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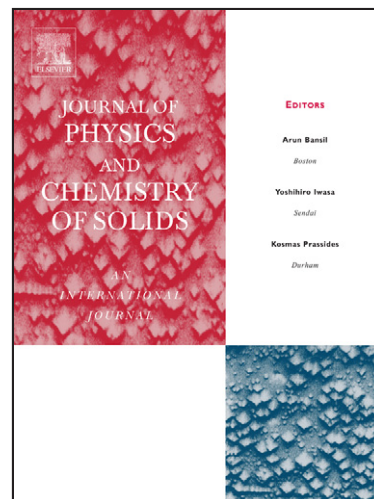
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The effect of silicon impurities on the phase diagram of iron and possible implications for the Earth's core structure

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Abstract

The hexagonal close-packed structure (hcp) is the accepted stable form of pure iron (Fe) under Earth's core conditions. Recently, however, a body-centred-cubic (bcc) phase of iron alloyed with lighter elements has been proposed. At relatively modest conditions, experiments have shown that small amounts of silicon (Si) can stabilise the bcc phase with respect to the hcp phase. This result has motivated our present study examining the effect of silicon on the bcc-hcp phase transition. We have performed *ab initio* calculations on both phases at zero Kelvin; our results are in good agreement with experiment.

Extending our results to core pressures and taking into account previous studies of pure iron at core temperatures, we conclude that the bcc phase of iron alloyed with silicon is likely to be the stable crystalline phase in the inner core.

Keywords: silicon; iron; ab initio; inner core; light elements

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1. Introduction

The Earth's inner core consists largely of iron. Density measurements suggest also the presence of other low atomic weight elements [1]. Quantifying those light elements and determining their role, however, remains a matter of controversy as present experiments cannot simultaneously reproduce the high pressure and temperature conditions of the core. Under ambient conditions, the iron crystal has a body-centred-cubic (bcc) structure. At pressures above ~ 15 GPa, (at room temperature), it adopts a hexagonal-close-packed (hcp) structure which persists to inner-core pressures. Temperature, however, has been shown to act in the opposite sense to pressure. For instance, Vočadlo et al. [5] used ab initio molecular dynamics (MD) simulations under inner-core pressures and temperatures to show that, while the hcp structure is still marginally more stable, the difference in free energy between the hcp and bcc phases becomes very small. Classical potential MD simulations of Belonoshko et al [6] show an even more pronounced effect of temperature and predict that the bcc phase of Fe actually becomes more stable than the hcp structure in the inner-core. Regardless of which is correct, it appears that the free energies of the bcc and hcp phases under core conditions are very similar. The preference of small concentrations of light elements for either phase may thus be the defining factor in determining which Fe structure is stable in the inner core. In particular, it has been shown theoretically [2] and experimentally [3] that, at high pressures, FeSi stabilises in the CsCl structure, which has identical atomic coordinates to bcc-Fe, rather than in the hcp structure. This suggests that Si may act to stabilise the bcc phase in the core. Indeed, this is supported by low pressure experiments which have shown that, at low concentrations (7.9 weight %), Si has a large effect on the stability field of bcc Fe, increasing the

transition pressure to hcp from 10-15 GPa up to 36 GPa at 300 K [4]. It is possible, therefore, that with an appropriate concentration of Si and at the high temperatures of the core, the bcc phase could be stabilised with respect to the hcp and the formation of a bcc-structured Fe-Si alloy would be favoured.

In order to test whether Si can stabilise the bcc phase sufficiently to make it the stable phase in the core, we used *ab initio* calculations to investigate the effect of silicon concentration on both the bcc/hcp phase transition and the equation of state of Fe-Si up to core pressures. In the next section we describe the simulation techniques used in our calculations and the way we obtained the equations of state for the different impurity concentrations in the different iron crystal structures. We then show how the relative enthalpy curves can be used to deduce the stable structure. We calculate the pressure of the bcc-hcp phase transition and compare it to experimental data. Finally we extend these results to Earth's core conditions, taking previous *ab initio* calculations [5] further by investigating different impurity concentrations and at different volumes, and we discuss possible implications for the inner core structure. Our conclusions give further validity to those of Vočadlo et al. [5].

