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# A New 3-DoF Planar Parallel Manipulator with Unlimited Rotation Capability 

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#### Abstract

Most of three-degree-of-freedom (3-DoF) planar parallel manipulators encountered today have a common disadvantage that is their low rotational capability. However, for many industrial applications, by example in automated assembly systems, cutting machines, simulators, or micro-motion manipulators, a high rotation capability is needed. To overcome such a difficulty, this paper focuses its attention on the proposal of a new 3-DoF planar parallel manipulator capable of high rotational capability. Firstly, structure and mobility of the suggested manipulator are discussed. Then the forward and inverse kinematic problems are analyzed, as well as it is disclosed its singular configurations. The shaking force and shaking moment balancing are also considered. The proposed design concept is illustrated by a driven demonstrator which is a first model of the suggested manipulator.

Keywords: design, modeling, singularity, 3-DoF planar parallel manipulator, unlimited rotation capability.


## I Introduction

In the search for a suitable means for simulating flight conditions for the safe training of helicopter pilots, the design of parallel mechanisms has been proposed having all the freedom of motion and capable of being controlled in all of them simultaneously. A typical 6-DoF parallel mechanism consists of a moving platform connected to a fixed base by six serial chains called legs or limbs. Due to its parallel structure these manipulators offer the advantages of low inertia, considerable stiffness, large payload to manipulator weight ratio and higher operating speeds. The advantages however come at the expense of a reduced workspace, difficult mechanical design and more complex kinematics and control algorithms. They have been utilized for many practical applications and many researchers have paid attention to the design of these structures. Therefore, a large number of papers place emphasis on the study of 6-DoF parallel manipulators [1], [2].

[^0]

Fig. 1. Kinematic chain of the suggested manipulator.
However, in most of applications, parallel manipulators with less than six degrees of freedom are more useful. These structures can be presented by the following principal groups: (i) 2-DoF translational manipulators [3]-[6]; (ii) planar 3-DoF parallel manipulators [7], [8]; (iii) spherical 3-DoF parallel manipulators [9]-[13]; (iv) 3-DOF translational parallel manipulators [14]-[22]; (v) 3-DOF parallel manipulators with combined translational and rotational motions [23][26]; (vi) 4-DOF parallel manipulators for Schoenflies motion [27]-[36]; (vii) 5-DOF parallel manipulators [37]-[39].

Recent reports indicates that the technology of parallel manipulators has not yet made a substantial impacts for the raison that the complicated nonlinearity of parallel manipulators in design and control is not completely accepted by end users [40], [41]. Thus, many basic problems are still opened in order to obtain an efficient exploitation of these structures. One of the drawbacks of the developed parallel structures is also the limited rotation capability. This problem has been studied in [42]-[44] for spatial parallel manipulators but it is not considered for planar parallel manipulators.
The aim of this paper is to propose a new planar 3DOF manipulator with unlimited rotation capability.

## II Description of the suggested manipulator

Let us consider the architecture of the suggested manipulator (Fig. 1). It is composed of three legs. Each leg is composed of two rigid links $O_{i} A_{i}$ and $A_{i} B_{i}(i=1, \ldots$, 3). The links $O_{i} A_{i}$ are connected to the base via actuated revolute joints located at axes $O_{i}$ and they are defined by the coordinates $q_{i}$. The platform of the manipulator is connected with the links $A_{i} B_{i}$ via revolute joints. The difference between the traditional planar $3-\underline{R} R R$ manipulator and the suggested architecture is the position coincidence of the axes $B_{1}$ and $B_{2}$. In this case, we obtain a structure in which the position $(x, y)$ of the centre $C$ of the platform is controlled by a $5 R$ planar manipulator $\left(O_{1} A_{1} C A_{2} O_{2}\right)$ and its orientation ( $\phi$ ) by a four-bar linkage $\left(O_{3} A_{3} B_{3} C\right)$. Thus, in the presented structure the linear displacements and the orientation are decoupled: the actuators 1 and 2 control the position of the end-effector, and actuator 3 its orientation.

As it is shown in Fig. 1 the axis $\boldsymbol{x}_{0}$ is along of the vector $O_{1} O_{2}$. The lengths of the elements $O_{i} A_{i}$ are denoted as $L_{1 i}$. The lengths of the elements $A_{i} B_{i}$ are denoted as $L_{2 i}$. The dimension of the platform $C B_{3}$ is denoted as $R$. The positions of the base axes $O_{i}$ along $x_{0}$ and $y_{0}$ axes are denoted as ( $x_{O i}, y_{O i}$ ), with $x_{O 1}=y_{O 1}=y_{O 2}$ $=0$.

