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► **To cite this version:**

T. Widemann, B. Sicardy, R. Dusser, C. Martinez, W. Beisker, et al.. Titania's radius and an upper limit on its atmosphere from the September 8, 2001 stellar occultation. *Icarus*, 2009, 199 (2), pp.458. 10.1016/j.icarus.2008.09.011 . hal-00506795

HAL Id: hal-00506795

<https://hal.science/hal-00506795v1>

Submitted on 29 Jul 2010

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Accepted Manuscript

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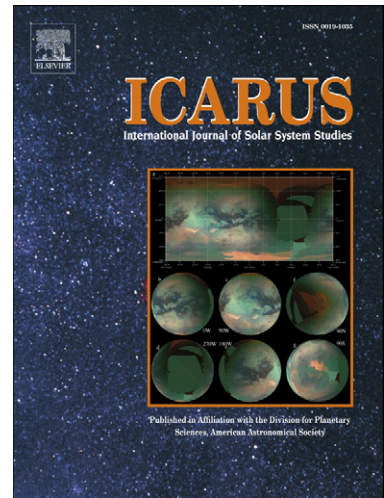
PII: S0019-1035(08)00340-0
DOI: [10.1016/j.icarus.2008.09.011](https://doi.org/10.1016/j.icarus.2008.09.011)
Reference: YICAR 8771

To appear in: *Icarus*

Received date: 14 April 2008
Revised date: 1 August 2008
Accepted date: 22 September 2008

Please cite this article as: T. Widemann et al., Titania's radius and an upper limit on its atmosphere from the September 8, 2001 stellar occultation, *Icarus* (2008), doi: [10.1016/j.icarus.2008.09.011](https://doi.org/10.1016/j.icarus.2008.09.011)

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Accepted version - October 17, 2008

**Titania's radius and an upper limit on its atmosphere
from the September 8, 2001 stellar occultation**

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Accepted for publication in *Icarus*, MS I10463

Manuscript pages : 30

Tables : 5 ; Figures : 17

– 2 –

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ABSTRACT

On September 8, 2001 around 2h UT, the largest Uranian moon, Titania, occulted Hipparcos star 106829 (alias SAO 164538, a $V=7.2$, K0 III star). This was the first-ever observed occultation by this satellite, a rare event as Titania subtends only 0.11 arcsec on the sky. The star’s unusual brightness allowed many observers, both amateurs or professionals, to monitor this unique event, providing fifty-seven occultations chords over three continents, all reported here.

Selecting the best 27 occultation chords, and assuming a circular limb, we derive Titania’s radius: $R_T = 788.4 \pm 0.6$ km ($1-\sigma$ error bar). This implies a density of $\rho = 1.711 \pm 0.005$ g cm $^{-3}$ using the value $GM = (2.343 \pm 0.006) \times 10^{11}$ m 3 sec $^{-2}$ derived by Taylor (1998). We do not detect any significant difference between equatorial and polar radii, in the limit $r_{\text{eq}} - r_{\text{po}} = -1.3 \pm 2.1$ km, in agreement with *Voyager* limb image retrieval during the 1986 flyby.

Titania’s offset with respect to the DE405 + URA027 (based on GUST86 theory) ephemeris is derived : $\Delta\alpha_T \cos(\delta_T) = -108 \pm 13$ mas and $\Delta\delta_T = -62 \pm 7$ mas (ICRF J2000.0 system). Most of this offset is attributable to a Uranus’ barycentric offset with respect to DE405, that we estimate to be : $\Delta\alpha_U \cos(\delta_U) = -100 \pm 25$ mas and $\Delta\delta_U = -85 \pm 25$ mas at the moment of occultation. This offset is confirmed by another Titania stellar occultation observed on August 1st, 2003, which provides an offset of $\Delta\alpha_T \cos(\delta_T) = -127 \pm 20$ mas and $\Delta\delta_T = -97 \pm 13$ mas for the satellite.

The combined ingress and egress data do not show any significant hint for atmospheric refraction, allowing us to set surface pressure limits at the level of 10-20 nbar. More specifically, we find an upper limit of 13 nbar ($1-\sigma$ level) at 70 K and 17 nbar at 80 K, for a putative isothermal CO $_2$ atmosphere. We also provide an upper limit of 8 nbar for a possible CH $_4$ atmosphere, and 22 nbar for pure N $_2$, again at the $1-\sigma$ level.

We finally constrain the stellar size using the time-resolved star disappearance and reappearance at ingress and egress. We find an angular diameter of 0.54 ± 0.03 mas (corresponding to 7.5 ± 0.4 km projected at Titania). With a distance of 170 ± 25 parsecs, this corresponds to a radius of 9.8 ± 0.2 solar radii for HIP 106829, typical of a K0 III giant.

Subject headings: Occultations ; Uranus, satellites ; Satellites, shapes ; Satellites, dynamics ; Ices ; Satellites, atmospheres

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1. Introduction

Among the various techniques used to probe the physical properties of distant objects in the solar system, ground-based stellar occultations are especially powerful. They provide kilometric accuracies or better on sizes and shapes, and may reveal tenuous atmospheres down to a few tens of nbar, as stellar rays are differentially refracted by a possible rarefied gas near the surface. On September 8, 2001 the bright ($V=7.2$) Hipparcos-catalog star HIP 106829 – a K0 III giant – was occulted by Titania, the largest Uranian satellite (Table 1), which angular diameter subtends 0.11 arcsec only on the sky. This rare event was independently predicted by Jean Meeus (Belgium) in 1999 and later by one of us (Claudio Martinez, Argentina) in 2001.

A great variety of observations were made using both small portable telescopes and larger, fixed instruments. The brightness of HIP 106829 allowed an exceptionally high number of observers to gather timings for the event, and light curves for some of them, using a wide variety of acquisition systems and timing techniques ; proper motion and parallax measurements in Hipparcos and Tycho-2 catalogs provided prediction of the stellar position in the International Celestial Reference System (ICRS) at the time of event. More than eighty reports from about seventy stations were gathered, spanning Western Europe, various islands in the northern Atlantic ocean and Caribbean region, as well as several countries in North and South America (Figures 1-3 and Table 2).

The main goals of the observations were to (i) determine Titania’s radius and possible oblateness ; (ii) determine Titania’s offset with respect to the DE405 + URA027 ephemeris ; (iii) to search for an atmosphere around Titania, or derive significant constraints (upper limits) on an atmosphere.

Another important and unique aspect of this observation is that our determination of Titania’s radius can be compared to remote sensing observations by the *Voyager* spacecraft during its January 1986 flyby. It allows us to validate a ground-based method for which a sub-kilometric accuracy is usually claimed. We determine an upper limit for a pure CO₂ atmosphere, along with other possible gaseous constituents (CH₄ and N₂) on Titania.

We finally address the ability of the occultation technique to probe tenuous atmospheres down to the ~ 10 nb level or below in distant solar system objects. As pressure levels detected during refractive occultations are inversely proportional to distances, we discuss how this method would quantitatively apply to the detection and characterization of atmospheres of trans-Neptunian objects at a few nanobar levels.

After a presentation and discussion of observing and timing techniques and limitations (Section 2), we derive the stellar diameter in Section 3, as a few stations could record individual images of the star as it disappeared (ingress) and re- appeared (egress) from behind Titanias limb. Titania’s offset with respect to the DE405 + URA027 ephemeris is given in Section 4. Titania’ size and an upper limit for its oblateness is provided in Section 5. Upper limits for various types of atmospheres are given in Section 6, before concluding remarks in Section 7.

2. Occultation chords

2.1. Circumstances of the event

The observation of this occultation was attempted from more than seventy ground-based stations, totalizing more than eighty reports (Table 2). Note that not all stations actually recorded the event, due to weather conditions, technical problems, or being out of the shadow path. Figure 1 shows a post-event reconstruction of Titania’s shadow trajectory on Earth. Titania’s shadow was cast on Earth’s night side at a velocity of 20.92 km s^{-1} in the plane of the sky, yielding for a maximum possible duration about 75 s. The shadow first swept at low elevation over densely populated areas of Western Europe: France, UK, Italy, Portugal, Spain, and Portugal/Madeira; Northern Africa: Morocco, Algeria, and Spain/Canary Islands (Figure 2). It was then visible at high elevation from the Caribbean: Aruba, Barbados, France/Martinique, Trinidad and Tobago, and finally South America: Ecuador, Venezuela, while being attempted from North America: Mexico and USA (Figure 3). The Moon was not visible in the sky at that moment, thus causing no interference with observations.

Among the 70 or so observing stations, nine were clouded out: Quito (Ecuador), Pompiano (Italy), Madeira and Funchal (Portugal), Santa Margarita (Trinidad), Mérida and other three amateur stations in Venezuela. Six were outside the shadow: Algiers (Algeria), Monterrey (Mexico), Greenbelt (USA), Temara (Morocco), Granada and Canary Islands (Spain) see Table 2.

Among all stations, the highest elevation recording was at Cerro El Bueran near Cuenca (Ecuador) at 3987 m altitude, followed by Llano del Hato (Mérida, Venezuela) at 3600 m, and Pic du Midi (France), at 2878 m. Lowest elevation was sea level. The largest telescope were Pic-du-Midi (France) 1.05-m, followed by Observatoire de Haute-Provence (France) 1-m and 0.8-m, Mérida (Venezuela) 0.6-m which was clouded out, and Sabadell-1 (Spain) 0.5-m, while the Granada (Spain) 0.4-m telescope was outside the shadow. A historical refractor telescope built in 1873, the 23.8-cm Mertz refractor in downtown Quito (Ecuador) was also set up for this observation, but was unfortunately clouded out.

2.2. Recording modes

As a wide range of telescope diameters had been used from 1.05-m (France/Pic-du-Midi) to a mere 5-cm (Venezuela/Maracaibo), as well as a large variety of camera devices, acquisition and timing methods, including visual and audio. Only a selection of observations turned out to be relevant for astrometry and limb fitting measurements, among which an even smaller selection consisted in extended lightcurves. A reliable method to constrain astrometry and limb shape of the occulting body is to combine frame by frame analysis and absolute timing capability. Frame by frame acquisition are provided by low-noise CCD cameras from various groups or vendors, such as IOC cameras by IOTA (International Occultation and Timing Association), Audine-series cameras

by AUDE (Association des Utilisateurs de Détecteurs Electroniques), ST-series cameras by SBIG (Santa Barbara Instrument Group), among others, and in some cases, analog video tapes (Table 2).

The timing methods were either GPS-based, internet/internal PC clock, visual or audio (about 25 stations) consisting in either stopwatch visual synchronization to a radio signal (DCF-77 or local/national radio), or audio recording of time signal or beeps, on the acquisition VHS tape or a separate audio recorder with observer's commentary. Absolute timing must be provided by a Global Positioning System (GPS), or an NTP server (Matsuda 1996), directly connected to the file acquisition/recording device or to the PC clock time. Direct reading from the internet, without such precautions, should be avoided even for relative time measurements. Table 2 provides ingress and egress times, the observer's position in terrestrial coordinates, telescope diameter, acquisition instrument, visual recording and timing methods for each individual station.

3. Star properties

To reconstruct the geometry of the event we need (1) the position of the star at epoch, (2) Titania’s ephemeris, (3) the observers’ geocentric coordinates and (4) the timings of the occultation (star ingress and egress) at each station. These timings allow us to reconstruct the 2-D geometry of the stellar occultation by Titania’s disk in the sky plane, and provide the offset between Titania’s actual position and its calculated ephemeris.

3.1. Star position

The ICRS position for star HIP 106829 is provided by the Vizier site (Ochsenbein et al. 2000). This star is not documented as either variable nor multiple in the Hipparcos catalog. Its ICRS position at Hipparcos epoch (1991.25) is $\alpha = 324.55809702^\circ$, $\delta = -14.91006013^\circ$ with error of 0.8 and 0.6 milli-arcsec (mas), respectively. The Hipparcos catalog provides a proper motion of $\mu_\alpha \cos(\delta) = 27.703 \pm 1.314$ mas year⁻¹ and $\mu_\delta = 29.5 \pm 0.72$ mas year⁻¹, while the Tycho 2 catalog gives $\mu_\alpha \cos(\delta) = 28.251 \pm 0.827$ mas year⁻¹ and $\mu_\delta = 29.5 \pm 0.8$ mas year⁻¹. Weighing those proper motions according to errors, we obtain a total motion of $\Delta\alpha \cos(\delta)_{\text{pm}} = 295.516 \pm 7.368$ mas and $\Delta\delta_{\text{pm}} = 310.290 \pm 5.629$ mas between the Hipparcos epoch and the date of occultation (2001.7683).

The annual parallax of the star, from Hipparcos, is $\pi'' = 5.89 \pm 0.91$ mas (Perryman et al. 1997). This yields a further correction of $\Delta\alpha \cos(\delta)_{\text{par}} = -2.294 \pm 0.354$ mas and $\Delta\delta_{\text{par}} = -0.838 \pm 0.130$ mas, and finally:

$$\begin{cases} \alpha = 324.55817850^\circ \pm [\Delta\alpha \cos(\delta) = 7.4\text{mas}] \\ \delta = -14.90997417^\circ \pm [\Delta\delta = 5.7\text{mas}], \end{cases} \quad (1)$$

where the uncertainties essentially come from the propagation of the proper motion error between 1991.25 and 2001. At the distance of Titania, $D = 2.8504 \times 10^9$ km (Table 1), one arcsec corresponds to 13,819 km. Thus, the error bars quoted above correspond to distances of ~ 100 km in the plane of the sky.

3.2. Stellar diameter

A few stations could record individual images of the star as it disappeared (ingress) and re-appeared (egress) from behind Titania’s limb. We have selected the four best light curves in terms of timing accuracy, namely Salinas-1 (0.25-m) and Salinas-2 (0.20-m) in Ecuador, Arikok in Aruba island (0.20-m), and Portimão-1 in Portugal (0.25-m). All four datasets were collected with IOC cameras. An example of lightcurve, obtained with the 25-cm reflector at Salinas-1, is displayed in Figure 4.

Individual fits to each gradual decrease and increase in star intensity have been performed for each of those experiments, providing eight timings (Table 2). Those times correspond to the

instant when the center of the stellar disk intersects Titania’ limb. Prior to the fit, the data were normalized between zero (Titania’ flux only) and unity (flux of Titania plus star outside occultation). The fits include the following steps : (1) Fresnel diffraction by a point-like source at distance $D = 2.8504 \times 10^9$ km from the observer are generated. The numerical scheme used to generate this diffraction pattern is described in details in Roques et al. (1987). Because the IOC’s were used in clear (no filter) mode, convolution with the camera bandwidth were performed. The resulting diffraction pattern is shown in Figure 5, see the thin upper curve ; (2) this profile was convolved by a 2-D stellar disk, taking into account limb darkening. The limb darkening profile was taken from Claret (2000), who provides a four-parameter model for the stellar disk specific intensity I : $I(\mu) = 1 - \sum_{k=1}^4 a_k (1 - \mu^{k/2})$, where $\mu = \cos(\gamma)$, and γ is the angle between the line of sight and the intensity emerging from the stellar surface. Note that the intensity is arbitrarily normalized to unity for $\mu = 1$. For a K0 giant star (effective temperature $T_{eff} = 4750$ K), this author gives : $a_{1,2,3,4} = 0.6699, -0.7671, 1.6405, -0.6607$, respectively ; (3) a final convolution accounts for the instrumental response, namely the fact that each data point actually represents the number of photons received during a finite time step Δt . Examples of such fits to the Salinas-1, Salinas-2 and Arikok lightcurves are shown in Figure 6.

The ingress/egress timings are derived from the classical minimization of:

$$\chi^2 = \sum \frac{(\Phi_{i,obs} - \Phi_{i,cal})^2}{\sigma_i^2}, \quad (2)$$

where Φ is the flux, “i” refers to the i^{th} data point, “obs” refers to observations, “cal” refers to calculated, and σ_i is the expected 1- σ error of the i^{th} data point. The latter is estimated from the signal fluctuations observed during a typical time interval of 2 mn around the event. Quoted formal errors on timings correspond to an increase of $\Delta\chi^2 = \chi^2 - \chi_{min}^2 = 1$ with respect to the best obtained value, χ_{min}^2 , the so-called 1- σ level, or more precisely, the 68.3% confidence level (Press et al. 1986).

In order to derive the stellar size, we need to align all the eight profiles along a common radial scale. To do so, we force the extremities of the four chords to lie on a common circle, with a reference radius $R_{T,occ} = 788.4$ km corresponding to Titania’s best fit value later determined in Section 5. This reference radius is arbitrary since small timing errors and/or topographic features along Titania’s limb may induce radial scatter at the km-level. This procedure is valid, however, as long as we are interested in the local behavior of the light curve during ingress and egress of the star.

Figure 5 shows the data points plotted versus distance to Titania’s shadow center. As noted before, the thin upper line shows the diffraction profile expected from a point-like star (but after convolution by the receptor bandwidth). Note that the main fringe has a width at half maximum of about 1 km. This is expected from the classical expression of the Fresnel scale, $L_F = \sqrt{\lambda D/2}$, where λ is the wavelength of observation and D is the distance to Titania. Thus, L_F varies from 0.9 to 1.1 km when λ varies from 0.6 to 0.9 μm (the typical coverage of IOC cameras), yielding the

kilometric scale quoted above.

A χ^2 minimization similar to that of Eq. 1 provides the best fit stellar diameter projected at Titania, $D_\star = 7.5 \pm 0.4$ km, corresponding to an angular diameter of 0.54 ± 0.03 mas. The quoted error bar corresponds again to a variation $\Delta\chi^2 = 1$ above the best fit.

Thus, the occultation pattern is dominated by stellar diameter, not by diffraction. Note, however that the formal error bars on ingress/egress times are of the order of 0.010-0.035 sec, corresponding to radial errors of 0.1-0.7 km depending on the star velocity perpendicular to Titania's limb. Thus, and at least for stations where individual images are available, sub-km radial errors can be achieved.

The stellar diameter obtained here can be compared to independent estimations, e.g. using the formulae of van Belle (1999). The magnitudes provided by the Simbad astronomical database (Wenger et al. 2000) are $m_B = 8.24$, $m_V = 7.20$, $m_J = 5.45$, $m_H = 4.90$, $m_K = 4.75$, from which we get an angular diameter of 0.59 mas, with typical errors of 10-20%. This is compatible with our determination, although with a larger error bar. The annual parallax of the star is 5.89 ± 0.91 mas (Perryman et al. 1997), corresponding to a distance of 170 ± 25 parsecs. Hence, our determination of the angular diameter yields a stellar radius of 9.8 ± 0.2 solar radii, where most of the error bars comes from the error on the annual parallax. This radius is typical of a K0 III giant star, for which $\log R/R_\odot = +1.2$ (Allen 1976).

4. Titania’s ephemeris offset

4.1. The September 8, 2001 occultation event

We first determine Titania’s predicted position for the September 8, 2001 event with Horizons ephemeris provided by NASA’s Jet Propulsion Laboratory (Giorgini et al. 1996). The on-line ephemeris is a combination of the DE405 motion of Uranus, and the URA027 satellite analytical ephemeris derived from the GUST86 theory (Laskar & Jacobson 1987). As indicated in Table 1, it provides (i) the latitude of sub-Earth point at 02:00 UT (8 September 2001), $B = -24.2^\circ$ (IAU convention), (ii) Titania’s north pole position angle, $P = 260.4^\circ$, with respect to the local J2000.0 celestial North, and (iii) the longitude of sub-Earth point, 343.5° (Earth and the Sun being about 1.2° apart as seen from Uranus). This allows us to reconstruct Titania’s orientation in the sky plane, identify the meridian facing Uranus, as shown on Figure 7, and associate a *titaniacentric* latitude to each ingress and egress occultation point, see Table 3. Note that the sub-occultation points provided in Table 3 represent a *subset* of the full dataset, as explained below.

Titania’s south pole was visible from Earth in the celestial East direction. As the Uranian system was moving westward in the sky at the time of occultation, the star ingress occurred in the northern Titania hemisphere, close to equatorial and mid-northern latitudes (Figures 7 *et sequ.*). Egress occurred in the southern Titania hemisphere, at higher planetocentric latitudes than during ingress, in fact near the satellite’s south polar region. Because the titaniacentric elevation of the observer is $B = -24.2^\circ$, the occultation could probe latitudes between $+65.8^\circ$ and -65.8° .

