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Luna.et.al.Latex.Source.tar.gz	



Solving large-scale real-world telecommunication problems using a grid-based genetic algorithm

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Abstract

This paper analyzes the use of a grid-based genetic algorithm (GrEA) to solve a real-world instance of a problem from the telecommunication domain. The problem, known as automatic frequency planning (AFP), is used in GSM networks (*Global System for Mobile communications*) to assign a number of fixed frequencies to a set of GSM transceivers located in the antennae of a cellular phone network. Real data instances of the AFP are very difficult to solve due to the NP-hard nature of the problem, so combining grid computing and metaheuristics comes out as a way to provide satisfactory solutions in a reasonable amount of time. GrEA has been deployed on a grid with up to 300 processors to solve an AFP instance of 2,612 transceivers. The results not only show that significant running times reductions are achieved, but that the search capability of GrEA outperforms clearly that of the equivalent non-grid algorithm.

Keywords: Frequency assignment problem; real-world problem solving; grid computing; genetic algorithms

1 Introduction

Frequency assignment is a well-known problem in Operations Research (Aardal, van Hoesel, Koster, Mannino and Sassano 2007) and it is of great importance in real GSM networks (*Global System for Mobile communications*) (Mouly and Paulet 1992). In these networks, the available frequency band is slotted into channels (or frequencies) that have to be allocated to the elementary transceivers (TRXs) installed in the base stations of the network. This problem is known as Automatic Frequency Planning (AFP), Frequency Assignment Problem (FAP), or even Channel Assignment Problem (CAP) (Eisenblätter 2001). An optimal

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8 frequency assignment allows the capacity of the networks to be increased by
9 avoiding the interferences provoked by channel reuse due to the limited available
10 radio spectrum, thus improving the quality of service for subscribers and an
11 income for the operators as well.

12 The AFP problem is an NP-hard problem (Hale 1980) which is even more
13 difficult to be addressed when defined in the context of GSM networks. In such
14 scenario, solving the problem properly requires realistic and precise interference
15 information from a real-world GSM network in order for an accurate frequency
16 plan to be computed. This information has to consider actual technologies cur-
17 rently used by GSM operators such as frequency hopping (Eisenblätter 2001).
18 This leads to further difficulties for telecommunication companies which, along
19 with the complexity of the problem itself and the large size of real-world net-
20 works, need accurate physical models of the GSM system (antennae, propaga-
21 tion, etc.). In this context, solving the AFP problem is a task demanding both
22 numerical and computational power in order to overcome the difficulties for find-
23 ing satisfactory solutions. The approach used in this work to cope with these
24 two practical requirements lies in using metaheuristics and grid computing.

25 Metaheuristics (Blum and Roli 2003) are a broad family of approximate
26 techniques that can be used to solve optimization problems. Contrary to exact
27 techniques, metaheuristics do not guarantee to find optimal solutions to the
28 problems, but they allow to reach good compromise solutions in a reasonable
29 amount of time. A metaheuristic can be defined a high level strategy which
30 controls a number of subordinated techniques (usually heuristics) in the search
31 for an optimum. These techniques are nowadays widely used. Among them,
32 Evolutionary Algorithms (EAs) and, in particular a subfamily of them, Genetic
33 Algorithms (GAs), have become very popular.

34 On the other hand, grid computing (Berman, Fox and Hey 2003, Foster and
35 Kesselman 1999) encompasses a number of issues related to the use of large-scale
36 distributed systems as a unique parallel computer. Grid computing systems are
37 a natural evolution of distributed systems in the way that the infrastructure
38 provided by the Internet allows hundreds and thousands of computers to be
39 joined, leading to a computing power that even supercomputers are unable to
40 provide; this way, algorithms which otherwise would be considered as unfeasible
41 can be executed in a reasonable amount of time.

42 In this paper, the performance of a distributed metaheuristic, a genetic algo-
43 rithm named GrEA, Grid-based Evolutionary Algorithm (Nebro, Luque, Luna
44 and Alba 2008), is analyzed. GrEA is designed to be executed in a grid com-
45 puting system based on Condor (Thain, Tannenbaum and Livny 2003), a grid
46 computing software. This algorithm has been applied to solve a real-world in-
47 stance of the AFP problem which corresponds to Denver (CO, USA), a city of
48 more than half a million people. This network is composed of 2,612 TRXs which
49 have to be assigned with 18 different available frequencies, so leading to a huge
50 search space of size $18^{2,612} \approx 5.11e^{3,263}$. A novel formulation of the problem pre-
51 sented in (Luna, Blum, Alba and Nebro 2007) has been used, which is directly
52 imported from real-world GSM frequency planning as currently conducted in
53 the industry.
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8 Even though the instances of any formulation of the problem are potentially
9 very large (e.g., the size of current cellular networks is continuously increas-
10 ing), few works approach this problem with parallel algorithms for addressing
11 the highly increasing computational resources required. In the field of EAs,
12 Crompton *et al.* (Crompton, Hurley and Stephens 1993, Crompton, Hurley and
13 Stephens 1994) presented a distributed GA (Alba and Troya 1999) that uses two
14 different encodings for the individuals and different recombination operators.
15 However, no details on the parallel computing platform are given. A parallel
16 GA for hybrid channel assignment is proposed by Kwok in (Kwok 2000). The
17 algorithm runs on a cluster composed of twelve Linux workstations. Many other
18 works exist in which the search model is parallel (Alba and Tomassini 2002), but
19 the execution is carried out on sequential machines, e.g., (Alabau, Idoumghar
20 and Schott 2002, Matsui, Watanabe and Tokoro 2005, Weinberg, Bachelet and
21 Talbi 2001). This is also a typical scenario in actual telecommunication com-
22 panies, where single computers—most times laptops—are used to perform the
23 optimization. Going one step further here, the AFP problem has been tackled
24 in a grid computing platform with the aim of solving a very large instance of
25 the problem in an affordable wall clock time.

26 The contributions of the present work can be summarized in the following
27 points:
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- 29 • A grid-based genetic algorithm has been used to solve a complex instance
30 of the AFP problem. To the best of our knowledge, this is the first time
31 this kind of problem is addressed with grid technologies (using up to 300
32 processors).
- 33 • An accurate statistical analysis has been carried out to validate the ob-
34 tained results.
- 35 • The study indicates that search capabilities of GrEA outperforms that of
36 the sequential counterpart.
- 37 • As a result of the experiments, the best solution to the considered problem
38 known so far has been obtained.

