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**Renner-Teller Interaction, High Angular Momentum States
and Spin-Orbit Interaction in the Electronic Spectrum of
ND₂**

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3 Renner-Teller Interaction, High Angular Momentum States and Spin-Orbit Interaction
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6 in the Electronic Spectrum of ND₂
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24
25 **Abstract**
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29 A rotational and vibrational analysis has been made of the ND₂ $\tilde{A}^2A_1 - \tilde{X}^2B_1$ emission
30 spectrum produced from the ultraviolet laser induced dissociation of both jet cooled
31 and room temperature deuterated ammonia. By a combination of these experimental
32 data with model calculation based upon the stretch-bender Renner-Teller
33
34 Hamiltonian, and a previous analysis of the NH₂ spectrum, most of the strong features
35 in the emission spectra have been assigned. The spectrum consists of transitions from
36 a narrow distribution of high angular momentum states peaking at K_a values of 7 in
37 the jet condition, and 8 at room temperature. Information has also been gained on the
38 high angular momentum states of previously inaccessible higher bending levels from
39 v₂ = 2 to v₂ = 6 in the \tilde{X}^2B_1 state.
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58 **Introduction**
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3 The Born-Oppenheimer approximation¹, published in 1927, is used to allow the
4 separation of the high frequency electronic motion from the low frequency nuclear
5 motion, and hence the separation of the vibronic Hamiltonian into an electronic and a
6 nuclear Hamiltonian. For this to be the case the vibrational energy separations must
7 be at least two orders of magnitude smaller than the electronic energy separations.
8 Similarly vibration and rotation may be separated if the rotational energy separations
9 are at least two orders of magnitude smaller than the vibrational energy separations.
10 In the period from 1927 until about 1960, much of the theoretical effort was devoted
11 to methods of deriving information about potential energy curves of electronic states
12 of diatomic molecules, or the potential energy surface of an electronic state of a
13 polyatomic molecule directly from the analysis of a high resolution spectrum. In
14 particular the analysis of the spectra recorded in the infrared and microwave region
15 relied upon the separation of vibrational and rotational motion.
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36 Within ten years of the Born-Oppenheimer paper¹, Teller and his collaborators^{2,3} had
37 identified specific examples of molecules in which the breakdown of the Born-
38 Oppenheimer separation could occur. The first of these is the Renner (or Renner-
39 Teller) effect² and the second is the Jahn-Teller effect³. Although the original Renner-
40 Teller paper, describing in detail the breakdown of the Born-Oppenheimer separation
41 in linear open-shell molecules, was published by Renner in 1934², the first
42 experimental measurements of a molecular example, the spectrum of NH₂ were not
43 made until 1952 by Herzberg and Ramsay⁴, and a detailed analysis published by
44 Dressler and Ramsay in 1959⁵. The spectrum of NH₂ is not an example of the type of
45 spectrum envisaged by Renner, as the static splitting between the two component
46 states is very large, with the lower component state having a bent equilibrium
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3 configuration. A second molecule, NCO, whose absorption spectrum was first
4 recorded in 1958⁶, and analysed by Dixon in 1960⁷ was the first molecule with a
5 linear equilibrium configuration of the type which Renner² had considered. A
6 theoretical treatment of the energy level pattern in NH₂ was given by Pople and
7 Longuet-Higgins⁸ and of the combined Renner and spin-orbit coupling in NCO type
8 molecules by Pople⁹.

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20 In 1961 Longuet Higgins¹⁰ wrote a review about both the Renner-Teller and Jahn-
21 Teller effect as two related examples of the strong coupling between vibrational and
22 electronic motions of molecules. In his introduction he wrote that “Most of us are so
23 used to thinking of the two independently that it requires quite an effort of mental
24 adjustment to abandon the idea that vibrational motions are determined by uniquely
25 defined potential functions.” He also noted, referring implicitly to recent
26 experimental studies of that era such as the analyses of the spectra of NH₂ and of
27 NCO, that “coupling effects produce, in particular molecules, some striking
28 experimental phenomena”. More recently Peric and Peyerimhoff¹¹ have given an
29 excellent comprehensive survey of the status of the Renner-Teller effect forty years
30 on. In their review they have classified the Hamiltonians used into “Minimal
31 Models”, “Pragmatic Models”, Benchmark Handling” and “Effective Hamiltonians”.
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It is the purpose of the present paper to show that the “Minimal Models” and
“Pragmatic Models” constitute types of effective Hamiltonians, as do the “Effective
Hamiltonians” defined by Peric and Peyerimhoff. The main differences between them
are associated with the type of reference frame used to help simplify the calculation,
and also the amplitude of the motion of the bending motion, which leads to the
splitting of the electronic degeneracy.

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6 The vehicle which we have chosen to demonstrate the applicability and usefulness of
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8 the pragmatic approach to the development and use of such effective Hamiltonians is
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10 the recently recorded emission spectrum of ND_2 ¹², and the contrast between the type
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12 of problem posed by such a spectrum and the original ND_2 spectrum analysed by
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14 Dressler and Ramsay⁵. We may note that in their original analysis of the spectrum of
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16 NH_2 , Dressler and Ramsay made great use of the “minimal” model of Pople and
17
18 Longuet–Higgins⁸ in order to understand the complex structure of the observed
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20 spectrum. In fact the comparison between the predicted and observed vibronic
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22 patterns given in their paper gave a very compelling verification of the occurrence of
23
24 Renner-Teller coupling in the NH_2 free radical.
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32 In the NH_2 free radical there is a very large change in the equilibrium bond angle
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34 between the ground state, whose geometry is very similar to that of water, and the
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36 excited state, which is almost linear. Both the ground \tilde{X}^2B_1 and the excited \tilde{A}^2A_1 state
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38 correlate with the two components of a degenerate $^2\Pi_u$ state of linear NH_2 . The
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40 Renner-Teller coupling is therefore between two states with a large static splitting of
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42 their potential energy surface at equilibrium, but which may become very strongly
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44 dynamically- coupled when the molecule executes large amplitude bending motion.
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46 Since the equilibrium geometries are so different, the absorption spectrum structure is
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48 dominated by the Franck-Condon allowed transitions, which results in the probing of
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50 excited states where the molecule is executing large amplitude bending motion. An
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52 understanding of the structure of the resulting spectrum therefore demands an
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54 understanding of both Renner-Teller and spin-orbit interaction and large amplitude
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56 motion.
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6 The original approaches to understanding the effects of large amplitude bending
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8 motion on Renner-Teller coupling, from the point of view of the analysis of
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10 experimental spectra, started about 1970. This coincided with an interest in the large
11
12 amplitude bending motion in closed shell molecules of the type considered originally
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14 by Hougen, Bunker and Johns (HBJ)¹³, and continued by Bunker and Jensen¹⁴ and
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16 their collaborators and more recently Tennyson and his group¹⁵. Water was the first
17
18 well documented example where the vibration rotation effective Hamiltonian
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20 expressed as a power series expansion of the type classified by Watson¹⁶ converged
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22 very slowly, and hence a search was made for methods of treating the large amplitude
23
24 motion explicitly.
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29 In the spectroscopy of closed shell molecules in which large amplitude motion is
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31 encountered, two basic philosophies have been used to achieving the construction of a
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33 satisfactory Hamiltonian, either concentrate on the isolation of the behaviour
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35 associated with a rogue large-amplitude coordinate, or use a new type of Hamiltonian
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37 in which motion in all coordinates is treated as potentially of large amplitude. With
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39 experimental evidence from the Frank-Condon patterns in electronic spectra that
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41 vibronic transitions to highly excited bending levels could be observed, Hougen
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43 Bunker and Johns (HBJ)¹⁵ developed a new method based upon the use of an angular
44
45 dependent reference frame. Their method treats the bending vibration as the rogue
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47 coordinate, while treating the rest of the motion using a standard effective
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49 Hamiltonian, as the stretching motion is assumed to be of small amplitude relative to
50
51 the reference frame. The calculations of Tennyson and his group for triatomics¹⁵, and
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53 tetraatomics¹¹, are very difficult to carry out, and are typical of the use of an
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3 instantaneous axis Hamiltonian to solve the full three-dimensional vibration-rotation
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6 problem.

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10 In open shell molecules the complexity of large amplitude motion on two coupled
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12 surfaces has meant that few groups have tackled the problem in the way in which
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14 Tennyson¹⁵ and his group have attacked the water problem. The closest to this has
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16 been the calculations of Carter and Handy¹⁷, using the ab initio data of Rosmus¹⁸ and
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18 Chambaud and their colleagues. In many triatomic molecules only the bending
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20 motion is of very large amplitude, but the coupling between the stretching and
21
22 bending motion, whilst weak, can often lead to complicated vibrational resonances.
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24 Since experimental data of molecules such as NH₂ may be partly analysed by
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26 experimentalists by treating the individual sub-bands in the spectrum as though they
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28 were similar in structure to those of diatomic molecules, it is indicative that the
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30 separation of the motion in the large amplitude coordinates from that of the rest of
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32 the vibration-rotation problem may be quite good as noted above. As a result one may
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34 seek to develop a Hamiltonian which is based upon the possibility of such a
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36 separation.

