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► **To cite this version:**

Raf Jans, Zeger Degraeve. Modeling Industrial Lot Sizing Problems: A Review. International Journal of Production Research, 2008, 46 (06), pp.1619-1643. <10.1080/00207540600902262>. <hal-00512940>

HAL Id: hal-00512940

<https://hal.science/hal-00512940v1>

Submitted on 1 Sep 2010

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Journal:	<i>International Journal of Production Research</i>
Manuscript ID:	TPRS-2005-IJPR-0281.R1
Manuscript Type:	State-of-the-Art Review
Date Submitted by the Author:	27-Apr-2006
Complete List of Authors:	Jans, Raf; RSM Erasmus University, School of Management Degraeve, Zeger; London Business School, Decision Sciences
Keywords:	MODELLING, LOT SIZING
Keywords (user):	



MODELING INDUSTRIAL LOT SIZING PROBLEMS: A REVIEW

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Accepted July 5, 2006

Abstract

In this paper we give an overview of recent developments in the field of modeling deterministic single-level dynamic lot sizing problems. The focus of this paper is on the modeling of various industrial extensions and not on the solution approaches. The timeliness of such a review stems from the growing industry need to solve more realistic and comprehensive production planning problems. First, several different basic lot sizing problems are defined. Many extensions of these problems have been proposed and the research basically expands in two opposite directions. The first line of research focuses on modeling the operational aspects in more detail. The discussion is organized around five aspects: the set ups, the characteristics of the production process, the inventory, demand side and rolling horizon. The second direction is towards more tactical and strategic models in which the lot sizing problem is a core substructure, such as integrated production-distribution planning or supplier selection. Recent advances in both directions are discussed. Finally, we give some concluding remarks and point out interesting areas for future research.

1. Introduction

In this review, we will discuss models that have been developed for optimizing production planning and inventory management. *Lot sizing* models determine the optimal timing and level of production. They can be classified according to their time scale, the demand distribution and the time horizon. The famous Economic Order Quantity model (EOQ) assumes a continuous time scale, constant demand rate and infinite time horizon. The extension to multiple items and constant production rates is known as the Economic Lot Scheduling Problem (ELSP) (Elmaghraby 1978, Zipkin 1991). The subject of this review is the *dynamic lot sizing problem* with a discrete time scale, deterministic dynamic demand and finite time horizon. We will see that lot sizing models will incorporate more and more scheduling aspects. These *scheduling* models essentially determine the start and finish times of jobs (scheduling), the order in which jobs are processed (sequencing) and the assignment of jobs to machines (loading). Lawler et al. (1993) give an extensive overview of models and algorithms for these problems.

A general overview of many different aspects of production planning and inventory management can be found in Graves et al. (1993) and in standard textbooks such as Silver et al. (1998), Hopp and Spearman (2000) or Vollmann et al. (1997). Several studies focus specifically on the dynamic lot sizing problem (De Bodt et al. 1984, Bahl et al. 1987, Kuik et al. 1994, Wolsey 1995, Drexl and Kimms 1997, Belvaux and Wolsey 2001, Karimi et al. 2003, Brahimi et al. 2006, Jans and Degraeve 2006).

This review has a threefold contribution. Since the excellent reviews of Kuik et al. (1994) and Drexl and Kimms (1997) the research on dynamic lot sizing has further grown substantially. First of all, this paper fills a gap by providing a comprehensive overview of the latest literature in this field. Second, this paper aims to provide a general review and an extensive list of references for researchers in the field. Although this literature review is very extensive, we realize that it is impossible to be exhaustive. We realize that a model and its solution approach are inherently linked: more complex models demand also more complex solution approaches to solve them. However, in this paper we focus on the modeling aspect as much as possible in order to create some structure in the ever growing literature. This focus also distinguishes

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3 this paper from other lot sizing reviews. A recent review of solution approaches can
4 be found in Jans and Degraeve (2006). We show that the lot sizing problem is a core
5 substructure in many applications by reviewing both more operational and tactical or
6 strategic problems. Third, a comprehensive review further allows us to indicate new
7 areas for further research. The power of production planning theory comes from the
8 ability to solve more and more complex industrial problems. Whereas the early
9 models were usually more compact, capturing the main trade-off, the extensions
10 focus more and more on incorporating relevant industrial concerns. Therefore, this
11 review is also very timely.
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23 2. Lot Sizing Models

24 2.1. The single item uncapacitated lot sizing problem

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27 The simplest form of the *dynamic lot sizing problem* is the single item uncapacitated
28 problem:
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$$30 \text{ Min } \sum_{t=1}^m (vc_t x_t + sc_t y_t + hc_t s_t) \quad (1)$$

$$31 \text{ s.t. } s_{t-1} + x_t = d_t + s_t \quad \forall t \in T \quad (2)$$

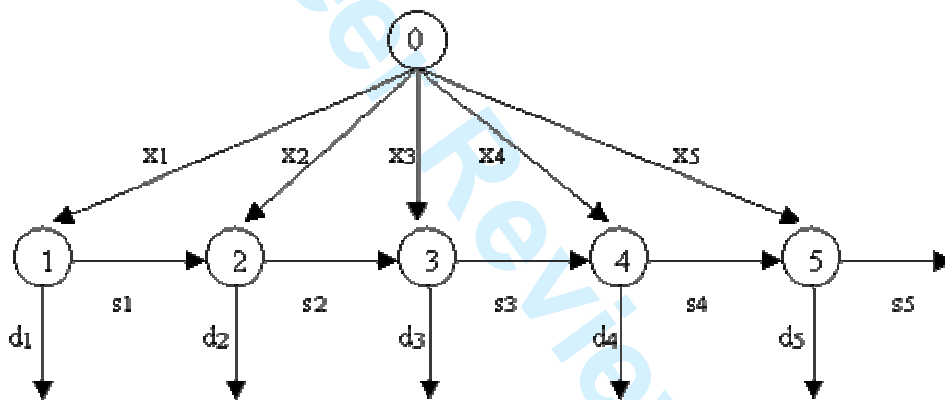
$$32 x_t \leq sd_{tm} y_t \quad \forall t \in T \quad (3)$$

