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A New 3-DoF Planar Parallel Manipulator with Unlimited Rotation Capability

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Abstract— Most of three-degree-of-freedom (3-DoF) planar parallel manipulators encountered today have a common disadvantage that is their low rotational capability. However, for many industrial applications, by example in automated assembly systems, cutting machines, simulators, or micro-motion manipulators, a high rotation capability is needed. To overcome such a difficulty, this paper focuses its attention on the proposal of a new 3-DoF planar parallel manipulator capable of high rotational capability. Firstly, structure and mobility of the suggested manipulator are discussed. Then the forward and inverse kinematic problems are analyzed, as well as it is disclosed its singular configurations. The shaking force and shaking moment balancing are also considered. The proposed design concept is illustrated by a driven demonstrator which is a first model of the suggested manipulator.

Keywords: design, modeling, singularity, 3-DoF planar parallel manipulator, unlimited rotation capability.

I Introduction

In the search for a suitable means for simulating flight conditions for the safe training of helicopter pilots, the design of parallel mechanisms has been proposed having all the freedom of motion and capable of being controlled in all of them simultaneously. A typical 6-DoF parallel mechanism consists of a moving platform connected to a fixed base by six serial chains called legs or limbs. Due to its parallel structure these manipulators offer the advantages of low inertia, considerable stiffness, large payload to manipulator weight ratio and higher operating speeds. The advantages however come at the expense of a reduced workspace, difficult mechanical design and more complex kinematics and control algorithms. They have been utilized for many practical applications and many researchers have paid attention to the design of these structures. Therefore, a large number of papers place emphasis on the study of 6-DoF parallel manipulators [1], [2].

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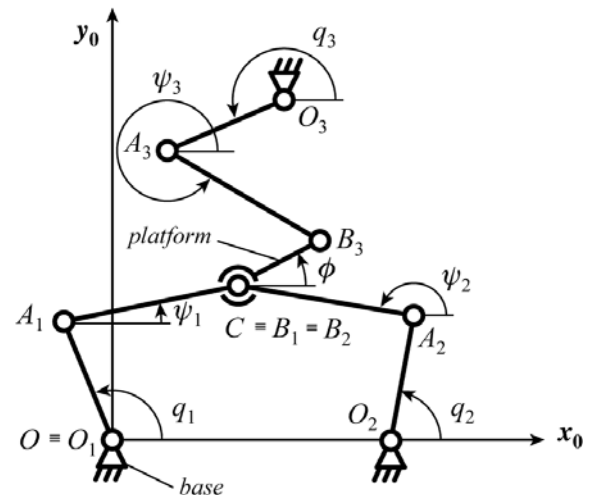


Fig. 1. Kinematic chain of the suggested manipulator.

However, in most of applications, parallel manipulators with less than six degrees of freedom are more useful. These structures can be presented by the following principal groups: (i) 2-DoF translational manipulators [3]–[6]; (ii) planar 3-DoF parallel manipulators [7], [8]; (iii) spherical 3-DoF parallel manipulators [9]–[13]; (iv) 3-DOF translational parallel manipulators [14]–[22]; (v) 3-DOF parallel manipulators with combined translational and rotational motions [23]–[26]; (vi) 4-DOF parallel manipulators for Schoenflies motion [27]–[36]; (vii) 5-DOF parallel manipulators [37]–[39].

Recent reports indicates that the technology of parallel manipulators has not yet made a substantial impacts for the reason that the complicated nonlinearity of parallel manipulators in design and control is not completely accepted by end users [40], [41]. Thus, many basic problems are still opened in order to obtain an efficient exploitation of these structures. One of the drawbacks of the developed parallel structures is also the limited rotation capability. This problem has been studied in [42]–[44] for spatial parallel manipulators but it is not considered for planar parallel manipulators.

The aim of this paper is to propose a new planar 3-DOF manipulator with unlimited rotation capability.

II Description of the suggested manipulator

Let us consider the architecture of the suggested manipulator (Fig. 1). It is composed of three legs. Each leg is composed of two rigid links O_iA_i and A_iB_i ($i = 1, \dots, 3$). The links O_iA_i are connected to the base via actuated revolute joints located at axes O_i and they are defined by the coordinates q_i . The platform of the manipulator is connected with the links A_iB_i via revolute joints. The difference between the traditional planar 3-RRR manipulator and the suggested architecture is the position coincidence of the axes B_1 and B_2 . In this case, we obtain a structure in which the position (x, y) of the centre C of the platform is controlled by a 5R planar manipulator ($O_1A_1CA_2O_2$) and its orientation (ϕ) by a four-bar linkage ($O_3A_3B_3C$). Thus, in the presented structure the linear displacements and the orientation are decoupled: the actuators 1 and 2 control the position of the end-effector, and actuator 3 its orientation.