Let us consider the geometric models of the manipulator. From the previous description, one can find the loop-closure equations:

$$
\begin{equation*}
\mathbf{O C}=\mathbf{O O}_{i}+\mathbf{O}_{i} \mathbf{A}_{i}+\mathbf{A}_{i} \mathbf{B}_{i}+\mathbf{B}_{i} \mathbf{C} \tag{1}
\end{equation*}
$$

from which it comes

$$
\left[\begin{array}{l}
x  \tag{2}\\
y
\end{array}\right]=\left[\begin{array}{l}
x_{O i}+L_{1 i} \cos q_{i}+L_{2 i} \cos \psi_{i}-x_{B i C} \\
y_{O i}+L_{1 i} \sin q_{i}+L_{2 i} \sin \psi_{i}-y_{B i C}
\end{array}\right]
$$

where $\left[x_{C B i}, y_{C B i}\right]^{T}$ represents the expression of vector $C B_{i}$ in the base frame. For $i=1$ or $2,\left[x_{B i C}, y_{B i C}\right]^{T}=\mathbf{0}$, and $\left[x_{C B 3}, y_{C B 3}\right]^{T}=R[\cos \phi, \sin \phi]^{T}$.

Rearranging (2) and squaring both sides, we obtain the following system:

$$
\begin{align*}
g_{1}= & \left(x-L_{11} \cos q_{1}\right)^{2}+\left(y-L_{11} \sin q_{1}\right)^{2}-L_{21}^{2}=0  \tag{3a}\\
g_{2}= & \left(x-x_{O 2}-L_{12} \cos q_{2}\right)^{2}+\left(y-L_{12} \sin q_{2}\right)^{2}-L_{22}^{2}=0  \tag{3b}\\
g_{3}= & \left(x+R \cos \phi-x_{O 3}-L_{13} \cos q_{3}\right)^{2}  \tag{3c}\\
& \ldots+\left(y+R \sin \phi-y_{O 3}-L_{13} \sin q_{3}\right)^{2}-L_{23}^{2}=0
\end{align*}
$$

more generically it can be written

$$
\begin{align*}
g_{i}= & \left(x+x_{C B i}-x_{O i}-L_{1 i} \cos q_{i}\right)^{2} \\
& \ldots+\left(y+y_{C B i}-y_{O i}-L_{1 i} \sin q_{i}\right)^{2}-L_{2 i}^{2}=0 \tag{4}
\end{align*}
$$

## III Inverse kinematics

Developing (4) and factorizing with respect to cosine and sine $q_{i}$, it comes

$$
\begin{equation*}
a_{i} \cos q_{i}+b_{i} \sin q_{i}+c_{i}=0 \tag{5}
\end{equation*}
$$

where

$$
\begin{align*}
& a_{i}=-2\left(x+x_{B i C}-x_{O i}\right) L_{1 i}  \tag{6a}\\
& b_{i}=-2\left(y+y_{B i C}-y_{O i}\right) L_{1 i}  \tag{6b}\\
& c_{i}=\left(x+x_{B i C}-x_{O i}\right)^{2}+\left(y+y_{B i C}-y_{O i}\right)^{2}+L_{1 i}^{2}-L_{2 i}^{2} \tag{6c}
\end{align*}
$$

Using the following relationships

$$
\begin{equation*}
\cos q_{i}=\frac{1-t_{i}^{2}}{1+t_{i}^{2}}, \sin q_{i}=\frac{2 t_{i}}{1+t_{i}^{2}} \text { with } t_{i}=\tan \left(\frac{q_{i}}{2}\right) \tag{7}
\end{equation*}
$$

(5) becomes

$$
\begin{equation*}
\left(c_{i}-a_{i}\right) t_{i}^{2}+2 b_{i} t_{i}+c_{i}+a_{i}=0 \tag{8}
\end{equation*}
$$

Thus, the solutions $t_{i}$ of this polynomial can be found as

$$
\begin{equation*}
t_{i}=\frac{-b_{i} \pm \sqrt{b_{i}^{2}-c_{i}^{2}+a_{i}^{2}}}{c_{i}-a_{i}} \tag{9}
\end{equation*}
$$

Therefore, for one given position of the end-effector, the inverse geometric model can be found as:

$$
\begin{equation*}
q_{i}=2 \tan ^{-1}\left(\frac{-b_{i} \pm \sqrt{b_{i}^{2}-c_{i}^{2}+a_{i}^{2}}}{c_{i}-a_{i}}\right) \tag{10}
\end{equation*}
$$

in which the sign $\pm$ stands for the two possible working modes of the leg $i$.

