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1 2 3 4 5 6 7 8	1 2 3 4 5 6 7 8	Optimization of Airfoil VOLUME/ISSUE	Engineering Optimization Vol. X, No. X, Month 200X, 000–000	
9 10 11 12 13 14 15 16 17 18	8 9 10 11 12 13 14	Optimization of <u>an</u> A Don	Airfoil Cooling System Using <u>a</u> Pareto ninance Approach Grzegorz Nowak	
19 20 21 22	15 16 17 18	Silesian University of Technology	y, Institute of Power Engineering and Turbomachinery, Gliwice, Poland	
23 24	19	Abstract		
25	20	The article deals with the optimization of the	airfoil internal cooling system in order to find the most efficient	Deleted: paper
26	21	distribution of passages to reduce thermal stre	ess and, at the same time, retain the temperature at a permissible	Formatted: Left
27	22	with the evolutionary algorithm, and thermo-	mechanical FEM simulations are used for the assessment of the	Deleted: ¶
28	24	particular cooling system candidates. Since th	he optimization involves several criteria, the multi-objective	
29	25	approach needs to be applied. The optimization	on process may focus either on the scaled function solution or on	Deleted: (
31	20	finding the front of optimal solutions (Pareto compared to the scaled function solution	optimal). In this <u>article</u> the latter approach is implemented and	Deleted:)
32	$\frac{2}{28}$	compared to the search runction solution.		Deleted: paper
33 34 35 36 37 38 30 41 42 43 44 56 51 52 53 45 56 57 58 50 60	29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46	Keywords: multi-objective optimizatio	on, evolutionary algorithm, airfoil cooling	



1					
2	1	• keeping stresses at a safe level			
3	2	• securing the proper durability and rigidity of the component			
4	3	Martin and Dulikravich (2001) put forward the following question: "Is it possible to			
5	4	design manufacturable turbine cooling configurations that simultaneously increase the turbine			
6	5	inlet temperature, decrease the coolant requirements, maintain material integrity and improve			
7	6	airfoil durability so that the engine capital and operating costs are reduced?"	Dele	ted:	
8	7	An application of the cooling system involves changes in the operational conditions of)
9	8	the component the machine and even the whole power generation unit. The changes affect			
10	9	temperature distributions stresses and in consequence the lifetime of components nower			
11	10	generation efficiency and machine complexity. In order to account for all these aspects a			
12	11	formulation of the optimization task has to involve many criteria and constraints. Because the			
13	12	parameters of the changes are related to different physical fields the optimization task			
14	12	becomes a multi objective and multi disciplinery one			
15	13	It is only in regent years that scientists become interested in the problems of optimization			
16	14	It is only in recent years that scientists became interested in the problems of optimization	Dela		
17	13	of the cooling systems of gas turbine blades. The reason for this situation was probably the	Dele	etea:	
10	10	nigh cost of optimization calculations, which results from the necessity of reliable			
10	1/	computational models that can predict both temperature and the failure of a blade. Lack or			
19	18	inaccessibility of high-efficient calculating machines precluded, until a certain moment, the			
20	19	necessary calculations. A substantial increase in the processor capacity of PC's and the			
21	20	development of parallel processing techniques have made it possible to deal with the problem			
22	21	on a bigger scale. Optimizing calculations concerning the components of the flow system of a	Dele	eted: s	
23	22	turbine (e.g. blades) mean having to carry out multiple flow- and thermal- analyses or	Dele	eted: e.g.	
24	23	conjugated tasks. Although precise solution of the processes influencing the optimization			
25	24	requires continuous development, the models used predict a correct trend in design changes.			
26	25	Since the optimization problem is a relative process, where the designs are compared to each			
27	26	other, the absolute values of the predictions are not always needed.			
28	27	The attempts to find the optimum choice of the cooling system made recently were			
29	28	focused mainly on convection cooling with the use of inner cooling channels. At the moment			
30	29	it is probably the only cooling mechanism that can be analysed in full. Other cooling systems			
31	30	e.g. film cooling, impingement cooling etc., because of the complexity of the phenomena	Dele	eted: e.g.	
32	31	taking place, are only analysed from the point of view of the "given state" (Garg, 2002), and			
33	32	only some chosen aspects are the subject of optimization, <i>e.g.</i> the outflow of the coolant from	Dele	eted: e.g.	
34	33	a single passage in film cooling. Talya <u>et</u> al. (2002) took film cooling into consideration in the	Dele	eted: t	
35	34	process of the profile shape optimization, but its structure was fixed and so were the inner	For	natted: Font: Italic	\neg
36	35	channels, which were only scaled according to the size and shape of the profile. For several	Dele	ted:	\neg
37	36	years now Dulikravich and his team (Martin and Dulikravich, 2001, Jeong et al., 2003 Dennis	Dela	atodi %	\dashv
38	37	et al., 2003a, b) have been doing research on various problems concerning optimization of			$ \longrightarrow $
30	38	turbine blade cooling with focus on flow- thermal- and strength criteria. The outcome of that		eted: et al	$ \longrightarrow$
40	39	research is the Multidisciplinary Computer Automated Design Optimization (MCADO). The	Dele	eted: et al	
40 Λ1	40	works are mainly concerned with optimization of the inner cooling channels (Dennis et al.,	Dele	eted: et al	
41 12	41	2003, Martin and Dulikravich, 2001) with a possible outflow of the cooling air at the trailing	Dele	eted: &	\neg
42 12	42	edge (Dulikravich et al., 1999). It can be seen in these works that, in spite of numerous	Dele	ted: et al	\neg
43	43	decision variables used in the calculations, the optimization process is strongly restricted with)
44 45	44	relation to changes in geometry, <i>j.e.</i> optimization affects for example the fillet radius of the	Dele	eted: i.e.	$\overline{}$
45	45	channel, the distance between the channels and the wall or the interspacing of the channels. In			
46	46	2003 Dennis <i>et al.</i> (2003a) presented an article on the optimization of the location of a large	Dele	eted: et al	
47	47	number of circular cooling channels. The location of these channels, however, was restricted	Dele	ted: paper	\neg
48	48	to a narrow area of the blade section close to the blade wall. The objective was to find a		Pupe.	
49	49	pattern for the distribution of the cooling holes so that the heat flux absorbed by the coolant			
50	50	could be maximally reduced with the temperature of the blade kept at the permissible level			
51	20	conte co matimung routeed, sint die temperature of the blade kept at the permissible level,			
52					
53					