As it is shown in Fig.1 the axis x_0 is along of the vector O_1O_2 . The lengths of the elements O_iA_i are denoted as L_{1i} . The lengths of the elements A_iB_i are denoted as L_{2i} . The dimension of the platform CB_3 is denoted as R . The positions of the base axes O_i along x_0 and y_0 axes are denoted as (x_{O_i}, y_{O_i}) , with $x_{O_1} = y_{O_1} = y_{O_2} = 0$.

Let us consider the geometric models of the manipulator. From the previous description, one can find the loop-closure equations:

$$\mathbf{OC} = \mathbf{OO}_i + \mathbf{O}_i\mathbf{A}_i + \mathbf{A}_i\mathbf{B}_i + \mathbf{B}_i\mathbf{C} \quad (1)$$

from which it comes

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} x_{O_i} + L_{1i} \cos q_i + L_{2i} \cos \psi_i - x_{B_{iC}} \\ y_{O_i} + L_{1i} \sin q_i + L_{2i} \sin \psi_i - y_{B_{iC}} \end{bmatrix} \quad (2)$$

where $[x_{CB_i}, y_{CB_i}]^T$ represents the expression of vector CB_i in the base frame. For $i = 1$ or 2 , $[x_{B_{iC}}, y_{B_{iC}}]^T = \mathbf{0}$, and $[x_{CB_3}, y_{CB_3}]^T = R [\cos \phi, \sin \phi]^T$.

Rearranging (2) and squaring both sides, we obtain the following system:

$$g_1 = (x - L_{11} \cos q_1)^2 + (y - L_{11} \sin q_1)^2 - L_{21}^2 = 0 \quad (3a)$$

$$g_2 = (x - x_{O_2} - L_{12} \cos q_2)^2 + (y - L_{12} \sin q_2)^2 - L_{22}^2 = 0 \quad (3b)$$

$$g_3 = (x + R \cos \phi - x_{O_3} - L_{13} \cos q_3)^2 + (y + R \sin \phi - y_{O_3} - L_{13} \sin q_3)^2 - L_{23}^2 = 0 \quad (3c)$$

more generically it can be written

$$g_i = (x + x_{CB_i} - x_{O_i} - L_{1i} \cos q_i)^2 + (y + y_{CB_i} - y_{O_i} - L_{1i} \sin q_i)^2 - L_{2i}^2 = 0 \quad (4)$$

III Inverse kinematics

Developing (4) and factorizing with respect to cosine and sine q_i , it comes

$$a_i \cos q_i + b_i \sin q_i + c_i = 0 \quad (5)$$

where

$$a_i = -2(x + x_{B_{iC}} - x_{O_i})L_{1i} \quad (6a)$$

$$b_i = -2(y + y_{B_{iC}} - y_{O_i})L_{1i} \quad (6b)$$

$$c_i = (x + x_{B_{iC}} - x_{O_i})^2 + (y + y_{B_{iC}} - y_{O_i})^2 + L_{1i}^2 - L_{2i}^2 \quad (6c)$$

Using the following relationships

$$\cos q_i = \frac{1 - t_i^2}{1 + t_i^2}, \quad \sin q_i = \frac{2t_i}{1 + t_i^2} \quad \text{with } t_i = \tan\left(\frac{q_i}{2}\right) \quad (7)$$

(5) becomes

$$(c_i - a_i)t_i^2 + 2b_it_i + c_i + a_i = 0 \quad (8)$$

Thus, the solutions t_i of this polynomial can be found as

$$t_i = \frac{-b_i \pm \sqrt{b_i^2 - c_i^2 + a_i^2}}{c_i - a_i} \quad (9)$$

Therefore, for one given position of the end-effector, the inverse geometric model can be found as:

$$q_i = 2 \tan^{-1} \left(\frac{-b_i \pm \sqrt{b_i^2 - c_i^2 + a_i^2}}{c_i - a_i} \right) \quad (10)$$

in which the sign \pm stands for the two possible working modes of the leg i .