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46 The first Hamiltonian of this type was developed by Dixon and his colleagues¹⁹, and
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48 was motivated by studies of the electronic spectrum of PH₂, the phosphorous
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50 analogue of NH₂. PH₂, like NH₂, has very different equilibrium geometries in the
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52 ground and first excited state. The method which they chose was to transform the
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54 coupled equations, including both the Renner-Teller and spin-orbit coupling, in order
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56 to produce rotationally adiabatic potential energy curves for the \tilde{X}^2B_1 and the \tilde{A}^2A_1
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58 vibronic states at each value of the bending angle. The remaining Renner-Teller
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3 coupling between the \tilde{X}^2B_1 and the \tilde{A}^2A_1 states then entered owing to the non-
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6 commutation of the diagonal nuclear kinetic energy operator and the angle dependent
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8 coordinate transformation. This method was published by Barrow, Dixon and
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10 Duxbury in 1974¹⁹, and forms the basis of many of the methods subsequently used to
11
12 tackle this type of problem. However, as there was little information about the
13
14 location of the bending vibrational levels associated with the ground electronic state, a
15
16 decision was taken to use a damping method¹⁹ to remove the effect of strong resonant
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18 interactions between levels formally belonging to the \tilde{X}^2B_1 and the \tilde{A}^2A_1 states.
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25 The key series of papers in which the effect of localised resonances were treated
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27 exactly were by Jungen and Merer and Hallin²⁰⁻²². Their method was based on that of
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29 Renner², and transformed the Hamiltonian matrix rather than the interaction
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31 Hamiltonian. The relationship between this and the BDD method has been given by
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33 Duxbury and Dixon²³. The usefulness of the original work on NH₂ by Jungen, Hallin
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35 and Merer has been demonstrated many times over the years following its publication.
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37 For example, Vervloet^{23,24} was able to use their calculated energy levels to aid the
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39 analysis of the spectra of highly excited levels of the ground electronic state of NH₂,
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41 whose details had not been included in their original fitting scheme. It therefore seems
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43 that this original bending-only model incorporates much of the essential physics of
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45 the problem, including the effect of the bonds stretching as the molecule executes
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47 very large amplitude bending motion. It was also used by Dixon and his colleagues²⁶
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49 as a starting point when they studied the states of high angular momentum in the
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51 electronic spectra of NH₂.
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3 The rovibronic states of ND_2 which we analyse in the present paper are also high
4 angular momentum states which arise when the free radical is produced by the
5 photodissociation of either ND_3 or ND_2H^{12} . In these experiments the isotopic forms of
6 the NH_2 free radical have been studied to aid the understanding of the
7 photodissociation processes which occur in vacuum ultraviolet photolysis of
8 ammonia. The free radical is then studied either using a flow cell, or a supersonic jet.
9 Studying the nascent states of the free radical allows part of the dissociation dynamics
10 to be inferred. Much of the theoretical understanding of this has been due to Dixon²⁶,
11 and the experiments carried out by Dixon and Ashfold and their colleagues at
12 Bristol^{26,27}, and Leone and his collaborators, particularly Woodbridge, Ashfold,
13 Loomis and Reid at JILA²⁸⁻³⁰. The experimental data on ND_2 analysed in this paper
14 was recorded by Reid, Leone and Loomis at JILA¹².

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34 It might be wondered why these unusual states were not seen in the original flash
35 photolysis experiments of Dressler and Ramsay. In the original flash photolysis
36 method the trihydrides were photolysed in the presence of a high pressure of a noble
37 gas such as argon to thermalise the free radical, so that its effective temperature was
38 close to room temperature. As a result the absorption spectrum of ND_2 recorded by
39 Dressler and Ramsay⁵ contains only transitions with little excitation of rotational
40 angular momentum about the linear molecule axis, K_a , whereas almost all the
41 transitions which we have identified in emission have much higher values of K_a .
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53 There is therefore no overlap between the vibronic levels of the \tilde{A}^2A_1 state measured
54 at JILA¹² and those of the original experiments carried at the National Research
55 Council of Canada in Ottawa.
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Experimental

A detailed description of the experimental apparatus has been given in previous publications on the dissociation dynamics of ammonia and deuterated ammonias, so only a very brief summary will be provided here^{12, 28-30}. The studies were performed both at room temperature, with a continuous flow of ammonia, and jet cooled, with a piezoelectric pulsed valve. The triggering of the ArF excimer laser, which initiates the photodissociation, and also the opening of the pulsed jet for the jet cooled studies, were both synchronised to the position of a moving mirror in a commercial continuous scan Fourier transform spectrometer (FTS). The emission from the electronically excited ND₂ fragments was then recorded using the FTS in this gated mode, to give a time history of the fluorescence. The spectrum was recorded in two wavenumber regions, from 5000 to 12,000 cm⁻¹ using an InSb detector, from 10,000 to 15,000 cm⁻¹ with a Si avalanche detector. In the overlap region from 10,000 to 12,000 cm⁻¹ the signal to noise ratio of the spectra measured using the avalanche detector was usually better, and were mainly used for the spectroscopic analysis. The resolution of the emission spectra was 0.2 cm⁻¹.

Analysis of the ND₂ $\tilde{A}^2A_1 - \tilde{X}^2B_1$ emission spectrum

An analysis of much of the emission spectrum was made by Reid, Loomis and Leone¹² in order to understand the effects of parent zero-point motion on the ND₂ \tilde{A}^2A_1 rotational distribution. However in their paper only an outline of the rotational analysis was given. In the present paper we have extended the analysis by making use of stretch-bender^{31,32} calculations of the spectrum of ND₂, using the potential

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3 developed by Alijah and Duxbury^{33,34} in their detailed modelling of the NH₂
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5 spectrum. We have also used the rotational term values of ND₂ derived from the
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7 analysis of high resolution laser magnetic resonance, electronic spectra, and
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9 microwave optical double resonance, by Muenchausen et. al.³⁵, and the very high
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11 angular momentum states measured in their far infrared FT spectra by Morino and
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13 Kawaguchi³⁶. Their use has been crucial in obtaining accurate values of the terms
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15 values in the \tilde{A}^2A_1 state, and subsequently of vibrationally excited levels in the \tilde{X}^2B_1
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17 state.
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25 Since the spectra of the ND₂ free radicals are due to emission from nascent free
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27 radicals produced from the photodissociation of their parent deuterated ammonia, the
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29 population of the excited state energy levels from which emission is observed reflect
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31 the way in which the free radical is produced in the photodissociation process. The
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33 distribution of intensity in the emission spectrum therefore reflects the distribution of
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35 angular momentum about the least axis of inertia, the a-axis, which correlates with the
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37 axis of linearity of linear ND₂. It has been found¹² that in ND₂ molecules produced by
38
39 the photolysis of jet cooled ND₃, the majority of the molecules are in rovibronic levels
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41 of the excited state with K_a=7. When room temperature ND₃ is photolysed the levels
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43 with K_a=8 are also populated with a similar or slightly greater probability¹² than those
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45 with K_a=7. The process responsible for this including the amount of available energy,
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47 has been described in a series of papers by Reid et al.^{12,29,30}. In order to show the
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49 effect of the photodissociation to produce a very non-Boltzman population of the
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51 excited state levels, in Figure 1 a survey of the emission spectrum from the photolysis
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53 of jet cooled ND₃ is shown. It may be seen that it is dominated by the ^RR branches
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55 and ^PP branches originating from the K'=7 angular momentum state of the zero-point
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3 vibrational level of the \tilde{A}^2A_1 state of ND_2 . In these low temperature spectra the main
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5 lines seen in these branches have $N' = K_a' = 7$. The spectra obtained from the
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7 photolysis of room temperature ND_3 are more complicated, but the origins of several
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9 of the branches with $K_a' \neq 7$ may be obtained by a direct comparison on these spectra
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11 with those obtained from the photolysis of the cold ND_3 . As only levels associated
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13 with the excitation of the bending vibration have been observed in these experiments,
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15 the transitions are labelled by the vibrational mode number, 2, and the number of
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17 vibrational quanta of the bending vibration which are excited in the \tilde{X}^2B_1 and \tilde{A}^2A_1
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19 states, i.e. $2_{v_2}^{v_1}$. The main bands seen in the cold spectrum are 2_0^0 , 2_1^0 , 2_2^0 , 2_3^0 , 2_4^0 and
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21 2_5^0 , as well as part of the 2_6^0 band.
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30 In the expanded section of the photodissociation product emission spectrum shown in
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32 Figure 2, it may be seen that in the room temperature dissociation spectrum there are
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34 a much larger number of emission lines than from the jet cooled parent. It may also be
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36 seen that the dominant pattern involves closely spaced doublets of approximately
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38 equal intensity. This doubling is due to spin-orbit splitting of the rovibronic energy
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40 levels in both the ground and the excited states of ND_2 . Using prolate symmetric rotor
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42 labelling with $K = K_a$, and with N being the total angular momentum neglecting
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44 electron spin, the F_1 level of the split rovibronic level has $J=N+1/2$ and the F_2 level
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46 $J=N-1/2$. As all the doubling associated with a-axis rotation is related to the spin-
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48 orbit splitting of the linear molecule, in the absence of strong localised resonances
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50 between the levels of the \tilde{A}^2A_1 and the \tilde{X}^2B_1 states, the sign of the splitting in the
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52 lower state is reversed from that in the excited state. It has been shown that in the
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54 \tilde{X}^2B_1 state²⁰⁻²² this splitting results in an inverted state where the energy of the F_2
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56 levels is greater than that of the F_1 levels, whereas in the \tilde{A}^2A_1 levels identified in
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3 these photodissociation experiments the excited state levels are regular, with the
4 energy of the F_1 levels greater than that of the F_2 levels. For the measured transitions
5 between the zero point levels of both the ground and the excited states the spin-orbit
6 splitting of the levels of the \tilde{X}^2B_1 state has been shown to be small, so that most of the
7 spin-orbit splitting observed in the spectra shown in Figure 2 is due to that in the
8 excited state. However, as the ${}^P P, N''=N'+1, K''=8$. and the ${}^R R, N''=N'-1, K=6$, both
9 originate from the levels with $N' \geq K', K'=7$, the difference between the measured
10 splitting of these transitions is related to the difference in the splitting in the \tilde{X}^2B_1
11 state. Moreover, as the energies of the F_1 and F_2 components of a rotational level in
12 the ground state are inverted, with F_1 at lower energy than F_2 , the magnitude of the
13 splitting in these pairs of ${}^P P$ and ${}^R R$ branches is greater than that of the excited state
14 N, K level. We can make use of this when following the splitting of the equivalent
15 branches of the sequence of levels terminating in successively higher bending
16 vibrational levels of the ground electronic state. As a result we can investigate the
17 influence on the magnitude of the spin-orbit splitting of these energy levels upon the
18 decreasing separations of these energy levels from that of the zero-point level of the
19 excited state. The variation of this splitting of equivalent transitions, having a
20 common pair of F_1 and F_2 components with $K' = 7$, with low and high values of v_2'' ,
21 is shown in Figure 3.