and so that the amount of steam necessary for the cooling could be reduced, too. Dennis *et* al., (2003b) presented another interesting work on the optimization of channels in the shape of a serpentine with three returns of the cooling agent. The problem was dealt within 3D with the use of thermal- and strength criteria. The results revealed a great potential in the cooling system; the right choice of the shape and distribution of cooling channels does affect the amount of the cooling agent and thermal stress, and, consequently, the durability of the blade. Nowak and Chmielniak (2005) presented the optimization of the distribution and

dimensions of circular cooling passages, with their set number. In this case the approach was that the cooling holes could move freely in the blade cross-section with feasibility criteria retained. In later works (Nowak et al., 2007, 2008) the problem of channel optimization was expanded to a multidisciplinary task including thermal- and strength- states with relation to economic criteria. The latest work of Verstraete et al. (2008) presents attempts to connect cooling channel optimization tasks with the thermal- flow- conjugated task. The objective of this approach is to increase the credibility of the boundary conditions formulated at the blade surface.

The problems of the optimization of the cooling systems for the airfoils of heat turbines usually involve a relatively large number of decision variables together with a complex, nonovert and sensitive to even small changes in parameters response of the system being analysed. That response, e.g. in temperature, stresses or other values, is not monotonic and is characterised by a great number of (local) extremes, which is a major problem for many optimization methods based on the gradient approach (Mueller, 2002). In these situations stochastic methods are preferred, which in fact can be seen in all the works mentioned in this article

The most often used stochastic method is the evolutionary algorithm, which, in spite of its downsides, is best suited for dealing with complex technical problems. A slightly different optimization method, also stochastic, was presented by Dennis et al. (2003a). The method is called Indirect Optimization based on Self Organisation (IOSO), and is a combination of the Response Surface Method with the evolutionary approach.

