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DEBtox theory and matrix population models as helpful tools in understanding the interaction between toxic cyanobacteria and zooplankton

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Abstract

- Bioassays were performed to find out how field samples of the toxic cyanobacteria Microcystis aeruginosa affect Moina micrura, a cladoceran found in the tropical Jacarepagua Lagoon (Rio de Janeiro, Brazil). The DEBtox approach has been proposed for use in analysing chronic toxicity tests as an alternative to calculating the usual safety parameters (NOEC, ECx). DEBtox theory deals with the energy balance between physiological processes (assimilation, maintenance, growth and reproduction), and it can be used to investigate and compare various hypotheses concerning the mechanism of action of a toxicant. Even though the DEBtox framework was designed for standard toxicity bioassays carried out with standard species (fish, daphnids), we applied the growth and reproduction models to M.micrura, by adapting the data available using a weight-length allometric relationship. Our mod-11 elling approach appeared to be very relevant at the individual level, and confirmed 12 previous conclusions about the toxic mechanism. In our study we also wanted to assess the toxic effects at the population level, which is a more relevant endpoint in 14 risk assessment. We therefore incorporated both lethal and sublethal toxic effects 15 in a matrix population model used to calculate the finite rate of population change as a continuous function of the exposure concentration. Alongside this calculation, 17 we constructed a confidence band to predict the critical exposure concentration for population health. Finally, we discuss our findings with regard to the prospects for 19 further refining the analysis of ecotoxicological data.
- 21 Key words: allometry, DEBtox models, matrix population model, Bayesian
- 22 inference, Moina micrura, Microcystis aeruginosa

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23 1 Introduction

One of the main objectives in ecotoxicology is to provide an estimation of safety parameters, e.g. No Observed Effect Concentration (NOEC) and x% Effect Concentration (ECx), that can be derived from standardarized toxicity tests (OECD, 1998; ISO, 2000). These approaches have been criticized for many reasons: 1) NOEC and ECx usually focus on a single endpoint (mortality, growth or reproduction); 2) the standard tests involve a fixed exposure time, irrespective of the properties of the chemical being tested; 3) they generally 30 use only a few standard species, which may not be relevant to the ecosystem 31 being investigated; 4) NOEC and ECx are based on purely descriptive regression models, and are unrelated to the physiological processes of the organisms 33 that are being tested, and to the toxicokinetics of the compound being tested 34 (Chapman, 1996; Kooijman & Bedaux, 1996; Péry et al., 2002; Jager et al., 2004, 2006). Biology-based models, such as DEBtox (Dynamic Energy Budget Theory applied to toxicity data) (Kooijman & Bedaux, 1996), have been pro-37 posed to overcome these shortcomings: 1) this modelling approach is based on the concept of No Effect Concentration (NEC), which is common to several biological processes and consequently to several sublethal endpoints (e.g. growth and reproduction); 2) DEBtox models take into account the toxicokinetics of the chemical being tested; 3) they were originally developed for a standard panel of species, but they can be adapted to others; 4) DEBtox theory is a 43 mechanistic modelling approach, based on several assumptions about how the test compound disrupts the energy balance between the various physiological processes.

In addition, ecotoxicology is now attempting to assess the impact of chemical

compounds not only on individuals, but also at higher organizational levels. For example, the population level is particularly relevant when different life stages may display different susceptibilities to toxic compounds (Emlen & Springman, 2007). In this case, the finite rate of population increase λ is considered to be a robust endpoint (Forbes & Calow, 1998). Various methods can be used to relate the effects of a compound on individuals to its impact on the finite rate of population increase. The one we chose was the matrix population model approach, which has already been successfully combined with DEBtox models (Lopes *et al.*, 2005; Billoir *et al.*, 2007).

Cyanobacteria are some of the most ancient organisms on Earth ($\simeq 4$ billion years), and the first to develop the ability to fix atmospheric carbon and release oxygen through photosynthesis. Another distinguishing characteristic of cyanobacteria is the fact that they produce secondary metabolites with toxic properties, known as cyanotoxins (Carmichael, 1992). Cyanotoxins have been responsible worldwide for deaths of wild and domestic animals, and also for some human fatalities (Ressom et al., 1994; Jochimsen et al., 1998; Carmichael et al., 2001). The most common cyanotoxins are the hepatotoxic peptides, which are produced by some genera of freshwater bloom-forming cyanobacteria such as *Microcystis*, *Anabaena* and *Oscillatoria*. In spite of the effects observed in non-target organisms, such as mammals, one of the most gener-67 ally accepted hypotheses to explain the evolutionary role of these toxins is that they are produced to protect cyanobacteria against their main predators, including the herbivorous zooplankton, such as Daphnia. According to this hy-70 pothesis, cyanotoxins act as chemical defenses against zooplankton predators, by decreasing their fitness (Lampert, 1981, 1987). The interaction between cyanobacteria and zooplankton has been widely used as a model system to

study the evolutionary role of cyanotoxins. Also, since cyanotoxins also pose some risk to human health, the ecotoxicology of the cyanobacteria-zooplankton system is used to study the mechanisms of action of these toxins in aquatic organisms, and can be used as the basis for guidelines for environmental health and water quality as well.