Titania’s offset is derived from a subset of ingress and egress times provided in Table 2. Each time gives the position of the observer in Titania’s shadow at ingress or egress, once the star position at epoch is established (Eq. 1). Titania’s motion in right ascension and declination is interpolated using a second-order polynomial, fitting twenty position steps calculated every minute and bracketting the event.

Practically, and owing to the wide variety of methods used here (CCD imaging, video, driftscan, visual, etc...), we have to establish selection criteria on the timings provided by the observing teams, in order to derive an accurate ephemeris offset through limb fitting.

We start with all the occultation chords provided in Table 2, using all possible timings at face value. The resulting fifty-seven chords are shown in Figure 7. Some of them have clearly wrong durations, due to various kinds of errors (wrong time base, confusions due to the nearby, brighter Uranus, especially for visual observations, etc...). Several chords appear to have correct durations, though, but are shifted in time due to errors in absolute time setup (due *e.g.* to delays of internet clocks, personal reaction timelags from manual stopwatch, misprints when writing reports, etc...). It is impossible to retrieve the exact origin of all those time shifts, and of course, to correct them afterwards. Such chords may be of interest, though, as their durations are correct to within a fraction of a second, *i.e.* a few kilometers in length. As such they can be included in a circular fit to Titania’s limb, as described in the next Section.

Thus, we have shifted all the chords along the direction of motion, so that all the chords have a common mediatrix¹. If Titania’s limb is circular and all the relative timings are correct, then all the extremities of the chords should lie on a common circle, after this procedure has been applied. Because of timing errors, as alluded to just before, and also due to possible topographic features along the limb, radial residuals $\Delta r = r_{i,obs} - r_{ref}$ with respect to a common circle of radius r_{ref} are observed.

To proceed forward, we have selected chords which have a residual radial dispersion $\Delta r < \pm 10$ km. This corresponds to an error of 0.5 to 2 sec in chord duration, depending on the observer’s location projected on Titania’s limb. The 10-km limit is of course arbitrary, but it appears that the most deviant chords are also those which are derived from either one, or a combination of the following observing circumstances : (i) smaller instruments (less than 15 cm in diameter), (ii) large time steps (no fraction of seconds available), (iii) documented problems, and/or (iv) visual observations, for which post-occultation corrections are impossible to make.²

This step eliminates 14 chords, leaving us with 43 chords, shown in Figure 8. The circle fitted to the chord extremities has been obtained iteratively. First we fit a circle to the chord extremities, then we shift the chords so that all their mediatrixes coincide with the circle diameter perpendicular to stellar motion, repeating that operation till the circle center varies by less than one kilometer. Once this is achieved, we obtain Titania’s offset with respect to its predicted position.

This offset, readily visible in Figure 8, amounts to $\Delta f = -1493$ km (sign meaning toward celestial west) and $\Delta g = -862$ km (toward celestial south). The internal accuracy of this offset is less than ~ 10 km, after the selection criterium on Δr for the 43 chords, described before. This corresponds to less than one milli-arc-second (1 mas = 13.8 km at Titania’s distance) and thus negligible compared to the accuracy on the star position of $\Delta\alpha \cos(\delta) = 7.4$ mas and $\Delta\delta = 5.7$ mas, see Eq. 1. In other words, the error bars on the offset is dominated by error bars on the star position, and not by the accuracy of our fit. With a range of 2.8504×10^9 km, Titania’s offset with respect to the DE405 + GUST86 prediction amounts to:

$$\begin{cases} \Delta\alpha_T \cos(\delta_T) = & -108 \pm 7 \text{ mas} \\ \Delta\delta_T = & -62 \pm 6 \text{ mas.} \end{cases} \quad (3)$$

Part of this offset is due to a general offset of Uranus barycenter with respect to DE405, and part is due to an offset in Titania’s motion around Uranus. To find out which of Uranus’ or Titania’s offsets prevail, let us consider some alternative ephemerides to DE405 and GUST86. While GUST86 was

¹The mediatrix of two points in a plane is the line equidistant to those two points.

²Two stations, however, have large radial residuals, while good accuracy is expected since ingress and egress timings come from video tapes with 0.15 to 0.35m telescopes. They are the Almerim station (Portugal), with $\Delta t = 1.55$ s corresponding to radial residual $\Delta r = -28.8$ km, for an expected error ≤ 0.1 s, and Sabadell-2 0.15m station (Spain), with $\Delta t = 2.04$ s and $\Delta r = -20.4$ km, for a claimed accuracy of 0.2 s. No explanation has been given for these large residuals.

fitted to observations made from 1911 to 1986, a new theory (“LA07”) has been fitted to more recent observations made from 1948 to 2003 (including Voyager observations) for better predicting the mutual events of 2007, see Lainey (2008).

Titania’s position with respect to Uranus on September 8, 2001 at 02h UT, as given by GUST86, is: $X = 11.0532$ arcsec and $Y = 11.4900$ arcsec, eastward and northward of Uranus ICRS J2000.0 position, respectively. A new theory LA07 gives $X = 11.0456$ arcsec and $Y = 11.5130$ arcsec. This yields a difference LA07 - GUST86 = -8 mas and +23 mas in right ascension and declination, respectively, with typical accuracy of 20-25 mas. This indicates that the offset given above (Eq. 3) is dominated by Uranus barycentric offset. Taking the LA07 theory as reference, our astrometric reconstruction discussed above yields the following Uranus offset, in the sense [our occultation observation minus DE405] of :

$$\begin{cases} \Delta\alpha_U \cos(\delta_U) = & -100 \pm 25 \text{ mas} \\ \Delta\delta_U = & -85 \pm 25 \text{ mas.} \end{cases} \quad (4)$$

A survey made at the Bordeaux meridian transit circle actually shows that Uranus’ offset averaged over several months around September 2001 amounts to: $\Delta\alpha_U \cos(\delta_U) = -98 \pm 10$ mas and $\Delta\delta_U = -122 \pm 10$ mas, see Arlot et al. (2008). This is fully consistent with our result in right ascension (difference of +2 mas with respect to our result), while the difference is barely significant in declination (difference of -37 mas).

We may finally compare the DE405 ephemeris with the newly released IMCCE ephemeris “INPOP06” (Fienga et al. 2008), which improves Uranus ephemeris. We have, in the sense [INPOP - DE405] : $\Delta\alpha_U \cos(\delta_U) = -66$ mas $\Delta\delta_U = -75$ mas. There is now a barely significant difference (+34 mas) in right ascension when compared to our result, and a fully consistent offset in declination (difference +10 mas with our result).

4.2. Additional offset constraints from the Aug. 1, 2003 event

We have a confirmation of this systematic offset from another stellar occultation by Titania, observed on August 1st, 2003 (Figure 9). The star involved, TYC 5806-696-1 ($V=10.3$) has the following ICRF position at epoch, $\alpha = 333.9773096^\circ \pm 20$ mas and $\delta = -11.6156551^\circ \pm 13$ mas (Table 1) with proper motion taken into account as for HIP 106829 on September 8, 2001, but not annual parallax, which is too small to be measured. The 2003 event was observed from two sites, in Mexico and USA, see Table 4 for locations, instrument characteristics and timings. With these two chords, we obtain a radius for Titania of 787.3 km, i.e. 1.1 km smaller than the radius obtained later in this paper, but with an uncertainty of ~ 4 km, vs. a fraction of km obtained with the September 2001 event. So, this occultation does not improve our radius determination presented in the next Section. However, the timing of the event is reliable enough to provide a significant Titania offset of -127 ± 20 mas and -97 ± 13 mas, where error bars come again from uncertainties

on the star position. This offset is fully consistent in right ascension with the offset obtained in 2001 (see Eq. 3), and barely larger – in absolute value – in declination. This difference remains marginal, however, when compared to error bars.

In summary, the offset established for the Sep. 8, 2001 occultation and confirmed by the Aug. 1, 2003 occultation is probably a manifestation of Uranus' offset slowly varying over years with respect to the DE405 ephemeris for the main part, and from Titania's uranocentric orbit for a small part.

5. Titania’s size and upper limit on oblateness

The next step of our analysis involves further selection among observed chords, in order to increase the accuracy on Titania’s size and shape. We keep the observations for which (i) frame by frame data acquisition and timing capability is provided, using a CCD or a video/camcorder equipment and (ii) visual observations and timings reported with radial residuals consistent with $\Delta r < \pm 5$ km, allowing us to obtain an improved timing of the star ingress and egress. Consequently, we eliminate timings obtained from drift scans observations, as the time interval during which the stellar trail disappears is actually affected by the point spread function (PSF). For instance, the occultation durations derived from the two IOC cameras at Salinas 1-2 (Ecuador) agree with each other to within 0.005 sec, while the drift scan observation made at the same site (Salinas-3, Ecuador) shows a large discrepancy of 1.8 sec, see Table 2, corresponding in that case to a difference in chord length of about 30 km. Although it might be possible to correct the effect of PSF convolution in the occultation length, even in that case, estimation of error bars would be problematical.

We noticed that the radial dispersion of the chord extremities show a marked concentration in an interval $\Delta r = \pm 5$ km (Figure 10), with some outliers between 5 and 10 km, that we have withdrawn from the fit. We therefore retained $\Delta r < \pm 5$ km as a selection criterium for the limb fitting analysis. All outliers, from the previous selection of 43 stations, except two, are from visual observations, for which it is now impossible to assess the degree of confidence. For the two remaining stations excluded with that method, Observatoire de Haute Provence (France) and Oeiras (Portugal), no satisfactory explanations have been given for their larger radial residuals.³ In contrast, we kept 13 visual observations reported by experienced observers for which we estimate an accuracy of about 0.2-0.3 sec for the occultation duration (even if the absolute timing may be off by much more than that, as detailed in Table 3). To support why the remaining visual timings may equal the relative accuracy of frame-by-frame recording, one can note in Figure 11 that many remaining visual chords (shown in black solid) are far away from shadow center, which may reduce significantly the projected star velocity perpendicular to the limb down to 6-14 km sec⁻¹, depending on the chord. Consequently, typical errors of 0.2-0.3 translate into radial residuals of typically 1-4 km, *i.e.* less than the 5-km limit we used to discriminate the CCD or video frame-by-frame observations for limb fitting, as explained above.

5.1. Circular fit

Twenty-seven occultation chords are finally kept for a circular limb fit. They consist in a total of 13 visual timing observations, 9 video recordings and 5 CCD recordings, plotted on Figure 11 and listed in Table 3. A first point to note is that even with the stations with the best timing accuracies, the radial residuals to a circular fit are quite larger than the expected accuracy of each

³ $\Delta r = +5.0$ and -8.8 km, respectively.

measurements. For instance, the Salinas-1, Salinas-2, Arikok, Pic du Midi and Portimão-1 chord extremities have formal radial accuracies of 0.1 to 0.4 km, while the observed radial residuals have values of $\Delta r = \pm 2$ km.

This indicates either that we grossly underestimate our error bars, or that this dispersion has a physical origin, not accounted for by our circular fit. This will be discussed later, but we can already mention here that images taken by the *Voyager* spacecraft in 1986 show typical r.m.s. limb radial dispersions of ± 1 km, with peak to peak amplitudes of ± 3 km (Thomas 1988). Our r.m.s. residuals of $\Delta r = \pm 2$ km are thus consistent with the *Voyager* images and are typical of what may be expected from the satellite topography itself, characterized by scarps 2-4 km high and an uneven crust. In other words, the pseudo random radial fluctuations that we observe are likely to be dominated by Titania's topography, not by the uncertainties on the durations of our 27 selected chords. There are only two stations for which the error bars exceed the typical limb radial dispersion, namely the Ponta Delgada (Azores Island, Portugal) and Marinha Grande (mainland Portugal) sites. Their timing accuracy is announced at ± 0.3 and ± 0.5 seconds, respectively, translating into radial accuracy of 3.1 and 4.1 km, respectively.

We now proceed to a circular fit to the extremities of the 27 selected chords. The free parameters of the fit are Titania's radius, $R_{T,occ}$, and the location of shadow center, as given by the offset ($\Delta f, \Delta g$). We define the χ^2 of the fit as:

$$\chi^2 = \sum_{i=1}^{54} \frac{(r_{i,obs} - R_{T,occ})^2}{\sigma_i^2} \quad (5)$$

where the $r_{i,obs}$'s are the 54 radii of the 27 chords extremities.

We will assume that the error σ_i^2 attached to each chord length is imposed by Titania's topography. Our best circular fit to the 27 selected chords then yields a radius $R_{T,occ} = 788.4$ km, with a dispersion of 1.6 km (Figure 11). Since we shifted the chords prior to the fit so that they have a common mediatrix, the two extremities of a given chord have the same radius, by definition. Consequently, there are actually $N = 27$ independent data points, while the fit has $M = 3$ adjusted parameters ($R_{T,occ}$, Δf and Δg), so that the expected minimum value of χ^2 is the number of degrees of freedom, $\chi_{min}^2 = \nu = N - M = 24$.

This value is obtained for $\sigma_i = 2.29$ km, a value that we keep for our error bar determination, except for the Ponta Delgada and Marinha Grande chords, for which we take 3.1 and 4.1 km, as explained before. Exploring the effect of fixed values of $R_{T,occ}$ on χ^2 , while keeping Δf and Δg as free parameters, we obtain the so-called 1- σ error bar (68.3% confidence level) for $R_{T,occ}$, such that $\Delta\chi^2 = \chi^2 - \chi_{min}^2 = 1$ (Press et al. 1986) :

$$R_{T,occ} = 788.4 \pm 0.6 \text{ km.} \quad (6)$$

This radius is fully compatible with the value derived by Thomas (1988) from the *Voyager*

images $R_{T,Voy} = 788.9 \pm 1.8$ km. This latter value is actually an average of seven limb profiles, none of them being *a priori* the one that we observed during the occultation.

We finally derive a mean density $\rho = 1.711 \pm 0.005$ g cm⁻³ for Titania, based on Taylor (1998) estimate of $GM = 2.343 \times 10^{11}$ m³ sec⁻² (Table 1). It lies within previously published value using *Voyager's* radius $R_{T,Voy} = 788.9 \pm 1.8$ (Thomas 1988) and improves by a factor of 10 the value of $\rho = 1.71 \pm 0.05$ g cm⁻³ by Jacobson et al. (1992). This density represents a silicate to ice ratio of ~ 0.5 (Brown et al. 1991), a much higher silicate fraction than the satellites of Saturn, in agreement with the observed relative depletion of surface ice in the Uranian system, that we discuss in Section 6.

5.2. Upper limit on oblateness

Estimating the satellite oblateness is hampered by the fact we have shifted the occulting chords in time, so that they have a common mediatrix. In doing so, we impose the radial residuals to be the same at each extremity of a given chord, *i.e.* at two different latitudes. This tends to mix up any low frequency pattern present along the limb. This effect is visible in Figure 12, where the points come by pairs with same radii.

However, we may give a rough estimation for the upper limit on oblateness in a simplified situation, namely assuming that Titania is an ellipsoid of revolution, with smaller axis aligned with its pole. At lowest order in oblateness $f = (r_{eq} - r_{po})/r_{eq}$, where r_{eq} (resp. r_{po}) is the equatorial (resp. polar) radius, the limb shape is given by $r = r_{eq}[1 - f \sin^2 \phi]$, where r is the radius at latitude ϕ . This limb profile is an even function of ϕ , so that the points of Figure 12 can be all folded in the interval $[0^\circ, 90^\circ]$. Furthermore, each pair of point corresponding to one chord can be replaced by a unique point with same radial residual, at a latitude which is the average of the latitudes of the two points.

Figure 13 shows the result of this operation. When the function $r_{eq}[1 - f \sin^2 \phi]$ is fitted to these data points, the overall radial residual is decreased. However, since one new free parameter is added (namely, the oblateness f), the χ^2 per degree of freedom of the fit actually increases, showing that no significant oblateness is detected in our data set. More precisely, we obtain an equator to pole difference of $r_{eq} - r_{po} = -1.3 \pm 2.1$ km, while the equatorial radius remains close to the circular fit value, $r_{eq} = 788.0 \pm 0.9$ km.

A rough estimation of the oblateness f of a slowly rotating fluid satellite is given by $f \sim q$ (Murray & Dermott 1999), where q is the dimensionless rotational factor $q = (4\pi^2 R^3)/(GMP^2) \sim 1.5 \times 10^{-4}$, using the GM and rotation period $P = 8.706$ days (Table 1). This would imply a difference $r_{eq} - r_{po} \sim 0.1$ km, *i.e.*, about 10 times smaller than the upper limit for $r_{eq} - r_{po}$ derived above from our data set. This finding is in agreement with *Voyager* limb image analysis by Thomas (1988) who find no observational evidence for oblateness. Another attempt was made in our analysis, assuming that Titania is elongated along the line joining the satellite to the planet

(*i.e.* along the suburanian point labelled “SU” in Figure 7). In this case, however, all the suboccultation points along the limb lie between 63° and 90° away from the point SU. This is a too narrow interval to yield any significant constraint on a possible elongation towards Uranus. Other directions of elongation might be possible, but the shifts of the chords described earlier make impossible a detection of such distortions.

Note that without absolute timing shifts discussed before, we would have reached a much more stringent upper limit for Titania’s oblateness. This is a strong argument for the importance of getting *absolute* timing accuracy at the 0.1-sec level or less.

6. Limits on an atmosphere around Titania

In this section, we use the occultation data to constrain the existence of an atmosphere around Titania. Potential origins for such an atmosphere include (i) solar-induced ice sublimation, which is strongly dependent on the surface temperature (ii) outgassing associated with hot-spot cryovolcanism. As discussed hereafter, the high sensitivity of occultation lightcurves to vertical refractivity variations allows us to derive significant constraints (upper limits) on an atmosphere.

6.1. Derivation of an initial atmospheric limit based on radius

A remarkable feature of this particular event, is the fact that we can directly compare a ground-based observation with remote sensing observations from a nearby spacecraft. The excellent agreement between the two results is a strong illustration of the power of ground-based observations, for which kilometeric accuracies or better can be reached.

We used the *Voyager* radius of $R_{T,Voy} = 788.9 \pm 1.8$ km as a reference as its value derived by Thomas (1988) results from images acquired during the 1986 flyby with no detectable atmospheric effect on the limb at close range. The difference of radii derived from our experiment and from *Voyager* is $\Delta R = R_{T,occ} - R_{T,Voy} = -0.5 \pm 1.9$ km is not significant, but can nevertheless be used to set an upper limit of a faint atmosphere around Titania⁴. Such a tenuous atmosphere could actually refract the stellar rays, reducing the shadow radius at Earth, with respect to the actual radius. This effect is illustrated in Figure 14, where various occultation profiles are generated, assuming isothermal ($T = 70$ K) CO₂ atmospheres with surface pressures of 0, 50, 100, 150 and 200 nbar. Those profiles are obtained by ray tracing, using a procedure described in details by Sicardy et al. (2006). The upper limit for the difference between *Voyager*'s and our measurement, $\Delta R \leq 2.4$ km sets a 1- σ upper limit of $p_s = 45$ nbar for the surface pressure of such a CO₂ atmosphere. One must be careful, however, that we did not observe the same limb as *Voyager* did, and that difference of 3-4 km are still possible, depending on the geometry of observation (Thomas 1988). So, a value of $p_s = 70$ nbar seems a safer 1- σ upper limit for a CO₂ atmosphere at $T = 70$ K, based on the upper limit of apparent shrinking of Titania's mean radius, see Figure 14. A tighter upper limit for an atmosphere around Uranus' largest moon can be inferred from the stellar flux refracted prior to, and after the stellar occultation by Titania's limb, as we examine in the next subsection.

⁴Ray bending by Titania's gravitational mass, due to general relativity, amounts to only 50 meters or so at the Earth's distance, and is thus irrelevant at our level of accuracy.