In this <u>article</u> the problem of optimization of the spacing and diameter of cylindrical cooling channels is dealt with in the multi-objective aspect with the use of various ways to run the evolution algorithm (different solution quality assessment methods). The results of the single-objective approach with objective function scaling and of the approach based on Pareto domination are presented. Because the solutions of multi-objective tasks are often ambiguous, the results are shown as a set of non-dominated solutions, from which the user can choose the final solution. The optimization task is based on the evolutionary algorithm with the use of the commercial solver FEM (ANSYS) to predict thermal and strength fields.

The Evolutionary Optimization

The notion evolutionary algorithm encompasses a whole class of numeric methods based on the mechanisms of natural selection and heredity. They combine the evolutionary principle of survival of an individual which is best adapted with the systematic, though randomised exchange of information (Goldberg, 2003). Algorithms of this type process populations of individuals which represent potential (though of a different quality) solutions to a problem. The essence of the genetic algorithm is to get, in subsequent generations, individuals with increasingly higher values of the fitness function. For this kind of process to take place, the subsequent generations have to change but the changes do not occur at random. The transformation of the present (parental) generation into the offspring generation takes place through a mathematical interpretation of the reproduction and mutation processes known from biology. How individuals contribute to these processes and what chances of survival they have is controlled by a selection procedure. The chance of survival, together

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2	1	with the chance of passing its own features on to the offspring generation, depend on the	Deleted: their
3	2	quality of the individual (its fitness).	
4	3	The structure of the individual plays the key role in the evolutionary optimization. So it must	
5	4	reflect all the design parameters which take part in the optimization process. The values of the	
6	5	parameters are most often not used directly, rather than encoded either in binary form or as a	
7	6	floating point number. In the first case the individuals are structured as strings of bits, whereas	
8	7	the latter requires vector form.	
9	8	Each individual is assessed to determine to what extent it meets the criteria posed. In the	
10	9	airfoil cooling system optimization, any relocation of channels and/or change in their size	
11	10	affects temperature distribution, stresses, cooling agent consumption or other values. On these	
12	11	grounds the evaluation criteria are formulated.	
13	12		
14	13		
15	14	Multi-objective optimization	
16	15	As has been mentioned before, the presence of the blade cooling system, apart from	Deleted: it
17	16	positive effects, causes also some negative phenomena. The objective of any optimization is	
18	17	to strengthen the former and eliminate or reduce the latter. This calls for having to meet many	
19	18	criteria which all contribute to the proper and efficient operation of both a single component	
20	19	and the entire machine. Moreover, as these objectives are often contradictory, the cooling	
21	20	system should be designed with consideration of possibly all the phenomena and parameters	
22	21	which affect the operation of a machine. Multi-objective optimization becomes essential,	Deleted: a must
23	22	One of the ways to deal with this type of tasks is task scaling and the use of the single-criteria	
24	23	algorithm, which involves a multi-dimensional objective function including all the optimised	
~ -			

parameters. Owing to this solution a single configuration of design parameters (the structure of the cooling system), which gives the extreme value of the objective function, is the result . It turns out, however, that this approach may be ambiguous because, taking all the optimization criteria into consideration, it is impossible to state beforehand which of the solutions is the best. There is a group of solutions which differ only in the aspect of quality with reference to specific criteria. These are the so-called non-dominated solutions, *i.e.* it is impossible to find better solutions that would meet all the criteria simultaneously. Non-dominated solutions are called Pareto optimal and their corresponding set of vectors containing the objectives is referred to as *Pareto front*. It can be seen that a multi-objective task usually has many solutions, from which, on the grounds of additional premises, the final one is selected.

From the mathematical point of view, we look for design parameters for which their corresponding objectives are non-dominated. The domination of vector $\mathbf{X}=\{x_1, x_2,..., x_n\}$ over vector $\mathbf{Y}=\{y_1, y_2,..., y_n\}$ in the case of the minimisation task (Fig. 1) can be formulated as follows (Wagner <u>et al.</u>, 2007):

$$\forall i \in \{1,..,n\}: x_i \leq y_i \text{ and } \mathbf{X} \neq \mathbf{Y}$$

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Numerical Tests

Test calculations were made for the C3X blade mentioned above, with the use of the evolutionary algorithm.