In this study, we used ecotoxicological data from the study of Ferrão-Filho & Azevedo (2003), which reported the effects of naturally-occurring cyanobacteria from a hypereutrophic coastal lagoon in Brazil, including data from lifetable and growth experiments with *Moina micrura* Kurs, a tropical freshwater cladoceran. In contrast to the big temperate cladocerans, such as *Daphnia* (2.0-4.0 mm body size), *M. micrura* is much smaller (0.8-1.0 mm body size), reaches maturity after only 2-3 days, and has a shorter life-cycle (no more than 20 days).

Our main goal was to study the interaction between *Microcystis* and *M. mi-crura* by applying the DEBtox modelling framework to experimental data, in order to validate some hypotheses, in particular concerning the mechanism of action of the toxicant. Our second goal was to improve the ecotoxicological relevance of the analysis. To do this, both lethal and sublethal effect models were included in matrix population models, allowing us to extrapolate the impact of toxic effects observed in individuals to the population level. Moreover, a confidence band was added to the population endpoint to predict critical exposure concentrations for population health.

⁹⁶ 2 Models and Methods

97 2.1 Data

The data were obtained from life-table and growth experiments (Experiments 2 and 5, respectively, described in Table I in the study of Ferrão-Filho & 99 Azevedo (2003)), carried out with a sample of a naturally occurring bloom 100 of cyanobacteria from Jacarepaguá Lagoon, in Rio de Janeiro (Brazil). The 101 sample consisted of particulate material (seston) collected with a plankton net 102 $(25 \mu m)$. This sample was centrifuged, and the supernatant containing large 103 colonies was discarded, while the settled material was used in the experiments. 104 This material consisted mostly of single cells and small colonies of *Microcystis* 105 $(5-20 \mu m)$, and a small proportion of algae and detritus. Different concen-106 trations of seston, expressed as organic carbon (0.25 to 1.5 mg C $\rm L^{-1}$), were 107 used in the experiments. The microcystin (toxin) concentration in this sample 108 was 3.1 mg g⁻¹ of dry weight, and nominal microcystin concentrations in the 109 seston treatments ranged from 1.6 to 9.4 $\mu g L^{-1}$. The controls (0.0 mg C L⁻¹ 110 of seston) consisted of animals fed solely with nutritious green algae at the 111 concentration of 1.0 mg C L^{-1} . To avoid interference from nutrition factors, 112 as a result of a poor food supply, the same amount of green algae was mixed 113 with all the seston treatments.

The life-table experiment was performed with 20 replicate animals (females)
per treatment, and lasted 16 days. Survivorship and neonates produced per
female, as the cumulative number of offspring, were recorded daily. The growth
experiment was performed with three replicate bottles containing 50 newborns
(< 24 h), and lasted 6 days, with samplings for weighting the animals on days

120 2, 4 and 6.

121 2.2 DEBtox modelling

At the individual level, we used DEBtox modelling (Kooijman & Bedaux, 122 1996) to describe the effects of the contaminant on life history traits measured 123 during the experiments (e.g. growth, reproduction). The DEBtox framework 124 is based on the DEB theory, which assumes that energy is derived from food, 125 and is assimilated to constitute reserves. These reserves are shared between 126 three main processes: maintenance, growth, and reproduction. DEBtox models 127 deal with sublethal effects by assuming that the contaminant affects the en-128 ergy balance, and consequently affects growth and reproduction. The DEBtox 129 theory also comprises a contamination kinetics model and a survival model 130 for the lethal effects of the toxicant. These different parts are presented below. 131 All DEBtox variables and parameters are summarized in Table 1.

2.2.1 Toxicological aspects

Lethal and sublethal effects of a contaminant are modelled using the following stress function:

$$s(c_q(t)) = c_*^{-1}(c_q(t) - NEC_*)_+ \quad (1)$$

where $(c_q(t) - NEC_*)_+ = \max(0, c_q(t) - NEC_*)$. Indeed, in accordance with the DEBtox theory (Kooijman & Bedaux, 1996), the contaminant is assumed to produce an effect when the concentration inside the organisms $(c_q(t))$ exceeds a concentration called the No Effect Concentration $(NEC_*, * = L \text{ for})$ the lethal effects, * = S for the sublethal effects). Moreover, the toxic effect is

assumed to be proportional to the excess above the NEC_* . c_* is the so-called tolerance concentration (Kooijman & Bedaux, 1996), which can be seen as a kind of toxicity rate reciprocal (* = L for the lethal effects, * = H, R, A, G, or M for the sublethal effects, depending on the mechanism of action being considered (see Sublethal effects)). $c_q(t)$ corresponds to the scaled concentration of the toxic compound inside the organism at time t, determinated by the following one-compartment kinetic model:

$$\frac{dc_q(t)}{dt} = \frac{c\dot{k}_e}{l(t)} - c_q(t)(\frac{\dot{k}_e}{l(t)} + \frac{d\ln(l(t)^3)}{dt}) \quad (2)$$

where k_e is the elimination rate, c the exposure concentration and l(t) the scaled body length at time t. The initial condition for the contamination kinetics equation was set at $c_q(t=0)=0$, as exposure started at the beginning of the experiment. For a more detailed explanation of this kinetics, see Kooijman & Bedaux (1996).

