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Ulf Winfried Liebal, Thomas Millat, Imke G. de Jong, Oscar P Kuipers, Uwe Völker, et al.. How mathematical modelling elucidates signalling in B. subtilis. Molecular Microbiology, 2010, 10.1111/j.1365-2958.2010.07283.x . hal-00563452

HAL Id: hal-00563452 https://hal.science/hal-00563452

Submitted on 5 Feb 2011

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How mathematical modelling elucidates signalling in B. subtilis

Journal:	Molecular Microbiology
Manuscript ID:	MMI-2010-10039.R1
Manuscript Type:	MicroReview
Date Submitted by the Author:	24-Jun-2010
Complete List of Authors:	Liebal, Ulf; Universität Rostock, Informatik und Elektrotechniche Fakultät Millat, Thomas; Universität Rostock, Informatik und Elektrotechniche Fakultät de Jong, Imke; University of Groningen, Molecular Genetics Kuipers, Oscar; University of Groningen, Department of Molecular Genetics Völker, Uwe; Ernst-Moritz-Arndt-University Greifswald, Interfaculty Institute of Genetics and Functional Genomics Wolkenhauer, Olaf; Universität Rostock, Informatik und Elektrotechniche Fakultät
Key Words:	Bacillus subtilis, chemotaxis, competence, mathematical modelling, sporulation



1	How mathematical modelling elucidates signalling in <i>B. subtilis</i>
2	Ulf W Liebal ^{1*} , Thomas Millat ¹ , Imke G de Jong ² ,
3	Oscar P Kuipers ² , Uwe Völker ³ and Olaf Wolkenhauer ¹
4	
5 6 7 8 9	 Dept. of Systems Biology and Bioinformatics, Institute of Computer Science, University of Rostock, 18051 Rostock, Germany Molecular Genetics, Biomolecular Sciences and Biotechnology Institute, University of Groningen, Haren, The Netherlands Interfaculty Institute of Genetics and Functional Genomics, Ernst-Moritz-Arndt-University Greifswald
10 11	 17487 Greifswald, Germany * Corresponding author: Dept. of Systems Biology and Bioinformatics. Institute of Computer Science
12	University of Rostock, 18051 Rostock, Germany. Tel.: +49 381 498 7577; Fax: +49 381 498 7572
13	E-mail: ulf.liebal@uni-rostock.de
14	
15 16	Running title: Mathematical modelling in B. subtilis
17	Subject categories: signal transduction, microbiology & pathogens
18 19	Keywords: Bacillus subtilis / chemotaxis / competence / mathematical modelling / sporulation
20	Character count (with spaces): ~64,500
21	Word count (- Title page, - references): ~7,300
22	References: ~ 85
23	

24 Abstract

Appropriate stimulus perception, signal processing and transduction ensure optimal 25 adaptation of bacteria to environmental challenges. In the Gram-positive model bacterium 26 Bacillus subtilis signalling networks and molecular interactions therein are well studied, 27 making this species a suitable candidate for the application of mathematical modelling. Here, 28 we review systems biology approaches, focusing on chemotaxis, sporulation, σ^{B} -dependent 29 30 general stress response and competence. Processes like chemotaxis and Z-ring assembly depend critically on the subcellular localisation of proteins. Environmental response 31 strategies, including sporulation and competence, are characterised by phenotypic 32 heterogeneity in isogenic cultures. The examples of mathematical modelling also include 33 investigations that have demonstrated how operon structure and signalling dynamics are 34 intricately interwoven to establish optimal responses. Our review illustrates that these 35 36 interdisciplinary approaches offer new insights into the response of B. subtilis to environmental challenges. These case studies reveal modelling as a tool to increase the 37 38 understanding of complex systems, to help formulating hypotheses and to guide the design of more directed experiments that test predictions. 39

40 Introduction

Bacillus subtilis is one of the best studied prokaryotes and serves as the main model organism 41 for Gram-positive bacteria. Research related to B. subtilis has provided substantial 42 information regarding the organisation of bacterial life cycles. This knowledge provides an 43 excellent basis for mathematical modelling of cellular processes. Indeed, Bacilli have been 44 investigated in theoretical biology for a long time. In the 1970s, Sargent compared different 45 models for the control of cell length (Sargent, 1975), which have since then been further 46 refined (e.g. Koch, 1992; Grover et al., 2004). Espinosa et al. (1977) examined the 47 acquisition of competence in cultures, while Jeong et al. (1990) presented a mathematical 48 model for growth processes including sporulation and central metabolism. Particularly during 49 the last decade there has been increased interest in systems biology, a discipline 50 encompassing the interaction of experimental approaches, mathematical modelling and 51 computer simulations (Wolkenhauer et al., 2003). B. subtilis has gained increasing attention 52 53 due to its capacity for developmental responses and population heterogeneity.

In this review we summarize recent results in the modelling of signalling systems and 54 survey how mathematical modelling provides a better understanding of sophisticated cellular 55 responses. The first models we review are related to chemotaxis. They have been made to 56 predict adaptation mechanisms of the rotational orientation of flagella in response to changes 57 in concentrations of external substances. Furthermore, we discuss models describing protein 58 localisation, which is an important factor for chemotactic signalling. We review spatial models 59 of MinCD and the early sporulation factors Spo0J/Soj and summarize mathematical 60 interpretations of the initiation of sporulation that attracted attention because of parallels to 61 developmental processes in eukaryotes. Additionally, we show how signalling processes that 62 include proteins of the spoIIA operon resemble the general stress response mediated by 63 sigma factor σ^{B} with respect to the use of the so-called partner switch mechanism. Recent 64 studies demonstrate how the operon organization of *spoOA* and *sinIR* supports their function 65 during sporulation. We also discuss models regarding another important developmental 66 process: competence. Different investigations have revealed the mechanism by which the 67 excitable response is induced and how the cell exits competence. Finally, an outlook to 68 future developments of the application of mathematical models is given. 69

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71 Chemotaxis

During colony growth B. subtilis can display two distinct phenotypes namely motile cells that respond to chemotactic signals and non-motile cells growing as connected chains (Kearns and Losick, 2005). Expression of chemotactic proteins in the *che-fla* operon is controlled by the sigma factor σ^{D} (Marquez *et al.*, 1990). Analysis of chemotaxis is Page 3 of 25

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interesting from two perspectives: Firstly, how cells in a population `decide' whether to become motile or not; Secondly, how the information of a chemotactic signal is transmitted from the receptor to the flagella to result in a directed movement. Here, we focus on the latter aspect since no mathematical models for the genetic regulation of σ^{D} expression have been published to date.

