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# Atomistic study of ordinary 1/2 $\langle$ 110] screw dislocations in single-phase and lamellar y-TiAl

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# Atomistic study of ordinary $\frac{1}{2}$ (110] screw dislocations in single-phase and lamellar $\gamma$ -TiAl

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#### Abstract

Computer simulation of the core structure and glide of ordinary  $\frac{1}{2}$  (110] screw dislocations in single-phase L1<sub>0</sub> TiAl and in two lamellae forming twin  $\gamma/\gamma$ -interface has been performed using recently constructed Bond-Order Potentials (BOPs). BOPs represent a semi - empirical, numerically efficient scheme that works within the orthogonal tight-binding approximation and is able to capture the directionality of bonding. We have studied dislocation glide in perfect  $L1_0$  TiAl and along a twin interface, transmission of an ordinary screw dislocation between lamellae, and the core structure, mobility and detachment of an interfacial  $\frac{1}{2}$  (110] screw dislocation from a twin boundary under applied shear stresses in directions parallel and perpendicular to a (111) plane. Our results show that the glide of ordinary  $\frac{1}{2}$  (110] straight screw dislocations under applied stresses in  $L1_0$  TiAl is characterized by zigzag movement on two conjugated {111} planes. The non-planar core of the  $\frac{1}{2}$  (110] screw dislocation is distorted asymmetrically when the elastic center of the dislocation is close to a twin  $\gamma/\gamma$ -interface and the dislocation moves on one of the (111) planes, depending on the magnitude of the corresponding Schmid factor. Ordinary dislocations become ordinary interfacial dislocations when they reach the interface. With increasing applied stress they can glide into the adjacent lamella, leaving no remnant interfacial dislocation.

### 1 Introduction

It is due to their low density, exceptionally high strength, hardness, creep resistance and corrosion resistance at high temperatures, that  $\gamma$ -TiAl-based alloys are considered for applications in aerospace and automotive industries. In spite of the promising high-temperature properties, the low ductility and

fracture toughness at room temperature have limited their commercial application so far. Gamma phase in its single-phase region is very brittle and therefore has not attracted much industrial interest. An improvement of ductility and fracture toughness at low temperatures can be achieved by special heat treatments leading to the formation of a refined two-phase lamellar structure, consisting of layers of  $\gamma$ -TiAl (tetragonal L1<sub>0</sub>) and  $\alpha_2$ -Ti<sub>3</sub>Al (hexagonal DO<sub>19</sub>) phases. The lamellar character, surprisingly, leads to higher room-temperature ductility which is practically zero for TiAl in the pure  $\gamma$ -phase structure [1, 2, 3]. The improvement of mechanical properties is evidently due to the presence of lamellar boundaries in the material. The reasons behind this phenomenon are not fully understood.

The ductility of a crystalline material is principally controlled by the interaction of dislocations with the applied stress and with other defects such as other dislocations, grain boundaries and precipitates. The main deformation modes in  $\gamma$ -TiAl are slip and twinning, both of which operate on the close-packed {111} planes [4]. Slip occurs via two types of dislocations: ordinary dislocations with Burgers vector  $\frac{1}{2}$  (110] and (101] superdislocations. The observed twinning is in the  $\eta_1 = \langle 112 \rangle$  direction with composition plane  $K_1 = (111)$ . In single crystals, superdislocations dominate at low temperatures and the glide of ordinary dislocations and twinning become dominant only at high temperatures [4, 5]. By contrast, in lamellar TiAl twinning is the prevailing mechanism at room temperature but high density and glide of  $\frac{1}{2}$  (110] ordinary dislocations in the  $\gamma$ -lamellae is also observed. The glide of (101] superdislocations becomes significant only at high temperatures [6].

To understand the role the interfaces play in enhancing the ductility, and the difference between deformation mechanisms in single-phase and twophase TiAl alloys, we have to gain deeper insight into the mechanisms of deformation and the transmission of dislocations across the lamellar boundaries at the atomic scale. The ductility is controlled predominantly by the properties of  $\gamma/\gamma$ -interfaces as they are much more frequent than those of the  $\gamma/\alpha_2$  type, and the  $\alpha_2$  phase is not very deformable. In the complex lamellar structure the interaction of dislocations with interfaces is very difficult to analyze by purely analytical or experimental means. There are three types of  $\gamma/\gamma$ -interface between the different orientation variants of  $\gamma$ -TiAl, formed by rotating about the [111] axis by angles of  $60^{\circ}$ ,  $120^{\circ}$  and  $180^{\circ}$  [6]. A similar orientation-based classification exists also for  $\alpha_2$  interfaces. The  $180^{\circ}$  interface is also referred to as the twin interface. Only in the case of the twin formed by a rotation of  $180^{\circ}$  about the normal to the interface do the  $\langle 110 \rangle$  directions across the interface remain parallel; hence this interface is fully coherent irrespective of the magnitude of lattice tetragonality. Twins comprise more than 60% of all  $\gamma/\gamma$ -interfaces [7]. The main reason is presumably the low energy of twin boundaries [8]. On the other twist boundaries, with rotations  $120^{\circ}$  and  $60^{\circ}$ , a network of interfacial dislocations forms at the lamellar boundaries to compensate the misfit caused by

the tetragonality of the  $L1_0$  structure. Such a network also compensates the misfit between  $\gamma$  and  $\alpha_2$  or forms as a result of the decomposition of impinging crystal dislocations [9]. It is possible that interfacial dislocations are mobile along the interface or can propagate inside the lamellae, and could thus increase the number of modes of plastic deformation.