## IV Forward kinematics

Due to the decoupling properties of the robot, the forward geometric model of this robot can be solved in two steps:

1. find the expression of $x$ and $y$ as a function of $q_{1}$ and $q_{2}$, using (3a) and (3b);
2. find the expression of $\phi$ as a function of $q_{1}, q_{2}$ and $q_{3}$ using (3c).
Developing (3a) and 3b and factorizing with respect to $x$ and $y$, it comes

$$
\begin{align*}
& x^{2}+d_{1} x+y^{2}+e_{1} y+f_{1}=0  \tag{11a}\\
& x^{2}+d_{2} x+y^{2}+e_{2} y+f_{2}=0 \tag{11b}
\end{align*}
$$

where

$$
\begin{gather*}
d_{i}=-2\left(x_{O i}+L_{1 i} \cos q_{i}\right)  \tag{12a}\\
e_{i}=-2 L_{1 i} \sin q_{i}  \tag{12b}\\
f_{i}=L_{1 i}^{2}-L_{2 i}^{2} \tag{12c}
\end{gather*}
$$

From (11a) and (11b), one can obtain the following relation

$$
\begin{equation*}
\left(d_{2}-d_{1}\right) x=-\left(e_{2}-e_{1}\right) y \tag{13}
\end{equation*}
$$

Introducing it into (11a) leads to, for $d_{2}-d_{1} \neq 0$ :

$$
\begin{equation*}
u_{1} y^{2}+v_{1} y+w_{1}=0 \tag{14}
\end{equation*}
$$

where

$$
\begin{gather*}
u_{1}=\left(d_{2}-d_{1}\right)^{2}+\left(e_{2}-e_{1}\right)^{2}  \tag{15a}\\
v_{1}=\left(d_{2}-d_{1}\right)\left(d_{2} e_{1}-d_{1} e_{2}\right)  \tag{15b}\\
w_{1}=\left(d_{2}-d_{1}\right)^{2} f_{1} \tag{15c}
\end{gather*}
$$

Solving (14) leads to

$$
\begin{equation*}
y=\frac{-v_{1} \pm \sqrt{v_{1}^{2}-4 u_{1} w_{1}}}{2 u_{1}} \tag{16}
\end{equation*}
$$

in which the sign $\pm$ stands for two possible assembly modes of the system composed of legs 1 and 2 . Introducing (16) into (13) allows finding the position of the end-effector.

Then, introducing (13) and (16) into (3c) and developing leads to

$$
\begin{equation*}
u_{2} \cos \phi+v_{2} \sin \phi+w_{2}=0 \tag{17}
\end{equation*}
$$

where

$$
\begin{array}{r}
u_{2}=2 R\left(x-x_{O 3}-L_{13} \cos q_{3}\right) \\
v_{2}=2 R\left(y-y_{O 3}-L_{13} \sin q_{3}\right) \\
w_{2}=\left(x-x_{O 3}-L_{13} \cos q_{3}\right)^{2} \\
\ldots+\left(y-y_{O 3}-L_{13} \sin q_{3}\right)^{2}-L_{23}^{2}+R^{2} \tag{18c}
\end{array} .
$$

Using the following relationships

$$
\begin{equation*}
\cos \phi=\frac{1-t^{2}}{1+t^{2}}, \sin \phi=\frac{2 t}{1+t^{2}} \text { with } t=\tan \left(\frac{\phi}{2}\right) \tag{19}
\end{equation*}
$$

(17) becomes

$$
\begin{equation*}
\left(w_{2}-u_{2}\right) t^{2}+2 v_{2} t+w_{2}+u_{2}=0 \tag{20}
\end{equation*}
$$

Thus, the solutions of this polynomial can be found as

$$
\begin{equation*}
t=\frac{-v_{2} \pm \sqrt{v_{2}^{2}-w_{2}^{2}+u_{2}^{2}}}{w_{2}-u_{2}} \tag{21}
\end{equation*}
$$

Therefore, for one given position of the end-effector, the inverse geometric model can be found as:

$$
\begin{equation*}
\phi=2 \tan ^{-1}\left(\frac{-v_{2} \pm \sqrt{v_{2}^{2}-w_{2}^{2}+u_{2}^{2}}}{w_{2}-u_{2}}\right) \tag{22}
\end{equation*}
$$

in which the sign $\pm$ stands for the two possible assembly modes of the platform.

## V Singularity analysis

Differentiating (3a) to (3c) with respect to time leads to the following relation:

$$
\begin{equation*}
\mathbf{A t}+\mathbf{B} \dot{\mathbf{q}}=\mathbf{0} \tag{23}
\end{equation*}
$$

where $\mathbf{t}=[\dot{x}, \dot{y}, \dot{\phi}]^{T}$ is the platform twist, $\dot{\mathbf{q}}=\left[\dot{q}_{1}, \dot{q}_{2}, \dot{q}_{3}\right]^{T}$ the vector of the articular velocities, and $\mathbf{A}$ and $\mathbf{B}$ two matrices of which expressions are

$$
\begin{gather*}
\mathbf{A}=\left[\left[\frac{\partial g_{i}}{\partial x}\right]\left[\frac{\partial g_{i}}{\partial y}\right]\left[\frac{\partial g_{i}}{\partial \phi}\right]\right]=\left[\begin{array}{cc}
\mathbf{r}_{1}^{T} & 0 \\
\mathbf{r}_{2}^{T} & 0 \\
\mathbf{r}_{3}^{T} & m_{3}
\end{array}\right]  \tag{24a}\\
\mathbf{B}=\left[\frac{\partial g_{i}}{\partial \mathbf{q}}\right]=\left[\begin{array}{ccc}
b_{11} & 0 & 0 \\
0 & b_{22} & 0 \\
0 & 0 & b_{33}
\end{array}\right] \tag{24b}
\end{gather*}
$$

