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Theoretical Analysis of a Large Momentum Beamsplitter using Bloch Oscillations

Pierre Cladé, Thomas Plisson, Saïda Guellati-Khélifa, François Nez, François Biraben

Laboratoire Kastler Brossel, UPMC, Ecole Normale Supérieure, CNRS, 4 place Jussieu, 75252 Paris Cedex 05, France

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Abstract. In this paper, we present the implementation of Bloch oscillations in an atomic interferometer to increase the separation of the two interfering paths. A numerical model, in very good agreement with the experiment, is developed. The contrast of the interferometer and its sensitivity to phase fluctuations and to intensity fluctuations are also calculated. We demonstrate that the sensitivity to phase fluctuations can be significantly reduced by using a suitable arrangement of Bloch oscillations pulses.

PACS. 03.75.Dg Atom and neutron interferometry – 37.25.+k Atom interferometry techniques – 67.85.-d Ultracold gases, trapped gases

1 Introduction

Atom interferometry is nowadays a corner stone in high precision measurement. It has been used to determine the fine structure constant [\[1](#page-12-0),[2\]](#page-12-0), as well as the Newton's gravitational constant[[3,4](#page-12-0)], to test general relativity[[5\]](#page-12-0) and to measure gravity[[6,7\]](#page-12-0). In these applications, the interferometers rely on momentum exchange between light and atoms to split and recombine atomic wave-packets. The sensitivity of the measurements is proportional to the spatial separation of the wave-packets in the interferometer. As the beamsplitters are performed with two photon Raman transition, the velocity difference between the arms of the interferometer δv is equal to $2v_r$ (where $v_r = \hbar k/m$ is the recoil velocity, k is the wavenumber of light and m the mass of the atoms). The sensitivity of the interferometer is thus proportional to $2v_rT$ where T is the typical duration of the interferometer¹.

Until recently, the main way to improve the sensitivity of interferometers in order to achieve higher precision measurements was to increase the duration T . However, it requires a careful control of phase noise of the lasers as well as vibrations in order to keep a good signal to noise ratio. Transversal spread of the atomic cloud or motion of the cloud inside the science chamber set a limit to this interaction time. Interaction times of the order of several hundreds of ms are achieved [\[6\]](#page-12-0).

Another method to increase the separation of the wavepackets and so the sensitivity of the interferometer consists in using a large momentum transfer pulse with a separation $\delta v > 2v_r$. High order Bragg diffraction of matter wave can be used to increase δv [[8\]](#page-12-0). However, the laser power required for Bragg diffraction increases sharply with δv [[9\]](#page-12-0). Recently, a double-diffraction technique has been proposed to enhance the area of a Raman atom interfer-ometer[[10](#page-12-0)]. Increasing δv can be also done with Bloch oscillations. It has been suggested and demonstrated by the group of W.D. Phillips on a Bose Einstein condensate [\[11\]](#page-12-0). The coherence of the acceleration with Bloch oscillations (BO) is a key point of the process[[12\]](#page-12-0). More recently, a group at Stanford/Berkeley and our group have implemented this method by inserting the so called large momentum transfer beam splitter (LMTBS) in an atom interferometer [\[13,9](#page-12-0)].

The large momentum transfer beam splitter (LMTBS) is realized with a suitable combination of two processes. The first one, realized with usual methods (Bragg pulse in the group of Stanford/Berkeley and Raman pulses in ours), implements a separation between two wavepackets. The second process is used to selectively and coherently accelerated only one of the wavepackets with Bloch oscillations in order to increase δv . This separation keeps the coherence between the two wave packets.

Our experiment where we demonstrate the realisation of a LMTBS has been described in a letter [\[13](#page-12-0)]. In this paper, we present a model that help us to calculate precisely the efficiency of the LMTBS (first part) and also the phase of the interferometer (second part). The calculation of this phase is a key point to understand the sensitivity of the interferometer (third part).

2 Bloch oscillations

In this section we describe the Bloch oscillation process that is used to increase the separation of atoms in the

¹ For a gravimeter, the velocity change due to gravity is also proportional to T , which leads to a sensitivity to gravity scaling as T^2

interferometer. The phenomenon of Bloch oscillation is a well understand tool to coherently accelerate ultra-cold atoms[\[14\]](#page-12-0). In order to realise a LMTBS, the difficulty is not only to efficiently accelerate atoms but to be able to accelerate only atoms from on arm of the interferometer, keeping the coherence between the two arms.

2.1 Phenomenological description of the acceleration

The Bloch oscillation acceleration is based on coherent transfer of momentum between an accelerated optical lattice and atoms. The optical lattice results from interference of the two lasers beams of the same intensity I , detuned by Δ from the one photon transition. The amplitude of the resulting standing wave is 4I. Atoms endure a periodic potential $U(x)$ due to light-shift (a.c. stark effect) which can be expressed as:

$$
U(x) = \frac{U_0}{2} (1 + \cos(2kx)),
$$
 (1)

where $k = 2\pi/\lambda = 2\pi \nu/c$ is the wavevector of the laser, $U_0 = h \frac{\Gamma^2}{8\Delta}$ $\frac{\Gamma^2}{8\Delta}\frac{I}{I_S}$ with Γ representing the natural linewidth of the excited state and I_S its saturation intensity. In the following, the constant part $U_0/2$ which does not play any role for the explanations is removed from every equation. Because of the periodicity of the potential, the eigenenergies of the system show a band structure [\[15](#page-12-0)]. Each eigenstate is described by a band index n and a quasimomentum q defined modulo $2\hbar k$ [[16\]](#page-12-0). The Fig. 1 represents this band structure, where the first Brillouin zone is unfolded. The splittings between bands at the center $(q = 0)$ and at the edge $(q = \hbar k)$ of the first Brillouin zone occurs where atoms are resonantly coupled by $U(x)$.

In a quantum optics view, the avoided crossing (Bragg resonance) between the first and second bands is connected to the resonance of the two photon transition between states of momentum $p = \pm \hbar k$. Similarly, the splitting between the second and third bands is due to a resonant four photon transition between states of momentum $p = \pm 2\hbar k$, and so on for the nth and $(n + 1)th$ band. The order of the transition grows with the band index, thus the higher the band index is, the weaker is the splitting between the bands.

When the atoms in the first band are subjected to a constant and uniform force, their quasimomentum increases linearly with time. If the force is weak enough to induce adiabatic transition, the atoms stay in the first band and therefore have a periodic motion (Bloch oscillations[[17\]](#page-12-0)). The time necessary for a variation of the quasimomentum of $2\hbar k$ is the period of the oscillations. For atoms in higher band, for a constant acceleration, the probability to make an adiabatic transition (stay in the same band) will be higher for low values of the band index.