2. Quantum mechanical simulation techniques

The calculations in this work were carried out using Density Functional Theory (DFT) [7] as implemented in the VASP code [8]. The exchange-correlation energy was represented by the generalised gradient approximation (GGA) [9], which achieves the highest accuracy for transition metals. We made use of the projected augmented wave (PAW)

method, where the wavefunction combines an all-electron core region with a pseudo-valence region. The PAW method was introduced by Blöchl [10], and it combines the accuracy of all-electron methods with the efficiency of pseudopotentials. With a relatively small number of plane waves, it can give results that agree accurately with all electron methods. Indeed, it has been previously shown that the use of this method gives accurate results for iron both under ambient and core conditions [11-15].

Unit cells of pure iron were constructed in the bcc and hcp structures. For the bcc case we used the 2-atom cubic unit cell. For the hcp case, the unit cell used was that of the anti-ferromagnetic II (afmII) structure which contains 8 atoms (see Figure 1), as this was shown to be the stable hcp phase at low pressures [16, 17].

VASP calculates the ground state ($T=0$) for each set of ionic positions and the electronic free energy is taken as the quantity to be minimised. Care was taken when choosing the k-point sampling grid and plane wave cutoff energies in order to have an energy convergence of no more than 0.004 eV/atom. A $14 \times 14 \times 14$ grid (equivalent to 84 k-points in the irreducible Brillouin zone (IBZ)) was used for bcc-Fe and a $9 \times 9 \times 9$ grid (125 k-points in the IBZ) for hcp-Fe, with a cutoff energy of 400eV. The same cutoff energy was used throughout the calculations.

Substitutional defects of silicon were created by replacing Fe with Si in hcp and bcc supercells. Three different concentrations were investigated which bracket the experimental value of 7.9 wt%, namely ~ 3.2 , ~ 6.7 and ~ 10.4 wt. %. Specifically, for both structures, that meant a substitutional defect of one, two and three Si atoms respectively

for each of the above concentrations. The supercell contained 16 atoms both in the bcc (a 2x2x2 multiplication of the 2-atom bcc unit cell) and in the hcp structure (a 1x1x2 multiplication of the afm II unit cell). A 5x5x5 k-point grid (18 k-points in the IBZ) was used for the bcc and a 9x9x5 (123 k-points in the IBZ) for the hcp phase. The structures were then allowed to relax and the total energy was calculated. In the supercells containing more than one Si defect, a number of trials were performed with the different possible configurations of the defect atoms. In the hcp supercells the Si atoms were placed at symmetric positions as far away from each other as possible, taking into account the periodic boundary conditions. This proved to be the most stable configuration. In the bcc case, two different substitutional configurations were found to be favoured at high and low pressures respectively, so both were taken into account.

Finding the ground state free energy E for a set of different volumes V allowed us to fit the E - V data to a 3rd order Birch-Murnaghan equation of state (EOS) [18] of the following form:

$$E(V) = \frac{9}{4} K_0 V_0 \frac{V_0}{V} \left[\frac{1}{2} \left(\frac{V_0}{V} \right)^{\frac{1}{3}} - \left(\frac{V_0}{V} \right)^{\frac{1}{3}} \right] + \frac{9}{16} K_0 (K' - 4) V_0 \left(\frac{V_0}{V} \right) \left[\left(\frac{V_0}{V} \right) - 3 \left(\frac{V_0}{V} \right)^{\frac{1}{3}} + 3 \left(\frac{V_0}{V} \right)^{\frac{1}{3}} \right] + E_0 - \frac{9}{16} K_0 V_0 (K' - 6)$$

The resulting EOS parameters were then used to obtain the enthalpies H at those volumes, and to plot the enthalpy as a function of pressure for the bcc and hcp phases of the different Si concentrations.