Evolutionary algorithm

The algorithm used for the search process was based on real-number coding of the design parameters. The operation of the change of individuals was realised by means_of recombination and mutation processes. The first of these processes was used as weight averaging of selected parental individuals:

$$\begin{bmatrix} a_1, a_2, \dots \end{bmatrix} \xrightarrow{recombination} \begin{bmatrix} m_1a_1 + (1 - m_1)b_1, m_2a_2 + (1 - m_2)b_2, \dots \end{bmatrix}$$

$$11 \qquad \begin{bmatrix} b_1, b_2, \dots \end{bmatrix} \xrightarrow{recombination} \begin{bmatrix} (1 - m_1)a_1 + m_1b_1, (1 - m_2)a_2 + m_2b_2, \dots \end{bmatrix}$$

 $(m_i \rightarrow \{0,1\}),$

where the weight m_i is chosen randomly for each *i*.

The mutation consisted in a random disturbance introduced into the vector of design parameters. The size of the disturbance, according to Michalewicz (1999), got smaller in proportion to the number of iterations (population number):

 $\begin{bmatrix} a_1, a_2, \dots \end{bmatrix} \xrightarrow{mutation} \begin{bmatrix} a_1 \pm \varepsilon_1, a_2 \pm \varepsilon_2, \dots \end{bmatrix}$ $\varepsilon_i = \varepsilon_{\max} \left(1 - RND^{\left(\frac{1-k}{K} \right)^b} \right) \quad (\varepsilon_{\max} \to \{0, 1\})$

where ε_{max} is the maximum (normalised) disturbance value, RND is the random variable with a uniform distribution, k/K is the ratio of the present iteration number to the maximum number of iterations to be carried out, and b is the constant parameter. Both operations occur with a specific probability, which is a parameter of the algorithm.

Fixed boundary conditions on the outer surface resulting from experimental research were assumed for a given profile. The values were given for 86 locations around the blade at its mid-height and between them a linear approximation was used. In the span-wise direction the boundary conditions were constant. The heat exchange on the surface of the channels was determined on the grounds of pipe-flow. Another assumption was that all the channels were fed with air of the same parameters and that in each of them the same fall in pressure is realised. Owing to this, Nusselt number was defined and then the heat transfer coefficient, which was constant in the whole channel. Following the experimental report of Hylton *et al.* (1983) the Nusselt number in a passage was found with the Dittus-Bolter equation (Hylton et *al.*, 1983):

$$Nu = 0.023 \text{Re}^{0.8} \text{Pr}^{0.4}$$

(2)

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On the grounds of the dependence which determines how the agent is heated in a pipe with a constant temperature, the coolant local temperature was defined (Lienhard IV and Lienhard V, 2008):

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 $T(z) = (T_{in} - T_{wall}) \exp\left(-\frac{h\pi d}{mc_p}z\right) + T_{wall}$

Wall temperature T_{wall} was an average for the whole channel and originated from the previous

iteration. To obtain the wall temperature, thermal calculations were performed twice, firstly,

for assumed T_{wall} and then with the computed one. This approach made it possible to predict

condition assessment can be introduced to make them more reliable, the simplified description

the wall temperature with satisfying accuracy. It has to be stressed that a mere consideration of constant boundary conditions at the external surface taken from the experiment, together with the Dittus-Bolter relation (2) for internal passages is a simplification of the actual problem. In reality a change in the cooling system structure affects thermal boundary conditions for the external flow. To take into account changes in the external flow, a Conjugate Heat Transfer predictions need to be conducted. This, however, is time consuming and, for the time being excluded from optimization tasks. On the other hand, although a lot of improvements in the boundary

of the problem seems to be appropriate for the testing of optimization methods.

Cooling system optimization is carried out for the blade C3X (Fig. 2), known from literature (Hylton <u>et al.</u>, 1983). It is originally equipped with 10 cylindrical internal cooling passages. The location of each of the passages can be described with three variables (2 coordinates of the centre and radius).

