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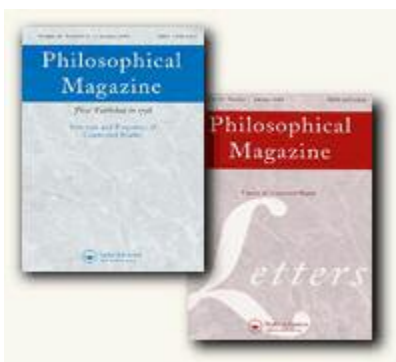
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Impurity diffusion of cerium and gadolinium in single- and polycrystalline yttria-stabilized zirconia

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Abstract

Yttria-stabilized zirconia (YSZ) ceramic is considered as an attractive material for solid oxide fuel cells or for nuclear applications such as inert matrix for the destruction of excess plutonium and host material for nuclear waste storage. Long term properties as phase stability depend on cation diffusion. Therefore, the present work is focused on the diffusion study of Ce and Gd in YSZ single crystals and high density polycrystals. A thin film of Ce or Gd was deposited either by spin-coating method or by physical vapour deposition on the surface of polished samples. The diffusion experiments were performed from 1173 to 1673 K under air. The Ce or Gd diffusion profiles were determined by secondary ion mass spectrometry. The analysis of the penetration profiles led to the determination of bulk diffusion (D_b) in single crystals and effective (D_{eff}), bulk and grain boundary diffusion coefficients (D_{gb}) were determined in polycrystals. The dependence of diffusion coefficients on temperature is described by means of Arrhenius equations and the diffusivity is compared with literature.

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1. Introduction

Yttria-stabilized zirconia (YSZ) is one of the most technologically important ceramic materials. It is widely used as electrolyte material in solid oxide fuel cells, oxygen sensors, oxygen separation membranes and thermal coating barriers. It is also considered as one of the most promising materials for use as inert matrix for the destruction of excess plutonium or good host material for nuclear waste storage [1]. These applications are based on refractory properties, high chemical durability, excellent radiation stability and the ability to form solid solutions in a wide range of solubilities with some actinide elements (Pu, U, Th) [2-4]. Furthermore, its

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3 stability in operating conditions mainly depends on the slow cation transport, which controls
4 processes such as creep, migration of dopants and impurities. Generally, some actinide
5 elements contained in high-level radioactive wastes can be simulated by rare earths : cerium as
6 tetravalent actinide and gadolinium as trivalent actinide. Up to now, some studies have been
7 performed to determine cation bulk diffusivities in cubic stabilized zirconia [5-10], and to a
8 much lesser extent to determine cation grain boundary diffusion coefficients [5-8]. The present
9 work is focused on a comparative study of both Ce and Gd diffusion in single crystalline YSZ
10 (9.5 mol% of yttria) and high density polycrystalline YSZ (8 and 10 mol% of yttria).
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2. Experimental

2.1. Material

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22 The YSZ polycrystals were prepared from high-purity powder 8 mol% (8YSZ) and 10 mol%
23 (10YSZ) yttria stabilized zirconia supplied by Tosoh Co. Ltd., Tokyo, Japan. These powders
24 were cold isostatically pressed at 250 MPa and sintered in air at 1723 K for 168 h with heating
25 and cooling rate of 5K/min [11]. From the sintered rods, round pellets were cut with nominal
26 dimensions of 10 mm diameter and 2 mm thickness. Pellets were then polished using diamond
27 pastes down to $\frac{1}{4}$ μm and further annealed in air for 10 h at 1673 K in order to eliminate
28 polishing stresses. The micrograph of a thermal-etched 8YSZ sample obtained by scanning
29 electron microscopy (SEM, figure 1) shows grains with an average diameter of 5 μm (2-10
30 μm). The density of the samples was measured by Archimedes method and full dense samples
31 with relative density of 99.5% of the theoretical one were obtained. Moreover, the homogeneity
32 and composition were checked by X-ray diffraction (XRD), Rutherford backscattering (RBS)
33 and electron microprobe. XRD patterns indicate that samples only exhibit the lines of the cubic
34 fluorite-type structure.
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46 Furthermore, 9.5 mol% yttria stabilized zirconia (9.5YSZ) pure single crystals $\langle 1\ 0\ 0 \rangle$ -oriented
47 supplied by Crystal GmbH, Berlin, Germany, were also investigated. Specimens with
48 dimensions of 5 mm x 5 mm x 1 mm were cut and used as-received.
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2.2. Diffusion experiments

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52 By the spin-coating method, a thin layer of CeO_2 and Gd_2O_3 was deposited on the YSZ
53 substrates. Ammonium cerium nitrate or gadolinium nitrate were used as starting materials.
54 Each salt was dissolved in distilled water. Then, few drops of nitric acid as well as citric acid
55 and ethylene glycol were added to the stirred clear solution. This mixture was heated using a
56 hot-plate in a ventilated fume hood to decompose nitrates and to get a viscous solution. After
57 cooling, the solution was dropped onto the polished surface of the YSZ samples. After drying, a
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3 thermal annealing at 573 K for 30 min followed by 10 min at 973 K was applied in order to
4 obtain an adherent coating. The thickness of the ceria or gadolinia film was estimated on a as-
5 deposited sample via a SIMS (secondary ion mass spectrometry) profile and a measurement of
6 the crater depth with a profilometer. The thickness is about of 70 nm, as shown in figure 2a.
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10 Additionally, physical vapour deposition technique (PVD) performed by THEVA GmbH was
11 used for producing CeO₂ regular thin films from metal cerium targets at 953 K. The thickness
12 of the so-obtained ceria film was also estimated on as-deposited sample to be about 80 nm, as
13 shown in figure 2b. The main difference is that the film deposited by the spin coating method
14 exhibits a somewhat irregular and a rough surface, which is not the case for the CeO₂ film
15 obtained by PVD. For the Ce profile obtained on as-deposited samples (Fig. 2a and b), a curve
16 tail can be distinguished. In fact, the samples have been subjected to a thermal annealing after
17 the deposition of Ce: at 973 K and at 953 K for a coating performed by spin coating or by PVD,
18 respectively. This heating is responsible for the slight penetration of the tracer before the
19 diffusion experiments.
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23 The Ce and Gd diffusion experiments were performed in air from 1173 to 1673 K. An attempt
24 of cerium diffusion was made at 873 K with the hope to determine bulk diffusion coefficients at
25 very low temperature (Fig.2c), but it was not satisfying and such temperature were discarded
26 further on. At the end of the annealing, the sample was quenched by pulling it out from the
27 furnace. The diffusion annealing time and temperature, reported in Table 1, were chosen so that
28 most of the experiments correspond to a B-type diffusion regime [12], which means that both
29 bulk and grain boundary diffusion coefficients can be determined. Nevertheless, some diffusion
30 tests were performed in C regime which leads only to determine diffusion coefficients in the
31 grain boundaries.
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2.3 Depth profiling by secondary ion mass spectrometry (SIMS)

The cerium and gadolinium depth profiles were established by secondary ion mass spectrometry (Cameca IMS4F-CNRS/Meudon/France), using either O₂⁺ or Cs⁺ primary ion source with energy of 10 keV. For cerium and gadolinium analysis, the evolution of ¹⁴⁰Ce and ¹⁴²Ce, ¹⁵⁸Gd and ¹⁶⁰Gd signals were recorded and ¹⁴⁰Ce and ¹⁵⁸Gd were retained since each of them corresponds to the most intense isotope. They excluded also any possible interference, for instance between Gd and Nd. For gadolinium, the GdO⁻ ion was analysed. The scanned area was 150 μm x 150 μm and the analyzed zone was limited by a diaphragm to 33 μm diameter. Such a size of the analyzed area compared to the grain size of polycrystalline samples will lead to average diffusion coefficients, as it is usual when working on polycrystalline materials. The availability of the results was verified by performing several analyses on different areas of the

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3 same sample. To avoid sample charging effects on sputtering, a normal electron flood gun was
4 used and a 30 nm thick gold layer was deposited on the samples. The limit of detection of the
5 apparatus is given as 1 count per second. After establishing the penetration profile, $I = f(t)$ by
6 SIMS analysis (Fig.3a), the crater depth was measured using a profilometer (KLA Tencor P1).
7 A typical crater profile is given in figure 3b. This measurement allowed to convert the
8 sputtering time into eroded depth, as shown in figure 3c.
9

10 11 12 13 14 *2.4. Determination of bulk and grain boundary diffusion coefficients*

15 In a first step, the cation (Ce or GdO) signals were normalised by zirconium signal which can
16 be considered as constant in the material (see Fig.2c), thus leading to the diffusing element
17 concentration. It appeared that there was no difference in the diffusion coefficients between the
18 analysis of the concentration and the direct analysis of the Ce or Gd intensity. As an example,
19 results obtained for the experiment made on 8YSZ at 1373 K were analysed with either the
20 concentration profile I_{Ce}/I_{Zr} or the cerium intensity I_{Ce} profile, as a function of the depth, and
21 will be compared with others in § 3.
22

