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Arnaud Dupays, Carlo Rizzo, Bignami Giovanni Fabrizio. Quantum vacuum influence on pulsars spindown evolution. EPL - Europhysics Letters, 2012, 98 (4), pp.49001. 10.1209/0295-5075/98/49001 . hal-00522696

HAL Id: hal-00522696

<https://hal.science/hal-00522696>

Submitted on 1 Oct 2010

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Quantum Vacuum influence on the evolution of Pulsars

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(Dated: October 1, 2010)*

In this letter we show that Quantum Vacuum Friction (QVF) should play an important role in neutron star evolution. Taking into account this effect we show that magnetars could be understood as a natural evolution of standard pulsars. For the Crab pulsar, of which the characteristic age is known, we present the first completely coherent time evolution for its period and braking index. For this pulsar we also give the predicted value of the current first derivative of the braking index, providing a very important test to confirm QVF.

PACS numbers:

Keywords:

One of the most fundamental Quantum ElectroDynamics (QED) prediction concerns electric and magnetic properties of vacuum [1, 2]. Following this idea, vacuum can be regarded as a standard medium with its own electromagnetic properties. Nevertheless, effects related to these properties are extremely weak and can only be tested in the presence of a very high electromagnetic field. For that reason, pulsars are very appropriate systems to look for evidences for vacuum properties [3, 4]. Pulsars are fast-rotating neutrons stars, with a very high magnetic dipole moment tilted with respect to their rotational axis. Typically, their mass is of the order of the solar mass, and their radius of the order of 10 km. But the most interesting feature of these stars is certainly their magnetic field which can exceed 10^8 T on their surface [5]. Pulsars are thus suitable laboratories to study magnetic properties of the surrounding vacuum. In particular, a class of pulsars called magnetars [6] is characterized by a long spinning period and a magnetic field on the surface which is supposed to be even greater than the QED critical field 4×10^9 T [7, 8]. At such a field non linear properties of quantum vacuum cannot be neglected. In general, the surface magnetic field of pulsars is inferred by comparing the measured period derivative with the one obtained using the energy loss rate given by the classical formula for a radiating rotating magnetic dipole. We believe that inferring a field exceeding the QED critical one using a pure classical formula (which neglects any QED effect) is questionable. Heyl et al. [9, 10] have shown that the energy loss rate of a radiating rotating magnetic dipole, calculated by taking into account QED differs very little by the classical one. The

use of a QED formula for the radiating dipole does not change in practise the inferred magnetic field on the surface of the pulsar.

Very recently, we have shown that a new energy loss process for pulsars should be taken into account, namely Quantum Vacuum Friction (QVF) resulting from the interaction between the non-stationary magnetic dipole moment of the star and its induced quantum vacuum magnetic dipole moment [11]. In the case of magnetars, with very high magnetic fields, we have shown that the QVF is the dominating energy loss process and has important consequences. In particular, the inferred value of the magnetic field no longer exceeds the QED critical field for all known magnetars.

In this letter we consider some astrophysical consequences of QVF. We show that QVF plays a crucial role in neutron star evolution. Taking into account this effect, we show that magnetars can simply be understood as a natural evolution state of typical pulsars, similar to the Crab pulsar. For the Crab pulsar, of which the characteristic age is known, we present the first completely coherent time evolution for its period and braking index. Let us first summarize the main results concerning QVF in highly magnetized neutron stars. Considering a neutron star rotating in vacuum, we denote by R its radius and B_0 the magnitude of the magnetic field at its surface. If P is the spinning period of the neutron star and θ the inclination angle of its magnetic dipole moment with respect to the rotation axis of the star, one can show that for $B_0 \leq 10^{10}$ T, the QVF energy loss rate \dot{E}_{qv} is given

by [11]

$$\dot{E}_{qv} \simeq \alpha \left(\frac{18\pi^2}{45} \right) \frac{\sin^2 \theta}{B_c^2 \mu_0 c} \frac{B_0^4 R^4}{P^2} \quad (1)$$

where $B_c = m_e^2 c^3 / e \hbar \simeq 4.4 \cdot 10^9$ T is the QED critical field, α the fine structure constant, μ_0 the vacuum permeability and c the light velocity in vacuo. Total energy loss rate of the star \dot{E} can thus be obtained by adding the classical dipolar radiative energy loss rate \dot{E}_r given by

$$\dot{E}_r = \left(\frac{128\pi^5}{3} \right) \frac{\sin^2 \theta}{\mu_0 c^3} \frac{B_0^2 R^6}{P^4} \quad (2)$$