Bloch oscillations were initially introduced in the case of a lattice and a uniform force. In our experiment, a constant acceleration is applied to the lattice. This acceleration acts like a force in the frame of the lattice (see

Fig. 1. Band structure of the optical lattice. This graph represents the band energy in the frame of the lattice as a function of the quasi-momentum. Because quasi-momentum is defined modulo $2\hbar k$, one can think of this graph as an unrolled cylinder where the vertical dot-dashed lines are overlapping.

Ref.[[12\]](#page-12-0)), and an equivalent of Bloch oscillations can be observed[[14\]](#page-12-0): the adiabatic transition corresponds to a change of velocity of 2 recoils, whereas a non-adiabatic transition does not change the velocity of the atom (free particle).

In our LMTBS, one wavepacket is loaded in the first band (A, see Fig. 1) and the second in the third band (B). The acceleration is small enough so that atoms in the first band are likely to make an adiabatic transition, but strong enough so that atoms initially in the third band change band. The atoms in the first band are periodically accelerated by 2 recoils momentum. In the same time, atoms in the third band are not accelerated. This process allows us to selectively accelerate atoms depending on their initial velocity.

Note that in our experiment, atoms with different velocities have also different internal states because of the Raman transition used to create the initial splitting. The amplitude of the lattice is then different for the two wavepackets. This effect could be used to select the wavepacket which is going to be accelerated. However for our experimental parameters, the difference in light shift is negligible and so the selection of the accelerated wavepacket relies only on its initial velocity and not its internal state.

2.2 Theoretical description of LMTBS

In order to optimize the efficiency of the LMT beamsplitter, the evolution of the atomic system has been computed. In the laboratory frame, the Hamiltonian of the particle is:

$$
H = \frac{\hat{p}^2}{2m} + V(\hat{x}, t)
$$
 (2)

where $V(x, t)$ is the accelerated periodic potential. If we denote by $U_0(t)$ the amplitude of the lattice and by $\delta \nu(t)$ the frequency difference between the two laser beam. Then

 $v(t) = 2k\delta\nu(t)$ is the velocity of the lattice and

$$
V(x,t) = \frac{U_0(t)}{2} \cos\left(2k\left(x - \int^t v(t')dt'\right)\right) \tag{3}
$$

We should note that, even if the lattice is accelerated, in the laboratory frame, this Hamiltonian is still periodic in space. Therefore the quasimomentum is still a good quantum number and is conserved. This Hamiltonian cannot be solved efficiently, because of the fast time variation of the potential. One could write the Hamiltonian in the accelerated frame. This Hamiltonian will be time independent, but will no longer be periodic, and the quasimomentum will not be conserved.

We use another and convenient transformation which consists in translating the wave function in position space by the quantity $X = \int_0^t v(t') dt'$:

$$
x' = x + X(t) \tag{4}
$$

$$
\psi'(x') = \psi(x) \tag{5}
$$

The Hamiltonian becomes:

$$
H(t) = \frac{(\hat{p} - mv(t))^2}{2m} + \frac{U_0(t)}{2} \cos(2k\hat{x}),
$$
 (6)

where the energy shift $mv(t)^2/2$ is left out. This Hamiltonian described the Bloch oscillation in the "solid-state physics" point of view[[12\]](#page-12-0). The advantage of this presentation is that the Hamiltonian is time independent when the lattice is moving at a constant velocity.

If we start with a plane wave of momentum p_0 (and therefore of quasi-momentum $q_0 = p_0$ modulo $2\hbar k$), the wavefunction will remain in the subspace of states of quasimomentum q_0 . We therefore choose to solve the problem in the basis of the plane wave of momentum $p_0 + 2l\hbar k$, $l \in \mathbb{Z}$ which is a basis of this subspace.

To solve numerically the problem i npractice, the momentum basis is restricted to a finite number of $l, |l| \leq$ N_{cut} . The value of N_{cut} is set by the maximal velocity of atoms in the optical lattice. It results from the sum of the number of oscillations (velocity of the atom) and the width of the velocity distribution of the Bloch states $(\Delta p/\hbar k)$. This width Δp is set by the Wannier function in momentum space[\[18\]](#page-12-0) which is given by the wave function of an atom trapped in a single well without tunnelling between sites. The frequency ω of the trap is proportional to $\sqrt{|U_0| E_r}$. For the ground state of an harmonic oscillator, $\Delta p = \sqrt{\hbar m \omega/2}$. We obtain that $\Delta p/\hbar k \simeq \sqrt[4]{U_0/E_r}$ [[18,19\]](#page-12-0). In our calculation, we have used $N_{\text{cut}} = 10$ for 2 oscillations and $U_0 \simeq 8E_r$.

The Hamiltonian is calculated using the dimensionless parameters $\kappa = U_0/8E_r$ (where $E_r = \frac{\hbar^2 k^2}{2m}$ is the recoil energy) and $p(t) = (p_0 + mv(t))/\hbar k$. All the units are scaled so that $\hbar = k = m = 1$.

The expression of the Hamiltonian H and the ket $|\psi\rangle$ are reduced to :

$$
H = \begin{bmatrix} \ddots & \kappa & 0 & \dots & 0 & \dots & 0 \\ \kappa & p_{-l}^2/2 & \kappa & \ddots & \vdots & & \vdots \\ 0 & \kappa & \ddots & \kappa & 0 & \dots & 0 \\ \vdots & \ddots & \kappa & p_0^2/2 & \kappa & \ddots & \vdots \\ 0 & \dots & 0 & \kappa & \ddots & \kappa & 0 \\ \vdots & & \vdots & \ddots & \kappa & p_l^2/2 & \kappa \\ 0 & \dots & 0 & \dots & 0 & \kappa & \ddots \end{bmatrix}, |\psi\rangle = \begin{bmatrix} \vdots \\ c_{-l} \\ \vdots \\ c_0 \\ \vdots \\ c_l \\ \vdots \end{bmatrix} (7)
$$

where $p_l = p(t) + 2l$. Each coefficient c_l represents the amplitude of probability for the state to be in the plane wave of momentum $2*l*h*k*$.