$$33 x_t, s_t \geq 0; y_t \in \{0,1\} \quad \forall t \in T \quad (4)$$

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36 We have three key variables in each period t : the production level (x_t), the set up
37 decision (y_t) and the inventory variable (s_t). With each of these key variables is a cost
38 associated: vc_t , sc_t and hc_t are respectively the variable production cost, set up cost
39 and holding cost in period t . T is the set of all periods in the planning horizon and m is
40 the last period. Demand for each period, d_t , is known and sd_{tk} is the cumulative
41 demand for period t until k . The objective is to minimize the total cost of production,
42 set up and inventory (1). We find here the same basic trade-off between set ups and
43 inventory which is also present in the EOQ formula. Demand can be met from
44 production in the current period or inventory left over from the previous period (2).
45 Any excess is carried over as inventory to the next period. In each period we need a
46 set up if we want to produce anything (3). As there is no ending inventory in an
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optimal solution, production is limited by the remaining cumulative demand. Finally, the production and inventory variables must be positive and the set up variables are binary (4). This problem was first discussed in the seminal paper by Wagner and Whitin (1958). Zangwill (1969) showed that this problem is actually a fixed charge network problem. For a 5 period problem, the network can be depicted as shown in Figure 1. The arcs $(0, t)$ correspond to the production variables x_t and have an associated unit flow cost of vc_t . If the production is strictly positive, i.e. $x_t > 0$, then there is also a fixed cost of sc_t on the arc. The arcs $(t, t+1)$ correspond to the inventory variables s_t and have a unit flow cost of hc_t . In network terms we say that node 0 is the supply or source node, nodes 1 to 5 are the demand nodes and the demand balance equations (2) correspond to the conservation of flow constraints.

Fig. 1. Network for the single item uncapacitated lot sizing problem



2.2. Capacitated Multi-Item Lot Sizing Problem (CLSP)

Of course, companies do not have an unlimited capacity and usually they make more than one product. Any realistic model has to take this into account. How these two elements are modeled, depends on the mode of production and the choice of the time period. In the *large bucket* model, several items can be produced on the same machine in the same time period. In the *small bucket* model, a machine can only produce one type of product in one period.

The capacitated multi-item lot sizing problem (CLSP) is the typical example of a *large bucket* model. There are n different items that can be produced and P is the set

of all these items. In each period, only a limited production capacity cap_t is available. Producing one unit of product i consumes vt_i units of capacity. The formulation is as follows:

$$\text{Min} \sum_{i \in P} \sum_{t \in T} (sc_{it} y_{it} + vc_{it} x_{it} + hc_{it} s_{it}) \quad (5)$$

$$\text{s.t.} \quad s_{i,t-1} + x_{it} = d_{it} + s_{it} \quad \forall i \in P, \forall t \in T \quad (6)$$

$$x_{it} \leq My_{it} \quad \forall i \in P, \forall t \in T \quad (7)$$

$$\sum_{i \in P} vt_i x_{it} \leq cap_t \quad \forall t \in T \quad (8)$$

$$x_{it}, s_{it} \geq 0; y_{it} \in \{0,1\} \quad \forall i \in P, \forall t \in T \quad (9)$$

We observe that in this formulation, product specific variables and parameters now have an extra index i to identify the item. For each item we have the demand balance equations (6) and set up constraints (7). The main difference with the uncapacitated model is the addition of the capacity constraint (8). In the set up constraint (7), the 'big M' is usually set equal to $\min\{cap_t / vt_i, sd_{im}\}$, as such the production is now limited by both the capacity and remaining demand (8).

The Continuous Set Up Lot Sizing Problem (CSLP) is a *small bucket* model:

$$\text{Min} \sum_{i \in P} \sum_{t \in T} (g_{it} z_{it} + sc_i y_{it} + vc_i x_{it} + hc_i s_{it}) \quad (10)$$

$$\text{s.t.} \quad s_{i,t-1} + x_{it} = d_{it} + s_{it} \quad \forall i \in P, \forall t \in T \quad (11)$$

$$\sum_{i=1}^n y_{it} \leq 1 \quad \forall t \in T \quad (12)$$

$$vt_i x_{it} \leq cap_t y_{it} \quad \forall i \in P, \forall t \in T \quad (13)$$

$$z_{it} \geq y_{it} - y_{i,t-1} \quad \forall i \in P, \forall t \in T \quad (14)$$

$$x_{it}, s_{it} \geq 0; y_{it}, z_{it} \in \{0,1\} \quad \forall i \in P, \forall t \in T \quad (15)$$

The new variable z_{it} is the start up variable and there is an associated start up cost of g_{it} . A start up occurs when the machine is set up for an item for which it was not set up in the previous period. The objective function (10) minimizes the total cost of start ups, set ups, variable production and inventory. We still have the regular demand constraints (11). Further, we have the *single mode* constraint (12), imposing that at most one type of product can be made in each time period. For each item, production

can be up to capacity if there is a set up (13). The start up variables are modeled in constraint (14). There will only be a start up if the machine is set up for an item for which it was not set up in the previous period. A set up can be carried over to the next period if production of the same product is continued. Finally, the set up and start up variables are binary (15). Karmarkar and Schrage (1985) consider this problem without set up costs and called it the *product cycling problem*. Karmarkar et al. (1987) study the single item version of the CSLP, both for the uncapacitated and capacitated case. This problem is also referred to as *lot sizing with start up costs* (Wolsey 1989, Sandbothe 1991).

The *Discrete Lot Sizing and Scheduling Problem* (DLSP) is a small bucket lot sizing model with a *discrete production policy*: if there is any production in a period, it must be at full capacity. The generic model (Fleischmann 1990) has a similar structure as the CSLP (10)-(15), except that the capacity and set up constraint (13) becomes an equality:

$$\forall i \in P, \forall t \in T \quad vt_i x_{it} = cap_t y_{it} \quad (14)$$

Note that the production variable can be substituted out through this constraint. Jordan and Drex1 (1998) showed the equivalence between DLSP for a single machine and the batch sequencing problem.