The only plausible way of studying such phenomena is by means of computer simulation. A number of computer simulations of the structure and properties of dislocations in single-phase L1<sub>0</sub>-TiAl have been made by previous authors [10, 11, 12, 13]. In these studies, central-force potentials were used to describe the atomic interactions in the material. These do not capture effects arising from the covalent and directional bonding characteristic of TiAl. The core structure and friction barrier of the ordinary  $\frac{1}{2}$  (110] dislocation was also studied using an *ab initio* density-functional theory (DFT) based method [14]. This approach provides a good description of the interatomic forces, but is limited in the number of atoms that can be simulated.

The most important precursor of atomistic simulations of the core structure and glide of dislocations and dislocation-interface interaction that involve systems composed of a large number of atoms, is a reliable description of inter-atomic interactions. First-principles methods based on DFT provide such a description most reliably but are limited by feasible block sizes that contain not more than a couple of hundred atoms and usually require use of periodic boundary conditions that are not well suited for dislocation studies. Recently, a Bond Order Potential (BOP) for  $L1_0$  TiAl was constructed and tested by a variety of calculations involving large deviations from the ideal  $L1_0$  lattice [15, 16]. BOPs were first formulated by Pettifor and coworkers [17, 18, 19] and represent a numerically efficient scheme that expresses the orthogonal tight-binding approximation in terms of short-ranged noncentral interatomic potentials [20]. The multi-atom character of the forces is thereby captured in a physical way that goes beyond the embedded-atom model for example, and BOPs can describe features such as the negative Cauchy pressures  $(C_{13} - C_{44} < 0, C_{12} - C_{66} < 0)$  that simpler models cannot. In the framework of the BOP for TiAl the energy of a system of atoms is divided into three parts: bond energy  $E^{\text{bond}}$  arising from the formation of the valence band and including terms dependent on bond angles; repulsive energy  $E^{\text{pair}}$  described by pair interactions, including the Coulomb repulsion of the nuclei; and an environmentally dependent part of the energy  $E^{\text{env}}$ , including the overlap repulsion that arises from the valence s, p electrons, which may be squeezed according to the Pauli principle by overlapping orbitals from neighbouring atoms. The tight-binding parameters entering  $E^{\text{bond}}$  are fitted to *ab initio* DFT data generated with the Tight-Binding Linear Combination of Muffin Tin Orbitals method (TB-LMTO).  $E^{\text{env}}$  and  $E^{\text{pair}}$  are constructed by fitting the Cauchy pressures and several equilibrium properties, namely lattice parameters, other elastic moduli and the cohesive energy [15]. A further advantage of BOPs is that they allow the

evaluation of the energy in a computation time that scales linearly with the number of atoms, so that it is feasible to simulate the thousands of atoms needed to study the interaction between dislocations and interfaces. Variants of the BOP method were implemented in the Oxford order-N package (OXON) [21]. Computer simulation of the core structure of ordinary  $\frac{1}{2}$  (110] screw dislocations and (101] superdislocations has been performed using the recently constructed BOP [16, 22]. The non-planar core of the ordinary  $\frac{1}{2}$  (110] screw dislocation, simulated by using BOP, is in excellent agreement with *ab initio* calculations.

In this paper we present results of atomistic simulations of the core structure and mobility of the ordinary screw  $\frac{1}{2}$  (110) dislocation in single-phase L1<sub>0</sub> TiAl and in two  $\gamma$  lamellae forming a twin  $\gamma/\gamma$ -interface. In our simulations we have used the BOP for TiAl developed in [15]. We study the glide of the  $\frac{1}{2}$  [110] screw dislocation in L10 TiAl and along a twin interface, in a direction parallel to the interface. We then follow the process of transmission of an ordinary screw dislocation between  $\gamma$  lamellae. Finally we study the core structure, mobility and detachment of an interfacial  $\frac{1}{2}$  [110] screw dislocation from a twin boundary, induced by applied shear stresses in directions parallel and perpendicular to a (111) plane. The aim of such simulations is to gain deeper insight into the  $\frac{1}{2}$  (110] dislocation glide in single-phase L1<sub>0</sub> TiAl and along a twin  $\gamma/\gamma$  lamellar boundary, the mechanisms of transmission of ordinary dislocation across the lamellar boundaries and to elucidate the reasons for the higher density and different behavior of  $\frac{1}{2}$  (110] dislocations in the  $\gamma$ -lamellae compared to non-lamellar L1<sub>0</sub> TiAl. Based on the results of these calculations we suggest reasons for the peculiar dislocation behaviour exhibited by the lamellar  $\gamma$ -phase material.