3. Results

The equation of state parameters for each silicon concentration are shown in Table 1. The parameters for pure iron [19-22] are also displayed, where the volume underestimation due to the GGA functional is apparent. For the higher concentrations of Si, where different Si configurations are favoured at low and high pressures, both sets of parameters are displayed. For the 6.7% concentration, this change of stability between the two configurations in bcc takes place at around 210 GPa, whereas for the 10.4% concentration, it takes place at around 80 GPa. The equation of state parameters were used to plot the enthalpy curves as a function of pressure for pure Fe and for the three different concentrations of Si considered here.

The enthalpy-pressure curves are plotted in Figure 2. Also indicated are the transition pressures for the pseudo-univariant reaction (i.e. the transition from one phase to another with the same composition, ignoring any possible solid-solutions). The calculated transition pressures are ~7 GPa, ~11 GPa, ~16 GPa and ~41 GPa, for concentrations of 0%, 3.2%, 6.7% and 10.4% Si respectively. In Figure 3 we plot the change in the transition pressure for the pseudo-univariant reaction as a function of composition. As can be seen, the effect of Si on the transition pressure is strongly non-linear. Also shown is the pressure range of the room temperature solid solution as found experimentally by Lin et al. [4] for a bulk composition containing 7.9% Si. Although the experimental solid solution cannot be used to establish the exact pressure of the pseudo-univariant reaction, for a particular composition the pseudo-univariant reaction must be bracketed by the minimum and maximum pressure where both phases are present. The experimental two-

phase region at that composition starts at about 4 GPa above the pure Fe transition and persists for about 20 GPa [4]. As can be seen in the figure, we calculate that 7.9% Si will increase the pressure of the pseudo-univariant transition by ~ 16 GPa, a value that falls within the experimental solid solution range. This adds some confidence to our results and confirms that the presence of Si can strongly increase the stability of the bcc phase over hcp.

We repeated the 0 K calculations at the pressure of the inner core boundary (ICB) (330 GPa). It is worth noting that the magnetic moments at such high pressures greatly diminish in the bcc phase, and disappear completely in the hcp phase. The results are given in Table 2. For pure iron, the calculated difference in enthalpies between the bcc and hcp structures of pure iron is 660 meV in favour of the hcp structure. As with the low pressure results, we find that Si strongly prefers the bcc phase, and in fact, at 10.4 wt. %, the enthalpy difference has dropped to only 115 meV. We also find, again consistent with the low pressure results, that the enthalpy difference drops almost linearly with increasing concentration of Si. These results show that at 330 GPa, Si defects are about 2.5eV per defect atom more stable in the bcc structure than in the hcp phase. This means that, for example, the suggested ~ 5 mol.% concentration of Si in the inner core [4, 5, 23] would lower the enthalpy difference between the two phases by 125 meV.

It is known that bcc-Fe is dynamically unstable at 0 K and high pressures [24, 25]. Our results, however, show that the addition of Si decreases the free energy difference between the two phases; the implication of this is that the magnitude of the instability is

also reduced. Indeed it may even be the case that the incorporation of Si removes the instability altogether, even at 0 K.

4. Discussion and Conclusion

Even though there is no doubt from our results that the inclusion of Si tends to stabilise bcc-Fe, the calculated enthalpy differences between the two pure Fe structures at $T=0$ still favour hcp stability at inner core pressures, at least for the concentrations considered here. However, the high temperatures of the core alter this significantly and recent ab initio results show that the difference between the free energies of the two phases of pure iron at ICB pressures and temperatures is only ~ 33 meV [5]. Since, as shown above, Si stabilises bcc over hcp by 2.5 eV per defect atom, less than 1.5 mol.% Si is needed to overcome the 33 meV required to make bcc stable. The higher but still modest concentration of 5 mol.% would provide a stabilisation enthalpy of 125 meV. This shows that even the relatively small concentrations of Si suggested for the inner core [26] are more than enough to stabilise bcc-Fe in the inner core. We conclude, therefore, that the presence of the bcc phase in the inner core cannot be ruled out.