The chemotactic behaviour of various organisms has been studied intensively in the 81 past and a thorough overview of the mathematical approaches is given by Tindall et al. 82 (2008). Mathematical modelling of chemotaxis started in the 1970s using E. coli as a model 83 organism (Tindall et al., 2008). Investigations in B. subtilis, notably by Ordal (e.g. Garrity 84 and Ordal, 1995), uncovered that although the molecular machinery is conserved between E. 85 coli and B. subtilis, the mechanism of chemotaxis is surprisingly different (Bischoff and 86 Ordal, 1991, Rao and Ordal, 2009). A simplified scheme displaying the mechanism of 87 88 chemotactic signalling in B. subtilis is shown in Figure 1. Once a ligand binds to a methylaccepting chemotaxis protein (MCP) receptor, CheR methylates while CheB demethylates 89 90 specific glutamate residues of the receptor. This change in methylation leads to the activation 91 of CheA which phosphorylates CheY. CheY~P binds to the flagellar motor protein FliM reversing the spin of the flagellum from clock- to counter-clockwise rotation (Garrity and 92 Ordal, 1995). Instead of tumbling, the cell now performs a directed movement along the 93 concentration gradient. Dephosphorylation of CheY~P is accomplished largely by FliY, 94 which is located at the base of the flagellum. An additional player is the CheCD heterodimer 95 that has three functions: i) CheCD binds CheY~P and thus competes with with binding to 96 FliM, ii) CheC displays weak CheY~P phosphatase activity, and iii) CheD increases CheA-97 receptor affinity by deamination of a glutamine residue on the receptor (Kristich and Ordal, 98 2002). Surprisingly, in contrast to *B. subtilis*, the *E. coli* CheY~P induces clockwise rotation 99 100 of the flagellum, resulting in smooth runs (Garrity and Ordal, 1995). The tumbling frequency will resume its pre-stimulus activity even if the attractant concentration remains constant, a 101 102 phenomenon called adaptivity.

103 Rao et al. (2004) presented a model that includes the previously mentioned signalling mechanisms. The authors assumed a mechanism by which CheY~P enhances the transition 104 105 of an active to an inactive receptor conformation. This assumption is experimentally testable as it requires an affinity of CheY~P to the receptor complex. The authors examined their 106 107 model with respect to a *cheBCDR* quadruple mutant to compare it with published data. The adapted model hints at causes for the observed oscillatory phenotype of the mutant. CheV, 108 109 an adaptor protein that mediates the interaction between CheA and the receptor, is assumed to generate a positive feedback loop concerning CheA activation while CheY~P stimulates 110 CheA deactivation. The authors also gave an explanation for the population heterogeneity 111

regarding chemotactic oscillations. Variations in the concentration of CheV by just a factor of two, achievable by gene expression noise, can determine the rise of oscillations (Rao *et al.*, 2004). However, there is a caveat in the model assumptions because not CheV is inhibiting CheA–receptor association but CheV~P (Aizawa *et al.*, 2002, Rao and Ordal, 2009).

117 Rao *et al.* concluded that the *B. subtilis* system is more robust, i.e. CheY~P steady 118 state levels and adaptation time are relatively independent of CheB and CheR. This is 119 thought to buffer against genetic mutations and probably reflects the more variable and 120 hostile environment in which *B. subtilis* lives. However, although the regulation of the 121 chemotactic systems of *B. subtilis* and *E. coli* differ, the motility of both organisms is similar 122 in effectiveness over five orders of magnitude of stimulus concentration (Rao *et al.*, 2004).

A very important aspect of chemotaxis is that the receptors are located at the poles, 123 while the flagella are evenly distributed on the cell surface. This implies that protein 124 localisation is an integral part of the signal transduction and needs to be considered. The 125 signalling molecule CheY~P has to diffuse from the poles throughout the cell volume to act 126 on the flagellum motor (Szurmant et al., 2003). Although the switching decision at a given 127 time is stochastic, the frequency of switching is a crucial parameter in controlling motility 128 and is ultrasensitive to the concentration of CheY~P. If spatial gradients of CheY~P 129 130 concentration exist along the cell, chemotaxis could be disrupted because motors receive conflicting signals as examined by Rao et al. (2005) using reaction-diffusion equations. 131 Again, they compared *B. subtilis* with *E. coli*. In *E. coli* the phosphatase for CheY~P is 132 located at the chemosensing receptor while in *B. subtilis* phosphatases are located both at the 133 receptor (CheC) as well as the flagellum motor (FliY) (Szurmant et al., 2003). The model 134 shows, that E. coli can establish a homogeneous CheY~P concentration throughout the cell, 135 because the kinase and the phosphatase are located close to each other. In contrast, for B. 136 subtilis a linear decrease of CheY~P concentration with increasing distance to the receptor is 137 predicted. However, simulations for B. subtilis indicate the presence of circular 138 concentration gradients around each flagellum motor that render the CheY~P levels 139 comparable at each motor base. The function of CheC could not be determined by the 140 simulations. CheC did not have an effect on the CheY~P gradient (Rao et al., 2005). The 141 authors speculated that the phosphatase network of B. subtilis optimises signal processing of 142 both membrane bound as well as soluble receptors, which have been found for aerotaxis 143 (Rao et al., 2005, Hou et al., 2000). 144

