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An Evolutionary Approach for the Motion Planning of Redundant and Hyper-redundant Manipulators

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Abstract

The trajectory planning of redundant robots is an important area of research and efficient optimization algorithms are needed. The pseudoinverse control is not repeatable, causing drift in joint space which is undesirable for physical control. This paper presents a new technique that combines the closed-loop pseudoinverse method with genetic algorithms, leading to an optimization criterion for repeatable control of redundant manipulators, and avoiding the joint angle drift problem. Computer simulations performed based on redundant and hyper-redundant planar manipulators show that, when the end-effector traces a closed path in the workspace, the robot returns to its initial configuration. The solution is repeatable for a workspace with and without obstacles in the sense that, after executing several cycles, the initial and final states of the manipulator are very close.

Keywords: Redundant Manipulators, Hyper-redundant Manipulators, Robots, Kinematics, Genetic Algorithms, Trajectory Planning.

1. Introduction

Kinematic redundancy occurs when a manipulator possesses more degrees of freedom than the required to execute a given task. In this case the inverse kinematics admits an infinite number of solutions, and a criterion to select one of them is required. Most of the research on redundancy deals with the use of these extra degrees of freedom and is referred to in the literature as the resolution of redundancy [1].

Many techniques for solving the kinematics of redundant manipulators that have been suggested control the end-effector indirectly, through the rates at which the joints are driven, using the pseudoinverse of the Jacobian (see, for instance, [2]). The pseudoinverse of the Jacobian matrix guarantees an optimal reconstruction of the desired end-effector velocity – in the least-squares sense – with the minimum-norm joint velocity. However, even though the joint velocities are instantaneously minimized, there is no guarantee that the kinematic singularities are avoided [3]. Moreover, this method has the generally undesirable property that repetitive end-effector motions do not necessarily yield repetitive joint motions. Klein and Huang [4] were the first to observe this phenomenon for the case of

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the pseudoinverse control of a planar three-link manipulator. A large volume of research has been produced in the last few years in this topic [5-8]. For example, Zhang *et al.* [9] solve the joint angle drift problem by means of a dual-neural-network based quadratic-programming approach.

Baillieul [10] proposed a modified Jacobian matrix called the extended jacobian matrix. The extended jacobian is a square matrix that contains the additional information necessary to optimize a certain function. The inverse kinematic solutions are obtained through the inverse of the extended jacobian. The algorithms, based on the computation of the extended jacobian matrix, have a major advantage over the pseudoinverse techniques, because they are locally cyclic [11]. The disadvantage of this approach is that, while mechanical singularities may be avoided, typical algorithmic singularities [12] arise from the way the constraint restricts the motion of the mechanism [13].

One optimization method that is gaining popularity for solving complex problems in robotics is the Genetic Algorithm (GA). GAs are population-based stochastic and global search methods. Their performance is superior to that revealed by classical optimization techniques [14] and has been used successfully in robot path planning.

Parker et al. [15] used GAs to position the end-effector of a robot at a target location, while minimizing the largest joint displacement. This method has some shortcomings, such as the lack of precision and is affected by the values of the weights. Arakawa et al. [16] proposed a virus-evolutionary genetic algorithm, composed of a host population and a virus population with subpopulations, for the trajectory generation of redundant manipulators without collision, that optimize the total energy. The operators of crossover, mutation, virus infection and selection are executed in each subpopulation independently. Kubota et al. [17] studied a hierarchical trajectory planning method for a redundant manipulator using a virus-evolutionary GA. This method runs, simultaneously, two processes. One process calculates some manipulator collision-free positions and the other generates a collision-free trajectory by combining these intermediate positions. De la Cueva and Ramos [18] proposed a GA for planning paths without collisions for two robots, both redundant and non-redundant, sharing the same workspace. The GA works directly over the task space adopting the direct kinematics. Each robot is associated to one population and each string of a population represents a complete robot path. Nishimura et al. [19] proposed a motion planning method using an artificial potential field and a GA for a hyperredundant manipulator whose workspace includes several obstacles. The motion planning is divided into two sub problems. The first is the "Path planning" that generates a trajectory leading the tip of manipulator to the goal without collisions, using the artificial potential field concept. The second consists in the "Collision-free sequence generation" that generates a sequence of movements by which distinct parts of the manipulator can avoid collisions with the obstacles. McAvoy and Sangolola [20] proposed an approach with GAs for optimal point-to-point motion planning of kinematically redundant manipulators. Their approach combines B-spline curves, for the generation of smooth trajectories, with Gas, for obtaining the optimal solution. Peng and Wei [21] presented the ASAGA trajectory planning method of redundant manipulators by combining a stochastic search algorithm (simulated annealing algorithm) and a GA. In the ASAGA the selection, crossover and mutation operators are adjusted by using an adaptive mechanism based on the fitness value. Zhang et al. [22] proposed an algorithm to solve the inverse kinematics of a flexible macro-micro manipulator system which combines a GA and a neural network. Pires et al. [23] proposed a multi-objective genetic algorithm, when considering up to five simultaneous objectives, to generate manipulator trajectories and for obstacle avoidance.