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51 The weaker emission lines seen in Figure 2 have two main origins, either they belong
52 to perpendicular Q branches associated with the much stronger ${}^P P$ and ${}^R R$ branches,
53 or they originate from excited bending levels of the \tilde{A}^2A_1 state. Reid et al³⁰ have used
54 a cross- correlation technique to analyse the change in the raw spectral emission data
55 with the variation in mixture composition, as it was found that the emission spectra
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3 produced by the photodissociation on ND₃ and ND₂H are significantly different. In
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5 particular they used this method to identify which of the patterns seen in this spectral
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7 region originated from vibrationally excited levels of ND₂ and which did not. An
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9 example is shown in Figure 5 of their paper. In Figure 4 we show an expanded part of
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11 the spectrum from room temperature dissociation, in which the ^RQ branches which lie
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13 to the red of the associated ^RR branch may be clearly seen. In Figure 5 we show an
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15 extract of a spectrum produced by the photodissociation of ND₃, and one containing
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17 only emission lines from excited bending levels of ND₂ derived by Reid et al³⁰. Use
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19 of this spectrum has enabled us to clearly identify many of the remaining weak
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21 emission lines seen in the spectra obtained by the photodissociation of ND₃.
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29 The assignments of the emission spectra of ND₂ are given in Table 1. In Table 2 we
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31 give the excited state term values derived from the experimental measurements of
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33 transitions in the 2₀⁰ and 2₁⁰ bands by using the v₂=0 and 1 term values obtained from
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35 the work of Muenchausen et. al.³⁵ and Morino and Kawaguchi³⁶. In this table they are
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37 compared with theoretical calculations based upon the NH₂ spectrum^{33,34}, using the
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39 stretch-bender Renner-Teller Hamiltonian³². In Table 3 we show the ground state
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41 term values derived from the earlier experimental work, and in Table 4 the term
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43 values of levels of the higher vibrational states of the ground electronic state. These
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45 latter term values were calculating by subtracting the values of the wavenumbers of
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47 the fluorescence spectra from the term values given in Table 2. The fluorescence
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49 spectra used were from the 2₂⁰, 2₃⁰, 2₄⁰ and 2₅⁰ bands, and also the much weaker 2₆⁰
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51 band.
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Stretch-Bender vibronic and rovibronic energy level calculations.

The calculations of the structure of the spectrum of the high angular momentum transitions in ND₂ was carried out using the Renner-Teller code based on the BDD¹⁹ Hamiltonian transformation coupled with the stretch-bender implementation³¹ of large amplitude bending and coupling with the symmetric stretching vibrations. The basis of this is described in detail by Duxbury et. al.³¹ and by Alijah and Duxbury³². The stretch-bender part of the Hamiltonian originated from an idea of Jungen, who together with Palivan developed its use for linear molecules, as well as for CH₂³¹. In the present paper we have made use of the parameterisation used by Alijah and Duxbury³²⁻³⁴ to fit the extensive data on the ground and excited states of NH₂. The parameters used in the present calculations are given in Table 5. They are identical to those used by Duxbury and Alijah³²⁻³⁴ except for changes in the values of the asymmetric stretching frequencies in the ground and excited states, which are corrected for the effects of deuteration, and for an adjustment to the value of the parameter used to allow for the quenching of orbital angular momentum, g_K . In our treatment of the Renner-Teller coupling we have considered the quenching of the orbital angular momentum as the molecule bends from the linear configuration. Following Jungen and Merer²⁰ we write the following expression for the electronic angular momentum coupling (an electronic Coriolis interaction) between the \tilde{A}^2A_1 and the \tilde{X}^2B_1 states:

$$\hbar^{-1} \langle {}^e A_1 | L_z | {}^e B_1 \rangle = \zeta_e^z \equiv \Lambda(\rho) = \Lambda - u(\rho) \quad (1)$$

In equation (1) $u(\rho)$ as a positive quantity, so that if it is non-zero its increase with increasing bending angle supplement, ρ , represent a quenching of angular momentum with departure from linearity. The function $g_K(\rho)$ was then defined²⁰ as

$$g_K(\rho) = 2A(\rho)u(\rho) = g_K^0 + g_K^2\rho^2 + \dots \quad (2)$$

where $A(\rho)$ is the angular dependent a-axis rotation constant, whose value tends to infinity as $\rho \rightarrow 0$. Hence, although $u(\rho)$ is isotopically independent, the value of g_K^0 is isotopically dependent, since the value of $A(\rho)$ for ND_2 will be smaller than that of NH_2 by a factor of ~ 0.56 ³¹. This correction has been made to the value of g_K to ensure isotopic invariance of the angular momentum quenching.

In Table 6 we show the values of the vibronic origins and effective spin-orbit coupling parameters, $A_{v_2,K}^{SO}$ of the vibronic levels observed in the original measurements by Dressler and Ramsay⁵, and in Table 7 the vibronic origins and $A_{v_2,K}^{SO}$ values for the high angular momentum states analysed in this work. It may be seen that the stretch-bender model using the NH_2 potential parameters gives a good representation of the vibronic structure of the ND_2 spectrum, and allows the results of the spectral analysis to be confirmed. The values of $A_{v_2,K}^{SO}$ in most of the excited state energy levels listed by Dressler and Ramsay⁵ are very small, owing to the complicated mixing associated with strong Fermi resonance coupling as discussed by Alijah and Duxbury for NH_2 ³²⁻³⁴. However the predicted behaviour of the splitting of levels with $K'=1$ is well reproduced by the current calculations, including the prediction of whether the excited state levels are regular, $T_{N+1/2} > T_{N-1/2}$, or inverted,

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$T_{N+\frac{1}{2}} < T_{N-\frac{1}{2}}$. Since the splitting in the lowest vibrational levels of the \tilde{X}^2B_1 state is known to be inverted, the sign of the splitting in excited state levels may be inferred if the excited state term values are derived from two transition terminating in ground state levels with very different spin-rotation splittings. The term values derived by Dressler and Ramsay had taken this into account⁵, but there is no comment about it within their paper. The portion of the spectrum of the 2_0^5 band (in the linear molecule labelling used by Dressler and Ramsay the excited state has $v_2=12$) shown in their paper shows clearly the spin-splittings in the Π sub-band. It is the excited state levels of this transition which have an inverted spin-orbit splitting.

This behaviour contrasts with that of the spin-orbit splitting of the high angular momentum states of the transitions from the $v_2=0$ and 1 states of \tilde{A}^2A_1 where the splitting is large and regular, as shown in Tables 2 and 7. It may be seen that the calculated values of the rotational dependence of the spin-orbit splittings presented in Table 2, which use the parameters derived from the least squares fitting by Alijah and Duxbury of the NH_2 spectrum^{33,34}, give a very good fit to the observed rotational variation of the spin-orbit splittings of the observed ND_2 term values.