145

146 **Protein localisation**

147 Protein localisation increases signal transduction speed, specificity, and sensitivity not

only for chemotaxis (Lewis, 2004, Shapiro et al., 2009, Vescovi et al., 2010). Preceding cell 148 149 division proper arrangement of the 'divisome' is critical (Graumann, 2007). The GTPase FtsZ determines the location of the division site as it assembles into a ring-like structure at 150 the midcell, thereby providing the frame for subsequent separation processes. The targeting 151 of FtsZ to the midcell is controlled by the MinCD/DivIVA system. DivIVA is located at the 152 153 cell poles, presumably because of its affinity for negative membrane curvature (Huang and Ramamurthi, 2010). The proteins MinCD associate with DivIVA and inhibit polymerisation 154 155 of FtsZ (Errington and Daniel, 2002). The hypothesis that the membrane binding equilibrium depends on membrane curvature and leads to MinCD clustering was tested by Howard 156 157 (2004). The significant finding of this study is not that MinCD pole localisation could be reproduced eventually, but rather to uncover the conditions and parameter values that were 158 159 necessary in silico. In the simulation the diffusion of membrane bound MinCD and DivIVA was very restricted (no diffusion was assumed for MinCD), DivIVA binds to the edges of 160 161 MinCD and binding of MinCD is heavily influenced by geometric effects. Indeed it seems it is DivIVA not MinCD which is the driving force for membrane curvature sensitivity (Huang 162 and Ramamurthi, 2010). 163

164 Another localisation phenomenon is chromosome segregation during cell division in conjunction with Spo0J/Soj interactions. Spo0J condenses at nucleoids to compact foci. This 165 process is catalysed by Soj, a protein that performs irregular oscillatory relocations from pole 166 to pole and nucleoid to nucleoid. The large fluctuations in the relocation process are likely to 167 168 be caused by the low copy numbers of Spo0J/Soj with each being present at about 1500 molecules per cell (Doubrovinski and Howard, 2005). To examine the nature of the 169 170 fluctuations, Doubrovinski and Howard (2005) formulated a stochastic reaction-diffusion model. They assumed cooperative binding of Soj and Spo0J to nucleoids. Depending on the 171 172 level of bound Soj, Spo0J can switch to its condensed form causing Soj to diffuse from the foci. After being released, Soj has to reacquire catalytic activity at the cell pole involving 173 interaction with MinD (Doubrovinski and Howard, 2005). The model was tested using the 174 Spo0J19 mutant, which displays a higher frequency of Soj relocations (Autret et al., 2001). 175 Analysis of the model indicates that two different modifications could reproduce the mutant 176 phenotype: either i) Soj is capable of getting reactivated in the cytoplasm without the need of 177 MinD or ii) Soj is more rapidly expelled from the condensed Spo0J foci. Doubrovinski and 178 Howard (2005) went on to simulate a hypothetical *ftsZ-soj* double mutant. In a cell carrying 179 only an *ftsZ* mutation Soj relocations are suspended. This Soj dysfunction can be suppressed 180 in silico with an additional Spo0J19 mutation. 181

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183 < Location of Figure 1>

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185 Phosphorelay

The phosphorelay provides a decision device for various phenotypic adaptation reactions 186 like competence, motility, biofilm formation, and cannibalism or even the return to 187 vegetative growth (Fawcett et al., 2000, Fujita et al., 2005, Lopez et al., 2008). To distribute 188 189 risk and benefit of any of the developmental responses, only part of an isogenic population 190 enters any of them (Dubnau and Losick, 2006, Smits et al., 2006, Veening et al., 2008b). The 191 five histidine kinases KinA-E are the environmental sensors that lead to an activation of the 192 phosphorelay. Among the signals sensed are nutritional stress, cell density, Krebs cycle, 193 DNA damage, and presence of extracellular matrix in biofilms (Claverys and Havarstein, 2007, Aguilar et al., 2010). The phosphorylated kinases transfer their phosphate group to the 194 195 Spo0F protein (Sonenshein, 2000, Errington, 2003, Piggot and Hilbert, 2004). The phosphate group of Spo0F~P is then sequentially and reversibly relayed to Spo0B and Spo0A, 196 197 respectively. The response regulators SpoOF and SpoOA are dephosphorylated by the 198 phosphatases RapA and Spo0E, respectively. These phosphatases are used for additional environmental regulation (RapA activity inhibited by PhrA) and genomic negative feedback 199 regulation (Spo0E expression activated by Spo0A~P). Phosphorylated Spo0A (Spo0A~P) is 200 the response regulator that directly or indirectly controls the expression of over 500 genes 201 (Fawcett et al., 2000). The genes under control of Spo0A~P can be classified according to 202 their affinity to the response regulator (Fujita et al., 2005). Genes with high affinity are 203 204 activated at early stages of phosphorelay activation, e.g. competence, cannibalism and 205 biofilm formation, while genes with low affinity are only activated once sufficiently high 206 levels of Spo0A~P have accumulated, e.g. sporulation genes like the spoIIA operon (Fujita et 207 al., 2005).

208 The processes outlined above have attracted various modelling efforts since the interactions within the system are well known and supported by a large body, albeit mostly 209 210 qualitative, experimental data. Because of the complexity of the phosphorelay network a prediction of its behaviour is difficult, if not impossible, without the help of computational 211 212 analysis. Next, we give a short integration of the modelling approaches with respect to the activation of the phosphorelay, followed by a more detailed discussion of the respective 213 214 models. Jabbari et al. (2010) examined how environmental and cellular conditions shape the decision for sporulation. While Jabbari et al. (2010) focussed on the elucidation of the 215 216 contributions of factors external to the phosphorelay, de Jong et al. (2004) investigated the dynamics of protein regulated by Spo0A~P following activation of the phosphorelay. A 217 stability analysis of a simplified model of the phosphorelay was performed by Morohashi et 218 al. (2007) while Bischofs et al. (2009) went a step further by asking how different 219

environmental signals are integrated by phosphatase activities on top of the phosphorelay 220 221 kinases. Within a given population the output of the phosphorelay is highly heterogeneous, enabling the population to follow several distinct phenotypes, a finding of investigations by 222 de Jong et al. (2010) and Chastanet et al. (2010). As indicated, the activation of the 223 phosphorelay is not just a preparation to sporulate but the starting signal for a variety of 224 225 responses. Schultz et al. (2009) started to additionally consider competence, aside from sporulation, being activated by Spo0A~P. For their study on the activation and dynamics of 226 227 extracytoplasmic protease synthesis Veening et al. (2007) neglected the phosphorelay 228 dynamics instead using AbrB, a Spo0A~P regulated repressor, as the input signal.

- The main goal of the modelling work by Jabbari *et al.* (2010) was to elucidate which environmental and cellular conditions allow the activation of sporulation (accumulation of Spo0A~P). Their model can be subdivided into several modules, namely the regulation of
- 232 1. KinAB activity,

233 2. the phosphorelay,

- 234 3. expression of SinIR proteins,
- 235 4. the activity of RapA by PhrA.