Having these ideas in mind, the paper is organized as follows. Section 2 introduces the fundamentals of the kinematics of redundant manipulators. Based on these concepts, section 3 presents the new closed-loop inverse kinematics algorithm with genetic algorithms (CLGA) and the open-loop genetic algorithm (OLGA). Section 4 presents the simulation results in a workspace without and with obstacles. For

comparison purposes some results for the closed-loop pseudoinverse (CLP) method are also presented. Finally, section 5 draws the main conclusions.

2. Kinematics and dynamics of redundant manipulators

We consider a manipulator with *n* degrees of freedom whose joint variables are denoted by $\mathbf{q} = [q_1, q_2, ..., q_n]^T$. We assume that the class of tasks we are interested in can be described by *m* variables, $\mathbf{x} = [x_1, x_2, ..., x_m]^T$, m < n, and that the relation between \mathbf{q} and \mathbf{x} is given by the direct kinematics:

$$\mathbf{x} = f(\mathbf{q}) \tag{1}$$

Differential kinematics of robot manipulators was introduced by Whitney [24] that proposed the use of differential relationships to solve for the joint motion from the Cartesian trajectory of the end-effector. Differentiating (1) with respect to time yields:

$$\dot{\mathbf{x}} = \mathbf{J}(\mathbf{q})\dot{\mathbf{q}} \tag{2}$$

where $\dot{\mathbf{x}} \in \mathbb{R}^m$, $\dot{\mathbf{q}} \in \mathbb{R}^n$ and $\mathbf{J}(\mathbf{q}) = \partial f(\mathbf{q}) / \partial \mathbf{q} \in \mathbb{R}^{m \times n}$. Hence, it is possible to calculate a path $\mathbf{q}(t)$ in terms of a prescribed trajectory $\mathbf{x}(t)$ in the operational space.

Equation (2) can be inverted to provide a solution in terms of the joint velocities:

$$\dot{\mathbf{q}} = \mathbf{J}^{\#}(\mathbf{q})\dot{\mathbf{x}}$$
(3)

where $\mathbf{J}^{\#}$ is the Moore-Penrose generalized inverse of the Jacobian \mathbf{J} [2, 25].

3. Robot trajectory control

The Jacobian of a *n*-link planar manipulator (i.e., m = 2) has a simple recursive nature according with the expressions:

$$\mathbf{J} = \begin{bmatrix} -l_1 S_1 - \dots - l_n S_{1\dots n} & \cdots & -l_n S_{1\dots n} \\ l_1 C_1 + \dots + l_n C_{1\dots n} & \cdots & l_n C_{1\dots n} \end{bmatrix}$$
(4)

where l_i is the length of link i, $q_{i...k} = q_i + ... + q_k$, $S_{i...k} = Sin(q_{i...k})$ and $C_{i...k} = Cos(q_{i...k})$, $i, k \in \mathbb{N}$.

In the closed-loop pseudoinverse (CLP) method the joint positions can be computed through the time integration of the expression:

$$\Delta \mathbf{q} = \mathbf{J}^{\#} \left(\mathbf{q} \right) \Delta \mathbf{x} \tag{5}$$

3

where $\Delta \mathbf{x} = \mathbf{x}_{ref} - \mathbf{x}$ and \mathbf{x}_{ref} is the vector of reference position in the operational space. Nevertheless, in a previous study, addressing the CLP method [26], it was concluded that this method leads to unpredictable, not repeatable, arm configurations and reveals properties resembling those that occur in chaotic systems.