The LMT pulse is switched on (and off) adiabatically to maximize the number of atoms transferred from an atomic state with well known momentum p_0 (plane wave) to a Bloch state with a quasimomentum $q_0 = p_0$ in the band n (and reciprocally)[\[18\]](#page-12-0). In between, the lattice is accelerated to transfer a given number of recoils to one component of the wavefunction. We denote by t_{adiab} the duration of the linear ramp used to switch on and off the lattice, T_{acc} the duration of the acceleration, 2N the number of transferred recoils, U_0 the maximal amplitude of the lattice and p_0 the initial momentum of the atoms.

2.3 Optimization of the acceleration

The optimization of the acceleration results from a compromise between an adiabatic acceleration of the atoms in the first band and a strong enough (non-adiabatic) acceleration of the atoms in the third band. Reciprocally, for a given acceleration, the amplitude of the lattice should be in a given range in order to satisfy this latest compromise. In our experiment, it is easier to vary the amplitude of the lattice. Therefore, we have plotted on the Fig. [2](#page-4-0) the probability for an atom to stay in its band as a function of the lattice amplitude κ for the first (solid line) and third (dashed line) bands. There is clearly an intermediate regime where the probability η_{11} for an atom to stay in the first band is high whereas the probability η_{34} for an atom to leave the third band (and reach the fourth one) is also high. The efficiency of the LMT is calculated as

$$
\eta = \eta_{11}\eta_{34}.\tag{8}
$$

It sets the contrast of the interference pattern of the two wavepackets. The value of η is plotted on Fig. [2](#page-4-0). For our experimental parameters (an acceleration of 2 recoils in 200 μ s), the maximum efficiency is about 98% for κ = 1. This maximum η_{max} , and the optimal value κ_{opt} of κ depends upon T_{acc} . The values of η_{max} and κ_{opt} versus T_{acc} are plotted on Fig. [3](#page-4-0). For an infinite duration of T_{acc} , the efficiency is closed to one while the value for $\kappa_{\rm opt}$ is nearby zero.

Fig. 2. Transfer probability as a function of the maximal optical depth $\kappa = U_0/8E_r$ of the lattice. The acceleration is in 200 μ s for N=2 recoils. Solid line: transfer probability for the first band η_{11} ; dashed line: for the third band, $\eta_{33} \approx 1 - \eta_{34}$; diamond: Efficiency of the LMT pulse, $\eta = \eta_{11}\eta_{34}$.

This behavior is understandable using the Landau-Zener criteria which can be used to calculate transition probabilities in the weak binding limit ($\kappa \ll 1$), [\[12\]](#page-12-0):

$$
\eta_{11} = 1 - \exp\left(-\pi \frac{\kappa^2}{a}\right) \tag{9}
$$

$$
\eta_{34} = \exp\left(-\pi \frac{\kappa^6}{768a}\right) \tag{10}
$$

where $a = m^2/\hbar^2 k^3 dv/dt$, is the dimension-less acceleration of the lattice. We clearly see that for a small value of κ , there is a value of a so that $\frac{\kappa^6}{768a} \ll 1$ and $\frac{\kappa^2}{a} \gg 1$ leading to efficiencies η_{11} and η_{34} close to one. In fact, there is no theoretical limitation to the weakness of κ . There is always a suitable value of a which sets η close to unity. However, this suitable value of a becomes very small, which means that an infinite amount of time is required for the acceleration. In an other way, with a given value of a, the higher is a, the lower is η with an optimized κ.

In the experimental point of view, the duration of LMT pulse can not be extend as much as we want. This duration has to be smaller than the time separation between the $\pi/2$ pulses of our interferometer. The time separation between $\pi/2$ pulses results from a compromise between the narrowest width of the atomic fringes (and so the resolution of the interferometer) and the vibrations of the experimental set up. Practically, the comparison of the theoretical and experimental results presented in this paper is done with $T_{\text{acc}} = 0.2 \text{ ms}$ (for two oscillations). We will briefly explain at the end of this paper a way to transfer a larger number of recoils using a non constant acceleration.

2.4 Adiabatic loading of atoms in the lattice

In the previous section, the efficiency η of the separation has been calculated assuming that atoms are initially in a

Fig. 3. Efficiency of the LMT pulse as a function of the total duration of the acceleration for two Bloch oscillations. For each value of the duration, we calculate the value $\kappa_{\rm opt}$ of the amplitude κ of the lattice that optimizes the efficiency. This value is plotted in the inset of the figure. The "saw tooth" shape of $\kappa_{\rm opt}$ (and therefore of η_{opt}) is due to small oscillations between the bands. They do not appear in the Landau-Zener model which doesn't take into this effect (lost atoms cannot go back into their initial band).

well defined Bloch state. Yet, in our experiment, we deal with a subrecoil velocity distribution, thus the best description of the initial state is in a plane wave basis. To load the atoms into a Bloch state, the lattice depth is increased adiabatically. Atoms in an initial momentum p_0 are loaded into the Bloch state $|n, p_0\rangle$, where the band index *n* is the nearest integer above $|p_0/\hbar k|$.

The amplitude of probability η_t to load atoms in a given band is defined as $|\langle \psi | n, p_0 \rangle|$ where $|\psi \rangle$ is the wave function and $|n, p_0\rangle$ the Bloch wave function. This probability depends upon the loading time t_{adiab} , the final depth of the lattice U_0 (the amplitude of the lattice is linearly increased) and the momentum p_0 . The Fig. [4](#page-5-0) shows, as functions of the duration t_{adiab} , the probabilities η_t to load atoms either in the first or in the third band. With an initial quasi-momentum $q_0 = 0.5$, the probability η_t is higher for the third band than for the first one because the coupling with the lattice gets weaker with the increase of band index.

On Fig. [5,](#page-5-0) this efficiency η_t is plotted versus the initial quasi-momentum for $t_{\text{adiab}} = 150 \,\mu s$ and for $U_0 = 8E_r$.

In the case of atoms loaded in the first band, the efficiency is maximum at the center of the first Brillouin zone $(p_0 = 0)$. At the edge of the first Brillouin zone $(p_0 = \hbar k)$, η_t is exactly 50%. In this situation, it is indeed not possible to adiabatically transfer the atoms into the optical lattice, because the initial state is degenerate. The same phenomena occurs on the two edges of the third zone ($p_0 = 2\hbar k$) and $p_0 = 3\hbar k$. The same difficulty happens at the end of the LMT pulse when the atoms are transferred back from the lattice to a well defined momentum state (plane wave).