6.2. Upper limits on the surface pressure based on lightcurves

Interpreting stellar occultation lightcurves in terms of atmospheric properties requires an assumption on its composition. A sublimation atmosphere reflects the composition of the surface. Near infrared spectroscopy has demonstrated the presence of water ice (e.g. Grundy et al. 1999 for the most recent study) and carbon dioxide (Grundy et al. 2006) on the surface of Titania (and Ariel, Umbriel and Oberon, with no detected CO₂ on Oberon). While H₂O ice is clearly involatile, CO₂ ice stability against sublimation over the course of a seasonal cycle of Titania can be considered. As shown by Grundy et al. (2006), its vapor pressure of about $p_{CO_2} = 1.6 \times 10^{-4}$ nbar for a mean surface temperature of $T = 70$ K is sufficient to induce significant sublimation-condensation cycles and seasonal redistribution.

We thus consider a CO₂ atmosphere as our baseline case. Deriving a constraint on the surface pressure requires the knowledge of carbon dioxide molecular refractivity (Table 1) and an assumption on the vertical temperature profile. We assumed isothermal atmospheres at temperatures of 60, 70, and 80 K. These are in the range of (i) the H₂O ice temperatures measured from the near-IR spectra (Grundy et al. 1999) and (ii) the mean 20- μ m brightness temperature (70 ± 7 K) determined by Brown et al. (1982). Due to the very small pressures involved, the atmosphere must be transparent to surface thermal radiation, so we did not consider tropospheric or mesospheric cooling. With a surface gravity of 0.38 m s^{-2} , the assumed surface temperatures correspond to pressure scale heights of 30, 34, and 39 km respectively.

To perform model fitting we have combined the stellar fluxes observed in four of our IOC datasets in Arikok (Aruba), Salinas-1 and -2 (Ecuador) and Portimão-1 (Portugal). All data points with $r > 792$ km were included in the fit, to the limit of significant signal drop due to partial occultation of the stellar disk by the limb, so the star remains essentially unocculted. Ingress and egress measurements were folded over, and data sets from different stations were separately fitted, taking into account their individual noise levels. The synthetic lightcurves were obtained by ray tracing, see Sicardy et al. (2006) for details. We calculate the χ^2 while keeping CO₂ ground pressure as free parameter, and determine the upper limit at $1-\sigma$ error bar (68.3% confidence level) so that $\Delta\chi^2 = \chi^2 - \chi_{\min}^2 = 1$. For a pure CO₂ isothermal atmosphere with $T = 60$ K, we find a maximum surface pressure $p = 9$ nbar. The corresponding atmospheric column density is 0.132 cm-amagat. The $1-\sigma$ pressure upper limit is 13 nbar for $T = 70$ K, and $p = 17$ nbar for $T = 80$ K (Table 5). Figure 15 illustrates the effect on the light curve of an isothermal, $T = 80$ K pure CO₂ atmosphere. In this figure, the shaded area shows the difference between this upper-limit of $1-\sigma$ and an airless model. As the contribution to errors of each data point depends not only of its uncertainty, but also on the relative velocity of the star, perpendicularly to the limb, we have binned the folded-over data from the four stations at constant radius intervals $\Delta r \sim 20$ km. Note that the binning has been performed for plotting purposes only in order to readily reflect the contribution of each lightcurve to the atmospheric detection (Figure 15).

We explored the possibility of other, more volatile, constituents, namely CH₄ and N₂. Al-

though such compounds are unlikely to be present as a permanent, stratified atmosphere given the instability of their surface frosts (see below), they could be temporarily present as possible products of outgassing associated with internal heating and cryovolcanism. For a pure CH_4 atmosphere, we assumed a “Pluto-like” stratosphere, produced by absorption of solar near-IR radiation. For definiteness, we adopted a temperature profile increasing from $T = 70$ K at the surface to an isothermal $T = 110$ K above 20 km. The resulting scale height is $H = 95$ km at the surface. In this case, the 1- σ detection upper limit is $p = 8$ nbar (Figure 16), corresponding to an atmospheric column density of 0.44 cm-amagat. For a pure N_2 atmosphere, assumed isothermal at 70 K (scale height $H = 55$ km), we find an upper limit $p = 22$ nbar with a corresponding atmospheric column density of 0.55 cm-amagat (Figure 17). On Figures 15 – 17, we have included as a smooth dotted line, the expected lightcurve for a detection event at 3- σ ($p = 18$ nbar for CH_4 , $p = 27$ nbar for CO_2 with $T = 80$ K, $p = 46$ nbar for N_2). Results are summarized in Table 5.

6.3. Discussion

As detailed above, we determine 1- σ upper limits of an atmosphere around Titania at the level of 10-20 nbar. Is it physically significant? For a sublimation equilibrium atmosphere, the equilibrium pressure is a very steep function of the temperature. Based on saturation laws described by Brown and Ziegler (1980), CO_2 vapor pressure p_{CO_2} is orders of magnitude below our derived surface pressure upper limits at $T = 70$ K. However, the surface temperature may be locally higher than this mean value. For example, Hanel et al. (1986) have measured maximum, sub-solar, temperatures of 86 ± 1 K and 84 ± 1 K at Miranda and Ariel from Voyager 2/IRIS measurements. Although no values are reported for Titania in that paper, even slightly higher values may be expected because Titania’s Bond albedo may be slightly lower (0.15 ± 0.02) than Miranda’s (0.18 ± 0.05) and Ariel’s (0.20 ± 0.04), see Helfenstein et al. (1988) and Buratti et al. (1990). In fact, the maximum surface temperature that can be expected on Titania is given by the instantaneous equilibrium with solar input, as :

$$T = \left(\frac{\Phi_0(1 - A_B)}{\epsilon_B \sigma r_h^2} \right)^{1/4} \quad (7)$$

where Φ_0 is the solar constant, A_B is Bond’s bolometric albedo, r_h is the distance to the Sun, σ is Stefan-Boltzmann’s constant and ϵ_B is the bolometric emissivity. With $\epsilon_B = 0.9$, the maximum possible temperature on Titania is 88.6 K. At this extreme temperature, $p_{\text{CO}_2} = 2.9$ nbar (Brown and Ziegler 1980), still a factor of 3-6 lower than the upper limit provided by our measurement. Thus, it is not surprising that we are unable to detect an equilibrium CO_2 atmosphere around Titania. We note also that the *Voyager* measurements were acquired at southern summer solstice, which is the period of maximum surface temperatures (in polar regions).

The situation is very different for N_2 and CH_4 , for which an equilibrium pressure of ~ 10 nbar is reached for temperatures as low as 29 K and 38 K, respectively. However, the problem is rather that Titania is too small to retain N_2 or CH_4 ices against a massive thermal evaporation, given their

high volatility (Jeans escape is proportional to equilibrium vapor pressure). Schaller and Brown (2007a) have recently examined the volatile loss and retention on distant icy (Kuiper Belt) Solar System objects. They find that a ~ 800 km object is able to retain its volatiles (N_2 , CH_4 , CO) over the age of the Solar System only if its “equivalent” temperature (essentially their perihelion temperature) is less than ~ 30 K. Clearly, an equilibrium atmosphere of N_2 and CH_4 is not expected on Titania, consistent with the absence of features due to their ices in its near-infrared spectrum.

Although the above arguments seem to rule out a significant sublimation atmosphere on Titania, there remains, in principle, the possibility of a plume-like atmosphere, similar to Enceladus’ – where the above discussion would apply as well. In Enceladus’ southern pole plume, Cassini/INMS measurements have indeed revealed the presence of volatile and involatile species, namely 91 % H_2O , 4 % N_2 , 3 % CO_2 and 1.6 % CH_4 , with a total pressure in the range $10^{-1} - 10^{-4}$ nbar (Waite et al. 2006). Another estimate of gas density within the plume was obtained from the stellar occultation of γ Orionis on July 14, 2005, observed with Cassini UVIS (Hansen et al. 2006), showing evidence for water vapor absorption, with a slant abundance of $1.5 \times 10^{16} \text{ cm}^{-2}$, and an exponential decline of slant column abundance versus altitude with a scale length of 80 km. From this, a $\sim 9 \times 10^{15} \text{ cm}^{-2}$ vertical column and a $\sim 10^9 \text{ cm}^{-3}$ surface density can be roughly estimated.

Converting this into a surface pressure would require an assumption on the unknown gas temperature, but for a gas temperature in the range 100 - 1000 K, the above numbers typically indicate a 0.01 – 0.1 nbar atmosphere. This remains significantly less than our upper limits. Titania’s surface is poorly constrained by its geological features : comparison with other major Uranian satellites suggests it was globally resurfaced up to 2 Ga ago (Croft & Soderblom (1991), see also Fig. 10 in Zahnle et al. (2003)). Crystalline water deposits may be considered as a possible indicator of recent heating episodes (e.g. Jewitt & Luu (2004)), and relatively high destruction and loss rates of CO_2 ice suggest a possible recent or ongoing source (Grundy et al. 2006). However, the presence of CO_2 ice does not seem to correlate with less-cratered, younger regions and no convincing evidence can be found for outgassing activity. This is opposed to Enceladus, where an age of 10-100 million years is estimated for the southern polar region (Porco et al. 2006), and probably even much younger for the “Tiger stripes” features from which the plume seems to originate.

In summary, the non-detection of an atmosphere of Titania is not surprising. However, our search demonstrates the power of the occultation technique to probe atmospheres down to pressure levels of ~ 10 nbar, much more tenuous than on Pluto or Triton, by typical factors of 10^3 . This is promising in view of the detection of volatile ices on several trans-Neptunian objects (TNO’s). Methane has been clearly detected on dwarf planets Eris, e.g. Licandro et al. (2006b), Makemake formerly known as 2005 FY₉ (Licandro et al. 2006a), and recently on Quaoar (Schaller and Brown 2007b), while the presence of N_2 on Eris is indirectly suggested (Licandro et al. 2006b; Dumas et al. 2007). At a current distance of 43 AU, and with its large size (1260 ± 190 km) which makes its ices marginally stable over the age of the Solar System (Schaller and Brown 2007a), Quaoar appears to be a promising occultation target for an atmosphere.

On a longer term, a monitoring of TNO atmospheres might reveal a seasonal variability due to sublimation-condensation exchanges, as has been observed on Pluto (Elliot et al. 2003; Sicardy et al. 2003; Elliot et al. 2007) and perhaps Triton (Elliot et al. 2000). Remembering also that pressure levels detected during refractive occultations are inversely proportional to distances, and considering that better signal to noise ratios than obtained in this work can be reached, it appears that atmospheres at the nanobar level can be detected for trans-Neptunian objects, using the method described in this paper.

7. Conclusions

The 8 September 2001 stellar occultation by Titania provides a newly determined radius for Titania, $R_T = 788.4 \pm 0.6$ km (1- σ error bar), in agreement with the *Voyager* limb image retrieval which gave $R_T = 788.9 \pm 1.8$ km (Thomas 1988). Our value, combined to the mass $GM = 2.343 \times 10^{11} \text{ m}^3 \text{ sec}^{-2}$ given by Taylor (1998), yields a density of $\rho = 1.711 \pm 0.005 \text{ g cm}^{-3}$. This represents a silicate to ice ratio of ~ 0.5 (Brown et al. 1991), a much higher silicate fraction than the satellites of Saturn, indicating a relative depletion of surface ice in the Uranian satellites. No oblateness is detected, down to a limit of $r_{\text{eq}} - r_{\text{po}} = -1.3 \pm 2.1$ km for the difference between equatorial and polar radii, again in agreement with *Voyager* results. Our measurements demonstrate the capabilities of stellar occultations to retrieve kilometeric or better accuracies for the size of objects in the outer solar system.

HIP 106829 angular diameter is derived : 0.54 ± 0.03 mas, corresponding to 9.8 ± 0.2 solar radii, typical of a K0 III giant star.

The offset of Titania with respect to the DE405 + URA027 (GUST86 theory) is found to be $\Delta\alpha_T \cos(\delta_T) = -108 \pm 13$ mas and $\Delta\delta_T = -62 \pm 7$ mas, in the ICRF J2000.0 reference frame. on Sept. 8, 2001, 2:00 UT. This is mainly attributable to an offset in Uranus barycentric ephemeris, that we estimate to $\Delta\alpha_U \cos(\delta_U) = -100 \pm 25$ mas and $\Delta\delta_U = -85 \pm 25$ mas. Another Titania occultation observed on August 1st, 2003, confirms this finding, as it yields an offset of $\Delta\alpha_T \cos(\delta_T) = -127 \pm 20$ mas and $\Delta\delta_T = -97 \pm 13$ for the satellite.

Our analysis allows to set upper limits to an atmosphere for Titania, at the level of 10-20 nbar for CO_2 , CH_4 or N_2 atmospheres. Although an atmosphere around Titania was not expected, this is 3 orders of magnitude less than the currently observed pressures on Pluto and Triton. As pressure levels detected during refractive occultations are inversely proportional to distances, the upper limits obtained on Titania open promising perspectives to constrain atmospheres of trans-Neptunian objects at a few nanobars level, as developed in this paper.

Acknowledgments. We thank Amanda A. S. Gulbis and an anonymous referee for extensive and constructive comments on the first version of this paper. We wish to thank Francis Kahn, director of the Institut de Recherche pour le Développement (IRD) at Quito, Ecuador, for logistics and advice. This paper is dedicated to the memory of Raymond Dusser, who passed away on September 8th, 2006, five years exactly after the event described here. Raymond actively participated to this campaign, and played a huge role in collecting results and connecting many of the people involved in this event. We vividly remember his crisp and cheerful comments on occultation issues, and others, that he used to send to many of us, over many years.

REFERENCES

- Allen, C.W. 1976, *Astrophysical Quantities*, London: Athlone (3rd edition), p. 209.
- Arlot, J.-E., Dourneau, G. & Le Campion, J.F. 2008, An analysis of Bordeaux meridian transit circle observations of planets and satellites (1997-2007), *A&A*, 484, 869-877
- Brown Jr, G. N. & Ziegler, W.T. 1980, Vapor pressure and heats of vaporization and sublimation of liquids and solids of interest in cryogenics below 1-atm pressure, *Adv. Cryogen. Eng.* 25, 662-670
- Brown, R.H., Cruikshank, D.P. & Morrison D. 1982, Diameters and albedos of satellites of Uranus, *Nature*, 300, 423-425
- Brown, R.H. & Cruikshank, D.P. 1983, The Uranian satellites Surface compositions and opposition brightness surges, *Icarus*, 55, 83-92
- Brown, R.H., Johnson, T.V., Synnott, S., Anderson, J.D., Jacobson, R.A., Dermott, S.F. and Thomas, P.C. 1991, Physical properties of the Uranian satellites, *Uranus*, Bergstrahl, Miner & Matthews Eds., Univ. of Arizona Press : Tucson, pp. 513-527
- Buratti, B., Wong, F., & Mosher, J. 1990, Surface properties and photometry of the Uranian satellites, *Icarus*, 84, 203-214
- Claret, A. 2000, A new non-linear limb-darkening law for LTE stellar atmosphere models : Calculations for $-5.0 < \log[M/H] < +1$, $2000 \text{ K} < T_{\text{eff}} < 50000 \text{ K}$, at several surface gravities, *A&A*, 363, 1081
- Croft, S.K. & Soderblom, L.A. 1991, Geology of the Uranian Satellites, *Uranus*, Bergstrahl, Miner & Matthews Eds., Univ. of Arizona Press : Tucson, pp. 561-628.
- Dumas, C., Merlin, F., Barucci, M. A., de Bergh, C., Hainault, O., Guilbert, A., Vernazza, P. & Doressoundiram, A. 2007, Surface composition of the largest dwarf planet 136199 Eris (2003 UB₃₁₃), *A&A*, 471, 331-334.
- Elliot, J. L., Person, M. J., McDonald, S. W., Buie, M. W., Dunham, E. W., Millis, R. L., Nye, R. A., Olkin, C. B., Wasserman, L. H., Young, L. A. & 8 coauthors, 2000, The Prediction and Observation of the 1997 July 18 Stellar Occultation by Triton: More Evidence for Distortion and Increasing Pressure in Triton's Atmosphere, *Icarus*, 148, 347-369
- Elliot, J.L., Ates, A., Babcock, B.A., Bosh, A.S, Buie, M.W. et al. 2003, The recent expansion of Pluto's atmosphere, *Nature*, 424, 165-168
- Elliot, J. L., Person, M. J., Gulbis, A. A. S., Souza, S. P., Adams, E. R., Babcock, B. A., Gangestad, J. W., Jaskot, A. E., Kramer, E. A., Pasachoff, J. M., Pike, R. E., Zuluaga, C. A., Bosh, A. S., Dieters, S. W., Francis, P. J., Giles, A. B., Greenhill, J. G., Lade, B., Lucas, R. & Ramm, D. J. 2007, Changes in Pluto's Atmosphere: 1988-2006, *AJ*, 134, 1-13

- Fienga, A., Manche, H., Laskar, J. & Gastineau, M. 2008, INPOP06: a new numerical planetary ephemeris, *A&A*, 477, 315-327
- Giorgini J.D., Yeomans D.K., Chamberlin A.B., Chodas P.W., Jacobson R.A., Keesey M.S., Lieske J.H., Ostro S.J., Standish E.M., & Wimberly R.N. 1996, JPL HORIZONS On-Line Solar System Data and Ephemeris Computation Service, *Bull. Am. Astron. Soc.*, 28(3), 1158. JPL/Horizons website as of Jul. 1, 2008 : <http://ssd.jpl.nasa.gov/horizons.html> .
- Grundy et al. 1999, Near-Infrared Spectra of Icy Outer Solar System Surfaces: Remote Determination of H₂O Ice Temperatures, *Icarus*, 142, 536-549
- Grundy, W.M., Young, L.A., Spencer, J.R., Johnson, R.E., Young, E.F. & Buie, M.W. 2006, Distributions of H₂O and CO₂ ices on Ariel, Umbriel, Titania, and Oberon from IRTF/SpEx observations, *Icarus*, 184, 543-555
- Hanel, R., Conrath, B., Flasar, F.M., Kunde, V., Maguire, W., Pearl, J., Pirraglia, J., Samuelson, R., Cruikshank, D., Gautier, D., Gierasch, P., Horn, L., & Schulte, P. 1986, Infrared observations of the Uranian system, *Science*, 233, 70-74
- Hansen, C.J., Esposito, L., Stewart, A.I.F., Colwell, J., Hendrix, A., Pryor, W., Shemansky, D. & R. West 2006, Enceladus' Water Vapor Plume, *Science*, 311, 1422-1425
- Helfenstein, P., Ververka, J. & Thomas, P. C 1988, Uranus satellites - Hapke parameters from Voyager disk-integrated photometry, *Icarus*, 74, 231-239
- Jacobson, R.A., Campbell, J.K., Taylor, A.H. & Synnott, S.P. 1992, The masses of Uranus and its major satellites from Voyager tracking data and Earth-based Uranian satellite data, *AJ*, 103, 2068-2078
- Jewitt, D.C. and Luu, J. 2004, Crystalline water ice on the Kuiper belt object (50000) Quaoar, *Nature*, 432, 731-733.
- Johnson, T.V., Brown, R.H. & Pollack, J.B. 1987, Uranus satellites – Densities and composition, *J. Geophys. Res.*, 92, 14884-14894
- Lainey, V. 2008, *Planet. Space Sci.*, submitted.
- Laskar, J., & Jacobson, R.A. 1987, GUST86 - an analytical ephemeris of the Uranian satellites, *A&A*, 188, 212-224
- Licandro, J., di Fabrizio, L., Pinilla-Alonso, N., de Leon, J., & Oliva, E. 2006a, The methane ice rich surface of large TNO 2005 FY₉ : a Pluto-twin in the trans-Neptunian belt?, *A&ALett.*, 445, L35-L38.
- Licandro, J., Grundy, W.M., Pinilla-Alonso, N., & Leisy, P. 2006b, Visible spectroscopy of 2003 UB₃₁₃ : evidence for N₂ ice on the surface of the largest TNO?, *A&ALett.*, 458, L5-L8.