155 2.2.2 Lethal effects

As far as the lethal effects were concerned, we used a classical modelling with a tolerance function q(t,c) expressed as the exponential of minus a cumulative hazard function. Thus, the probability q(t,c) of surviving until time t with an exposure concentration of c can be written as follows:

$$q(t,c) = \exp(-\int_{0}^{t} \dot{h}(\tau,c)d\tau)$$
 (3)

where $\dot{h}(\tau,c)$ is the hazard rate at time τ and exposure concentration $c.~\dot{h}(\tau,c)$ is written as follows:

$$\dot{h}(\tau,c) = \begin{cases} \dot{m} + s(c_q(\tau)) & \text{if } c > NEC_L \text{ and } \tau > t_0 \\ \dot{m} & \text{else} \end{cases}$$

where t_0 is the time at which $c_q(\tau)$ exceeds NEC_L : $t_0 = -\dot{k}_e^{-1} \ln(1 - \frac{NEC_L}{c})$ being defined only if $c > NEC_L$.

2.2.3 Sublethal effects

Five possible mechanisms of action were proposed to deal with sublethal ef-167 fects of the contaminant on the various processes considered in the DEBtox 168 framework (assimilation, maintenance, growth, reproduction): an increase in 169 maintenance costs (Maintenance), an increase in growth costs (Growth), a 170 decrease in assimilation (Assimilation), an increase in egg production costs 171 (Costs), or a surmortality during oogenesis (Hazard) (Kooijman & Bedaux, 172 1996). These five assumptions led to different equations for modelling growth 173 and reproduction, the endpoints potentially measured in toxicity tests involv-174 ing zooplankton. Contaminant kinetics, individual growth and reproduction 175 are interrelated, so the corresponding equations had to be considered simulta-176 neously. All the equations are summarized in Table 2 (Billoir et al., in press), 177 and their variables and parameters in Table 1.

179 2.2.4 DEBtox parameter estimation

In this study, the investment ratio g was fixed at g = 1, the reference value for 180 control organisms at optimal temperature (Kooijman & Bedaux, 1996; Kooi-181 jman et al., 2003), and the ingestion rate as a fraction of its maximum value, 182 f, was fixed at f = 1, as the organisms were fed ad libitum. We collected data 183 for 16 days, but we only used the data from day 0 to 10 to fit the models, 184 because after 10 days, senescence effects appeared, which were not taken into 185 account in the models. For the estimation of survival DEBtox parameters $(k_e,$ 186 NEC_L , k_t and m), we performed nonlinear regression of equation (3) on the 187 survival data, based on a least squares criterion, implying data independence, 188 homoscedasticity and normal error assumptions. To minimize the residual sum 189 of squares, we used the optim() function implemented in the R language (R 190 Development Core Team, 2007). For the estimation of the growth and repro-191 duction DEBtox parameters (\dot{k}_e , NEC_S , c_* , L_m , γ , \dot{R}_m and l_p), Billoir et al. 192 (in press) have shown that nonlinear regression is sometimes inadequate, so we 193 used Bayesian inference with WinBugs (Lunn et al., 2000) and WBDiff (Lunn, 194 2004) softwares, as proposed by Billoir et al. (resubmitted). From the arbitrary 195 prior probability distribution for each parameter, Bayesian inference provides 196 estimates as samples of posterior distributions given the data. Moreover, this 197 estimation method made it easy to fit growth and reproduction data simulta-198 neously. In this study, we used slightly informative prior distributions which 199 are summarized in Table 3. After checking the convergence of the estimation 200 process, we considered the posterior distribution means as estimates. k_e was 201 involved in both the lethal and sublethal models, and consequently it was es-202 timated in two different ways, which could yield different values. Thereafter, 203 though this is questionable (see Discussion), we kept both these estimates,

205 and used each for the models for which it had been estimated.

206 2.3 Allometric relationship

As only dry body weight data were available, rather than the body length data required to fit DEBtox models, these two quantities were related using an allometric relationship. The typical form for such a relationship is as follows (Jerison, 1973):

$$y = ax^b$$
 or $\log(y) = \log(a) + b\log(x)$ (13)

where y and x are biological quantities, a and b are both regression parameters. In our case, y corresponded to the body length, and x corresponded to the 213 dry body weight. To estimate the a and b parameters, we performed a linear 214 regression in the log-log representation with data collected between day 2 and 215 6 in five independent growth experiments performed on M. micrura fed with 216 different kinds of food (data from Ferrão-Filho et al. (2005)). As neither body 217 length nor dry body weight was a controlled variable, we used an orthogonal 218 regression method. Once the allometric relationship had been established, we 219 used it to infer body lengths from dry body weights, once again for weight 220 data collected between day 2 and 6 in the toxicity experiments with seston. 221