Fig. 4. Transfer probability for the loading of atoms in the optical lattice as a function of loading time t_{adiab} . The quasimomentum is $q_0 = 0.5$ and the final amplitude of the lattice is $U_0 = 8E_r.$

Fig. 5. Transfer probability for the loading of atoms in the optical lattice as a function of the initial quasi-momentum q_0 in unit of $\hbar k$ for atoms in the first and third band of the lattice, $t_{\text{adiab}} = 150 \text{ }\mu\text{s} \text{ and } \kappa = 1.$

2.5 Total efficiency of the LMT

We have calculated the total efficiency η_{tot} with the following parameters: $t_{\text{adiab}} = 150 \mu s$, $T_{\text{acc}} = 200 \mu s$, $N = 2$, $U_0 = 8E_r$. Those parameters correspond to an optimization of the efficiency, keeping the total time (defined as $2t_{\text{adiab}} + T_{\text{acc}}$ constant but varying the amplitude of the lattice and t_{adiab} (see Fig. 6).

The total efficiency is plotted as a function of the initial momentum p_0 on Fig. 7. It is computed including the contributions of the adiabatic loading (and unloading) of the atoms in the lattice. In the first band, the state of initial quasimomentum $q_0 = 1$ and in the third bands, the states of initial quasi-momentum $q_0 = 0$ and $q_0 = 1$ are degenerated states. Therefore these atoms cannot be adiabatically loaded in the lattice. Consequently, it is important to optimize the width of the initial momentum distribution such that it fits in the range where the process is very efficient. However, the wider is the initial velocity distribution loaded into the LMT pulse, the higher is the

Fig. 6. Time evolution of the amplitude $\kappa = U_0/8E_r$ of the lattice and of the velocity v of the lattice for a beam splitter with 2 oscillations. These parameters correspond to an acceleration of about 100 m.s^{-1} .

Fig. 7. Total efficiency η_{tot} of the LMT pulse as a function of the initial momentum p_0 .

number of atoms that contributes to the interferometer and so the larger is the signal to noise ratio. Nevertheless, note that the total efficiency is larger than 95% on a wide range of p_0 .

3 Phase shift of the interferometer

In the preceding section, we have calculated the efficiency of the LMT beamsplitter. This efficiency is one of the key parameter for calculating the contrast of the interferometer. Another parameter of the interferometer, is the phase shift. In the following section, we describe in detail how it can be calculated.

3.1 Ramsey-Bordé interferometer

Let us briefly recall the principle of a Ramsey Bordé interferometer realized with Raman pulses (see Fig. [8\)](#page-6-0). It is based on a succession of four $\pi/2$ Raman pulses (or, a succession $\pi/2$ - π - $\pi/2$). Each Raman pulse couples two states (labeled $|g_1\rangle$ and $|g_2\rangle$) of the hyperfine structure of the ground state of the atom via a two photon transition in a Λ scheme. The two laser used for the transition are counterpropagating, therefore, the two states have different velocities. This allow us to split the initial wave packet

in two. The relative phase between the two states is determined by the phase of the laser beams used for the Raman transition. The second and third pulse are used as mirror to modify the trajectory of atoms and the fourth pulse is used to recombine the two wavepackets.

A simple way to precisely understand the output fringes pattern of the interferometer is to consider the contribution of each pair of $\pi/2$ pulses. After the first pair of $\pi/2$ pulses, the velocity distribution of atoms in state $|g_2\rangle$ follows a Ramsey fringes pattern (see Fig. 8). Thanks to the Doppler effect, the frequency difference between Raman beams sets the center of the Ramsey fringes pattern and select the most populated velocity class in the initial velocity distribution. Atoms which have not been transferred are eliminated. The second set of $\pi/2$ pulses, also Doppler sensitive, is used to probe the selected velocity distribution. The resulting signal of the interferometer is the product of these two Ramsey distributions. By scanning the frequency difference of the lasers used for the second set of pulses, the second Ramsey pattern is translated in velocity space. The resulting signal versus laser frequency difference is the convolution of the two distributions created with each pair of $\pi/2$ pulses. The center of this convolution profile gives access to the velocity of the selected atoms.

The resolution of the velocity measurement is given by the fringe width. For a counterpropagating Raman transition, the Doppler shift of an atom at velocity v is 2kv. The frequency splitting of the fringes in the convolution profile is $2\pi/T_{\text{Ramsey}}$, *i.e.* $\lambda/2T_{\text{Ramsey}}$ in velocity space. This expression can also be understood as resulting from the interference of two selected wave packets: they are spatially separated by $\Delta X = 2v_rT_{\text{Ramsey}}$. In velocity space, the interference produces fringes with a separation $\frac{h}{m\varDelta X}=\frac{\lambda}{2T_{\mathrm{Ramsey}}}$.

There are different ways of modelling an atomic interferometer. One can, for example, use the Feynman path integral method [\[20,21\]](#page-12-0). However, this method does not fit very well with the description of Bloch oscillation made in the first section of this paper, where we use plane wave.

We therefore describe the atom interferometer using also a plane wave basis. We will first introduce how this description can be used for a regular Ramsey-Bordé interferometer and then extend it to the LMT interferometer.

3.2 Modelisation of the interferometer

We are going to calculate the evolution of a wave packet through the interferometer. This wavepacket will be descibed as a superposition of plane waves with a mean momentum p_0 . During the interferometer the packet will be split into two paths (labeled A and B). Looking only to the evolution of a plane wave one can calculate the interference fringes and also the positions of the center of the wave-packet, given by the derivative of the phase with respect to the momentum p_0 .

Fig. 8. Scheme of the usual Ramsey Bordé interferometer. A first set of two $\pi/2$ pulses, separated by a delay T_{Ramsey} , select a Ramsey fringe pattern in velocity space (1). A second set of two $\pi/2$ pulses, with the same delay is used to close the interferometer. The probability for an atom to be transferred by the second set of $\pi/2$ pulses from one state to the other is recorded as a function of the difference between the frequency of the laser during selection δ_{sel} and measurement δ_{meas} (2). This interferometer measure then the velocity variation between the selection and measurement pulses.

Fig. 9. Scheme of an interferometer using LMT beamsplitters. With this scheme four LMT Bloch pulses (labelled B) are inserted between the Raman $\pi/2$ pulses. In the experiment, we use a more sophisticated scheme described Fig. [10](#page-8-0).

