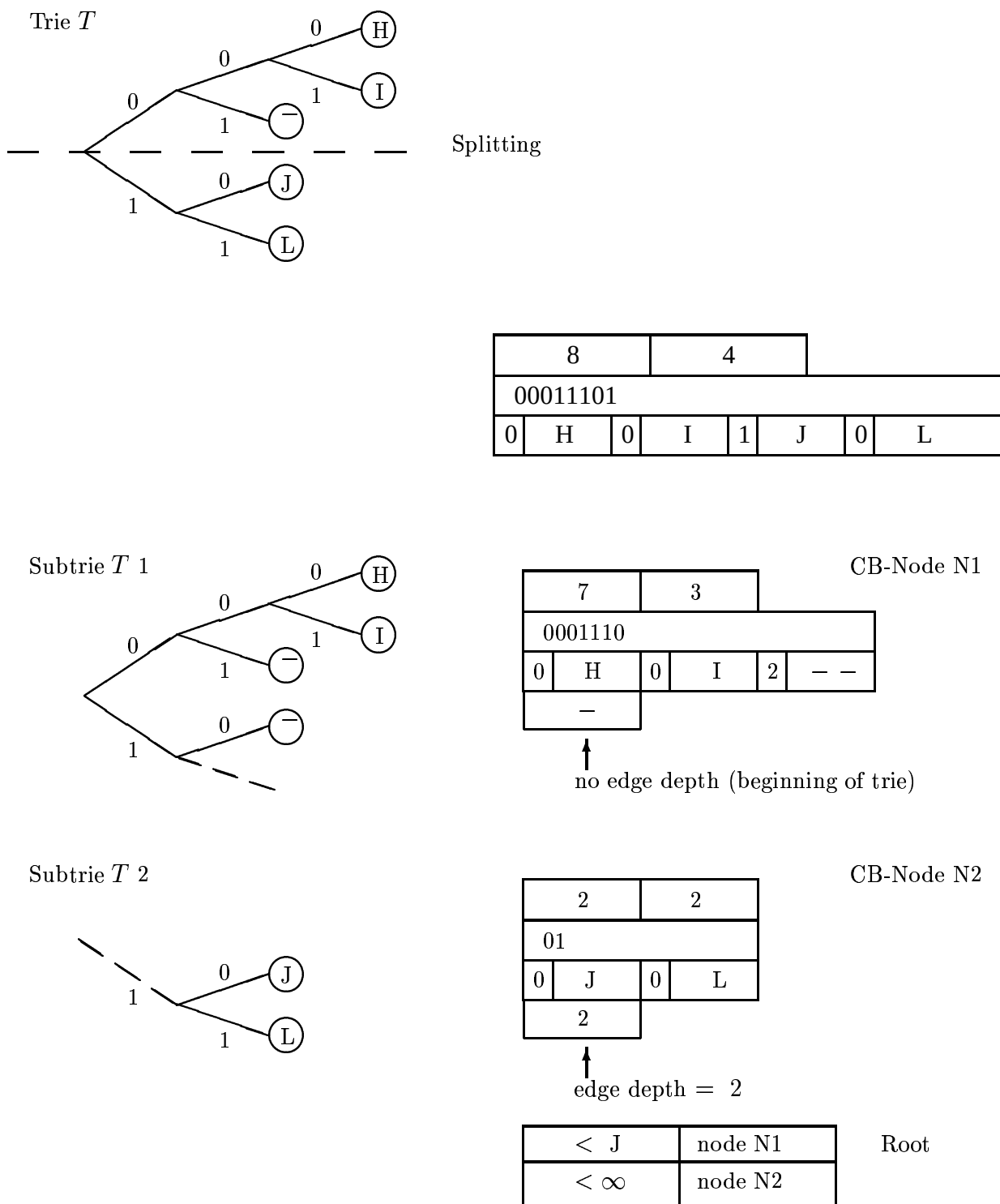


Figure 11: Trie Splitting and corresponding CB-nodes

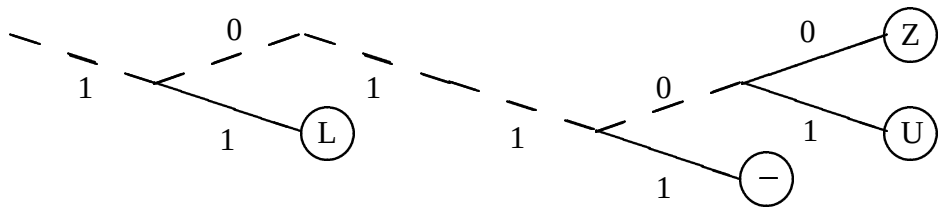
4.3 Insertions

When the edge-depth remains unchanged, the insertion algorithm is the same as the one used for a compact-trie.