3. Further Extensions of Lot Sizing Models

Production planning problems are often classified according to the hierarchical framework of strategic, tactical and operational decision making (e.g. Bitran and Tirupati 1993). Depending on the decision horizon and level of aggregation, lot sizing models are usually classified as either tactical or operational models. A yearly master production schedule at the plant level is used for tactical planning. Production sequencing and loading are operational decisions and determining the lot sizes for products in the next month falls somewhere in between. We observe that the basic lot sizing models from the previous section are extended in two different directions. On one hand, lot sizing formulations include more operational and scheduling issues in order to model more accurately the production process, costs and demand side. We

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organize these extensions around four topics: set ups, production, inventory and demand, but clearly some extensions relate to more than one of them. Here we also discuss the use of these models in a rolling horizon way. On the other hand, these models are incorporated into more tactical and strategic problems for which the operational lot sizing decisions are a core substructure.

3.1 Operational models

3.1.1. Extension on the set ups

Sometimes, there are not only set ups for individual items, called *minor set ups*, but there is a *joint or major set up* as well, which is incurred when at least one product is produced. These joint costs are used to model general economies of scale in manufacturing or procurement. This problem is extensively studied (Veinott 1969, Atkins and Iyogun 1988) and is sometimes referred to as the *coordinated replenishment problem* (Kao 1979, Chung et al. 1996, 2000, Robinson and Gao 1996, Robinson and Lawrence 2004) or the *joint replenishment problem* (Joneja 1990, Federgruen and Tzur 1994). In the case where the orders can be shipped via multiple modes, there is a different set up structure associated with each mode (Jaruphongsa et al. 2005). Production planning models *without set ups* have also been considered. Bowman (1956) shows that for the problem with convex cost functions, this problem can be solved as a transportation problem. Lotfi and Chen (1991) and Hindi (1995) discuss the capacitated case. On the other hand, sometimes the only objective is to minimize the costs of set ups or start ups. This is the case for the *Changeover Scheduling Problem* (CSP) (Glassey 1968, Hu et al. 1987, Blocher and Chand 1996^{a,b}, Blocher et al. 1999). The problem assumes a discrete production policy and is as such related to the DLSP. A changeover is performed when production is switched to another product. In the DLSP terminology, this was called a start up. No inventory holding, production or set up costs are considered. Miller and Wolsey (2003) consider the discrete lot sizing problem with set ups but without start ups. Note that there is sometimes confusion in the literature between the terms set up and start up and we use the definition according to Vanderbeck (1998). In the *production smoothing* problem (Zangwill 1966^b, Korgaonker 1977), a penalty proportional to the changes in production level is charged instead of a set up cost.

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5 Several authors (e.g. Manne 1958, Kleindorfer and Newson 1975, Newson 1975,
6 Trigeiro et al. 1989, Diaby et al. 1992, Du Merle et al. 1997, Armantano et al. 1999,
7 Gopalakrishnan et al. 2001, Degraeve and Jans 2003, Hindi et al. 2003, Jans and
8 Degraeve 2004^b) consider *set up times* for the CLSP. The set up times represent the
9 capacity lost due to cleaning, preheating, machine adjustments, calibration, inspection,
10 test runs, change in tooling, etc., when the production for a new item starts. The set up
11 time must be accounted for in the capacity constraint. Salomon et al. (1991) and
12 Cattrysse et al. (1993) consider start up times for the DLSP. They assume that start up
13 times must equal an integral multiple of the time bucket, but it is also possible to
14 model start up times which are a fraction of the time bucket (De Matta and Guignard
15 1994^b, Jans and Degraeve 2004^a). Vanderbeck (1998) formulates a CSLP with
16 fractional start up times.
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28 An often considered critique on the CLSP states that this model does not allow a set
29 up to be carried over from one period to the next, even if the last product in one
30 period and the first product in the next are the same. This has led to new models
31 which allow for such a *set up carry over*, at the expense of introducing additional
32 binary variables (Gopalakrishnan et al. 1995, Sox and Goa 1999, Gopalakrishnan
33 2000, Porkka et al. 2003, Gupta and Magnusson 2005). This problem is also referred
34 to as the capacitated lot sizing problem *with linked lot sizes* (Suerie and Stadtler 2003).
35 Computational results show that this model leads to considerable cost savings through
36 the set up carry over (Gopalokrishnan et al. 2001). The *Proportional Lot Sizing and*
37 *Scheduling Problem* (PLSP) relaxes the restriction of allowing production for only
38 one product in each time period as imposed by the DLSP and CSLP. In the PLSP at
39 most two different items can be produced in each time period. There is still at most
40 one set up in each period, but the set up from the previous period can be carried over
41 to the next period. Hence, if two items are produced in period t , then the first item
42 must be the same as the last item in the previous period. Drexl and Haase (1995,
43 1996) discuss this model and extensions such as set up times and multiple machines.
44 A further refinement allows the set up times to be split between two periods (Suerie
45 2006). Kimms (1996^{a,b}, 1999) presents the multi-level version of the PLSP.
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3 The PLSP and the model with set up carry over are examples of lot sizing problems
4 that incorporate more and more sequencing aspects. A further step for the CLSP is to
5 determine a sequence for all the products within a time period, and not just for the
6 first and last one. This is necessary if set up costs or times are *sequence dependent*
7 (Dilts and Ramsing 1989, Haase 1996, Fleischmann and Meyr 1997, Kang et al. 1999,
8 Laguna 1999, Clark and Clark 2000, Haase and Kimms 2000, Meyr 2000, Gupta and
9 Magnusson 2005). In the *General Lot Sizing and Scheduling Problem* (Fleischmann
10 and Meyr 1997), the macro-periods are divided into a fixed number of micro-periods
11 with variable length, which allows the sequencing of products. Fleischmann (1994)
12 considers the DLSP with sequence dependent start up costs. His heuristic procedure is
13 based on the transformation of the problem into a Traveling Salesman Problem with
14 Time Windows. Salomon et al. (1997) describe an algorithm for the DLSP with both
15 sequence dependent start up costs and start up times. De Matta and Guignard (1994^b)
16 also model sequence dependent cost and set up times in a DLSP in the process
17 industry. In his review on change-over modeling Wolsey (1997) studies sequence
18 dependent start ups for the CSLP. Belvaux and Wolsy (2000, 2001) present a
19 comprehensive lot sizing model, including sequence dependent costs or times and
20 *switch off* variables. Potts and Van Wassenhove (1992) discuss the integration of
21 scheduling and lot sizing from a scheduling perspective.
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39 Small set up costs and times are essential for implementing a successful Just-In-Time
40 approach. *Set up cost and time reduction* programmes require an initial capital
41 investment and result in a more flexible production. Zangwill (1987) points out that
42 some intuitive implications of a set up reduction in an EOQ environment do not
43 necessarily hold in the context of dynamic lot sizing. Mekler (1993), Diaby (1995)
44 and Denizel et al. (1997) offer models to evaluate the tradeoff between the cost and
45 benefits of a set up time reduction within a dynamic lot sizing framework. The set up
46 times and costs are variables and depend on previous investment decisions. Another
47 way to achieve lower set up costs is through learning. According to the theory of the
48 *learning curve*, production costs decrease as cumulative output increases over time.
49 Chand and Sethi (1990) present a lot sizing model with learning in set ups. Set up
50 costs depend on the total number of set ups up to now and there is a declining set up
51 cost for successive set ups. Benefits from smaller lot sizes are captured in terms of
52 reduced set up costs. Tzur (1996) provide a more general model where the costs of a
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3 set up still depend on the number of previous set ups, but can both decrease or
4 increase, as long as the total set up costs are nondecreasing. Examples of increasing
5 set up costs are the cases where the set up cost increases with the usage of the
6 machine or when some maintenance is necessary after a specific number of set ups.
7 Learning can also decrease the set up time (Pratsini 2000).
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14 Almost all of the dynamic lot sizing models assume that production is done on
15 reliable machines. Kuhn (1997) analyses the effects of *set up recovery* with machine
16 breakdowns and corrective maintenance for the single item uncapacitated lot sizing
17 problem. In a first case, the assumption is made that the set up is totally lost after a
18 breakdown. In a second case, the costs of resuming production of the same item after
19 a breakdown is lower compared to the original set up cost.
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26 3.1.2. Extensions on the Production