Acknowledgements

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Figure and table captions

Figure 1: The afmII structure. The arrows on the atoms represent the spin direction.

White atoms are positioned at $z=1/4$, black atoms at $z=3/4$. The 8-atom cell that was used is marked with dashed lines. It is the smallest possible cell for this structure, and is a $2 \times 2 \times 1$ multiplication of the primitive hcp cell.

Figure 2: Calculated enthalpy curves for bcc and hcp structures at 3 different concentrations of silicon. The arrows indicate the transition pressures for the pseudo-univariant reactions.

Figure 3: Change in the transition pressure ($\Delta P = P_{tr}^{FeX} - P_{tr}^{Fe}$) for the pseudo-univariant reaction as a function of composition. The gray bar represents the experimental pressure range of the 300K solid solution [4] for a bulk composition containing 7.9% Si. We can see that our result on the pseudo-univariant reaction at 7.9% Si falls well within that range. The solid line is a weighted fit through the ab initio results.

Table 1: The parameters of the Birch-Murnaghan 3rd order equation of state, for the different concentrations of silicon. For pure iron, the experimental parameters are also displayed (b,d).

Table 2: The enthalpy differences between the bcc and hcp structures at $P=330\text{GPa}$ and $T=0\text{K}$. At $T=0\text{K}$ the hcp phase is always more stable, but one can see that the difference drops almost linearly as the percentage of Si increases.

Tables

wt. %Si	Fe structure	V_0 (\AA^3)	K_0 (GPa)	K'
0	bcc	11.39(1)	203(3)	4.36(3)
	ref. [17]	11.355(7)	201.502(8)	4.29(1)
	ref. [19]	11.78	166.4	5.29
	hcp-afmII	10.48(3)	229(7)	5.12(13)
	ref. [22]	10.55	209	5.2
	ref. [21]	11.176(17)	165(4)	5.33(90)
~3.2	bcc	11.34(2)	201(3)	4.39(3)
	hcp-afmII	10.55(8)	216(12)	4.95(19)
~6.7	bcc 1:	11.15(3)	216(6)	4.35(8)
	bcc 2:	11.28(3)	198(6)	4.41(9)
	hcp-afmII	10.55(4)	238(9)	4.84(14)
~10.4	bcc 1:	11.12(4)	212(7)	4.47(9)
	bcc 2:	11.31(5)	156(7)	5.25(12)
	hcp-afmII	10.61(3)	239(8)	4.67(11)

1: Derived from the Si configuration most stable at low pressures.

2: Derived from the Si configuration most stable at core pressures.

Table 1: The parameters of the Birch-Murnaghan 3rd order equation of state, for the different concentrations of silicon. For pure iron, the experimental parameters are also displayed (b,d).

wt. % Si	$\Delta H = H_{\text{bcc}} - H_{\text{hcp}}$
0	660
3.2	503
6.7	354
10.4	115

Table 2: *The enthalpy differences between the bcc and hcp structures at $P=330\text{GPa}$ and $T=0\text{K}$. At $T=0\text{K}$ the hcp phase is always more stable, but one can see that the difference drops almost linearly as the percentage of Si increases.*