23 Thus, further on, Ce and Gd profiles were directly considered. In the same way, the similarity
24 in the analysis of intensity or concentration for which the background has been subtracted
25 indicates that it is not necessary to subtract it. Once again, for the experiment made on 8YSZ at
26 1373 K (Figs.3), diffusion coefficients were also calculated from the concentration profile after
27 having subtracted the background, and they will be compared with other results, later on (§ 3).
28 Another mode to avoid problems due to the sputtering rate consists in verifying that the
29 primary current is constant. It was done during the analyses and maximum variations of 5%
30 were observed. It means that the concentration variations are negligible in regard to the
31 uncertainty of diffusion coefficients. Concerning the drift of the background (value of the
32 signal given by an element when it is absent from the matrix), as there is no matrix signal drift,
33 the background cannot present a drift and cannot be responsible for the appearance of a curve
34 tail. According to our experiments, this background is often varying between 5 and 10 counts
35 per second (see Figs.2c and 7a).
36

37 Another point which has to be discussed concerns the film roughness variations according to
38 the deposition method. Indeed, the curve tails could be affected by the roughness. But, though
39 the roughness of the films deposited by the spin coating method is higher than the roughness of
40 films obtained by PVD, it was observed that the diffusion coefficients obtained from
41 experiments with spin coating deposition are not different from those obtained from PVD.
42 Thus, the influence of the roughness can be neglected.
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For polycrystals, two distinct regions can be determined on the Ce or Gd diffusion profiles (Figs.4 and 5) at temperatures higher than 1173K (diffusion in B regime) : (i) near the surface, a fast decrease of the concentration is observed (region 1) and (ii) far from the surface, the concentration slowly decreases (region 2). The concentration near the surface should correspond to the contribution of either bulk diffusion or effective diffusion, while the concentration far from the surface, i.e. the curve tail, should correspond to the grain boundary diffusion [13].

From region 1 (Figs.4b and 5b), an effective diffusion coefficient D_{eff} , i.e. bulk diffusion with contribution of grain boundary diffusion, was determined using a solution of the Fick's second law for diffusion from a thin layer of the deposited tracer [13]:

$$\frac{C(x)}{C_0} = \exp\left(-\frac{x^2}{4D_{\text{eff}} t}\right) \quad (1)$$

The comparison of the bulk diffusion penetration and the deposited film thickness suggests that, in some cases, the thick film solution of Fick's equations should be used. It was done, for instance in the case of cerium diffusion in 10YSZ at 1473 K. The analysis with the thick film solution led to the same diffusion coefficients, so that the thin film solution was used further on.

From the tail of the profile (region 2), the Whipple / Le Claire model [14] was used to determine the parameter $\alpha D_{\text{gb}} \delta$ using the following equation:

$$\alpha D_{\text{gb}} \delta = 0.661 \left[-\frac{\partial(\ln C)}{\partial x^{6/5}} \right]^{-5/3} \left(\frac{4D_b}{t} \right)^{1/2} \quad (2)$$

where D_{gb} is the grain boundary diffusion coefficient, δ is the grain boundary width and α is a dimensionless segregation factor [13]. According to this model, a plot of $\ln C$ versus $x^{6/5}$ should yield a straight line for the experimental points corresponding to region 2 and the slope of this straight line (Figs.4c and 5c) allows the determination of : $\left[-\frac{\partial(\ln C)}{\partial x^{6/5}} \right]^{-5/3}$.

Hart's equation [15] was then used to relate the effective diffusion coefficient with the bulk diffusion coefficient (D_b) and with the grain boundary diffusion coefficient through the following relationship:

$$D_{\text{eff}} = f \alpha D_{\text{gb}} + (1-f)D_b \quad (3)$$

where f is the fraction of atomic sites located on the grain-boundaries. f may be calculated through the expression $f = 3\delta/\phi$ [13] where ϕ is the grain size of polycrystal and δ the grain

boundary width, conventionally taken as 1 nm [16]. In the present study, f is thus equal to 6×10^{-4} for all polycrystalline samples.

It can be noted that such equations (1-3) can be used to analyze curve tails obtained in single crystals in which aligned dislocations, i.e. sub-boundaries, are present [13].

In the case of C-type regime experiments [12], which concerns experiments performed at 1173K, bulk diffusion is not detected, because of the small tracer penetration. Then the first region is associated to grain boundary diffusion, as shown in figure 6. The parameter αD_{gb} is determined by the following equation:

$$\frac{C(x)}{C_s} = \operatorname{erfc}\left(\frac{x}{2\sqrt{\alpha D_{gb} t}}\right) \quad (4)$$

where C_s is the diffusing element concentration at the surface. A second region appears in the diffusion curves due to the transport of cerium or gadolinium in the residual porosities.

For single crystals, the diffusion profile should show only one region corresponding to a fast decrease of the intensity and related to the bulk diffusion. Thus, the bulk diffusivity can be obtained from eqn.1 (diffusion from thin layer) by replacing D_{eff} by D_b :

$$\frac{C(x)}{C_0} = \exp\left(-\frac{x^2}{4D_b t}\right) \quad (5)$$

3. Results

Figures 3 to 8 show various penetration profiles and analyses of these profiles. At first, it was checked that both tracer deposition methods (PVD and spin coating) lead to similar results. Thus, diffusion experiments at 1673 K were performed for two days with a Ce film deposited either by the spin coating method or by PVD on the samples. The experimental values deduced from samples with PVD coating of ceria are also given in Table 1. No significant difference between the deposition methods is observed. Moreover, for the experiment performed on 8YSZ at 1373 K, the results obtained when analysing the concentration profiles and when subtracting the background are given in italics in Table 1 with other results, relative to intensity profiles without subtracting the background. It can be seen that the differences with the diffusion coefficient values retained in this study are smaller than the uncertainty on diffusion coefficients.

As a general case, the penetration profiles in polycrystals show two regions corresponding to different diffusion mechanisms (Figs.3-6). According to a B regime (see Table 1), the first part

of the profile corresponds to effective diffusion and the second part of the profile, i.e. the curve tail, is characteristic of the diffusion along grain boundaries. More precisely, the slope of the straight line $\ln I = f(x^2)$ in the first part (Figs.4b and 5b) corresponds to the theoretical diffusion profile given by eqn.1 for effective diffusion. In the second part (Figs.4c and 5c), the slope of the straight line $\ln I = f(x^{6/5})$ corresponds to the gradient $-\partial \ln C / \partial x^{6/5}$ necessary to solve eqn.2. Similar profiles were obtained also for diffusion experiments established in C-type regime (see Table 1 and Figs.6a and 6c), though it was expected to obtain only one part in the diffusion profile. In this case, the first part of the profiles is related to grain boundary diffusion and the slope of the straight line obtained in figures 6b and 6d correspond to the theoretical diffusion profile given by eqn.4. The second part of these profiles is associated to the diffusion in the residual porosity in our sintered samples.

For single crystals, only one region associated to bulk diffusion was expected in the penetration profile. This was effectively obtained at high temperature (1673 K) as shown in figure 7a. According to eqn.1, the slope of the plot $\ln I = f(x^2)$ (Fig.7b) leads to the value of the bulk diffusion coefficient. However, at smaller diffusion temperatures (1473 and 1373 K), two regions are observed (Fig.8a). Plotting the logarithm of the intensity versus x^2 in the first part leads to a diffusion coefficient which should be reasonably associated to bulk diffusion. At both temperatures the second part of the profiles satisfies eqn.2 (Fig.8c). The mechanism which leads to this second part will be discussed further on.

From all these profiles, according to the procedure explained in §2.4, bulk, effective and grain boundary diffusion coefficients ($\alpha D_{gb} \delta$) were obtained. All the values are gathered in Table 1. The diffusion coefficients obtained for polycrystals are plotted as a function of the inverse temperature in figures 9a and 9b, and activation energy values deduced from the Arrhenius lines are given in Table 2.

4. Discussion

From figure 9, some differences appear either in the diffusion coefficients or in the activation energies. These differences are discussed according to the possible influence of various parameters successively.

4.1 Bulk diffusion and grain boundary diffusion in cubic stabilized zirconia

As expected, the grain boundary diffusion is higher of about 5 orders of magnitude than the bulk diffusion as in literature, for instance results of Oishi et al. [5-7] and Kowalski et al. [8].

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3 The activation energy of bulk diffusion is of the same order of magnitude than that suggested
4 by Kilo et al. [9] for a diffusion process via cationic vacancies. In most cases of literature data,
5 the activation energies for bulk diffusion are between 390 kJ/mol and 540 kJ/mol, which is
6 close to our values (Table 2). However, from figures 9-10 and Table 2, it appears that the
7 activation energy of grain boundary diffusion is included between 500 kJ/mol and 600 kJ/mol.
8 These values are at least equal or even higher than the activation energies of bulk diffusion.
9 According to Monty and Atkinson [17], the activation energy for grain boundary diffusion in
10 oxides should be roughly 2/3 of the activation energy of bulk diffusion. It is not the case for our
11 results and that is one reason at least for expressing αD_{gb} rather than D_{gb} . The α factor is a way
12 to express that the diffusing impurity concentration changes in the grain boundaries during the
13 impurity diffusion and it depends on the interaction between the diffusing impurity and the
14 grain boundaries, but also on other species segregating [18]. This affects the grain boundary
15 diffusion profiles by changing their slopes and leads to apparent grain boundary diffusion
16 coefficients. Thus, as suggested in other studies performed on oxides [19-20], the high
17 activation energy obtained in this study could be related to segregation or precipitation
18 phenomena along grain boundaries, but we do not have evidence of such a phenomenon.