### 2 Modelling the $\frac{1}{2}\langle 110 ]$ screw dislocation in L1<sub>0</sub> TiAl

In our dislocation calculations the L1<sub>0</sub> TiAl crystal was constructed of two  $(1\bar{1}0)$  planes forming one period in the  $[1\bar{1}0]$  direction, along which periodic boundary conditions were applied. We set the x, y, and z axis of the simulation cell parallel to the  $[\bar{1}\bar{1}2]$ , [111], and  $[1\bar{1}0]$  directions, respectively. The simulation block is divided into two sub-blocks. The positions of atoms in the inner sub-block, which includes the dislocation line, are adjusted so as to attain minimum of the energy (the so-called 'active atoms'). The atoms in the outer sub-block are kept fixed in the positions of the corresponding perfect lattice ('inert atoms').

The  $\frac{1}{2}$  [110] left handed screw dislocation was introduced by displacing the atoms in both regions from their perfect lattice positions according to the corresponding anisotropic elastic displacement field [23]. A molecular statics method of minimizing the energy of the system was employed. During

the relaxation the inert atoms retain their initial displacement while the active atoms are shifted until a minimum energy configuration is found. The relaxation was terminated when the force on every atom was smaller than  $5 \cdot 10^{-2} \,\mathrm{eV/\AA}$ .

In order to estimate the lattice friction stress we started with a simulation block containing the fully relaxed core structure of a  $\frac{1}{2}$  [1 $\overline{1}$ 0] ordinary screw dislocation. To this we have applied an incrementally increasing pure shear stress in the [1 $\overline{1}$ 0] direction on the (111) plane. In practice this stress is imposed by applying the appropriate homogeneous shear strain, which is evaluated with anisotropic elasticity theory. This strain was superimposed on the dislocation displacement field for all the atoms. Relaxation was carried out at every incremental step in the applied stress, until the dislocation started to move.

The motion of the dislocation is illustrated (Figure 1) by a series of differential displacement plots [24]. The light and dark circles represent the positions of Al and Ti atoms, respectively. At zero applied stress a non-planar core structure of the  $\frac{1}{2}$  (110] screw dislocation was found, which was distributed symmetrically on two {111} planes (Fig. 1a). The same core structure has been reported previously in [14] and [16]. As the shear stress is applied, the dislocation begins to distort with the displacements extending asymmetrically along the {111} planes. The stress at which the dislocation starts to move is the critical resolved shear stress (CRSS) on the slip plane (the Peierls stress). The magnitude of the CRSS on the (111) plane we predict for TiAl is  $0.015C_{44}$  ( $C_{44} = 0.680$  Mbar). This value is in agreement with the lattice frictional stress predicted by a DFT method (greater than  $0.01C_{44}$ ) [14].

As the dislocation goes over the Peierls barrier (Fig. 1b), its core structure continues to be non-planar but rather distorted in comparison to the unstressed core. With the increase of the applied stress above the frictional barrier the displacements extend along the cross-slip plane. The concentration of strain on the (111) plane leads to cross-slip of the dislocation along the conjugated (11 $\bar{1}$ ) (Fig. 1c). After moving one lattice spacing on (11 $\bar{1}$ ) the dislocation cross-slips again and starts gliding on the (111) plane (Fig. 1d). Similar motion of the ordinary screw dislocation, starting with glide on (11 $\bar{1}$ ), was found when the glide stress was applied on the (11 $\bar{1}$ ) plane.

The differential displacement plots illustrating a dislocation moving by one lattice spacing along the primary (111) plane are very similar to the previous DFT calculations of the same system, using a flexible boundary condition method [14]. An interesting characteristic of the glide of the  $\frac{1}{2}$  (110] screw dislocation in an ideal L1<sub>0</sub> TiAl crystal, predicted by BOP for TiAl, is the crossslip of the ordinary dislocation on the conjugated (111) plane after moving by one lattice spacing along the primary (111) plane. The

cross-slip of the ordinary dislocation after the first step along the primary plane can not be confirmed by the previous *ab initio* calculations, because the DFT simulations do not report results for the dislocation behaviour in response to increase of the applied stress above the CRSS.

The discrepancy between the critical resolved shear stresses predicted by BOP and DFT methods as well as the zigzag motion of the dislocation may be due to the size of the cell used in the simulations. Although artifacts arising from the use of fixed boundary conditions cannot be excluded entirely, we used five different simulation cells to model the motion of the dislocation in order to determine the sensitivity of the critical resolved shear stress and the dislocation motion to the size of the simulation cell. The calculations described here, are performed with supercells of 210, 288, 1680, 2208 and 2520 active atoms. The results obtained from all five simulation cell sizes are qualitatively similar; the Peierls stresses agree to within a margin of error of  $0.001C_{44}$ . In particular, there is no observed decrease in the Peierls stress associated with an increase in cell size.