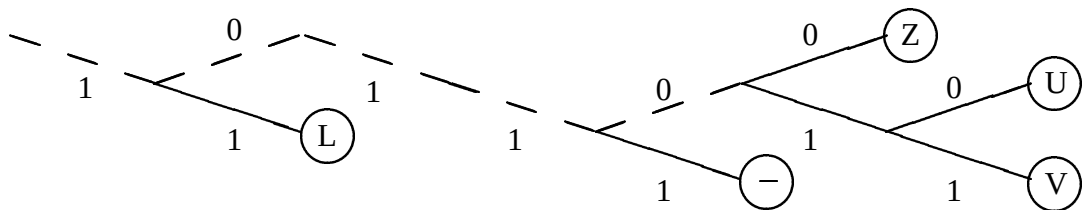
When the edge-depth is modified, the new edge-depth is the position of the first bit that differs in the binary representation of the edge key and of the inserted key; 1-NIL-leaves created by the insertion have to be handled in the bit-map and in the pointers-list; 0-NIL-leaves created by the insertion before the edge key have to be handled only if the inserted key is smaller than the edge key.



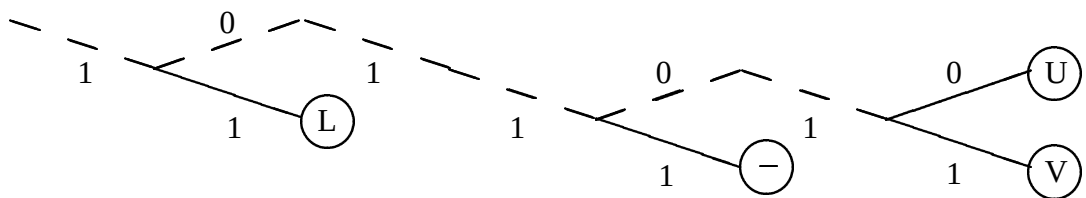
Subtrie T 3 : Z = 10110000, L = 11000000 (ed = 4)



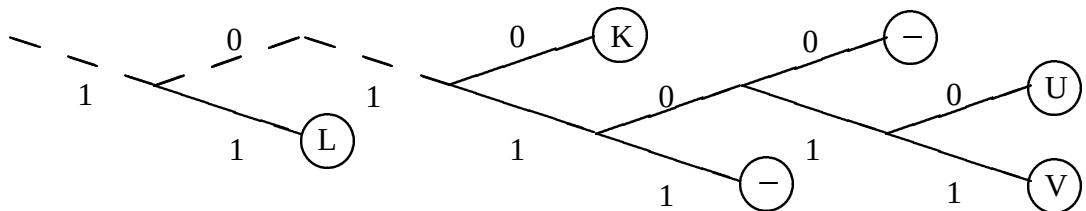
insert U = 10110100 (ed = 6)



insert $V = 10110110$ (ed = 7)



suppress Z (ed = 7)



insert K = 10100000 (ed = 4)

Figure 13: edge-depth modifications corresponding to key insertions and suppressions