- Matsuda, K. 1996, Time keeping office and NTP servers, *Astron. Her.*, Vol. 89, No5, pp. 210-215.
Network Time Protocol website as of Jul. 1, 2008 : <http://www.ntp.org>
- Murray, C.D., & Dermott, S.F. 1999, *Solar System Dynamics* (Cambridge University Press)
- Ochsenbein F., Bauer P., & Marcout J. 2000, *A&AS*, 143, 221. VizieR website as of Jul. 1, 2008 :
<http://vizier.u-strasbg.fr>
- Perryman M.A.C., et al. 1997, *The Hipparcos Catalogue*, *A&A*, 323, L49-L52
- Porco, C.C., Helfenstein, P., Thomas, P.C., Ingersoll, A.P., et al 2006, Cassini Observes the Active South Pole of Enceladus, *Science*, 311, 1393.
- Press, W. H., Flannery, B. P., Teukolsky, S A., & Vetterling, W. T. 1986, *Numerical Recipes* (Cambridge University Press)
- Roques, F., Moncuquet, M., & Sicardy, B. 1987, Stellar occultations by small bodies : diffraction effects, *AJ*, 93, 1549-1558
- Schaller, E.L. & Brown, M.E. 2007a, Volatile loss and retention on Kuiper Belt Objects, *ApJ*, 659, L61-L64
- Schaller, E.L. & Brown, M.E. 2007b, Detection of Methane on Kuiper Belt Object (50000) Quaoar, *ApJ*, 670, L49-L51
- Sicardy, B., Widemann, T., Lellouch, E., Veillet, C., Cuillandre, J.-C et al. 2003, Large Changes In Pluto's Atmosphere As Revealed By Recent Stellar Occultations, *Nature*, 424, 168-170
- Sicardy, B., Colas, F., Widemann, T., Bellucci, A., Beisker, W., Kretlow, M., Ferri, F., Lacour, S., Lecacheux, J., Lellouch, E., Pau, S., Renner, S. et al. 2006, The two Titan stellar occultations of 14 November 2003, *J. Geophys. Res.*, Volume 111, Issue E11, E11S91.
- Taylor, D.B. 1998, Ephemerides of the five major Uranian satellites by numerical integration, *A&A*, 330, 362-374
- Thomas, P.C. 1988, Radii, shapes, and topography of the satellites of Uranus from limb coordinates, *Icarus*, 73, 427-441
- van Belle, G.T. 1999, Predicting stellar angular sizes, *Publ. Astron. Soc. Pac.*, 111, 1515-1523
- Waite, J. H., Combi, M. R., Ip, W.-H., Cravens, T. E., McNutt, R. L., Kasprzak, W., Yelle, R., Luhmann, J. et al. 2006, Cassini Ion and Neutral Mass Spectrometer : Enceladus Plume Composition and Structure, *Science*, 311,1419-1422
- Washburn, E. W. 1930, *International Critical Tables of Numerical Data : Physics, Chemistry & Technology*. Vol. 7, McGraw-Hill, New York, 11

- Wenger, M., Ochsenbein, F., Egret, D., Dubois, P., Bonnarel, F., Borde, S., Genova, F., Jasniewicz, G., Laloë, S., Lesteven, S. & Monier, R. 2000, The SIMBAD astronomical database. The CDS reference database for astronomical objects, *A&AS*, 143, 9-22. Simbad website as of Jul. 1, 2008 : <http://simbad.u-strasbg.fr>
- Zahnle, K, Schenk, P. Levison, & H., Dones, L. 2003, Cratering rates in the outer Solar System, *Icarus*, 163, 263-289

Table 1. Various parameters adopted in this paper.

Titania physical properties	
Gravitational constant	$G = 6.67259 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ sec}^{-2}$
Titania's mass ^a	$GM = (2.343 \pm 0.006) \times 10^{11} \text{ m}^3 \text{ sec}^{-2}$
Rotation period ^a	$P = 8.706 \text{ days}$
Bond albedo ^b	$A_B = 0.15 \pm 0.02$
Stellar occultations geometry	
Sept. 8, 2001 02:00 UT	
Distance ^c (km)	$2.8504 \times 10^9 \text{ km}$
North pole position angle	$P = 260.4^\circ$
Sub-observer latitude	$B = -24.17^\circ$
Sub-observer longitude	$L = 343.5^\circ$
Star position at epoch (ICRF)	$\alpha = 324.55817850^\circ \pm 7.4 \text{ mas}$ $\delta = -14.90997417^\circ \pm 5.7 \text{ mas}$
Aug. 1, 2003 04:28 UT	
Distance (km)	$2.8557 \times 10^9 \text{ km}$
North pole position angle	$P = 257.6^\circ$
Sub-observer latitude	$B = -15.67^\circ$
Sub-observer longitude	$L = 164.3^\circ$
Star position at epoch (ICRF)	$\alpha = 333.9773096^\circ \pm 20 \text{ mas}$ $\delta = -11.6156551^\circ \pm 13 \text{ mas}$
Atmospheric refractivity modeling	
Carbon dioxide molecular mass	$\mu = 7.308 \times 10^{-26} \text{ kg}$
Carbon dioxide molecular refractivity ^e	$K_{CO_2} = 1.566 \times 10^{-23} \text{ cm}^3 \text{ molecule}^{-1}$
Methane molecular mass	$\mu = 2.664 \times 10^{-26} \text{ kg}$
Methane molecular refractivity ^e	$K_{CH_4} = 1.549 \times 10^{-23} \text{ cm}^3 \text{ molecule}^{-1}$
Nitrogen molecular mass	$\mu = 4.652 \times 10^{-26} \text{ kg}$
Nitrogen molecular refractivity ^e	$K_{N_2} = 1.023 \times 10^{-23} +$ $(5.888 \times 10^{-26} / \lambda_{\mu\text{m}}^2) \text{ cm}^3 \text{ molecule}^{-1}$

^aTaylor (1998)^bBuratti et al. (1990)^cyields a scale of 13,819 km at Titania per arcsec on the sky^dPerryman et al. (1997)^eWashburn (1930)Note. — Mass determination using fixed J₂ solution 4 from Taylor (1998).

Table 2. Circumstances and timings of September 8, 2001 occultation of HIP 106829 by Titania, ordered by country of observing stations/datasets and event chronology from Northeast to Southwest.

Site name	Lat.(d:m:s) Lon.(d:m:s) Alt. (m)	Ingress UT Egress UT Cycle time	Telescope Instrument/Receptor Timing ref. and remarks	Observers
United Kingdom				
<i>Teversham</i> ^b	52:12:06 N 00:11:30 E 10 m	01:54:29.75 01:55:40-43.0 vis.	R 0.16m Newt. Audio recording MSF & observer's commentary	C. R. Hills
<i>Worth Hill Obs., Bournemouth</i> ^{b,c,d}	50:35:52.9 N 02:01:50.5 W 140 m	01:54:29.08±0.03 01:55:42.11±0.03 0.04 sec	R 0.25m S/C Vid. DCF-77	A.J. Elliott
<i>Binfield</i> ^b	51:25:26 N 00:47:19.45 W 73 m	01:54:30 01:55:41 vis.	r 0.25m Yolo off-axis timings Junghans "Mega" radio	R. Miles T. Platt
Italy				
<i>Pompiano, Brescia</i>	45:26:14.2 N 09:59:30.3 E 94 m	clouded out	R 0.2m S/C n.a. n.a.	C. Cremaschini
France				
<i>Calern, Obs. Côte d'Azur</i> ^{b,c}	43:44:54 N 06:55:36 E 1270 m	01:54:28 01:55:05 n.a.	R 0.2m S/C Aud. CCD PC time from internet	P. Dubreuil
<i>Puimichel</i> ^{b,c}	43:58:53.1 N 06:02:10.0 E 680 m	01:54:19.7±0.4 01:55:05.8±0.4 n.a.	n.a. Audine, drift scan bad seeing (10")	C. Cavadore, C. Demeautis
<i>Obs. Haute Provence</i> ^{b,c}	43:55:46 N 05:42:45 E 650 m	01:54:21 01:55:07 0.04 sec	R 0.8m + R 0.6m CCD & vid. SVHS recorder No data on R 0.6m	W. Thuillot, P. Henriquet, O. Labrevoir, G. Rau
<i>Marseille</i> ^{b,c}	43:18:28 N 05:24:53 E 90 m	01:54:26 01:55:05 0.04 s	R 0.26m, Newt. radio-piloted video & comments	J.F. Coliac
<i>Les Orfeuilles, Marseille</i> ^{b,c,d}	43:18:57 N 05:27:55 E 180 m	01:54:25.3±0.2 01:55:03.5±0.2 vis.	R 0.2m S/C, micro-calculator HP71 calibrated with speaking clock and DCF 77	J. Piraux

Table 2—Continued

Site name	Lat.(d:m:s) Lon.(d:m:s) Alt. (m)	Ingress UT Egress UT Cycle time	Telescope Instrument/Receptor Timing ref. and remarks	Observers
<i>Notre Dame de Lamaron, Plateau d'Albion</i> ^b	44:00:11.2 N 05:04:05.4 E 1090 m	01:54:21.087 01:55:07.765 0.040 sec	R 0.08m Vid., digital camcorder Speaking clock, tape recorder, Stopwatch, beep every 10 sec	F. Gorry, C. Marlot, Ch. Marlot, C. Sire
<i>Salon</i> ^{b,c}	43:36:00 N ^e 05:06:00 E 40 m	01:54:25 01:55:09 0.04 s	R 0.2m S/C Webcam Compro PS39 DCF77 timing	B. Bayle
<i>St Martin de Crau</i> ^{b,c}	43:38:00 N ^e 04:49:00 E 20 m	01:54:25 01:55:12 vis.	R 0.2m S/C Radio clock, accuracy 1 sec	E. Simian
<i>St Maurice de Cazevieille</i> ^{b,c,d}	44:00:36 N 04:14:06 E 190 m	01:54:20.9 01:55:12.7 vis.	R 0.2m S/C DCF77, stopwatch	A.M. Blommers
<i>Nîmes</i> ^b	43:48:05 N 04:14:05 E 170 m	01:54:22 01:55:18 vis.	R 0.114m Newt. Speaking clock, stopwatch, tape recorder	J. Fulgence
<i>Obs. de Mauguio</i> ^{b,c}	43:34:07 N 03:57:07 E n.a.	01:54:180 01:55:070 0.015 sec	R 0.305m S/C LX200 CCD KaF400 Time set on internet	C. Leyrat, C. Sauzeaud, B. Stephanus
<i>Obs. Malibert, Pezenas</i> ^{b,c}	43:26:48 N 03:22:46 E n.a.	01:54:28 01:55:17 vis.	R 0.15m Mak-Cass. Speaking clock	T. Rafaelli
<i>Guitalens</i> ^b	43:38:34.7 N 02:02:11.2 E 148 m	01:54:22.6 01:55:18.9 n.a.	4 x R 0.2m S/C, Four Audine cameras, drift scan DCF 77	C. Buil, R. Delmas, V. Desnoux, C. Jasinski, A. Klotz, D. Marchais
<i>Rabastens</i>	43:49:00 N ^e 01:43:00 E (approx.)	duration 59 sec vis.	r 0.4m n.a.	M. Rieugnie
<i>Obs. Jolimont Toulouse</i>	43:36:43 N 01:27:46 E 189 m	n.a. 01:55:15 n.a.	n.a. Partly cloudy	G. Bouderand, J.-P.Cazard, C. Lambin, P.O. Pujat, F. Schwartz

Table 2—Continued

Site name	Lat.(d:m:s) Lon.(d:m:s) Alt. (m)	Ingress UT Egress UT Cycle time	Telescope Instrument/Receptor Timing ref. and remarks	Observers
<i>Châtellerault</i> ^{b,c,d}	46:50:21.0 N 00:34:02.9 E 131 m	01:54:19.9 01:55:33.1 vis.	r 0.1m, stopwatch DCF, synchro : Cuno inserter	E. Bredner
<i>Poitiers</i>	46:35:00 N ^e 00:20:00 E (approx.)	no data	n.a.	J. Berthier
<i>St Maurice la Clouère</i> ^b	46:22:00 N 00:30:00 E 120 m	01:54:20.9±0.2 00:55:12.7±0.2 vis.	R 0.12m Newt.	P. Langlais, S. Rivaud, P. Burlot
<i>St Savinien sur Charente</i> ^{b,c}	45:53:26.5 N 00:38:58.0 W 30 m	01:54:24.20 01:55:36.03 0.1 sec	R 0.2m S/C Aud. KAF 401E NTP server, poor absolute accuracy (several sec)	E. Brochard
<i>Bordeaux</i> ^b	44:50:07 N 00:31:42 W 73 m	01:54:21 01:55:27 4.5 sec	R 0.6m, CCD camera	J.-F. Lecampion, M. Rapaport
<i>Pic du Midi</i> ^{b,c,d}	42:56:12 N 00:08:32 E 2870 m	01:54:23.046±0.02 01:55:20.606±0.02 0.17 sec	R 1.0m, vid. & CCD (not used here) GPS timing	J. Lecacheux
<i>Obs. de Dax</i> ^b	43:41:36.4 N 01:01:49.8 W 11 m	Missed Ingress 01:55:34.70 n.a.	R 0.32m Newt. Aud. CCD DCF 77 timing	Ph. Dupouy, M. Lavayssière
<i>Fort de France</i> ^{b,c}	14:37:04 N 61:04:57 W n.a.	01:58:12.9 01:59:26.5 vis.	r 0.09m	O. Chaptal
Algeria				
<i>Algiers</i>	36:45:00 N 03:20:00 E 200 m	no event from 01:47 to 02:19, vis.	R 0.114m Newt.	K. Daiffallah
Morocco				
<i>Les Sables d'Or Temara</i>	33:55:07.4 N 06:58:08.6 W	no events for several mn	R 0.06m DCF 77 and short wave	R. Dusser

Table 2—Continued

Site name	Lat.(d:m:s) Lon.(d:m:s) Alt. (m)	Ingress UT Egress UT Cycle time	Telescope Instrument/Receptor Timing ref. and remarks	Observers
	6 m	around 01:55, vis.	receptor, tape & stopwatch	
Spain				
<i>Alella</i> ^{b,c,d}	41:29:02.3 N 02:18:01.8 E 45 m	01:54:29.03±0.1 01:55:00.04±0.1 0.04 sec	R 0.24m S/C vid. + CCD, stopwatch, 10MHz signals	C. Clarasso-Llauger
<i>Barcelona-1</i> ^{b,c,d}	41:25:18.9 N 02:12:10.0 E 60 m	01:54:31.9±0.2 01:55:01.6±0.2 vis.	R 0.258m Dobson stopwatch DCF77	D. Fernández
<i>Barcelona-2.1,</i> <i>L'Ordal</i> ^{b,c,d}	41:23:32.4 N 01:52:48.0 E 540 m	01:54:31.7±0.2 01:55:03.4±0.2 vis.	R 0.21m Newt. stopwatch, DCF77	J. Aloy-Doménech
<i>Barcelona-2.2,</i> <i>L'Ordal</i> ^{b,c,d}	41:23:32.4 N 01:52:48.0 E 540 m	01:54:31.7±0.2 01:55:03.5±0.2 vis.	R 0.203m Newt. stopwatch + DCF77	M. Gabaldá-Sánchez
<i>Barcelona-2.3,</i> <i>L'Ordal</i> ^{b,c,d}	41:23:32.4 N 01:52:48.0 E 540 m	01:54:31.5±0.2 01:55:03.3±0.2 vis.	R 0.21m Newt. stopwatch + DCF77	X. Otazu-Porter
<i>Barcelona-3</i> ^{b,c,d}	41:23:06.4 N 02:08:16.0 E 60 m	01:54:32.2±0.2 01:55:02.0±0.2 vis.	R 0.1m Newt. stopwatch & radio signal	E. Masana
<i>Esplugues</i> <i>de Llobregat</i> ^b	41:22:38 N 02:05:37 E 120 m	n.a. 01:54:59.8	R 0.20m CCD Cookbook, drift scan Manual set up of PC clock	F. Casarramona
<i>St Esteve</i> <i>Sesrovires</i> ^{b,c,d}	41:29:41.5 N 01:52:25.7 E 180 m	01:54:30.8±0.2 01:55:04.2±0.2 vis.	R 0.2m Newt. tape + DCF77	C. Schnabel
<i>Obs. AAS</i> <i>Sabadell-1</i> ^{b,c,d}	41:33:03 N 02:05:29 E 231 m	01:54:30.865±0.1 01:55:03.825±0.1 0.25 sec	R 0.5m IOC, manual set up of PC clock	R. Casas, J.A. Ros
<i>Obs. AAS</i> <i>Sabadell-2</i> ^b	41:33:03 N 02:05:29 E 231 m	01:54:31.2 01:54:59.6 0.2 sec	R 0.15m Newt., webcam, manual set up of PC clock with time beeps	A. Ardanuy

Table 2—Continued

Site name	Lat.(d:m:s) Lon.(d:m:s) Alt. (m)	Ingress UT Egress UT Cycle time	Telescope Instrument/Receptor Timing ref. and remarks	Observers
<i>Hortonedá</i> ^{b,c,d}	42:14:49 N 01:02:35 E 1001 m	01:54:23.2±0.2 01:55:11.0±0.2 vis.	R 0.203m Newt. stopwatch, time-signal from RNE1 station	A. Roca
<i>Castellón</i> ^{b,c,d}	40:00:31.5 N 00:01:48.2 W 85 m	01:54:40.3±0.2 01:54:59.6±0.2 vis.	R 0.2m S/C & video, DCF77	C. Labordena
<i>Zaragoza</i> ^{b,c,d}	41:37:29.4 N 01:02:30.5 W 330 m	01:54:27.6±0.2 01:55:18.7±0.2 vis.	R 0.12m Newt. stopwatch, time-signal from RNE1 station	O. Canales-Moreno
<i>Cerro Los Molinos, Alcublas</i> ^{b,c,d}	39:47:41 N 00:41:24 W 903 m	01:54:39.9±0.2 01:55:01.5±0.2 vis.	R 0.2m Newt. stop watch and tape	L. Rivas, V. Ferrer
<i>Granada</i>	37:10:54 N 03:23:05 W n.a.	no event from 01:50:08 to 02:02:37	R 0.4m & R 0.25m CCD surveillance video camera	J.L. Ortiz
<i>Roque de los Muchachos, Canaries Island</i>	28:45:44 N 17:52:42 W 2333 m	no event from 1:52 to 2:03, vis.	R 0.125m Newt., R 0.2m S/C & R 0.25m	J. Fernández-Arozena, L.L. Martín-Rodríguez
Portugal				
<i>Linhaceira, Tomar</i> ^{b,c,d}	39:31:22.6 N 08:23:01.5 W 90 m	01:54:36.35±0.02 01:55:37.39±0.02 0.04 sec	R 0.25m Newt. low-light vid. with AGC, VHS, DCF 77	R. Gonçalves
<i>Almeirim</i> ^b	39:10:50 N 08:34:58 W 10 m	01:54 37.7 01:55:34.0 0.04 sec	R 0.25m Webcam + PC Antennal timing	C. Reis
<i>Marinha Grande</i> ^{b,c,d}	39:45:00 N ^e 09:01:58.8 W 30 m	01:54:36.98±0.5 01:55:41.31±0.5 0.04 sec	R 0.4m S/C vid. timing from internet	J. Clérigo
<i>Alvito</i> ^{b,c,d}	38:11:01.8 N 08:06:11.0 W 50 m	01:54:40.0±0.08 01:55:30.8±0.08 0.04 sec	R 0.25m S/C, vid., PAL system, PC Compaq 10 MHz times signal	C. Oliveira