These values are the design parameters and, obviously, affect the structure of the individual. So the optimization problem is formulated and solved over a 30 dimensional design space. As Michalewicz's work (1993) shows, the real-number coding of technical problems of a continuous character is more beneficial and efficient. It has been confirmed by the author's own studies as well. Because of that, the task of optimization is dealt with the use of this type of variable representation. Earlier studies showed that the use of Cartesian coordinates is ineffective in domains as complex as the airfoil cross-section. Modification of the individuals due to the evolution within the global Cartesian system leads to a very high fraction of the population to violate the constraints. That is why the variables describing the channel are defined in a local curvilinear coordinate system, associated with the blade (Nowak G., Wróblewski W., 2007). In this case the axis of abscissa follows the airfoil's suction side and the axis of ordinates is always perpendicular to it. The coordinates are additionally normalized. In this way the individual's genotype renders the structure of the cooling system in a unit square.

Evaluation

The choice of optimization objectives was determined on the basis of the airfoil's durability and the thermal efficiency of the whole cycle. To reduce deterioration effects (oxidation and corrosion) within the material, it was important to provide operation at the lowest component temperature possible. This temperature, on one hand, must not exceed the permissible level. On the other hand, a lower temperature results in higher material limits and extends the lifetime of the hot gas path components. The life increase can be significant for modern aero engines operated at very high gas temperature. Although in the case study the operational temperature is too low to induce the deterioration effects mentioned, it was decided to take the maximum material temperature into account to show possibilities of its reduction in parallel with other objectives. Another factor influencing the component's life is the stress level, either maximum tensile or equivalent one. The former is responsible for the

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fracture propagation, the latter - for the fatigue and creep process. Which factor prevails depends on the material behaviour. In this work it was decided to consider the stress level in the form of its relative value called the failure factor, which is a ratio of the actual stress components to the allowable (desired) ones.

 $s_{\sigma} = \frac{\sigma_{\max}^{i}}{\sigma_{all}^{i}}$ The allowable stress components were assumed as linear functions of the blade temperature. For the normal components the allowable stress changed in the range of 350-180 MPa within the temperature interval of 400-800 K. For the shear stress the change was 200-100 MPa.

The application of a cooling system leads to a cycle efficiency drop which results from air extraction from the compressor. The air is then directed into a component being cooled, and finally the turbine flow path. The efficiency drop can be reduced by a decrease in the coolant mass flow.

The optimization calculations were made for two ways of algorithm realisation. One was based on the translation of a multi-objective optimization problem into a single-objective one by means of a weighted sum of objectives and, in consequence, it used the singleobjective evolutionary algorithm. The other employed the method of Pareto domination in a multi-objective algorithm. In both cases, three values, which reflected the critical aspects of blade operation, were the subject of optimization: maximum blade temperature (T_{max}) , maximum failure factor (s_{α}) and the total mass flow of the coolant (*m*). The stress involved in the failure factor resulted from thermal load only. The objective was to minimize all the values. In the case of scaling, the objective function was formulated as a weighted sum of the component functions.

$$f = \sum_{i} w_i f_i \quad \text{where} \quad \sum_{i} w_i = 1 \tag{4}$$

The component functions are of the same form:

$$f_i = (y_i - y_{ti})^2 \quad \text{where} \quad y_i = \{T_{\max}, s_\sigma, \dot{m}\}$$
(5)

The values marked with index t are the target values of the parameters, and for the calculations presented they are, respectively : 650K, 0.9, 50g/s. The fitness value formulated as:

$$F = N - \frac{n_d}{\left(n_{ds} + 1\right)} \tag{6}$$

was determined for the multi-objective task on the grounds of the assessment of the objective vector of the form:

j

$$\mathbf{V} = \left[\frac{T_t}{T_{\max}}, \frac{s_{\sigma \pi}}{s_{\sigma \max}}, \frac{\dot{m}_t}{\dot{m}}\right] \tag{7}$$

where N is the population size, n_d is the number of individuals that dominate a given solution, and n_{ds} is the number of the individuals dominated by the assessed one. This evaluation is shown in Fig. 1 for X_1 solution. The individuals enclosed within the lower-left rectangle dominate over X_1 , whereas those within the top-right one (in Fig.1 only X_5) are dominated by X_1 .