39 The rest of the paper is structured as follows. In the next section, the reader
40 is provided with details on the frequency planning in GSM networks. Section 3
41 details GrEA, the Grid-based GA approach. Some implementations details are
42 given in next section. In Section 5 the experimental results are presented and
43 analyzed. Finally, the conclusions and lines of future work are included in
44 Section 6.
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49 2 Frequency assignment in GSM networks

50 In the following, a brief description of the GSM architecture is provided first,
51 whereby the basic terminology of the problem is introduced. Next, the de-
52 tails on the frequency planning task in GSM networks are given. Finally, a
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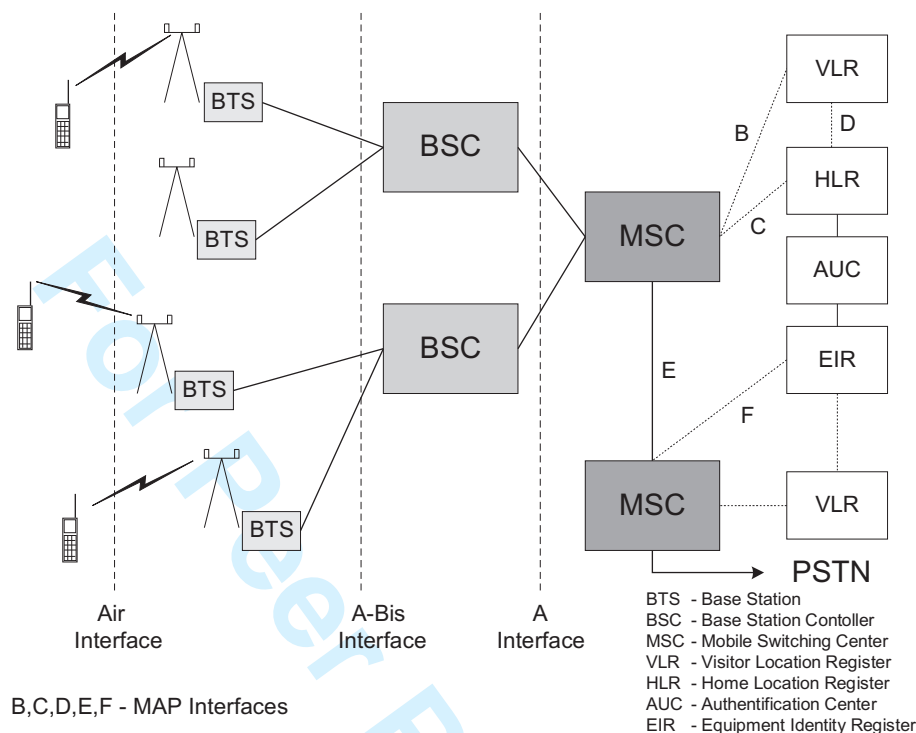


Figure 1: Outline of the GSM network architecture.

precise mathematical formulation of the AFP model addressed in this paper is presented.

2.1 The GSM system

An outline of the GSM network architecture is shown in Figure 1. As can be seen, GSM networks consist of many different components. The most relevant ones to frequency planning are the Base Transceiver Stations (BTSs) and the transceivers (TRXs). Essentially, a BTS is a set of TRXs. In GSM, one TRX is shared by up to eight users in TDMA (*Time Division Multiple Access*) mode. The main role of a TRX is to provide conversion between the digital traffic data on the network side and radio communication between the mobile terminal and the GSM network. The site at which a BTS is installed is usually organized in sectors: one to three sectors are typical. The area in which each sector operates defines a cell.

The solid lines connecting components in Figure 1 carry both traffic information (voice or data) as well as the “in-band” signaling information. The dotted lines are signaling lines. The information exchanged over these lines is necessary for supporting user mobility, network features, operation and maintenance, au-

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8 authentication, encryption, and many other functions necessary for the network's
9 proper operation.

10 11 2.2 Frequency planning in GSM networks

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13 The frequency planning is the last step in the layout of a GSM network. Prior
14 to tackling this problem, the network designer has to address some other issues:
15 where to install the BTSs or how to set configuration parameters of the antennae
16 (tilt, azimuth, etc.), among others (Mishra 2004). Once the sites for the BTSs
17 are selected and the sector layout is decided, the number of TRXs to be installed
18 per sector has to be fixed. This number depends on the traffic demand that the
19 corresponding sector has to hold. Frequency planning lies in the assignment of
20 a channel (a frequency) to every TRX (Eisenblätter 2001). The optimization
21 problem arises because the usable radio spectrum is generally very scarce and,
22 consequently, frequencies have to be reused by many TRXs in the network.

23 The multiple use of a same frequency may cause interferences that may
24 reduce the quality of service (QoS) down to unsatisfactory levels. Indeed, sig-
25 nificant interference may occur if the same or adjacent channels are used in
26 neighboring, overlapping cells. The point here is that computing this level of
27 interference is a difficult task which depends not only on the channels, but also
28 on the radio signals and the properties of the environment. The more accurate
29 the measure of the interference in a given GSM network, the higher the quality
30 of the frequency plan that can be computed for this network. Several ways of
31 quantifying this interference exist, ranging from theoretical methods to exten-
32 sive measurements (Kuurne 2002). They all result in a so-called *interference*
33 *matrix*, denoted by M . Each element $M(i, j)$ of M indicates the degradation
34 of the network quality if cells i and j operate on the same frequency. This is
35 called *co-channel interference*. Apart from co-channel interference, a so-called
36 *adjacent-channel interference* may exist, which occurs when two TRXs operate
37 on adjacent channels (i.e., one TRX operates on channel f and the other on
38 channel $f + 1$ or $f - 1$). An accurate interference matrix is therefore an essential
39 requirement for frequency planning because the ultimate goal of any frequency
40 assignment algorithm will be to minimize the sum of the interferences.