2.22 2.4 Matrix population model

2.4.1 Principles

To extrapolate the effects of contaminants from the individual to the population level we used matrix population models, which were first proposed by

(Leslie, 1945, 1948), and which have already been coupled to DEBtox models (Lopes et al., 2005; Billoir et al., 2007). These discrete time models deal with 227 populations subdivided into classes based on age or body length. Individuals 228 pass from one class to the next at each time step, the number depending on 229 their survival rates. The number of age-class 1 offspring produced by adults 230 depended on their fecundity rates. Only females were taken into consideration 231 in our study. Let N(t) represent the population at time t (the components 232 of the vector are the size of each class). If L denotes the Leslie matrix, the 233 population dynamics is modelled using the following matrix equation: 234

$$N(t+1) = LN(t)$$

Within this matrix modelling framework, the dominant eigenvalue of \mathbf{L} , denoted by λ , corresponds to the finite rate of population increase (Caswell, 2001; Skalski *et al.*, 2007). If $\lambda > 1$, the population increases. The finite rate of population increase, λ , is related to another common index at the population level, the intrinsic rate of population increase, r, with $\lambda = \exp(r)$.

41 2.4.2 Application

In our case, an age-specific population structure was more appropriate, because we had far more information about reproduction and survival as a function of age than about body length, which was deduced from weight measurements using the allometric relationship. The effect models of DEBtox theory
provided survival (Equation (3)) and reproduction (Equations (8 to 12)) as
functions of time, t, and of the toxicant exposure concentration, c. This also
made it possible to calculate the vital rates as continuous functions of t and c.

We decided to use a pre-breeding census (Caswell, 2001), meaning that data

were collected just before the birth pulse. Let P_i be the probability of surviving from one age class to the next and F_i be the fecundity rate, *i.e.* the number of offspring reaching age class 1 per female of age class i. Hence, we got:

$$P_i(c) = \frac{q(i+1,c)}{q(i,c)}$$
 (14) and $F_i(c) = \int_i^{i+1} P_1(c)\dot{R}(t,c)dt$ (15)

where q(i,c) is the probability of surviving until age class i for a toxicant exposure concentration c (Equation (3)), and R(t,c) is the reproduction rate at time t and exposure concentration c (Equations (8 to 12)).

We used a matrix model with 10 age classes and a time step of 1 day (0-1 day, 1-2 days, ..., 9-10 days), because we used data over 10 days to fit individual models. M. M micrura can live and reproduce for more than 10 days, so we added a term G_{10} to the diagonal of the matrix, allowing the organisms to loop in the last age class. However, in the experiments under consideration, almost all of the organisms had died after 16 days, including the controls. Consequently, we used $G_{10} = 0.5P_9$, ensuring a survival probability of less than 1 % after 16 days.

Assuming that reproduction can occur from age class 2, the matrix is written as follows:

$$\mathbf{L} = \begin{pmatrix} 0 & F_2 & F_3 & \cdots & F_9 & F_{10} \\ P_1 & 0 & 0 & \cdots & 0 & 0 \\ 0 & P_2 & 0 & \cdots & 0 & 0 \\ & & & & & & \\ 0 & 0 & P_3 & \cdots & 0 & 0 \\ & & & & & & \\ 0 & 0 & 0 & \cdots & P_9 & G_{10} \end{pmatrix}$$

where all the matrix coefficients depend on the exposure concentration. To evaluate the effects of cyanobacteria on zooplankton at the population level, the finite rate of population increase, λ , was plotted as a function of the exposure concentration.

2.4.3 Confidence interval for λ

In order to evaluate a confidence interval for the finite rate of population increase, λ , we proposed a method based on bootstrapping. For both lethal and sublethal parameters, we drew 10000 DEBtox parameter sets: in their 95 % Beale joint confidence region (Beale, 1960) for the lethal ones $(\dot{k}_e, NEC_L, \dot{k}_t)$ and m which were estimated by nonlinear regression, and in the sample of the joint posterior distribution for the sublethal ones $(\dot{k}_e, NEC_S, c_*, L_m, \gamma, \dot{R}_m)$ and l_p which was provided by the Bayesian inference. From each parameter set, we next deduced the vital rates of the matrix population model and the

corresponding λ , thus we obtained 10000 λ values. Finally, we considered the 2.5th and 97.5th quantiles of this sample as the limits of a 95% confidence interval for λ , the finite rate of population increase.

285 3 Results

3.1 Allometric relationship

All the data we used to calculate the allometric relationship are plotted in Figure 1 (A). They were consistent with underlying hypotheses of the model, we did not identify any outlier or marginal value. The orthogonal linear regression gave good results, with distances to the regression line close to normality (Figure 1 (B)). We obtained the following allometric relationship (Jerison, 1973):

$$y = \exp(6.42)x^{0.144}$$
 or $\log(y) = 6.42 + 0.144\log(x)$

x being the dry weight and y being the body length.