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Preliminary calculations showed, however, that there is a need to complete the individual
 assessment procedure with a penalty function to modify the values of the parameters being
 optimised, should they exceed permissible values.

Since the optimization is carried out with an automatic model generation, the user's influence on the mesh reliability is highly limited. To keep the results accuracy on an acceptable level, it is necessary to perform the FEM structural computations with higher order elements. The reason for this is that <u>the high thermal gradients</u>, which result from <u>the cooling</u>, produce, high

8 stresses limited to a small area. If linear elements are used, the stresses are averaged over the 9 element, and in consequence the results can be substantially incorrect. The stresses (or failure 10 factor) can be significantly underestimated in critical locations. The application of mesh with 11 nonlinear elements is however much more computationally expensive both in terms of time 12 and computer resources.

14 Results

The optimization calculations carried out for profile C3X provided new configurations of the cooling system. The configurations differ from the original structure in the placement of individual channels and their size. The results show that similar effects, from the point of view of the optimization criteria, can be achieved with various distribution and even various number of cooling passages. The number of channels varied in the course of the search process usually between 7 and 10 although there were individuals with 4 or 5 passages. A higher number of cooling channels causes a fall in the blade temperature but usually generates higher failure factors and, in the case of larger diameters, increases coolant consumption. In the case of configurations with fewer passages the tendencies are opposite - less cooling results in a lower stress level and reduced coolant usage.

From the point of view of the optimization criteria, the new configurations of the cooling system are more functional. All the optimised values have been improved (compare Fig. 3 and Fig. 4). The maximum temperature of the blade fell by 8K with failure factor drop from over 1.16 to below 1.05, and with almost 45% reduction in the total coolant mass flow (from 90g/s in the reference case to less than 50g/s in the optimised one).

In the case of the method using the weighted sum of objectives, the solution of the optimization task is obtained with a maximum value of the fitness function. This solution, however, depends closely on how the objective function is formulated. Even a slight change of weights in formula (4) leads to a different channel distribution. This feature of the method usually requires some test computations in order to adjust the weights within the objective function. It is more vivid in the cases where specific objective spaces are of a different range. It may happen that a huge change of one objective can affect the objective function in the same manner as slight change in another one. The algorithm will promote an objective that requires less change to obtain a bigger effect. Different weight sets may give comparable objective function values in which different criteria are strengthened. So the choice of weights can be time consuming and is specific to the task in question.

In the case of the method based on Pareto domination, the result is a set of *p*-optimal solutions which best meet specific criteria. The calculations which were carried out provided a set of 16 non-dominated solutions, some of which are presented in Fig. 5. The results are presented also in the objective space (Fig. 6) in the form of a class scatter chart. The number of non-dominated individuals is too small to generate a continuous 3D surface plot, so the chart presents the Pareto front in temperature-failure factor planes for several classes of the coolant mass flow. This figure shows that intensive cooling (low temperature) requires increased coolant mass flow and induces higher failure factors. The opposite tendency is visible for less cooling. If the failure factor is limited to 1, which can be treated as a value that results in a nominal lifetime, there are three configurations which fall in this range. All of

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them are cooled with significantly lower amount of air (below 60 g/s) if compared to the reference case and in two of them the maximum temperature of the blade is also lower by 15-17K. The failure factor limitation is however not obeyed by the single-objective solution for which the value is 1.049 despite very low coolant consumption. Since the failure factor seems to be the most important from the point of view of components' lifetime further optimization is required, which would need weight changes within the objective function. Decrease of the failure factor results in an increase of lifetime. Similar tendency can be observed for the maximum material temperature of the hot components.