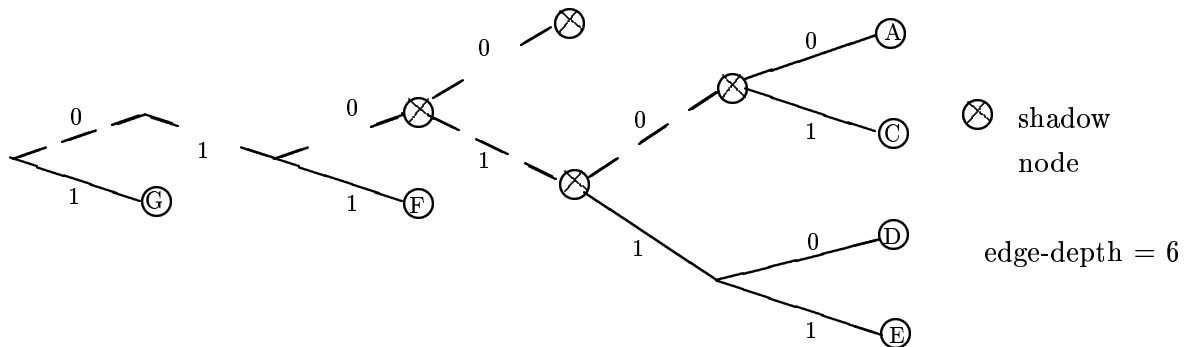
4.4 Deletions

When the edge key is not deleted, the algorithm is the same as in the case of compact trie.

When the edge key is deleted, compute the depth and the position inside the bit-list of the next data leaf (pointer 2 of the pointers-list). Then iterate upwards by checking the key bits of this data with decreasing depth; stop iterating when a 1-brother is either an interior node (detected in bit-map) or a data-leaf (detected in pointers-list). Conclude by updating the bit-map, the edge-depth and the pointers-list.

4.5 Retrieval

The description of the retrieval algorithm implies subtree skipping; therefore shadow interior nodes and shadow 0-leaves must be handled along the edge.

Figure 14: Edge-subtrie skipping (retrieve key F)

Retrieval of key F is proceeded by skipping the subtree containing the keys A, C, D, E , and four shadow nodes; this subtree contains 4 interior nodes (3 shadow), and 5 leaves (1 shadow); there is no subtree to skip if the retrieval key is smaller than the key-edge; there is one and only one edge-subtree to skip if the retrieval key is greater than the edge-key, and if the position of the first bit which differs in the binary representation of the retrieval key and of the edge-key is inferior or equal to the edge-depth.

There may be several ordinary subtrees skipped during the retrieval processing.

The edge-subtrie-skipping algorithm is given in Appendix A.

4.6 Depth edge calculus

The splitting process requires the computation of the depth of the new edge key (first key of the rightmost of the two brother CB-nodes exchanging entries).

This computation makes use of a stack algorithm, as shown in Figure 15.

The pile is built from the positions of the 0-bits of the last node being accessed in preorder traversal of the trie, along the bit-map.

For each 0-node (0-bit in the bit-map), the depth is increased by one and empiled.

For a 1-node, if the preceding bit is a zero, the depth remains unchanged, elsewhere the depth is equal to the top of the pile; then unpiling is performed.

When proceeding with an edge key, the starting depth is the edge-depth and the pile has to be loaded with the 0-bit positions of the edge-key (limited to the edge-depth); then the node depth may be computed as previously.