31 4.2. Effect of yttria content in cubic stabilized zirconia

32 Figure 10 gathers all the results on 8YSZ and on 10YSZ polycrystals. In the temperature range
33 and the yttria amount studied here, the diffusion coefficients along grain boundaries do not
34 seem to be dependent on the yttria content. Nevertheless, the Arrhenius lines associated to Ce
35 or Gd diffusion in 10YSZ have a higher slope than the lines associated to diffusion in 8YSZ :
36 activation energies of 506 ± 12 kJ/mol (Ce diffusion) and 507 ± 8 kJ/mol (Gd diffusion) in
37 8YSZ are obtained whereas values of 599 ± 88 kJ/mol (Ce diffusion) and 582 ± 19 kJ/mol (Gd
38 diffusion) are determined in 10YSZ. Consequently, it can be expected that at lower
39 temperatures the grain boundary diffusion would be slower in 10YSZ than in 8YSZ, possibly
40 on account of yttria segregation along grain boundaries when its amount increases. The recent
41 analysis of M. Kilo [21] does not exclude this possibility and, as suggested above, the high
42 values of grain boundary diffusion activation energies could be justified by such a segregation
43 phenomenon.

44 Concerning bulk diffusion, differences are slightly higher, but are not clearly related to the
45 yttria content. Indeed, cerium diffusion is slightly higher in 10YSZ, while gadolinium diffusion
46 is slightly higher in 8YSZ (Fig.10). In other words, bulk diffusivity in 8YSZ is enclosed by
47 bulk diffusivity in 10YSZ. Kilo et al. [9], with an higher yttria content, observed a decrease of
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4 the cation self-diffusion, since cation diffusion probably occurs via the zirconium vacancy $V_{Zr}^{4'}$.
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6 So, the cationic vacancy amount decreases when the yttria content increases, leading to a
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8 slowing of cation diffusivity which should be detected. It is not so clear in our study, perhaps
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10 due to the fact that the yttria content range is small.

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12 Consequently, in the narrow yttria content range studied here, it can be considered that there is
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14 no significant effect of this content on the diffusivity.

15 16 4.3. Comparison of cerium and gadolinium diffusivities

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18 The Ce bulk diffusivity (Fig.10) is slightly higher than that of Gd in both 8YSZ and 10YSZ.
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20 Considering the ionic radius of cerium (Ce^{4+}) and gadolinium (Gd^{3+}), respectively 0.097 nm
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22 and 0.1053 nm [22], it seems that the higher diffusion of cerium in 8YSZ and 10YSZ is
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24 associated to its smaller ionic radius. Note that the ionic radii are given with the assumption
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26 that these elements are eightfold-coordinated, as it can be expected from the fluorite cubic
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28 structure. So, it can be concluded as also remarked by Kilo [21] that the bulk diffusion
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30 decreases when the ionic radius increases.

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32 No influence of the size effect is seen on the grain boundary diffusion. The cerium and
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34 gadolinium grain boundary diffusion coefficients are very close in polycrystals (Fig.10).
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36 Indeed, in the case of grain boundary diffusivity, the correlation between D_{gb} and the ionic
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38 radius of the diffusing species is not obvious. For instance, although Ca^{2+} ionic radius is very
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40 high, it diffuses faster than other diffusing species with a smaller ionic radius [9, 21].

41
42 For an application as transmutation matrix of actinides, it is interesting to note that Ce diffusion
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44 or Gd diffusion is nearly as slow as the host cation self-diffusion (Zr) in yttria-stabilized
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46 zirconia [9, 21]. In fact, cerium or gadolinium is used in the present work to simulate the
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48 actinides that will be incorporated in zirconia matrix and transmuted into nuclear reactor. So, it
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50 is preferable that these radioactive elements should diffuse slowly through the ceramic under
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52 the thermal neutron flux during irradiation experiments in which the temperature was
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54 calculated to be more than about 1773 K [23].

55 56 4.4. Diffusion in single crystals

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58 Coming to results concerning the diffusion of cerium in single crystals, it can be observed on
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60 figure 11, (Table 1), that bulk diffusion, deduced from the first part of the experimental curves
(if two parts in the curve), is higher than in polycrystals. It was verified that the single crystals
were not heterogeneous, without porosity and without secondary phase, which could be at the
origin of the diffusivity increase.

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3 In a first step, it was considered that two types of point defects could ensure the cation
4 diffusion, as suggested by Solmon in her study on anionic self-diffusion in YSZ single crystals
5 [24, 25]. But, such a phenomenon, if it exists, should also act in polycrystalline materials,
6 which is not the case, and, besides, it is unlikely that complex defects would lead to faster
7 diffusion.
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11 It can also be remarked that the bulk diffusivity determined in our study in 9.5 YSZ single
12 crystal are similar to the bulk diffusion coefficients obtained by Taylor [10] on a 11.1YSZ
13 single crystal (Fig.11) : the values of D_b obtained in single crystals are always higher than the
14 ones obtained in polycrystals. In the case of Taylor et al., it could be due to the difference in
15 yttria content. However, a higher yttria amount should lead to a decrease of the bulk diffusion
16 coefficients, as mentioned in § 4.2. Thus, the difference in yttria content between our single and
17 polycrystals cannot account for the difference in bulk diffusivity.
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21 It should be considered that the evolution of the cationic dopant concentration could influence
22 the bulk diffusion coefficient. Again, with such an assumption, the influence would also be
23 detected in the case of diffusion in polycrystals. Moreover, according to the small concentration
24 of cationic dopant, it can be considered that the dopant diffusing atoms (Ce or Gd) are always
25 surrounded by host atoms, which corresponds to the solution of Fick equations for thin films
26 [13].
27

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30 Another possibility is that the diffusion coefficient deduced from the first part of the profiles
31 for single crystals should be disturbed by diffusion in short-circuits. In this case, the two parts
32 of our curves, obtained only at the lowest temperatures (1373 and 1473 K), would be associated
33 to effective diffusion for the first part and diffusion in dislocations for the second part. If the
34 dislocations are aligned in sub-boundaries, the profiles obtained at 1473 and 1373 K can be
35 analysed as for the grain boundaries, using eqns. 1-3 (see § 2.4) [13]. Then, analysis of the first
36 part would lead to an effective diffusion coefficient, but, in order to solve equation 3, a fraction
37 of atoms diffusing along the sub-boundaries has to be chosen. Calculations performed to obtain
38 bulk diffusion coefficients in single crystals similar to those concerning diffusion of cerium in
39 8YSZ and 10YSZ polycrystals lead to a f value of the same order of magnitude than the f value
40 of polycrystals ($\sim 5 \times 10^{-4}$). Taking into account the relatively small dislocation density in such
41 materials, this fraction of diffusing atoms in sub-boundaries is too important, and the analysis
42 was not pushed further on. Nevertheless, it is likely that, in single crystals, the first part of the
43 penetration profiles does not correspond to bulk diffusion only but may be disturbed by
44 dislocations and/or by sub-boundary diffusion. Our results suggest that results of Taylor [10]
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3 correspond also to overestimated bulk diffusion coefficients, diffusion being disturbed by sub-
4 boundaries.
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7 Finally, it is important to note that, according to a recent work on anisotropic dielectric
8 properties in 8YSZ [26], it was found that oxygen ions easily diffuse along the $\langle 100 \rangle$ direction.
9 In oxides, anisotropy of cationic diffusion was already observed, for instance in Cr_2O_3 [27] and
10 in Fe_2O_3 [28, 29 and see also 13]. It was also observed in native oxides such as NiO [30]. Even
11 if our diffusion data could be partially increased by diffusion along sub-boundaries, a
12 crystallographic orientation effect could also explain the higher values of the bulk diffusion
13 coefficients, as the single crystals investigated in the present work and those used by Taylor et
14 al. [10] are oriented along $[100]$,
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16 4.5. Comparison with other literature data

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18 Comparison with literature data is made in figures 12 and 13. The activation energy of bulk
19 diffusion of all results is of the same order of magnitude and close to the value expected for a
20 diffusion process via cationic vacancies [9]. There is agreement with the effect of the ionic
21 radius of the diffusing species: in Taylor study as in our study, cerium diffuses slightly faster
22 than gadolinium, confirming that the size of the diffusing species plays a major role in the bulk
23 cation diffusion mechanism.
24

25
26 In a recent analysis of results on tracer diffusion in YSZ [21], it is suggested that, while the
27 cation bulk diffusion should be mainly ruled by ionic size effects, cation grain boundary
28 diffusion might be dominated by charge effects. This classification does not seem so clear from
29 figure 13 where grain boundary diffusion data are gathered. Indeed, the charge of Gd^{3+} ions and
30 of Ce^{4+} ions is different but their grain boundary diffusivity is very close. Ti^{4+} which has the
31 same charge than Zr^{4+} ion diffuses very fastly. The diffusivity of Ca^{2+} is still faster than the
32 diffusivity of other cations, although the ionic radius of Ca^{2+} is higher (0.112 nm) than those of
33 Gd^{3+} (0.1053 nm) and of Ce^{4+} (0.097 nm).
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35 5. Conclusion

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37 The diffusion study of Ce and Gd in 9.5YSZ single crystals and in 8YSZ and 10YSZ high
38 density polycrystals from 1173 to 1673 K in air, led to the following results:
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- 40 1. The grain boundary diffusion D_{gb} is higher (about 5 orders of magnitude) than the bulk
41 diffusion D_b .
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- 43 2. For the narrow yttria content range used in this study, there is no significant effect of
44 the composition on the diffusivities in polycrystals. The cation bulk diffusivity in YSZ
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3 seems to be correlated to the ionic radius of the diffusing species: the higher the ionic
4 radius, the slower the bulk diffusion.
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7 3. In YSZ single crystal, it is suggested that the penetration profile corresponds to an
8 effective diffusion coefficient D_{eff} , and not to a bulk one D_{b} , due to the presence of sub-
9 boundaries. Moreover, the higher bulk diffusion coefficient in single crystals (when
10 compared to polycrystals) can be related to anisotropy effects: it is possible that easy
11 diffusion occurs along [100] direction.
12
13 4. The activation energies for bulk diffusion are similar in both single crystals and
14 polycrystals. The comparison of the bulk diffusion activation energy with the literature
15 suggests that cation diffusion occurs via cation vacancy V_{Zr}^{4+} . The Ce or Gd diffusion is
16 as slow as the host cation self-diffusion (Zr) in yttria-stabilized zirconia.
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18 5. The activation energies have the same order of magnitude for both bulk diffusion and
19 grain boundary diffusion, even higher for grain boundary diffusion in some cases. This
20 result could be related to segregation phenomena along grain boundaries.
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Figure Captions

1- SEM micrograph of polished and thermal-etched surface of the 8YSZ ceramic after sintering at 1723 K for 168h.