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30 In some manufacturing environments, production is done in *batches* (Lipmann 1969,
31 Lee 1989, Pochet and Wolsey 1993, Constantino 1998, Van Vyve 2003). In the
32 mathematical formulation, the set up variable y_{it} becomes general integer instead of
33 binary and indicates the number of batches produced. Every time production exceeds
34 a multiple of the batch size, a new set up cost is incurred. This is for example the case
35 in an environment where production is limited by a tank size. Each time one has to fill
36 the tank again a set up cost is incurred, even if the same item is produced. This can
37 also be interpreted as a stepwise cargo cost function (Lee 2004) where the capacity of
38 each cargo is limited. Ben-Khedher and Yano (1994) assume that containers, which
39 may be only partially filled, are assigned to trucks and there is a fixed charge for each
40 truck used. Elmaghraby and Bawle (1972), Dorsey et al. (1974), Van Vyve (2003)
41 and Li et al. (2004) impose that production is done in exact multiples of the batch size.
42 Hence these models assume a discrete production policy but do not consider start up
43 interactions over time. Manufactured units may not be available instantaneously, but
44 arrive only in inventory after the whole batch has been completed (Brüggemann and
45 Jahnke 1994, 2000). Stowers and Palekar (1997) and Bhatia and Palekar (2001)
46 consider a variant of the joint replenishment lot sizing problem where products
47 belonging to the same family can only be made in a *fixed proportion* to each other. A
48 product can be part of several different families. This type of production occurs in the
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3 manufacturing of metal or plastic plates and die-cast parts and in some chemical
4 production problems. It is referred to as lot sizing with *strong set up interaction*. In an
5 oil refinery, sets of products are produced simultaneously in same process, but the rate
6 depends on the mode of operation (Persson et al. 2004). Love (1973) extends the lot
7 sizing problem by introducing *lower and upper bounds on the production*. Production
8 below some level is not allowed because of technical constraints or in order to make
9 full use of the resource (Anderson and Cheah 1993, Constantino 1998, Mercé and
10 Fontan 2003, Lee 2004).
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19 In many production processes, *tools* such as dies or molds are required and they are
20 often shared among several products. Tools, machines and products are interrelated as
21 there are compatibility requirements between them (Brown et al. 1981). The problem
22 is further complicated as there is only a limited availability of both the machines and
23 tools. Jans and Degraeve (2004^a) model such a production planning problem for a tire
24 manufacturer where the number of molds is a limiting factor. Akturk and Onen (2002)
25 also integrate a lot sizing and tool management problem.
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33 We observed that the boundaries between lot sizing and scheduling are fading with
34 the introduction of sequence dependent set up costs and times. Lasserre (1992) and
35 Dauzère-Péres and Lasserre (1994) provide a further example of this by integrating a
36 classical multi-period lot sizing problem with a *job shop scheduling* problem. The lot
37 sizing decision determines the due dates and processing times of the jobs. The
38 capacity constraints are modelled at machine level by the regular job-shop precedence
39 relations and disjunctive constraints. It is also an integration of discrete and
40 continuous time planning models.
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49 When *multiple parallel machines* are available, the lot sizing problem does not only
50 include the timing and level of production, but also the allocation of production to
51 machines. As such the loading decision has to be considered as well. Özdamar and
52 Birbil (1998), Özdamar and Barbarosoğlu (1999), Kang et al. (1999), Clark and Clark
53 (2000) and Belvaux and Wolsey (2000) extend the Capacitated Lot Sizing Problem
54 with *multiple machines* with different production efficiencies. The DLSP and CSLP
55 have also been extended with multiple identical machines (Lasdon and Terjung 1971)
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3 and multiple machines with different efficiencies (Salomon et al. 1991, De Matta and
4 Guignard 1994^{a,b}, 1995, Jans and Degraeve 2004^a).
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9 *Production costs* can also change. Quantity discounts are sometimes considered in a
10 lot sizing model, mostly in the case of purchasing decisions. Many quantity discount
11 schemes result in a piecewise linear cost function (Shaw and Wagelmans 1998).
12 Usually three types of quantity discounts are considered. The all-units discount
13 (Prentis and Khumawala 1989, Chung et al. 1996) gives a reduction in the purchase
14 price on all the units of a product if you buy more than a specific amount. Degraeve
15 and Roodhooft (2000) model a multi-item purchasing environment where the discount
16 is given on the total amount bought. Chan et al. (2002) propose a modified all-unit
17 discount structure: if the total cost is higher than the total cost at the start of the next
18 quantity interval, you only pay the lower cost. In the case of the incremental quantity
19 discount (Diaby and Martel 1993, Chung et al. 1996, 2000), the reduction is only
20 valid for the amounts in a specific interval. A third alternative is the truckload
21 discount scheme (Li et al. 2004), where a less-than-truckload rate is charged until the
22 total cost equal the truckload rate. If the total quantity is more than a truckload, this
23 same scheme is applied for the excess quantity. Chu et al. (2005) consider a general
24 economies-of-scale function for the ordering costs. When the production costs are
25 actually distribution costs, van Norden and van de Velde (2005) argue that there is a
26 dual cost structure. Any amount up to a reserved capacity is charged at a specific cost,
27 and any amount above is charged at a higher cost.
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44 *Cyclical schedules*, where the time between subsequent set ups is constant, are often
45 used in practice. Bahl and Ritzman (1984) use cyclical schedules in a lower bounding
46 heuristic. Campbell and Mabert (1991) impose such cyclical schedules for the CLSP
47 with set up times. In their study, costs increases only by 5% on average compared to
48 the best non-cyclical schedules.
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55 In the distribution, inventory control and production planning literature, there is a
56 growing interest in *reverse logistics* (Fleischmann et al. 1997). Items return from the
57 customers to the manufacturer and can be reused, either directly or after
58 remanufacturing. Remanufacturing includes testing, repair, disassembly and
59 reassembly operations. Another option is to recycle the scrap material or reuse some
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3 parts as components. Taking these aspects into consideration requires an adaptation in
4 the production planning models (Fleischmann et al. 1997, Guide 2000). Few dynamic
5 lot sizing models have been proposed to accommodate such changes. Richter and
6 Sombrutzki (2000) extend the ULS with remanufacturing. Demand can be met either
7 from newly manufactured products or from return products which have been
8 remanufactured. These two product categories have different set up costs (van den
9 Heuvel 2004) or a joint set up cost (Teunter et al. 2005). In practice, the two
10 categories also have different unit (re)manufacturing costs and there is the possibility
11 of disposal of some of the returned products (Richter and Weber 2001). Yang et al.
12 (2005) analyze the problem with concave costs. Beltrán and Krass (2002) consider the
13 case where the returned goods are in good enough condition to be resold immediately
14 without remanufacturing. In their model, demand can be negative due to the returns
15 and they allow for the disposal of excess inventory. Kelle and Silver (1989) model a
16 similar problem, but take into account the uncertainty in the arrival of the returned
17 goods. They impose a service level constraint and next transform the problem into an
18 ULS with negative demands. In a mathematical programming model for order
19 quantity determination in a purchasing context, Degraeve and Roodhooft (1999)
20 incorporate additional revenues due to repurchases of old products by the supplier.
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3.1.3. Extensions on the inventory