IV Forward kinematics

Due to the decoupling properties of the robot, the forward geometric model of this robot can be solved in two steps:

1. find the expression of x and y as a function of q_1 and q_2 , using (3a) and (3b);
2. find the expression of ϕ as a function of q_1 , q_2 and q_3 using (3c).

Developing (3a) and 3b and factorizing with respect to x and y , it comes

$$x^2 + d_1x + y^2 + e_1y + f_1 = 0 \quad (11a)$$

$$x^2 + d_2x + y^2 + e_2y + f_2 = 0 \quad (11b)$$

where

$$d_i = -2(x_{O_i} + L_{1i} \cos q_i) \quad (12a)$$

$$e_i = -2L_{1i} \sin q_i \quad (12b)$$

$$f_i = L_{1i}^2 - L_{2i}^2 \quad (12c)$$

From (11a) and (11b), one can obtain the following relation

$$(d_2 - d_1)x = -(e_2 - e_1)y \quad (13)$$

Introducing it into (11a) leads to, for $d_2 - d_1 \neq 0$:

$$u_1 y^2 + v_1 y + w_1 = 0 \quad (14)$$

where

$$u_1 = (d_2 - d_1)^2 + (e_2 - e_1)^2 \quad (15a)$$

$$v_1 = (d_2 - d_1)(d_2 e_1 - d_1 e_2) \quad (15b)$$

$$w_1 = (d_2 - d_1)^2 f_1 \quad (15c)$$

Solving (14) leads to

$$y = \frac{-v_1 \pm \sqrt{v_1^2 - 4u_1 w_1}}{2u_1} \quad (16)$$

in which the sign \pm stands for two possible assembly modes of the system composed of legs 1 and 2. Introducing (16) into (13) allows finding the position of the end-effector.

Then, introducing (13) and (16) into (3c) and developing leads to

$$u_2 \cos \phi + v_2 \sin \phi + w_2 = 0 \quad (17)$$

where

$$u_2 = 2R(x - x_{O_3} - L_{13} \cos q_3) \quad (18a)$$

$$v_2 = 2R(y - y_{O_3} - L_{13} \sin q_3) \quad (18b)$$

$$w_2 = (x - x_{O_3} - L_{13} \cos q_3)^2 + (y - y_{O_3} - L_{13} \sin q_3)^2 - L_{23}^2 + R^2 \quad (18c)$$

Using the following relationships

$$\cos \phi = \frac{1-t^2}{1+t^2}, \quad \sin \phi = \frac{2t}{1+t^2} \quad \text{with } t = \tan\left(\frac{\phi}{2}\right) \quad (19)$$

(17) becomes

$$(w_2 - u_2)t^2 + 2v_2 t + w_2 + u_2 = 0 \quad (20)$$

Thus, the solutions of this polynomial can be found as

$$t = \frac{-v_2 \pm \sqrt{v_2^2 - w_2^2 + u_2^2}}{w_2 - u_2} \quad (21)$$

Therefore, for one given position of the end-effector, the inverse geometric model can be found as:

$$\phi = 2 \tan^{-1} \left(\frac{-v_2 \pm \sqrt{v_2^2 - w_2^2 + u_2^2}}{w_2 - u_2} \right) \quad (22)$$

in which the sign \pm stands for the two possible assembly modes of the platform.

V Singularity analysis

Differentiating (3a) to (3c) with respect to time leads to the following relation:

$$\mathbf{A}\mathbf{t} + \mathbf{B}\dot{\mathbf{q}} = \mathbf{0} \quad (23)$$

where $\mathbf{t} = [\dot{x}, \dot{y}, \dot{\phi}]^T$ is the platform twist, $\dot{\mathbf{q}} = [\dot{q}_1, \dot{q}_2, \dot{q}_3]^T$ the vector of the articular velocities, and \mathbf{A} and \mathbf{B} two matrices of which expressions are

$$\mathbf{A} = \begin{bmatrix} \left[\frac{\partial g_i}{\partial x} \right] & \left[\frac{\partial g_i}{\partial y} \right] & \left[\frac{\partial g_i}{\partial \phi} \right] \end{bmatrix} = \begin{bmatrix} \mathbf{r}_1^T & 0 \\ \mathbf{r}_2^T & 0 \\ \mathbf{r}_3^T & m_3 \end{bmatrix} \quad (24a)$$