with

$$
\begin{gather*}
\mathbf{r}_{i}^{T}=\left[\cos \psi_{i}, \sin \psi_{i}\right]^{T}  \tag{25a}\\
m_{3}=R \sin \left(\phi-\psi_{3}\right)  \tag{25b}\\
b_{i i}=L_{1} L_{2} \sin \left(\psi_{i}-q_{i}\right) \tag{25c}
\end{gather*}
$$

where $\mathbf{r}_{i}$ is the direction of the wrench applied by the leg $i$ on the platform, and $m_{i}$ its moment.

As a result:

1. the Type 1 singularities appear when $b_{i i}=0$, for $i=1$, 2 or 3 ; such relation appear when the segments $O_{i} A_{i}$ and $A_{i} C_{i}$ are located on the same line (Fig. 2)
2. a first case of Type 2 singularities appear when $m_{3}=0$; such relation appear when the segments $C B_{3}$ and $A_{3} B_{3}$ are located on the same line (Fig. 3a)
3. a second case of Type 2 singularities appear when $\mathbf{r}_{\mathbf{1}}$ is collinear to $\mathbf{r}_{2}$; such relation appear when the segments $A_{1} B_{1}$ and $A_{2} B_{2}$ are located on the same line (Fig. 3b)

(a) first case

(b) second case

Fig. 3. Examples of Type 2 singularities.
It known that in the case of high-speed motions, the shaking force and shaking moment bring about variable dynamic loads on the frame and, as result, vibrations.

One of the effective means for reduction of these vibrations is the mass balancing of moving links of manipulators. Therefore in the next section the shaking force and shaking moment balancing of the suggested manipulator is considered

## VI Balancing

Let us start by shaking force balancing of the suggested manipulator.

## A. Shaking force balancing

In order to achieve the dynamic balancing of the suggested manipulator, we first have to ensure that it is force balanced. For this purpose, the masse of the platform could be substituted by two equivalent point masses located at the axes $B_{3}$ and $C$ :

$$
\left[\begin{array}{cc}
1 & 1  \tag{26}\\
L_{B_{3} S_{p l}} & -L_{C S_{p l}}
\end{array}\right]\left[\begin{array}{c}
m_{B_{3}} \\
m_{C}
\end{array}\right]=\left[\begin{array}{c}
m_{p l} \\
0
\end{array}\right]
$$

where $m_{B 3}$ is the point mass located on the joint axis $B_{3}$; $m_{C}$ is the point mass located on the joint axis $C$; $m_{p l}$ is the mass of the moving platform; $L_{B 3 S p l}$ is the distance of joint centre $B_{3}$ from the centre of mass $S_{p l}$ of the platform; $L_{C S p l}$ is the distance of axe $C$ from the centre of mass $S_{p l}$ of the platform. This allows for the transformation of the manipulator balancing problem into a problem of balancing legs carrying concentrated masses.

The centre of mass of each leg relative to its base $O_{i}$ (Fig. 1) can be found by the expressions [45]:

$$
\begin{align*}
& x_{S i}=\left(m_{i} x_{S i}+m_{i}^{\prime} x_{S i}^{\prime}+m_{B i} x_{B i}\right) /\left(m_{i}+m_{i}^{\prime}+m_{B i}\right)  \tag{27}\\
& y_{S i}=\left(m_{i} y_{S i}+m_{i}^{\prime} y_{S i}+m_{B i} y_{B i}\right) /\left(m_{i}+m_{i}^{\prime}+m_{B i}\right) \tag{28}
\end{align*}
$$

where

$$
\begin{align*}
& x_{S i}=R_{i} \cos q_{i}  \tag{29}\\
& y_{S i}=R_{i} \sin q_{i}  \tag{30}\\
& x_{S i}^{\prime}=L_{1 i} \cos q_{i}+R_{i}^{\prime} \cos \psi_{i}  \tag{31}\\
& y_{S i}^{\prime}=L_{1 i} \sin q_{i}+R_{i}^{\prime} \sin \psi_{i}  \tag{32}\\
& x_{B i}=L_{1 i} \cos q_{i}+L_{2 i} \cos \psi_{i}  \tag{33}\\
& y_{B i}=L_{1 i} \sin q_{i}+L_{2 i} \sin \psi_{i} \tag{34}
\end{align*}
$$

$m_{i}$ and $m_{i}^{\prime}$ are the masses of links $O_{i} A_{i}$ and $A_{i} B_{i} ; m_{B 1}=$ $m_{B 2}=0.5 m_{C} ; R_{i}$ is the distance of the centre of mass $S_{i}$ of the link $O_{i} A_{i}$ from the joint centre $O_{i} ; R_{i}$ is the distance of the centre of mass $S_{i}^{\prime}$ of the link $A_{i} B_{i}$ from the joint centre $A_{i}$.