Table 2—Continued

Site name	Lat.(d:m:s) Lon.(d:m:s) Alt. (m)	Ingress UT Egress UT Cycle time	Telescope Instrument/Receptor Timing ref. and remarks	Observers
<i>Alcácer do Sal</i> ^{b,c}	38:21:38.9 N 08:28:33 W 25 m	01:54:41 01:55:34 vis.	R 0.2m S/C, stopwatch timing origin n.a.	C. Marciano
<i>Setúbal</i> ^{b,c}	38:30 N ^e 08:55 W 40 m	01:54:36.5 01:55:33.0 1/15 sec	R 0.25m S/C, CCD, timing origin n.a.	R. Nunes, P. Coelho
<i>Carcavelos</i> ^{b,c}	38:41:11.4 N 09:20:44.5 W 56 m	01:54:42 01:55:41 0.1 s	R 0.25m S/C, CCD, GPS	C. Saraiva, P. Figueiredo
<i>Oeiras</i> ^{b,c}	38:41:07 N 09:19:25 W 50 m	01:54:36 01:55:34 1/3.325 sec	R 0.25m SC, SBIG's ST-237 refrigerated CCD	A. Cidadão
<i>Portimão-1</i> ^{a,b,c,d} <i>0.25m</i>	37:08:28.7 N 08:37:33.2 W 64 m	01:54:45.611±0.035 01:55:27.831±0.035 ±0.27 sec (fitted)	R 0.25m S/C IOC, TC 245 chip DCF 77	H. Denzau, P. Ré, F. Tonel
<i>COAA Algarve</i> , ^{b,c,d} <i>Portimão-2</i>	37:11:24.6 N 08:36:01.8 W 65 m	01:54:44.84±0.06 01:55:27.72±0.06 1/14.995 sec	R 0.2m Newt. low-light vid., AVI 60kHz timing, soundtrack	B.M. Ewen-Smith, S. Ward, D. Ford
<i>Espada Station, Funchal, Madeira</i>	32:38:15.3 N 16:56:07.8 W 35 m	clouded out	R 0.35m S/C	R. Hill, W.B. Hubbard, J. Laurindo Sobrinho, F. Teodoro de Gois, J. Afonso da Silva Mendes, M. Joaquim
<i>Ponta Delgada, Açores</i> ^{b,c,d}	37:44:38 N 25:40:38 W 50 m	01:55:18.25±0.30 01:56:31.15±0.30 0.04 s	R 0.3m S/C vid. & PC, DCF 77	J. Gonçalves, J. Porto
United States of America				
<i>Greenbelt, Maryland</i>	38:59:10.1 N 76:52:09.9 W 53 m	no event	R 0.2m S/C vid.	D. Dunham
Aruba				
<i>Arikok</i> ^{a,b,c,d}	12:29:55.6 N	01:58:59.140±0.005	R 0.2m S/C	T. Widemann

Table 2—Continued

Site name	Lat.(d:m:s) Lon.(d:m:s) Alt. (m)	Ingress UT Egress UT Cycle time	Telescope Instrument/Receptor Timing ref. and remarks	Observers
<i>0.20m</i>	69:55:34.1 W 99 m	02:00:08.680±0.005 ±0.110 sec (fitted)	IOC, TC245 chip GPS time	
<i>Wela</i> ^b	12:29:00.5 N 69:57:49.6 W 30 m	01:59:00.1 02:00:11.3 vis.	R 0.318m Dobson Colorado time-signal station 15 MHz, stopwatch, cassette recorder	E. van Ballegoij
Barbados				
<i>Bridgetown</i> ^b	13:05:07 N 59:35:10 W 74 m	01:58:14.4 01:59:22.9 vis.	R 0.35m S/C, WWV time signal radio station, tape recorder	R. Jones, H. Callender, W. Sutherland
Trinidad & Tobago				
<i>Santa Margarita, Trinidad</i>	n.a. n.a. n.a.	clouded out	R 0.2m S/C CCD	S. Bumgarner
<i>Arnosvale, Tobago</i>	11:13:54 N 60:45:42 W 100 m	duration: 70.9 sec	R 0.3m S/C, CCD w/increased gain, Trinidad & Tobago Astron. Society's VHS video recorder	M. Imbert, B. Mitchell, J. Lockhart, W. Barrow, D. Cornwall
Venezuela				
<i>Obs. ARVAL, Caracas</i> ^{b,c,d}	10:30:08.6 N 66:50:39.4 W 915 m	01:58:50.00±0.05 02:00:04.73±0.05 1/30 sec	R 0.125m S/C, PC23C, camera VHS tape (SP speed)	A. Arnal, G. Eleizalde, A. Valencia
<i>Casetejas</i>	10:04:44.91 N 69:14:54.86 W 465 m	clouded out	n.a.	A. Peña, S. Radaelli
<i>Tamaca</i>	10:09:43.25 N 69:19:02.88 W 595 m	clouded out	n.a.	J. Santiago, K. Vieira
<i>Bobares 1</i> ^{b,c}	10:16:19.5 N 69:27:20.52 W 620 m	01:59:00.25 02:00:13.50 vis.	R 0.275m S/C	V. Ladino, T. Lizardo, P. Maley,

Table 2—Continued

Site name	Lat.(d:m:s) Lon.(d:m:s) Alt. (m)	Ingress UT Egress UT Cycle time	Telescope Instrument/Receptor Timing ref. and remarks	Observers
<i>Bobares 2</i>	10:16:37.43 N 69:27:18 W 640 m	clouded out	n.a.	C. Guillén, G. Sánchez
<i>Maracaibo, Zulia^b</i>	10:42:53 N 71:37:25 W n.a.	about 01:59:00 about 02:00:00 vis.	r 0.05m	H. Mendt
<i>Mérida</i>	08:47:00 N 70:52:00 W 3600 m	clouded out	R 0.6m IOC TC245 chip + R 1.0m, video	O. Contreras, F. Díaz, E. Guzmán, M. Kretlow, F. Moreno, O. Naranjo, L. Omar Porras, P. Rosenzweig
Ecuador				
<i>Salinas 1^{a, b, c, d} 0.25m</i>	00:28:01.5 N 78:11:06.6 W 2040 m	02:00:11.341±0.01 02:01:11.166±0.01 ±0.26 sec (fitted)	R 0.25m S/C IOC, TC245 chip GPS time	B. Sicardy E. Recalde
<i>Salinas 2^{a, b, c, d} 0.20m</i>	00:28:01.5 N 78:11:06.6 W 2040 m	02:00:11.290±0.02 02:01:11.120±0.02 ±0.22 sec (fitted)	R 0.2m S/C IOC, TC245 chip GPS time	W. Beisker, M. Mascaró
<i>Salinas-3</i>	00:28:01.5 N 78:11:06.6 W 2040 m	02:00:12.150 02:01:10.185 ±0.100 sec	R 0.2m S/C Audine camera drift scan, manual time setup	C. Birnbaum, F. Colas, S. Pau
<i>Quito</i>	00:12:54.4 S 78:30:09.6 W 2818 m	clouded out	r 0.238m Mertz webcam	R. Cósias, E. López, E. Pallo, R. Percz, D. Pulupa, X. Simbaña, A. Yajamín
<i>Cerro El Buerán, Cuenca^b</i>	02:39:46.3 S 78:58:24.2 W 3987 m	02:00:17.4 02:01:36.9 vis.	r 0.1m	P. Rodas

Table 2—Continued

Site name	Lat.(d:m:s)	Ingress UT	Telescope	Observers
	Lon.(d:m:s)	Egress UT	Instrument/Receptor	
	Alt. (m)	Cycle time	Timing ref. and remarks	
Mexico				
<i>Monterrey</i>	25:38:36 N 100:22:26 W 659 m	no event from 01:51 to 02:05	R 0.175m Astrovid camera	P. Valdés Sada

^aThe four stations/datasets used for stellar diameter (Section 3) and atmospheric model fitting (Section 6). Quoted error bars are formal errors from diffraction limb fitting and are at most 0.035 s. Larger, systematic errors on absolute timing may be present at the ± 0.3 s level (see text).

^bThe fifty-seven stations with reported timings (shown in Figure 7). Error bars at these stations are those reported by observers and have not been modified by us.

^cThe forty-three stations with $\Delta r = r_{i,obs} - r_{ref} \leq 10$ km used for Titania’s ephemeris offset using time-shifted chords (Section 4 and Figure 8)

^dThe twenty-seven stations used for Titania’s size and oblateness through limb fitting (Section 5, fit parameters listed in Table 3). Among them are thirteen visual observations made by experienced observers, for which we estimate an accuracy of about 0.2-0.3 sec

^eUndocumented site or one or more observer’s coordinates at ± 1 arcmin error level.

Note. — Abbreviations and acronyms : Cycle time = Recording time resolution ; Telescope : R = reflector ; r = refractor ; Newt. = Newton ; S/C = Schmidt-Cassegrain ; Instrument/Receptor : IOC = Iota camera, Aud. = Audine camera, SBIG = Sbig camera, Vid. = video/camcorder, Vis. = Visual ; Timing source/reference : MSF (or NPL) = UK 60 kHz time signal, DCF77 = Germany 77.5kHz time signal, WWVB = NIST 60 kHz time signal, Colorado ; n.a. = not available/specified.

Table 3. Circular fit to 27 selected chords, Sep. 8, 2001 event. The free parameters of the fit are Titania's radius, $R_{T,occ}$, and the location of shadow center, as given by the offset $\Delta f, \Delta g$ (see text).

Site ^a	Rec. ^b	Δt^c (sec)	Ingress			Egress			C/A ^f (km)	Δr^g (km)
			Latitude ^d (deg)	f^e (km)	g^e (km)	Latitude ^d (deg)	f^e (km)	g^e (km)		
<i>Arikok</i> , 0.2m	ccd	+0.093	+65.7	-2275.3	-957.8	-45.4	-973.7	-271.1	+279.6	-1.37
<i>Worth Hill</i> , 0.25m	vid.	+0.243	+65.6	-2261.0	-1044.5	-50.4	-911.6	-330.2	+197.3	-0.05
<i>Ponta D.</i> , 0.3m	vid.	-0.531	+65.3	-2251.7	-1068.2	-52.0	-894.8	-354.1	+170.2	-3.17
<i>Caracas</i> , 0.125m	vid.	-2.520	+59.5	-2184.4	-1248.3	-61.1	-784.9	-510.7	-020.1	+2.74
<i>Chatellerault</i> , 0.1m	vis.	-0.378	+50.4	-2078.3	-1393.4	-65.6	-725.7	-678.1	-196.8	+1.57
<i>Marinha G.</i> , 0.4m	vid.	-0.415	+36.7	-1898.8	-1540.1	-62.5	-705.7	-911.3	-411.4	+1.56
<i>Linhaceira</i> , 0.25m	vid.	+0.235	+33.0	-1846.4	-1565.3	-60.3	-714.5	-968.7	-458.1	-1.48
<i>Salinas-1</i> , 0.25m	ccd	-0.381	+32.0	-1833.6	-1573.5	-59.8	-714.6	-981.7	-470.4	+0.25
<i>Salinas-2</i> , 0.2m	ccd	-0.333	+32.0	-1833.7	-1573.5	-59.8	-714.6	-981.6	-470.4	+0.29
<i>Pic du Midi</i> , 1m	vid.	+0.290	+28.8	-1787.4	-1595.3	-57.5	-722.8	-1033.0	-511.6	+1.66
<i>St Maurice Caz.</i> , 0.2m	vis.	-0.153	+23.2	-1705.3	-1619.9	-53.2	-748.5	-1114.1	-571.5	-1.21
<i>Zaragoza</i> , 0.12m	vis.	-0.018	+22.6	-1696.0	-1624.5	-52.6	-750.3	-1125.3	-580.3	+0.78
<i>Alvito</i> , 0.25m	vid.	+0.455	+22.4	-1693.2	-1626.1	-52.4	-751.0	-1129.7	-583.4	+1.59
<i>Hortoneda</i> , 0.203m	vis.	+2.808	+19.7	-1652.6	-1631.8	-50.2	-768.6	-1165.0	-606.9	-2.02
<i>COAA</i> , 0.2m	vid.	+0.402	+15.5	-1590.6	-1643.3	-46.5	-794.9	-1224.2	-646.5	-0.81
<i>Portimão-1</i> , 0.25m	ccd	+0.007	+15.0	-1583.0	-1642.8	-46.0	-799.6	-1230.2	-649.6	-2.19
<i>Orfeuilles</i> , 0.2m	vis.	-0.431	+11.5	-1529.6	-1647.1	-43.0	-824.9	-1274.6	-677.7	-2.04
<i>St Esteve</i> , 0.2m	vis.	+0.265	+07.8	-1473.4	-1648.6	-39.5	-855.8	-1322.5	-705.5	-1.09
<i>Sabadell-1</i> , 0.5m	ccd	+0.097	+07.4	-1467.7	-1649.5	-39.1	-858.3	-1327.6	-708.9	-0.08
<i>Barcelona-2.1</i> , 0.21m	vis.	+0.091	+06.5	-1453.4	-1648.5	-38.3	-867.2	-1338.9	-714.7	-0.49
<i>Barcelona-2.2</i> , 0.203m	vis.	+0.041	+06.5	-1454.3	-1649.0	-38.3	-866.3	-1338.4	-714.7	-0.04
<i>Barcelona-2.3</i> , 0.21m	vis.	+0.241	+06.5	-1454.3	-1649.0	-38.3	-866.3	-1338.4	-714.7	-0.05
<i>Alella</i> , 0.24m	vid.	+2.492	+05.8	-1443.1	-1652.4	-37.6	-869.8	-1349.6	-722.9	+4.01
<i>Barcelona-1</i> , 0.258m	vis.	+0.384	+04.9	-1430.2	-1647.5	-36.8	-881.0	-1357.5	-724.7	+0.12
<i>Barcelona-3</i> , 0.1m	vis.	+0.111	+04.9	-1430.8	-1648.7	-36.9	-879.8	-1357.7	-725.4	+1.24
<i>Alcublas</i> , 0.2m	vis.	+0.255	-01.0	-1341.9	-1634.4	-31.1	-942.1	-1423.4	-754.3	-0.77
<i>Castellón</i> , 0.2m	vis.	-0.046	-02.7	-1316.8	-1630.1	-29.5	-959.7	-1441.7	-762.3	+0.31

^aSee Table 2. Chords have been sorted in order of decreasing closest approach (C/A) distances. This corresponds from top to bottom in Figure 11.

^bType of recording mode : CCD, vid.= video or vis.= visual.

^cApplied time shift, see text for details.

^dSub-occultation titaniacentric latitude.

^ePosition in sky plane, see Figure 11.

^fClosest approach to shadow center. Positive means observer North of shadow center, negative otherwise.

^gRadial residual to circular fit (plotted in Figure 12).

Note. — Best fitting circle radius $R_T = 788.4$ km, center : $f_c = -1494.1$ km, $g_c = -861.6$ km, r.m.s. radial dispersion : 1.58 km, no oblateness detected. See text, Section 5 for details.

Table 4. Titania occultation, August 1, 2003, circumstances and timings. Same abbreviations as in Table 2.

Site name	Lat.(d:m:s) Lon.(d:m:s) Alt. (m)	Ingress UT Egress UT Cycle time	Telescope Instrument/Receptor Timing ref. and remarks	Observers
Mexico				
<i>Observatorio UANL</i>	25:54:51.5 N 100:08:35.6 W 385 m	04:28:08.49±0.05 04:29:22.01±0.03 ±0.05/0.03 sec	R 0.3m S/C, Astrovid video with GPS time insertion	P. Valdés Sada, R. Hernández, E. Castro
United States of America				
<i>George Observatory</i>	29:22:30 N 95:35:37 W 24 m	04:27:53±1 04:28:53±1 ±1 sec	R 0.9m S/C, video with WWVB time signal	A. Hernández P. Maley B. Wilson

Table 5. Modelling results for Titania's atmosphere surface pressure at equilibrium, with detection upper limits in standard deviation units for CO₂, CH₄ and N₂.

gas	$(dz/dT)_z$ (K km ⁻¹)	T(z > 20km) (K)	surface scale height (km)		surface pressure upper limit (nb)	column density (cm-amagat)
CO ₂	0	60	30	1- σ	9	0.132
				3- σ	20	0.293
CO ₂	0	70	35	1- σ	13	0.193
				3- σ	28	0.410
CO ₂	0	80	40	1- σ	17	0.257
				3- σ	37	0.549
CH ₄	2	110	95	1- σ	8	0.436
				3- σ	18	0.954
N ₂	0	70	55	1- σ	22	0.550
				3- σ	46	1.150

Titania stellar occultation, 08 September 2001

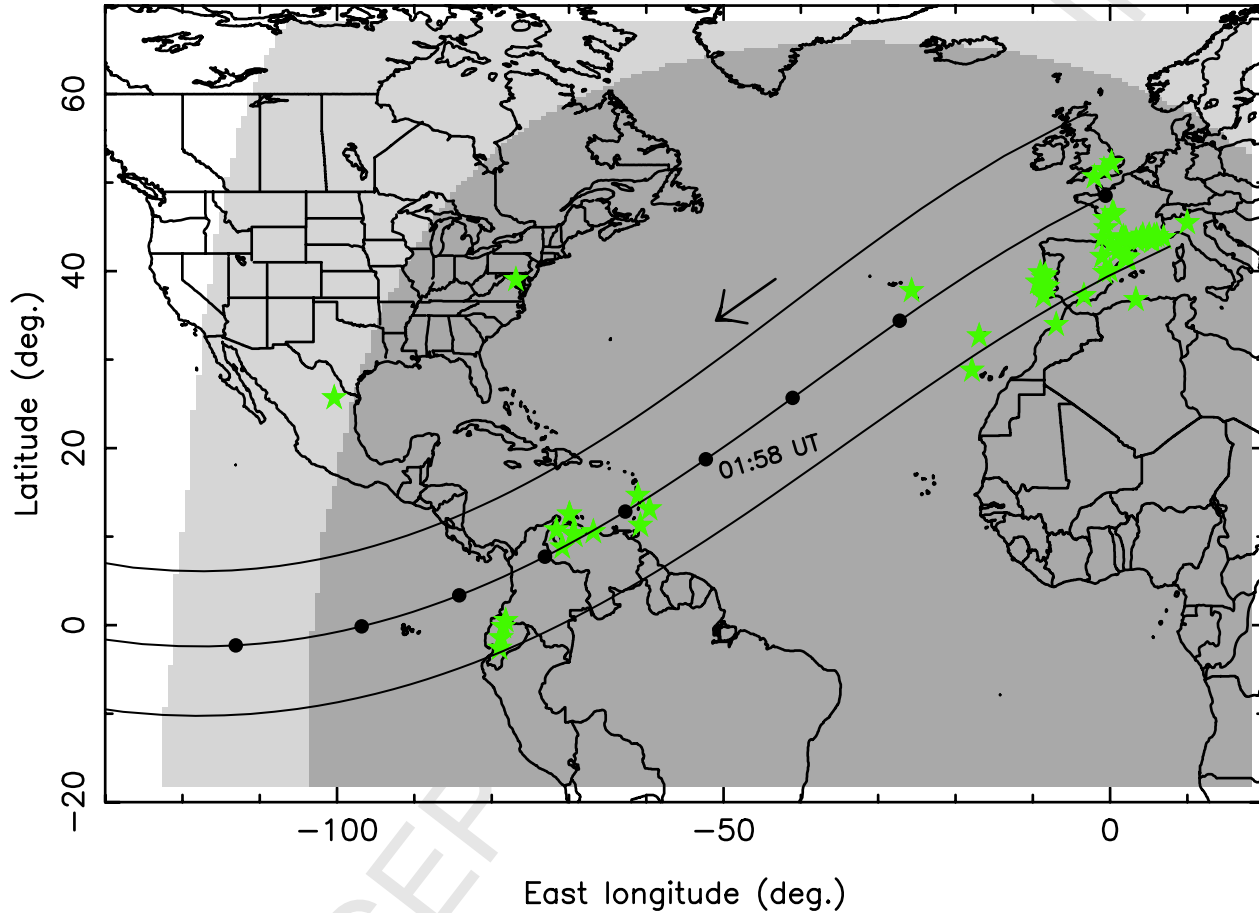


Fig. 1.— Path of Titania’s shadow on Earth on September 8, 2001, according to the post-occultation analysis presented in this paper. Motion is from upper right to lower left. The darker grey zone is for night time (Sun below -18° with respect to local horizon), lighter grey is for astronomical twilight (Sun between 0° and -18° below local horizon) and white is for day time. Dots along the centerline are plotted every minute. This is where the event duration was maximum, about 72 sec. The green star symbols indicate all the stations reported in Table 2, among which fifty-seven reported timings. The event was observed at low elevation from France, UK, Italy, Spain, Morocco, Portugal around 1:55 UT, and near zenith in the Caribbean region (Barbados, Tobago, Aruba) and from Northern South-America (Ecuador, Venezuela); around 2:00 UT.