It is important to stress that the spinning period dependence is not the same for the classical radiative process and for the QVF. The ratio of classical to QVF losses decreases like $1/P^2$ for large P , so that QVF becomes more important for slowly rotating neutron stars. Let us now study how QVF drastically changes the evolution of a pulsar. The evolution of a pulsar in period P and slowdown \dot{P} is usually described in a logarithmic $P - \dot{P}$ diagram as shown in fig. 1, where we have plotted all of the currently known pulsars (~ 1700) for which P and \dot{P} have been measured [12]. On this diagram, we have also indicated lines of constant magnetic field in the case where only the classical radiative energy loss process is considered (dotted lines) together with the case for which QVF is taken into account (solid curves). These lines are obtained by matching the loss in rotational energy \dot{E} with $\dot{E}_r + \dot{E}_{qv}$. Since \dot{E} is given by

$$\dot{E} = 4\pi^2 I \dot{P} P^{-3} \quad (3)$$

where a neutron star moment of inertia of $I = 10^{45}$ g.cm² is assumed, we get

$$\dot{P} = \left(\frac{32\pi^3}{3I} \right) \frac{B_0^2 R^6}{\mu_0 c^3 P} + \alpha \left(\frac{3}{16I} \right) \frac{B_0^4 R^4 P}{B_c^2 \mu_0 c} \quad (4)$$

where $\sin \theta$ is taken, as usual, equal to 1. The first term in eq. (4) corresponds to the classical contribution, which gives the asymptotic behaviour for small P . The second term is the correction due to QVF, which becomes important for large P . In fig. 1 we clearly distinguish two different evolution areas : pulsars located in the upper right area of the figure (gray) have an energy loss process dominated by QVF, whereas pulsars in the lower left area have classical magnetic dipole emission as the main energy loss. Defining the borderline between both areas as

$$\frac{d \log \dot{P}}{d \log P} = 0 \quad (5)$$

we get

$$\frac{\ddot{P} P}{\dot{P}^3} = 0 \quad (6)$$

Since $P \neq 0$, this equation implies that $\ddot{P} = 0$ and thus, the borderline between both areas corresponds to pulsars having a constant slowdown \dot{P} . Assuming that the

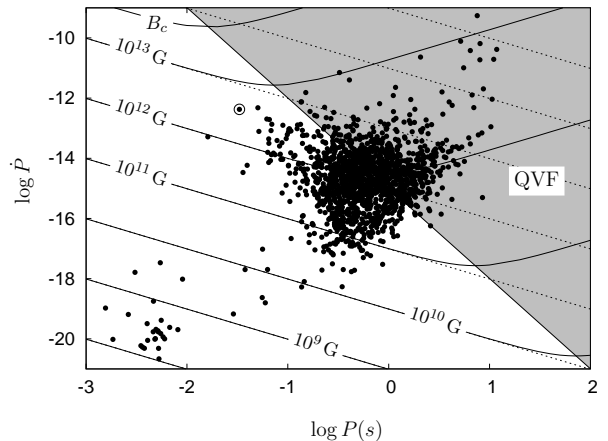


FIG. 1: $P - \dot{P}$ -diagram for the currently known pulsars. Pulsars located in the upper right area (gray) have an energy loss process dominated by QVF. The Crab pulsar is marked as a circle filled with a dot.

pulsar's magnetic field to remain constant during its evolution, we can describe the evolution of the star following the line on which it is situated today. Let us first ignore QVF. Since the rotational period of a pulsar increases with time, the natural evolution of these stars corresponds to a fall towards the lower right area of the figure along a given straight dotted line, depending of the value of their magnetic field. In this case, pulsars located in the upper right area can exhibit surface magnetic fields above the quantum critical field. Since these stars cannot be connected by a straight line of constant magnetic field to other pulsars with lower rotational period, we have to assume that these stars are very young, even if their rotational period is already high. For that reason, this class of pulsars, called magnetars, seems to be very different in nature from other standard pulsars. To understand the structure of these stars and the physical process involved which should give rise to such a huge surface magnetic field remains an open question. If we take into account QVF, we see that all magnetars are now connected by a modified line of constant magnetic field to pulsars with lower rotational period. Remarkably enough, their surface magnetic field becomes lower than the critical quantum field. We can then conclude, as far as QVF exists, that magnetars could be understood as a natural evolution of standard pulsars. Such a very important astrophysical consequence of quantum vacuum effect shows that testing the validity of the QVF theory would be crucial in the future to understand pulsars physics. It is also important to stress that with magnetic fields below the critical quantum field, the current explanation for the emission properties of Anomalous X-ray Pul-