Thus, for the position of centre of mass to remain constant it is sufficient that the coefficients of the variables $q_{i}$ and $\psi_{i}$ be equal to zero, i.e.


Fig. 4. Shaking moment balancing of fully force-balanced manipulator by an inertia flywheel.

$$
\begin{align*}
& m_{i}^{\prime} R_{i}^{\prime}+m_{B_{i}} L_{2 i}=0  \tag{35}\\
& m_{i} R_{i}+\left(m_{i}^{\prime}+m_{B_{i}}\right) L_{1 i}=0 \tag{36}
\end{align*}
$$

The conditions (35) and (36) can be satisfied by adding two counterweights on each leg, which produce negative values of radii $R$ and $R^{\prime}$. After such a redistribution of masses, the centre of mass of the manipulator remains motionless for any motion of links and hence, the manipulator transmits no inertia loads to its base (Fig. 4).

## B. Shaking moment balancing

Now that the inertia force balancing is achieved, we have to consider the cancellation of the shaking moment. For the suggested manipulator, the shaking moment balancing is constructively more efficient by inertia flywheel [45]. Fig. 4 shows the fully force-balanced manipulator and balancing inertia flywheel, which is mounted on the base of the manipulator.

To balance this shaking moment, the inertia flywheel with an axial moment of inertia denoted as $I$ can be used. The angular acceleration of this inertia flywheel driven by a complementary actuator 4 is the following:

$$
\begin{equation*}
\ddot{q}=M^{\text {sh }} / I \tag{37}
\end{equation*}
$$

It should be mentioned that the axial inertia moment of the flywheel must be selected in such a manner that its rotation with prescribed acceleration will be feasible.

Therefore, the reaction of the balancing inertia flywheel on the frame cancels the shaking moment due to the parallel manipulator. In other words, the actuator,
which moves the balancing inertia flywheel with a prescribed angular acceleration $\ddot{q}$ has a reaction on the frame which is similar but opposite to the shaking moment of the parallel manipulator. Thus, full shaking moment is annulled. The angular velocity $\dot{q}(t)$ and angular displacements $q(t)$ can be determined by simple integration of the obtained values of $\ddot{q}(t)$.

In order to numerically verify the shaking force and shaking moment balancing of the manipulator an ADAMS model was developed and dynamic simulations were carried out.

For the simulations, the geometric parameters used are of the model are those of the demonstrator that is given in section VII. With regard to mass and inertia parameters the following values have been used:

- $m_{1}=m_{2}=0,497 \mathrm{~kg}, m_{3}=0,565 \mathrm{~kg}, m^{\prime}{ }_{1}=m^{\prime}{ }_{2}=0,483$ $\mathrm{kg}, m^{\prime}{ }_{3}=0,620 \mathrm{~kg}, m_{p l}=0,210 \mathrm{~kg} ;$
- $I_{1}=I_{2}=1,43 \cdot 10^{-3} \mathrm{~kg} \cdot \mathrm{~m}^{2}, I_{3}=2,08 \cdot 10^{-3} \mathrm{~kg} \cdot \mathrm{~m}^{2}, I_{1}{ }^{\prime}=I^{\prime}{ }_{2}$ $=1,32 \cdot 10^{-3} \mathrm{~kg} \cdot \mathrm{~m}^{2}, I_{3}^{\prime}=2,73 \cdot 10^{-3} \mathrm{~kg} \cdot \mathrm{~m}^{2}, I_{p l}=0,26 \cdot 10^{-3}$ kg.m²;
- $R_{i}=0.5 L_{1 i}, R_{i}^{\prime}=0.5 L_{2 i}, L_{B 3 S p l}=L_{C S p l}=0.5 R$;

In order to cancel the shaking force the counterweights should be added. Their parameters are given by:

- $L_{\text {OiCpi }}=0.5 L_{1 i}, L_{\text {AiCp }(i+3)}=0.5 L_{2 i}$;
- $m_{C p 1}=m_{C p 2}=3.06 \mathrm{~kg}, m_{C p 3}=3.68 \mathrm{~kg}, m_{C p 4}=m_{C p 5}=$ $0.694 \mathrm{~kg}, m_{C p 6}=0.830 \mathrm{~kg}$;
where $L_{O i C p i}$ corresponds to the distance between point $O_{i}$ and the counterweights positioned at $C_{p i}$ and $L_{A i C p(i+3)}$ to the distance between point $A_{i}$ and the counterweights positioned at $C_{p(i+3)}$ (Fig. 4); $m_{C p i}$ is the mass of the counterweight located at $C_{p i}$.