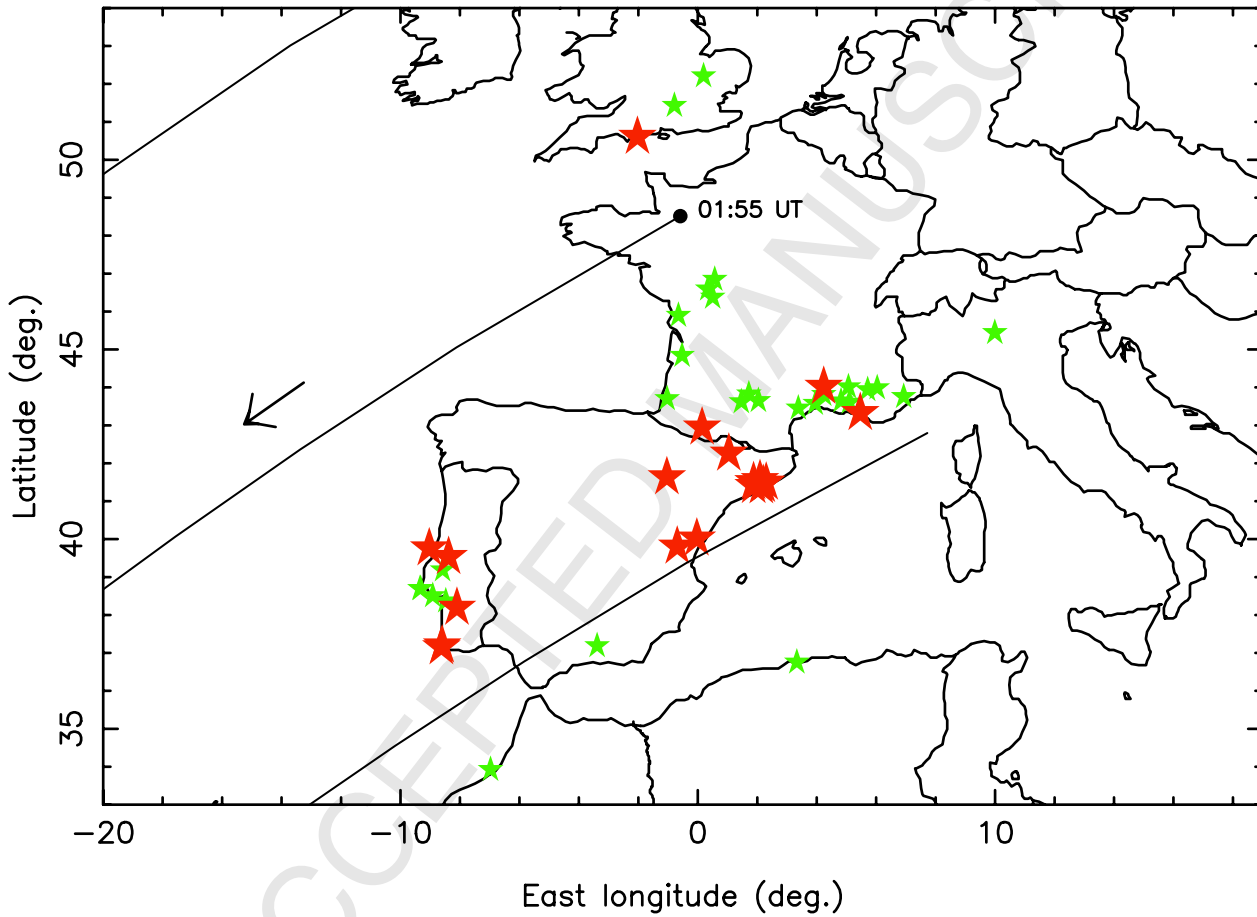


Fig. 2.— Enlargement of Figure 1. Titania's shadow over Europe and Africa observing stations. Green star symbols are for stations where observations were attempted and/or achieved, Red star symbols mark the subset of twenty-seven stations used for limb fitting (Section 5). See Table 2 for circumstances and timings, and Table 3 for limb fitting data.

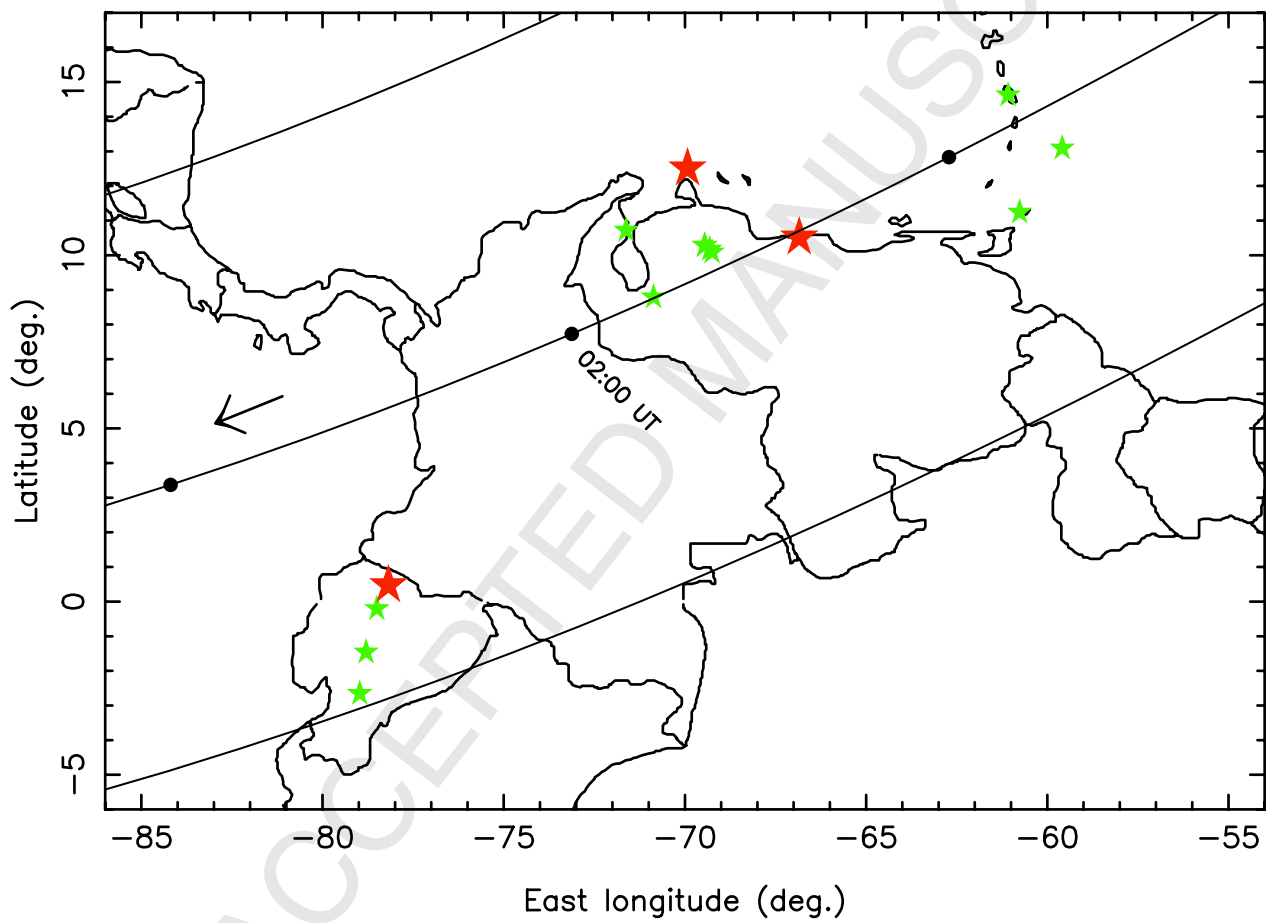


Fig. 3.— Same as Figure 2, for Central and South America. See Table 2 for circumstances and timings, and Table 3 for limb fitting data.

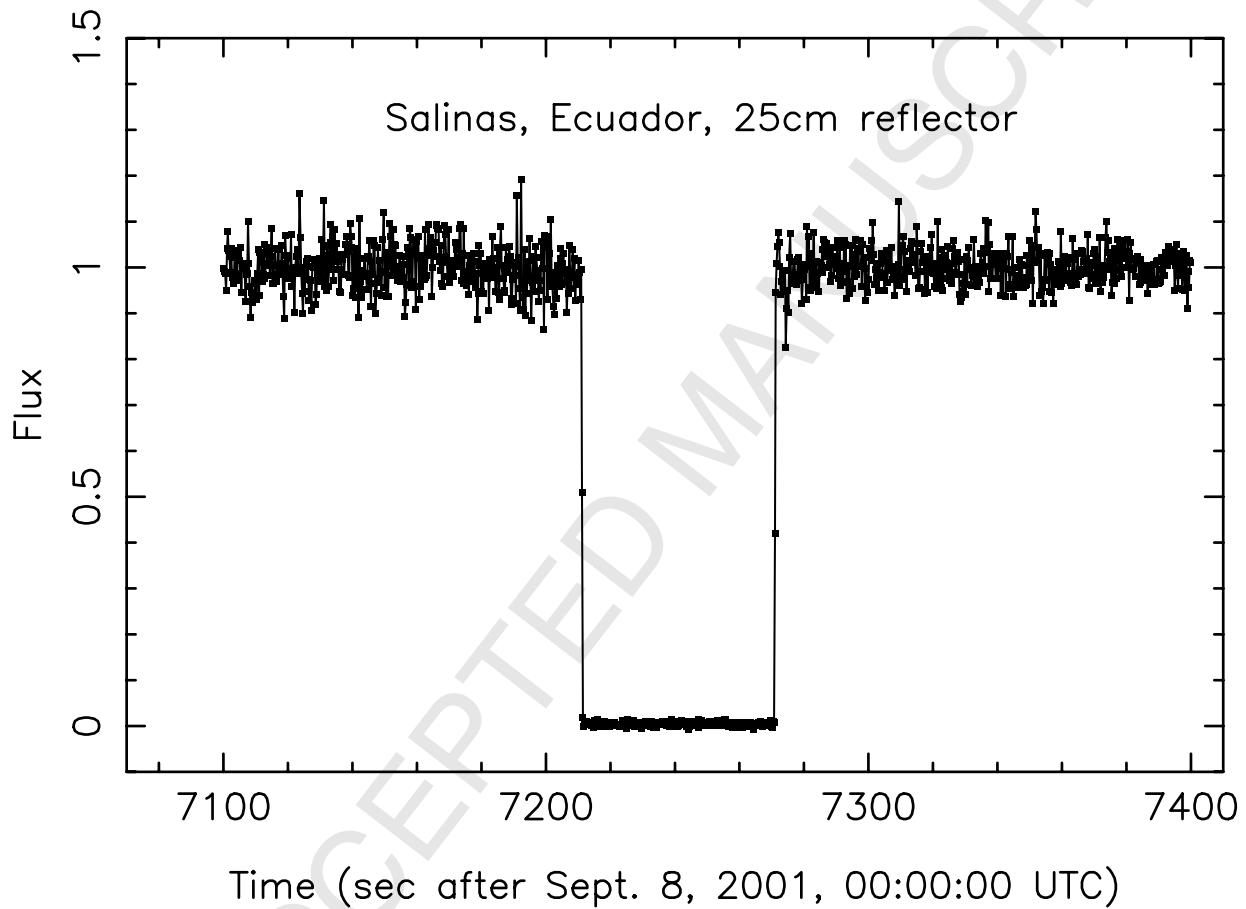


Fig. 4.— Example of a light curve, obtained with the 0.25m reflector at Salinas. All data points are shown, with a cycle time of 0.26 sec, see Table 2. The flux from the star (plus the much fainter Titania) has been divided by a running average (over 5 sec) of Uranus' flux, in order to correct for low frequency sky transparency variations. Finally, the data have been normalized between zero (Titania only) and unity (full stellar + Titania flux).

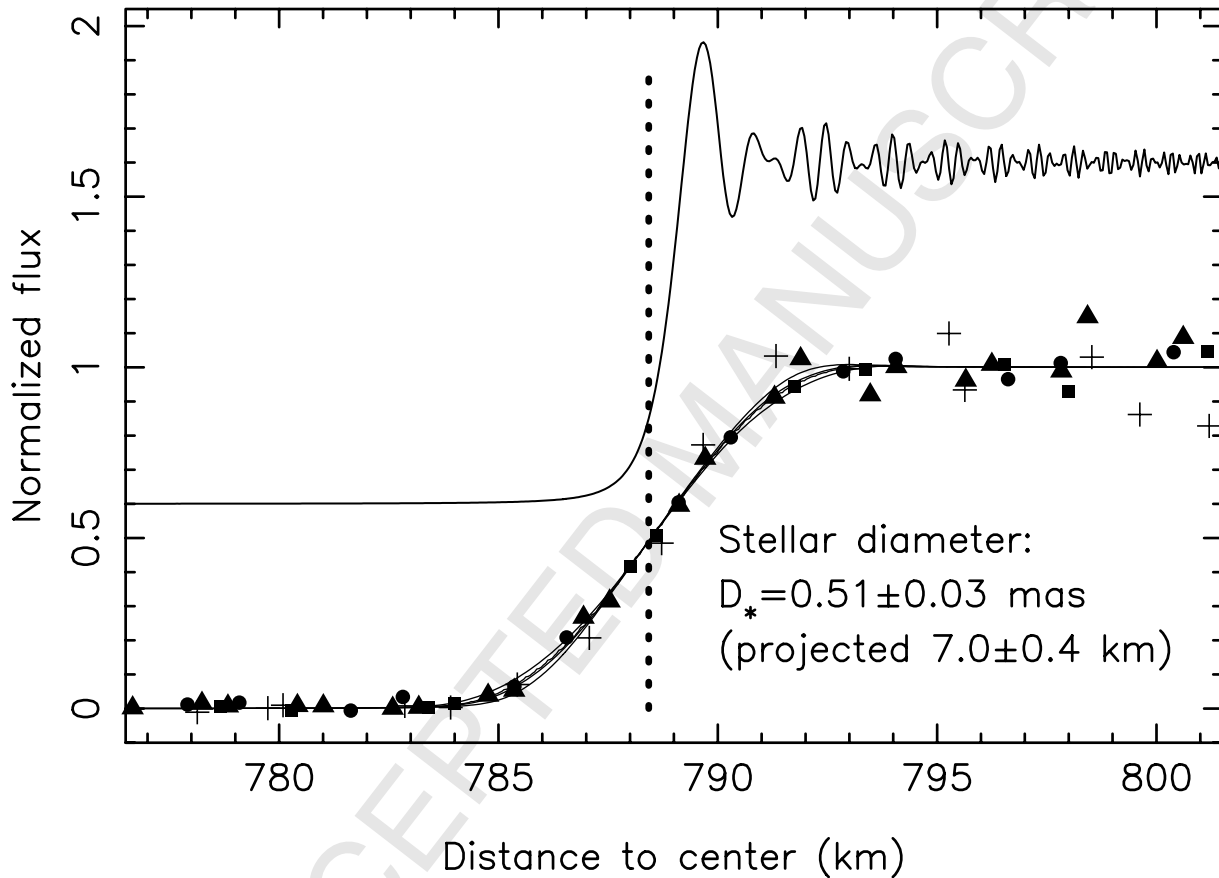


Fig. 5.— Fit the stellar diameter from the Salinas-1 0.25m (squares), Salinas-2 0.20m (bullets), Arikok 0.20m (triangles) and Portimão-1 0.25m (crosses) light curves (see Table 2). Data are normalized between 0 (no star) and 1 (full signal). The vertical dotted line is the location of an edge at 788.4 km, corresponding to the Titania radius obtained in this paper. The upper thin curve is shifted vertically by +0.6 for better viewing, and shows the expected diffraction pattern from a point-like source. Thin lines superimposed to the data are best fits with stellar diameter taken into account. They are slightly different from each other, as the response of each instrument varies with integration time. See text for details.

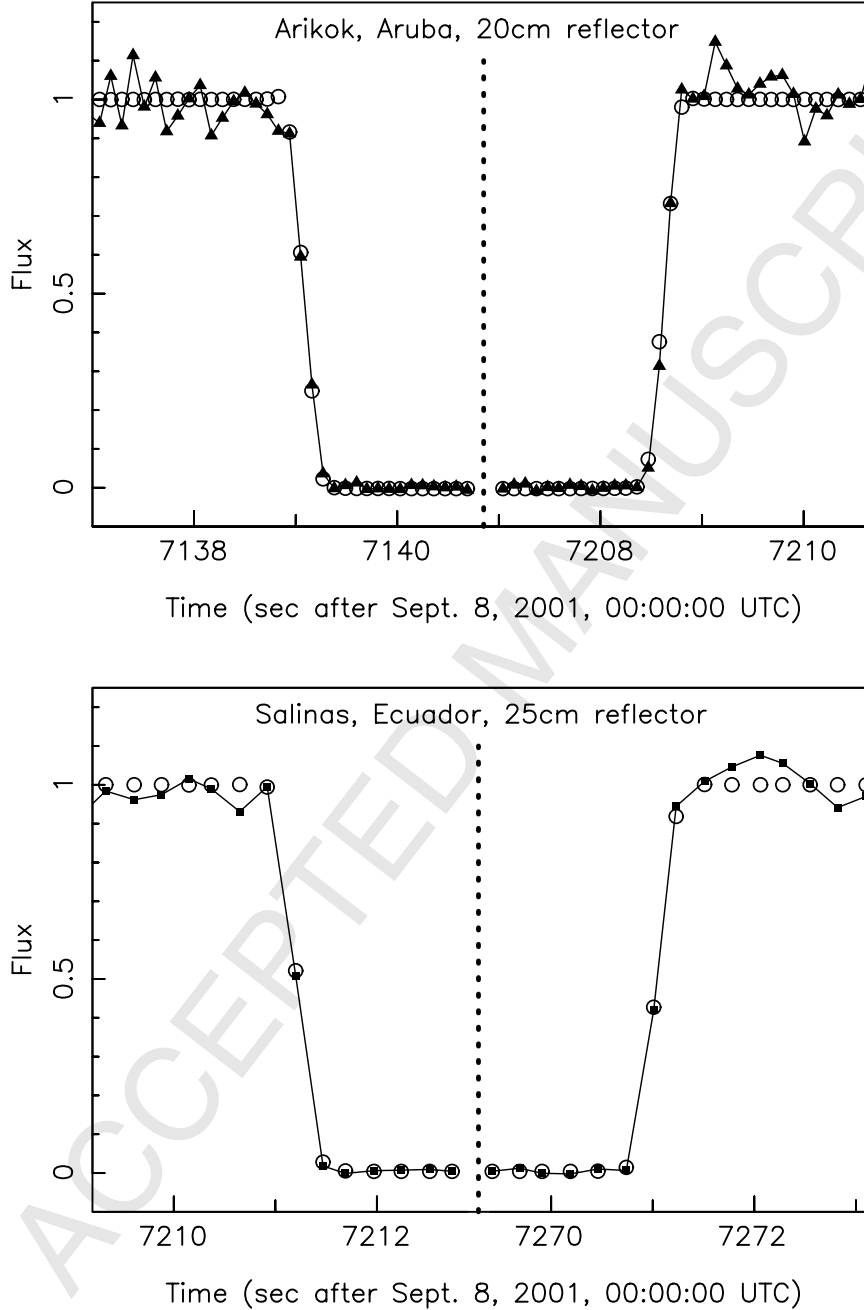


Fig. 6.— *Upper panel:* Fit to the Arikok, Aruba, ingress and egress light curves (solid line). The triangles are the individual data points, while the open circles are from a best fit model, taking into account diffraction, stellar diameter and instrumental response, see text for details. Besides providing the stellar diameter, see Figure 5, the fit yields the stellar half-light times at disappearance and re-appearance, and associated error bars, see Table 2. *Lower panel:* The same for the Salinas-1 0.25m reflector data, where the square are individual data points, see also Figure 4. On both plots, note the discontinuity in time at the vertical dotted line, in order for the light curves to fit into the figure. Also, note the better sampling of the Arikok light curve, due to a smaller cycle time (0.11 sec vs. 0.26 sec, see Table 2).