$$\mathbf{B} = \begin{bmatrix} \frac{\partial g_i}{\partial \mathbf{q}} \end{bmatrix} = \begin{bmatrix} b_{11} & 0 & 0 \\ 0 & b_{22} & 0 \\ 0 & 0 & b_{33} \end{bmatrix} \quad (24b)$$

with

$$\mathbf{r}_i^T = [\cos \psi_i, \sin \psi_i]^T \quad (25a)$$

$$m_3 = R \sin(\phi - \psi_3) \quad (25b)$$

$$b_{ii} = L_1 L_2 \sin(\psi_i - q_i) \quad (25c)$$

where \mathbf{r}_i is the direction of the wrench applied by the leg i on the platform, and m_i its moment.

As a result:

1. the Type 1 singularities appear when $b_{ii} = 0$, for $i = 1, 2$ or 3 ; such relation appear when the segments $O_i A_i$ and $A_i C_i$ are located on the same line (Fig. 2)
2. a first case of Type 2 singularities appear when $m_3 = 0$; such relation appear when the segments CB_3 and $A_3 B_3$ are located on the same line (Fig. 3a)
3. a second case of Type 2 singularities appear when \mathbf{r}_1 is collinear to \mathbf{r}_2 ; such relation appear when the segments $A_1 B_1$ and $A_2 B_2$ are located on the same line (Fig. 3b)

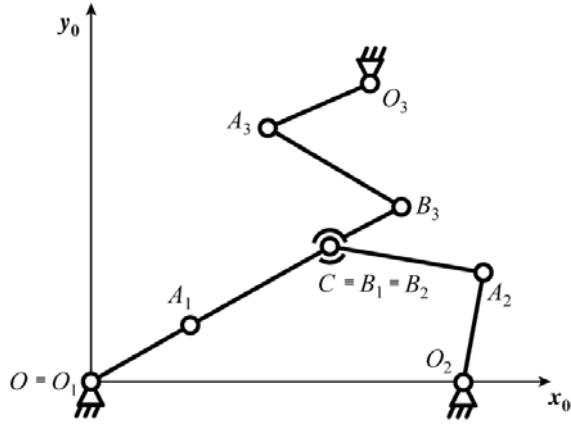
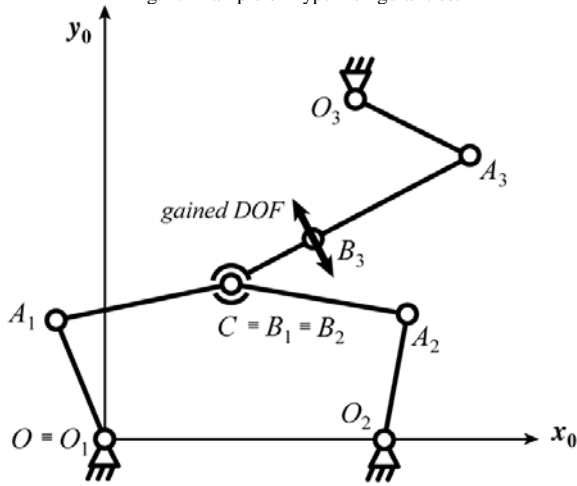
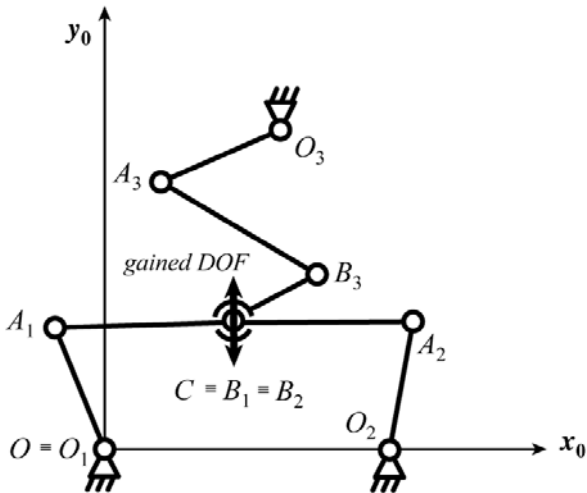


Fig. 2. Example of Type 1 singularities.



(a) first case



(b) second case

Fig. 3. Examples of Type 2 singularities.

It known that in the case of high-speed motions, the shaking force and shaking moment bring about variable dynamic loads on the frame and, as result, vibrations.