2- Ce-profile obtained by SIMS on as-deposited YSZ sample using the spin coating method (a), PVD method (b). Figure 2c gives an example of background for the Ce profile after a diffusion attempt performed at 873 K on a single crystal.

3- Penetration profile of cerium in 8YSZ polycrystal after a diffusion treatment at 1373 K vs time(a); typical crater profile(b); vs the depth (c).

4-Analysis of the penetration profile obtained by SIMS for Ce diffusion at 1473 K in 10YSZ (a); Region 1 with a sharp slope corresponds to the effective diffusion including bulk and grain boundary diffusion(b). Region 2 with a weak slope is associated to grain boundary diffusion (c).

5- Analysis of the penetration profile obtained by SIMS for Gd diffusion at 1473K in 10YSZ (a); Region 1 with a sharp slope corresponds to the effective diffusion including bulk and grain boundary diffusion, and the slope of the straight line corresponds to the theoretical diffusion profile given by eqn.1 for effective diffusion (b). Region 2 with a weak slope is associated to grain boundary diffusion, and the slope of the straight line corresponds to the gradient $-\partial \ln C/\partial x^{6/5}$ necessary to solve eqn.2 (c).

6- Penetration profiles obtained in the case of C-type regime experiments: diffusion of Gd at 1173 K in 8YSZ polycrystal (a and b), diffusion of Ce at 1173 K in 8YSZ polycrystal (c and d). As-obtained profiles (a and c), and analysis of the profile according to eqn. 4 (b and d).

7- Penetration profile of Ce in 9.5YSZ single crystal after diffusion at 1673 K for 2 days (a), and analysis (b).

8- Penetration profile of Ce in 9.5YSZ single crystal after diffusion at 1373 K for 1 month (a), analysis according to eqn.1 (b) and analysis according to eqn.2 (c).

9- Arrhenius plot of bulk and grain boundary diffusivities of Ce and Gd in 8YSZ (a) and 10YSZ (b) polycrystals.

10- Comparison of diffusivities according to the yttria content in stabilized zirconia.

11- Comparison, in an Arrhenius plot, of our results (polycrystals and single crystal) with literature data on bulk diffusion of cations. (*) corresponds to single crystal samples.

12- Comparison, in an Arrhenius plot, of our results with literature data on grain boundary diffusion of cations

Table 1: Ce and Gd diffusion coefficients in cubic yttria-stabilized zirconia.

Samples	Diffusing species	Deposition technique	Temperature (K)	Time (days)	D_{eff} ($\text{cm}^2 \cdot \text{s}^{-1}$)	D_{b} ($\text{cm}^2 \cdot \text{s}^{-1}$)	αD_{gb} ($\text{cm}^2 \cdot \text{s}^{-1}$)
8YSZ Polycrystal	Ce^{4+}	Sp	1673	2	$8.3 \cdot 10^{-15}$	$4.9 \cdot 10^{-16}$	$1.3 \cdot 10^{-11}$
		PVD	1673		$1.6 \cdot 10^{-14}$	$3.3 \cdot 10^{-16}$	$2.6 \cdot 10^{-11}$
		Sp	1473	19	$6.6 \cdot 10^{-17}$	$2.9 \cdot 10^{-18}$	$1.1 \cdot 10^{-13}$
		Sp	1373	30	$4.4 \cdot 10^{-18}$	$1.5 \cdot 10^{-19}$	$7.2 \cdot 10^{-15}$
			1373*		$4.6 \cdot 10^{-18}$	$8.4 \cdot 10^{-20}$	$7.6 \cdot 10^{-15}$
			1373**		$4.5 \cdot 10^{-18}$	$1.8 \cdot 10^{-19}$	$7.3 \cdot 10^{-15}$
		Sp	1173	60			$2.4 \cdot 10^{-18}$
	Gd^{3+}	Sp	1673	2	$5.2 \cdot 10^{-15}$	$7.5 \cdot 10^{-17}$	$8.5 \cdot 10^{-12}$
		Sp	1573	8	$6.6 \cdot 10^{-16}$	$1.1 \cdot 10^{-17}$	$1.1 \cdot 10^{-12}$
		Sp	1473	19	$5.2 \cdot 10^{-17}$	$1.1 \cdot 10^{-18}$	$8.4 \cdot 10^{-14}$
Sp		1173	60			$1.7 \cdot 10^{-18}$	
10YSZ Polycrystal	Ce^{4+}	Sp	1673	2	$4.2 \cdot 10^{-15}$	$2.7 \cdot 10^{-16}$	$6.5 \cdot 10^{-12}$
		PVD	1673		$8.5 \cdot 10^{-15}$	$2.9 \cdot 10^{-16}$	$1.4 \cdot 10^{-11}$
		Sp	1473	19	$2.9 \cdot 10^{-16}$	$6.8 \cdot 10^{-18}$	$4.7 \cdot 10^{-13}$
		Sp	1373	30	$5.9 \cdot 10^{-18}$	$8.7 \cdot 10^{-19}$	$8.4 \cdot 10^{-15}$
		Sp	1173	60			$1.2 \cdot 10^{-19}$
	Gd^{3+}	Sp	1673	2	$3.7 \cdot 10^{-15}$	$1.1 \cdot 10^{-16}$	$5.9 \cdot 10^{-12}$
		Sp	1573	8	$4.3 \cdot 10^{-16}$	$4.0 \cdot 10^{-18}$	$7.0 \cdot 10^{-13}$
		Sp	1473	19	$6.4 \cdot 10^{-17}$	$7.7 \cdot 10^{-19}$	$1.1 \cdot 10^{-13}$
		Sp	1373	30	$2.0 \cdot 10^{-18}$	$8.7 \cdot 10^{-21}$	$3.3 \cdot 10^{-15}$
		Sp	1173	60			$1.2 \cdot 10^{-19}$
9.5YSZ Single crystal	Ce^{4+}	Sp	1673	2		$5.9 \cdot 10^{-15}$	
		PVD	1673			$4 \cdot 10^{-15}$	
		Sp	1473	19		$6.0 \cdot 10^{-17}$	
		Sp	1373	30		$8.8 \cdot 10^{-18}$	

Sp = spin coating deposition method. * Analysis of the concentration profile, ** analysis of the concentration profile after subtracting the background.

Table 2 : Activation energy (kJ/mol) for bulk and grain boundary diffusion of Ce and Gd in yttria-stabilized zirconia

Diffusing element	Zirconia samples	A.E. for D_b (kJ/mol)	A.E. for αD_{gb} (kJ/mol)
Ce	8YSZ	516 (± 7)	506 (± 12)
	10YSZ	366 (± 8)	599 (± 88)
	9.5YSZ (single crystal)	420 (± 39)	
Gd	8YSZ	433 (± 7)	507 (± 8)
	10YSZ	574 (± 23)	582 (± 19)