In Fig. 5 are presented the shaking force and shaking moment before (full black line) and after (dotted black line) balancing. It is observed that, after mass balancing, the shaking force is cancelled while the shaking moment increases. In order to balance the shaking moment, an optimal trajectory planning is introduced into the control of the inertia flywheel using eq. (37). Taking into account that the axial moment of inertia of the flywheel is equal to $0.02 \mathrm{~kg} . \mathrm{m}^{2}$, its optimal displacement is presented at Fig. 6. After the use of this optimal planning, the shaking moment is also cancelled (Fig. 7c, grey full line).

## VII Demonstrator

In order to better illustrate the proposed concept, a driven demonstrator has been built. The parameters of the manipulator are the following: $L_{11}=L_{12}=155 \mathrm{~mm}, L_{21}=$ $L_{22}=150 \mathrm{~mm}, L_{13}=180 \mathrm{~mm}, L_{23}=200 \mathrm{~mm}, R=50 \mathrm{~mm}$, $O_{1}=(0,0) \mathrm{mm}, O_{2}=(180,0) \mathrm{mm}$ and $O_{3}=(80,420) \mathrm{mm}$.

Fig. 7 shows the motions generated by this driven demonstrator which is a first model of the suggested manipulator. Its theoretical workspace is presented at Fig. 8. It can be computed geometrically as the intersections of six portions of circles described by [2]:


Fig. 5. Shaking force before (full black line) and after (dotted black line) mass redistribution and shaking moment before (black lines) and after (grey line) balancing by the inertia flywheel.

- two circles $C_{1}$ and $C_{4}$ centred in $O_{1}$, of respective radii equal to $L_{11}+L_{21}$ and $L_{11}-L_{21}$; these circles represent the extreme displacements of the robot leg 1 ;
- two circles $C_{2}$ and $C_{5}$ centred in $O_{2}$, of respective radii equal to $L_{12}+L_{22}$ and $L_{12}-L_{22}$; these circles represent the extreme displacements of the robot leg 2 ;


Fig. 6. Definition of the optimal angular displacement for the inertia flywheel.


Fig. 7. Motion generation via a driven demonstrator built in the SouthWest State University of Kursk.

- two circles $C_{3}$ and $C_{6}$, centred in $O_{3}$, of radius equal to $L_{13}+L_{23}-R$ and $L_{13}-L_{23}+R$; these circle represents the extreme displacements of the robot end-effector linked to leg 3 for any platform orientation;


Fig. 8. Maximal reachable workspace of the robot (to scale).
As $5 R$ robots have the ability to cross the Type 1 singular configurations [46], it can be shown that any of the workspace points can be attained without crossing of the Type 2 singular configurations presented at Fig. 3b, that are due to the $5 R$ positioning architecture. It should also be mentioned that the Type 2 singularities presented at Fig. 3a, that appear for some specific platform orientations, can be crossed using optimal motion generation [47].

Taking into account these considerations, it is possible to define the maximal regular workspaces of the robot, for any platform orientation [48], [49]. It is proposed here to characterize the size of two different maximal regular workspaces: a circle and a square. Using some CAD software [50], it can be shown that, for this driven demonstrator:

- the maximal inscribed circle is centred in (90, 64.5) mm and has a radius of 105.75 mm
- the maximal inscribed square is centred in $(90,85)$ mm and has a edge length of 170 mm .
Finally, it should be noted that for dynamic tests a prototype will be developed with prescribed mass/inertia parameters and optimized control system.


## VIII Conclusion

In this paper, the development of a new 3-DoF planar parallel manipulator with unlimited rotation capability was addressed. The advantage of the proposed design concept is the high rotational capability, which can be useful for many industrial applications: in automated assembly systems, cutting machines, simulators, micromotion manipulators. This is a first publication, in which structural and kinematic properties were disclosed, as well as the shaking force and moment balancing. The linear displacements and orientation of the platform is
illustrated via a driven demonstrator, which is a first driven model of the manipulator.

Dynamic simulations, optimization and tests, that can perform this design concept will be a next step of this project.