One of the effective means for reduction of these vibrations is the mass balancing of moving links of manipulators. Therefore in the next section the shaking force and shaking moment balancing of the suggested manipulator is considered

VI Balancing

Let us start by shaking force balancing of the suggested manipulator.

A. Shaking force balancing

In order to achieve the dynamic balancing of the suggested manipulator, we first have to ensure that it is force balanced. For this purpose, the masse of the platform could be substituted by two equivalent point masses located at the axes B_3 and C :

$$\begin{bmatrix} 1 & 1 \\ L_{B_3 S_{pl}} & -L_{C S_{pl}} \end{bmatrix} \begin{bmatrix} m_{B_3} \\ m_C \end{bmatrix} = \begin{bmatrix} m_{pl} \\ 0 \end{bmatrix} \quad (26)$$

where m_{B_3} is the point mass located on the joint axis B_3 ; m_C is the point mass located on the joint axis C ; m_{pl} is the mass of the moving platform; $L_{B_3 S_{pl}}$ is the distance of joint centre B_3 from the centre of mass S_{pl} of the platform; $L_{C S_{pl}}$ is the distance of axe C from the centre of mass S_{pl} of the platform. This allows for the transformation of the manipulator balancing problem into a problem of balancing legs carrying concentrated masses.

The centre of mass of each leg relative to its base O_i (Fig. 1) can be found by the expressions [45]:

$$x_{S_i} = (m_i x_{S_i} + m'_i x'_{S_i} + m_{B_i} x_{B_i}) / (m_i + m'_i + m_{B_i}) \quad (27)$$

$$y_{S_i} = (m_i y_{S_i} + m'_i y'_{S_i} + m_{B_i} y_{B_i}) / (m_i + m'_i + m_{B_i}) \quad (28)$$

where

$$x_{S_i} = R_i \cos q_i \quad (29)$$

$$y_{S_i} = R_i \sin q_i \quad (30)$$

$$x'_{S_i} = L_i \cos q_i + R'_i \cos \psi_i \quad (31)$$

$$y'_{S_i} = L_i \sin q_i + R'_i \sin \psi_i \quad (32)$$

$$x_{B_i} = L_{1i} \cos q_i + L_{2i} \cos \psi_i \quad (33)$$

$$y_{B_i} = L_{1i} \sin q_i + L_{2i} \sin \psi_i \quad (34)$$

m_i and m'_i are the masses of links $O_i A_i$ and $A_i B_i$; $m_{B_1} = m_{B_2} = 0.5 m_C$; R_i is the distance of the centre of mass S_i of the link $O_i A_i$ from the joint centre O_i ; R'_i is the distance of the centre of mass S'_i of the link $A_i B_i$ from the joint centre A_i .

Thus, for the position of centre of mass to remain constant it is sufficient that the coefficients of the variables q_i and ψ_i be equal to zero, i.e.

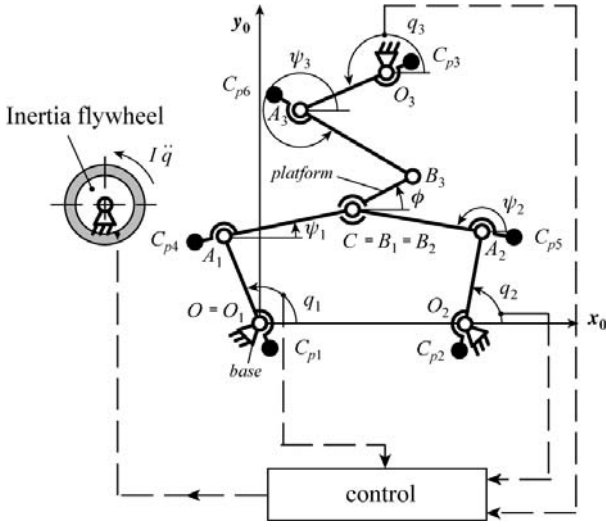


Fig. 4. Shaking moment balancing of fully force-balanced manipulator by an inertia flywheel.

$$m'_i R'_i + m_{B_i} L_{2i} = 0 \quad (35)$$

$$m_i R_i + (m'_i + m_{B_i}) L_{1i} = 0 \quad (36)$$

The conditions (35) and (36) can be satisfied by adding two counterweights on each leg, which produce negative values of radii R and R' . After such a redistribution of masses, the centre of mass of the manipulator remains motionless for any motion of links and hence, the manipulator transmits no inertia loads to its base (Fig. 4).