sars (AXPs) and Soft Gamma-ray Repeaters (SGRs) can not be applied to our model [13], and so, this emission remains an open question. Another interesting result of taking QVF into account in magnetized rotating neutron stars is a completely coherent time evolution of pulsars, as we will show in the following. Let us illustrate this point in detail with the Crab pulsar (the one marked as a circle filled with a dot in fig.1). Situated in the center of the Crab Nebula which is the remnant of the Super Novae SN1054, the Crab pulsar is certainly one of the most well-known pulsars [14]. A very interesting feature of this pulsar is that historical records indicate its characteristic age to be ~ 955 yr. This indication, together with accurate measurements of its current spin period P , first and second time derivative of the spin period, respectively \dot{P}_1 and \dot{P}_2 , drastically constrains its rotational evolution dynamics. Rewriting eq. (4) as

$$\dot{P} = \frac{K_r}{P} + K_{qv}P \quad (7)$$

where $K_r = \dot{E}_r \times (P^4/4\pi^2 I)$ and $K_{qv} = \dot{E}_{qv} \times (P^2/4\pi^2 I)$, the age of a pulsar τ is given by

$$\tau = \int_{t_0}^t dt' = \int_{P_i}^P \frac{dP'}{\frac{K_r}{P'} + K_{qv}P'} \quad (8)$$

where t denotes the current date and P_i the initial spin period at $t = t_0$. We obtain

$$\tau = \frac{1}{2K_{qv}} \ln \left(\frac{K_r + K_{qv}P^2}{K_r + K_{qv}P_i^2} \right) \quad (9)$$

If $K_{qv} \ll K_r$ eq. (9) becomes

$$\tau \simeq \frac{1}{2K_r} (P^2 - P_i^2) \quad (10)$$

From eq. (7) we have in this case $K_r \simeq \dot{P}P$, so that

$$\tau \simeq \frac{P}{2\dot{P}} \left(1 - \left(\frac{P_i}{P} \right)^2 \right) \quad (11)$$

which is the expression usually employed to estimate the characteristic age of a pulsar. Inverting eq. (9) (resp. eq. (11)) we obtain the spin period as a function of time when classical and QVF energy loss processes are taken into account (resp. when QVF is neglected). Both cases are presented in fig. 2 for the Crab pulsar. In this figure, $t = 0$ corresponds to current time (i.e "today"). Since the age of this pulsar is known, we can estimate the initial spin period P_i .

Using the classical expression we obtain $P_i = 16$ ms, whereas we get $P_i = 18$ ms when QVF is taken into account. Since the energy loss process of the Crab pulsar is dominated by classical radiation (see fig. 1), we are not surprised that the global time evolution of this star does not drastically change when QVF effects are

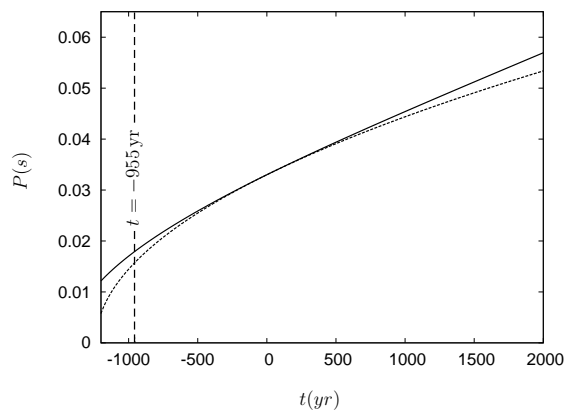


FIG. 2: Spin period of the Crab pulsar as a function of time when QVF is taken into account (full line) and when QVF is neglected (dotted line). $t = 0$ corresponds to current time (i.e "today").

included. Nevertheless, the most important difference between both calculations is that the one taking into account QVF is the only one which provides a spin period evolution completely coherent with current observations, in particular with the current value of the braking index, as we will discuss in the following.

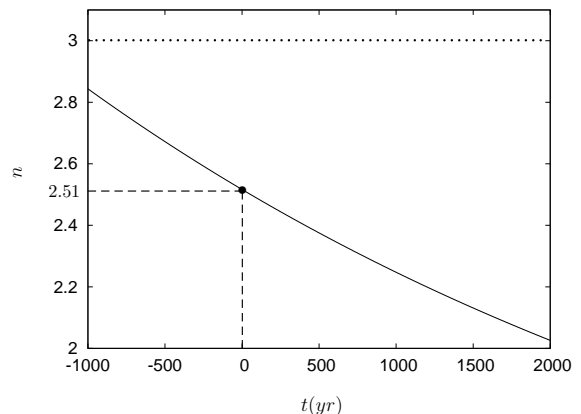


FIG. 3: Braking index of the Crab pulsar as a function of time when QVF is taken into account (full line) and when QVF is neglected (dotted line). $t = 0$ corresponds to current time.

