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**ENERGY CRITERION FOR MODELLING DAMAGE EVOLUTION IN CROSS-PLY
COMPOSITE LAMINATES**

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Abstract

The energy dissipated in cross-ply laminates during loading-unloading loops is obtained from stress-strain curves for cross-ply laminates and used in an energy based approach to predict the development of matrix cracking. The dissipated energy is correlated to the crack density growth data recorded for a reference laminate. The critical strain energy release rate, G_c obtained in this way is increasing with the applied strain. This phenomenon reflects the statistical nature of G_c distribution in the 90-layer: the first cracks (lower strain) develop in positions with lower fracture toughness. The obtained G_c data are in a good agreement with fracture toughness data obtained using LEFM based “compliance calibration” model in which the stiffness change with increasing strain is used. Finally the matrix cracking development is successfully simulated using in the LEFM model, the data for critical strain energy release rate and an earlier derived stiffness-crack density relationship. It has been demonstrated that knowing the laminates geometry and measuring the laminate stiffness reduction with strain or (alternatively measuring the dissipated energy) the damage evolution may be simulated, thus reducing the necessity for optical observations to validation only.

Keywords: A. Polymer-matrix composites (PMCs); B. Matrix cracking; C. Damage mechanics; C. Fracture mechanics ; D. Raman spectroscopy

Introduction

Damage Mechanics is the field intensively developing during the last decades and providing tools for studies of composite materials behaviour after damage initiation. For the damage initiation prediction appropriate strength based criteria could be used. Designing structural elements for functionality in the presence of damage, the above sequence has to be accounted for when structure's durability is assessed. Damage in laminated composite materials develops in three subsequent and mostly interlaced forms: matrix cracking (intralaminar damage), delaminations (interlaminar damage) and fibres failure (laminates collapse). The interfaces between the aforementioned damage modes are not well defined, that is matrix cracking may be accompanied with local delaminations and/or fibres breakage. However, intralaminar, or as it is often called, transverse matrix cracking in plies oriented at angles different than the loading axes is considered to appear first. Therefore, during the last thirty years it has been the main subject of studies for many researchers [1-5]. The crack density and damage entity characteristics in terms of damage vectors and tensors, crack opening displacements etc were used to quantify the effect of damage on the overall behaviour of laminates [1-7].

Modelling the initiation and development of matrix cracking in a composite system starts with the evaluation of the stresses distributions within the laminate. In the reviews [1-5] all the main different approaches for the stress distribution determination could be found. Since the internal stress state is quantified the intralaminar cracking evolution could be modelled. The models proposed may be categorized, according to their basic approaches, into two main groups: strength based models and fracture mechanics based models; see

review [4]. Most of the stress based models account for the strength distribution within the laminate and the probability of local failure.

Among physical quantities, used to characterize micro damage development in laminates due to thermo-mechanical loading, the most often used is the critical strain energy release rate (often erroneously called fracture toughness). It is commonly considered as a material constant; however, an appropriate test for its determination is still an open question. In static crack growth problems, the critical strain energy release rate for the crack growth is either appropriately chosen in order to satisfy experimental damage evolution data [3, 14], or derived from cracking data and G using the stress state provided analytically [15-20] or numerically (finite elements) [21]. The attempts to use measured laminate Young's modulus changes or the measured dissipated energy are more rarely described in the literature.

The strain energy release rate, G , is usually calculated analyzing the stress state change with increasing crack density or using the change in the calculated elastic modulus of the laminate. Together with independently obtained G_c it is used to model damage evolution in composite laminates under both static and fatigue loading. Monitoring crack growth under fatigue has been presented by several researchers [9-13], while detailed review can be found in [4]. The G_c is used in the Paris power law criterion for individual crack growth during cyclic loading [27]. As a crack initiation criterion for composite laminates under static flexure loading, G_c has been used by Smith and Ogin [22-23]. One example of an approach which incorporates probabilities in the fracture mechanics analysis is the early analytical model proposed by Laws and Dvorak [8]. Statistical G_c distribution was extensively used by Wang et al; see for example [27].

In the present paper the critical strain energy release rate for two glass fibre reinforced epoxy composite systems is derived using the dissipated energy obtained from stress - strain curves recorded during an ordinary loading-unloading tensile test with increasing maximum and

using the observed crack density relationship with the applied strain for a reference laminate. As an alternative method for G_c determination the stiffness reduction with strain is used. The obtained G_c values strongly depend on the maximum strain level in the loading loop which reflects the statistical nature of the fracture toughness distribution along the 90-ply: the G_c values for lower strains correspond to cracks in the weakest locations whereas the new cracks appearing at higher strains require more energy. Finally, theoretical predictions of the crack density as a function of applied strain are performed using the obtained G_c and an analytical model describing the longitudinal modulus degradation as a function of crack density [26].