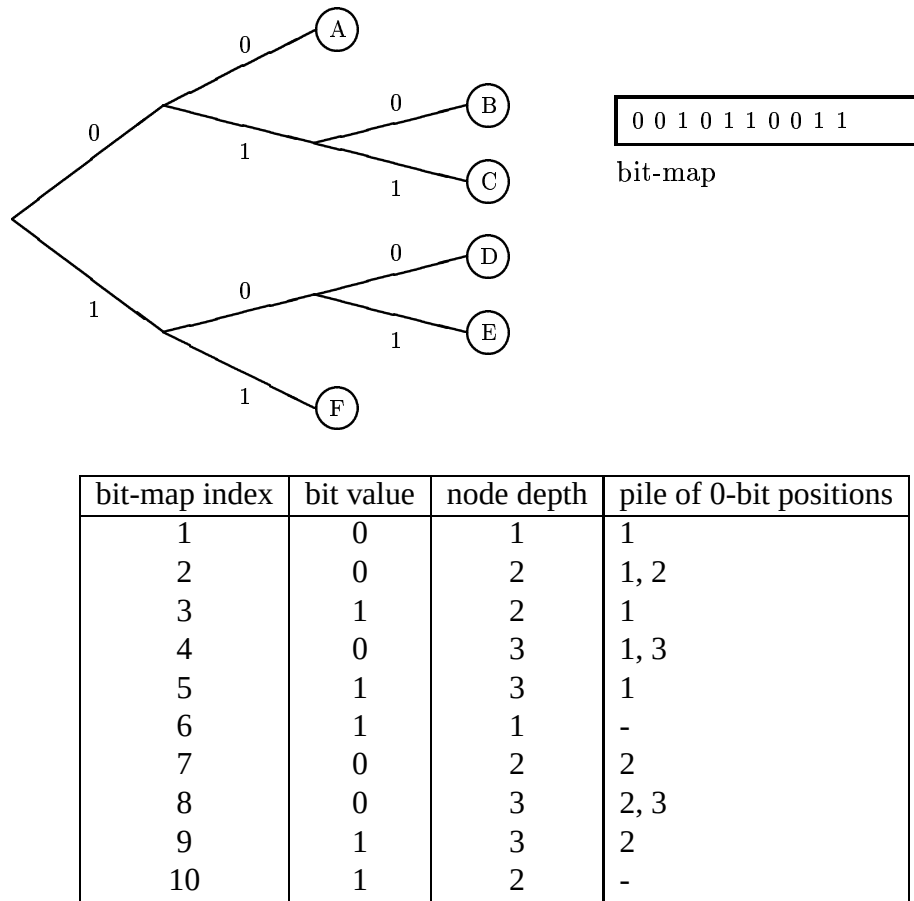


Figure 15: node depth computing

4.7 Merging and Balancing

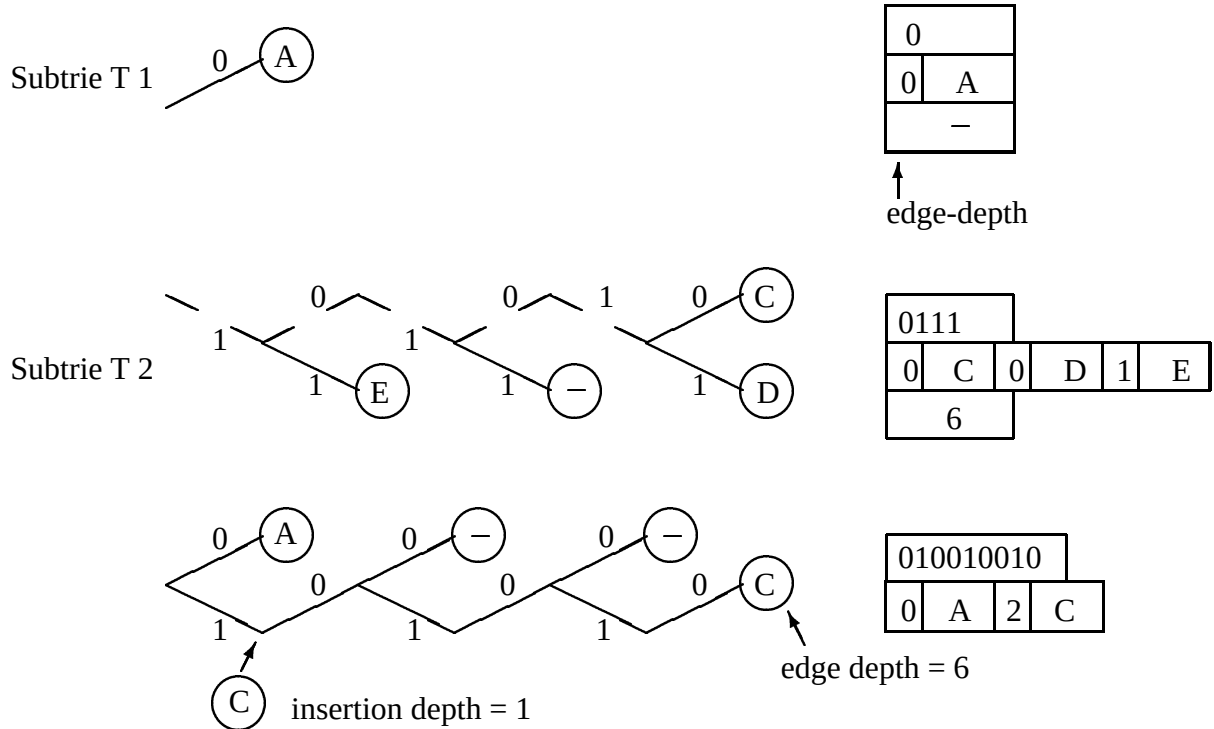
The balancing process between two CB-nodes may be done by merging the 2 CB-nodes in a double-size one, and then by splitting this node in two CB-nodes; therefore we only have to consider the merging process.