The braking index, n , is a fundamental dimensionless quantity given by [15]

$$n = \frac{\nu \ddot{\nu}}{\dot{\nu}^2} \quad (12)$$

where ν is the spin frequency of the pulsar and $\dot{\nu}$ (resp. $\ddot{\nu}$), denotes the first (resp. the second) derivative of ν with respect to time. This parameter describes the rate at which a pulsar loses rotational energy. Introducing the spin period $P = 1/\nu$, we rewrite the braking index as

$$n = 2 - \frac{P\ddot{P}}{\dot{P}^2} \quad (13)$$

From this expression we see that the borderline between gray and white plotted in fig. 1 corresponds to pulsars having a braking index equal to 2 ($\dot{P} = 0$). Pulsars located in the upper right area of the figure (gray) have a braking index lower than 2, whereas braking index of pulsars in the lower left area is higher. In the following we study the time evolution of n for $t > 0$. We denote by P_0 the current spin period, and by P_1 and P_2 , the current values of the first and the second derivative of P with respect to time. The current value of n is

$$n_0 = 2 - \frac{P_0 P_2}{P_1^2} \quad (14)$$

At this stage it is important to stress that the constant value $n = 3$ is expected for pure classical radiation models, whereas the current measured value is $n_0 = 2.51$ for the Crab pulsar. This discrepancy shows that pure classical radiation models would not lead to a realistic picture for this pulsar's time evolution. Adding QVF effects, solution of eq. (7) becomes, for $t \geq 0$

$$p^2(t) = \left(\frac{K_r}{K_{qv}} + P_0^2 \right) e^{2K_{qv}t} - \frac{K_r}{K_{qv}} \quad (15)$$

This expression allows us to calculate the first and the second derivative of P with respect to time, and to match $\dot{P}(0)$ with P_1 and $\ddot{P}(0)$ with P_2 , obtaining

$$K_{qv} = \frac{P_0 P_2 + P_1^2}{2P_0 P_1} \quad (16)$$

and

$$K_r = \frac{P_0 P_1^2 - P_2 P_0^2}{2P_1} \quad (17)$$

Finally, the time evolution of the spin period is given by

$$P(t) = \sqrt{\frac{2P_0 P_1}{A} (e^{At} - 1) + P_0^2} \quad (18)$$

with

$$A = \left(\frac{P_2}{P_1} + \frac{P_1}{P_0} \right) \quad (19)$$

Using eq. (18), we can calculate the braking index

$$\begin{aligned} n(t) &= 1 - \left(\frac{P_0 P_2}{P_1^2} - 1 \right) e^{-At} \\ &= 1 - (1 - n_0) e^{-At} \end{aligned} \quad (20)$$

The braking index time evolution for the Crab pulsar is presented in fig. (3). When QVF is taken into account, the braking index is a decreasing function with respect to time which is consistent with a global rotation slowdown. From eq. (20) we can predict the current value of the first derivative of n given by

$$\dot{n}(0) = A(1 - n_0) \quad (21)$$

As far as we know, there are only two pulsars in the ATNF catalogue [12] for which the calculated value of $\dot{n}(0)$ can be compared with our estimation given by eq. (21). These stars are the Crab pulsar and the B1509-58 pulsar. For the Crab pulsar we get $\dot{n}(0) \sim -1.8421 \cdot 10^{-11} \text{ s}^{-1}$ and $\dot{n}^c(0) \sim 1.5676 \cdot 10^{-13} \text{ s}^{-1}$, whereas for the B1509-58 pulsar we get $\dot{n}(0) \sim -1.3550 \cdot 10^{-11} \text{ s}^{-1}$, a value in perfect agreement with the calculated one $\dot{n}^c(0) \sim -1.2500 \cdot 10^{-11} \text{ s}^{-1}$. These results show that new measurements of $\dot{n}(0)$ are needed to improve statistics and thus provide a very important test to confirm our QVF predictions.

In this letter we have shown that QVF should play an important role in neutron star evolution. Taking into account this effect, we have shown that the surface magnetic field of magnetars becomes lower than the critical quantum field, so that magnetars could be simply understood as a natural evolution of standard pulsars. For pulsars for which the braking index is known, QVF provides a completely coherent spindown history, as illustrated with the Crab pulsar. For this pulsar we have also given the predicted value of the current first derivative of the braking index, suggesting a very important test to confirm QVF.

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