The small systematic shifts of the origin between the observed and calculated positions of the vibronic origins are probably due in part to the omission of some of the effects of the changes in zero point motion between the hydride and the deuteride. For the high angular momentum states the differences may also reflect the effects of the parameterisation of the bond stretching in the stretch-bender model, since the shape of the effective K-dependent bending potential energy curves discussed by Duxbury and Alijah³²⁻³⁴ is very dependent upon the effective bond length used to

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2
3 calculate $A(\rho)$, the angular dependent a-axis rotation constant. The variation of this
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6 effective potential with K is shown in Figure 8 of Ref. [34].
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10 11 12 13 **Conclusion**

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17 We have demonstrated that, even in the absence of ab-initio calculations, the type of
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19 effective Hamiltonian represented by the stretch-bender, with Renner-Teller and spin-
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21 orbit coupling included, allows us to make connections between sets of experimental
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23 data recorded under very different conditions, and having almost no energy levels in
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25 common. As Peric and Peyerimhoff¹¹ have noted, both the stretch-bender
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27 Hamiltonian^{31,32} and the MORBID Hamiltonian¹⁴ of Jensen and Bunker, may give
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29 results which approach those of their “benchmark” goal. Most spectroscopic analysis
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31 has made use of some type of effective Hamiltonian to derive molecular information
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33 directly from the experimental spectrum. In studies of diatomic molecules much of
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35 the effort that has been made to derive as much information as possible directly from
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37 a spectrum has been described in detail by Lefebvre-Brion and Field³⁷.
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51 Even with the use of theoretical approaches of the type described by Jungen and
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53 Merer²⁰, and by Dixon and Duxbury^{19,23} and their collaborators, a direct attack on a
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55 spectrum requires high quality experimental data. The present analysis has certainly
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57 benefited from the availability of high quality spectroscopic information on the 0,0,0
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59 and 0,1,0 levels of the ground \tilde{X}^2B_1 state, which have allowed us to derive the term
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values of rotational levels in the zero-point level excited \tilde{A}^2A_1 state having $K_a = 6,7,8$

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3 and 9. These levels have in turn been used to derive term values for rotational levels
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5 of the vibrational levels in the \tilde{X}^2B_1 state having values of v_2 from 2 to 6.
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10 However the fact that only a limited number of vibronic states were accessed in the
11 present series of experiments demonstrates a major problem in inverting the
12 experimental spectra of polyatomic molecules to derive potential energy surfaces.
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16 The limitations on the states accessed are due to both the method of production of free
17 radicals or radical ions, and also to the selectivity about which parts of the potential
18 energy surface are explored due to the Franck-Condon factors. The major influence
19 of the Franck-Condon principle on selectivity is exemplified by the electronic spectra
20 of NH_2 and ND_2 , where there is a great deal of information about bending but little
21 about stretching, as there is very little change in bond-length on electronic excitation.
22 This means that in general only a limited amount of experimental information about
23 potential energy surfaces is available from the analysis of the spectra of polyatomic
24 molecules, even those like ND_2 having only one atom more than a diatomic molecule.
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52 computer code used here.
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Table 1

Assignments of the emission spectra of ND₂ recorded in time gated mode following the photo-dissociation of ND₃. The sub branches are aligned so that transitions from lower state levels to a common upper state level are paired. The K values of the common upper state levels are indicated. The vibrational transitions are indicated using the notation (vibration number)_{v''}.

P branches			Vibrational Transition	R branches		
F ₁	F ₂		2 ₀ ¹	F ₁	F ₂	
13691.91	13682.06	P 8,8	K' = 7	14061.85	14052.22	R 6,6
13666.67	13657.78	P 9,8		14058.89	14050.32	R 7,6
13640.00	13632.70	P 10,8		14054.07	14046.67	R 8,6
13390.74	13379.26	P 7,7	K' = 6	13712.59	13701.48	R 5,5
13366.30	13357.78	P 8,7		13710.00	13701.48	R 5,5
13341.11	13333.7	P 9,7		13706.32	13699.63	R 5,5
13093.70	13084.63	P 6,6	K' = 5	13365.42	13356.85	R 4,4
			2 ₀ ⁰			
12983.71	12976.91	P 10,10	K' = 9	13446.37	13439.78	R 8,8
12956.16	12948.73	P 11,10		13440.74	13434.07	R 9,8
12925.56	12918.89	P 12,10		13432.59	13425.93	R 9,8
12707.63	12699.02	P 9,9	K' = 8	13124.46	13116.24	R 7,7
12679.84	12672.02	P 10,9		13118.98	13111.55	R 8,7
12649.71	12643.44	P 11,9		13110.96	13104.67	R 9,7
12432.68	12424.46	P 8,8	K' = 7	12802.94	12794.32	R 6,6
12406.26	12399.22	P 9,8		12798.24	12791.19	R 7,6
12378.67	12372.21	P 10,8		12792.68	12786.5	R 8,6

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4							
5	12164.19	12156.75	P 7,7	$K' = 6$	12486.11	12478.47	R 5,5
6							
7				2_1^1			
8	12534.83	12524.67	P 8,8	$K' = 7$	12924.12	12914.23	R 6,6
9							
10	12509.50	12500.50	P 9,8		12920.82	12912.37	R 7,6
11							
12							
13							
14	12243.7	12232.22	P 7,7	$K' = 6$	12582.96	12571.76	R 5,5
15							
16	12218.89	12210.37	P 8,7		12580.28	12572.04	R 5,5
17							
18	12193.33	12185.93	P 9,7		12576.67	12569.63	R 5,5
19							
20							
21							
22	11955.73	11945.83	P 7,7	$K' = 5$	12244.04	12234.08	R 4,4
23							
24				2_1^0			
25							
26	11805.15	11798.04	P 10,10	$K' = 9$	12289.24	12283.56	R 8,8
27							
28	11777.01	11769.90	P 11,10		12282.39	12276.32	R 9,8
29							
30							
31	11746.08	11739.28	P 12,10		12274.76	12268.10	R 10,8
32							
33							
34	11539.92	11531.31	P 9,9	$K' = 8$	11977.69	11969.08	R 7,7
35							
36	11511.86	11504.12	P 10,9		11971.43	11963.99	R 8,7
37							
38	11481.55	11474.74	P 11,9		11968.74	11963.48	R 9,7
39							
40							
41							
42	11276.29	11267.63	P 8,8	$K' = 7$	11664.77	11656.56	R 6,6
43							
44	11248.87	11241.65	P 9,8		11660.47	11653.42	R 7,6
45							
46	11221.44	11214.23	p 10,8		11654.63	11648.34	R 8,6
47							
48							
49							
50	11017.19	11009.43	P 7,7	$K' = 6$	11356.36	11348.92	R 5,5
51							
52	10993.25	10985.8	P 8,7		11354.4	11347.55	R 6,5
53							
54	10966.24	10959.98	P 9,7		11349.71	11343.64	R 7,5
55							
56	10936.89	10931.41	P 10,7				
57							
58							
59				2_2^1			
60							

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2							
3							
4							
5	11396.96	11386.52	P 8,8	K' = 7	11802.89	11792.89	R 6,6
6							
7	11371.78	11362.74	P 9,8		11799.67	11790.89	R 7,6
8							
9	11344.81	11337.41	P 10,8		11794.54	11787.15	R 8,6
10							
11	11113.80	11102.12	P 7,7	K' = 6	11470.33	11458.94	R 5,5
12							
13	11089.00	11080.33	P 8,7		11467.61	11459.33	R 6,5
14							
15	1063.36	11055.90	P 9,7				
16							
17							
18							
19	10834.63	10825.37	P 6,6	K' = 5	11138.11	11129.08	R 4,4
20							
21							
22				2_2^0			
23							
24							
25	10663.33	10656.30	P 10,10	K' = 9	11151.11	11144.44	R 8,8
26							
27	10636.11	10628.70	P10,9		11145.93	11138.52	R 9,8
28							
29	10605.93	10598.89	P10,9		11137.41	11130.74	R 9,8
30							
31							
32							
33	10399.57	10391.12	P 9,9	K' = 8	10847.47	10838.96	R 7,7
34							
35	10373.50	10366.22	P10,9		10841.55	10833.79	R 8,7
36							
37					10825.31	10819.14	R 9,7
38							
39					10811.11	10605.64	R 10,7
40							
41							
42							
43	10137.52	10129.02	P 8,8	K' = 7	10543.64	10535.23	R 6,6
44							
45	10111.65	10103.88	P 9,8		10539.53	10532.09	R 7,6
46							
47	10083.55	10076.62	P 10,8		10533.46	10526.81	R 8,6
48							
49	10054.43	10048.87	P 11,8		10525.64	18519.96	R 9,6
50							
51							
52							
53	9887.43	9879.30	P 7,7	K' = 6	10243.81	10236.04	R 5,5
54							
55	9863.12	9855.73	P 8,7		10241.04	10234.25	R 6,5
56							
57	9836.41	9829.76	P 9,7				
58							
59							
60							