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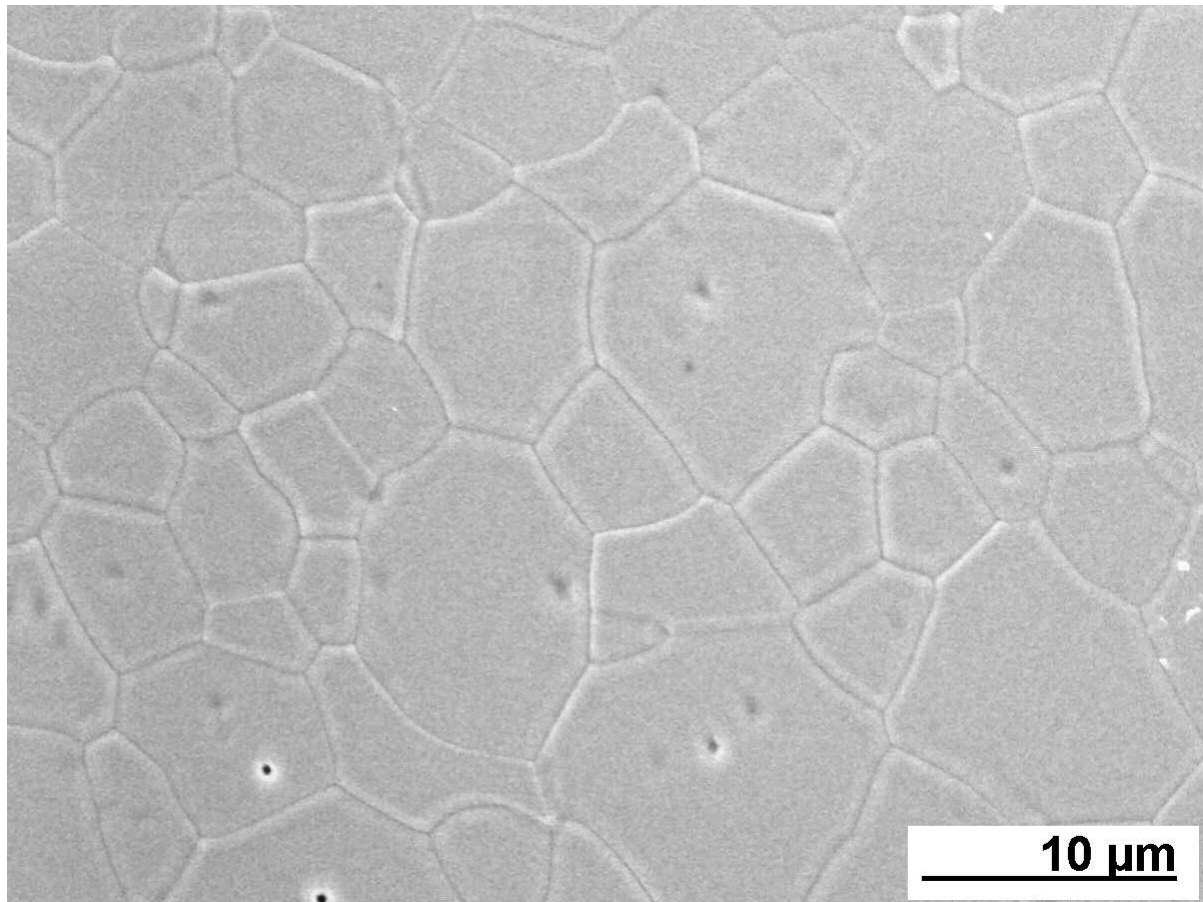