295 3.2 Lethal effects

The survival data were fitted by a nonlinear regression based on the least squares criterion. Results are presented in Figure 2. Although the theoretical curves did not all fit the data perfectly (Figure 2), we considered that the fits were satisfactory for our purposes. We were not attempting to describe the survival data accurately, but just wanted to exapplate the results from the individual level to the population level.

2 3.3 Sublethal effects

Simultaneous fitting performed by Bayesian inference on growth and repro-303 duction data with the five assumptions about the mechanism of action of the 304 toxicant are shown in Figure 3. For reasons of clarity, data replicates are not 305 shown, and we only plotted the replicate mean for each time and each expo-306 sure concentration. Figure 3 allowed us to visualize the quality of fit, and to 307 compare the different assumptions about the seston mechanism of action. The 308 two best models seemed to be the Assimilation and the Maintenance models 309 (Figure 3 (A) and (C)). With these two assumptions of either decreased as-310 similation or increased maintenance costs, the DEBtox models fitted both the 311 reproduction and growth data well, except for reproduction at 1.0 mg C L^{-1} . 312 However, we had only few replicates of the data at this concentration, because 313 of high mortality. Consequently, the reproduction data at 1.0 mg C L⁻¹ were 314 not as reliable as the data measured at lower exposure concentrations. 315

As far as the other assumptions about mechanism of action of the seston were concerned (Figure 3 (B), (D) and (E)), they clearly disagreed with the growth 317 data. The Costs and Hazard models considered no effect of the contaminant 318 on the growth process (Figure 3 (D2) and (E2)), whatever the exposure con-319 centration. The assumption of increased growth costs (Growth model) (Figure 320 3 (B2)) did not match the body length data. Moreover, this mechanism of 321 action is marked by a delay in the onset of reproduction as soon as the No 322 Effect Concentration (NEC) is exceeded. This feature is not obvious from the 323 reproduction data (Figure 3 (B1)), as a delay in the onset of reproduction 324 was only noticed for the two highest concentrations of seston (1.0 and 1.5 mg $C\ L^{-1}$, which were less reliable), and although a clear effect of seston was

already observed at lower concentrations (0.25 and 0.5 mg C $\rm L^{-1}$), this was not accompanied by any delay in the onset of reproduction.

29 3.4 Population level

As a population endpoint, the finite rate of population increase λ is represented as a function of seston exposure concentration in Figure 4 (A), with 331 the five possible assumptions concerning the toxicological mechanism of ac-332 tion. We have also included in the graph the results reported by Ferrão-Filho 333 & Azevedo (2003): in their study, they calculated the intrinsic population 334 rate of increase r, and we were able to compare this to our results by using 335 $\lambda = \exp(r)$. For exposure concentrations between 0 and 0.5 mg C L⁻¹, our re-336 sults seemed to be consistent with those obtained by Ferrão-Filho & Azevedo 337 (2003), though we obtained slightly lower values in general. From about 0.7 338 $\operatorname{mg} \operatorname{C} \operatorname{L}^{-1}$, with the Maintenance, Growth and Assimilation models, we ob-339 served a drastic drop in population growth due to effects on reproduction. Indeed, using these three assumptions to explain the mechanism of action of 341 the seston, the DEBtox models predicted no reproduction at all for exposure 342 concentrations from 1.0 mg C L⁻¹ (Figure 3 (A1, B1 and C1)). Consequently, the choice of the mechanism of action strongly influenced the threshold con-344 centration from which the population was predicted to go extinct $(\lambda = 1)$, as 345 this threshold concentration ranged from 0.75 to 1.2 mg C L^{-1} , depending on 346 the mechanism of action considered. Ferrão-Filho & Azevedo (2003) obtained 347 $\lambda \approx 1.05$ for the exposure concentration of 1.0 mg C L⁻¹This prediction was 348 much more optimistic than our results ($\lambda \approx 0.25$) using the two best models of sublethal effects at the individual level (the Assimilation and Maintenance

models).

We also calculated a confidence interval for λ , and in Figure 4 (B) we show the results obtained with the Assimilation model which appeared to be one of the two best models for describing sublethal effects. Calculating a confidence interval for λ as a continuous function of exposure concentration led to a confidence band that could also be read horizontally. This enabled us to deduce a prediction interval for the threshold concentration leading to population extinction ($\lambda = 1$): 0.68-0.82 mg C L⁻¹ with the Assimilation model. We obtained similar results with the Maintenance model.

360 4 Discussion

The best fits for our data were obtained with the Assimilation and Mainte-361 nance models, which suggests that these indirect effects (a decrease in food 362 assimilation and an increase in maintenance costs) are the most probable 363 mechanisms of action of cyanobacteria on M. micrura. This was consistent 364 with the results of Ferrão-Filho & Azevedo (2003), which showed that ses-365 ton containing toxic *Microcystis* reduced the filtering rate (and therefore the 366 food assimilation) and fitness (measured as the intrinsic rate of population 367 increase, r) in this cladoceran species. Moreover, microcystins are known to 368 inhibit the activity of protein phosphatase 1 and 2A in Daphnia (DeMott & 369 Dhawale, 1995), which leads ultimately to the disruption of the cell cytoskele-370 ton (Carmichael, 1992). Recent research has also shown that microcystins 371 can cause gut damage in *Daphnia* by disrupting contact between gut cells 372 (Rohrlack et al., 2005). This biochemical-cellular mechanism of action of the 373 microcystins is therefore completely compatible with the decrease in assimi-

lation predicted by DEBtox models used to analyse the data of *M. micrura*exposed to toxic *Microcystis* containing microcystins.