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## References

[1] Dasgupta, B and Mruthyunjaya, T.S. The Stewart platform manipulator: a review. Mechanism and Machine Theory, 35(1):15-40, 2000.
[2] Merlet, J.-P. Parallel Robots. Springer, 432p., 2006.
[3] Gao, F. et al. Performance evaluation of two degrees of freedom parallel robots. Mechanism and Machine Theory, 33(2):661-668, 1998.
[4] Huang, T. et al. Conceptual design and dimensional synthesis of a novel 2-DoF translational parallel robot for pick-and place operations. ASME Journal of Mechanical Design, 126(3):449-455, 2004.
[5] Wu, J. S. et al. Analysis and application of a 2-DOF planar parallel mechanism, ASME Journal of Mechanical Design, 129(4):434437, 2007.
[6] Da Silva, M. M. et al. Integrating structural and input design of a 2-DOF high-speed parallel manipulator: a flexible model-based approach. Mechanism and Machine Theory, 45(11):1509-1519, 2010.
[7] Gosselin, C.M. and Angeles, J. The optimum kinematic design of a planar tree-degrees-of-freedom parallel manipulator. ASME Journal of Mechanical Design, 110(1):35-41, 1988.
[8] Foucault, S. and Gosselin, C. M. Synthesis, design and prototyping of a tree-of-freedom reactionless parallel manipulator. ASME Journal of Mechanical Design, 126(6):992-999, 2004.
[9] Gosselin, C.M. and Angetes, J. The optimum kinematic design of a spherical three-degree-of-freedom parallel Manipulator, ASME Journal of Mechanical Design, 111(2):202-207, 1989.
[10] Gosselin, C. M. and Lavoie, E. On the kinemaric design of spherical three degree-of-freedom parallel manipulators, International Journal of Robotics Research. 12(4): 394-402, 1993.
[11] Gosselin, C. M., Sefrioui, J., and Richard, M. J. On the direct kinematics of spherical three-degree-of-freedom parallel manipulators of general architecture. ASME Journal of Mechanical Design, 116(2): 594-598, 1994.
[12] Vischer, P. and Claver, R. Argos: a novel 3-DOF parallel wrist mechanism. International Journal of Robotics Research. 19(1): 511, 2000.
[13] Karouia, A. and Hervé, J.M. A three-DOF tripod for generating spherical rotation. Advances in Robot Kinematics, Lenarcic J. and Stanisic M., Eds. Kluwer Academic Publishers, pages 395-402, 2000.
[14] Clavel, R. Delta, a fast robot with parallel geometry. In proceedings of the 18th International Symposium on Industrial Robot, Lausanne, 26-28 April 1988, pages 91-100, 1988.
[15] Tsai, L.-W. Kinematics of a three-dof platform with three extensible limbs, in: J. Lenarcic, V. Parenti-Castelli, (Eds.). Recent Advances in Robot Kinematics, Kluwer, pages 401-410, 1996.
[16] Hervé, J.M. Group mathematics and parallel link mechanisms. In IMACS/SICE Int. Symp. on Robotics, Mechatronics, and Manufacturing Systems, Kobe, 16-20 September 1992, pages 459-464, 1992.
[17] Ceccarelli, M. A new 3-DOF spatial parallel mechanism. Mechanism and Machine Theory, 32(8): 895-902, 1997.
[18] Carricato, M and Parenti-Castelli, V. A family of 3-DOF translational parallel manipulators. ASME Journal of Mechanical Design, 125(2): 302-307, 2003.
[19] Kim, D. and Chung, W.K. Kinematic condition analysis of threeDOF pure translational parallel manipulators. ASME Journal of Mechanical Design, 125(2): 323-331, 2003.
[20] Kong, X. and Gosselin, C.M. A class of 3-DOF translational parallel manipulator with linear input-output equations. In Workshop on Fundamental Issues and Future Research for Parallel Mechanisms and Manipulators, Quebec City, Quebec, Canada, 2002, pages 25-32, 2002.
[21] Gosselin, C.M., Kong, X., Foucault, S. and Bonev, I.A. A fully decoupled 3-DOF translational parallel mechanism. In PKM International Conference, Chemnitz, Germany, 2004, pages 595610, 2004.
[22] Caro S., Wenger P., Bennis F. and Chablat D. Sensitivity Analysis of the Orthoglide, a 3-DOF Translational Parallel Kinematic Machine. ASME Journal of Mechanical Design, 128(2): 392-402, 2006.
[23] Lee, K.M. and Shah, D. Kinematic analysis of a three-degrees-offreedom in-parallel actuated manipulator. IEEE Journal of Robotics and Automation, 4(3):354-360, 1988.
[24] Dunlop, G.R. and Jones, T.P. Position analysis of a 3-DOF parallel manipulator, Mechanism and Machine Theory, 32(8):903-920, 1997.
[25] Carretero, J. et al. Kinematic analysis and optimization of an three degree-of-freedom spatial planar manipulator. ASME Journal of Mechanical Design, 122(1): 17-24, 2000.
[26] Jin, Q. and Yang, T.L. Synthesis and analysis of a group of 3-degree-of-freedom partially decouped parallel manipulators. ASME Journal of Mechanical Design, 126(2): 301-306, 2004.
[27] Rolland, L. The Manta and the Kanuk: Novel 4-DOF Parallel Manipulators for Industrial Handling. In ASME IMECE'99 Conference, Nashville, USA, November, pages 831-844, 1999.