41 In real-life situations, additional complicating factors such as separation con-
42 straints among cells, or advanced interference reduction techniques such as fre-
43 quency hopping or dynamic power control may be considered. The interested
44 reader is referred to (Eisenblätter 2001) for a more detailed description of fre-
45 quency planning in actual GSM networks.
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48 2.3 Mathematical formulation

49 Let $T = \{t_1, t_2, \dots, t_n\}$ be a set of n transceivers, and let $F_i = \{f_{i1}, \dots, f_{ik}\} \subset \mathbb{N}$
50 be the set of valid frequencies that can be assigned to a transceiver $t_i \in T$,
51 $i = 1, \dots, n$. Note that k —the cardinality of F_i — is not necessarily the same
52 for all the transceivers. Furthermore, let $S = \{s_1, s_2, \dots, s_m\}$ be a set of given
53 sectors (or cells) of cardinality m . Each transceiver $t_i \in T$ is installed in exactly
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one of the m sectors. Henceforth we denote the sector in which a transceiver t_i is installed by $s(t_i) \in S$. Finally, given is a matrix $M = \{(\mu_{ij}, \sigma_{ij})\}_{m \times m}$, called the *interference matrix*. The two elements μ_{ij} and σ_{ij} of a matrix entry $M(i, j) = (\mu_{ij}, \sigma_{ij})$ are numerical values greater than or equal to zero. In fact, μ_{ij} represents the mean and σ_{ij} the standard deviation of a Gaussian probability distribution describing the carrier-to-interference ratio (C/I) (Walke 2002) when sectors i and j operate on a same frequency. The higher the mean value, the lower the interference and thus the better the communication quality. Note that the interference matrix is defined at sector (cell) level, because the transceivers installed in each sector all serve the same area.

A solution to the problem is obtained by assigning to each transceiver $t_i \in T$ one of the frequencies from F_i . A solution (or frequency plan) is henceforth denoted by $p \in F_1 \times F_2 \times \dots \times F_n$, where $p(t_i) \in F_i$ is the frequency assigned to transceiver t_i . The objective is to find a solution p that minimizes the following cost function:

$$C(p) = \sum_{t \in T} \sum_{u \in T, u \neq t} C_{\text{sig}}(p, t, u) . \quad (1)$$

In order to define the function $C_{\text{sig}}(p, t, u)$, let s_t and s_u be the sectors in which the transceivers t and u are installed, that is, $s_t = s(t)$ and $s_u = s(u)$, respectively. Moreover, let $\mu_{s_t s_u}$ and $\sigma_{s_t s_u}$ be the two elements of the corresponding matrix entry $M(s_t, s_u)$ of the interference matrix with respect to sectors s_t and s_u . Then, $C_{\text{sig}}(p, t, u) =$

$$\begin{cases} K & \text{if } s_t = s_u, |p(t) - p(u)| < 2 \\ C_{\text{co}}(\mu_{s_t s_u}, \sigma_{s_t s_u}) & \text{if } s_t \neq s_u, \mu_{s_t s_u} > 0, |p(t) - p(u)| = 0 \\ C_{\text{adj}}(\mu_{s_t s_u}, \sigma_{s_t s_u}) & \text{if } s_t \neq s_u, \mu_{s_t s_u} > 0, |p(t) - p(u)| = 1 \\ 0 & \text{otherwise.} \end{cases} \quad (2)$$

$K \gg 0$ is a very large constant defined by the network designer so as to make it undesirable allocating the same or adjacent frequencies to transceivers serving the same area. Furthermore, function $C_{\text{co}}(\mu, \sigma)$ is defined as follows:

$$C_{\text{co}}(\mu, \sigma) = 100 \left(1.0 - Q \left(\frac{c_{\text{SH}} - \mu}{\sigma} \right) \right) \quad (3)$$

where

$$Q(z) = \int_z^{\infty} \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}} dx \quad (4)$$

is the tail integral of a Gaussian probability distribution function with zero mean and unit variance, and c_{SH} is a minimum quality signalling threshold. Function Q is widely used in digital communication systems because it characterizes the error probability performance of digital signals (Simon and Alouini 2005). This means that $Q\left(\frac{c_{\text{SH}} - \mu}{\sigma}\right)$ is the probability of the C/I ratio being greater than c_{SH} and, therefore, $C_{\text{co}}(\mu_{s_t s_u}, \sigma_{s_t s_u})$ computes the probability of the C/I ratio

in the serving area of sector s_t being below the quality threshold due to the interferences provoked by sector s_u . That is, if this probability is low, the C/I value in the sector s_t is not likely to be degraded by the interfering signal coming from sector s_u and thus the communication quality yielded is high. (Note that this fits with the definition of a minimization problem.) On the contrary, a high probability —and consequently a high cost— causes the C/I mostly to be below the minimum threshold c_{SH} and thus incurring in low quality communications.

As function Q has no closed form for the integral, it has to be evaluated numerically. For this purpose, the complementary error function E has been used:

$$Q(z) = \frac{1}{2}E\left(\frac{z}{\sqrt{2}}\right) \quad (5)$$

In (Press, Flannery, Teukolsky and Vetterling 1992), a numerical method is presented that allows the value of E to be computed with a fractional error smaller than $1.2 \cdot 10^{-7}$. Analogously, function $C_{adj}(\mu, \sigma)$ is defined as

$$\begin{aligned} C_{adj}(\mu, \sigma) &= 100 \left(1.0 - Q\left(\frac{c_{SH} - c_{ACR} - \mu}{\sigma}\right)\right) \\ &= 100 \left(1.0 - \frac{1}{2}E\left(\frac{c_{SH} - c_{ACR} - \mu}{\sigma\sqrt{2}}\right)\right). \end{aligned} \quad (6)$$

The only difference between functions C_{co} and C_{adj} is the additional constant $c_{ACR} > 0$ (*adjacent channel rejection*) in the definition of function C_{adj} . This hardware specific constant measures the receiver's ability to receive the wanted signal in the presence of an unwanted signal at an adjacent channel. Note that the effect of constant c_{ACR} is that $C_{adj}(\mu, \sigma) < C_{co}(\mu, \sigma)$. This makes sense, since using adjacent frequencies (channels) does not provoke such a strong interference as using the same frequencies.

Our model ultimately aims at measuring the overall signalling performance of the GSM network. The keystone of this model is to be found in the definition of the interference matrix, which includes the entire probability distribution of the C/I ratio. This definition, which is directly imported from real world GSM frequency planning as currently conducted in the industry (and not generated in a computer by sampling random variables), allows not only the computation of high performance frequency plans, but also the prediction of QoS. Indeed, both the definition of the interference matrix and the subsequent computations to obtain the cost values are motivated by real-world GSM networks since they are related to the computation of the BER (Bit Error Rate) performance of Gaussian Minimum Shift Keying (GMSK), the modulation scheme used for GSM (Simon and Alouini 2005).

3 Using GrEA for solving the AFP problem

This section is devoted to presenting the algorithmic approach used for solving the AFP problem described in Section 2. Next, GrEA is introduced along with the representation of the individuals, the genetic operators applied, and a local search algorithm used to improve the solutions.