Genetic algorithms (GAs) are a method for solving both constrained and unconstrained optimization problems, based on the mechanics of natural genetics and selection, that was first introduced by Holland [27]. A GA allows a population composed of many individuals to evolve under specified selection rules to a state that maximizes the fitness or the cost function. The GA modifies repeatedly the population of individuals (possible solutions). At each step, the genetic algorithm selects individuals at random, from the current population, to be parents, and uses them to produce the offspring for the next generation. Over successive generations, the population evolves towards an optimal solution. The GAs can be applied to solve a variety of optimization problems that are not well suited for standard optimization algorithms, including problems in which the objective function is discontinuous, not differentiable, stochastic, or highly nonlinear.

Bearing these facts in mind, in this paper we propose a new method that combines the CLP with a GA, namely the closed-loop inverse kinematics algorithm with genetic algorithms (CLGA).

In order to find an initial joint configuration of the manipulator is used another GA, adopting the direct kinematics, which is denoted as OLGA.

In both cases the optimal configuration is the one that minimizes the fitness function according to some specified criteria.

3.1 The CLGA formulation

The CLGA adopts the closed-loop structure without requiring the calculation of the pseudoinverse. The CLGA uses an extended Jacobian matrix, $\mathbf{J}^* \in \mathbb{R}^{n \times n}$, and an extended vector, $\Delta \mathbf{x}^* \in \mathbb{R}^n$, as a way to limit the joint configurations for a given end-effector position.

The definition of \mathbf{J}^* and $\Delta \mathbf{x}^*$ take the form:

$$\mathbf{J}^{*} = \begin{bmatrix} -l_{1}S_{1} - \dots - l_{n}S_{1\dots n} & \cdots & -l_{n}S_{1\dots n} \\ \underline{l_{1}C_{1} + \dots + l_{n}C_{1\dots n}} & \cdots & \underline{l_{n}C_{1\dots n}} \\ j_{(m+1)1} & \cdots & j_{(m+1)n} \\ \dots & \dots & \dots \\ j_{n1} & \cdots & j_{nn} \end{bmatrix} \qquad \Delta \mathbf{x}^{*} = \begin{bmatrix} \Delta x_{1} \\ \underline{\Delta x_{2}} \\ \overline{\Delta x_{m+1}} \\ \vdots \\ \Delta x_{n} \end{bmatrix}$$
(6)

where the matrix elements j_{ik} and Δx_i , i = m+1,...,n and k = 1,...,n, are values generated by the GA, satisfying the additional imposed constraints.

3.1.1 Representation and operators in the CLGA

An initial population of strings, with dimension $n_P = N$, is constructed at random and the search is then carried out among this population. Each chromosome (string) is implemented by a matrix of $n_V = (n-m) \times (n+1)$ values (genes), with j_{dk} and Δx_d , d = 1, ..., n-m, k = 1, ..., n, consisting in floating-point numbers initialized in the range $[var_{min}, var_{max}]$. For the generation T, the ith chromosome of the population is represented as:

$$\left[\mathbf{J}^{(T,i)} \vdots \Delta \mathbf{x}^{(T,i)}\right]$$
(7)

where $\mathbf{J}^{(T,i)} = \left[j_{dk}^{(T,i)} \right] \in \mathbb{R}^{(n-m) \times n}$ and $\Delta \mathbf{x}^{(T,i)} = \left[\Delta x_d^{(T,i)} \right] \in \mathbb{R}^{n-m}$.

The three different operators used in the genetic algorithm are reproduction, crossover and mutation. In what respecting the reproduction operator, the successive generations of new strings are generated on the basis of their fitness function. In this case, it is used a rank weighting to select the strings from the old to the new population. For the crossover operator, the strings are randomly grouped together into pairs and a crossover point is randomly selected for each one of the n-m lines of the parent. Then crossover is performed among pairs. Finally, for the mutation operator, one variable value from the n_V values of the chromosome is replaced with a new random one.

The CLGA procedure is shown in figure 1, where \mathbf{x}_{ref} is the vector of reference position in the operational space and \mathbf{x}_{ini} is a vector representing the position of the end-effecter in the operational space.