The output of the interferometer can be precisely calculated. We have to solve the Schrödinger equation:

$$
i\hbar \frac{\partial |\psi\rangle}{\partial t} = H(t) |\psi\rangle \tag{11}
$$

where the Hamiltonian $H(t)$ is the sum of the free Hamiltonian H_0 and the Raman interaction $V_R(t)$ with

$$
H_0 = \frac{\hat{p}^2}{2m} + \hbar \omega_{12} |g_2\rangle \langle g_2| \tag{12}
$$

where $\hbar\omega_{12}$ is the energy difference between the two states $|g_2\rangle$ and $|g_1\rangle$ and

$$
V_{\rm R}(t) = \frac{\Omega(t)}{2} \left(e^{i(\phi_{\rm R}(t) + k_{\rm eff}\hat{x})} |e\rangle \langle g| + h.c. \right) \tag{13}
$$

where $\Omega(t)$ is equal to the Rabi pulsation of the two photon Raman transition $(\Omega_0$ during the pulses and 0 elsewhere), $\hbar k_{\text{eff}}$ is the effective recoil transferred by the Raman pulses and $\phi_R(t)$ is the phase difference between the two lasers.

We choose to solve this Hamiltonian using the plane wave basis. We then have a two levels system $|g_1, p_0\rangle$ and $|g_2, p_0 + \hbar k_{\text{eff}}\rangle$. We also write the phase of the laser as $\phi_R(t) = \omega_{12}t + \phi(t)$ and change the ket $|g_2\rangle$ to $e^{i\omega_{12}t} |g_2\rangle$ (rotating frame). The Hamiltonian is then this 2x2 matrix:

$$
H = \begin{bmatrix} p_0^2/2m & \Omega(t)e^{i\phi(t)}/2\\ \Omega(t)e^{-i\phi(t)}/2 & (p_0 + \hbar k_{\text{eff}})^2/2m \end{bmatrix}
$$
 (14)

This Hamiltonian contains the phase shift induced by the kinetic energy and the phase transferred from light to atoms during a Raman transition. Assuming that $\phi(t)$ is almost constant during the pulse, we obtain that from $|g\rangle$ to $|e\rangle$ we add a phase $\phi(t)$ and from $|e\rangle$ to $|g\rangle$ we remove this phase.

The final proportion of atoms transferred to state $|e\rangle$ will vary as $\sin(\Phi)$ with $\Phi = \phi_A - \phi_B$ is the phase difference of the two paths with:

$$
\phi_A = \phi_1 - \phi_3 + \phi_A^{\text{sel}}(p_0) + \phi_A^{\text{mes}}(p_0)
$$
 (15)

$$
\phi_B = \phi_2 - \phi_4 + \phi_B^{\text{sel}}(p_0) + \phi_B^{\text{mes}}(p_0)
$$
 (16)

where $\phi_i = \phi(t_i)$ are the phases at the time $t_{1,2,3,4}$ of the four Raman pulses and $\phi_{A/B}^{\text{sel/mes}}(p_0)$ are the phases due to kinetic energy:

$$
\phi_A^{\text{sel}}(p_0) = \phi_B^{\text{mes}}(p_0) = T_{\text{Ramsey}} \frac{(p_0 + \hbar k_{\text{eff}})^2}{2m\hbar} \quad (17)
$$

$$
\phi_B^{\text{sel}}(p_0) = \phi_A^{\text{mes}}(p_0) = T_{\text{Ramsey}} \frac{p_0^2}{2m\hbar} \tag{18}
$$

The phase can also be written as

$$
\Phi = \Phi_{\text{laser}} + \Phi_{\text{kinetic}} \tag{19}
$$

with $\Phi_{\text{laser}} = (\phi_1 - \phi_3) - (\phi_2 - \phi_4)$ and $\Phi_{\text{kinetic}} = (\phi_A^{\text{sel}}(p_0) +$ $\phi_A^{\text{mes}}(p_0) - (\phi_B^{\text{sel}}(p_0) + \phi_B^{\text{mes}}(p_0)).$

We observe that $\Phi_{\text{kinetic}} = 0$ when the velocity of atoms is constant between the pulses. In the case where there are uniform forces that change p_0 , we have to integrate the kinetic energy and we obtain that:

$$
\Phi_{\text{kinetic}} = \frac{k_{\text{eff}}}{m} \int_0^{T_{\text{Ramsey}}} (p_0(t_1 + \tau) - p_0(t_3 + \tau)) \text{d}\tau \tag{20}
$$

The phase is a direct measurement of the momentum variation between the first pair of pulses and the second one.

Let us consider the case where there is a small change of velocity δv between the second and third pulse. The sensitivity of the interferometer is proportional to the derivative of Φ with respect to δv .

Using the more general value of Φ , and the fact that $\phi_A^{\text{sel}}(p_0) = \phi_B^{\text{mes}}(p_0)$ and $\phi_B^{\text{sel}}(p_0) = \phi_A^{\text{mes}}(p_0)$, we calculate that

$$
\frac{\partial \Phi}{\partial \delta v} = m \left(\frac{\partial \phi_A^{\text{sel}}}{\partial p} - \frac{\partial \phi_B^{\text{sel}}}{\partial p} \right) \tag{21}
$$

This equation tell us that in order to compute the sensitivity of the interferometer, we need only to calculate precisely the phase shift accumulated during half of the interferometer. Provided that the forces are uniform, this phase can be calculated for plane waves only.

Further more, in quantum mechanics, the mean position $\langle X \rangle$ of a wave-packet can be calculated as the derivative of the phase with respect to momentum:

$$
\langle X \rangle = \hbar \frac{\partial \phi}{\partial p} \tag{22}
$$

The equation 21 shows directly that the sensitivity is proportional to the spatial separation of the wave-packet:

$$
\frac{\partial \Phi}{\partial \delta v} = \frac{m}{\hbar} \left(\langle X_A \rangle - \langle X_B \rangle \right) \tag{23}
$$

4 Large area interferometer

The interferometer based on large momentum transfer (LMT) Bloch pulses is similar to the usual Ramsey Bordé interferometer. Raman pulses are used in the same configuration and the LMT Bloch pulses are simply inserted between the two $\pi/2$ pulses used either for the selection or the measurement of the velocity. A first implementation consists in accelerating and then decelerating the atoms of one arm of the interferometer for the selection (and then the atoms of the other arm for the measurement). The temporal sequence of such an interferometer is presented on Fig. [9.](#page-6-0)

In the following section, we will present how this acceleration is implemented, and then the numerical calculation of the phase shift Φ of such an interferometer.