The KinA/B activity controls the initiation of the phosphorelay and sensitivity to 236 environmental conditions. The phosphorelay controls how much Spo0A~P can be generated 237 eventually (Sonenshein, 2000). SinR is a repressor of SpoOA, other late sporulation genes, as 238 well as genes for motility and competence and is inhibited by SinI (Bai et al., 1993). PhrA is 239 a phosphatase regulator that inhibits the activity of the receptor aspartyl phosphatase RapA. 240 PhrA is secreted to the medium and re-imported by the oligopeptide permeases (Opp, 241 Spo0K) (Piggot and Hilbert, 2004). The phosphorelay leads to the phosphorylation of Spo0A 242 that inhibits the expression of AbrB and due to its inherent instability the drop in AbrB 243 concentration which results in i) an elevated expression of σ^{H} , and a subsequent increase in 244 Spo0F and Spo0A concentrations, ii) higher concentrations of KinB, iii) lower levels of 245 AbrB with the subsequent reduction in the concentration of the transcription factor Hpr and 246 increased SinIR expression, and iv) a reduced level of Hpr leads to de-repression of opp 247 genes thus increasing the role of quorum sensing by Phr proteins. The environmental signals 248 and cellular states that Jabbari et al. (2010) investigated are: 249

- 250 1. population density sensed via PhrA
- 251 2. cellular nutrient and energy availability sensed via CodY-GTP
- 252 3. competence decision sensed via the level of ComA
- 253 4. condition of the DNA sensed via Sda

The authors transformed these four cellular states into yes/no decisions and assigned *a priori* whether sporulation is desirable or not. Contradictions of simulations with the *a priori*

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256 assigned sporulation decisions was observed for the condition of a cell in a large population 257 (high PhrA level), no nutrients available (no CodY-GTP), no competence (no ComA) but damaged DNA (high Sda level). Contrary to expectations, the model induced sporulation 258 even with damaged DNA, albeit after a significant time delay compared to cells without 259 damaged DNA. In the model, this delay is caused by the sporulation positive signal of PhrA 260 261 emitted from neighbouring cells. Eventually, PhrA and nutrient limitation are stronger than inhibition of KinA by Sda. Thus, PhrA not only acts as a quorum sensing molecule, as shown 262 263 by Bischofs et al. (2009), but also as a timer allowing cells to repair the DNA. Significantly, 264 the authors conclude that activation of PhrA and RapA transcription by ComA serves to 265 heighten the sensitivity of the phosphorelay towards the input signals (Jabbari et al., 2010). This increase in phosphorelay sensitivity might well be a cause for the heterogeneity in the 266 267 phosphorelay output as observed by de Jong et al. (2010) and Chastanet et al. (2010).

The model of de Jong et al. (2003) is relatively similar to that of Jabbari et al. (2010) 268 269 with respect to the biological scope. But in contrast to Jabbari *et al.* who tested the inputoutput completeness of our understanding, de Jong *et al.* compared their model with a dozen 270 sporulation mutants. This allowed them to test whether our understanding of the internal 271 structure of the initial sporulation network is correct. Furthermore, the model of de Jong et 272 al. is based on a different modelling framework compared to Jabbari et al. De Jong et al. 273 used discrete time and protein concentration steps. This model allows predictions about 274 relative steady-state concentrations of the components considered, but a comparison with the 275 dynamic simulations of Jabbari et al. is not possible. One outcome of the simulations by de 276 Jong *et al.* is that activation of the phosphorelay can result in two steady state solutions with 277 or without increased levels of Spo0A~P. The reason is a competition of activating KinA and 278 279 inhibiting Spo0E activity in the sporulation network. The system is extremely sensitive with 280 respect to environmental variation and noise in gene transcription, providing an explanation for the observed phenotypic variations in experiments. These findings were further 281 282 corroborated by Morohashi et al. (2007) who performed a stability analysis with a simple model of the phosphorelay. Their model only considers phosphorylation of Spo0A~P by an 283 284 entity called phosphorelay and its dephosphorylation by Spo0E. They conclude that the feedback of Spo0E that influences the distribution of sporulating to nonsporulating cells. 285

A more detailed examination of the phosphorelay mechanism has been conducted by Bischofs *et al.* (2009). The authors focused particularly on the integration of starvation signals from the medium by quorum sensing mechanisms involving Raps and Phrs. The authors examined the steady-state level of Spo0A~P in response to varying ratios of kinase activity (the environmental signal) to phosphatase activity by the Raps (the population signal). Four different phenotypes are possible: 1. Spo0A~P is not affected by changes in

292 kinase and phosphatase activity, 2. and 3. Spo0A~P is either sensitive to changes in kinase-293 or phosphatase activity, 4. Spo0A~P is sensitive to changes of both kinase and phosphatase activity. Only mechanisms underlying the fourth phenotype can properly integrate the 294 different signals termed by the authors 'signal integration regime'. Interestingly, SpoOB, the 295 second phosphotransferase of the phosphorelay, is devoid of feedback regulations by 296 297 Spo0A~P. Bischofs et al. (2009) showed that if a positive feedback from Spo0A~P to Spo0B would be present, the cell would not be able to properly integrate nutrient level and 298 299 population density and thus not being able to measure the 'food per cell'.

Even though the goal of systems biology is to increase our understanding of the 300 behaviour and dynamics of complex systems, most models discussed in this review focused 301 on supposedly separate and simplified functional modules of signal transduction. However, 302 we can only understand *B. subtilis* in greater detail if we gain more insight in the interplay 303 and cross-talk of the different environmental response strategies. A step towards dealing with 304 this challenge was taken by Schultz and co-workers (2009). They studied interactions 305 between the processes of sporulation, competence and quorum sensing. Their work showed 306 that small noise levels in many environmental and community related signals transmitted by 307 308 Phrs and Raps resulted in a great variability in the concentration of Spo0A~P, which in turn eventually lead to phenotypic diversity in isogenic populations. The authors related the 309 310 mutual inhibition of Spo0A~P by AbrB and Spo0E to the synthetic genetic regulatory network called `repressilator' that was designed by Elowitz and Leibler (2000) to display 311 312 oscillations. It is an intriguing question whether the early phase of sporulation should be composed of a regulatory network that could generate oscillations and how those detrimental 313 314 oscillations could be suppressed.