1	Begin
2	T = 0
3	calculate $\Delta \mathbf{x} = \mathbf{x}_{ref} - \mathbf{x}_{ini}$, J
4	initialize random population $P(T) = \left[\begin{bmatrix} \mathbf{J}^{(T,1)} \\ \vdots \\ \Delta \mathbf{x}^{(T,1)} \end{bmatrix}, \dots, \begin{bmatrix} \mathbf{J}^{(T,N)} \\ \vdots \\ \Delta \mathbf{x}^{(T,N)} \end{bmatrix} \right]$
5	get $\Delta \mathbf{q} = \mathbf{J}^{*-1}(\mathbf{q})\Delta \mathbf{x}^*$ and $\mathbf{q} = \int \Delta \mathbf{q}$
6	evaluate $P(T)$
7	repeat
8	selection parents from $P(T)$
9	crossover $P(T)$
10	mutation $P(T)$
11	form new generation $P(T)$
12	get $\Delta \mathbf{q} = \mathbf{J}^{*-1}(\mathbf{q})\Delta \mathbf{x}^*$ and $\mathbf{q} = \int \Delta \mathbf{q}$
13	evaluate $P(T)$
14	T = T + 1
15	until termination condition is TRUE
16	get new q
17	End

Fig. 1. Procedure for the CLGA.

3.1.2 Optimization criteria

The fitness function minimizes the joint displacement between the current joint position and the initial joint position, through the following function:

$$f_1 = A\dot{\mathbf{q}}^T\dot{\mathbf{q}} + B\left(\frac{\mathbf{q} - \mathbf{q}_0}{\Delta t}\right)^T \left(\frac{\mathbf{q} - \mathbf{q}_0}{\Delta t}\right)$$
(8)

where $A, B \in \mathbb{R}^+$ denotes weighting factors, \mathbf{q}_0 and \mathbf{q} represents the initial and current joint configurations, respectively, and Δt is a step time increment.

3.2 The OLGA formulation

The OLGA trajectory planning adopts a simple open-loop structure, as we can see in figure 2. An initial population of strings, with dimension $n_P = N$, is constructed at random and the search is then carried out among this population. Each chromosome is defined through an array of $n_V = n$ values, q_i , i = 1, ..., n, represented as floating-point numbers initialized in the range $[q_{\min}, q_{\max}]$. For the generation T, the ith chromosome of the population is represented as:

$$\mathbf{q}^{(T,i)} = \left(q_1^{(T,i)}, \ \dots, q_n^{(T,i)}\right)$$
(9)

The end-effector position, $\mathbf{x}^{(T,i)}$, for each configuration, $\mathbf{q}^{(T,i)}$, is easily calculated using the direct kinematics.

3.2.1 Optimization criteria

The evaluation function is defined based on the positional error of the end-effector:

$$P_{error} = \sqrt{\left(x_{c} - x_{f}\right)^{2} + \left(y_{c} - y_{f}\right)^{2}}$$
(10)

where $\mathbf{x}_c = (x_c, y_c)$ and $\mathbf{x}_f = (x_f, y_f)$ are vectors representing the end-effector current position and the desired final position, respectively. Therefore, the algorithm minimizes the function $f_2 = P_{error}$. 1 Begin 2 T = 0initialize random population $P(T) = \begin{bmatrix} q^{(T,1)}, q^{(T,2)}, \dots, q^{(T,N)} \end{bmatrix}$ 3 get $\mathbf{X} = \left[\mathbf{x}^{(T,1)}, \dots, \mathbf{x}^{(T,N)} \right]$ using direct kinematics 4 evaluate P(T)5 Repeat 6 selection parents from P(T)7 crossover P(T)8 mutation P(T)9 form new generation P(T)10 get X using direct kinematics 11 evaluate P(T)12 T = T + 113 14 until termination condition is TRUE get new q 15 16 End

Fig. 2. Procedure for the OLGA.

4. Simulation results

In this section we start by analyzing the performance of the CLGA for a free workspace and then we study the effect of including several types of obstacles in the working environment.

Without lacking of generality, in the following experiments are adopted arms having identical link lengths, $l_1 = l_2 = ... = l_n$.

The experiments consist in the analysis of the kinematic performance of a planar manipulator with $n = \{3, 4, 5, 6, 7\}$ rotational joints, denoted as *nR*-robot, that is required to repeat a circular motion in the operational space with frequency $\omega_0 = 7.0 \text{ rad sec}^{-1}$, center at $r = (x_1^2 + x_2^2)^{1/2}$, radius $\rho = 0.5$ and a step time increment of $\Delta t = 10^{-3}$ sec. The goal here is to position the end-effector of the *nR*-robot at a target location while minimizing the joint angle drift using the fitness function f_1 with A = B = 1.

The initial joint configuration is obtained using the OLGA with the fitness function f_2 .