[28] Pierrot, F., Marquet, F., Company, O., and Gil., T. H4 Parallel Robot: Modeling, Design and Preliminary Experiments. In IEEE International Conference on Robotics and Automation, Soul, Korea, pages 3256-3261, 2001.
[29] Angeles, J., Morozov, A., and Navarro, O. A Novel Manipulator Architecture for the Production of SCARA motions. in IEEE International Conference on Robotics and Automation, San Francisco, CA, pages 2370-2375, 2000.
[30] Angeles, J., and Morozov, A., 2005. Four-degree-of-freedom parallel manipulator for producing schonflies motions. Patent US2005262959, December 1, 2005.
[31] Angeles, J. The Morphology Design for a Parallel SchönfliesMotion Generator. In Proceedings of the Second International Colloquium on Robotic Systems for Handling and Assembly, Braunschweig, Germany, pages 37-56, 2005.
[32] Yang, T. L., Jin, Q., Liu, A. X., Yao, F. H., and Luo, Y. Structure Synthesis of 4-DOF (3-Translation and 1-Rotation) Parallel Robot Mechanisms Based on the Units of Single-Opened-Chain. In ASME Design Engineering Technical Conference, Pittsburgh, PA, Paper No. DETC2001/DAC-21152, 2001.
[33] Li, Q. C. and Huang, Z. Type Synthesis of 4-DOF Parallel Manipulators. In IEEE International Conference on Robotics and Automation, Taipei, Taiwan, pages 755-760, 2003.
[34] Carricato, M. Fully Isotropic Four-Degrees-of-Freedom Parallel Mechanisms for Schoenflies Motion. International Journal of Robotics Research. 24(5): 397-414, 2005.
[35] Gogu., G. Singularity-Free Fully-Isotropic Parallel Manipulators with Schönflies Motions. In International Conference on Advanced Robotics, July 18-20, pages 194-201, 2005.
[36] Richard, P.L., Gosselin, C., and Kong, X. Kinematic Analysis and Prototyping of a Partially Decoupled 4-DOF 3T1R Parallel Manipualtor. ASME Journal of Mechanical Design. 129(6):611616, 2007.
[37] Jin, Q. et al. Structure synthesis of a class of five-DOF parallel robot mechanisms based on single-open-chain units. In ASME Design Engineering Technical Conference Pittsburgh, PA, Paper No. DETC2001/DAC-21153, 2001.
[38] Chablat, D. and Wenger, Ph. Device for the movement and orientation of an object in space and use thereof in rapid machining. European patent EP1597017, November 23 ${ }^{\text {rd }}$, 2005.
[39] Briot, S., Arakelian, V. and Guégan S. PAMINSA: A new family of partially decoupled parallel. Mechanism and Machine Theory, 44(2): 425-444, 2009.
[40] Merlet, J.P. An initiative for the kinematic study of parallel manipulators. Workshop on Fundamental Issues and Future Research Directions for Parallel Mechanisms and Manipulators, Québec, Canada, October 3-4, 2002.
[41] Brogårdh, T. PKM Research - Important issues, as seen from a product development perspective at ABB Robotics", Workshop on Fundamental Issues and Future Research Directions for Parallel Mechanisms and Manipulators, Québec, Canada October 3-4, 2002.
[42] Liu X.-J., Wang J. and Pritschow G. A new family of spatial 3DOF fully-parallel manipulators with high rotational capability. Mechanism and Machine Theory, 40(4): 475-494, 2005.
[43] Company O et al. Schoenflies motion generation: A new non redundant parallel manipulator with unlimited rotation capability. In IEEE International Conference on Robotics and Automation, Barcelona, Spain, pages 3261-3266, 2005.
[44] Nabat, V. Parallel robot with articulated platforms: from concept to industrial solution for pick-and-place operations. PhD dissertation, Montpellier, 138p. 2007.
[45] Arakelian, V and Smith, M. R. Design of planar 3-DOF 3-RRR reactionless parallel manipulators. Mechatronics, 18(10): 601-606 2008.
[46] Campos, L., Bourbonnais, F., Bonev, I.A., and Bigras, P. Development of a five-bar parallel robot with large workspace. ASME 2010 International Design Engineering Technical Conferences (IDETC 2010), Montreal, QC, Canada, 2010.
[47] Briot, S. and Arakelian, V. Optimal force generation of parallel manipulators for passing through the singular positions. The International Journal of Robotics Research, 27(8):967-983, 2008.
[48] Ur-rehman R., Caro S., Chablat D., Wenger P. Multiobjective path placement optimization of parallel kinematics machines based on energy consumption, shaking forces and maximum actuators torques: application to the Orthoglide, Mechanism and Machine Theory, 45(8): 1125-1141, 2010.
[49] Chablat, D., and Wenger, P. The kinematic analysis of a symmetrical three-degree-of-freedom planar parallel manipulator. CISM-IFToMM Symposium on Robot Design, Dynamics and Control, Montreal, Canada, June 2004.
[50] Bonev, I.A., and Ryu, J. A Geometrical method for computing the constant-orientation workspace of 6-PRRS parallel manipulators, Mechanism and Machine Theory, 36(1): 1-13, 2001.


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