# 3 The $\frac{1}{2}$ (110] ordinary screw dislocation in lamellar L1<sub>0</sub> TiAl

## 3.1 Core structures and friction stress along a $\gamma$ -phase twin boundary

A rectangular parallelepiped simulation cell was used in all simulations of dislocation-twin boundary interactions. To simulate the interaction of  $\frac{1}{2}$  [110] screw dislocations with  $\gamma$ -phase twin boundaries, the size of the simulation cell was 26 atomic layers along the [111] direction, 55 nm along the [112] direction and one periodic unit along the [110] direction. To introduce the twin boundary, the upper half of the block was rotated with respect to the lower by  $180^{\circ}$  about the [111] direction. As before, the simulation cell was divided into an inner region of active atoms and an outer, fixed region, with periodic boundary conditions parallel to the dislocation line. The simulation block consists of 336 active and 456 inert atoms. Initially, the cell was relaxed to allow for atomic rearrangement at or near the interface. A dislocation was introduced into the simulation cell after the initial relaxation by displacing all atoms according to the anisotropic elastic displacement field of a dislocation on a planar interface [26]. We illustrate in Fig. 2a and Fig. 2b the dislocation core structures found for two  $\frac{1}{2}[1\overline{1}0]$ screw dislocations with their initial elastic centers introduced at different distances from the twin boundary. The cores are non-planar, distorted near

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58 59 60 the interface, and the extensions into the (111) plane are asymmetrical. The concentration of strain on the twin boundary increases as the elastic centers of the dislocations approach the boundary. With no applied strain, the core is neither attracted nor repelled from the boundary. This result is not surprising, because twin boundaries do not introduce coherency stresses or any elastic constant mismatch, which otherwise could induce forces on a lattice dislocation in the lamellae.

A series of calculations at various applied strains was used to determine the frictional barrier and motion of the dislocation, starting with its elastic center in the upper lamella one atomic layer away from the boundary (Fig. 2b). The sense of the shear strain is such that the force on the dislocation pushes it in [ $\overline{112}$ ] (with respect to the lower crystal) direction, parallel to the interface. The motion of the dislocation is illustrated (Figure 3) in a series of differential displacement plots. In contrast to its motion in the perfect crystal, the dislocation core structure along a twin interface is only very slightly distorted as the dislocation goes over the Peierls barrier (Fig.3b) and it continues gliding parallel to the boundary as the applied stress is raised. When the dislocation moves it has to stay in the (111) plane as there is no continuation of the (111) plane across the interface. If the glide force applied to the dislocation is reversed it still moves on the (111) plane, but due to the asymmetric core structure the frictional stress in the [ $11\overline{2}$ ] direction is lower (0.024C<sub>44</sub>) than in the [ $\overline{112}$ ] direction.

### 3.2 The barrier strength of a $\gamma$ -phase twin boundary

To simulate the mechanism of transmission of a  $\frac{1}{2}\langle 110 \rangle$  screw dislocation through a twin boundary and to determine the blocking strength of the boundary to this dislocation, we again applied an increasing shear strain to the initially relaxed configuration described in Section 3.1. As before, the dislocation was initially located one atomic layer from the boundary (Fig. 2b). This time the sense of the applied shear strain was such that the force on the dislocation pushes it towards the boundary. The stress at which a dislocation overcomes the obstacle presented by the interface is its "barrier strength". Since the (111) slip planes in the two lamellae are not continuous across the boundary, the dislocation has to cross-slip for transmission of slip across the boundary. As a result, the blocking strength of the twin boundary is expected to be substantially larger than the friction stress in an ideal crystal, and competing processes such as indirect transmission of slip across the boundary become more probable.

At an applied stress of  $0.015C_{44}$ , the screw dislocation moves close to the lamellar boundary and is blocked (Fig. 4a). The core structure is distorted significantly and spread asymmetrically within the boundary and in (11 $\overline{1}$ ) planes on either side. The concentration of strain on the (11 $\overline{1}$ ) plane in the second crystal is displaced along the boundary from the intersection between the boundary and the (111) plane on which the strain in the first lamella is concentrated. The concentration of strain on the (111) plane in the second lamella increases with increasing applied stress (Fig. 4b). At an applied stress of  $0.0417C_{44}$  (Fig. 4c), the dislocation overcomes the obstacle and moves into the second lamella. Since the transmission of the dislocation takes place at a stress much higher than the friction barrier in the perfect crystal, our molecular static approach, whereby the energy of the system is minimized, does not allow us to trace the propagation of the dislocation immediately after its detachment from the interface. However, an analysis of the position of the dislocation after it has passed through the boundary shows that its path in the second lamella follows the same type of zigzag motion on (111) and  $(11\overline{1})$  planes that was observed in the ideal crystal. The (111) plane in the second lamella with the highest strain concentration is the initial glide plane for the dislocation after crossing the boundary. This plane is displaced along the interface from the intersection with the interface of the  $(11\overline{1})$  active slip system in the first crystal. Due to the high magnitude of the applied stress the distortion of the core structure observed in the second lamella is even bigger than that observed in the perfect crystal.