It has to be stressed that during the optimization process specific cooling candidates were evaluated on the basis of relationship (6) only, and no penalty method, regardless of any particular objective value, was used. The above selection was made for the final generation to present the solutions which were situated in an assumed range of the objective space. This space is usually limited by permissible values of temperature, the failure factor or other parameters. The structures of the cooling configurations obtained differ from each other according to their location on the Pareto front (Fig. 6). A close distance along the surface provides similar solutions, whereas remote solutions result in highly different cooling candidates. In the case of a low blade temperature the cooling system usually consists of ten bigger passages which provide a high coolant mass flow. Such solutions generally produce a higher thermal stress and in turn a higher failure factor (the actual stress growth is higher than the allowable stress due to temperature reduction). At the other end of the front, for low failure factor values, the cooling candidates are composed of a fewer number of channels (4-5 passages), whose size is small. In consequence, the coolant mass flow is limited, which makes the airfoil's temperature rise.

Comparing the solution for both approaches with the same measure (weighted objective function in the single-objective optimization) the single-objective method provided a cooling configuration slightly worse (less than 1%) than the best Pareto candidate. This solution belongs to the Pareto front (the 2 cross-marked individuals in Fig. 6 with lower temperature and failure factor objectives use more coolant) and it does not dominate any individual within the multi-objective non-dominated set. The specific objective values and single-objective function values for both optimization approaches and the reference case are given in Table 1.

In both optimization techniques the solution time was comparable although the number of generations calculated was different. In the case of the single-objective approach the algorithm converged after about 35 generations, whereas the multi-objective one required about 60-70 generations. Both tasks were carried out with a population of 60 individuals. However in the first case the number of cooling candidates to be assessed per generation was essentially higher than in the other. The reason is that in the single-objective algorithm only 5% of the best individuals were copied to the successive population, whereas in the multi-objective approach it was the whole Pareto front. In the initial stage of the search process the non-dominated set was quite small (8-10 individuals) but as the algorithm advanced, the front increased, until it filled up the whole population.

Numerical simulations have proved the efficiency of both approaches but the Pareto domination method is characterised by one specific advantage. To function properly, the method of objective function scaling must be duly matched to the character of the task, and this calls for a great number of tests to determine how individual criteria affect the process and direction of optimization. In the multi-objective approach it is necessary to compare the objectives without having to fix the impact of the individual criteria on the direction of the search.

50 Conclusions

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2	1	The objective of the study was to compare how two different approaches to the	
3	2	optimization task of the cooling system of the blades of gas turbines function when numerous	
4	3	criteria have to be met. The method based on objective function scaling was compared with	
5	4	the method of Pareto domination. The former provides a single solution which depends on the	
6	5	choice of the weights in the objective function; the latter offers a set of non-dominated	_
1	6	solutions, <i>i.e.</i> solutions which best meet specific, individual criteria. The evolutionary	
8	7	algorithm was used for the optimization, which is a typical approach while looking for a	
9	8	Pareto front.	
10	9	Numerical simulations have shown that both approaches are equally efficient when it	
11	10	comes to the time of solution finding, but an essential advantage of the Pareto domination	
12	11	method is to be noticed. It does not require the knowledge of how the optimised parameters	
13	12	depend on each other because it is only the specific parameters themselves or the functions on	
14	13	which they are built that are subject to comparison. The knowledge of the dependence is	
15	14	essential in the weighted single-objective method. The weight values for specific criteria	
16	15	structure the running of the algorithm and have a direct influence on the final result of the	
17	10	optimization process. A proper determination of the objective function usually requires some	
18	1/	preliminary tests which should be accepted as part of the optimization cost. The	
19	10	the multi-objective Derete dominance method seems to be the right choice	
20	20	the multi-objective rateto dominance method seems to be the right choice.	
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Case	T_{max} K	S .	m o/s	f
Reference	706 7	1.163	90 0	9.06
Single-Objective	698.7	1.049	49.4	9.83
Multi-Objective	689.6	0.982	55.0	9.89

2

Figure 1. Pareto domination

Figure 2. C3X airfoil

Figure 3. Temperature (left) and failure factor (right) distribution for original cooling system configuration

Figure 4. Temperature (left) and failure factor (right) distribution for single objective optimization

Figure 5. Selected *p-optimal* solutions (failure factor contour)

Figure 6. Pareto front

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C3X airfoil 323x248mm (96 x 96 DPI)

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Temperature (left) and failure factor (right) distribution for single objective optimization 235x139mm (150 x 150 DPI)