An important assumption of DEB theory is that food is shared between four main metabolic processes: assimilation, somatic maintenance, growth and re-378 production. As cyanobacteria form part of the zooplankton diet, they are also 379 a source of energy, and so toxins (i.e. microcystins) can be assimilated di-380 rectly with food from the gut. Our findings show that the DEBtox theory 381 can provide an excellent framework for studying the effects of cyanobacteria 382 on zooplankton, since the exposure of zooplankton to cyanotoxins is directly 383 coupled to the assimilation of food in the gut, and can therefore interfere with 384 the energy balance.

As far as DEBtox parameter estimation was concerned, we used a set of methods that had already been proposed: nonlinear regression for survival models 387 (Kooijman & Bedaux, 1996; Billoir et al., 2007), and Bayesian inference for 388 the growth and reproduction models (Billoir et al., resubmitted). However, 389 when growth, reproduction and survival data are all available, it would be 390 more logical to estimate all the parameters simultaneously especially because 391 the kinetic parameter \dot{k}_e is involved in both the sublethal and lethal models. 392 Jager et al. (2004) performed a simultaneous estimation of this type, but they 393 ran into some statistical issues, such as very large confidence intervals, and 394 the need to fix k_e . We are currently trying to extend the Bayesian approach 395 by integrating a survival module into the Bayesian model. We hope to report the results of this work in the near future. 397

At the population level, our results and those of Ferrão-Filho & Azevedo (2003)
differ somewhat. Using the data collected for the exposure concentration of

1.0 mg C L⁻¹, they obtained an intrinsic rate of population increase r = 0.042(equivalent to $\lambda = \exp(r) = 1.043$). In contrast, our results for the Assimila-401 tion and Maintenance models were much more pessimistic ($\lambda \ll 1$), indicating 402 that population health was threatened using the same exposure concentration. 403 However, we obtained fewer data for this exposure concentration than for the 404 lower concentrations, as a result of high mortality. Using data collected solely 405 at one exposure concentration did not seem to be as reliable as that obtained 406 by our methodology. Indeed, with the DEBtox modelling approach, all the 407 exposure concentrations tested were considered simultaneously, as the models 408 were continuous in exposure concentration. Moreover, the Bayesian inference took into account the amount of data available for each exposure concentra-410 tion tested. Combining both approaches made it possible to achieve the best 411 inference of the finite rate of population increase, λ , as a continuous function 412 of the exposure concentration. 413

The use of native species, such as M. micrura, and naturally occurring sam-414 ples of cyanoabacteria are important issues in ecotoxicology, as this leads to better extrapolation of results from laboratory to the field. Although this 416 is not a standard test species, like D. magna, the biology of M. micrura is 417 relatively well known, and has been shown to be very sensitive to cyanobacte-418 ria, especially to toxic *Microcystis* (Ferrão-Filho *et al.*, 2000; Nandini, 2000). 419 However, although the application of DEBtox and matrix population models 420 to natural samples gave more realistic results than when we used laboratory 421 samples (i.e. cultures), caution was still called for when extrapolating from 422 these results to field situations. The threshold concentrations calculated from 423 laboratory toxicity tests could sometimes be underproctective, because other 424 stresses (predation, density-dependence, etc...) were not taken into account.

In contrast, our results seemed to be overprotective. The predicted threshold concentration range of 0.68-0.82 mg C L^{-1} , above which the population 427 would become extinct was much lower than the values commonly found in the 428 Jacarepaguá Lagoon (2.7-38.1 mg C L^{-1} ; (Ferrão-Filho et al., 2002)). Also, in 429 spite of some reported outbreaks of M. micrura populations in this lagoon, 430 it is important to note that this species coexists with high concentrations of 431 Microcystis and microcystins (Ferrão-Filho et al., 2002). This was attributed 432 mainly to the predominance of *Microcystis* colonies of large size (> 20 μ m) 433 that cannot be eaten by most cladocerans (Ferrão-Filho & Azevedo, 2003). 434

Even though the DEBtox framework has been applied to standard toxicicity 435 bioassays involving D. magna, a much larger cladoceran, our results showed 436 that this model can also be applied to other zooplankton species, such as M. 437 micrura, which is a much smaller cladoceran with a shorter life cycle. Once 438 again, the combination of DEBtox and matrix population models appeared 439 very useful when extrapolating from the individual to the population level. All 440 lethal and sublethal effects were integrated into the finite rate of population increase, which is much more ecologically relevant than any statistically-based 442 parameter (such as NOEC and ECx) derived from a single endpoint (such as 443 mortality, growth or reproduction). Moreover, our methodology made it possible to calculate the finite rate of population increase as a continuous function 445 of time. Thanks to matrix population modelling, sensitivity analysis could 446 also be used to gain demographic information, as in Billoir et al. (2007). Here, 447 we used a fresh approach: parameter uncertainty was taken into account and 448 integrated into a confidence band, which enabled us to provide a prediction in-440 terval for the threshold concentration leading to population extinction (when 450 λ becomes < 1). In conclusion, our results showed the potential value of us-

- ing nested models to predict the threshold concentrations of cyanobacteria
- required for zooplankton population extinction to occur. These could be used
- as parameters in guidelines for protecting both aquatic life and environmental
- 455 health.