### $\frac{1}{2}$ (110] Interfacial dislocations

### 4.1 Core structure

Interfacial dislocations may arise to compensate misfit between orientation variants with 120° and 60° rotations, to compensate small grown-in deviations from the exact crystallographic misorientation, or as a result of decomposition of impinging crystal dislocations. The structures of the twin boundaries on (111) are preserved by displacements equal to the Burgers vector of the ordinary dislocation [25]. Therefore, the Burgers vectors of the ordinary dislocations, at the twin boundary. In particular, the Burgers vector of a  $\frac{1}{2}$  (110] screw twin  $\gamma/\gamma$ -interfacial dislocation is parallel to the boundary. It can be anticipated that this type of interfacial dislocation dislocation is mobile along the interface, and could thus increase the ease of plastic deformation, consequently increasing the desired toughness of the material. Due to the orientation of the  $\frac{1}{2}$  (110] interfacial dislocations with respect to the crystal interior they do not need to be attached to the interface but can propagate inside the lamellae when an appropriate glide stress is applied.

To determine the core structures and mobility of a  $\frac{1}{2}$  (110] screw interfacial dislocation, it was introduced into a simulation cell containing a 180° twin boundary in the way described previously. The relaxed structure of the  $\frac{1}{2}$  [110] screw interfacial dislocation at a twin interface is shown in Fig. 5a using the method of differential displacements. As before, the non-planar core structure spread asymmetrically into the boundary and (111) planes in both

lamellae. The concentration of strain on the (111) plane in the upper crystal is displaced along the interface from the intersection with the interface of the  $(11\overline{1})$  plane on which the strain in the lower crystal is concentrated. No dissociation of the interfacial  $\frac{1}{2}$  (110] screw dislocation into Shockley partials separated by the complex stacking fault (CSF) was observed. The reason is presumably the high energy of the CSF  $(550 \,\mathrm{mJ/m^2})$  at the twin boundary, which is even higher than the energy of the CSF  $(412 \text{ mJ/m}^2)$  calculated in bulk  $L1_0$  TiAl [8, 16]. The motion of the dislocation on applying a pure shear stress in the [110] direction on the (111) plane is illustrated (Fig. 5) in a series of differential displacement plots. The sense of the applied shear strain was to produce a glide force in the  $[11\overline{2}]$  direction. The interfacial dislocation starts to move on the interface in this direction at an applied stress of  $0.028C_{44}$  (Fig. 5b). As the dislocation moves through one lattice spacing along  $[11\overline{2}]$  its core structure is not distorted compared to the configuration it had without stress, and it continues gliding on the boundary as the applied stress is increased above the friction barrier. Unlike the case of the  $\frac{1}{2}$  (110] screw dislocation moving in the [112] direction we found considerable distortion of the core structure on reversing the sense of the glide force. On increasing the applied stress the interfacial dislocation tends to detach from the boundary. No glide of the ordinary interfacial screw dislocation along the interface in the  $[\bar{1}\bar{1}2]$  direction was predicted by BOP for TiAl.

### 4.2 Transformation to a lattice dislocation

To simulate the detachment of the interfacial  $\frac{1}{2}$  (110] screw dislocation from the twin boundary, its transformation to a lattice dislocation and propagation inside the crystal interior, we applied a stepwise increasing shear strain to the initially relaxed interfacial dislocation core structure (Fig. 5a). Similarly to the case of transmission of dislocations through a lamellar boundary, the applied shear strain is perpendicular to the interface and induces a glide force in the  $[\bar{1}\bar{1}\bar{1}]$  direction. The core structure starts to distort at an applied stress of  $0.020C_{44}$  (Fig. 6a). When the applied stress exceeded  $0.025C_{44}$ , the core structure spreads into the twin boundary and two {111} planes in the lower lamella and the interfacial dislocation transformed to a lattice  $\frac{1}{2}$  (110] screw dislocation with its elastic center displaced several atomic layers away from the boundary (Fig. 6c). The core structure is distorted compared to the core of ordinary dislocations along the interface (Fig. 2) due to the applied stress.

Comparison between Fig. 4a and Fig. 5a shows that when ordinary dislocations reach the boundary they become ordinary interfacial dislocations. Hence, the mechanism of transmission of a  $\frac{1}{2}$  (110] screw dislocation through a twin boundary after the formation of interfacial dislocation is similar to the mechanism of detachment of the interfacial  $\frac{1}{2}$  (110] screw dislocation from the interface. The difference between the two cases is due to the high applied stress in the simulation block necessary for the formation of the interfacial dislocation in Fig. 4a, as an intermediate step of the transmission of the dislocation into the adjacent lamella. As a result, the interfacial dislocation shown in Fig. 5a detaches from the boundary at a lower stress than the stress necessary for the transmission of ordinary screw dislocation through the interface (Fig. 4). In the case of lower stress applied in the lattice, the molecular statics method allows us to trace better the propagation of the detaching dislocation in the second crystal. While the proximity of the boundary distorts asymmetrically the core structure of the dislocation, with increasing stress the displacements extend along the  $(11\overline{1})$  slip plane (Fig. 6b). Several atomic layers away from the interface, the ordinary dislocation recovers its typical core structure, spreading into two  $\{111\}$  planes (Fig. 6c) and its glide again becomes a zigzag motion on (111) and (111) planes. It may be supposed that the propagation of the dislocation in the second lamella when it is transmitted through the boundary is completely analogous.