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42 The inventory can also be bounded by *upper and lower limits* (Love 1973, Swoveland
43 1975, Erenguc and Aksoy 1990, Sandbothe and Thompson 1993, Gutiérrez et al. 2002,
44 Jaruphongsas et al. 2004). Loparic, Pochet and Wolsey (2001) consider safety stocks
45 by imposing a lower bound on the inventory in each period. *Fixed charges on the*
46 *stocks* (Van Vyve and Ortega 2004) are useful for an environment with complex
47 stocking operations or for situations where there are combinatorial constraints on
48 stocks, such as in the chemical industry where only one type of product can be stored
49 in a tank.
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58 Martel and Gascon (1998) make a subtle change to the classical uncapacitated lot
59 sizing problem in a purchase context. The unit purchase cost can vary over time and
60 the holding cost is *price-dependent*, whereas in the standard model, the unit inventory

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3 holding cost can vary, but is known in advance and does not depend on the purchase
4 price. The inventory cost is calculated as the purchase price multiplied by a constant
5 inventory holding charge.
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10 Lot sizing problems have also been extended with the issue of *perishable inventory*.
11 Veinott (1969) permits the proportional growth or deterioration of inventory. Hsu
12 (2000) and Chu et al. (2005) consider the uncapacitated single item lot sizing problem
13 with an age dependent inventory cost as well as an age dependent deterioration rate
14 where a part of the inventory is lost by carrying it to the next period. Jain and Silver
15 (1994) look at the problem with random life time perishability. According to some
16 stochastic process, the total inventory becomes either worthless or remains usable for
17 at least the next period.
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28 3.1.4. Extension on the demand 29 30