3.1 GrEA

GrEA (Nebro et al. 2008) is a steady state GA (ssGA) following the master/worker parallel model. It has been developed on top of Condor (Thain et al. 2003) and the MW framework (Linderoth, Kulkarni, Goux and Yoder 2000). GrEA is also a hybrid algorithm (Talbi 2002) since a local search method, which was specially designed for this AFP problem in (Luna et al. 2007), is applied to the individuals that are generated after the recombination and mutation operators. The basic idea is that a master process executes the main loop of the ssGA and the workers perform the function evaluations and the local search step in an asynchronous way. Contrary to a sequential ssGA, GrEA performs several individual evaluations in parallel; ideally, there should be as many parallel evaluations as available processors in the grid.

Algorithm 1 Pseudo-code for GrEA-master

```

1: population  $\leftarrow \emptyset$ 
2: Initialize taskList
3: while not stoppingCondition do
4:   Receive task
5:   individual  $\leftarrow$  task.individual
6:   Insert individual into population
7:   while new available workers do
8:     newIndividual  $\leftarrow$  GA_step()
9:     newTask  $\leftarrow$  new Task(newIndividual)
10:    taskList.add(newTask)
11:  end while
12: end while

```

For better describing the algorithm, let us call GrEA-master the part of the algorithm corresponding to the master process, as opposed to the worker counterpart, named GrEA-worker. The pseudo-code of GrEA-master is described in Algorithm 1. GrEA-master starts by creating an empty population (line 1) and generating a task list, each task containing an randomly generated individual (line 2). The tasks in the list are sent to the available workers by the underlying Condor system (see Section 4.2). After these two steps, GrEA-master works in a reactive way: when a task is received from a worker (line 4), the individual contained in that task is extracted (line 5), and it is inserted into the population (line 6). Then, for each new available worker detected, the following steps are carried out: first, a GA step (selection, recombination, and mutation) is executed (line 8), producing a new individual; second, this individual is added to a new task (line 9); finally, this task is inserted into the task list which is ready to be sent to a worker (by Condor).

The mission of GrEA-worker is to receive an individual, evaluate it, and apply the local search. Since the local search may modify the individual, it has to be returned back to the GrEA-master. The pseudo-code of GrEA-worker is included in Algorithm 2.

Algorithm 2 Pseudo-code for GrEA-worker

```

1: while true do
2:   Receive task
3:   individual  $\leftarrow$  task.individual
4:   newIndividual  $\leftarrow$  LocalSearch(individual)
5:   newTask  $\leftarrow$  new Task(newIndividual)
6:   Return newTask
7: end while

```

Salient features of GrEA are the awareness of new processors and fault tolerance. These characteristics play a key role in order to make GrEA a grid-enabled algorithm. Thus, whenever a new processor is detected by GrEA, a GA step is performed and a new individual is obtained for evaluation in the worker that will be deployed in the new processor. Concerning fault tolerance, crashes in GrEA-master are automatically managed by Condor by using checkpointing; faults in the processes running GrEA-worker are simply ignored because they do not affect the working principles of the genetic algorithm. For further details, the reader is referred to (Nebro et al. 2008).

3.2 Solution encoding and genetic operators

As defined in Section 2.3, a solution to the problem is obtained by assigning to each transceiver $t_i \in T$ one of the frequencies from F_i , the set of valid frequencies for TRX t_i . A solution is therefore encoded as an array of integer values, p , where $p(t_i) \in F_i$ is the frequency assigned to transceiver t_i . That is, the solutions manipulated by GrEA are tentative frequency plans of the given AFP problem instance.

As to the genetic operators, binary tournament has been used as the selection scheme. This operator works by randomly choosing two individuals from the population and the one having the best (lowest) fitness is selected. GrEA applies uniform crossover (UX) in which every allele of the offspring (i.e., the frequency of each TRX) is chosen randomly from one of the two parents with a probability of 0.5. Finally, the mutation operator used is random mutation, in which the frequencies of a set of randomly chosen TRXs of the solution are reassigned with a random valid frequency. Note that the two operators always assign valid frequencies to each TRX and no repair step is required.

It is well known that randomized genetic operators, and especially classical recombination operators, perform very badly in GAs for solving frequency assignment problems (Crisan and Mühlenbein 1998, Dorne and Hao 1995). However, when combined with an accurate local search method (hybridization), they achieve a good intensification/diversification tradeoff. This is the approach followed in this work: the highly randomized UX and random mutation are devoted to explore new regions of the search space, while the local search (see next section) is designed to seek for accurate solutions located in these regions.

3.3 Local search

In order for a GA to perform well on AFP problems, its hybridization with a local search algorithm is almost mandatory. Indeed, the most recent and efficient GAs for solving several flavors of the problem are endowed with some kind of local search: a probabilistic Tabu Search in (Alabau et al. 2002), an adaptation of Markov Decision Processes in (Idoumghar and Schott 2006), the CAP3 method in (Kim, Smith and Lee 2007), or others specifically designed for the problem being solved (Colombo 2006, Matsui, Watanabe and Tokoro 2003). The usage of local search turned out also to be essential in ACO algorithms for solving frequency assignment problems (Graham, Montemani, Moon and Smith 2007), and particularly in the version of the AFP problem used, as shown in (Luna et al. 2007).

Algorithm 3 Pseudo-code for the local search

```

1: input: a solution  $p$ , a number of steps  $d$ 
2:  $improved \leftarrow \mathbf{true}$ 
3:  $k \leftarrow 1$ 
4: while  $k \leq d$  and  $improved = \mathbf{true}$  do
5:    $improved \leftarrow \mathbf{false}$ 
6:   Rank every TRX  $t_i$  with  $CC(p, t_i)$ 
7:   for  $i \leftarrow 1$  to  $n$  do
8:     Replace frequency  $p(t_i)$  with the frequency from  $F_i$  that most reduces
     the objective function value
9:     if the objective function value was reduced then  $improved = \mathbf{true}$ 
10:    Update  $CC(p, t_i)$ 
11:   end for
12:    $k \leftarrow k + 1$ 
13: end while
14: output: a possibly improved solution  $p$ 