We will call the CB-node containing the keys of inferior (resp. superior) value as inferior (resp. superior) CB-node; the merging process will be performed by a special kind of insertion of the first key of the superior CB-node into the inferior CB-node, then by a concatenation of the two bit-maps, and by a concatenation of the two pointers-lists (with exclusion of the first bit and of the first pointer of the superior CB-node).

Figure 16 and Figure 17 show the two different cases of merging insertion; in case A (insertion depth < edge depth), an ordinary insertion would give a two bits 01 bit-map; this bit-map (and the pointer-list) is extended with interior nodes and NIL- $\emptyset$ -leaves until the edge depth of the superior node is reached; no 1-leaves have to be handled.

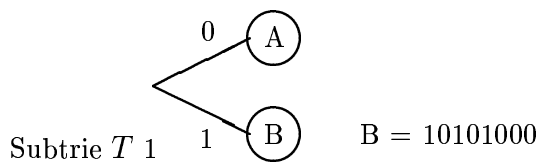
In case *B* (insertion depth > edge depth), neither interior nodes nor NIL- $\emptyset$ -leaves have to be handled, but NIL-1-leaves have to be handled in the bit-map and in the pointer-list, between the edge depth and the insertion depth.

During pointer-list concatenation, if the last pointer of the CB-inferior node is a NIL-pointer (no valid data), this NIL-pointer (number of NIL-leaves) has to be added to the NIL-part of the second NIL-pointer of the CB-superior node.

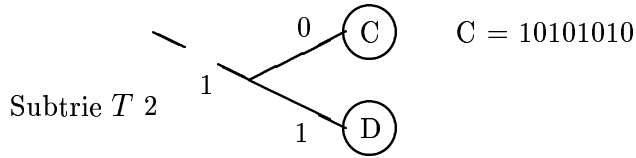


Case A : insertion depth < edge depth

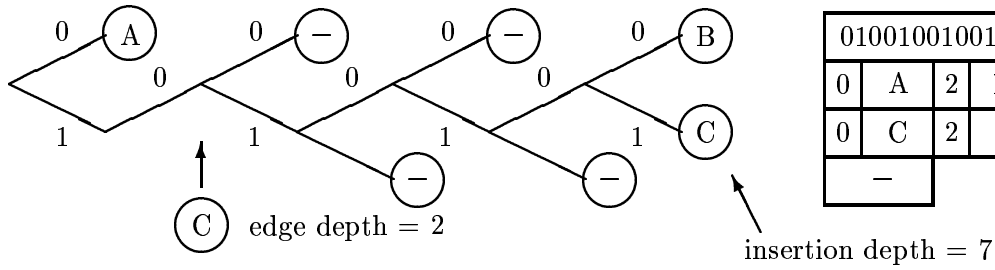
Figure 16: Merging Insertion of data *C* in subtrie *T1* for subtrees-merging of *T1* and *T2*



01			
0	A	0	B
	—		



01			
0	C	0	D
	2		



0100100100111			
0	A	2	B
0	C	2	—
	—		

Case B : insertion depth > edge depth

Figure 17: Merging Insertion of data C in subtrie T_1 for subtrees-merging of T_1 and T_2

5 Experimental results

5.1 Experimental results on the Unix Dictionary

Experimental results have been obtained on the Unix “words” dictionary.

The CB-node structure is given in Appendix A.

The experimental results (Appendix B) show that the number of NIL-leaves is about 400% of the number of data-leaves; this gives an average of 10 bits per key in the bit-map, and an average of 18 bits per key when counting the 8 bits of the NIL-pointers. These results are strongly dependent on the structure of alphanumeric data.

It is noticeable that purely sequential keys would produce no NIL-leaves, and therefore would request 2 bits per key in the bit-map, or 10 bits per key when including the bits of the NIL-pointers.

Randomly distributed keys request 11 bits per key.