31 By allowing *backlogging* (e.g. Zangwill 1966^a, Pochet and Wolsey 1988, Federgruen
32 and Tzur 1993) demand can be met by production in a later period at a specific cost.
33 Backlogging corresponds in fact to a negative inventory level. The objective function
34 includes the backlog cost. We can use inventory from the previous period, allow
35 backlog or produce now to satisfy demand, build up inventory or satisfy backlog from
36 a previous period. The case with backlogging is also a single source fixed charge
37 network problem (Zangwill 1969). Backlogging results in a flow from demand point t
38 to $t-1$, in the opposite direction of the inventory flow. Swoveland (1975) imposes that
39 orders are not backlogged for more than a prescribed number of periods. The
40 extension with backlogging is also considered for the DLSP (Jans and Degraeve
41 2004^a) and for the coordinated replenishment problem (Robinson and Gao 1996). Hsu
42 and Lowe (2001) study the problem with age dependent backlog costs. Another way
43 of satisfying demand if not enough products are available in time is product
44 *substitution* (Hsu et al. 2005). Demand for e.g. a low quality product can also be met
45 by offering the high quality product at the price of the low quality product. It is also
46 possible that a product first need to be transformed, which leads to an extra
47 conversion cost.
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3 Lot sizing models with *stockouts* (Sandbothe and Thompson 1990, 1993, Aksen et al.
4 2003) have been proposed as an alternative to situations where backlogging is allowed.
5 When demand cannot be met in time, *lost sales* are incurred instead of backlogging. A
6 variable l_t representing the lost sales is added into the demand equation and the cost of
7 a stockout is properly accounted for in the objective function.
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13 Considering *sales* (Brown et al. 1981, Kang et al. 1999, Loparic, Pochet and Wolsey
14 2001) instead of fixed demands leads to a profit maximization approach instead of the
15 traditional cost minimization. The demand equation is extended with a variable v_t for
16 the sales and an upper bound of d_t is imposed on these potential sales. The unit selling
17 price is given. Hung and Chien (2000) model a profit maximization approach with
18 different demand classes that have different profitibilities. The two models of
19 maximizing sales and minimizing costs with lost sales are equivalent as demand can
20 be rewritten as the sum of the sales and lost sales.
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30 Lee et al. (2001) discuss the single item uncapacitated dynamic lot sizing problem
31 with a *demand time window*. For each demand an earliest and latest delivery date is
32 specified and demand can be satisfied in this period without penalty. They prove that
33 there exists an optimal solution in which demand is not split: the complete demand for
34 a specific order is covered by production from the same period. Hwang and
35 Jaruphongsa (2006) analyse the case with a speculative cost structure. An extension to
36 a two-echelon supply chain is provided in Jaruphongsa et al. (2004). Another
37 extension is the incorporation of time windows for the suppliers who are shipping the
38 goods via a crossdock (Lim et al. 2005). Also Wolsey (2006) makes a distinction
39 between production time windows and delivery time windows.
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51 3.1.5. Time Horizon

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53 Schedules are usually implemented in a *rolling horizon* fashion. Only the first period
54 of a plan is implemented and the demand forecast is updated by looking one period
55 further. A new plan is calculated using this updated input. Experiments (Baker 1977,
56 Blackburn and Millen 1980) have indicated that the Wagner-Whitin algorithm is no
57 longer optimal in a rolling horizon framework and simple lot sizing heuristics may
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outperform optimal algorithms for small planning horizons. New research (Simpson 2001), however, indicates that the Wagner-Whitin rule still outperforms all the other heuristics in a wide variety of cases. For an extensive review on rolling horizons and related literature we refer the reader to Chand et al. (2002). The rolling horizon approach can result in nervousness of the planning in the sense that schedules must be frequently changed. These changes might result in extra costs (Kazan et al. 2000). Recently, two methods have been proposed to mitigate the end-of-horizon effect basically by looking beyond the current planning horizon. Stadtler (2000) takes only a fraction of the costs for the last set up period into account. The last set up may be advantageous beyond the planning horizon, so only a proportion of the set up cost has to be borne within the planning horizon. Fisher et al. (2001) impose an appropriate level of ending inventory by assigning a positive value to this ending inventory in the objective function. This positive value is calculated by estimating the future set up costs that are avoided as a result of the ending inventory. Experiments in both papers indicate that these adaptations are quite effective in general and they usually outperform simple heuristics or the unadapted WW algorithm. Van den Heuvel and Wagelmans (2005) point out that the superior performance of Fisher et al. (2001) is mainly due to the availability of accurate information about future demand.

3.2. Tactical and strategic models

Hierarchical production planning (Hax and Meal 1975, Bitran, Haas and Hax 1981, Graves 1982, Bitran and Tirupati 1993) is a sequential procedure for solving production planning at different levels of aggregation. First, decisions are taken at the highest level and they set the limitations for the decisions at a lower level. Items are aggregated into families and families into types. A type is a set of items that have a similar demand pattern and have one aggregate production rate. Within a family, items share the same set up. In the aggregate model, at the type level, the main decision is the determination of the level for regular and overtime capacity and the total production for a type. This decision sets bounds on the model for the family production planning. Here the objective is to minimize the total set up cost for all families within a type. Within the limits of the family batch sizes, production quantities are determined for each item. An application of this type of planning is