Figure 2

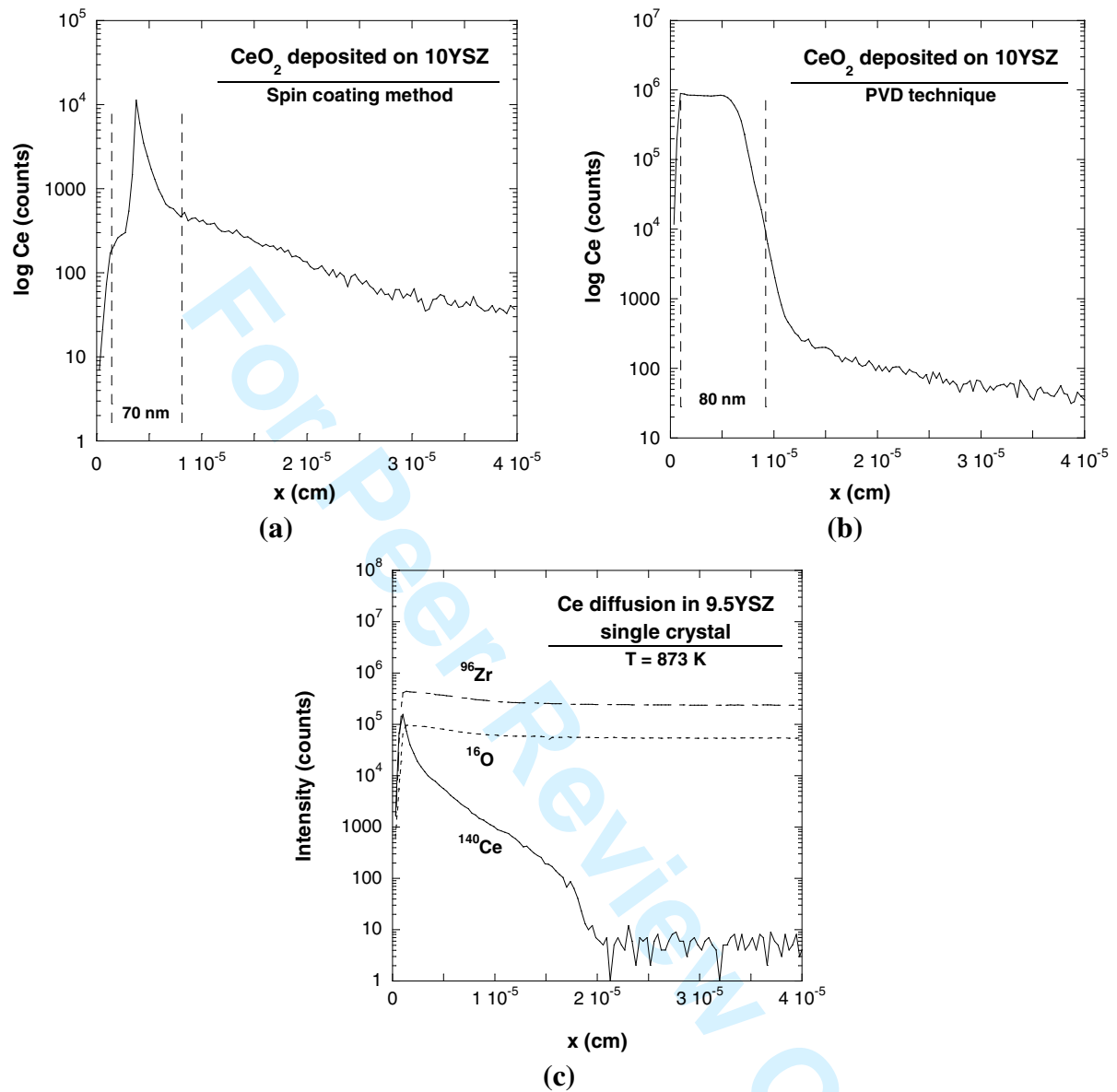


Figure 3

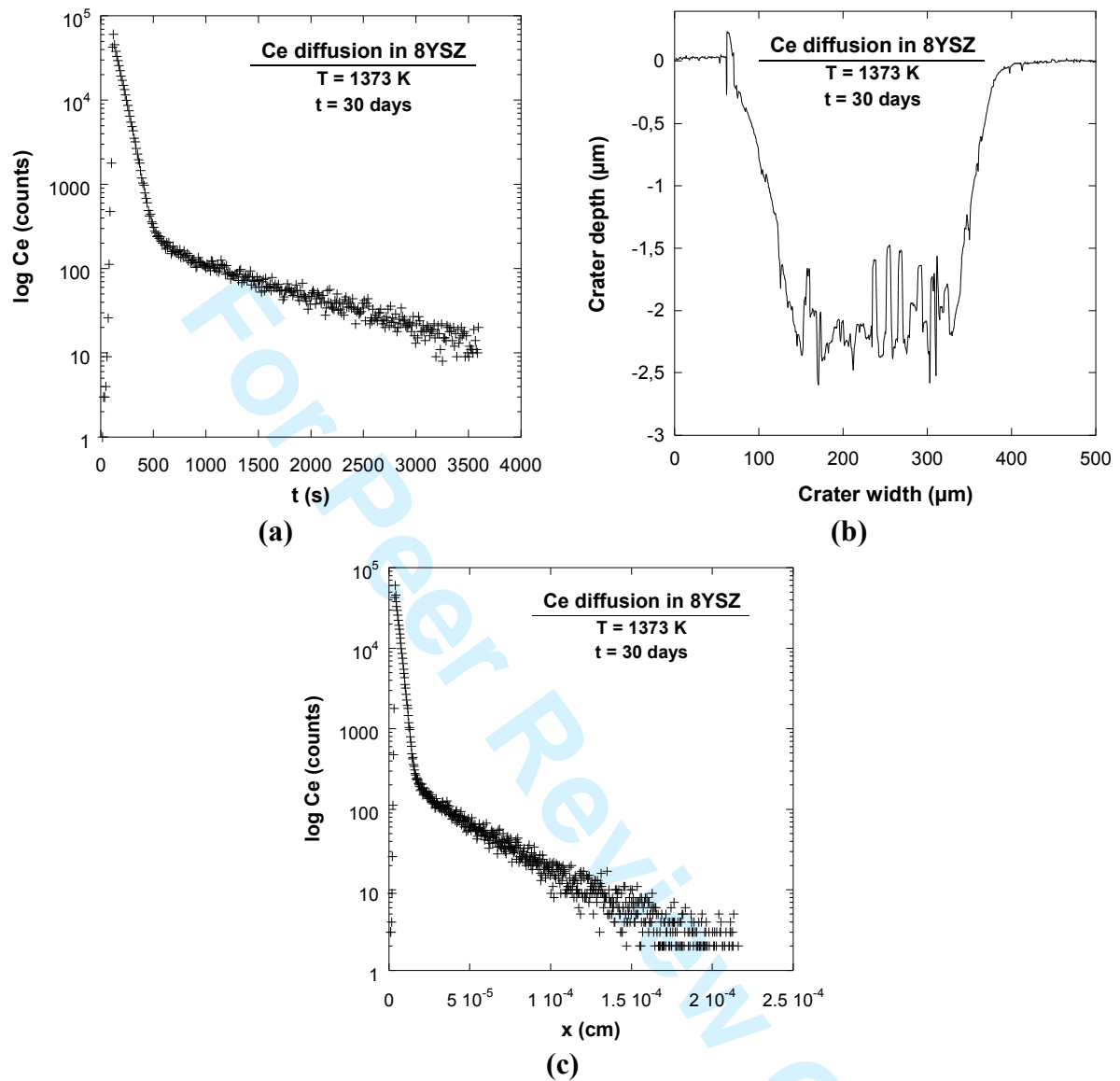


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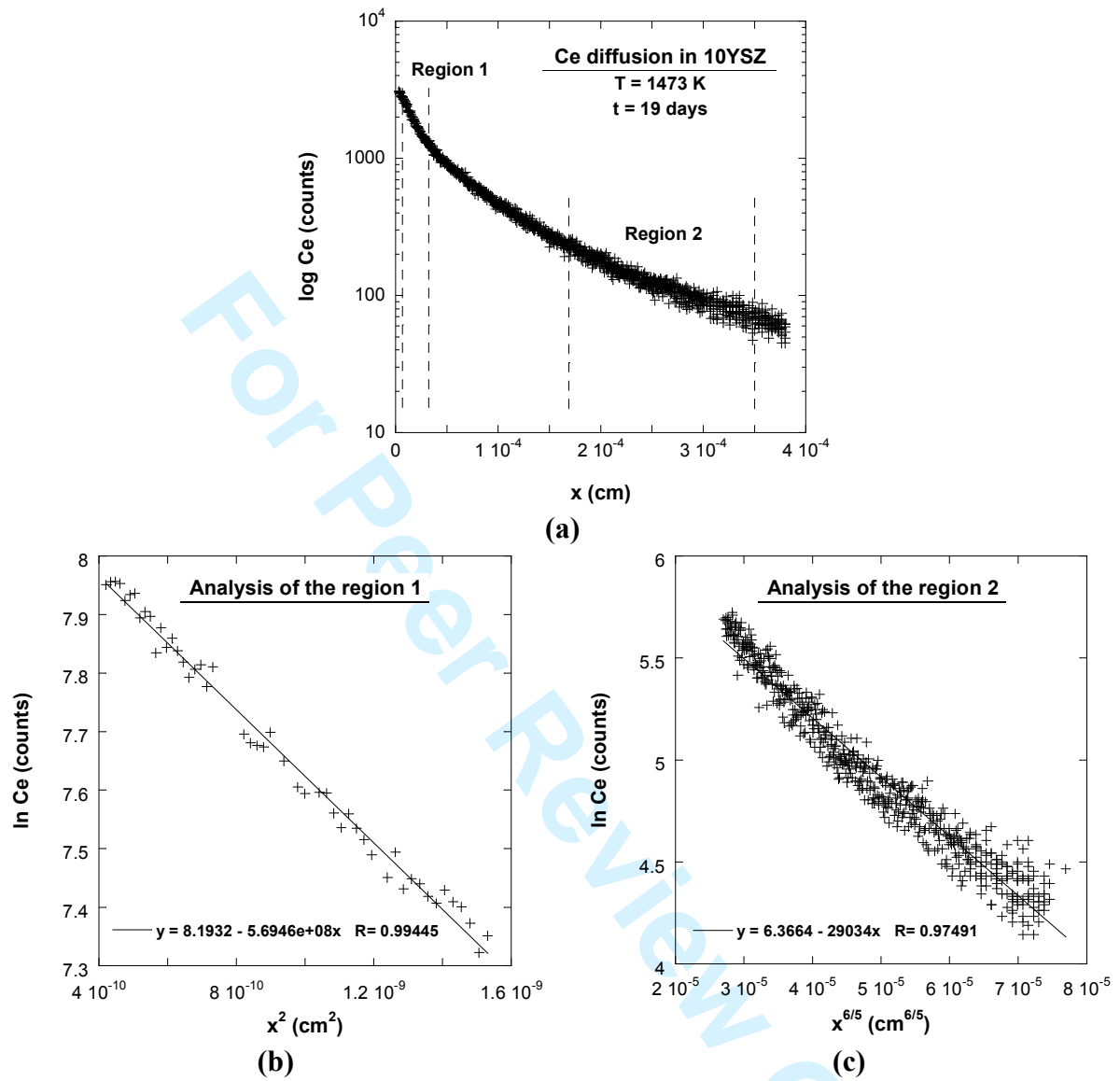


Figure 5

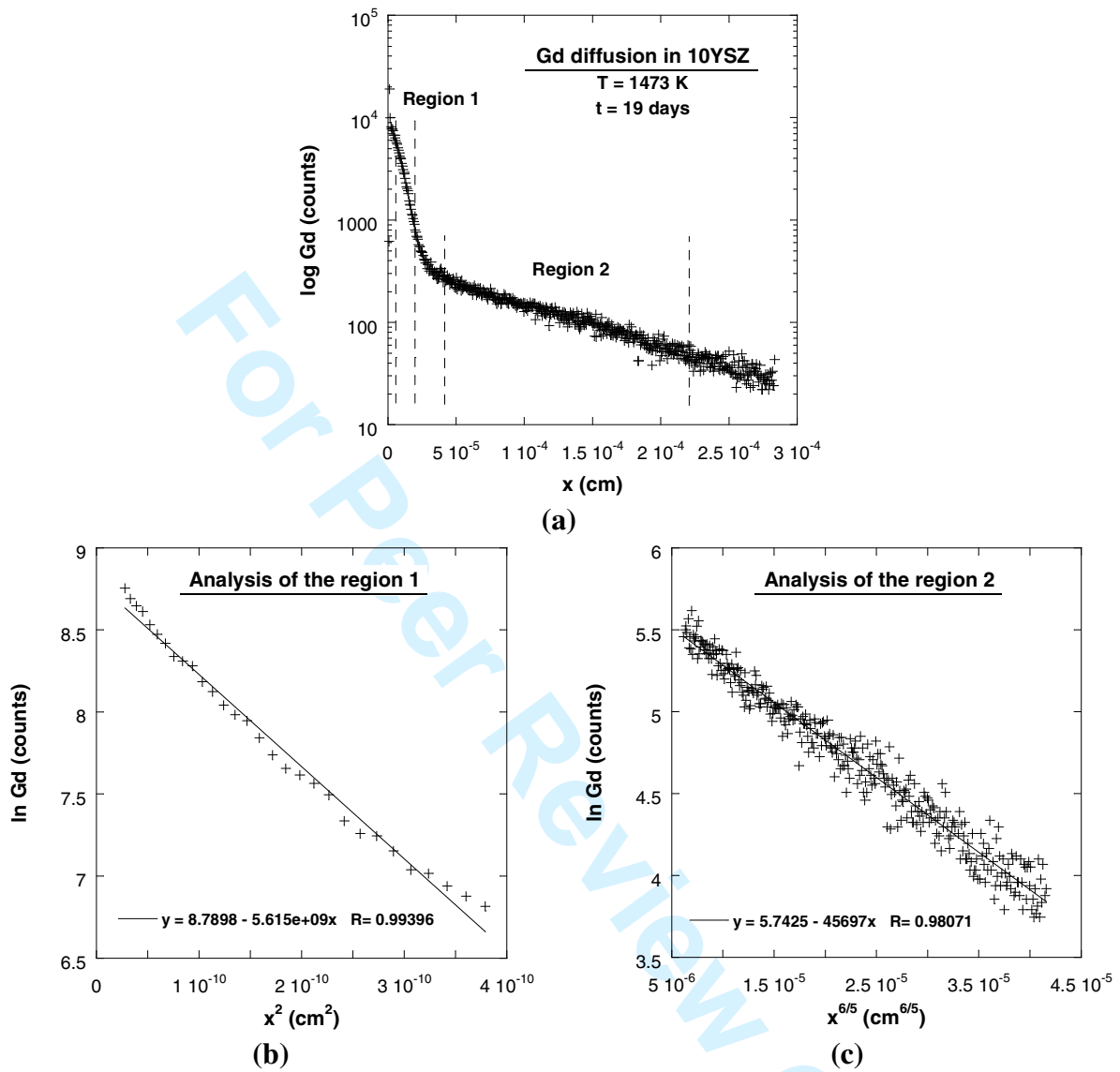
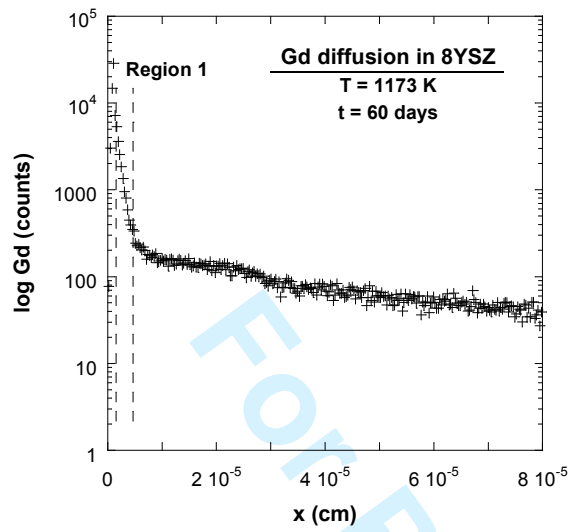
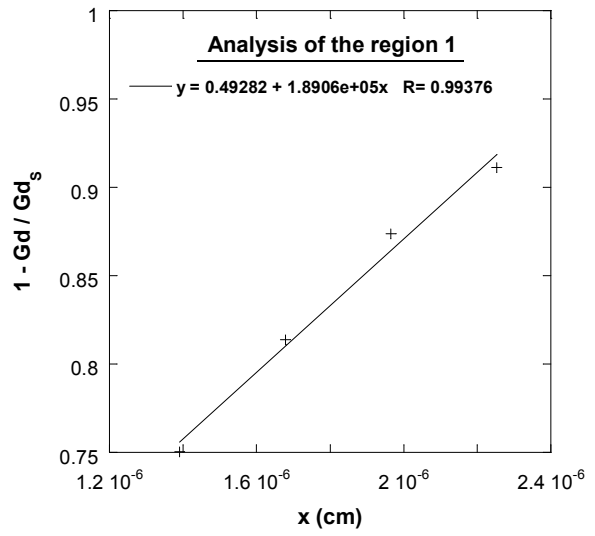