```

The local search method used in this work is included in Algorithm 3. It first ranks the TRXs with respect to their component cost, CC . Given a frequency plan p and a TRX t , $CC(p, t)$ is defined as

$$CC(p, t) = \sum_{u \in T, u \neq t} C_{\text{sig}}(p, t, u) \quad (7)$$

that is, $CC(p, t)$ is the value with which TRX t contributes to the total cost of the frequency plan p (Eq. (2) defines C_{sig}). This ranking allows the TRXs incurring in the strongest interference to be assigned in the beginning so as to quickly fix low quality assignments and to lead to further improvements. Then, all the TRXs are traversed and the frequency that most reduces the AFP cost of the entire plan (Eq. 1) is chosen (line 8). In the solved AFP instance, this would require $2,612 \times 18 = 47,016$ evaluations of the AFP cost at each step, which makes the local search unaffordable. Therefore, rather than using Eq. 1 for

computing the new objective function value, an incremental cost function has been used because the increase of the AFP cost caused by the setting $p(t_i) = f$ can be computed as follows:

$$\Delta(p, p(t_i) = f) = \sum_{t \in \hat{T}} (C_{\text{sig}}(p, t, t_i) + C_{\text{sig}}(p, t_i, t)) . \quad (8)$$

Finally, the component cost of each TRX is updated and a new iteration starts (line 10 of Algorithm 3) so as to reassign again first those TRXs that most contribute to the AFP cost. Parameter d indicates for how many steps this algorithm should be maximally executed. After some preliminary tests with the instance solved in this work (see Section 5.2), the local search converges towards a local minimum after six steps and this is the value used for the subsequent experimentation.

4 Implementation details

In this section a brief introduction to Condor is given as well as details about how the MW library is used to implement GrEA.

4.1 Condor

Condor is a Grid system software package designed to manage distributed collections (pools) of processors spread among a campus or other organizations (Thain et al. 2003). Each machine is supposed to have an owner, who can specify the conditions under which jobs are allowed to run; by default, a Condor job stops when a workstation's owner begins using the computer. Hence, Condor jobs use processor cycles that otherwise would be wasted. Compared to other grid computing software, Condor is easy to install and to administrate, and existing programs do not need to be modified or re-compiled to be executed under Condor (they must only be re-linked with the Condor library).

Salient features of Condor includes remote system calls, job checkpointing, and process migration. Furthermore, Condor pools can be composed of heterogeneous machines, and several pools can be combined using Globus (Foster and Kesselman 1997) and Condor-G (Frey, Tannenbaum, Foster, Livny and Tuecke 2001).

4.2 The MW library

GrEA has been implemented using MW (Linderoth et al. 2000), a software library that enables the development of master-worker parallel applications on top of Condor using C++.

An MW application consists mainly of subclassing three base classes: MW-Task, MWDriver, and MWWorker. A MWTask represents the unit of work to be computed by a worker. It includes the inputs and outputs to be marshaled to and from the workers. In this implementation, the input is an integer array

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8 (the permutation representing an individual) and the output is a real value con-
9 taining the fitness value plus another integer array (because the individual can
10 be modified by an improvement method). The MWWorker provides the context
11 for the task to run; in concrete, in GrEA the subclass of MWWorker contains
12 the GrEA-worker code. Finally, the MWDriver subclass manages the whole
13 process: creating tasks, receiving the results of the computations, and deciding
14 when the computation is complete. The GrEA-master code is executed in this
15 subclass.

16 The MW framework works with Condor to find computing resources for
17 the available tasks, handle communication between the nodes, re-assign tasks if
18 their current machine fails, and globally manage all the parallel computations.
19 That is, MW generates tasks whose computation is subsequently managed by
20 Condor. MW provides hooks to save the state of the driver, so that if the driver,
21 or its machine crashes, the computation can make progress upon driver restart.

22 MW can run with one of several RMComm (Resource Management and
23 Communication) implementations. This layer implements communication be-
24 tween the master and the workers, and the management of the worker ma-
25 chines. There are several choices, including communicating via PVM, sockets,
26 and shared files. We have chosen the last option because it is the most ro-
27 bust; for example, if the driver (master) crashes, the workers can continue their
28 computation, which is not possible using PVM and sockets. Although process
29 communication using files is rather slow, this application is not intensive in data
30 exchanges, and the communication costs can be acceptable if the computation
31 time is long enough.
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34 4.3 Grid platform details

35 In the experiments the computers of seven laboratories of the Computer Science
36 Department of the University of Málaga have been used. Many of them are
37 equipped with PCs having modern Intel Core 2 Duo, 3 GHz processors. This
38 means that each processor has two cores, so Condor assumes that there are
39 two processors per computer. For the sake of clarity, the term *processor* will
40 be used throughout the paper, although the correct term is *core*. The Condor
41 pool also includes slower single-core machines with Pentium 4 at 1.66 GHz and
42 AMD Athlon at 1.1 GHz and 2.0 GHz. Up to 300 processors have been used,
43 being all interconnected through a 100 Mbps Fast Ethernet network. The code
44 is written in C++, and all the machines run different flavors of Linux (Fedora
45 Core, Debian, SuSE, etc.).
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48 5 Results

49 This section presents the experiments conducted to evaluate GrEA. First, some
50 details of the algorithm settings are given and, second, the GSM network in-
51 stance used is described. Finally, the experiments are presented from the point
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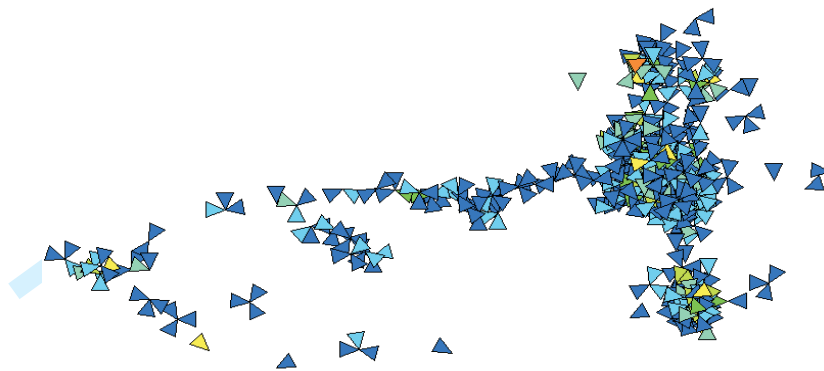


Figure 2: Topology of the GSM network used.

of view of both parallelism (the parallel efficiency, the workers used, and the tasks computed per minute are analyzed in detail) and numerical accuracy.

5.1 Experimental setup

The results of running the sequential counterpart of GrEA has been included here. It is a standard ssGA which uses the same operators (selection, crossover, mutation, and local search). The aim is to test the performance of GrEA in terms of both the parallelism of the grid-based approach and its numerical accuracy. The parameter settings of these two GAs are detailed in Table 1.