				2_3^0			
7	9258.97	9250.09	P 9,9	K' = 8	9729.20	9720.15	R 7,7
9	9282.35	9224.21	P 10,9		9723.29	9715.16	R 8,7
13	9009.34	9000.09	P 8,8	K' = 7	9435.68	9426.80	R 6,6
15	8982.72	8974.95	P 9,8		9431.24	9423.11	R 7,6
17	8955.27	8947.87	P 10,8		9425.33	9418.67	R 8,6
19	8925.69	8919.78	P 11,8		9417.19	9411.28	R 9,6
23	8768.95	8760.81	P 7,7	K' = 6	9145.84	9137.71	R 5,5
25	8744.55	8737.15	P 8,7			9135.68	R 6,5
27	8717.19	8711.28	P 9,7		9151.02	9142.88	R 7,5
29	8688.36	8682.44	P 10,7				
				2_4^0			
35	8133.09	8123.48	P 9,9	K' = 8	8621.81	8612.94	R 7,7
37	8104.99	8096.86	P 10,9		8615.90	8607.76	R 8,7
39	8076.16	8068.02	P 11,9		8632.16	8625.51	R 9,7
43	7891.31	7882.44	P 8,8	K' = 7	8339.37	8330.50	R 6,6
45	7865.43	7857.30	P 9,8		8334.94	8326.80	R 7,6
47	7837.99	7830.59	P 10,8		8321.63	8314.97	R 8,6
49	7808.50	7802.59	P 11,8				
53	7661.37	7652.50	P 7,7	K' = 6	8060.63	8052.50	R 5,5
55	7636.97	7629.58	P 8,7		8076.16	8068.02	R 6,5
57	7610.35	7603.70	P 9,7				
				2_5^0			

7014.60	7005.29	P 9,9	K' = 8	7524.03	7514.42	R 7,7
6987.04	6979.02	P 10,9		7518.12	7509.61	R 8,7
6782.99	6772.83	P 8,8	K' = 7	7254.34	7244.18	R 6,6
6757.12	6748.80	P 9,8		7241.41		R 7,6
6729.39	6722.00	P10,8				
6700.74	6694.27	P 11,8				
6563.77	6554.71	P 7,7	K' = 6	6987.69	6979.15	R 5,5
6539.37	6531.42	P 8,7		6985.62	6977.86	R 6,5
			206			
			2_6^0			
5906.84	5897.97	P 9,9	K' = 8	6434.75	6424.40	R 7,7
5880.22	5871.35	P 10,9				
5682.81	5672.83	P 8,8	K' = 7	6178.56	6168.21	R 6,6
5656.19	5648.43	P 9,8		6174.68	6160.44	R 7,6
5474.31	5465.43	P 7,7	K' = 6			
5456.56	5445.47	P 8,7				
			2_7^0			
			K' = 8	5337.15		R 7,7

Table 2

Experimentally determined and calculated term values (in cm^{-1}) for ND_2 (\tilde{A}^2A_1), $v_2' = 0$ and 1 vibrational states. The first entry of a pair refers to the F_1 level and the second to the F_2 level. The parameters used for the calculation are given in Table 5, and the calculated effective spin-orbit constants in Table 7.

v_2'	K_a	$v_2' = 0$			$v_2' = 1$			$v_2' = 2$			
		obs.	calc.	o-c.	obs.	calc.	o-c.	obs.	calc.	o-c.	
0	6	12843.03	12765.45	77.6	12907.02	12830.2	76.8	12979.64	12902.6	77.2	
		12836.50	12759.82	76.7	12901.06	12824.5	76.5	12974.27	12897.6	76.7	
	7	13308.47	13229.86	78.6	13380.99	13303.1	77.9	13463.38	13386.3	77.1	
		13301.16	13222.67	78.5	13374.89	13296.6	78.3	13457.94	13382.9	75.0	
	8	13803.41	13719.28	84.1	13885.78			13976.65			
		13796.15	13712.08	84.1	13879.23			13971.51			
	9	14322.0	14235.75	86.3	14415.7			14517.2			
		14316.6	14228.66	87.9	14409.6			14511.7			
	1	5	13599.3	13556.8	42.7						
			13591.8	13533.8	38.0						
		6	14069.50	14013.52	56.0	14132.99	14078.2	54.8	14206.73	14151.7	55.0
			14059.32	14004.24	55.1	14125.57	14070.3	55.3	14200.23	14145.5	54.8
7		14567.59	14506.41	61.2	14641.28	14580.4	60.8	14724.8	14665.0	59.8	
		14558.46	14497.37	61.1	14633.73	14572.6	61.1	14718.3	14658.5	59.8	

Table 3

Term values (in cm^{-1}) with high values of K_a for the 0,0,0 and 0,1,0 vibrational levels of the $\tilde{X},^2B_1$ state of ND₂. For the 0,0,0 vibrational state, the levels with values of $K_a = 4$ are taken from Muenchausen et. al.³⁵, with those of higher values of K_a being derived from the rotational transitions measured by Morino and Kawaguchi³⁶. All the term values of the 0,1,0 vibrational state are taken from Muenchausen et. al.³⁵. In both cases we have averaged the small asymmetry splittings to derive effective symmetric top levels, since the asymmetry splittings of the transitions cannot be resolved at the resolution of the laser induced fluorescence spectra, 0.2 cm^{-1} .

$v_2'' = 0$								
N, K_a								
$N''=K_a''$		$N''=K_a''+1$		$N''=K_a''+2$		$N''=K_a''+3$		
4,4	233.755	5,4	288.659	6,4	354.894	7,4	432.486	
	234.320		289.178		355.354		432.905	
5,5	357.219	6,5	423.109	7,5	500.183	8,5	588.481	
	357.937		423.776		500.782		589.032	
6,6	505.800	7,6	582.683	8,6	670.682	9,6	769.796	
	506.665		583.493		671.420		770.479	
7,7	678.890	8,7	766.799	9,7	865.763	10,7	975.754	
	679.894		767.747		866.637		976.568	
8,8	875.775	9,8	974.789	10,8	1084.754	11,8	1205.665	
	876.957		975.869		1085.756		1206.604	
9,9	1095.841	10,9	1205.946	11,9	1326.942	12,9	1458.804	
	1097.147		1207.151		1328.068		1459.865	
10,10	1338.310	10,10	1459.537	12,10	1591.591			
	1339.731		1460.859		1592.833			

$v_2'' = 1$

$N''=K_a''$		$N''=K_a''+1$		$N''=K_a''+2$		$N''=K_a''+3$	
4,4	1356.079 1356.806	5,4	1411.139 1411.759	6,4	1477.436 1477.978	7,4	1555.115 1555.606
5,5	1486.672 1487.578	6,5	1552.625 1553.515	7,5	1629.928 1630.635	8,5	1718.359 1719.004
6,6	1643.436 1644.510	7,6	1720.533 1721.488	8,6	1808.717 1809.583	9,6	1908.026 1908.824

Table 4

Experimentally determined term values (in cm^{-1}) for ND_2 for the higher vibrational levels of \tilde{X}^2B_1 . These were determined using the differences between the wavenumbers of the emission lines of ND_2 and those of the new term values of the \tilde{A}^2A_1 state given in Table 2. The precision of new excited state term values relies in turn on the use of the ground state term values given in Table 3, in combination with the fluorescence spectra terminating in levels with $v_2''=0$ and 1, which are given in Table 1. The first entry of a pair refers to F_1 and the second to F_2 .

$v_2 = 1$			
N, K_a $K \equiv K_a$	$N'' = K''$	$N'' = K'' + 1$	$N'' = K'' + 2$
7,7	1825.8	1914.1	2013.4
	1827.1	1915.2	2014.3
8,8	2032.8	2131.7	2242.3
	2033.5	2133.1	2243.5
9,9	2263.5	2373.9	2495.1
	2264.8	2375.1	2496.8
10,10	2516.9	2638.7	
	2518.6	2639.7	
$v_2 = 2$			
5,5	2599.2	2666.0	2746.0
	2600.5	2666.8	
6,6	2764.8	2841.5	2929.9
	2765.9	2842.8	2931.1
7,7	2955.9	3044.2	3151.3
	2957.2	3045.4	3152.4
8,8	3183.7	3280.1	
	3185.0	3280.1	

		$v_2 = 3$		
5,5	3697.2			3828.6
	3698.8	3765.4		3831.4
6,6	3872.8	3949.8		4038.1
	3874.4	3951.8		4039.3
7,7	4074.2	4162.5		
	4066.8	4164.1		
8,8	4299.1	4398.3		4508.1
	4301.1	4399.9		4510.1
9,9	4544.4	4603.4		
	4546.1	4655.0		
		$v_2 = 4$		
5,5	4782.4	4830.9		4941.5
	4784.0	4833.0		
6,6	4969.1	5046.1		5141.8
	4970.7	5048.1		5143.0
7,7	5181.6	5269.9		5344.5
	5183.2	5271.5		5346.0
8,8	5417.2	5515.6		5625.4
	5418.7	5517.6		5627.3
9,9	5670.3	5780.8		5900.5
	5672.7	5782.4		5903.5
		$v_2 = 5$		
5,5	5909.4	6001.1		6022.5

	5913.0	6003.5	
6,6	6054.1 6057.0	6139.6	6254.8
7,7	6279.4 6281.7	6367.7 6369.6	
8,8	6525.5 6528.3	6623.9 6626.1	6734.0 6735.9
9,9	6788.4 6790.4	6898.5 6900.3	
	$v_2 = 6$		
6,6	7129.9 7133.0	7206.3 7214.4	
7,7	7368.7 7371.8		
8,8	7625.7 7628.3	7724.8 7726.5	
9,9	7896.6 7898.2	8005.6 8007.9	

Table 5

Parameters used to model the rotational structure of the \tilde{X}^2B_1 and \tilde{A}^2A_1 states of ND_2 and the Renner-Teller coupling between them. Most of the parameters are identical to those used to calculate the spectrum of NH_2 (refs. 33 and 34). The parameters which differ from those used for NH_2 , are those in which the parameter used for NH_2 was not isotopically independent. The parameters which required to be changed are the asymmetric stretching frequencies ω_3 for the \tilde{A}^2A_1 and the \tilde{X}^2B_1 states, and the value of the parameter for the variation of $\langle L_z \rangle$, g_K .