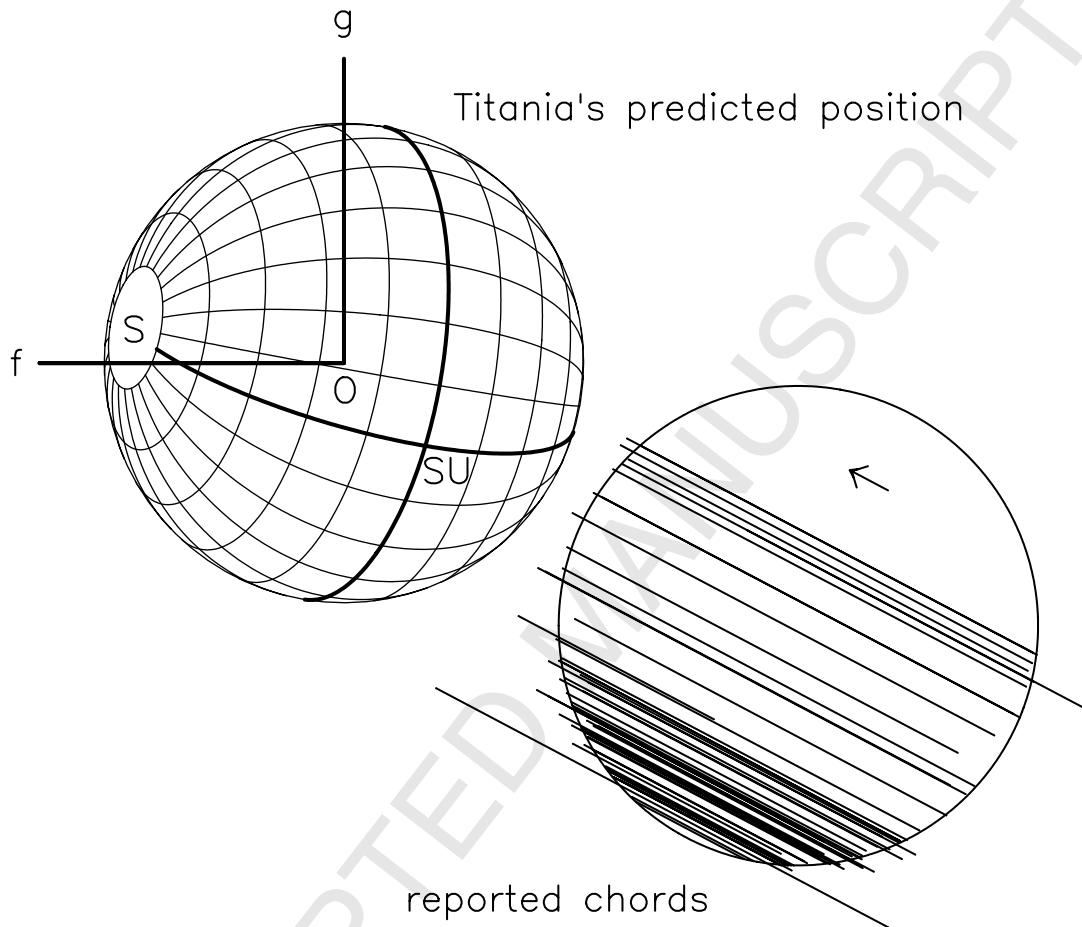


Fig. 7.— Fifty-seven occultation chords with reported timings (Table 2). The origin “O” of the diagram is located at the expected center of Titania’s disk in ICRS J2000.0 coordinates, as derived from the star position predicted at time of event (Eq. 1) and DE405+URA027 Titania ephemeris. The arrow indicates the direction of motion in the sky plane. The horizontal and vertical bars are aligned with the local celestial ICRS J2000.0 N-S and E-W directions, respectively, and have lengths of 1000 km, with celestial North up and celestial East left. The scale is 13,819 km per arcsec. Label “S” stands for Titania’s south pole (IAU convention). Meridians and parallels on Titania’s globe are plotted every 15° , with thicker lines delineating Titania’s equator and origin of longitudes (the meridian facing Uranus). The intersection of this meridian with Titania’s equator defines the sub-Uranus point on Titania, labelled “SU”. Sub-observer latitude at Titania is -24.2° , and north pole position angle is 260.4° , see Table 1. An offset with respect to the expected Titania’s position is clearly visible, see Section 4. The circle surrounding the chords is the best circular fit to Titania’s limb (Section 5).

– 52 –

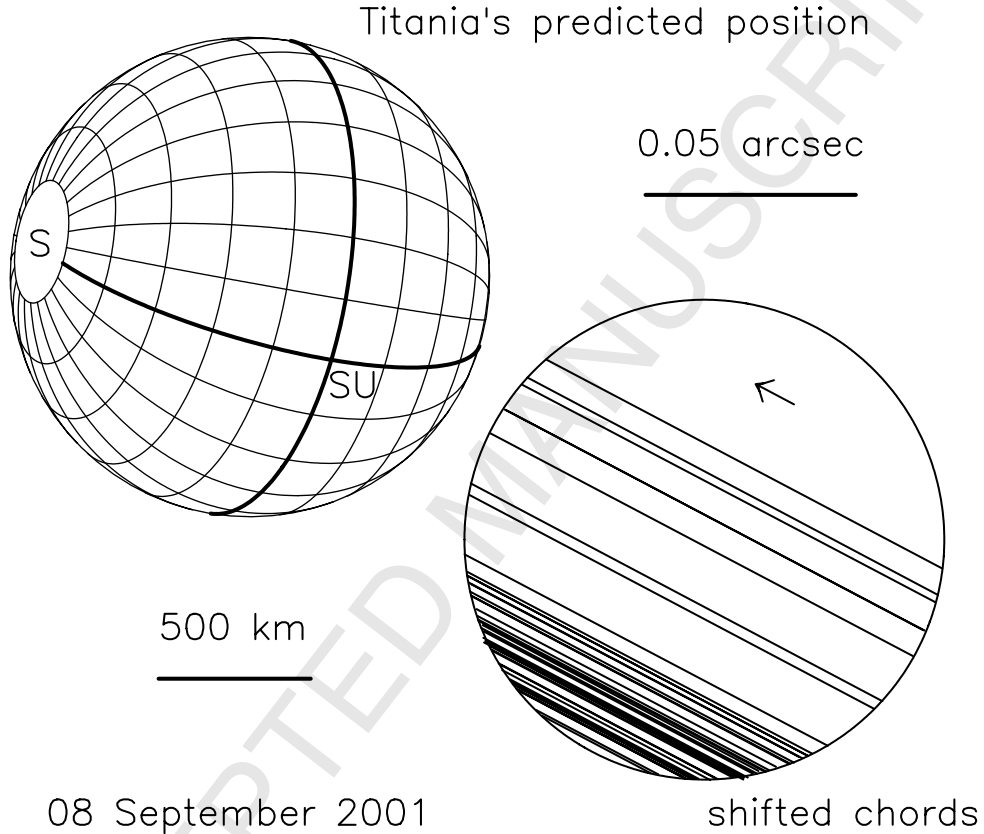


Fig. 8.— Same as Figure 7, but limited to the forty-three stations with radial residual $\Delta r = r - r_{ref} \leq 10$ km used for Titania’s ephemeris offset determination (Table 2 and Section 4). This corresponds to an error of 0.5 to 2 sec in chord duration, depending on the observer’s location projected on the limb. The occultation chords have also been displaced along their own direction so that they share the same mediatrix. This is equivalent to applying a time shift to each of those stations, to compensate for their absolute timing error, see text for details. The offset in ICRS J2000.0 celestial coordinates, between Titania’s expected position (globe at upper left) and observed position is $\Delta\alpha \cos(\delta) = -108 \pm 13$ mas and $\Delta\delta = -62 \pm 7$ mas. Like in Figure 7 the circle surrounding the chords is the best circular fit to Titania’s limb.

- 53 -

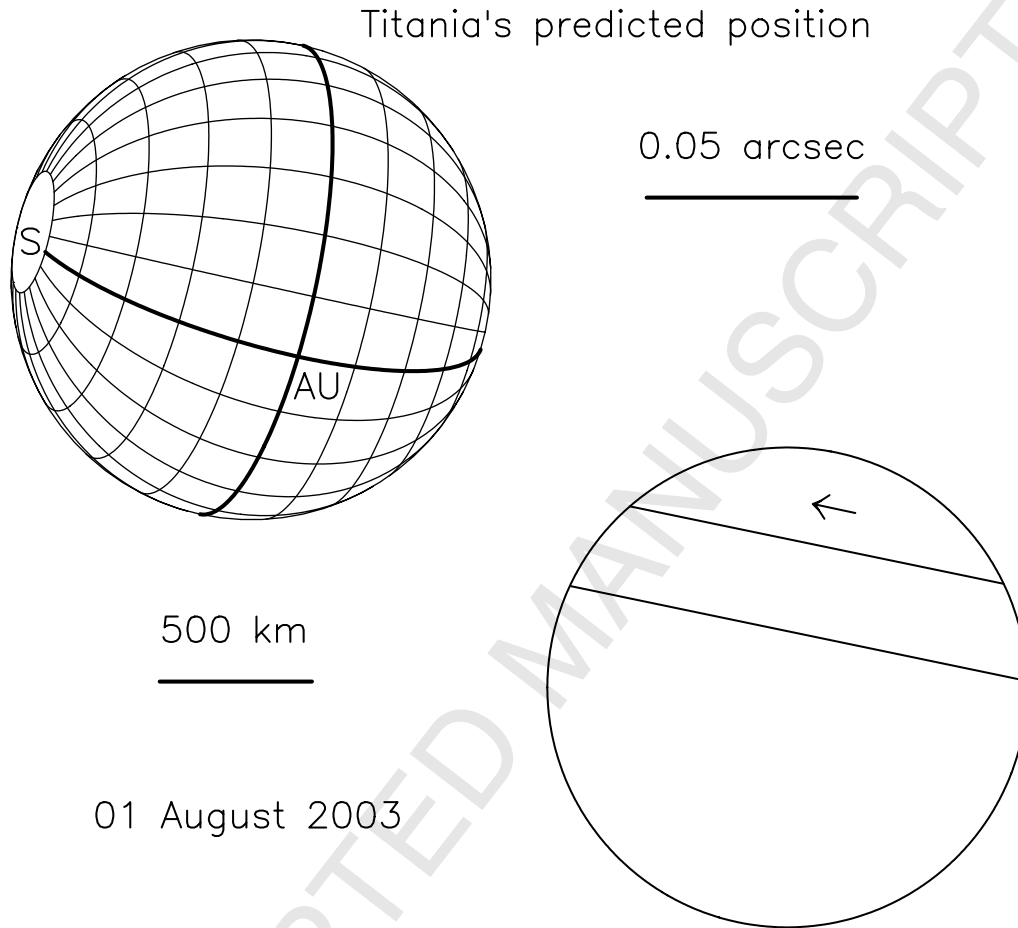


Fig. 9.— The two occultation chords derived from the additional timings provided by the Aug. 1, 2003 occultation (see Table 4) and used for an additional offset constraint to Titania's ephemeris position. The Figure shows Titania's orientation and direction of motion in the sky plane in ICRS J2000.0 coordinates. Label "S" is Titania's south pole ; titianicentric meridians and parallels are plotted every 15° . "AU" designates the anti-suburbanian meridian at longitude 180° , as prime meridian is on the far side. See text, Section 4 for details.

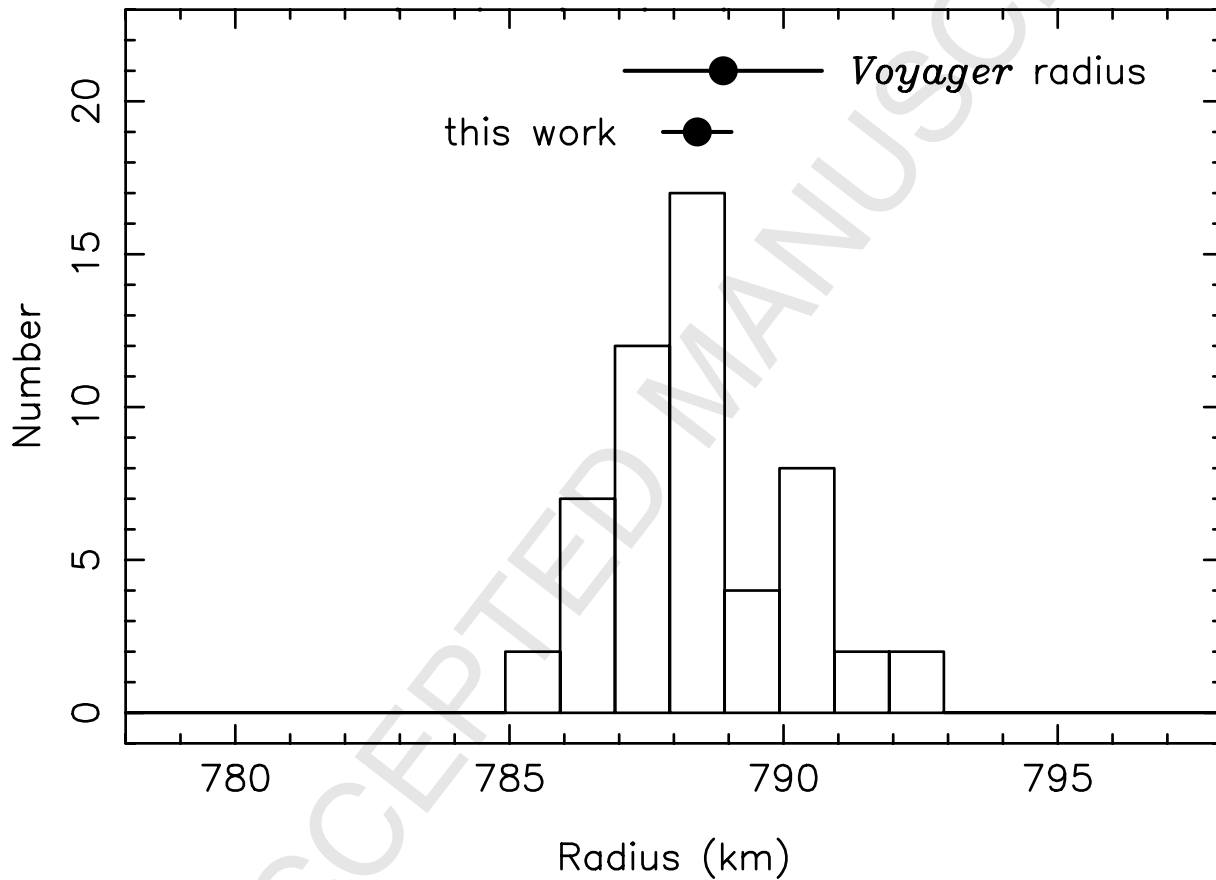


Fig. 10.— Histogram of radial residuals for our best circular fit to both extremities of the twenty-seven occultations chords of see Fig. 11, reported in Table 3. Our fitted Titania’s radius, $R_{T,occ} = 788.4 \pm 0.6$ km, is shown as a black dot with associated error bars, just below the value derived from *Voyager* images, $R_{T,Voy} = 788.9 \pm 1.8$ (Thomas 1988). Most of the dispersion seen in this histogram is likely to be caused by topographic features along Titania’s limb, see Section 5, ¶5.1.

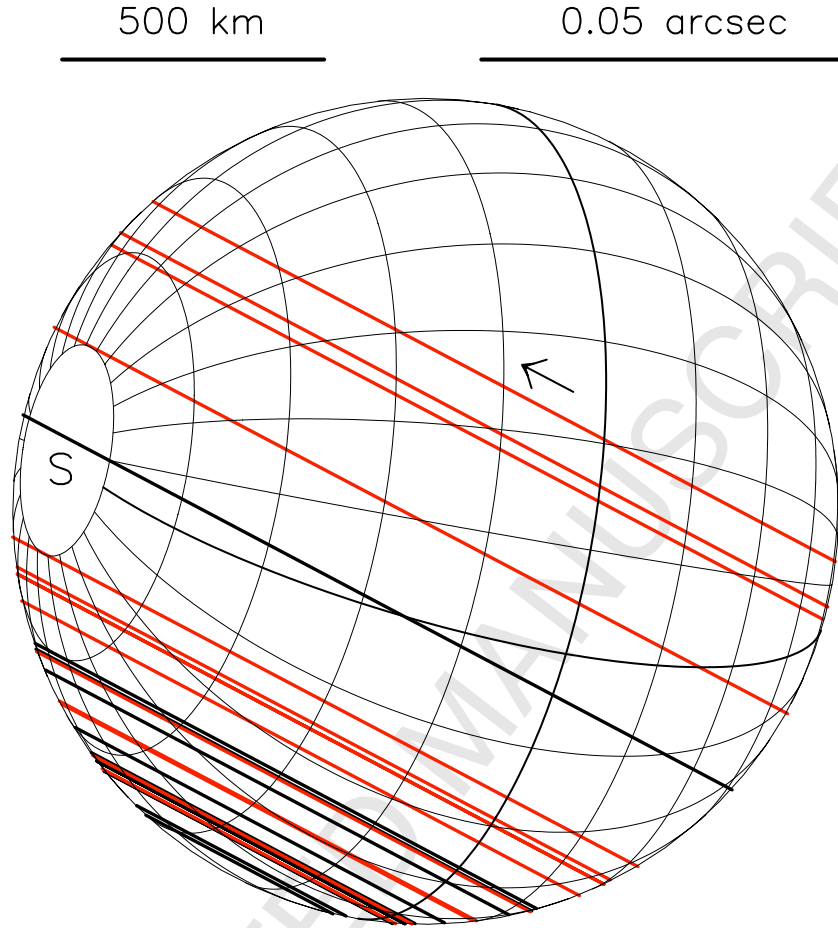


Fig. 11.— The twenty-seven occultation chords used for Titania’s size and oblateness determination through limb fitting (see Section 5). The free parameters of the fit are Titania’s radius, $R_{T,occ}$, and the location of shadow center, as given by the offset $(\Delta f, \Delta g)$. Time shifted chords have been superimposed on a figure of Titania that has been shifted by the ephemeris corrections in Eq. 3. Corresponding ground stations are listed as a subset of Table 2 (footnote “d”). Among them are thirteen visual observations reported by experienced observers (black chords). Red color indicates chords obtained from electronic, frame-by-frame recording of the event (CCD or video), Table 3 lists the applied time shift, sub-occultation titaniacentric latitude coordinate of ingress and egress points, closest approach to shadow center and radial residuals Δr .

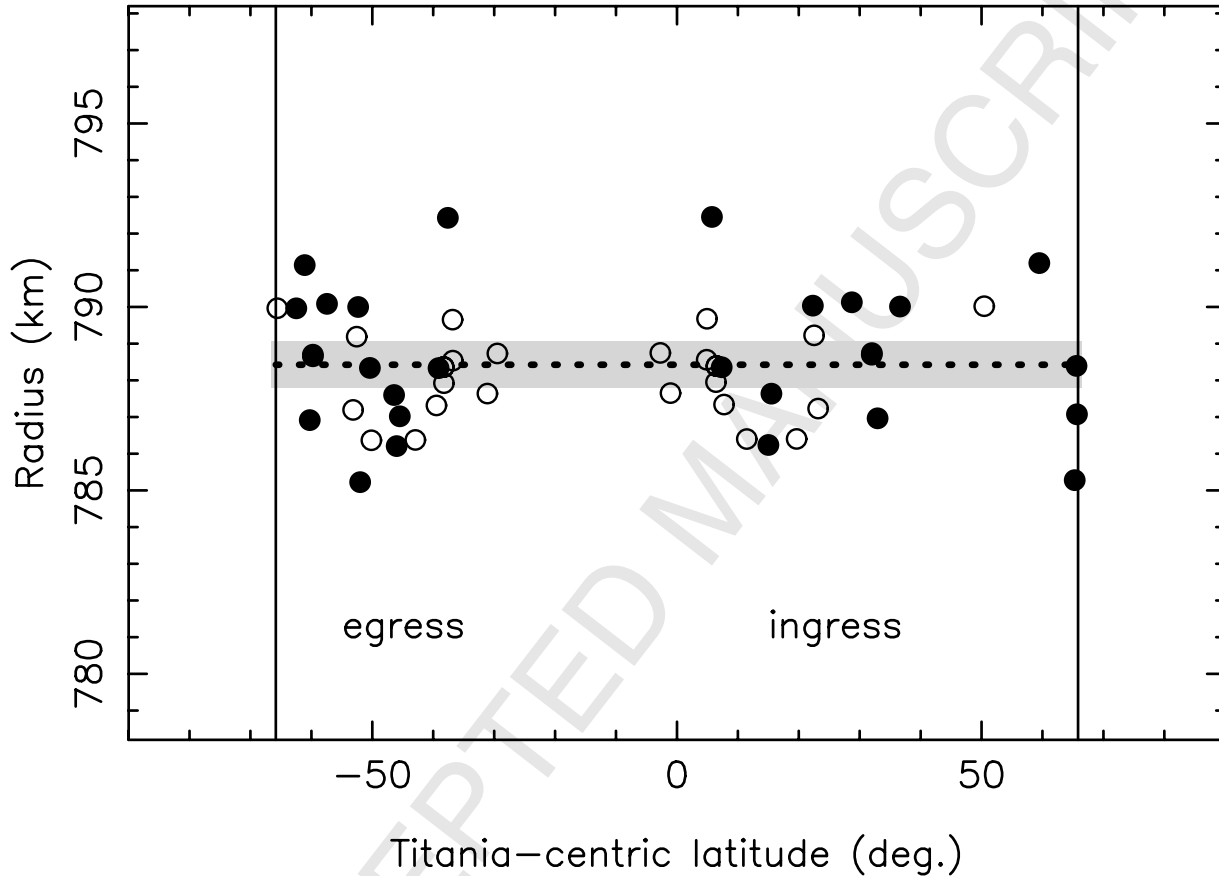


Fig. 12.— Upper limit on Titania’s oblateness.— Residuals of the best circular fit to the 27 occultation chords shown in Figure 11. X-axis is the titaniacentric latitude, with South pole on the left and North pole on the right, from -90° to $+90^\circ$. Y-axis is the distance to Titania’s shadow center. The dotted horizontal line corresponds to the radius of our best circular fit, $R_{T,occ} = 788.4 \pm 0.6$ km, with its error bar (± 0.6 km, shaded rectangle). Bullets indicate the ingress and egress distances $r_{i,obs}$ versus sub-occultation latitude on Titania, after each 27 chords has been shifted in absolute time so they have a common mediatrix. This explains why the points come by pairs (ingress at right and egress at left) with the same distance to shadow center imposing their extremities to have the same radial residuals with respect to a reference circle. The vertical lines marks the maximum latitudes ($\pm 65.8^\circ$) reachable during the occultation, due to the titaniacentric elevation $B = -24.2^\circ$ of the observers during the Sept. 8, 2001 event. Solid bullets are from the 14 stations with an electronic record of the event (CCD or video), while open bullets are from the 13 best visual observations, see Section 5.