### 5 Discussion

Our atomistic simulation results for  $L1_0$  TiAl show that the glide of ordinary  $\frac{1}{2}$  (110] straight dislocations in the screw orientation under an applied stress is characterized by zigzag movement on two conjugated  $\{111\}$  planes. When the dislocation moves by one lattice spacing along the primary (111)plane its core structure at the new location is rather distorted, compared to its initial configuration, due to the high resolved shear stress. The distorted core structure leads to cross slip of the ordinary dislocation on the  $(11\overline{1})$ plane with increasing stress. The combination and succession of the cross slip planes depends on the orientation of the applied shear stress and on the magnitude of the corresponding Schmid factors. The same motion in between (111) and (11 $\overline{1}$ ) planes was found even if the Schmid factor for one of the planes is zero. The non-planar core of the  $\frac{1}{2}$  (110] screw dislocation, spread into two planes of the  $\{111\}$  type, is distorted asymmetrically when the elastic center of the dislocation is close (within 2-3 atomic layers) to a twin boundary. While the proximity of the interface distorts the core structure of the dislocation, it moves on just one or other of the (111) planes, depending on the magnitude of the corresponding Schmid factor. We therefore see two glide mechanisms, depending on how close the dislocation lies to a twin boundary. Due to the asymmetric core structure close to the boundary the frictional barriers for (111) glide in  $[\overline{112}]$  and  $[11\overline{2}]$  directions are different. The dislocation starts to move under an applied stress of  $0.027C_{44}$ in [112] and  $0.024C_{44}$  in the opposite direction.

The zigzag motion of the dislocation leading on average to glide on the (001) plane as predicted by our BOP simulations has

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not been observed in practice in TiAl. The reasons for this discrepancy have yet to be clarified. It may be due to several factors. The second step along  $(11\overline{1})$  plane is not confirmed by DFT simulations and may be effect of the potential or the fixed boundary conditions used in the simulations. The results of the atomistic simulations describing the glide of a  $\frac{1}{2}$  (110] screw dislocation and its Peierls stress are for straight dislocations in stoichiometric material at 0° K. Real dislocations are always in the shape of loops and their mixed part must stay in the glide plane. The results of our atomistic simulations indicate that the second step on the cross-slip plane is due to the distortion of the dislocation core structure after moving one lattice spacing on the primary plane as a result of the high critical resolved shear stress. Both BOP and DFT simulations of straight dislocations predict values for the critical resolved shear stress more than twice the extrapolated experimental value at low temperature. The reasons behind this are not well understood. This may be because the lattice frictional stress is large enough to favour movement by kink-pair formation. Solid-solution softening in TiAl alloys can also be caused by deviations from stoichiometry [28]. At lower stress the dislocation core structure of the screw segments will be less distorted and the first step along (111) can repeat itself with increasing stress [29].

However, there is much experimental evidence that the double cross slip of the screw segments, predicted by BOP, is an essential characteristic of the glide of ordinary dislocations. TEM analyses [30, 31, 32] of ordinary dislocations under stress have shown that they are elongated along their screw orientation and anchored at many points. The screw segments separated by pinning points are observed to lie in different planes, implying that they have cross slipped onto parallel (111) planes [32]. The experimental observations show a dislocation structure more consistent with dislocation glide involving propagation of macro-kinks, formed as a result of frequent double cross slip. If no obstacle opposes the lateral propagation of the edge segments lying in the cross slip plane, the whole dislocation moves onto a primary glide plane parallel to the initial one and no trace of cross-slip can be seen. If the same dislocation makes the same double cross slip but in a crystal containing extrinsic obstacles, the micrographs show formation of pinning points and several segments of dislocations lying in different planes. The models explaining the experimental results require that the ordinary screw dislocation will easily cross slip, and that the lattice frictional stress is large enough to favour movement by kink-pair formation. The present 2D simulations can not provide the necessary information about the core structures of screw

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segment containing kinks or jogs, their response to applied stress and influence on the mobility of ordinary screw dislocations. Three dimensional simulations of the activation and propagation of dislocations in nonlamellar and lamellar crystal would be required to fully understand the influence of the two different predicted glide mechanisms on the macroscopic yield in single-phase and lamellar  $\gamma$ -TiAl.

The lamellar interfaces have two-fold functions in the deformation of lamellar crystals of TiAl. The lamellar boundaries are large reservoirs of dislocations, which may assist plastic deformation. However, these interfaces oppose the activation of deformation systems. The results addressed in the previous sections indicate that ordinary dislocation slip can be activated inside the  $\gamma$  lamellae. However, the confinement of the lamellar interfaces leads to the highly anisotropic deformation behaviour. Inui et al. [6] reports two deformation modes for polysynthetically twinned crystals of TiAl: an easy mode, characterized by glide parallel to the lamellar boundaries, and a hard mode, characterized by glide perpendicular to the interfaces. In agreement with this observation, the present atomistic simulation results predict that the mobility of lattice  $\frac{1}{2}$  (110] screw dislocations close to a twin interface in a direction parallel to the interface is higher than in the perpendicular direction. The mobility of both the lattice and interfacial ordinary dislocations along the interface could thus increase plastic deformation in this direction.