\tilde{A}^2A_1 state			
Bond length variation			
$r(\rho=0)$			0.996 Å
a , coefficient of ρ^2			0.000 Å
b , coefficient of $\tan^2 \rho$			0.1063 Å
f_0	13249.59±160	$\text{cm}^{-1}\text{rad}^{-2}$	
m	35.814	deg	
H	729.9	cm^{-1}	
k_4	-0.35±50		$\text{cm}^{-1}\text{rad}^{-4}$
c_1	-53.01±5		cm^{-1}
f_{rr}^s	8.9093	aJ Å ²	
x_1	-0.0025		
ω_3	2536.7	cm^{-1}	
x_3	-0.0033		
δ_{11}	17.07	cm^{-1}	
δ_{21}	0.00	cm^{-1}	
δk_{41}	131.94 ±130	$\text{cm}^{-1}\text{rad}^{-4}$	
\tilde{X}^2B_1 state			
Bond length variation			
$r(\rho=0)$			0.996 Å
a , coefficient of ρ^2			0.0146 Å
b , coefficient of $\tan^2 \rho$			0.0185 Å
f_0	33596.53±130	$\text{cm}^{-1}\text{rad}^{-2}$	
m	77.6	deg	
H	11773.67	cm^{-1}	
k_4	374.1±40		$\text{cm}^{-1}\text{rad}^{-4}$
c_1	154.22 ±40	cm^{-1}	
f_{rr}^s	8.3955	aJ Å ²	
x_1	-0.01440		
ω_3	2391.1	cm^{-1}	
x_3	-0.0093		
δ_{11}	505.55 ±100	cm^{-1}	
δ_{21}	-781.93±250	cm^{-1}	
δk_{41}	765.98±400	$\text{cm}^{-1}\text{rad}^{-4}$	
δk_{42}	-793.14±300	$\text{cm}^{-1}\text{rad}^{-4}$	

Spin-orbit coupling parameter , A^{SO}	61.6	cm^{-1}
Variation of $\langle L_z \rangle$, g_K	3.36	cm^{-1}

The errors on the parameters were those derived from the final least squares fitting of the NH_2 spectrum.

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Table 6

Observed and calculated molecular parameters (in cm^{-1}) for the vibronic levels of the \tilde{X}^2B_1 and the \tilde{A}^2A_1 states of ND_2 which were analysed by Dressler and Ramsay (D&R)⁵. The average vibronic origins are denoted by T, and the vibronic spin orbit coupling constant by $A_{v,K}^{SO}$. $A_{v,K}^{SO}$ is identically zero for levels having $K=0$. Since the stretch-bender model incorporates the effects of Fermi resonance, these may be observed for some of the higher vibrational levels of ND_2 , and are indicated by the inclusion of ν_1 .

State		\tilde{X}^2B_1			\tilde{A}^2A_1				
					calc.	obs.			
ν_1, ν_2, ν_3	$K=0$	$A_{v,K}^{SO}$	ν_1, ν_2, ν_3	ν_1, ν_2, ν_3	$A_{v,K}^{SO}$	$A_{v,K}^{SO}$	T', D&R	obs.- calc.	
\tilde{X}^2B_1			\tilde{X}^2B_1	\tilde{A}^2A_1					
(0, 0, 0)		0		(0, 0, 0)	11000.9				
(0, 1, 0)	1109.73			(0, 1, 0)	11785.5				
(0, 2, 0)	2200.37			(0, 2, 0)	12688.5				
(1, 0, 0)	2365.29			(0, 3, 0)	13702.8				
(0, 3, 0)	3271.93			(0, 4, 0)	14810.0		14844.28	34.3	
(1, 1, 0)	3470.53			(0, 5, 0)	15993.9		16014.42	20.5	
(0, 4, 0)	4323.91			(0, 6, 0)	17227.7		17224.44	-3.3	
(1, 2, 0)	4559.64			(1, 4, 0)	17283.5		17361	77.5	
(0, 5, 0)	5355.23			(0, 7, 0)	18557.7		18588.41	30.71	
(0, 6, 0)	6364.22			(0, 8, 0)	19898.5		19924.77	26.27	
K=1									
(0, 0, 0)	13.16	-0.146		(0, 0, 0)	11127.6	5.34			
(0, 1, 0)	1123.72	-0.179	(0,12, 0)		11595.3	-16.06			
(0, 2, 0)	2215.36	-0.225		(0, 1, 0)	12055.2	8.47			
(0, 3, 0)	3288.14	-0.289	(0,13, 0)		12376.4	-14.95			
(0, 4, 0)	4341.70	-0.382		(0, 2, 0)	13053.5	12.48			
(0, 5, 0)	5375.01	-0.524	(0,14, 0)		13256.8	-15.83			
(0, 6, 0)	6386.62	-0.752		(0, 3, 0)	14103.6	6.11			
			(0,15, 0)		14254.5	-14.81			
			(0,16, 0)		15107.2	5.76			
				(0, 4, 0)	15373.4	-6.42	(b)	15399.7	26.3
			(0,17, 0)		16125.1	1.61			
				(0, 5, 0)	16585.0	-1.39	-1.8	16600.3	15.3
			(0,18, 0)		17162.9	-1.17			
				(0, 6, 0)	17882.7	-0.90	2.4	17944.4	61.7
K=2									
			(0,11, 0)		11126.2	-12.98			

1										
2										
3										
4	(0, 0, 0)	52.57	-0.290	(0, 0, 0)	11338.1	5.47				
5	(0, 1, 0)	1165.59	-0.356	(0,12, 0)	11946.5	-13.21				
6	(0, 2, 0)	2260.20	-0.444	(0, 1, 0)	12356.9	9.18				
7	(0, 3, 0)	3336.66	-0.569	(0,13, 0)	12819.8	-13.79				
8	(0, 4, 0)	4394.75	-0.747	(0, 2, 0)	13425.5	12.52				
9	(0, 5, 0)	5433.84	-1.012	(0,14, 0)	13752.5	-14.65				
10	(0, 6, 0)	6452.95	-1.428	(0, 3, 0)	14522.5	12.90				
11				(0,15, 0)	14772.0	-11.42				
12				(0,16, 0)	15581.7	6.73				
13				(0, 4, 0)	15920.5	-6.36	c	15936.1	15.6	
14				(0,17, 0)	166201	9.81				
15				(0, 5, 0)	17147.2	-1.79	c	17141.1	-6.1	
16				(0,18, 0)	18216.0	5.00				
17				(0, 6, 0)	18469.1	3.12	d	18485.6	16.5	
18				(0,20,0) ^a	(0, 7, 0)	19759.0	9.36			
19				(0,20,0) ^a	(0, 7, 0)	19895.9	-11.00	d	19857.5	-38.4
20										
21										
22										
23										
24		K=3								
25	(0, 0, 0)	118.04	-0.431	(0, 0, 0)	11613.1	6.37				
26	(0, 1, 0)	1235.06	-0.527	(0,12, 0)	12297.2	-12.34				
27	(0, 2, 0)	2334.50	-0.654	(0, 1, 0)	12705.2	9.99				
28	(0, 3, 0)	3416.83	-0.831	(0,13, 0)	13231.0	-13.69				
29	(0, 4, 0)	4482.14	-1.08	(0, 2, 0)	13848.0	6.12				
30	(0, 5, 0)	5530.26	-1.441	(0,14, 0)	14213.9	-15.29				
31	(0, 6, 0)	6560.82	-1.983	(0, 3, 0)	14972.1	12.65				
32				(0,15, 0)	15274.2	-13.59				
33				(0,16, 0)	16067.8	4.75				
34				(0, 4, 0)	16450.8	-4.63				
35				(0,17, 0)	17139.2	-0.70				
36				(0, 5, 0)	17748.3	-3.18				
37								17838	89.666	

- a, Strong calculated resonant interaction between the two nearly degenerate states, ${}^2B_1 v_2 = 20$ and ${}^2A_1 v_2 = 7$, leads to the predicted 50:50 mixing.
- b Perturbed
- c Unresolved splitting
- d Inverted splitting, small.