B. Shaking moment balancing

Now that the inertia force balancing is achieved, we have to consider the cancellation of the shaking moment. For the suggested manipulator, the shaking moment balancing is constructively more efficient by inertia flywheel [45]. Fig. 4 shows the fully force-balanced manipulator and balancing inertia flywheel, which is mounted on the base of the manipulator.

To balance this shaking moment, the inertia flywheel with an axial moment of inertia denoted as I can be used. The angular acceleration of this inertia flywheel driven by a complementary actuator 4 is the following:

$$\ddot{q} = M^{sh} / I \quad (37)$$

It should be mentioned that the axial inertia moment of the flywheel must be selected in such a manner that its rotation with prescribed acceleration will be feasible.

Therefore, the reaction of the balancing inertia flywheel on the frame cancels the shaking moment due to the parallel manipulator. In other words, the actuator,

which moves the balancing inertia flywheel with a prescribed angular acceleration \ddot{q} has a reaction on the frame which is similar but opposite to the shaking moment of the parallel manipulator. Thus, full shaking moment is annulled. The angular velocity $\dot{q}(t)$ and angular displacements $q(t)$ can be determined by simple integration of the obtained values of $\ddot{q}(t)$.

In order to numerically verify the shaking force and shaking moment balancing of the manipulator an ADAMS model was developed and dynamic simulations were carried out.

For the simulations, the geometric parameters used are of the model are those of the demonstrator that is given in section VII. With regard to mass and inertia parameters the following values have been used:

- $m_1 = m_2 = 0,497$ kg, $m_3 = 0,565$ kg, $m'_1 = m'_2 = 0,483$ kg, $m'_3 = 0,620$ kg, $m_{pl} = 0,210$ kg;
- $I_1 = I_2 = 1,43 \cdot 10^{-3}$ kg.m², $I_3 = 2,08 \cdot 10^{-3}$ kg.m², $I'_1 = I'_2 = 1,32 \cdot 10^{-3}$ kg.m², $I'_3 = 2,73 \cdot 10^{-3}$ kg.m², $I_{pl} = 0,26 \cdot 10^{-3}$ kg.m²;

- $R_i = 0.5 L_{1i}$, $R'_i = 0.5 L_{2i}$, $L_{B3Spl} = L_{CSpl} = 0.5 R$;

In order to cancel the shaking force the counterweights should be added. Their parameters are given by:

- $L_{O_i C_{p_i}} = 0.5 L_{1i}$, $L_{A_i C_{p(i+3)}} = 0.5 L_{2i}$;
- $m_{C_{p1}} = m_{C_{p2}} = 3.06$ kg, $m_{C_{p3}} = 3.68$ kg, $m_{C_{p4}} = m_{C_{p5}} = 0.694$ kg, $m_{C_{p6}} = 0.830$ kg;

where $L_{O_i C_{p_i}}$ corresponds to the distance between point O_i and the counterweights positioned at C_{p_i} and $L_{A_i C_{p(i+3)}}$ to the distance between point A_i and the counterweights positioned at $C_{p(i+3)}$ (Fig. 4); $m_{C_{p_i}}$ is the mass of the counterweight located at C_{p_i} .

In Fig. 5 are presented the shaking force and shaking moment before (full black line) and after (dotted black line) balancing. It is observed that, after mass balancing, the shaking force is cancelled while the shaking moment increases. In order to balance the shaking moment, an optimal trajectory planning is introduced into the control of the inertia flywheel using eq. (37). Taking into account that the axial moment of inertia of the flywheel is equal to 0.02 kg.m², its optimal displacement is presented at Fig. 6. After the use of this optimal planning, the shaking moment is also cancelled (Fig. 7c, grey full line).

VII Demonstrator

In order to better illustrate the proposed concept, a driven demonstrator has been built. The parameters of the manipulator are the following: $L_{11} = L_{12} = 155$ mm, $L_{21} = L_{22} = 150$ mm, $L_{13} = 180$ mm, $L_{23} = 200$ mm, $R = 50$ mm, $O_1 = (0, 0)$ mm, $O_2 = (180, 0)$ mm and $O_3 = (80, 420)$ mm.