The distribution of the NIL-pointers values provides ideas for further improving the structure; for instance, handling the NIL-pointer-list independently of the data pointer list, it is simple to add a secondary bit-list where each 1-bit corresponds to the presence of a NIL-pointer; the NIL-pointer list is reduced to the non-zero NIL pointers; in this case, the number of bits used to represent the Unix dictionary is reduced to 16 bits. Improvement is still possible: NIL-pointers may be represented as half a byte, one byte or two bytes long fields, (of the form 0xxx, 10xxxxxx, 11xxxxxxxxxxxxxx); this representation would require only 14 bits per key for the Unix dictionary, 3 bits per key for sequential data and 4 bits per key for random data.

Performances of bit-string handling are not optimal and experimental results provide better performances with 50-entries CB-nodes than with 100-entries CB-nodes (this could also be an effect of the locally sequential algorithm); this suggests that the number of entries in a CB-node is a parameter to be chosen carefully; programming the bit-string handling in assembly language would certainly improve the performances; suggestions are also made in [3] for improving the bit-handling.

5.2 Comparison of the Compact-Balanced Trie and of the Compact 0-complete Trees

The Compact 0-complete Tree [12] uses a 4-byte structure per key, one byte being the current bounding node depth and the 3 next bytes being data or NIL-pointer.

Orlandic and Pfaltz have done asymptotic analysis of the Compact 0-complete Tree [13]; the average storage utilization is 57%; as we pointed out in chapter 2, there is no possibility of improving this storage utilization by progressive merging of nodes.

In contrast, our experimental results exhibit an average of 5 bytes per key (bit-map, NIL-pointer, data-pointer), but B -tree like flexibility allows by a progressive scanning of the index to force a 100% filling rate, for any key-distribution.

Therefore, a 1000 byte Node would contain an average of 150 entries in the case of the Compact 0-complete Trees and about 200 entries in case of the Compact-Balanced Tries (after forcing a 100% filling rate).

The difference would be bigger with heavier structures.

Moreover, like in B -tree case, a 50% storage utilization is guaranteed for any Node of a Compact-Balanced Trie.

The Compact 0-complete Tree has the advantage in terms of algorithm simplicity and of implementation ease, while the Compact-Balanced Trie has the advantage in terms of storage utilization and of worst cases handling.

6 Conclusions

The Compact-Balanced Tries require between one and two bytes to represent a key; in contrast to this excellent compaction result, the relative moderate performance of the bit-map handling and the relative complexity of the algorithm are slight drawbacks.

The B -tree type structure of the Compact-Balanced Trie allows partial locking of the structure and multi-user parallel processing; for this reason, Compact-Balanced Tries could be of efficient usage in a parallel machine like Bubba [2].

Balanced Compact Tries offer compactness and all the B -tree properties; they are therefore a secure choice for implementation of memory databases.

Balanced Compact Tries can also manage clustering ordered indexes without any special difficulty.

The worst case of insertion corresponds to pairs of keys having their N first bits in common; in this case, the number of NIL-leaves is about N , and the number of bits used to represent these keys is about $2N$ (in the bit-map representation); therefore, if N is large, and if there is a

large number of such pairs of key, a Patricia-tree like method [7] would locally be more space-saving than the bit-map representation. This worst case would require about the same amount of memory in a Compact-Balanced Trie as in a classical B -tree.

When coping with random key distributions, and remarking that the bit-map representation is a minimal representation for a trie, it is not unreasonable to think that the indexing method we propose approaches a theoretical optimum in terms of compactness.

We proved that the linear representation of tries can be segmented and handled with a complete flexibility; this important novelty allows us to step down from global linearity of the algorithms to local linearity and insures that worst cases of insertions are handled as well as a B -tree could do; these flexibility and compactness results improve the best results obtained at the moment for such indexes.

The research presented in this paper could be extended in different ways: it is not easy to conjecture if a compact representation may be found for multidimensional data; however, as it has been done with B -trees, a Compact Balanced Trie may be used for each dimension of such data; it would be interesting to see if an extension of B -trees to multidimensional case, as done with *KB-Trees* [6] could be applied to Compact Balanced Tries; the comparison with *grid files*, as done by Kriegel [9], or with *BANG files* [5], would then be an interesting subject.