Table 7

Observed and calculated molecular parameters (in cm^{-1}) for the vibronic levels of the \tilde{X}^2B_1 and the \tilde{A}^2A_1 states of ND_2 which are measured in the high angular momentum emission spectrum. The average vibronic origins are denoted by T, and the vibronic spin orbit coupling constant by $A_{v,K}^{SO}$.

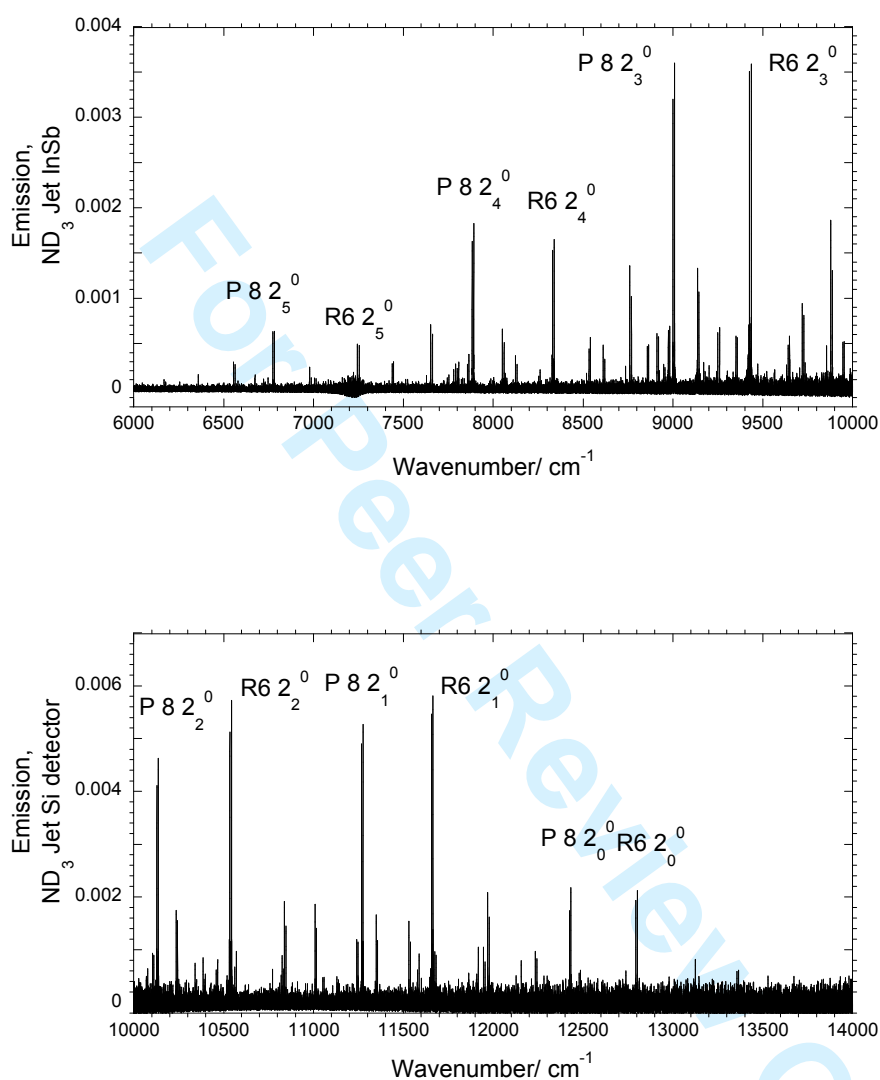
State (v_1, v_2, v_3) \tilde{X}^2B_1	\tilde{X}^2B_1		\tilde{A}^2A_1		T'	$A_{v,K}^{SO}$	T' obs.	obs- calc	\bar{B}^a obs	\bar{B}^a calc
	$K = K_a$	$A_{v,K}^{SO}$	(v_1, v_2, v_3) \tilde{X}^2B_1	(v_1, v_2, v_3) \tilde{A}^2A_1						
	K=5		(0,11,0)		12028.5	-9.91				
(0,0,0)	325.82	-0.70	(0,0,0)		12320.5	7.67				
(0,1,0)	1454.95	-0.85	(0,12,0)		13031.8	-11.26				
					13524.0					
(0,2,0)	2568.73	-1.04	(0,13,0)			10.26				
(0,3,0)	3668.20	-1.29			14052.0	-12.56				
(0,4,0)	4754.11	-1.63								
(0,5,0)	5827.13	-2.09	(0,2,0)		14738.8	-12.03				
(0,6,0)	6887.95	-2.72								
	K=6		(0,11,0)		12374.5	-9.24				
(0,0,0)	467.28	-0.82	(0,0,0)		12740.6	7.79	12812.2	71.6	4.59	4.63
(0,1,0)	1604.17	-0.99	(0,12,0)		13414.5	-10.52				
(0,2,0)	2726.98	-1.20	(0,1,0)		13984.1	10.20	14008.9	24.8	4.65	4.66
(0,3,0)	3837.01	-1.48	(0,13,0)		14467.5	-11.66				
(0,4,0)	4935.31	-1.84	(0,2,0)		15238.2	10.93				
(0,5,0)	6022.82	-2.32								
(0,6,0)	7100.53	-2.95								
	K=7		(0,11,0)		12736.7	-8.58				
(0,0,0)	633.04	-0.94	(0,0,0)		13194.8	7.81	13272.8	78.0	4.57	4.67
(0,1,0)	1778.56	-1.12	(0,12,0)		13807.2	-9.75				
(0,2,0)	2911.28	-1.35	(0,1,0)		14472.9	9.83	14534.0	61.1	4.66	4.7
(0,3,0)	4032.77	-1.64	(0,13,0)		14888.3	-10.72				
(0,4,0)	5144.25	-2.01	(0,2,0)		15753.4	9.46				
(0,5,0)	6246.86	-2.49								
(0,6,0)	7341.74	-3.10								

K=8										
			(0,11, 0)		13113.8	-7.95				
(0, 0, 0)	822.46	-1.05		(0, 0, 0)	13679.7	768	13763.0	85.8	4.6	4.71
(0, 1, 0)	1977.32	-1.25	(0,12, 0)		14202.9	-8.98				
(0, 2, 0)	3120.58	-1.48		(0, 1, 0)	14987.0	9.30				
(0, 3, 0)	4354.08	-1.78	(0,13, 0)		15315.3	-9.68				
(0, 4, 0)	5379.17	-2.15		(0, 2, 0)	16282.3	5.83				
(0, 5, 0)	6497.08	-2.62								
(0, 6, 0)	7608.99	-3.20								
K=9										
(0, 0, 0)	1034.90	-1.16		(0, 0, 0)	14191.5	7.49	14277.3	85.0	4.67	4.73
(0, 1, 0)	2199.62	-1.36	(0,12, 0)		14621.1	-8.10				
(0, 2, 0)	3353.72	-1.60		(0, 1, 0)	15523.1	8.58				
(0, 3, 0)	4499.53	-1.89	(0,13,0)		15747.1	-8.28				
(0, 4, 0)	5638.36	-2.26	(0,14,0)		16802.6	-1.41				
(0, 5, 0)	6771.43	-2.71		(0, 2, 0)	16989.7	-1.77				
(0, 6, 0)	7899.90	-3.25								
K=10										
			(0,11, 0)		14202.1	-7.6				
(0, 0, 0)	1272.36	-1.26		(0, 0, 0)	14721.99	7.19				
(0, 1, 0)	2454.77	-1.48	(0,12, 0)		15390.62	-8.46				
(0, 2, 0)	3632.17	-1.75		(0, 1, 0)	16083.47	8.55				
(0, 3, 0)	4805.86	-2.07	(0,13, 0)		16587.71	-9.26				
(0, 4, 0)	5977.09	-2.47		(0, 2, 0)	17475.51	9.59				
(0, 5, 0)	7147.11	-2.94	(0,14, 0)		17801.63	-9.69				
(0, 6, 0)	8317.12	-3.5								