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Symbol	Status	Dimension	Interpretation
t	covariable	Т	time from the experiment beginning, and also organism age
c	covariable	C	exposure concentration
c_q	variable	C	internal concentration
s	variable	-	stress function
q	variable	-	survival probability
h	variable	T^{-1}	hazard rate
l	variable	-	scaled body length
Ŕ	variable	$\# { m T}^{-1}$	reproduction rate
NEC_*	parameter	C	No Effect Concentration for lethal $(*=L)$, sublethal effects $(*=S)$
c_*	parameter	CT^{-1} or C	tolerance concentration, $* = L, H, R, A, G, \text{ or } M$
\dot{k}_e	parameter	T^{-1}	elimination rate
\dot{m}	parameter	T^{-1}	control mortality rate
l_b	parameter	-	scaled body length at birth
Ϋ	parameter	T^{-1}	von Bertalanffy growth rate
l_p	parameter		scaled body length at puberty
\dot{R}_M	parameter	#T ⁻¹	maximum reproduction rate
f	parameter	_	ingestion rate as a fraction of its maximum
g	parameter	-	investment ratio

Table 1

Quantities considered in the DEBtox framework, their status (variable, covariable, or parameter), their dimension and their biological interpretation. T, C and # denote the dimensions of time, concentration and number respectively. Dots denote rates.

Mode of action	Growth	Reproduction
Growth	$\frac{dl}{dt} = \dot{\gamma} \frac{f+g}{f+g(1+s(c_q(t)))} (f-l(t)) (4)$	$\dot{R}(l(t)) = \frac{\dot{R}M}{1 - l_p^3} [fl(t)^2 (\frac{g(1 + s(c_q(t))) + l}{g(1 + s(c_q(t))) + f}) - l_p^3] (8)$
Maintenance	$\frac{dl}{dt} = \dot{\gamma}(f - l(1 + s(c_q(t)))) (5)$	$\dot{R}(l(t)) = \frac{\dot{R}M}{1 - l_p^3} (1 + s(c_q(t))) [fl(t)^2 (\frac{g(1 + s(c_q(t)))^{-1} + l(t)}{g + f}) - l_p^3] $ (9)
Assimilation	$\frac{dl}{dt} = \dot{\gamma} \frac{f+g}{f(1-s(c_q(t)))+g} (f(1-s(c_q(t))) - l(t)) $ (6)	$\dot{R}(l(t)) = \frac{\dot{R}_M}{1 - l_p^3} \left[f(1 - s(c_q(t))) l(t)^2 \left(\frac{g + l(t)}{g + f(1 - s(c_q(t)))} \right) - l_p^3 \right] $ (10)
Hazard	$\frac{dl}{dt} = \dot{\gamma}(f - l(t)) (7)$	$\dot{R}(l(t)) = \frac{\dot{R}_M}{1 - l_p^3} [fl(t)^2 (\frac{g + l(t)}{g + f}) - l_p^3] e^{-s(c_q(t))} $ (11)
Costs	$\frac{dl}{dt} = \dot{\gamma}(f - l(t)) (7)$	$\dot{R}(l(t)) = \frac{\dot{R}_M}{1 - l_p^3} \left[f(t)^2 \left(\frac{g + l(t)}{g + f} \right) - l_p^3 \right] (1 + s(c_q(t)))^{-1} $ (12)

Table 2 $\label{eq:decomposition} \mbox{DEBtox growth and reproduction equations for each assumption about the toxicant mode of action.}$

Parameter (unit)	Distribution
$L_m \; (\mu \mathrm{m})$	$N(1000, 100) \ I(500, +\infty)$
γ̈́ (-)	U(0,2)
l_p (-)	N(0.75, 0.1) I(0.5, 1)
$\dot{R}_m \ (\# d^{-1})$	$N(5,2) \ I(0,+\infty)$
$\dot{k}_{f e}~({ m d}^{-1})$	U(0.0001, 10)
$NEC \; (\mathrm{mg} \; \mathrm{C} \; \mathrm{L}^{-1})$	U(0, 1.5)
$c_* * = H, R, G, \text{ or } M \text{ (mg C L}^{-1})$	U(0,20)
$c_A \text{ (mg C L}^{-1}\text{)}$	U(2, 20)

Table 3

Prior distributions used for the DEBtox sublethal parameter estimation which was performed by Bayesian inference. N(m, sd)I(a, b) denotes a normal distribution with mean m and standard deviation sd, where I(a, b) represents interval censoring (see Spiegelhalter et al., 2003, p. 12 for details) (Spiegelhalter et al., 2003). U(c, d) denotes a uniform distribution between c and d.