Experimental

Two cross-ply glass fibres reinforced composite systems (GFRP) were used for the dissipated energy calculations. The first (GF1) was manufactured using a modified frame-winding technique. Detailed description of the procedure can be found in the literature [6-7]. A steel frame welded at 90° was used for the glass fibres winding with the inner layer wound firstly. Then, the 0° layer was wound. Tensile coupons were cut from the laminates according to ASTM D3039 standard. A Shell “Epicote” 828 resin was used and cured with nadic methyl-anhydride and accelerator K61B in the ratio 100:60:4. The laminate was cured between thick glass plates under 8-10 bar pressure for 3h at 100 °C, followed by a post-cure at 150 °C for 3h. The fibre volume fraction of the thus produced plates was 63 %, the laminate ply thickness was 0.64-mm for the 0° plies and 0.62-mm for the 90° plies.

In the case of the second composite system (GF2) three different laminates with different ply thicknesses were considered. They were manufactured using a vacuum bag technique from unidirectional prepreps with the commercial code VICOTEX NVE 913/28%/192/EC9756. The laminates were cured at 90 °C for 30 min followed by post curing at 120 °C for 60 min under 3-7 bar pressure. Three laminates stacking sequences were

manufactured, $[0/90_4]_s$ (GF2_1-4), $[0/90_2]_s$ (GF2_1-2) and $[0_2/90_2]_s$, (GF2_2-2) with an average thickness of 1.35, 0.80 and 1.04 mm, respectively. Specimens were cut according to the ASTM D3039 standard in the reinforcement direction of the outer layers. Specimen edges were polished in order to eliminate any defects that may appear during sawing. It has been proved [24] that edge polishing is the cause for rapid crack propagation, thus the development of cracks covering the full specimen width is expected. Details on the GF2 material manufacturing can be found in [25].

GF1 laminates were subjected to a repeated mechanical tensile testing for the crack pattern development. The mechanical tensile loading was applied through an MTS 858 Mini Bionix tester [6]. The loading rate was 0.1 mm/min to achieve controlled and stable crack growth. An electrical strain gauge has been attached on the specimen in order to control the resulting strain. The specimen was loaded up to a certain strain level and unloaded to zero stress level. Then the procedure was repeated for higher strain levels until reaching the so called crack saturation point. The stress-strain curves thus produced are presented in Fig. 2a. Crack density at each strain level, see the transverse crack appearance in Fig 1, was monitored using the technique of laser Raman spectroscopy [6-7]. The initial Young's modulus of the laminate was calculated from the first stress-strain curve provided by the attached strain gauge and the MTS load cell.

GF2 material laminates were tested under quasi-static stepwise tensile loading with an applied displacement rate of 2mm/min [25]. Loading was periodically interrupted and the specimens were unloaded for measuring the crack density. Crack density was monitored by optical means in transmitted light, which was possible due to the partial transparency of the materials [25]. The applied strain in the loading direction was measured by an extensometer. The Young's modulus at each loading step was derived from the corresponding unloading stress-strain curve within the 0.1% to 0.3% axial strain range [25].

The two different composite systems subjected to rather different strain rates were used to demonstrate that the suggested methodology is applicable in wide range of materials behaviour. The strain rate for all laminates belonging to same material system was kept constant. Thus the possible effects of more brittle material behaviour at high strain rates and the creep rupture type of effects at low strain rate are included in corresponding values of G_c . Due to these possible additional effects no comparison of both materials is made.

Modelling

In a displacement controlled test the critical strain energy release rate, G_c , is defined by the well known equation

$$-\left. \frac{\partial U}{\partial A} \right|_{\varepsilon = \text{constant}} = G_c(\varepsilon) \quad (1)$$

where U is the strain energy of the specimen, while A is the total crack surface area formed by all cracks, that is

$$A = N w h_{90} \quad (2)$$

where N is the number of cracks formed, w is the specimen width and h_{90} is the 90°-layer thickness. The strain energy of the specimen (ignoring thermal stresses which are not large in a glass fibre composite laminates) can be written as

$$U = \frac{E_x}{2} \varepsilon^2 V \quad (3)$$

E_x is the damaged laminate longitudinal Young's modulus, ε is the applied strain and V is the specimen volume

$$V = L w h \quad (4)$$

L is the specimen length and h its thickness.

Substituting eqs (2)-(4) into eq (1) the following expression for G_c can be extracted

$$-\frac{1}{2} \varepsilon^2 L \frac{h}{h_{90}} \frac{\partial E_x}{\partial N} = G_c(\varepsilon) \quad (5)$$

Crack density, ρ , is defined as the ratio of the total number of cracks within a length over the length. Thus for the specimen with length, L , it is

$$\rho = \frac{N}{L} \quad (6)$$

Combining eqs (5) and (6) G_c is expressed as a function of crack density

$$-\frac{1}{2} \varepsilon^2 \frac{h}{h_{90}} \frac{\partial E_x}{\partial \rho} = G_c(\varepsilon) \quad (7)$$

It has been shown [26] that the dependence of laminate longitudinal Young's modulus, E_x , on crack density in the damaged cross-ply laminate is of the form

$$E_x = \frac{E_0}{1 + A_0 \rho u(\rho)} \quad (8)$$

where E_0 is undamaged laminate longitudinal Young's modulus, A_0 is a constant which value depends on the model used (ex. shear lag) and $u(\rho)$ is average crack opening displacement normalized with respect to the far-field stress in the 90-layer. We assume, for the sake of simplicity, that the normalized crack opening does not depend on the distance between cracks

$$u(\rho) = u_0 \quad (9)$$

where the value of u_0 can be calculated by any existing stress model. Actually u is not a constant and it decreases at high crack density when the interaction between cracks is noticeable. In this paper the model proposed by Lundmark and Varna [26] is used.