Fig. 7 shows the motions generated by this driven demonstrator which is a first model of the suggested manipulator. Its theoretical workspace is presented at Fig. 8. It can be computed geometrically as the intersections of six portions of circles described by [2]:

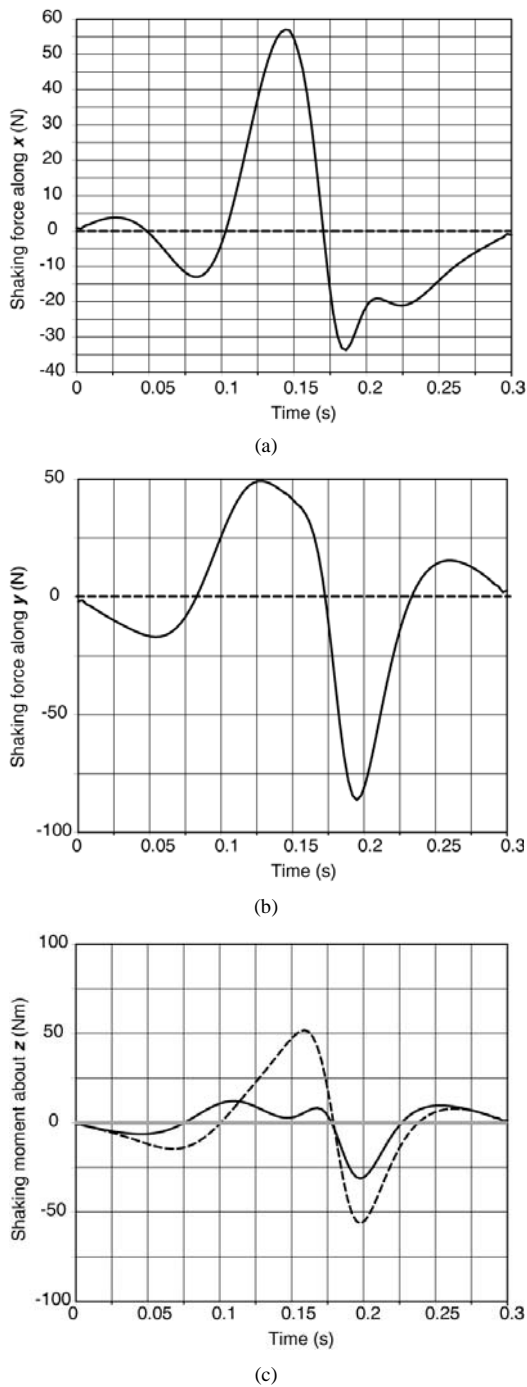


Fig. 5. Shaking force before (full black line) and after (dotted black line) mass redistribution and shaking moment before (black lines) and after (grey line) balancing by the inertia flywheel.

- two circles C_1 and C_4 centred in O_1 , of respective radii equal to $L_{11} + L_{21}$ and $L_{11} - L_{21}$; these circles represent the extreme displacements of the robot leg 1;
- two circles C_2 and C_5 centred in O_2 , of respective radii equal to $L_{12} + L_{22}$ and $L_{12} - L_{22}$; these circles represent the extreme displacements of the robot leg 2;

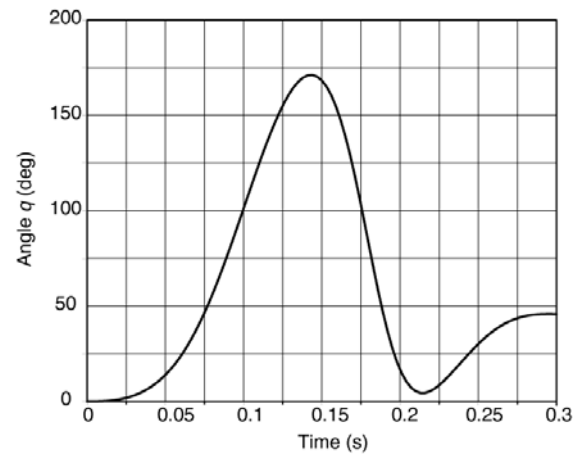


Fig. 6. Definition of the optimal angular displacement for the inertia flywheel.