The coherency stresses at the twin lamellar interface can exert a Peach-Köhler force acting on the glide dislocations, which attracts or repels dislocations from the interface. Similar forces do not act on ordinary dislocations in screw orientation and in accordance with this elastic interaction of the dislocations with the interfaces were not predicted by the atomistic simulations. It can be seen from the results presented in the previous sections, that the coherency stresses do not induce non-glide stresses, which modify the core structure of the ordinary screw dislocations (Fig. 2a). In addition to elastic interactions between the lamellar boundaries and the gliding dislocations, the stacking-fault energy changes at the interface ('chemical' or 'gamma surface' mismatch) can result in dislocation core structure changes as the dislocation moves from one lamella to the next. Since the energy of the CSF at the twin boundary is even higher than the energy of the CSF calculated in bulk  $L1_0$  TiAl, the ordinary screw dislocation retains its non-planar core structure as the dislocation approaches the interface and no dissociation into Shockley partials separated by CSF at the interface was predicted by the atomistic simulations.

For this particular crystallographic orientation of the  $\gamma$  lamellae, under an applied stress ordinary dislocations can glide through the twin boundaries. Their Burgers vectors are ordinary on both sides of the interface. In absence of gamma surface and long-range elastic interactions, the blocking strength of the twin interface to the glide of ordinary dislocations is a re-

sult of the discontinuity of the slip planes across the interface. As a result, the ordinary screw dislocations have to cross-slip for transmission of slip across the interface. The blocking strength of twin boundaries to the glide of  $\frac{1}{2}$  (110] screw dislocations is found to exceed  $0.040C_{44}$ . When ordinary dislocations reach the boundary they become ordinary interfacial dislocations. These dislocations can glide further in the adjacent lamella under an increasing applied stress, because the directions of their Burgers vectors on either of the twin boundary coincide. In agreement with TEM observations and empirical slip transmission rules [33, 34] the atomistic simulation of ordinary dislocations remaining on the interface. Ordinary screw dislocations recover their typical core structure once they have left the boundary, spreading into two {111} planes, and their glide again becomes a zigzag motion on (111) and (111) planes.

Following the above calculations we may speculate on a mechanism for the increased number of ordinary dislocations observed within a lamellar structure. The higher density of ordinary dislocations in the lamellar microstructure can be interpreted through the effect of the interfaces, where a very high density of ordinary interfacial dislocations is found [35]. Most probably the reason for the high density of ordinary interfacial dislocations is the decomposition of the superdislocations with a Burgers vector of type  $\langle 101 \rangle$  into ordinary dislocations at the lamellar interface. The transformation of a superdislocation into two ordinary dislocations at a lamellar interface is allowed for twin and other orientations, when the Burgers vector of the superdislocation is parallel to the interface [35]. Detachment of ordinary interfacial dislocations, accumulated at the lamellar boundaries, and their propagation into the interior of the lamellae could be one of the possible reasons for the experimentally observed higher density of ordinary dislocations in lamellar than in non-lamellar TiAl at low temperature.

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### References



- Kim, Y.-W., 1989, Intermetallic alloys based on gamma titanium aluminide. JOM 41, 24.
- [2] Appel, F., Wagner, R., Mater. Sci. Eng. R22, 1998, 187.

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- [3] Yamaguchi et all, 1995, in "High-Temperature Intermetallic Alloys VI, Part 1", edited by J. A. Horton et all, Mat. Res. Soc. Symp. Proc., vol. 364, (Pittsburgh, PA: Materials Research Society), p. 3
- [4] M. Yamaguchi, H. Inui, S. Yokoshima, K. Kishida and D. R. Johnson, Mat. Sci. Eng. A 213, 1996, 25.
- [5] Inui, H., Matsumuro, M., Wu, D.-H., and Yamaguchi, M., Phil. Mag. A 75, 1997, 395.
- [6] Inui H., Oh M. H., Nakamura A., and Yamaguchi M., Phil. Mag. A 66, 1992, 539.
- [7] S. Zghal, S. Naka, A. Couret, Acta Mater. A 45, 1997, 3005.
- [8] C.L. Fu and M.H. Yoo, Scripta Mater. 37, 1997, 1453.
- [9] V. Paidar, S. Zghal, A. Couret, Mater. Sci. Forum 294-296, 1999, 385.
- [10] A. Girshick and V. Vitek, High-Temperature Ordered Intermetallic Alloys VI, edited by J.Horton, I. Baker, S. Hanada, R. D. Noebe and D. Schwartz (Pittsburgh, Materials ResearchSociety), Vol. 364, 1995, 145.
- [11] R. Mahapatra, A. Girshick, D. P. Pope and V. Vitek, Scripta Metall. et Mat. 33, 1995, 1921.
- [12] Simmons, J. P., Rao, S. I., and Dimiduk, D. M., Philos. Mag. A 75, 1997, 1299.
- [13] J. Panova and D. Farkas, Philos. Mag. A 78, 1998, 389.
- [14] C. Woodward and S. I. Rao, Phil. Mag. A 84, 2004, 401.
- [15] Znam S., D. Ngueyen-Manh, Pettifor D.G. and Vitek V., Phil. Mag., 83, 2003, 415.
- [16] Znam, S., 2001, Ph.D. Thesis, University of Pennsylvania.
- [17] Pettifor D.G., Phys. Rev. Lett. 63, 1989, 2480.
- [18] Aoki M. and Pettifor D.G., in Physics of Trans. Metals, edited by P.M. Oppeneer and J.Kubler -World Scientific, Singapore, 1993, 299.
- [19] D. G. Pettifor, I. I. Oleinik, D. Nguyen-Manh and V. Vitek, Comp. Mat. Sci. 23, 2002, 33.
- [20] Finnis M., Interatomic Forces in Condensed Matter, Oxford University Press, 2003.
- [21] Horsfield A.P., Bratkovsky A.M., Fearn M., Pettifor D.G., and Aoki M., Phys. Rev. B 53, 1996, 12694.