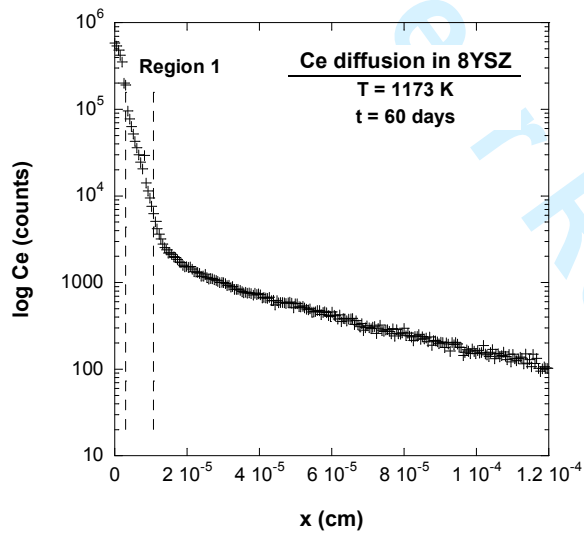
Figure 6



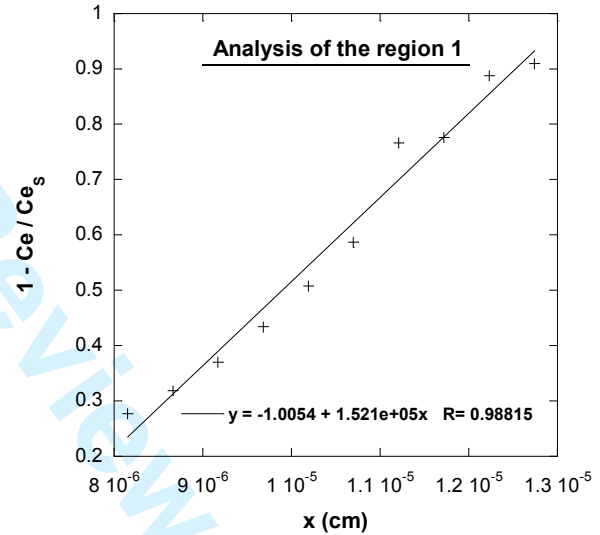
(a)



(b)



(c)



(d)

Figure 7

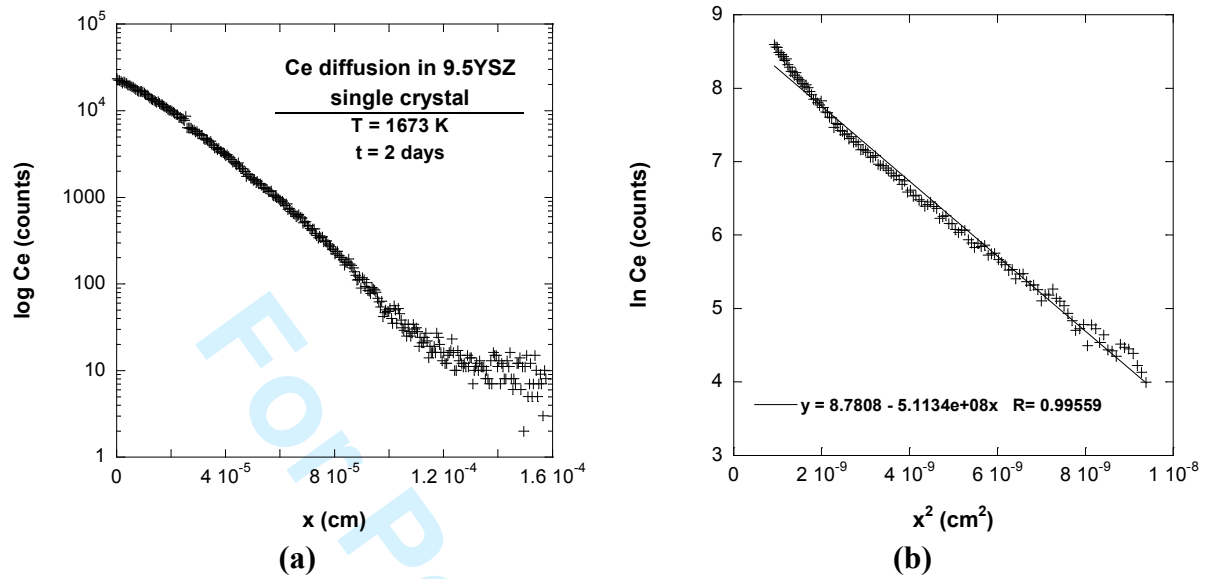
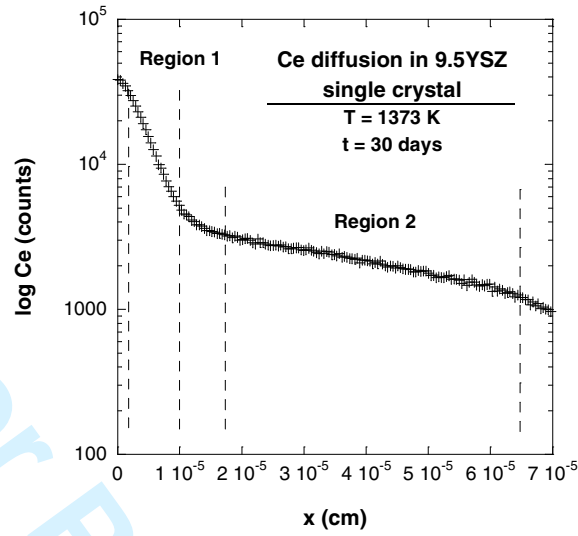
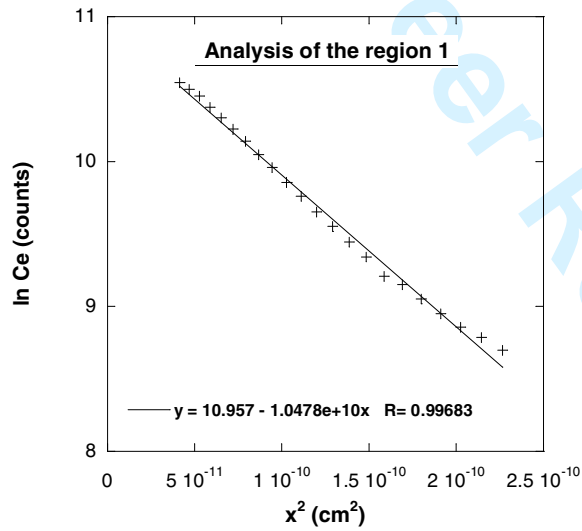


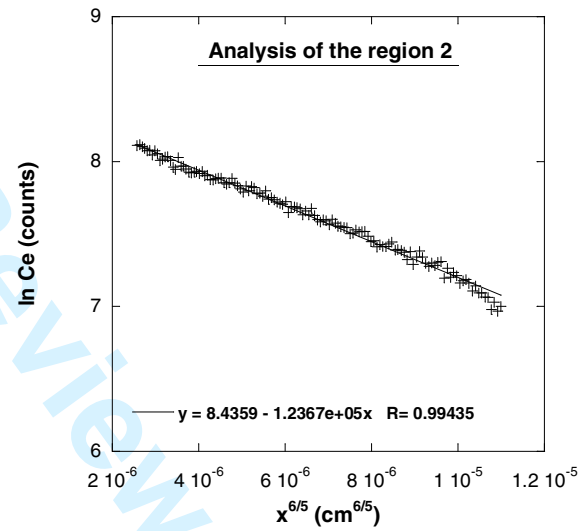
Figure 8



(a)