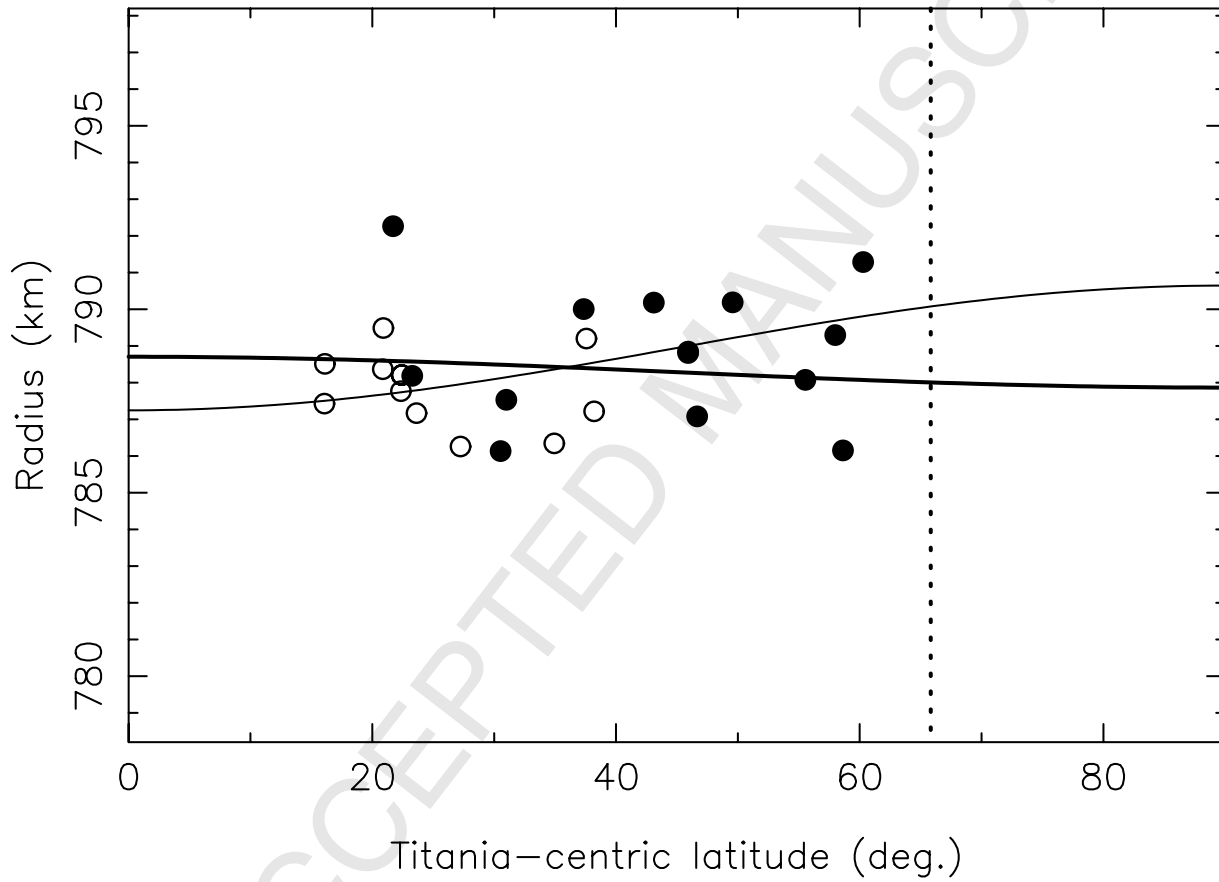


Fig. 13.— Same as Fig. 12, after plotting all latitudes in absolute value, and averaging them over ingress and egress values. The thicker line corresponds to the upper limit of an oblate limb of the form $r = r_{\text{eq}}[1 - f \sin^2 \phi]$, with a difference between equatorial and polar radius of $r_{\text{eq}} - r_{\text{po}} = +0.8$ km. The thin line is the upper limit of a prolate limb, with $r_{\text{eq}} - r_{\text{po}} = -3.4$ km. See text for details.

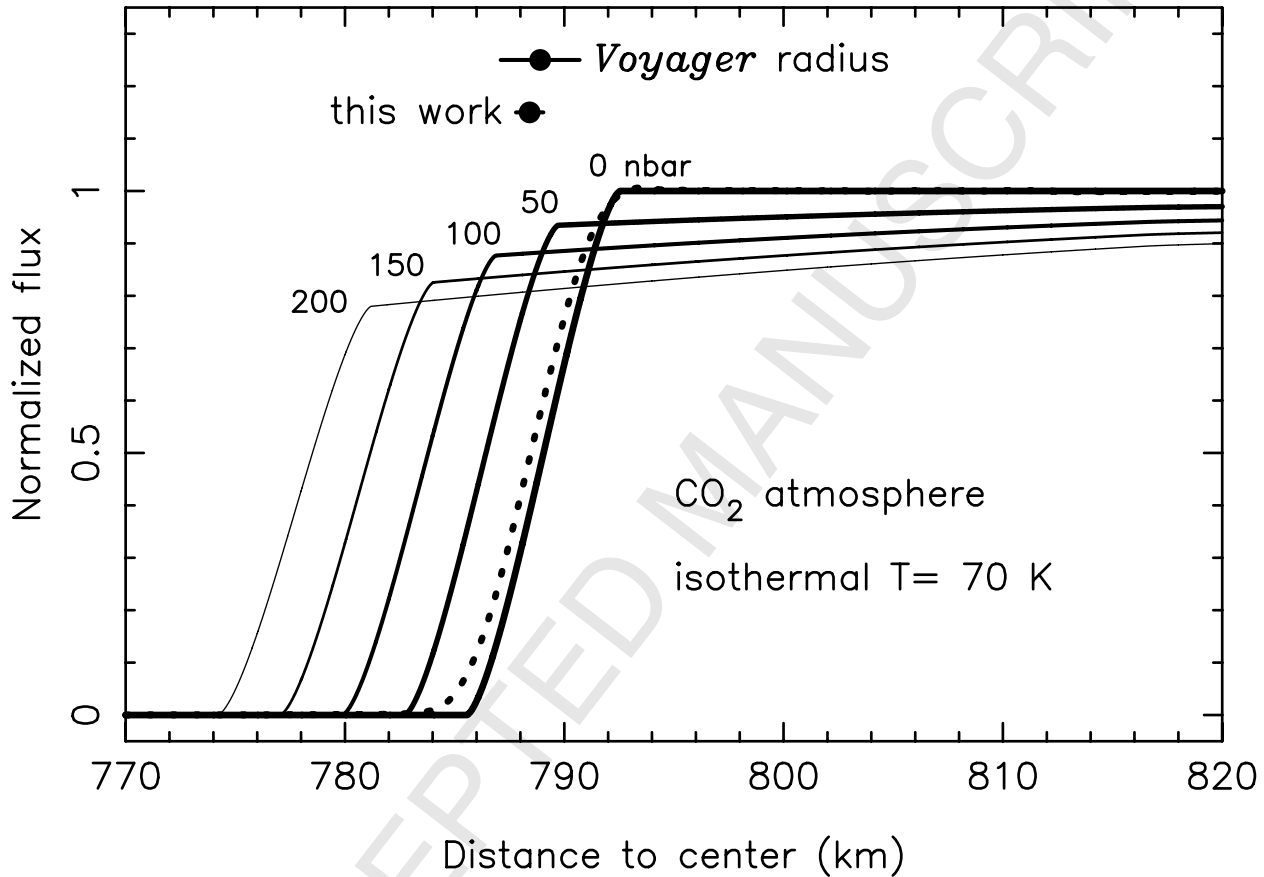


Fig. 14.— Examples of shrinkings of Titania’s shadow radius due to ray bending by a model CO_2 isothermal atmosphere ($T = 70 \text{ K}$) with surface pressures of 0, 50, 100, 150, 200 nbar, in order of decreasing line thicknesses, see also labels above each curve. The model takes into account the smoothing by a 0.51 mas diameter star (but does not account for diffraction effects), and assumes the radius derived from *Voyager* images, 788.9 km (Thomas 1988). The *Voyager* radius and our own measurement are shown by black dots with associated error bars at the top. The dotted line is the diffracting model which best fits our data, see Fig. 5. For this particular model (CO_2 at $T=70\text{K}$), we find that Titania’s apparent radius decreases by about 0.056 km per nbar added to the surface pressure. The stellar drop just prior to the occultation by Titania’s limb amounts to about 1.1×10^{-3} per nbar. For instance, a 200 nbar atmosphere shrinks the radius by about 11.2 km, and causes a drop of 22% by the time the star reaches the satellite limb. See text, Section 6, ¶6.1.

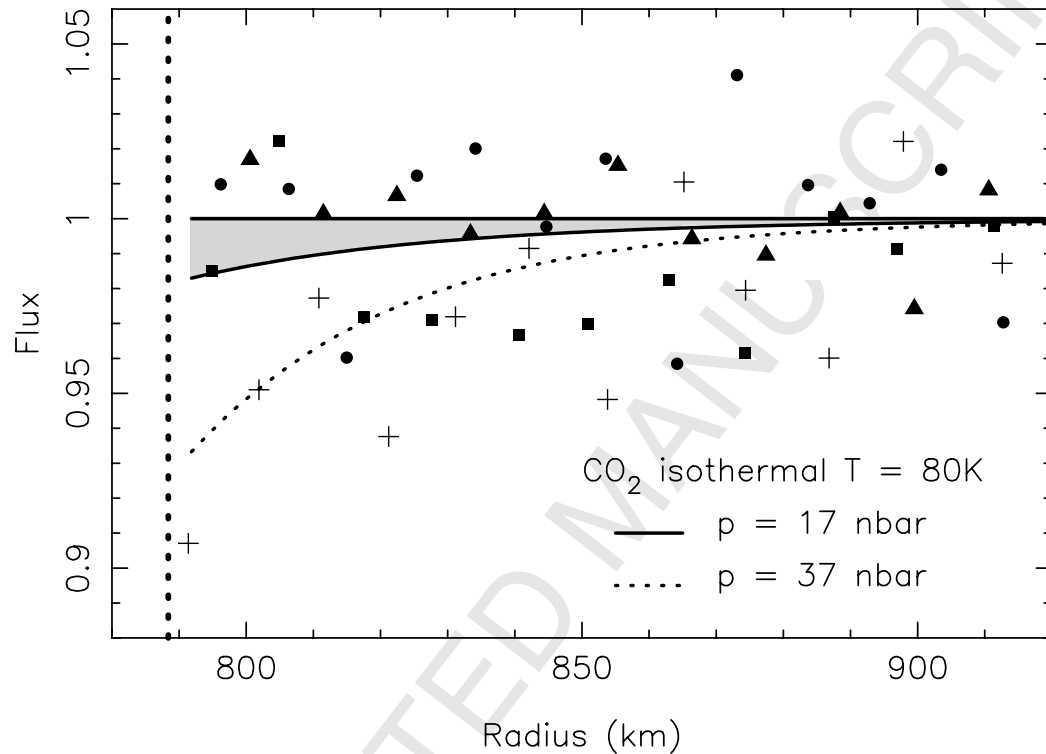


Fig. 15.— Same as Fig. 5, but at different scales, to illustrate the effect of a faint atmosphere on the light curves. Symbols are the same as in Fig. 5, namely Salinas-1 0.25m (squares), Salinas-2 0.20m (bullets), Arikok 0.20m (triangles) and Portimão-1 0.25m (crosses). For each of the four lightcurves, the before-ingress and after-egress data points have been folded over and binned over ~ 20 km vertical bins, in order to take into account the relative velocity of the star perpendicularly to each limb, so that the radial sampling Δr is constant at each station on the plot. In this way the actual contribution of stations to vertical sampling can be assessed, although the fit to model was performed on *actual* data points. The point on left (Portimão) corresponds to the stellar drop behind Titania’s limb at $r < 792$ km (those data points were *not* included in the fit). The dotted vertical line corresponds to our estimate of Titania’s radius best value of 788.4 km. The smooth solid line is the $1\text{-}\sigma$ upper limit for the fit of actual data points to a CO_2 isothermal ($T = 80$ K) model atmosphere, with a surface pressure of 17 nbar. The dotted line is the $3\text{-}\sigma$ upper limit ($p = 27$ nbar). The shaded area shows the difference between this model and an airless model. See Table 5 and text for details.

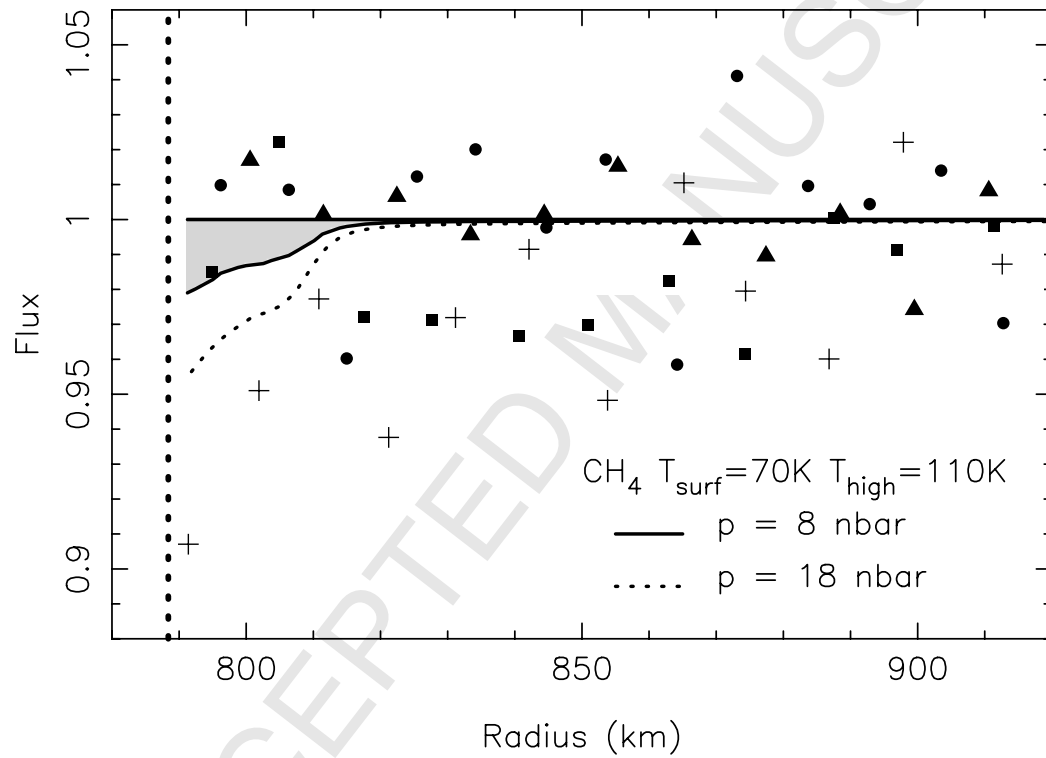


Fig. 16.— Same as Fig. 15, but for methane. The smooth solid line is the $1\text{-}\sigma$ upper limit for a heated CH_4 atmosphere with $T = 70\text{ K}$ at surface level and $T = 110\text{ K}$ above 20 km , with a surface pressure of 8 nbar . The shaded area shows the difference between this model and an airless model, while the dotted line shows the $3\text{-}\sigma$ upper limit ($p = 18\text{ nbar}$) for comparison. See Table 5 and text for details.

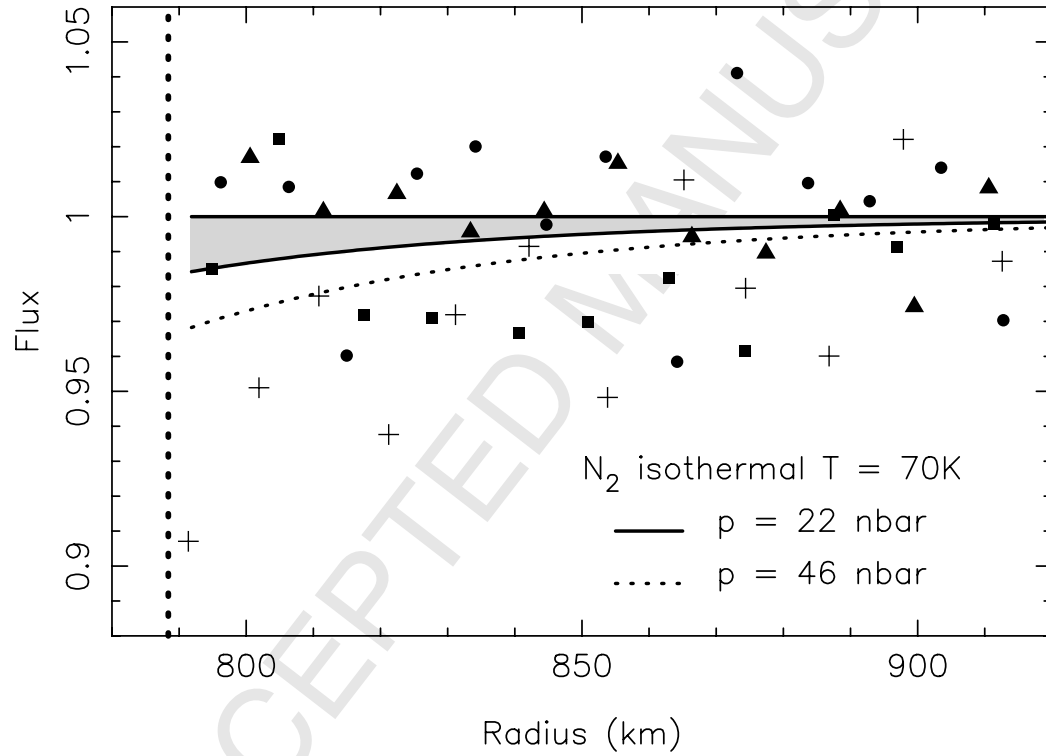


Fig. 17.— Same as Fig. 16, but for an isothermal, $T = 70$ K N_2 atmosphere. The $1\text{-}\sigma$ upper limit is 22 nbar, corresponding to 0.550 cm-amagat (solid line) while the $3\text{-}\sigma$ upper limit corresponds to $p = 46$ nbar or 1.150 cm-amagat (dotted line).