Page 15 of 32

- [22] R. Porizek, S. Znam, D. Nguyen-Manh, V. Vitek and D. G. Pettifor, Mat. Res. Soc. Symp.Proc. vol. 753, 2003, BB4.3.1.
- [23] Hirth, J. P. and Lothe, J., Theory of Dislocations, 2nd edn. Wiley-Interscience, New York, 1982.
- [24] Vitek, V., Cryst. Lattice Defects, 5, 1974, 1.
- [25] V. Paidar, J. of Alloys and Compounds 378, 2004, 89.
- [26] D. M. Barnett and J. Lothe, J. Phys. F: Metal Phys., Vol. 4, 1974, 1618.
- [27] Inui, H., Matsumuro, M., Wu, D. H., and Yamaguchi, M., 1997, Phil. Mag. A, 75, 395.
- [28] Sriram, S., Vasudevan, V. K., and Dimiduk, D. M., 1995, Mater Sci. Engng, A193, 217.
- [29] Vitek, V., (2006, private communication).
- [30] Sriram, S., Dimiduk, D. M., Hazzledine, P. M., and Vasudevan, V. K., 1997, Phil. Mag., 76, 965.
- [31] Viguier B, Hemker KJ, Bonneville J, Louchet F, Martin JL. Phil. Mag. A 1995, 71, 1295.
- [32] A. Couret, Intermetallics 9, 2001, 899.
- [33] Hu D., Loretto M.H., Intermetallics, 7, 1999, 1299.
- [34] S. Zghal, A. Coujou, A. Couret, Phil. Mag. A 81, 2001, 345.
- [35] L. Parrini, J. of Alloys and Compounds 270, 1998, 203.



#### FIGURE CAPTIONS

Fig. 1a-d. Differential displacement plots showing the screw components of a  $\frac{1}{2} \langle 110 \rangle$  screw dislocation moving under a pure (111) glide stress. The open circle marks the original position of the dislocation.

Fig. 1a. Applied stress  $\sigma_{zy} = 0$ 

Fig. 1b. Applied stress  $\sigma_{zy} = -0.015C_{44}$ 

Fig. 1c. Applied stress  $\sigma_{zy} = -0.017C_{44}$ 

Fig. 1d. Applied stress  $\sigma_{zy} = -0.020C_{44}$ 

Fig. 2a, b. Differential displacement plots showing the screw components of the predicted equilibrium dislocations cores for  $\frac{1}{2} \langle 110 \rangle$  screw dislocations in TiAl along a twin  $\gamma/\gamma$ -interface. The open circle marks the original position of the elastic centers of dislocations.

Fig. 3a-b. Differential displacement plots showing the screw components of a  $\frac{1}{2} \langle 110 \rangle$  screw dislocations moving along a twin  $\gamma/\gamma$ -interface under a pure (111) glide stress.

Fig. 3a. Applied stress  $\sigma_{zy} = -0.020C_{44}$ 

Fig. 3b. Applied stress  $\sigma_{zy} = -0.027C_{44}$ 

Fig. 4a-c. Differential displacement plots of the relaxed configurations of  $\frac{1}{2}$  (110] screw dislocations in a  $\gamma/\gamma$  bilayer simulation cell at applied stresses in direction toward the interface.

Fig. 4a. Applied stress  $\sigma_{zx} = -0.015C_{44}$ 

Fig. 4b. Applied stress  $\sigma_{zx} = -0.040C_{44}$ 

Fig. 4c. Applied stress  $\sigma_{zx} = -0.0417C_{44}$ 

Fig. 5a-b. Differential displacement plots showing the screw components of a  $\frac{1}{2}$  (110] interfacial screw dislocations moving along a twin  $\gamma/\gamma$ -interface under a pure (111) glide stress.

Fig. 5a. Applied stress  $\sigma_{zy} = 0$ 

Fig. 5b. Applied stress  $\sigma_{zy} = 0.028C_{44}$ 

Fig. 6a-c. Differential displacement plots of the relaxed configurations of  $\frac{1}{2}$  (110] screw interfacial dislocations detaching from the lamellar boundary at applied stresses in direction perpendicular to the interface.

Fig. 6a. Applied stress  $\sigma_{zx} = -0.020C_{44}$ 

Fig. 6b. Applied stress  $\sigma_{zx} = -0.025C_{44}$ 

Fig. 6c. Applied stress  $\sigma_{zx} = -0.032C_{44}$ 