An overarching conclusion for most of the discussed articles investigating the 315 phosphorelay concerns the generation of variability in the SpoOA~P output. Jabbari et al. 316 317 (2010) as well as Schultz et al. (2009) observed that Phr and Rap proteins sensitize the output to the input. de Jong et al. (2003) and Morohashi et al. (2007) detected the competition 318 319 between SpoOE and KinA as a source for variability and bistability. Further information comes from studies by de Jong et al. (2010) and Chastanet et al. (2010) who examined the 320 321 heterogeneity in gene expression after activation of SpoOA. Because of the experimental classification of cells in sporulators and non-sporulators as well as the positive and negative 322 323 feedback regulations with respect to phosphorylation and dephosphorylation of SpoOA it was tempting to view the phosphorelay as a bistable switch. Bistability is a property that describes 324 325 the switching of the system between an activated and de-activated state (Millat et al., 2008). 326 Under such a regime, the system can be sensitive to a signal, leading to a switch-like transition into a new steady state. Once it is activated, the system can resist deactivation, see 327

Figure 2. Bistability is particularly interesting for biological systems as it provides the cell a way for fast yes/no decisions as well as enabling a heterogeneous population with only some

cells being activated (Veening *et al.*, 2008).

331 Bistability is implicated with several of the *B. subtilis* signalling networks, including (ComK)(Maamar and Dubnau, 2005), production of exoproteases 332 competence 333 (DegU)(Veening et al., 2007) or biofilm formation (SinR)(Chai et al., 2007). However, the data by de Jong et al. and Chastanet et al. show that there is no bistability in Spo0A~P, 334 instead Spo0A~P induced expression is highly heterogeneous. Neither is σ^{H} , providing the 335 positive feedback via KinA, necessary for establishing a heterogeneous Spo0A~P signal. To 336 reproduce a sufficient accumulation in Spo0A~P using a computational model Chastanet et 337 al. had to increase the concentration of all phophorelay proteins. This modelling outcome is 338 surprising since Spo0B concentration remains constant during stationary phase (de Jong et 339 al., 2010) and since the modelling of Bischofs et al. (2009) showed that Spo0A~P driven 340 spo0B expression would mean a violation of the signal integration of nutrients and 341 community density. Sporulation is an all-or-nothing process and surely has to be controlled 342 with switch-like dynamics. It seems however, that the phosphorelay is not the sporulation 343 344 switch but prepares the cell for a variety of phenotypic diverse responses (Lopez et al., 2008).

- 345
- 346 < Location of Figure 2>
- 347

348 Sporulation

One of the most conspicuous phenotypes of B. subtilis is sporulation. The final 349 commitment to this developmental process is established by σ^F dependent gene expression 350 (Dworkin and Losick, 2005). Spo0A~P mediated expression of sigF is crucial for 351 establishing compartment-specific gene expression during sporulation. Two studies 352 thoroughly investigated the regulation of σ^{F} activity using ordinary differential equation 353 models. One study focused on molecular processes that lead to asymmetrical differentiation 354 (Iber et al., 2006) while the other primarily aimed to uncover the principles of irreversibility 355 of the $\sigma^{\rm F}$ activation (Igoshin *et al.*, 2006). A simplified graphical description of the regulation 356 of σ^{F} activity is shown in Figure 1. Its activity is negatively regulated by the formation of a 357 heterodimer with SpoIIAB (AB), upon which the binding of the sigma factor to its target 358 DNA is prevented. SpoIIAA (AA) is able to competitively bind to AB and release σ^{F} . 359 However, in non-sporulating conditions AA is predominantly phosphorylated by the kinase 360 activity of AB. Thus, the steady state ratio of phosphorylated to non-phosphorylated AA 361 determines the level of free σ^{F} . This level is additionally regulated by the rate of 362

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dephosphorylation via the phosphatase SpoIIE (IIE). Iber et al. (2006) modelled in detail the 363 different states which exist for AB: i) its basic form of a homodimer, ii) bound with σ^{F} , and 364 iii) bound with one or two molecules of AA (phosphorylated or non-phosphorylated). Each 365 of these configurations harbours combinations of ATP and ADP in the nucleotide binding 366 pockets of the dimer. Finally, the number of states doubles since a central aspect of the model 367 368 is the allosteric functionality of AB. In any configuration AB is either in a relaxed or in a tense conformation that affects its enzymatic activity (Iber et al., 2006). Ultimately, the 369 370 authors determined 50 states connected by 150 reactions and 25 rate constants. The model 371 was successful in approximating qualitative results of a number of published experiments. A 372 quantitative demand of the model regarding the reaction rate constant of IIE phosphatase was 373 that it is 75 to 150 times lower compared with *in vitro* rates. In order to resolve this paradox, 374 IIE activity was measured by the authors in an assay with supposedly more in vivo like conditions (switching from manganese to magnesium dominated solutions) and indeed the 375 376 phosphatase activity matched the model predictions. Iber et al. (2006) modelled the higher activity of σ^{F} in the forespore by assuming that the IIE phosphatase associates with FtsZ 377 homogeneously over the septum. The forespore volume is about four times smaller than that 378 379 of the mother cell, thus the concentration of phosphatase facing the forespore is four times larger compared to the mother cell (Iber *et al.*, 2006). This concentration difference leads to 380 an effective increase in the ratio of IIE to the substrate AA in the forespore and is the primary 381 developmental trigger. The model did not include alternative triggers for the activation of σ^{F} 382 like effectors that are compartment specific expressed due to the genetic asymmetry (Feucht 383 et al., 2002) and thus cannot judge these effects. The allostery of the AB kinase activity 384 further amplifies the the different AA~P dephosphorylation dynamics in the two 385 386 compartments. Furthermore, the result implies that the allosteric system is optimised to 387 reduce the need of ATP (Iber et al., 2006).