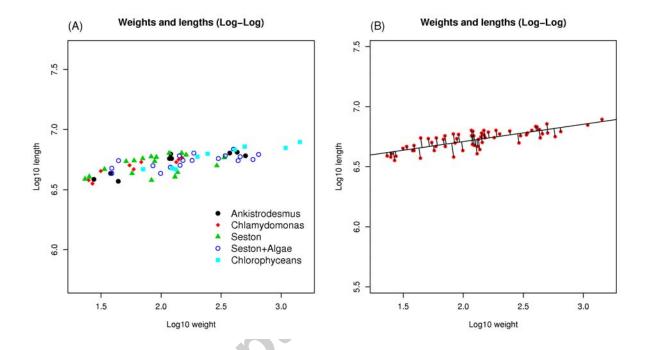


Fig. 1. (A) Log-Log representation of the data used to establish the length/dry weight allometric relationship. Data were collected during experiments involving various kinds of food (data from Ferrão-Filho *et al.* (2005)). (B) Orthogonal linear regression fit on these data.

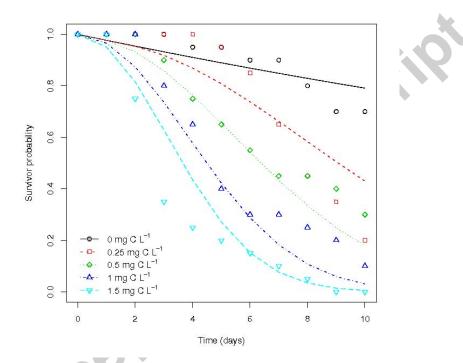


Fig. 2. Fitting performed by nonlinear regression of survival data: time profile of survival probability for various seston exposure concentrations (0, 0.25, 0.5, 1.0, 1.5 mg C $\rm L^{-1}$)

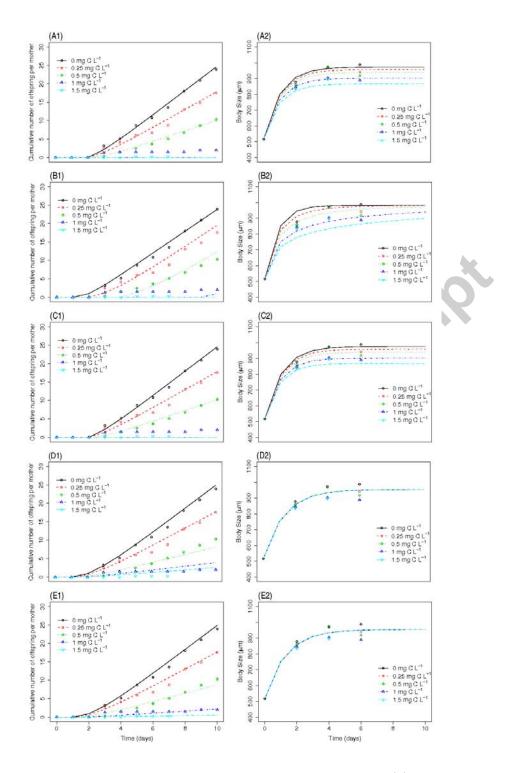


Fig. 3. Simultaneous fitting performed by Bayesian inference of (1) reproduction and (2) growth data under the assumption of (A) a decrease in Assimilation (B) an increase in the Growth costs (C) an increase in the Maintenance costs (D) an increase in egg production Costs, and (E) excess mortality during oogenesis (Hazard): time profiles of the cumulative number of offspring and body length for various seston exposure concentrations (0, 0.25, 0.5, 1.0, 1.5 mg C $\rm L^{-1})$

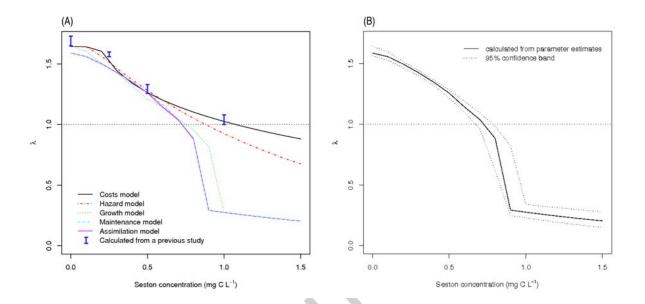


Fig. 4. (A) Evolution of the finite rate of population increase λ of M. micrura as a function of the seston exposure concentration (mg C L⁻¹). Comparison of the five assumptions about the toxicological mechanism of action: Hazard, Costs, Maintenance, Growth and Assimilation. The results from Ferrão-Filho & Azevedo (2003) (means \pm SE) are also shown on this graph. (B) Change in the finite rate of population increase λ of M. micrura and its confidence interval as a function of seston exposure concentration (mg C L⁻¹) when we assumed that a decrease in Assimilation was the toxicological mechanism of action.