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3 described in Liberatore and Miller (1985) and Oliff and Burch (1985). There is a lot
4 of interaction between the different levels and the sequential optimization does
5 usually not result in a global optimum. The reason that detailed integrated models are
6 yet scarce is of course their complexity, which make them difficult to solve. Yet there
7 exist some models which integrate lot sizing and decisions at higher hierarchical
8 levels.
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16 *Aggregate planning* extends the lot sizing models further at a more tactical level by
17 including labor resource decisions such as hiring and firing (e.g. Dzielinski, Baker
18 and Manne 1963, Thomas and McClain 1993, Nam and Logendran 1992, Aghezzaf
19 2000). The decision on set up cost and time reduction, as discussed in the previous
20 section, can also be viewed as the integration of lot sizing in a more tactical decision.
21 Another example is the integration of lot sizing and *capacity expansion* decisions.
22 Rao (1976) considers a lot sizing model where additional capacity can be bought in
23 each period. The extra capacity is also available in all the subsequent periods, in
24 contrast with temporary capacity expansion from overtime. Rajagopalan and
25 Swaminathan (2001) optimize the capacity acquisition, production and inventory
26 decisions over time in an environment with increasing demand. There is the following
27 trade-off: Capacity investments can be postponed by building up inventory earlier. On
28 the other hand, buying additional capacity can lead to smaller inventories by reducing
29 lot sizes. Bradley and Arntzen (1999) discuss a case study where simultaneously
30 considering capacity and inventory decisions leads to superior financial results. In the
31 model of Atamturk and Hochbaum (2001) variable demand can be met by production,
32 inventory, *subcontracting* or *capacity acquisition*. A second way of modeling capacity
33 expansion problems is to define the demand as the demand for the incremental
34 capacity (Luss 1982, Chand et al. 2000, Hsu 2002) and there is no modeling of the
35 underlying production lot sizing anymore.
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53 Interest in modeling the interaction between the production stage and upstream
54 (suppliers) and downstream (distribution) activities is growing. Whereas previously
55 these relationships were considered at an aggregate level, it is useful to consider
56 inbound logistics, production and distribution simultaneously at an operational level.
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58 The general message of these models is that strategic or tactical decisions, such as
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3 investment decisions or supplier selection, should take operational concerns, in this
4 case lot sizing, into account.
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7 The lot sizing structure shows up as a subproblem in the *supplier selection* problem
8 considered by Degraeve and Roodhooft (1999, 2000) and Degraeve, Labro and
9 Roodhooft (2000). They model the total cost of ownership at four different levels, i.e.
10 supplier, order, batch and unit level. These costs include the regular order cost,
11 purchase price and inventory holding cost, but can also take into account quality
12 differences, discounts, reception costs for batches and the cost for managing the
13 relationship with the supplier. Basnet and Leung (2005) study a special case with a
14 supplier-dependent order cost.
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18 Global models for *supply chain optimization* simultaneously consider production,
19 transportation and demand planning. The coordination of production and distribution
20 planning results in cost savings compared to separate optimization of these activities
21 (Chandra and Fisher 1994). Herer and Tzur (2001) consider a multi-location single-
22 item problem where transshipments of stock between locations at the same
23 distribution level are allowed. Transshipments can be beneficial in a deterministic
24 environment due to the presence of fixed order costs or differences in holding costs.
25 Another extension is the inclusion of capacitated vehicles to model the transportation
26 between two stages (Anily and Tzur 2005, 2006). A case study in the fertilizer
27 industry (Haq et al. 1991) describes a multi-level structure with plants, warehouses
28 and retailers and incorporates set up costs and times, production and distribution lead
29 times and the costs for production, set up, inventory and transportation. Martin et al.
30 (1993), Diaby and Martel (1993), Kaminsky and Simchi-Levi (2003), Lee et al.
31 (2003), Jolayemi and Olorunniwo (2004) and Sambasivan and Yahya (2005) discuss
32 models for integrated production, distribution and inventory planning. Bhutta et al.
33 (2003) also take capacity investment decision into account, next to the production and
34 distribution problems. Federgruen and Tzur (1999) study a two-echelon distribution
35 network with one warehouse and many retailers and model it as a dynamic lot sizing
36 problem. Timpe and Kallrath (2000) describe an actual application in the chemical
37 process industry combining batch and campaign production with change-overs in a
38 multi-site setting, raw materials inventory management, transportation between
39 production sites and sales point, inventories at the sales points, different prices for
40 different customers and external purchase possibilities. Their objective function is
41 maximizing the total contribution. Van Hoesel et al. (2002) consider a serial supply
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3 chain with one manufacturer and multiple warehouses and they globally optimize the
4 production, inventory and transportation decisions. A general overview of interesting
5 issues for global supply chain optimization at the supplier, plant and distribution stage
6 is given in Erengüç et al. (1999).
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10 11 12 **4. Conclusions and New Research Directions** 13

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15 While some extensions are motivated from the literature or general practical
16 observations (e.g. Jaruphongsa et al. 2005, Van Vyve and Ortega 2004), many of the
17 extensions discussed in Section 3 are inspired by a specific real life problem.
18 Typically, the authors relate their model to a case observed in practice: “This paper
19 was motivated by a production planning problem encountered while working with a
20 multinational manufacturing firm” (Miller and Wolsey 2003); “Motivated by a
21 problem faced by a large manufacturer of a consumer product, we explore the
22 interaction between production planning and capacity acquisition decisions.”
23 (Rajagopalan and Swaminathan 2001); “A real-world problem in a company
24 manufacturing steel rolled products provided motivation to this research”
25 (Sambasivan and Yahya 2005). This provides sound industrial validation for the
26 research on extended lot-sizing models. Some of these papers try to fit the real life
27 case into a more generally applicable model and test it on randomly generated data
28 sets. This is usually done to analyse their algorithm and check the impact of some
29 specific parameters (e.g. Gupta and Mangusson 2005, Haase and Kims 2000, Porkka
30 et al. 2003, Robinson and Lawrence 2004, Sambasivan and Yahya 2005,). Other
31 papers analyse the real life problem, provide a new formulation and perform
32 computational experiments on real life data (e.g. Belvaux and Wolsey 2000, 2001,
33 Degraeve and Roodhooft 1999, De Matta and Guignard 1994, Grunow et al. 2002,
34 Jans and Degraeve 2004^a, Kang et al. 1999, Meyer 2000, Miller and Wolsey 2003,
35 Rajagopalan and Swaminathan 2001). For some case studies, the practical
36 implementation and actual company impact is also discussed in the paper (Bradley
37 and Arntzen 1999, Haq et al. 1991, Lee and Chen 2002, Liberatore and Miller 1985,
38 Martin et al. 1993, Oliff and Burch 1985, Timpe and Kallrath 2000, Van Wassenhove
39 and De Bodt 1983). The applications of deterministic lot-sizing can be found in many
40 different industries: injection moulding (Brown et al. 1981, Van Wassenhove and De
41 Bodt 1983), glass industry (Martin et al. 1993), consumer products (Rajagopalan and
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3 Swaminathan 2001), tire industry (Gorenstein 1970, Jans and Degraeve 2004^a, Lasdon
4 and Terjung 1971), chemical industry (Grunow et al. 2002, Haq et al. 1991, Kallrath
5 2005, Lee and Chen 2002, Persson et al. 2004, Robinson and Lawrence 2004, Timpe
6 and Kallrath 2000), pharmaceutical industry (Grunow et al. 2003), steel industry
7 (Degraeve and Roodhooft 1999, Dutta and Fourer 2001, Sambasivan and Yahya
8 2005), paper industry (Gupta and Mangusson 2005, Porkka et al. 2003), tile
9 manufacturing (De Matta and Guignard 1994), and the electronics industry (Bradley
10 and Arntzen 1999). The many academic papers that are inspired by or solve real life
11 lot sizing problems provide support for the applicability of the models and indicate
12 the possible benefits of lot sizing in practice.
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23 The numerous extensions of the basic lot sizing problem show that it can be used to
24 model a variety of industrial problems. Boundaries between lot sizing and scheduling
25 are fading and further integration of lot sizing, sequencing and loading constitute a
26 challenging research track. Lot sizing on parallel machines is just one example for
27 new research opportunities. Also the increased attention to model specific
28 characteristics of the production process and to accurately represent costs will be
29 valuable in solving real life planning problems. Further, the integration of lot sizing
30 into more global models opens an interesting area for further research. In the case
31 where products have to be manufactured and shipped to different distribution centers,
32 retailers or end customers, it makes sense to consider production and distribution
33 simultaneously at an operational level. In such a situation we should consider fixed
34 and variable costs for both production and transportation and coordinate lot sizing,
35 vehicle loading and routing decisions. New models could also take into account the
36 coordination between multiple plants or further downstream activities such as packing.
37 Another research direction is coordination of lot sizing with decisions from other
38 functional areas such as demand planning and pricing decisions (van den Heuvel and
39 Wagelmans 2006, Geunes et al. 2006, Deng and Yano 2006) in marketing, as is done
40 for other lot sizing models (Goyal and Gunasekaran 1995, Kim and Lee 1998, Abad
41 1996, 2003).
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58 Pochet (2001) indicates that modeling production planning problems in the process
59 industry constitute a promising area for new research, whereas most of the lot sizing
60 literature is focused on discrete manufacturing. Some distinguishing characteristics,