A similar study has been performed by Igoshin et al. (2006), who examined the same 388 regulation system with more or less the same intermediate complexes. However, instead of 389 the allosteric nature of AB their model focused on the so-called 'dead-end complex' of 390 AA~P-AB-ADP. The dead-end complex serves to buffer the concentration of AB such that 391 AB is unable to titrate σ^{F} . Igoshin *et al.* (2007) constructed a model with 27 states, 55 392 reactions and 12 independent parameters. Analyses of the steady state concentration of σ^{F} 393 394 under various conditions revealed that for certain physiologically feasible circumstances the system shows a hysteretic response, *i.e.*, activation of the system is more easily achieved than 395 396 deactivation. The hysteretic behaviour necessitates a higher concentration of AA over AB (considering monomers) in the model, a situation that could arguably take place in the 397 398 forespore since AB is much more unstable than AA (Dworkin, 2003, Igoshin et al., 2006).

The authors suggest that the dead-end complex of AA~P-AB-ADP is effectively causing 399 increased σ^{F} activity in the forespore and that the stability of the complex serves to conserve 400 ATP. A saving of ATP was also implicated by Iber et al. (2006) with respect to the allosteric 401 forms of AB. However, how the submicromolar concentrations of the AB-AA complex may 402 contribute to the conservation of ATP present in millimolar concentrations is not discussed. 403 404 Both studies by Iber et al. (2006) and Igoshin et al. (2006) explain the compartment specific 405 developments during sporulation, however, they assumed different mechanisms, Iber et al. 406 with AB allostery and Igoshin et al. with AB-AA dead-end complex.

407

408 Competence

Besides sporulation, the development of competence is one of the best studied phenotypic 409 410 adaptations of B. subtilis and is a widely used example for stochasticity in survival 411 strategies (Raj and van Oudenaarden, 2008; Leisner et al., 2008). During late exponential 412 growth when nutrient availability decreases and the population density increases, about 10 % 413 of the individuals in a *B. subtilis* population become competent (Hamoen *et al.*, 2003). Competence development is governed by ComK, a transcriptional factor that regulates the 414 415 expression of more than 100 genes including those required for DNA binding and uptake (Hamoen et al., 2002; Ogura et al., 2002; Berka et al. 2002). As shown in Figure 1, comK 416 417 expression is controlled by a positive feedback loop, since ComK binds to its own promoter, and by a negative feedback loop via ComS. ComS protects ComK from degradation by the 418 419 MecA/ClpC/ClpP proteolytic complex. Nevertheless, ComK inhibits expression of *comS* (Maamar and Dubnau, 2005; Süel et al., 2006). Development of competence is tightly 420 connected with the activation of the phosphorelay (Lopez et al., 2008). The expression of 421 *comK* is inhibited by AbrB and thus *comK* expression can only be effectively activated if the 422 concentration level of AbrB is sufficiently reduced by inhibition via Spo0A~P (Hamoen et 423 al., 2003). However, further increases in concentration of in Spo0A~P are leading to a 424 derepression of rok, an inhibitor of comK expression, and thus again development of 425 competence is blocked (Hamoen et al., 2003). Development of competence is additionally 426 regulated via pheromones and quorum sensing (Lopez et al., 2008). The pheromone ComX 427 428 activates autophosphorylation of ComP which activates the transcription factor ComA by 429 transfer of the phosphate group (Hamoen et al., 2003). A second pheromone PhrC (also: 430 competence stimulating factor, CSF) promotes competence by inhibition of RapC, the ComA~P phosphatase (Lopez and Kolter, 2009). ComA~P induces the expression of ComS, 431 thus stabilizing ComK but also induces expression of PhrA-RapA (Lopez et al., 2008). 432 ComA~P as an input to the phosphorelay was examined by Jabbari et al. (2010) while 433 434 Schultz et al. (2009) simulated the dynamic sequential activation of competence and

435 sporulation respectively.

The competence system is an example for excitability: a small perturbation induces a 436 significant developmental response which however is only transient and the cell eventually 437 returns to vegetative growth (Süel et al., 2007; Lindner et al., 2004). Positive autoregulation 438 439 of ComK was found to be the most important factor for the transition to competence (Maamar and Dubnau, 2005; Smits et al., 2005). Süel and colleagues (2006) assembled a 440 model to investigate the importance of ComS for switching to competence. They added a 441 noise term to the equation of ComS generation and simulated the concentrations of ComK 442 and ComS. Their model predicted that if ComK positively affects transcription of comS then 443 444 the competence state becomes much more stable without affecting the probability to enter this stress pathway. Experiments with mutants, in which ComS is positively controlled by 445 446 ComK, revealed that 4.2 % of the mutant cells entered competence, similar to wild type cells with a percentage of 3.6 %. In accordance to the simulations, 88 % of the mutant cells were 447 448 locked in the competent state compared to 39 % of wild type cells. Next, Süel and colleagues (2007) have examined the factors controlling entry to competence and the duration of that 449 450 state. They found that the higher the *comK* expression rate, the higher the probability to enter competence. These findings apply until an oscillation-like regime with successive enter and 451 exit cycles is reached. ComS in turn determines the duration of competence that finally leads 452 to a bimodal distribution of competent cells. Additionally, they showed that after 453 sensitisation of the cell by environmental signals, it is noise that stimulates activation of 454 competence. They used an *ftsW* mutant which develops long filamentous cells that are 455 connected via a common cytoplasm. In this mutant noise is reduced due to the averaging 456 457 affect implied by diffusion while the physiological mean concentrations are not affected. Indeed it turned out that the probability to develop competence becomes lower with 458 decreasing noise. 459

Maamar and coworkers (2007) employed a stochastic simulation approach, using the 460 Gillespie algorithm (Gillespie, 2007), to address the question whether the noise is of 461 transcriptional or translational origin. They performed experiments in which transcription is 462 463 improved and translation of ComK is reduced, resulting in conditions with relatively constant ComK levels. The analysis revealed that fewer cells became competent in the 464 465 engineered strains, showing that increased levels of transcription result in less competence. The authors argue that the initiation of competence is controlled by noise, and that the source 466 of the noise can be attributed to irregularities in transcription. An interesting condition of 467 competence is that the phenotype can only be developed within a certain time window in 468 469 culture conditions (Maamar et al., 2007; Leisner et al., 2007). This idea requires that the system is robust most of the time to become sensitive and excitable to gene expression noise 470

13

471 under specific conditions.