Because of the stochastic nature of GAs, 30 independent runs of GrEA have been done, but only ten runs of ssGA were performed due to time constraints (each execution lasts more than five days on a Pentium IV at 2.8 GHz). Working with real problems and grids is very hard, and thus a small number of independent runs is usually reported (Kuś 2007, Lim, Ong, Jin, Sendhoff and Lee 2007, Melab, Cahon and Talbi 2006). The same is done here with ssGA, but reporting on 30 independent runs for GrEA, a value considered as a minimum for statistical significance.

5.2 GSM instance used

The GSM network used here has 711 sectors with 2,612 TRXs to be assigned a frequency; the constants in Equations 2, 3, and 6 were set to $K = 100\,000$, $c_{SH} = 6\,dB$, and $c_{ACR} = 18\,dB$, respectively. Each TRX has 18 available channels (from 134 to 151). Figure 2 displays the network topology, every triangle representing a sectorized antenna in which operate several TRXs.

This GSM network is currently operating in Denver (CO, USA), a 400 km² city with more than 500,000 people, so its solution is of great practical interest. The data source to build the interference matrix based on the C/I probability distribution uses thousands of Mobile Measurement Reports (MMRs) (Kuurne

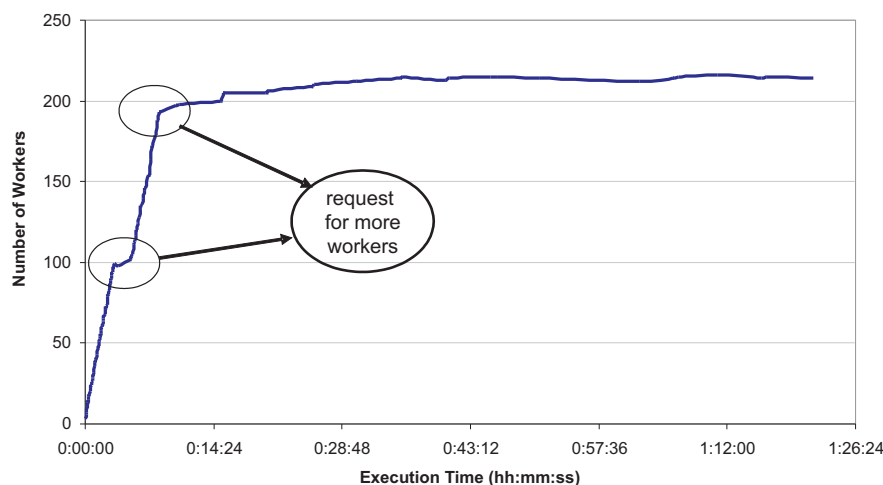


Figure 3: Number of workers during a typical GrEA execution.

2002) rather than propagation prediction models. MMRs are a more accurate data source, as they capture the call location pattern in the network and do not rely on predictions. These properties make this GSM problem more realistic than standard available benchmarks (FAP Web 2008). Indeed, the most similar available instances are the COST 259 benchmark, but the basic traffic load is drawn at random according to an empirically observed distribution, and signals are predicted with several propagation models. The Philadelphia, CELAR and GRAPH instances (FAP Web 2008) are even simpler.

5.3 Parallel performance

In this section the performance of GrEA is analyzed when solving the considered AFP network. Table 2 summarizes the best value, the mean, \bar{x} , and the standard deviation, σ_n , of several performance measures.

Although the Condor pool is composed of 300 processors at most, a maximum number of 282 have been used, and 235 on average. This is typical behaviour of grid computing systems, where the number of available processors is dynamic, and they have to be shared among different users.

If the average number of active workers is considered, it is around 140 on average. This is a consequence of the behaviour of GrEA under Condor/MW. Whenever an MW application has tasks to be computed, it asks the Condor system for available workers. The way MW asks for more workers to Condor is by requesting a predefined number of them. This fixed number is configurable and it has been set up to be 100 workers. This value corresponds to the set of initial tasks created to evaluate the initial population, thus guaranteeing that

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8 there will be in the beginning one worker for each task. This effect can be
9 observed in Fig. 3. It can be seen that, at the beginning of the computation,
10 the number of worker tasks increase up to 100; after a few minutes, another
11 100 processors are requested to the grid system. Finally, the algorithm obtains
12 the rest of available processors. Although the total number of processors are
13 roughly constant (about 220 in the execution depicted in Fig. 3), the average
14 number of them is affected by the initial stage of the algorithm.

15 An advantage of using grid computing systems is to solve, in a reasonable
16 amount of time, problems which otherwise would be considered as unfeasible.
17 In Table 2 it can be observed that the average total CPU time reported by
18 Condor (i.e., the sum of the computing time of all the processors) is near to
19 8 days, while the wall clock time is 1.36 hours (more than 139 times faster).
20 These values clearly state the benefits of using the proposed approach.

21 The parallel performance reported by Condor is about 72% (a parallel effi-
22 ciency of 0.72), which can be considered as an excellent result in a grid platform.
23 However, the computation/communication could be improved by using a more
24 computing intensive local search. Additional experiments have been done with
25 10 and 20 local search steps ($d = 10$ and $d = 20$), and the parallel performance
26 grew up to 81% and 90%, respectively. The point here is that the local search
27 strategy is so accurate that it reaches a local optimum after five or six iterations,
28 and therefore the numerical results are similar to the ones reported in this work.
29 It is clear then that there is room for increasing the efficiency of GrEA.

30 The last two rows of Table 2 include the computing times of the sequential
31 ssGA when solving the considered AFP problem (about 5.4 days), as well as
32 the parallel efficiency against the average wall clock time required by GrEA.
33 When comparing both ssGA and GrEA, the efficiency goes down to 41.28%.
34 The explanation is twofold. On the one hand, ssGA has been compiled with
35 several optimization options to speedup the computation as much as possible,
36 and some of them are related to the type of processor of the machine where the
37 program runs; these options are disabled in GrEA due to the heterogeneity of
38 the processors in the grid. On the other hand, there are processors in the grid
39 platform that are much slower (see Section 4.3) than the one used to run ssGA,
40 a Pentium 4 at 2.8 GHz, so therefore workers spend longer times to compute the
41 same tasks thus delaying the entire computation. However, in practical terms,
42 ssGA requires more than five days to solve the problem while the grid only
43 needs one hour and a half, so the benefits of this approach still holds.