4.1 Implementation of LMTBS in the set-up

In our experiment, another arrangement slightly more complicated than the one on Fig. [9](#page-6-0) is used: we accelerate successively each arm of the interferometer with two LMT pulses of opposite directions and then decelerate them with two other pulses. As we will see later, in such a way the contribution of some systematic effects is reduced because the two arms are illuminated with Bloch beams in a more symmetric way. The whole interferometer used in our experiment is presented on Fig. [10](#page-8-0). It is realized with four Raman $\pi/2$ pulses and eight LMT Bloch pulses (la-beled B on the figure [10\)](#page-8-0): each $\pi/2$ pulse is associated with two LMT pulses used to accelerate selectively each arm of the interferometer.

After the first $\pi/2$ pulse, atoms are in a superposition of states $|g_1, p_0\rangle$ and $|g_2, p_0 + 2\hbar k\rangle$. A first LMT pulse is used to accelerate atoms with initial momentum $p_0 + 2\hbar k$.

Fig. 10. Temporal sequence of the interferometer for $N=2$. From bottom to top: intensity of the Raman (dashed line) and Bloch (solid line) beams; velocity of the atoms in the first and second arms of the interferometer; trajectories of atoms in the two arms.

Their momentum became $p_0 + 2\hbar k + 2N\hbar k$ after N oscillations. Then atoms with initial momentum p_0 are accelerated in the opposite direction. Therefore a superposition of $|g_2, p_0 + 2\hbar k + 2N\hbar k\rangle$ and $|g_1, p_0 - 2N\hbar k\rangle$ states is created. After a delay T_{Ramsey} , the same sequence of two LMT pulses is repeated but in reverse order, to bring back atom states in the initial superposition of $|g_1, p_0\rangle$ and $|g_2, p_0 + 2\hbar k\rangle$. Finally, the sequence is ended with a second Raman $\pi/2$ -pulse. The wavefunction of atoms in the state $|g_2\rangle$ results from the interference between atoms transferred during the first $\pi/2$ pulse and atoms transferred during the second one of the selection sequence.

The interferometer is then closed in position space using a second set of Raman and LMT pulses identical to the first one. As for the regular interferometer, the resulting signal of the interferometer (population in $|g_1\rangle$ and $|g_2\rangle$) vary as $\sin(\Phi)$, where Φ is the phase difference between the two arms of the interferometer.

On can write Φ as the sum of three phases:

$$
\Phi = \Phi_{\text{Raman}} + \Phi_{\text{Bloch}} + \Phi_{\text{kinetic}} \tag{24}
$$

The Raman and kinetic phase are the same as for the usual Ramsey-Bordé interferometer. The Bloch phase includes all the phases shift during the Bloch separation, due to the phase of the laser, the light shift of atoms in the lattice and the kinetic energy.

The Bloch phase is the difference between the Bloch phase $\Phi_{\text{Bloch}}^{A/B}$ accumulated in the path A and B. For a given sequence of the optical lattice (velocity and amplitude) and an initial momentum p_0 , we calculate the coefficients c_l (c.f. eq. [7\)](#page-3-0) corresponding to the evolution of the state $|p_0\rangle$ (resp. $|p_0 + 2\hbar k\rangle$) using the model described earlier. The contribution of the first pulse to Bloch phase is deduced from the phases of the coefficients c_{-N} (resp.

Fig. 11. Interference fringes observed using the scheme depicted on Fig. 10. On this figure, the main source of noise is the detection noise.

 c_{N+1}). The same method is used for all Bloch pulses. This allow us finally to calculate the total phase for the 2 first beamsplitter, $\Phi_{\text{sel}}^{A/B}$. From this phase we deduce the position of the wave packets $\langle X_{A/B} \rangle = \frac{\partial \Phi_{\text{sel}}^{A/B}}{\partial p_0}$. The sensitivity of the interferometer can be deduced using equation([23\)](#page-7-0).

4.2 Experimental results

The experimental setup and the main results have been described in a previous paper[[13\]](#page-12-0). We briefly remind the results to compare them with the theoretical model. We use rubidium 87 atoms, consequently the two levels coupled by the Raman transition are the $|F = 2\rangle$ and $|F = 1\rangle$ hyperfine level of the ground state.

The Fig. 11 shows the proportion of atoms detected in the internal state $F = 1$ as a function of the frequency difference between selection and measurement using the time sequence reported on Fig. 10.

The periodicity of the fringes (Fig. 11) is about $\delta_{\rm sep}$ = 50 Hz for the time sequence depicted on Fig. 10.

Quantitatively, δ_{sep} can be compared with the periodicity of fringes of an interferometer without LMT Bloch pulses. With a delay of 5 ms between the two Ramsey pulses of the selection, the periodicity would have been 200 Hz. Therefore with LMT pulses, the sensitivity of the interferometer is improved by about four.

We can define an effective time $T_{\text{eff}} = 1/\delta_{\text{sep}}$, which is of about 20 ms. Because the fringes spacing depends only on the separation of the two arms of the interferometer, the effective time T_{eff} can be viewed as the Ramsey time in a regular Ramsey-Bordé interferometer which leads to the same spatial separation of the two wave packets.

More rigorously, T_{eff} and the spatial separation $\langle X_A \rangle$ – $\langle X_A \rangle$ of the two wave packets are linked through the fol-

Fig. 12. Effective time T_{eff} as a function of the total time of the selection. The temporal sequence described Fig. [10](#page-8-0) is kept constant, except for T_{Ramsey} . Solid curve: Numerical calculations. Inset: sensitivity gain of the LMT interferometer compared to a regular Ramsey Bordé interferometer of the same total duration.

lowing equation:

$$
T_{\text{eff}} = \frac{\langle X_A \rangle - \langle X_B \rangle}{2v_r}.
$$
 (25)

The dependence of T_{eff} with the duration of the selection sequence has been also investigated experimentally. The duration of the time-sequence of the interferometer is adjusted by changing T_{Ramsey} keeping the same $\pi/2$ -Bloch-Bloch sequence. The variation of T_{eff} versus T_{Ramsey} is reported again on Fig. 12. There is an excellent agreement between experiment and calculations.

In the inset of the Fig. 12, we have also plotted the gain in resolution (ratio between the effective time and the real time) as a function of the duration of the selection. At the limit where T_{Ramsey} is long, the duration of the pulses can be neglected and the gain will be exactly $2N+1$, i.e. 5 for our parameters. At shorter times, this gain is smaller.

The experimental data fits well with the predicted time which is a strong evidence that the fringes observed on Fig. [11](#page-8-0) are due to the LMT pulses.

4.3 Light shift in the interferometer

Light shift in the interferometer are one of the main source of systematic effect. Furthermore they can induce a reduction of the contrast of interference.