The average of the positional error for n_C cycles is given by the expression:

$$\overline{P}_{error} = \frac{\sum_{i=1}^{k} P_{error}}{k}$$
(11)

where k is the number of sampling points and is defined as:

$$k = \frac{2\pi}{\omega_0 \Delta t} n_C \tag{12}$$

The average of the total joint displacement for the *nR*-robot is given by the expression:

$$\overline{\Delta \mathbf{q}} = \frac{\left\| \Delta \mathbf{q} \right\|}{n} \tag{13}$$

where $\Delta \mathbf{q} = \mathbf{q}_f - \mathbf{q}_0$, is the vector of the joint displacement between the final, \mathbf{q}_f , and the initial, \mathbf{q}_0 , joint configurations, and $\|\cdot\|$ represents the Euclidean norm.

The CLGA algorithm adopts crossover probabilities of $p_c = 0.5$ for $n = \{3, 4, 5, 6, 7\}$ and mutation probabilities of $p_m = 0.5$ and $p_m = 0.3$ for $n = \{3, 4\}$ and $n = \{5, 6, 7\}$, respectively. The string population is $n_P = \{200, 400, 800, 1200, 1600\}$ for $n = \{3, 4, 5, 6, 7\}$, respectively, and the results are obtained for $n_G = 200$ consecutive generations. Each variable value is initialized in the range [-1, 1].

The OLGA algorithm adopts crossover and mutation probabilities of $p_c = 0.5$ and $p_m = 0.5$, respectively, a string population of $n_P = 1600$ and the results are obtained for $n_G = 200$ consecutive generations. Each variable value is initialized in the range $[-2\pi, 2\pi]$.

4.2.1 The CLGA performance in a workspace without obstacles

The average of the positional error, \overline{P}_{error} , for $n = \{3, 4, 5, 6, 7\}$ rotational joints, $n_C = 50$ cycles and radial distance $r = \{0.7, 1.0, 2.0\}$, is depicted in figure 3.

We observe that:

- i) the CLGA gives good precision in the task of positioning the end-effector at the target position;
- ii) in general, we get better results for the radial distance r = 2.0 and worse results for the radial distance r = 0.7;
- iii) in general, the positional error gets worse when the number of joints increases.



Fig. 3. \overline{P}_{error} of the *nR*-robot during $n_c = 50$ cycles for $n = \{3, 4, 5, 6, 7\}$ and $r = \{0.7, 1.0, 2.0\}$.

Figures 4-5 show successive robot configurations, for $n = \{3, 7\}$ rotational joints and r = 2.0, during the 1st and 50th cycles, respectively. As we can see, the joint configurations are very similar, for both cycles, revealing that the joint positions are repetitive. For comparison purposes, figures 6-7 show successive robot configurations, for $n = \{3, 7\}$ rotational joints and r = 2.0, during the 1st and 50th cycles, respectively, for the CLP method. As we can see, the joint configurations are very different revealing that the joint positions are not repetitive.



Fig. 4. CLGA successive robot configurations of the 3*R*-robot for the 1st and 50th cycles, respectively, and r = 2.0.



Fig. 5.CLGA successive robot configurations of the 7*R*-robot for the 1st and 50th cycles, respectively, and r = 2.0.



Fig. 6. CLP successive robot configurations of the 3*R*-robot for the 1st and 50th cycles, respectively, and r = 2.0.



Fig. 7. CLP successive robot configurations of the 7*R*-robot for the 1^{st} and 50^{th} cycles, respectively, and r = 2.0.

In order to evaluate the joint angle drift after executing $n_c = 50$ cycles, table 1 shows the average of the total joint displacement, $\overline{\Delta q}$, when $n = \{3, 4, 5, 6, 7\}$ and $r = \{0.7, 1.0, 2.0\}$, for the CLGA and the CLP methods. We verify that for the CLGA we get some drift in joint positions, but the values are very similar for all the manipulators and for all of the radial distances. For the CLP we get an high drift in the joint positions revealing that this method leads to unpredictable arm configurations.