Figures

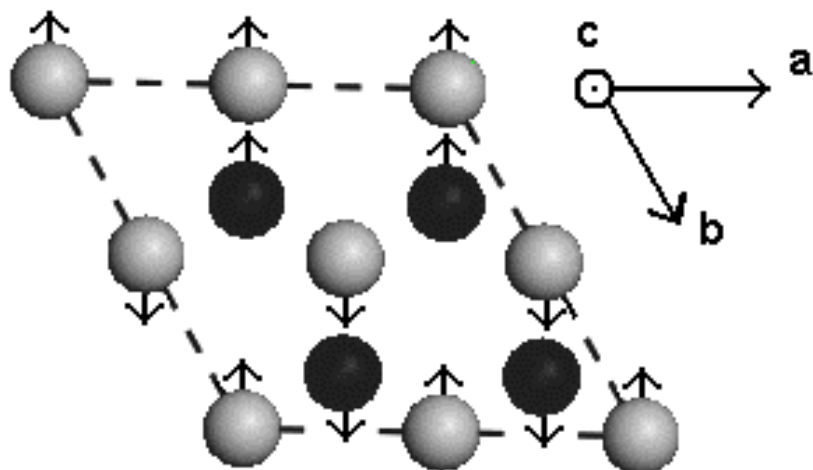


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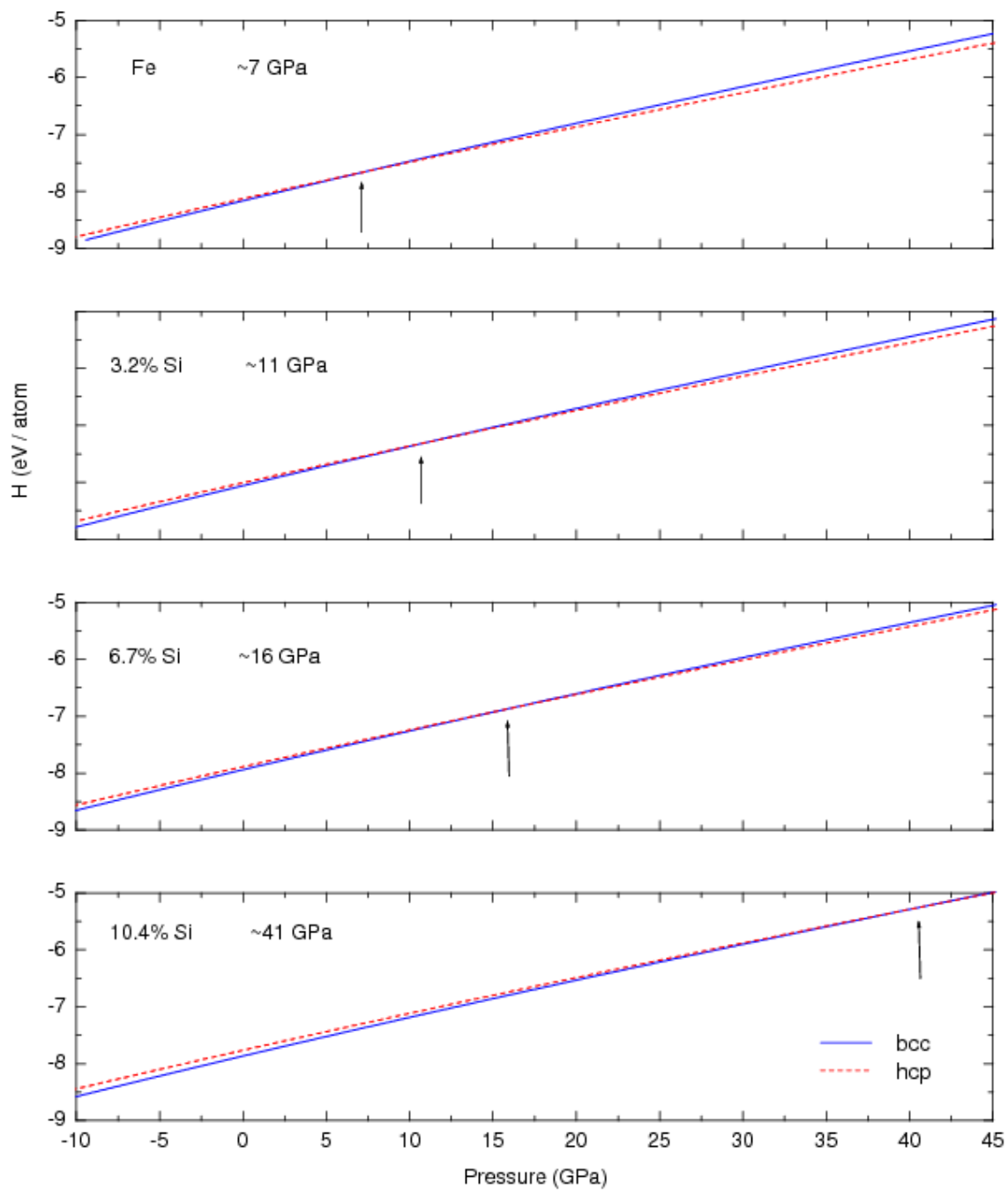