The mean energy of atoms is indeed shifted when the lattice is switched on. This shift is not the same between the different bands and it depends on the intensity of the lattice. Our scheme (see Fig. [10](#page-8-0)) is on average symmetric: that is the time spent by atoms in a given energy band is equal for each arm of the interferometer. Consequently, there is no associated systematic shift if the intensity seen by atoms is constant. However, experimentally, this condition is never realized because of temporal fluctuations

of the laser intensity and because of motion of the atoms through the spatial profile of the laser beam. In the first case, fluctuations of the intensity will be the same for each atom, leading to a phase noise in the interference pattern. In the second case, the light shift contribution will be averaged over all the atoms, leading to a reduction of the fringes contrast.

The light shift are implicitly included in the phase Φ_{Bloch} obtained by integrating the Schrödinger equation. This phase depends on the intensity of the laser over time. For small variation of intensity, one could linearized the variation of the phase and compute the functional derivative of the phase with respect to the intensity:

$$
a(t) = \frac{\delta \Phi}{\delta I(t)}\tag{26}
$$

In the experiment the intensity of the laser is modulate by an acousto-optic modulator. The intensity is therefore the product of the modulation $(M(t))$ due to the AOM and the intensity without modulation $I_0(t)$. If we assume that the modulation for the LMT pulse does not fluctuate $(\delta M(t) = 0)$, then the fluctuation of the phase is mainly due to fluctuations of $I_0(t)$ around its constant mean value I_0 .

In the following instead of calculating $\frac{\delta \Phi}{\delta I(t)}$, we choose to calculate the functional derivative with respect to the normalized derivative of $I_0(t)$, $1/I_0 dI_0(t)/dt$, that we denote by $g_I(t)$. We choose to use the derivative, because it is more convenient numerically and also lead to a dimensionless functional derivative. At first order, one can therefore write that:

$$
\delta \Phi = \int_{-\infty}^{\infty} g_I(t) \frac{1}{I_0} \frac{\mathrm{d}I_0}{\mathrm{d}t} dt \ . \tag{27}
$$

In the following, q_I is referred as the sensitivity function to the relative derivative of intensity.

Numerically, $g_I(t)$ is computed by looking to the variation of the phase Φ_{Bloch} for a small change of the intensity $I_0(t')$ for $t' > t$ (Heaviside function). The temporal evolution of the function g_I during the sequence described previously on Fig. [10](#page-8-0) is reported on Fig. [13](#page-10-0).

The inset is a zoom of g_I at the beginning of the sequence. In the inset, the contributions to g_I of each arm $(g_I^A \text{ and } g_I^B)$ are plotted. In the experiment, atoms that are in excited band experience on average, the mean potential of the lattice, $U_0/2$, whereas atoms in the first band, are in dark region (blue detuned lattice) and less subjected to light shift.

The phases in the inset of Fig. [13](#page-10-0) are calculated with eq. [6](#page-3-0) in which the common light shift $U_0(t)/2$ is left out. This changes the values of g_I^A and g_I^B but not the value of g_I . Within this energy reference, an atom moving fast with respect to the lattice does not see a phase shift $(\langle \cos(2k\hat{x}) \rangle =$ 0) whereas an atom trapped into the lattice sees a phase shift $(\langle \cos(2k\hat{x})\rangle \approx -1)$. Therefore the main contribution to the phase shift originates from the lower band. Consequently, it explains why the initial increase of g_I principally arises from the first band.

Fig. 13. Sensitivity function of the interferometer to the relative derivative of intensity. The temporal sequence is described Fig. [10](#page-8-0). Inset: zoom on the two first LMT pulses. The contribution from the two arms of the interferometer are displayed separately. A constant phase shift corresponding to the average light shift of an atom in the lattice is subtracted from both curves.

This phase shift is almost compensated by the other arm during the second LMT pulse. Indeed, the first two LMT pulses do not act in a symmetric way between the two arms because non-accelerated atoms are not in the same excited band during the first and second LMT pulses. During the first LMT pulse, non-accelerated atoms endure a small light shift (see the variation of g_I^B , around $t=0.6$ ms in the inset of Fig. 13, arrow labeled a). While during the second LMT pulse, non-accelerated atoms are moving too fast with respect to the lattice to see a light shift (see the plot of g_I^A which remains constant during the second LMT, at t around 1.2 ms, arrow labeled b).

In the case of the interferometer with only four LMT pulses (see Fig. [9\)](#page-6-0), the initial phase due to the first LMT pulse is compensated only at the end of the interferometer, after about 10 ms, whereas in our scheme, 90% of this phase shift is compensate after 1 ms. The sensitivity of our interferometer to a linear variation of the phase $\int g_I(t) dt$) is then reduced by a factor of 10 compared to an interferometer with four LMT pulses.

From the sensitivity function q_I , the reduction of the contrast due to the motion of atoms during the interferometer can be precisely calculated. For that, the phase shift accumulated along a trajectory must be calculated. At first order, it is expressed as

$$
\phi = \int g_I \frac{1}{I_0} \frac{\mathrm{d}I_0}{\mathrm{d}t} \mathrm{d}t \approx \left(\int g_I \mathrm{d}t \right) \frac{1}{I_0} \left. \frac{\mathrm{d}I_0}{\mathrm{d}t} \right|_{t=0} \tag{28}
$$

The contrast C is given by $C = e^{-\Delta \phi^2/2}$ where $\Delta \phi$ is the variance of the phase ϕ . $\Delta\phi$ is given by:

$$
\Delta \phi = \sigma_{\dot{I}} \left| \int g_I \mathrm{d}t \right|, \tag{29}
$$

where σ_i , which represents the relative variance of $\frac{dI_0}{dt}$ over the entire atomic cloud, is calculated with

$$
\sigma_{\dot{I}} = \frac{1}{I_0} \sqrt{\left\langle \left(\frac{\mathrm{d}I_0}{\mathrm{d}t}\right)^2 \right\rangle}. \tag{30}
$$

To evaluate σ_I numerically, Gaussian distributions are used to described the position and the velocity of the atoms. Then $\sigma_{\dot{I}}$ can be expressed as:

$$
\sigma_{\dot{I}} = 4\sqrt{2}\sigma_v \frac{\sigma}{w_L^2} \frac{1}{1 + 8\frac{\sigma^2}{w_L^2}}.\tag{31}
$$

in which σ denotes the RMS value of the position of the atoms in one direction and σ_v the RMS value of their velocity, w_L represents the waist of the Gaussian laser beam. With ours experimental parameters $(w_L = 2 \text{ mm},$ $\sigma = 600 \mu \text{m}, \sigma_v = 2v_r$, the value of σ_i is around 5.9 s⁻¹.