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3 such as the use of flexible recipes, the existence of by-products, the integration of lot
4 sizing and scheduling, storage constraints and a focus on profit maximization, affect
5 the planning and scheduling. A further general discussion can be found in Crama et al.
6 (2001) and Kallrath (2002, 2005), whereas some specific problems are presented in
7 Smith-Daniels and Ritzman (1988), Selen and Heuts (1990), Heuts et al. (1992),
8 Grunow et al. (2002, 2003), Rajaram and Karmarkar (2004), Persson et al. (2004).
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16 One of the major limitations of the lot sizing models that we discuss in this review is
17 the assumption of deterministic demand and processing times. In many manufacturing
18 environments, there is some degree of uncertainty. As a consequence, the
19 performance evaluation criteria differ in a deterministic and stochastic environment.
20 The deterministic lot sizing models formulate the problem as a trade-off between
21 inventory costs and set up costs. However, they fail to capture the problem of queuing
22 and congestion found in stochastic manufacturing environments (Banker et al. 1988,
23 Rummel 2000). Karmarkar (1987) examines the relationship between lot sizes and
24 lead times in such a stochastic environment. He argues that the lead time is a good
25 proxy for many costs, as larger lead times adversely affect the work-in-process
26 inventory, the safety stock and responsiveness to the customer. Karmarkar shows that
27 there exists a convex relationship between lot sizes and lead times. Small batches lead
28 to more set ups, a higher utilization rate and consequently to longer lead times. This is
29 the saturation effect. On the other hand, larger lot sizes lead to increased lead times
30 due to the batching effect. Deterministic and stochastic lot sizing models also suggest
31 qualitatively different optimal solutions. From basic queuing theory it is known that
32 when the capacity utilization increases to 100%, the waiting times become infinite.
33 This suggests that some slack capacity should be included in the planning. In
34 deterministic capacitated lot sizing models, however, the capacity constraint will be
35 binding in many periods and so there is no slack capacity available. In a stochastic
36 environment, the schedule stability also becomes an important objective (Bourland
37 and Yano 1994). Stochastic inventory models (e.g. Eppen and Martin 1988, Zipkin
38 2000) and lot sizing models based on queuing theory (e.g. Karmarkar 1987, Suri et al.
39 1993, Lambrecht et al. 1998), are more appropriate to capture the complexity of a
40 stochastic environment. The combination of such models are used to analyse
41 integrated production-inventory systems where inventory replenishment rules trigger
42 production and can cause queues in the manufacturing environment (e.g. Van Nyen et
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3 al. 2005). Hence, one should be careful in the choice of model and verify that the
4 underlying assumptions and trade-offs are a good approximation of the reality. For a
5 further discussion of deterministic versus stochastic planning models, we refer to
6 Karmarkar (1993). Zhang and Graves (1997) incorporate random machine failures in
7 their analysis of cyclic schedules for products with a stable demand rate. Some
8 research has been done to incorporate uncertainty into the dynamic lot sizing problem
9 as well such as stochastic demand (Bookbinder and Tan 1988, Sox and Muckstadt
10 1996, 1997, Sox et al. 1999, Tarim and Kingsman 2004, Guan et al. 2006), stochastic
11 lead times (Nevison and Burstein 1984), uncertainty in demand timing (Burstein et al.
12 1984, Gutiérrez et al. 2004), or a combination of demand and supply uncertainty
13 (Anderson 1989).
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24 Finally, the interaction between modeling and algorithms will play an important role
25 in future research. The inclusion of industrial concerns lead to larger and more
26 complex models and consequently more complex algorithms are needed to solve them.
27 Solution approaches for integrated models will be based on previous research on the
28 separate models. Existing knowledge about the structure and properties of a specific
29 subproblem can be exploited in solving integrated models. Lot sizing problems are
30 challenging because many extensions are very hard to solve. Jans and Degraeve
31 (2005) review several techniques to tighten the formulations (Dantzig-Wolfe
32 decomposition, Lagrange relaxation, cutting planes and variable redefinition) and to
33 obtain good quality solutions using (meta-) heuristics. The development of algorithms
34 based on the combination of some of these techniques has already led to promising
35 results. Vanderbeck (1998) combines branch-and-price and cutting planes for solving
36 the CLSP. Dantzig-Wolfe decomposition can be combined with Lagrange relaxation
37 to speed up the column generation process, either by using Lagrange relaxation to
38 solve the master (Cattrysse et al. 1993, Jans and Degraeve 2004^a) or by using
39 Lagrange relaxation to generate new columns (Degraeve and Jans 2003). To obtain
40 stronger bounds, Lagrange relaxation is applied to a variable redefinition
41 reformulation (Jans and Degraeve 2004^b). Many more opportunities for combining
42 algorithms are still largely unexplored.
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