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Figure 9

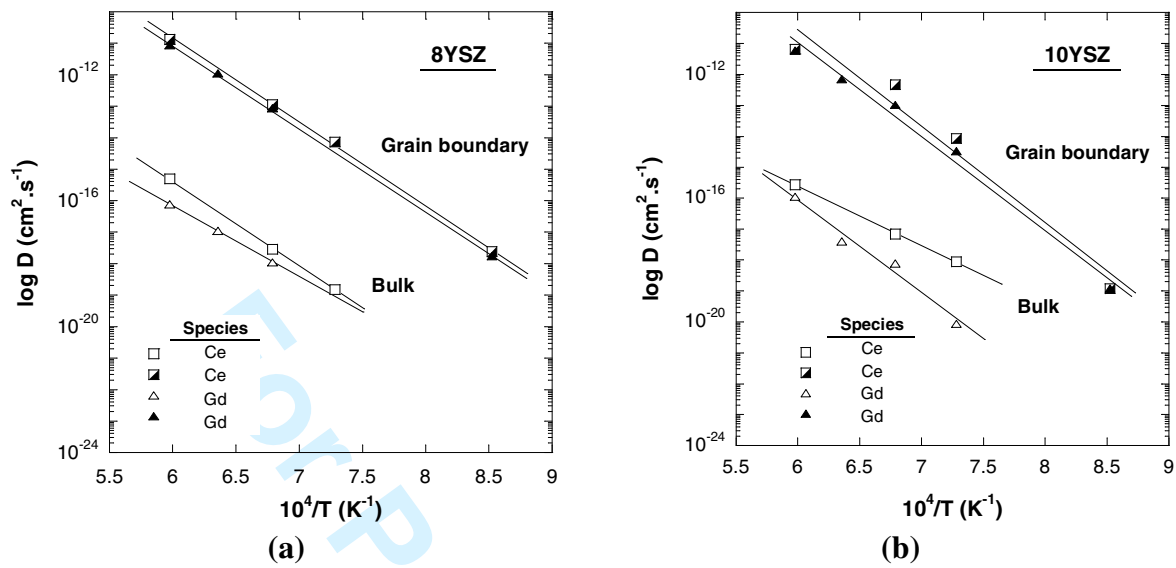


Figure 10

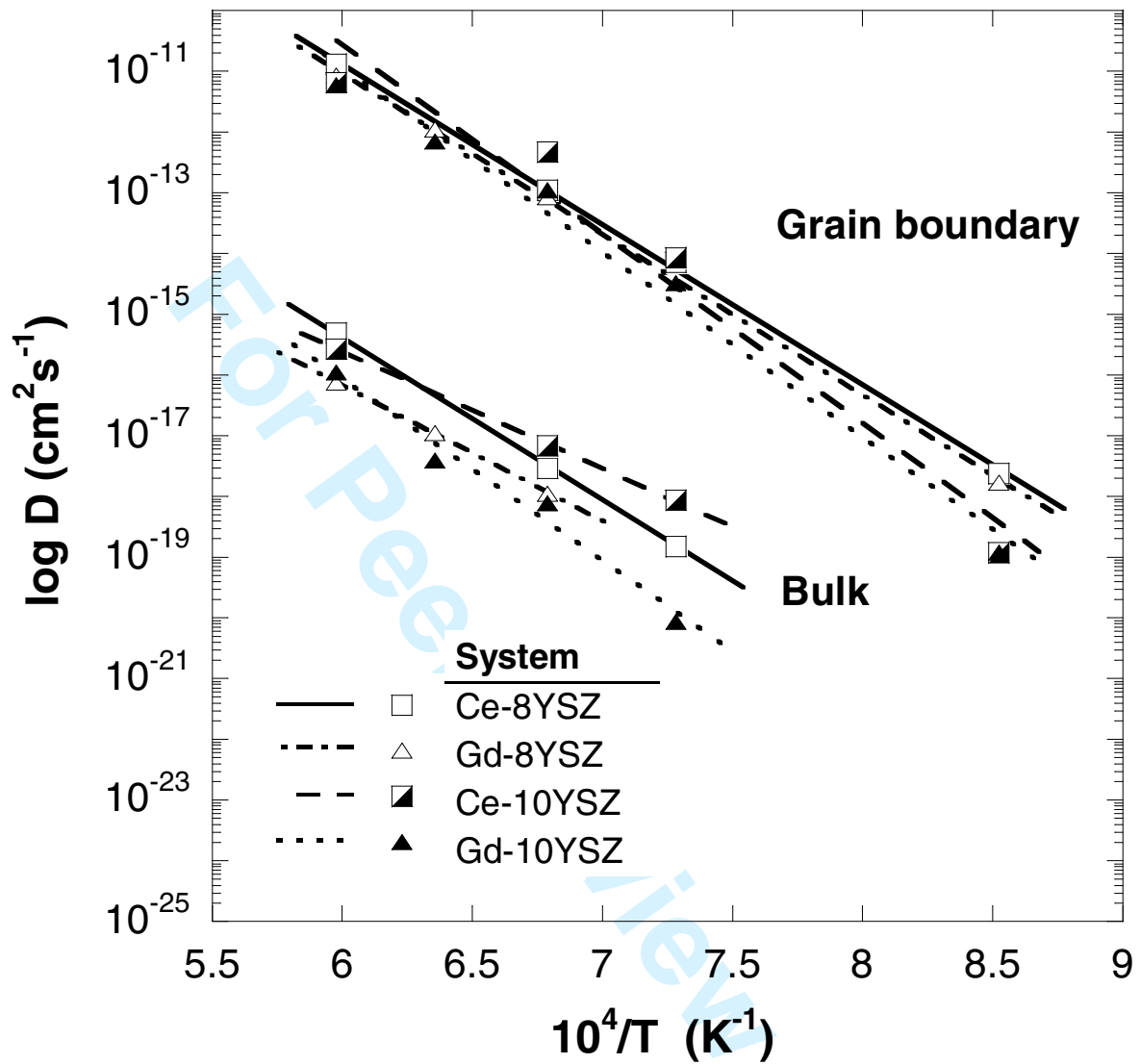


Figure 11

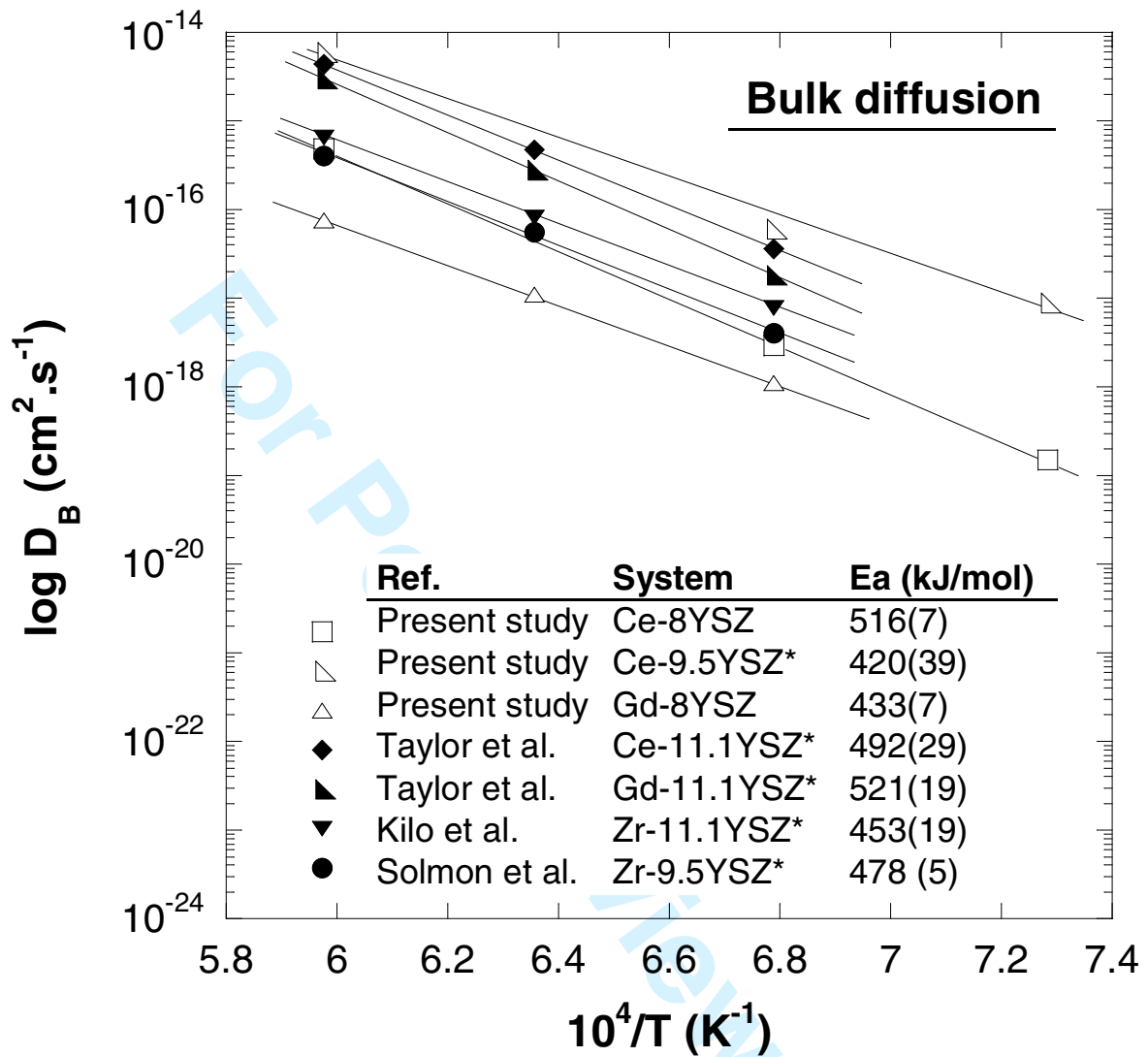


Figure 12