For the eight LMT pulses scheme used in our experiment, we have calculated that: $\int g_I dt \approx 48 \times 10^{-3}$ rad · s. Therefore, the values of $\Delta\phi$ and C are : $\Delta\phi = 0.28$ rad and $C = 96\%.$

With the four pulses scheme, those values become $\Delta \phi =$ 2.8 rad and $C = 2\%$. This clearly shows that in our experiment, the eight LMT pulses scheme must be used to observe interferences.

We emphasize that there is a correlation between the velocity and the position of atoms because of the small time of flight before the beginning of the interferometer. This results in a biased intensity variation leading to a systematic effect in the interferometer. This effect can be canceled by inverting the order of the two LMT pulses for each beamsplitter because the sign of q_I and consequently the one of ϕ is reversed.

5 Improving LMT beamsplitter

5.1 Current limitations

The contrast of the fringes observed Fig. [11](#page-8-0) is ten times smaller than the one without LMT pulses. This weak contrast can not be explain with light shifts. In the experiment, light shift is under control when the LMT pulses are used on both arms of the interferometer. Other sources contribute to this reduction. The main one arises from inhomogeneities in the initial momentum distribution of atoms and intensity of the laser. The maximum efficiency computed has been obtained for an atom with a defined velocity and a given laser intensity. But in our set-up, the initial velocity distribution is spread over about $0.5 v_r$, consequently the effective efficiency for a LMT pulse is reduced from 98% to 95%. Moreover, because of the initial size of the cloud and the finite waist of the laser, the variations of the intensity seen by atoms are in the order of 20%. As it can be easily see on Fig. [2](#page-4-0), this effect pushes away the efficiency from the optimal configuration by few percents. The contribution of spontaneous emission of atoms trapped in the lattice is also non negligible. In our regular experiments with Bloch oscillations[[18\]](#page-12-0), atoms, located at the bottom of the lattice wells, are oscillating in the first band. As the potential of the lattice is blue detuned, the spontaneous emission is reduced, because the light intensity is minimal at the position of atoms[[18\]](#page-12-0). Unfortunately, this demonstration does not apply to atoms in the excited bands. The estimated spontaneous emission rates of those atoms is around 4%.

All these effects added together reduce significantly the efficiency of each of the 8 LMT beamsplitter used in the interferometer and explain the reduction of contrast that we have observed. However, using a laser beam with a larger waist, a higher intensity (and a larger detuning) should allow us to reduce significantly these effects.

5.2 Sequence of a 10 recoil beamsplitter

As mention previously, it is not possible to realize a larger momentum separation while keeping a good efficiency with the scheme of the LMT, in which constant acceleration is used (c.f. Fig [3\)](#page-4-0).

To overcome this limitation, a process with different acceleration steps can be foreseen. The first step is identical to the one described earlier, with two Bloch oscillations. For the second one, the depth of the lattice is raised to enable a larger acceleration.

As explained previously, a long time and a relatively weak lattice are necessary to realize the first splitting with a good efficiency. For a given time, the optimal value of the amplitude of the lattice is a compromise between good adiabaticity of Bloch oscillations in the first band and a high Landau-Zener tunneling for the third band $(n = 3)$. However, this condition is less restricting when atoms are in a higher band $(n > 3)$. For those atoms, the Landau-Zener tunneling is higher so one can expect a better efficiency with the same duration or the same efficiency with a shorter duration. That is, a larger acceleration can be use to increase separation with a good efficiency.

The realization of a beam splitter with ten oscillations is presented on Fig. 14. The initial separation with two BOs is achieved in 130 μ s while the second separation with eight BO is done in only 160 μ s. The maximal efficiency is calculated to be about 98%. This is very close to the efficiency with two BOs beamsplitter. The main losses arise from the initial splitting of two recoils. The additional losses come from the lack of adiabaticity during the change of the lattice intensity. As Bloch oscillations is a very efficient process, no significant losses arises from the additional recoils transferred after the first two oscillations. The main limitations will come from the reduction of contrast due to intensity fluctuations.

To estimate this limitation, the sensitivity function q_I , with ten BOs, is plotted on Fig. 15. It is significantly larger

Fig. 14. Scheme of a beamsplitter with 10 oscillations.

Fig. 15. Sensitivity function q_I of the interferometer using a 10 Bloch oscillations LMT pulse, as described in Fig. 14.

than the one with two BOs because of the increase of the depth of the lattice. The sensitivity to a linear variation of intensity $\int g_I dt$ is about 95×10^{-3} rad · s. That is twice as much as the one for the interferometer with two BO (see section [3.1\)](#page-5-0). This is the reason why the improved LMT was not implemented yet on our current apparatus (the visibility of fringes for the "two BOs scheme" is already quite weak).

6 Conclusion

In this paper, we have theoretically and experimentally studied the implementation of a large momentum beamsplitter in a Ramsey-Bordé interferometer. We have realized a separation of 10 recoils between the two arms of the interferometer. By reducing the contrast of the fringes, light shift is the main limitation of this interferometer. Nevertheless, we have developed a method to reduce this effect by a factor of ten and so realize an interferometer with a separation of ten recoils between the two arms. Our model is in very good agreement with the experiment, in which a gain of four in the resolution, compared to a usual interferometer, was observed. This method seems to be very promising for the realization of an interferometer with a separation of several tens of recoil velocities.

The limitation due to light shift has been strongly reduced by accelerating successively both arms of the interferometer. Moreover a way to systematically cancel it would be to accelerate both arms of the interferometer simultaneously (instead of doing it successively). This can be done by applying two counter-propagating accelerated lattices. This scheme is already used by the Stanford/Berkeley¹⁶. N. Ashcroft, N. Mermin, Solid State Physics (Brooks/Cole, group [9]. In their experiment, a high order Bragg beamsplitter is initially used, before the double BO acceleration. We are also currently investigating this possibility of using the double BO acceleration but with an initial velocity separation given by a two photon Raman pulse. It seems that only two recoils is two small to perform a good separation and a higher initial separation may be required. A relevant method could be to use the double-diffraction technique described in Ref. [10] which allow an initial separation of 4 recoils. In this scheme, light shift would be completely suppressed. One of the remaining source of noise will be then the phase/vibration noise. This noise can be calculated with a numerical model identical to the one used in this paper.

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