Leisner et al. (2009) examined the system from a different perspective by addressing 472 the question under which condition bistability arises. They ignored the negative feedback 473 loop of comS transcriptional regulation by ComK and used ComS as an external parameter 474 that represents quorum sensing signals. Their results imply that during exponential growth, 475 476 when ComS levels are low and ComK degradation is high, the system is monostable which indicates that variation in the protein concentrations are not sufficient to activate competence. 477 478 Only if ComK levels increase due to reduced degradation the system can enter the transition 479 state leading to bistability as response to noise in expression (Leisner et al., 2009).

480

481 **Production of extracytoplasmic proteases**

One of the alternative responses following Spo0A activation is the increase in expression 482 of the extracellular protease AprE (subtilisin) and Bpr (bacillopeptidase) (Murray et al., 483 2009, Lopez et al., 2008, Lopez and Kolter, 2009). Initiation of sporulation can be delayed by 484 the production of extracellular proteases, which break down proteins in the environment to 485 provide the cells with additional nutrients. The pivotal regulator is DegU. In its 486 phosphorylated form as DegU~P the expression of exoproteases, among them AprE, is 487 stimulated while competence is suppressed (Murray et al., 2009). DegU~P is phosphorylated 488 by DegS~P which in turn autophosphorylates in response to as yet unknown environmental 489 490 signals. Regulation of DegU is integrated in the phosphorelay network, as well. DegQ, an activator for DegU phosphorylation by DegS~P, is activated by ComA~P (Murray et al., 491 492 2009). Thus, DegU is connected with the cell density measurement via ComX (Murray et al., 2009). Veening et al. (2008a) conducted several experiments and used mathematical 493 494 modelling to detect the original signals and the mechanisms that regulate the dynamics of AprE expression. Transcription of the proteases is additionally inhibited by AbrB. This 495 496 inhibition is compensated upon phosphorylation of Spo0A at early stages in the preparation of sporulation (Veening et al., 2008a). Veening et al. (2008a) have built a mechanistic model 497 498 of the DegSU two-component system and used experimentally measured AbrB levels to empirically include regulation through sporulation signals. Deterministic analyses uncovered 499 bistability of DegU depending on the ratio of phosphorylated/non-phosphorylated protein. 500 The model predicted an increase in AprE levels until 20 hours of growth. Indeed that 501 502 prediction was subsequently verified by the authors in microculture experiments (Veening et al., 2008a). 503

504

505 σ^{B} -response – Partner switch mechanism

506 The partner switch mechanism, including proteins on the spoIIA operon, is based on

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exclusive mutual interaction of an anti-sigma factor with both a sigma factor and an anti-507 anti-sigma factor (Hecker et al., 2007, Price, 2002, Hecker and Völker, 2001). In addition 508 to the irreversible initiation of sporulation, the principle of partner switching mechanism 509 observed for σ^{F} is also seen in other adaptation responses. One of them is the general stress 510 response, which is mediated by σ^{B} and activated by a whole collection of environmental 511 challenges including the transition from exponential to stationary phase (Price, 2002, Hecker 512 et al., 2007). Although both share a similar regulation scheme, they display critical 513 mechanistic differences which reflect the different physiological needs of the cell (Price, 514 2002). The anti-anti-sigma factor RsbV (V) is homologous to SpoIIAA and the anti-sigma 515 factor RsbW (W) corresponds to SpoIIAB. Comparable to the *spoIIA* interaction network the 516 phosphorylation status of V regulates the available pool of free σ^{B} . However, while there is 517 only one phosphatase of SpoIIAA, SpoIIE, which is activated following the formation of the 518 polar septum (Dworkin, 2003, Feucht et al., 2002), two phosphatases dephosphorylate V~P 519 520 in a stress dependent manner (Hecker *et al.*, 2007). RsbU (U) reacts largely to physical stress while RsbP reacts to nutritional stress (Hecker et al., 2007, Price, 2002). The main difference 521 in the structures of the sporulation and general stress response is the dead-end complex of 522 AA~P-AB-ADP, which does not exist for V~P-W-ADP because the latter complex can 523 quickly exchange nucleotides (Price, 2002). Since the dead-end complex is missing, the 524 general stress response is readily reversible. This reversibility is necessary since the 525 physiological task of σ^{B} is to respond to temporary cues from the environment. The second 526 difference is the transcriptional feedback loop since all three proteins, V, W, σ^{B} , are arranged 527 in an autoregulated operon (Price, 2002). Following $\sigma^{\rm B}$ activation by energy stress the 528 increased expression of σ^{B} and V provides the potential for further amplification of σ^{B} 529 activity. In contrast σ^{B} driven W expression on the operon counteracts the positive feedback 530 loop since W deactivates σ^{B} by dimension. Based on the analysis of the *spoIIA* operon, 531 Igoshin *et al.* (2007) compared the differences of σ^{F} and σ^{B} . Simulations showed that this 532 negative feedback by W results in a two stage response, *i.e.*, the full activity of σ^{B} is not 533 abruptly achieved as it would be without negative feedback. The positive transcriptional 534 feedback increases the capacity for regulation, *i.e.*, it maximises the differences in free σ^{B} 535 before and after stress activation (Igoshin et al., 2007). While Igoshin et al. (2007) included 536 RsbX, which is involved in negative regulation in response to environmental challenges 537 (Hecker et al., 2007), they did not include the partner switch that controls the activity of the 538 phospatase RsbU which is responsible for environmental stress response activation of σ^{B} . 539 540

541 **Operon organisation of stress responses**

542 Operon organization can improve the performance of stress response strategies. This was

examined by Iber (2006) or the spoIIA network and by Voigt et al. (2005) for the 543 phosphorelay with respect to the SinI/R dynamics. The implications of the co-regulation 544 hypothesis of the operon theory by Jacob and Monod (1961) has been tested by Iber (2006) 545 based on her model of the dynamics of the spoIIA network during sporulation (Iber et al., 546 2006). The central question addressed with the existing and validated model was how 547 548 sporulation efficiency is affected if noise in protein expression is either coupled or uncoupled among the proteins of the spoIIA operon (Figure 1). This coupling can, to a certain degree, 549 550 be justified by the assumption that ribosomes can continue protein synthesis on one mRNA 551 to a following protein coding region without dissociation and re-association rounds. These 552 conditions are met for the mRNA of AA and AB, which have an overlap of four bases. 553 Simulations of sporulation efficiency showed that the detrimental effects of expression noise 554 are more pronounced if protein expression is uncoupled. An operon organisation therefore reduces noise by means of co-expression (Iber, 2006; Tabor et al., 2008). This implies that 555 556 operon organisation would be disadvantageous for regulation of competence, in which noise 557 plays a purposeful role (Süel et al., 2006).