Figure 2: Calculated enthalpy curves for *bcc* and *hcp* structures at 3 different concentrations of silicon. The arrows indicate the transition pressures for the pseudo-univariant reactions.

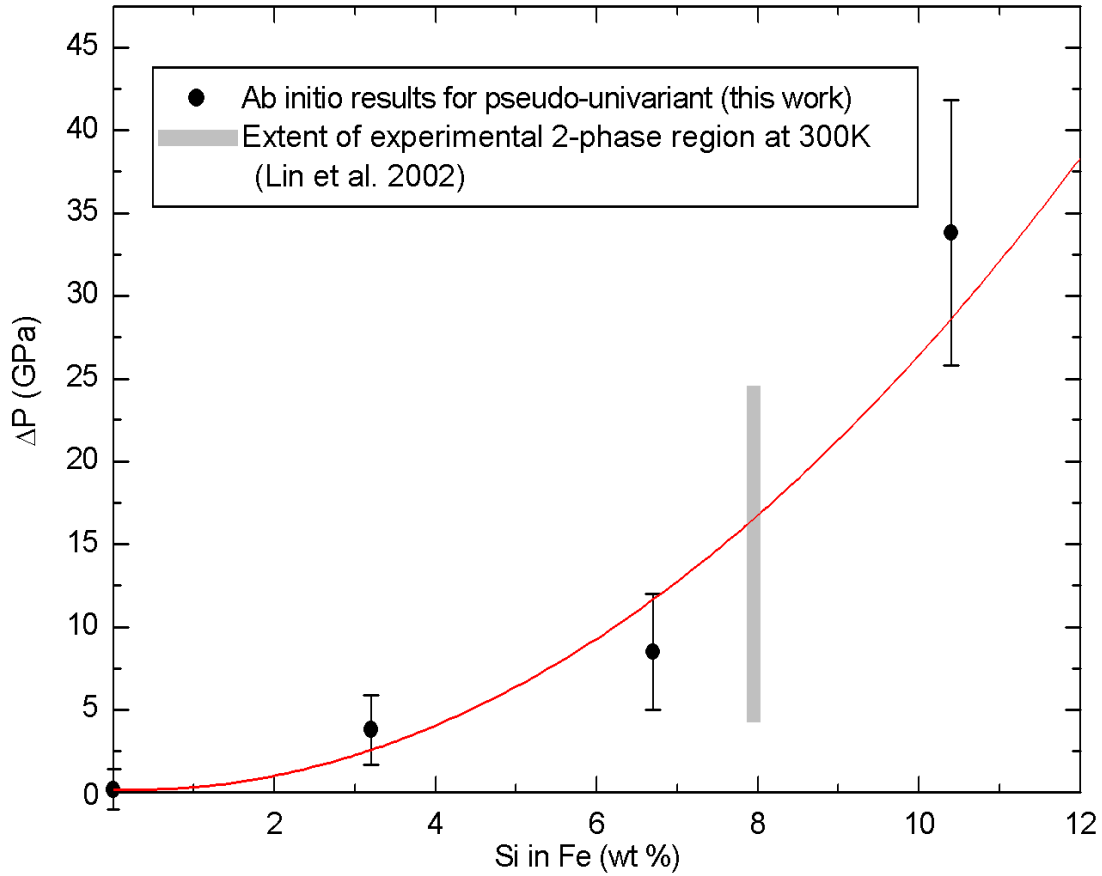


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