Another field of research would be the probabilistic analysis of the NIL-pointers, in both cases of random keys and of alphanumeric keys; results in this direction would allow a further tuning of the structure.

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A Skip-edge-subtrie algorithm

```

struct node {

    int ed;                /* edge-depth
    int nbbit              /* current number of bit of the bit-map
    int nbpointer;         /* current number of pointers of the pointers-list

    int    bit-map [BMAPSIZE];
    int    pointer [PTRSSIZE]; /* first character is NIL-pointers
                                /* next 3 characters are DATA-pointers

};
int bx;                  /* bit-map index
int px;                  /* pointer index

```

```

skipestrie (differ)          /*          JUMP EDGE SUBTRIE

int differ;                  /* position of the first bit differing
                             /* between the retrieval-key and the edge-k
{

    struct node *n = &currentnode;

    char          *edgekey = n->pointer[0];

    int  interior;          /* number of interior nodes (shadows include
    int  leaf;              /* number of leaf      nodes (shadows include

    int  eb = differ;       /* (key) edge bit position-number

    bx = px = 0;

    /* HANDLING OF THE SHADOW NODES */

    for ( interior=0, leaf=0; eb < n->ed; eb++, interior++ )
        if ( bit( edgekey, eb ) == 1 ) leaf++;
    if ( bit( edgekey, n->ed ) == 1 ) leaf++;

    /* HANDLING OF NODES ALONG THE BIT-MAP CONTENT */

    do {
        if ( bx == n->nbbit-1 || bit( n->bitmap, bx+1) == 1 )
            { leaf++; px++; }
        else interior++;
    }
    while( leaf < interior + 1 );
}

bit( adr, posi )             /*          BIT VALUE          */

                             /* return the value of the bit at position */
                             /* "posi", first bit being highest bit of */
                             /* address "adr"                          */

```

B Experimental results

Experimentals Results on the Unix Words Dictionary

Number of words inserted	= 24259
Average size of the words	= 7 bytes = 56 bits
Bit-map size	= 249719 bits
Number of non-zero NIL-pointers	= 14796
Average number of bits used for a word	= 10 + 8 (NIL-pointer-size) = 18
Number maximum of entries per node	= 100
Number of NIL-leaves	= 101125

Distribution of NIL-sequence :

(a NIL-sequence is a number of consecutive -- in sense of pre-order traversal -- NIL-leaves, represented in the NIL-pointers; NIL-sequence[11] stands for a sequence of 11 consecutive NIL-pointers)

NIL-sequence[1] = 2303	NIL-sequence[25] = 64
NIL-sequence[2] = 1779	NIL-sequence[26] = 53
NIL-sequence[3] = 1557	NIL-sequence[27] = 39
NIL-sequence[4] = 1206	NIL-sequence[28] = 45
NIL-sequence[5] = 1045	NIL-sequence[29] = 26
NIL-sequence[6] = 963	NIL-sequence[30] = 17
NIL-sequence[7] = 761	NIL-sequence[31] = 22
NIL-sequence[8] = 692	NIL-sequence[32] = 17
NIL-sequence[9] = 551	NIL-sequence[33] = 19
NIL-sequence[10] = 535	NIL-sequence[34] = 8
NIL-sequence[11] = 454	NIL-sequence[35] = 9
NIL-sequence[12] = 371	NIL-sequence[36] = 4
NIL-sequence[13] = 342	NIL-sequence[37] = 7
NIL-sequence[14] = 318	NIL-sequence[38] = 3
NIL-sequence[15] = 277	NIL-sequence[39] = 4
NIL-sequence[16] = 190	NIL-sequence[40] = 2
NIL-sequence[17] = 178	NIL-sequence[41] = 1
NIL-sequence[18] = 151	NIL-sequence[42] = 2
NIL-sequence[19] = 138	NIL-sequence[44] = 2
NIL-sequence[20] = 127	NIL-sequence[46] = 2
NIL-sequence[21] = 106	NIL-sequence[47] = 2
NIL-sequence[22] = 87	NIL-sequence[48] = 1
NIL-sequence[23] = 63	NIL-sequence[52] = 1

NIL-sequence[24] = 52

NIL-sequence[65] = 1