CLGA	<i>r</i> = 0.7	<i>r</i> = 1.0	r = 2.0		
3 <i>R</i>	9.96E-04	8.84E-04	1.08E-03		
4 <i>R</i>	7.12E-04	7.38E-04	5.70E-04		
5 <i>R</i>	6.73E-04	5.42E-04	6.15E-04		
6 <i>R</i>	5.98E-04	4.81E-04	8.57E-04		
7 <i>R</i>	1.26E-03	5.44E-04	5.39E-04		

CLP	P $r = 0.7$ $r = 1.0$		<i>r</i> = 2.0		
3 <i>R</i>	1.35E+01	6.41E+00	5.80E-01		
4 <i>R</i>	8.2E+00	4.4E+00	5.8E-01		
5 <i>R</i>	7.2E+00	2.2E+00	4.4E-01		
6 <i>R</i>	5.4E+00	4.9E+00	3.0E-01		
7 <i>R</i>	4.2E+00	2.4E+00	2.0E-01		

Table 1. CLGA and CLP average of the total joint displacement, $\Delta \mathbf{q}$, of the *nR*-robot, $r = \{0.7, 1.0, 2.0\}$ and after $n_C = 50$ cycles.

Figure 8-9 shows the joint positions and the Fourier transform of the robot joint velocities for the 1st joint and $n_c = 50$, $n = \{3, 7\}$ and $r = \{0.7, 2.0\}$, with the CLGA and the CLP methods. For the other joints the results are similar to those of the 1st joint.



Fig. 8. The {3, 7} *R*-robot 1st joint positions *versus* time and $\left|F\left\{\dot{q}_1(t)\right\}\right|$ vs ω/ω_0 during $n_c = 50$ cycles for r = 0.7 and (a) CLGA (b) CLP.

For the CLGA, we conclude that:

- i) repetitive trajectories in the operational space lead to periodic trajectories in the joint space;
- ii) the initial and final joint positions, for each of the cycles, are very close;
- iii) the signal energy is concentrated essentially in the fundamental and multiple higher harmonics.

For the CLP, we conclude that the results depend on the circle being executed. Besides the position drifts, occur unpredictable motions with severe variations that lead to high joint transients. Moreover, for r = 0.7 we verify that a large part of the energy is distributed along several sub-harmonics, revealing properties similar to those that occur in chaotic systems.

We verify that the CLGA has a good performance in repetitive motion tasks because we get not only a good positioning but also a repetitive behavior.



Fig. 9. The {3, 7} *R*-robot 1st joint positions *versus* time and $\left|F\left\{\dot{q}_1(t)\right\}\right|$ vs ω/ω_0 during $n_c = 50$ cycles for r = 2.0 and (a) CLGA (b) CLP.

4.2.2 The CLGA performance in a workspace with obstacles

This section presents the results of several simulations, when considering two obstacles in the workspace. At the end of the section, are presented some examples in a workspace with three obstacles. When, for a given joint configuration, some part of the manipulator is inside an obstacle, the CLGA simply rejects the configuration and generates a new population element.

4.2.2.1 The CLGA performance in a workspace with two obstacles

In the experiments, the position of the obstacles in the workspace depends on the radial distance. In figures 10-12 are represented the positions of the obstacles in the workspace for each radial distance, O(r; i), for $r = \{0.7, 1.0, 2.0\}$ and i = 1, 2, 3.



The average of the positional error, \overline{P}_{error} , for $n = \{3, 4, 5, 6, 7\}$, $n_c = 50$ cycles and O(r; i) for $r = \{0.7, 1.0, 2.0\}$, i = 1, 2, 3, is presented in figures 13-15, respectively.

We observe that:

- i) the CLGA gives good precision in the task of positioning the end-effector at the target position, while avoiding the obstacles in the workspace;
- ii) in general, we get better results for the radial distance r = 2.0 and worse results for r = 0.7;
- iii) in general, the positional error, \overline{P}_{error} , gets worse when the number of joints increases.



Fig. 13. \overline{P}_{error} of the *nR*-robot during $n_C = 50$ cycles for O(0.7; i), i = 1, 2, 3.



Fig. 14. \overline{P}_{error} of the *nR*-robot during $n_C = 50$ cycles for O(1.0; i), i = 1, 2, 3.



Figures 16-17 show successive robot configurations, for $n = \{3, 7\}$ and O(2.0; i), i = 1, 2, 3, during the 1st and 50th cycles, respectively, revealing that the motion is repetitive.



Fig. 16. Successive robot configurations of the 3R-robot for the 1st and 50th cycles, respectively, and O(2.0; i), i = 1, 2, 3.



Fig. 17. Successive robot configurations of the 7*R*-robot for the 1st and 50th cycles, respectively, and O(2.0; i), i = 1, 2, 3.