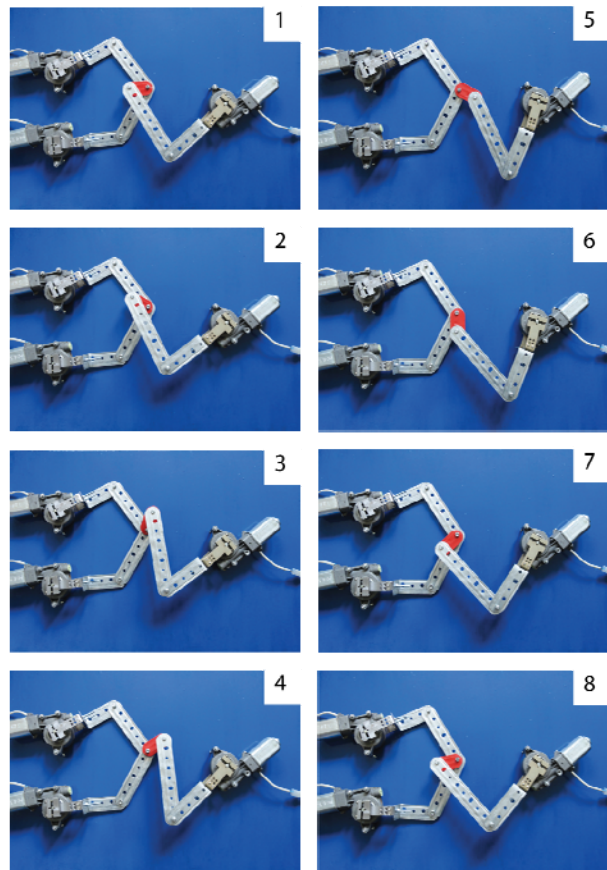


Fig. 7. Motion generation via a driven demonstrator built in the South-West State University of Kursk.

- two circles C_3 and C_6 , centred in O_3 , of radius equal to $L_{13} + L_{23} - R$ and $L_{13} - L_{23} + R$; these circle represents the extreme displacements of the robot end-effector linked to leg 3 for any platform orientation;

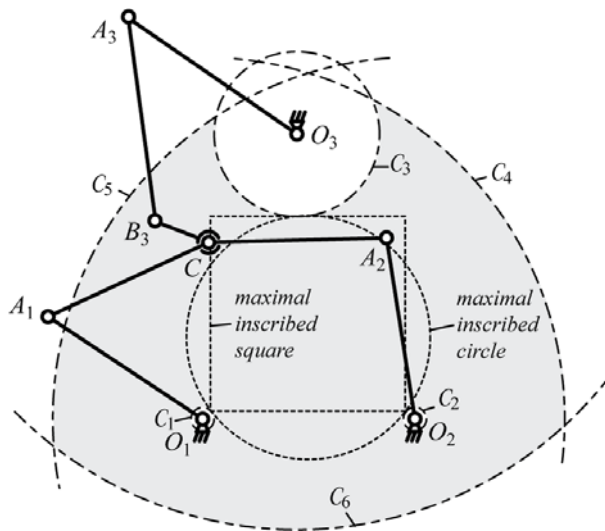


Fig. 8. Maximal reachable workspace of the robot (to scale).

As 5R robots have the ability to cross the Type 1 singular configurations [46], it can be shown that any of the workspace points can be attained without crossing of the Type 2 singular configurations presented at Fig. 3b, that are due to the 5R positioning architecture. It should also be mentioned that the Type 2 singularities presented at Fig. 3a, that appear for some specific platform orientations, can be crossed using optimal motion generation [47].

Taking into account these considerations, it is possible to define the maximal regular workspaces of the robot, for any platform orientation [48], [49]. It is proposed here to characterize the size of two different maximal regular workspaces: a circle and a square. Using some CAD software [50], it can be shown that, for this driven demonstrator:

- the maximal inscribed circle is centred in (90, 64.5) mm and has a radius of 105.75 mm
- the maximal inscribed square is centred in (90, 85) mm and has a edge length of 170 mm.

Finally, it should be noted that for dynamic tests a prototype will be developed with prescribed mass/inertia parameters and optimized control system.

VIII Conclusion

In this paper, the development of a new 3-DOF planar parallel manipulator with unlimited rotation capability was addressed. The advantage of the proposed design concept is the high rotational capability, which can be useful for many industrial applications: in automated assembly systems, cutting machines, simulators, micro-motion manipulators. This is a first publication, in which structural and kinematic properties were disclosed, as well as the shaking force and moment balancing. The linear displacements and orientation of the platform is

illustrated via a driven demonstrator, which is a first driven model of the manipulator.

Dynamic simulations, optimization and tests, that can perform this design concept will be a next step of this project.

Acknowledgments

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