44 The throughput (tasks computed per minute) of GrEA when solving the
45 AFP problem is analyzed next. In Fig. 4 it can be observed that this number
46 remains almost constant around 630 tasks per minute. This contrasts with the
47 behaviour of the algorithm reported in (Nebro et al. 2008), where the throughput
48 dropped in time due to the computation time of the tasks decreasing when the
49 search progressed (from 30 seconds at the beginning down to two seconds at
50 60% of the computation). This issue does not appear when evaluating the AFP,
51 so it is not necessary to dynamically adjust the computation grain as in (Nebro
52 et al. 2008).
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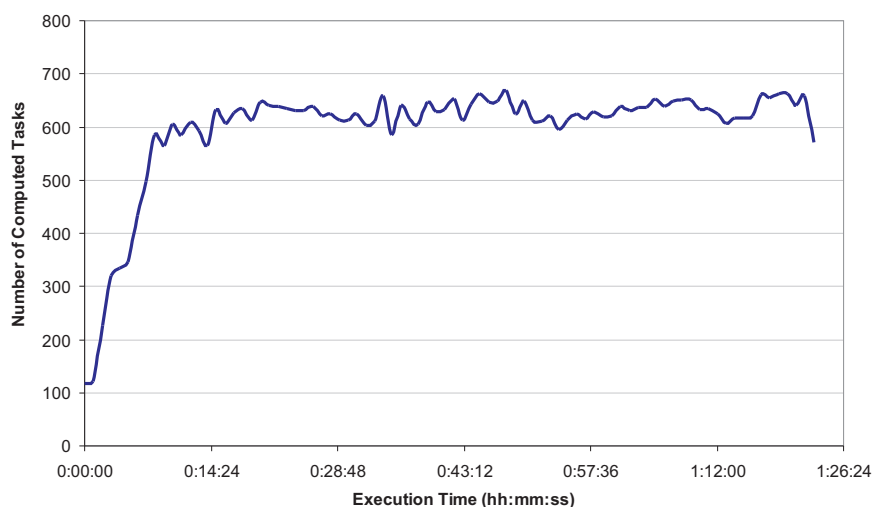


Figure 4: Tasks per minute computed by GrEA.

5.4 Accuracy

In this section the numerical efficiency of GrEA is compared to both ssGA and the algorithm which reported the best results for this problem so far, the ACO presented in (Luna et al. 2007) (its parameterization is detailed in the given reference). Even though the GAs and the ACO algorithm are not directly comparable (the ACO execution time was limited to 30 minutes because other measures were used), the previous results on the problem cannot be ignored and they are included both for completeness and for showing the competitiveness of this proposals.

Table 3 includes the best (lowest), the mean, \bar{x} , and the standard deviation, σ_n , of the resulting AFP costs reached by the three algorithms. As stated before, 30 independent runs for GrEA and 10 for ssGA have been run. For the ACO algorithm, the results reported in (Luna et al. 2007) have been used. An accurate statistical analysis has been performed here in order to numerically compare the algorithms with confidence (Demšar 2006, Sheskin 2003). Firstly, a Kolmogorov-Smirnov test is performed in order to check whether the values of the results follow a normal (gaussian) distribution or not. If the distribution is normal, the Levene test checks for the homogeneity of the variances. If samples have equal variance (positive Levene test), an ANOVA test is done; otherwise a Welch test is performed. For non-gaussian distributions, the non-parametric Kruskal-Wallis test is used to compare the medians of the algorithms. Fig. 5 summarizes the statistical analysis. A confidence level of 95% is always considered (i.e., significance level of 5% or p -value under 0.05) in the statistical tests,

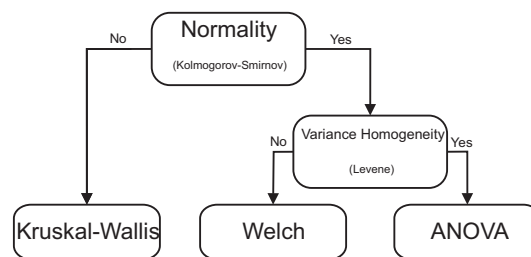


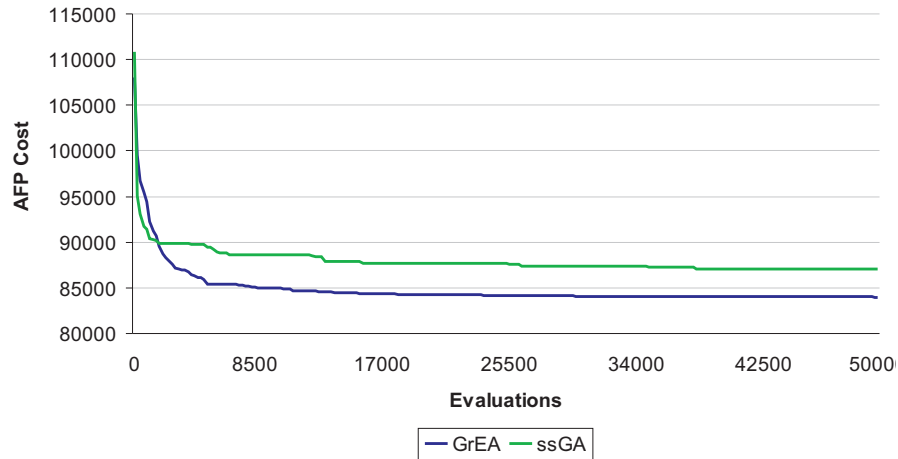
Figure 5: Statistical analysis performed in this work.

which means that the differences are unlikely to have occurred by chance with a probability of 95%. The result tables show \bar{x} and σ_n because all the samples follow a gaussian distribution. The cell having the best result has a gray colored background.

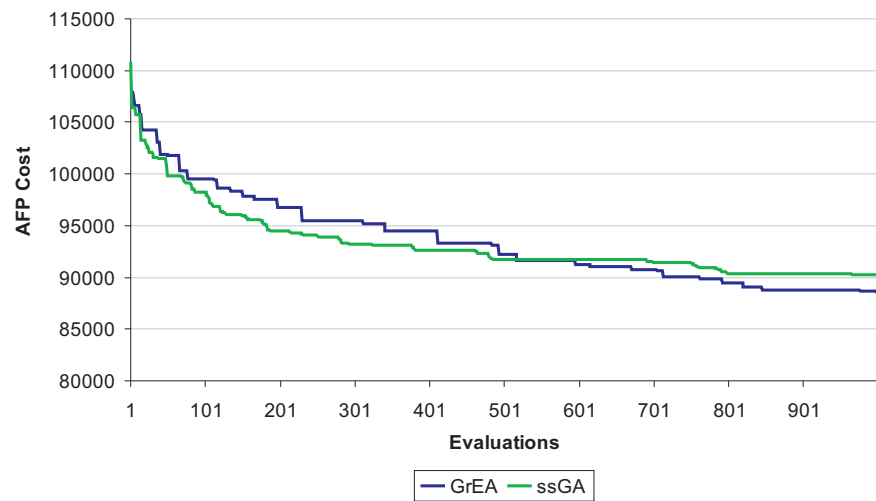
To further analyze the results statistically, a post-hoc testing phase has been included in Table 4 which allows for a multiple comparison of the samples. The `multcompare` function provided by Matlab © has been used. This function chooses the most appropriate type of critical value to be used in the multiple comparison, which ranges from the more conservative *HSD* or *Tukey-Kramer* method to less conservative *Scheffe's S* procedure (Hochberg and Tamhane 1987). The same confidence level has been kept for this testing phase ($\alpha = 0.05$). The “+” symbols in the table point out that all pairwise comparisons among the algorithms are significant.