Table 2 shows the average of the joint displacement, $\overline{\Delta \mathbf{q}}$, for $n = \{3, 4, 5, 6, 7\}$, and O(r; i), $r = \{0.7, 1.0, 2.0\}$, i = 1, 2, 3. We conclude that the results are consistent with those we obtained in a workspace without obstacles.

	O (0.7; 1)	O (0.7; 2)	O (0.7; 3)	O (1.0; 1)	O (1.0; 2)	O (1.0; 3)	O (2.0; 1)	O (2.0; 2)	O (2.0; 3)
3 <i>R</i>	8.63E-04	1.11E-03	1.02E-03	7.57E-04	7.63E-04	8.02E-04	6.15E-04	6.64E-04	6.51E-04
4R	6.16E-04	6.86E-04	5.98E-04	6.07E-04	7.39E-04	6.85E-04	4.29E-04	4.19E-04	4.22E-04
5R	7.31E-04	7.04E-04	5.40E-04	5.63E-04	4.63E-04	4.74E-04	3.56E-04	4.16E-04	7.14E-04
6 <i>R</i>	4.66E-04	6.28E-04	5.92E-04	4.67E-04	3.45E-04	6.23E-04	2.38E-04	2.96E-04	7.33E-04
7R	5.16E-04	3.75E-04	3.95E-04	4.63E-04	5.39E-04	2.95E-04	7.07E-04	3.94E-04	1.96E-03

Table 2. The average of the joint displacement of the *nR*-robot, $\overline{\Delta \mathbf{q}}$, after $n_c = 50$ cycles for $O(r; \mathbf{i})$, $r = \{0.7, 1.0, 2.0\}$, i = 1, 2, 3.

Figures 18-20 show the joint positions and the Fourier transform of the robot joint velocities for the 1st joint and $n_c = 50$ cycles, $n = \{3, 7\}$, O(2.0; i), i = 1, 2, 3. For the others joints the results are similar to the verified ones for the 1st joint.

We conclude that:

- i) repetitive trajectories in the operational space lead to periodic trajectories in the joint space;
- ii) the initial and final joint positions for each one of the cycles are very close;
- iii) the signal energy is concentrated essentially in the fundamental and multiple higher harmonics.

We observe also that the results are consistent with those of the previous section and that the presence of obstacles does not present an additional complexity for the CLGA to reach a repetitive solution.



Fig. 18. The {3, 7} *R*-robot 1st joint positions *versus* time and $|F\{\dot{q}_1(t)\}|$ vs ω/ω_0 during $n_c = 50$ cycles for O(2.0; 1).

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4.2.2.2 The CLGA performance in a workspace with three obstacles

One of the problems that occurs when we use the repeatability criterion is that, if the initial joint configuration of the manipulator is not well adjusted for the task, then will occur 'jumps' of the robot structure to prevent the collision with the obstacles. In the experiments the trajectory is repetitive and, therefore, these jumps may occur during several cycles.

In figures 21-22 we use a workspace with three obstacles. For n = 3, after two different executions of the algorithm, we obtained two different initial joint configurations with distinct consequences, in terms of the positional error and performance in the execution of the task. However, if we use a manipulator with n = 7 rotational joints there is no problem to find a good solution for the initial positions. Anyway, the manipulator motion is always repeatable and the drift in the joint positions is similar to the one we obtained in the previous experiments.



Fig. 21. Successive robot configurations of the 3R-robot for the 1^{st} and 2^{nd} cycles, respectively, for a workspace with three obstacles and r = 2.0, with two different initial joint configurations.



Fig. 22. Successive robot configurations of the 7*R*-robot for the 1^{st} and 2^{nd} cycles, respectively, for a workspace with three obstacles and r = 2.0.

5. Conclusions

A CLGA algorithm that combines the CLP with a GA scheme was presented. Several experiments were developed to study the performance of the CLGA when the manipulator is required to repeat a

circular motion in the operational space, while satisfying an optimization criterion, in a workspace without and with obstacles.

The results show that the CLGA gives good results in the perspective of the positional error and the repeatability of the joint positions. In what concerns the drift in the joint angles, there is no zero-drift but the results seem to be acceptable for all manipulators under analysis.

It is shown that the presence of obstacles does not present an additional complexity for the CLGA. However, the initial configuration of the manipulator plays an important role in the performance of the manipulator in a workspace with obstacles. In fact, if the initial configuration is not adjusted adequately for the required task, then jumps may occur in the joint positions to prevent the collision with the obstacles.

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