A conceptually related study has been published by Voigt *et al.* (2005), in which the 558 authors investigated possible dynamics regarding the co-regulation of *sinI* and *sinR* with a 559 special focus on evolutionary implications. As described earlier and shown in Figure 1, SinR 560 is a sporulation inhibitor and controls biofilm formation and SinI is the antagonist that 561 deactivates SinR (Bai *et al.*, 1993) A σ^{A} -dependent internal promoter upstream of *sinR* (P3) 562 establishes an excess of SinR over SinI molecules during vegetative growth. In the model 563 SinR represses activation of the promoter upstream of *sinI* (P1/2) that transcribes the whole 564 operon (sinI+sinR). These mutual negative feedback relations can generate a variety of 565 566 dynamics in SinI, ranging from a graded response to bistability, oscillation and pulse 567 response. The dynamics are most sensitive to the production rate of SinR and indeed a sequence comparison of several *Bacillus* genera shows a pronounced conservation of the P3 568 569 promoter region. The sporulation probability is determined by the efficiency of the P1 promoter as well as the SinI-R protein-protein interaction. Since different Bacilli are adapted 570 571 to distinct environments it seems likely that their tendency to enter sporulation evolved differently. Sequence comparison reflects this drift since the P1 promoter is very diverse and 572 573 SinI accumulated mutations that could potentially affect the dimerisation rate of SinI and SinR while still allowing for dimerization (Voigt et al., 2005). However, new experimental 574 575 findings challenge two model assumptions, namely that SinR inhibits the sinI (Chu et al., 2005) and the spoOA promoter (Kearns et al., 2004). These inhibitions are necessary for the 576 development of bistability, thus, either the SinIR network is not intrinsically bistable or there 577 are of yet unknown negative feedbacks. Nonetheless, the article by Voigt et al. (2005) 578

579 expands our understanding of σ -factor anti- σ -factor interactions and depicts the potential to 580 understand evolutionary tendencies that take place over years based on the dynamic events 581 of protein concentrations that occur within minutes at most.

582

583 Conclusion

The complexity of signalling in *B. subtilis* has motivated numerous studies that used mathematical modelling to elucidate principles and mechanisms of the cell's response to changing environmental conditions. Despite the apparent gap between the complexity of cell signalling networks and the simplicity of their models, many positive examples exist in which mathematical modelling has offered additional insights and in which the models provided guidance for the design of experiments.

For example, analyses of the phosphorelay by Bischofs *et al.* (2009) convincingly showed how the regulation is organised to optimise the information of available nutrient per cell. The combination of model and experiments by Maamar and co-workers (2007) could elegantly explain that temporal regulation of transcription controls the frequency of transition to the competent state.

The formation of heterogeneous subpopulations within isogenic populations (Dubnau 595 and Losick, 2006; Smits et al., 2006) and the question of how cell responses are determined 596 597 by past experiences (Wolf et al., 2008; Veening et al., 2008b) provide further challenges that motivate the application of mathematical modelling. Rather than studying individual 598 responses in isolation, it is also important to address questions about the interplay of 599 different environmental response strategies. An example in this direction is the work of 600 Schultz and co-workers (2009) that looked at sporulation and competence. Following on 601 from this, future studies should consider signalling between genetically identical individuals 602 603 and eventually address interspecies interactions (Bassler and Losick, 2006; Little et al., 2008). 604

The knowledge of many regulatory mechanisms can be transferred from E. coli to B. 605 subtilis. In some cases, however, due to their evolutionary distance these two model 606 607 organisms have developed different environmental response strategies. Spore formation in B. subtilis is one example for a strategy that exists in this organism, but not in E. coli, while in 608 other cases even protein homologues function in a surprisingly different way. An example is 609 610 CheY~P, which induces completely different chemotactic responses in E. coli and B. subtilis. This suggests that exciting problems remain that have to be addressed specifically 611 612 for B. subtilis. No doubt, this Gram-positive model organism provides plenty of challenges and exciting opportunities for mathematical modelling. 613

614

615 Acknowledgements

616 The authors like to thank Peter Raasch, Anja Möller, and Dinto José for stimulating

617 discussions and corrections on the manuscript. UWL, TM, UV, and OW acknowledge

support by the BMBF and IGdJ thanks NWO-ALW for support, all on the trans-nationalBaCell-SysMO project.

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Reaction diagram for the main signalling cascades discussed in this review. The figure shows the signal transduction that leads to switching of flagella rotation after binding of a ligand (Lig) (green) (Rao and Ordal, 2009), regulation of competence development (yellow)(Hamoen et al., 2003), the switch of the response regulator DegU to DegU~P (dark blue) (Murray et al., 2009), activation of σ^{B} mediated general stress response (grey) (Hecker et al., 2007), phosphorylation of SpoOA via the phosphorelay (dark red) (Piggot and Hilbert, 2004), and the reactions in the SpoIIA network towards commitment to sporulation (pink) (Errington, 2003). The upper part shows only interactions in the cytoplasm while the lower part indicates the genomic interconnections of the transcription factors (derived from DBTBS at http://dbtbs.hgc.jp). The environmental signals that lead to the activation of KinA-E, DegS and RsbUP are mostly unknown.



Hysteretic signal-response curve that can give rise to bistability. In the study of Igoshin et al. (2006) the authors tested dynamical properties of the availability of σ^F (response) as a function of the dephosphorylation rate of AA~P (signal). For particular parameter region of the dephosphorylation the system becomes bistable. Under such conditions the inactive state can easily switch to the active state characterized by a high σ^F availability at latest at a signal strength S_{on} (AA~P dephosphorylation rate threshold). However, the active state is robust against deactivation (decrease in AA~P dephosphorylation), since the signal strength S_{off} is reached at lower value compared to S_{on}. In the transition zone the response is highly sensitive to changes in the signal, with a sufficient perturbation the system can switch easily from the inactive to the active state.