The first conclusion that can be drawn from the results is that the two GAs outperform the ACO algorithm. As stated before, this is somehow expected because the computational effort used in the GAs is pretty much larger than the ACO one. The improvements are noticeable in both the best solution (88,345.95 down to 83,991.30) and the average solution (90,382.56 down to 84,936.32). If σ_n is considered as a measure of robustness, GrEA and ssGA also outperform the ACO approach.

But the really interesting fact that Table 3 shows is that GrEA has computed more accurate frequency plans (lower AFP costs) than its sequential counterpart, ssGA, and with statistical confidence, as the “+” symbols of Table 4 show (indeed, this is the only actual goal of companies). The relevance of these results arises because these two algorithms share the same operators and parameter settings, and they also use the same computational effort. The only difference is the asynchronism introduced in GrEA, in which individuals evaluated by slower processors are returned back when several iterations (with individuals sent to faster processors) have proceeded. This means a higher diversity in the search is introduced, especially in the early steps, which later guides the algorithm towards high quality solutions (Alba and Troya 2001). Figure 6 graphically displays this fact by including the best AFP cost of a typical run of GrEA and ssGA. In the left-hand side of the figure the evolution of the fitness during the entire computation (50,000 iterations) is shown. It can be seen that GrEA gets



(a)



(b)

Figure 6: Evolution of the AFP cost in GrEA and ssGA during (a) the whole execution and (b) the 1,000 first iterations.

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8 stuck later than ssGA and from then they both improve the solution slightly. In
9 Fig. 6b the first 1,000 generations of the same execution have been enlarged in
10 order to show the higher diversity in GrEA at the beginning of the computation.
11 Indeed, ssGA outperforms GrEA in the first 500 iterations, but it finds difficul-
12 ties to continue after that (see the flat regions during iterations 500 and 700).
13 In the meanwhile, GrEA keeps improving the solution. Within the context of
14 this work, it can be concluded that deploying a ssGA on the grid is not only a
15 way of reducing the computational time, but also of improving the underlying
16 search models which allow the algorithm to compute more accurate solutions.
17

18 6 Conclusions and future works

19
20 This work addresses a real-world instance of the AFP problem. The considered
21 instance has a huge search space, so the approach has been to combine the use
22 of metaheuristics (numerically powerful) and grid computing (computationally
23 powerful). In particular, the algorithm GrEA has been used. It is a grid-
24 enabled GA that runs on a grid platform composed up to 300 processors.
25

26 The problem has been first analyzed from the point of view of its solution
27 by a sequential GA; thus, issues such as the problem representation, genetic
28 operators (selection, mutation, crossover), and local search strategy, have been
29 addressed. A very accurate formulation has been used, which is rarely found in
30 the literature of this problem. Second, the GrEA algorithm has been applied
31 to solve a complex AFP instance corresponding to an actual city in the USA
32 (Denver).
33

34 The experiments carried out reveal that ssGA requires about five days of
35 computation in a modern PC, while executing GrEA in the grid reduces the
36 times to one hour and a half. The overall parallel efficiency obtained is around
37 72%, which is a quite satisfactory value considering the number of processors
38 used and that the shared files in Condor is being used as the message passing
39 mechanism. This value also suggests that there is more room for improve-
40 ment; for example, more steps in the local search could bring a better compu-
41 tation/communication ratio.

42 While the reduction of the computing time from several days to less than
43 two hours is an interesting result in practical terms, it is also remarkable that
44 the search capability of the GrEA algorithm outperforms that of the equivalent
45 sequential GA. The fact that better (lower) fitness values can be obtained in
46 the parallel algorithm would allow us to reduce the computing time even more
47 in order to have high quality solutions in shorter times; this can be useful
48 in real scenarios, where telecommunication companies need to perform many
49 simulations to achieve a satisfactory frequency plan for large cities (like Los
50 Angeles, with more than 40,000 TRXs).

51 As future work, we are interested to use GrEA to solve even more larger
52 instances of the AFP (e.g., the aforementioned Los Angeles instance). The use
53 of this algorithm to solve other problems from the telecommunication domain,
54 such as ACP (Automatic Cell Planing), is a matter of future research.
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Table 1: Parameter settings of the GAs

Parameter	Value
Population size	100 individuals
Representation	Integer (array of size 2,612)
Crossover operator	Uniform Crossover ($p_c = 0.5$)
Mutation operator	Random ($p_m = 0.01$)
Local Search Steps	6
Selection method	Binary Tournament
Replacement strategy	Worst Individual
Stopping Condition	50,000 iterations

Table 2: Performance measures of GrEA.

Measure	Best value	\bar{x}	σ_n
Max Number of Workers	282	235	24
Average Number of Active Workers	164	140	10
Total CPU Time (s)	659,149 (7.62 days)	680,274 (7.87 days)	8,476
Wall Clock Time (s)	4,094 (1.14 hours)	4,879 (1.36 hours)	429
MW Parallel Performance	73.44%	71.79%	0.72%
Sequential ssGA Time (s)	463,014 (3.36 days)	473,259 (5.48 days)	12,321
Average Parallel Efficiency		41.28%	

Table 3: Numerical efficiency of the algorithms.

Algorithm	AFP Cost		
	Best (min)	\bar{x}	σ_n
ACO	88,345.95	90,382.56	935.31
ssGA	85,463.20	86,234.68	523.75
GrEA	83,991.30	84,936.32	375.89

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For Peer Review Only

Table 4: Post-hoc tests of the results.

ssGA	+	
GrEA	+	+
	ACO	ssGA

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