a $\bar{B} = \frac{1}{2}(B + C)$

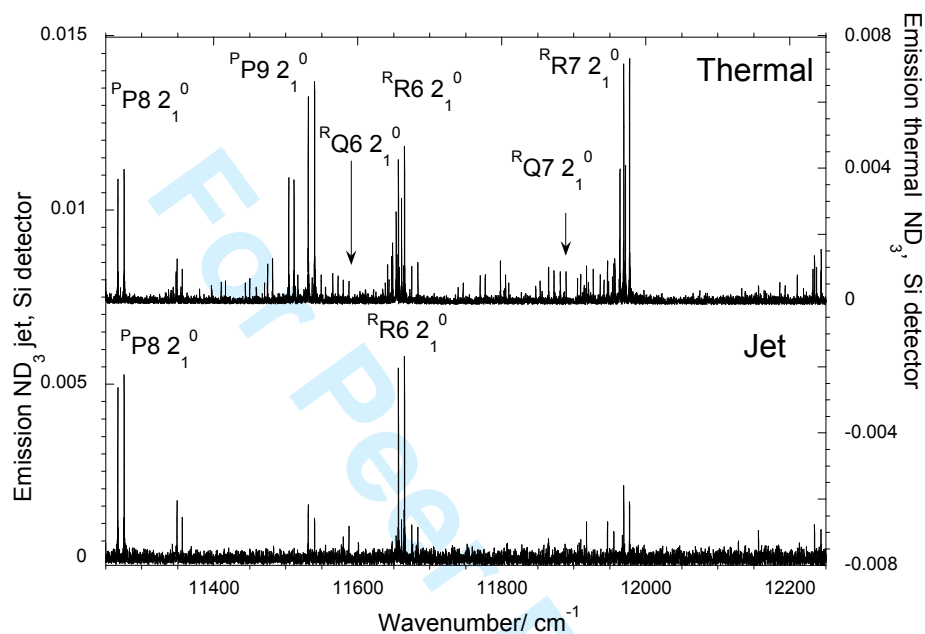
Figures and Figure Captions

Figure 1



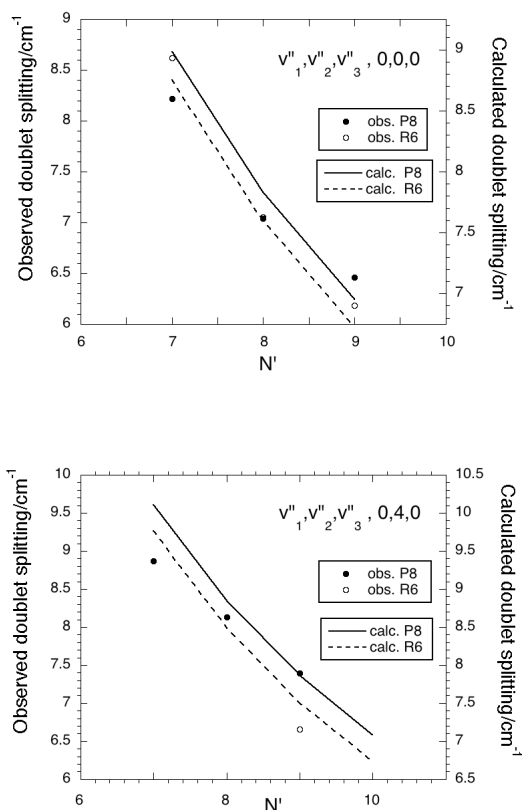
A survey of the entire product emission spectrum of $\text{ND}_2(\tilde{A}^2A_1)$ from the photodissociation of jet cooled ND_3 . 1(a) 6000-10,000 cm^{-1} , InSb detector: 1(b) 10,000 to 14,000 cm^{-1} , a Si avalanche detector. This spectrum is dominated by the strong $^R\text{R6}$ and $^P\text{P8}$ transitions with $N=K$, resulting from the production of ND_2 in the 0,0,0 level of the \tilde{A}^2A_1 state predominantly with $K_a=7$.

Figure 2



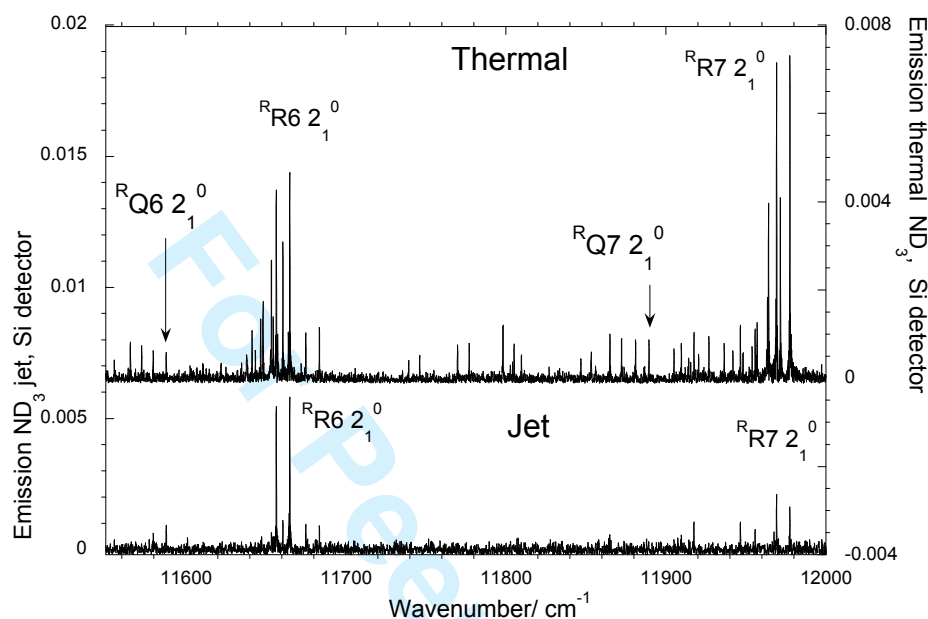
An expanded section of the spectrum showing the doublet structure of the transitions, and also demonstrating the more complex patterns seen $^R R$ and $^P P$ branches in the spectra produced from the photodissociation of room temperature ND_3 . In this spectrum the strongly degraded structure of the $^P P$ branches contrasts with the compact structure of the $^R R$ branches.

Figure 3



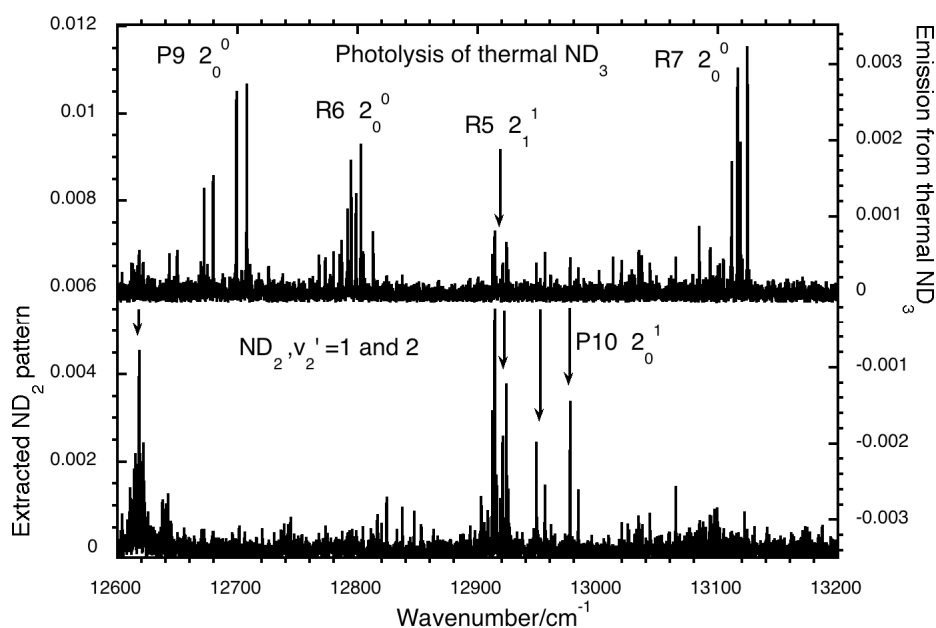
Plots of the effects of spin uncoupling on the separation of the F₁-F₂ doublets of the ^RR6 and ^PP8 transitions in (a) the 2₀⁰ and (b) the 2₄⁰ bands. The experimental splitting is compared with that calculated using the stretch-bender Renner-Teller Hamiltonian^{31,32} using the same parameters as for NH₂, see Table 5. It may be seen that the doublet splittings are significantly greater when v₂^{''} is increased from 0 to 4, but the errors in the experimental measurements are larger than the calculated increase in the splitting from ^RR to ^PP components of transitions sharing a pair of F₁ and F₂ with the same values of N' and K_a'.

Figure 4



An expanded section of the spectrum shown in Figure 2. The RQ7 and RQ6 transitions are located on the red side of the equivalent RR7 and RR6 branches. Although these Q branches are weak and difficult to detect in the jet cooled spectrum, near the band centre when $K_a' = 0$ and 1, the line strength of the RQ and equivalent P Q branches is much greater than that of the RR and PP transitions. However it has been difficult to find evidence for the occurrence of these branches with $K_a' = 0$ and 1 in the emission spectrum of ND_2 obtained from the photodissociation of ND_3 .

Figure 5



A comparison of the spectrum produced from the photodissociation of room temperature ND₃ with an “extracted” spectrum of emission from ND₂ (\tilde{A}^2A_1) in which only the $v_2' = 1$ and 2 states are populated. This method of extracting product state emission patterns has been described by Reid, Loomis and Leone³⁰. An example of this is shown in Fig 5 of [30] in which an overview spectrum showing this use of this extraction method to aid the comparison of these, and related spectra, is presented. In the present spectra it may be seen that several of the weak sub-band structures in the ND₃ spectrum are clearly identified as belonging to hot bands having $v_2' = 1$ and 2. The most obvious patterns are indicated by arrows. The strongest transitions originating from $v_2' = 1$ are identified.