Differentiating eq (8) and taking into account eq (9) the partial derivative of the E_x with respect to ρ is calculated. Then eq (7) becomes

$$\frac{1}{2} \varepsilon^2 \frac{h}{h_{90}} \frac{E_0}{(1 + A_0 \rho u_0)^2} A_0 u_0 = G_c(\varepsilon) \quad (10)$$

which can be rewritten using eq (8) as

$$\frac{1}{2} \varepsilon^2 \frac{h}{h_{90}} E_x^2 \frac{A_0 u_0}{E_0} = G_c(\varepsilon) \quad (11)$$

The constant A_0 as calculated from [26] is given by

$$A_0 = \frac{E_T}{E_0} \frac{2 h_{90}}{h_{90} + 2 h_0} h_{90} \quad (12)$$

According to the studies performed by Lundmark and Varna [26] the crack opening displacement in an internal layer can be represented by the following power law

$$u_0 = A_m + B_m \left(\frac{E_T}{E_L} \right)^{n_m} \quad (13)$$

where the constants A_m , B_m and n_m are given by following empirical forms

$$\begin{aligned} A_m &= 0.52 \\ B_m &= 0.3075 + 0.1652 \left(\frac{h_{90} - 2 h_0}{2 h_0} \right) \\ n_m &= 0.030667 \left(\frac{h_{90}}{2 h_0} \right)^2 - 0.0626 \left(\frac{h_{90}}{2 h_0} \right) + 0.7037 \end{aligned} \quad (14)$$

Results - Discussion

A “stop-and-go” procedure was employed in the crack forming experimental investigation on both composite systems. The specimen was loaded up to a certain strain level where new cracks formed, while the applied strain was controlled by the strain gauge attached on one side of the specimen (GF1) or the extensometer along the loading direction (GF2).

Following, they were unloaded to zero stress, while the residual strain was recorded and the crack pattern was monitored. In the case of GF1 laminate the crack pattern was mapped indirectly through the use of laser Raman spectroscopy for measuring the strain arising within the 0° lamina due to cracking. Details on this method have been referred in previously published works [6-7]. The crack pattern arising in the GF2 laminates at all strain levels and for all types of specimens used was monitored using an optical microscope. This procedure

was repeated until the crack forming mode of damage was completed by reaching the so-called saturation point. The stress-strain curves are presented in Figure 2a-d.

The first step in the experimental critical strain energy release rate determination is the calculation of the dissipated energy, U_d , at each loading-unloading cycle. By integrating the loading stress-strain curve the energy, U_l , given to the material is calculated, which includes both the strain energy and the additional work performed on additional displacements due to increase of the total crack area. The integration of the unloading curve corresponds to the energy returned, U_u . The difference between these two values represents the total dissipated energy, U_d , in each loading cycle

$$U_d = U_l - U_u \quad (15)$$

The dissipated energy differs from the mechanical strain energy U introduced in the previous section. It includes also viscoelastic effects as well as reduction of strain energy related to thermal stresses as a consequence of thermal stress relaxation due to cracking. The latter phenomenon results in small permanent tensile strains after each loading-unloading cycle. The additional work performed by the external load related to additional macro-scale displacements due to the cracks growth is also included.

The dissipated energy for both materials systems as a function of the maximum applied strain in the cycle is presented in Fig. 3. Each maximum applied strain corresponds to a unique crack density, ρ , value for each different material and lay-up. The procedure for its determination is described in Section “Experimental”. Alternatively, the measured stiffness reduction with strain and the theoretical model can be used to extract the corresponding crack density. Using these data and the data presented in Fig. 3 a diagram of the dissipated energy as a function of ρ for all experiments can be constructed. U_d versus transverse crack density is presented in Fig. 4.

Experimental G_c value is given by the total derivative of the dissipated energy, U_d ,

with respect to the total crack surface formed, A

$$G_c = \frac{dU_d}{dA} \quad (17)$$

Polynomial fitting of the experimental data in Fig. 4 has been used in order to determine the G_c according to eq. 17 for each different crack density value. The crack density, ρ , is related to A with expression (2) where N is the number of cracks formed that is related to ρ by (6).

Using equations (2), (6) and (17) the following expression, relating G_c with ρ through the actual 90°-layer volume, V_{90} , is constructed

$$G_c = \frac{1}{V_{90}} \frac{dU_d}{d\rho} \quad (18)$$

The critical strain energy release rate G_c as a function of ρ is presented in Fig. 5. Data presented in Fig. 5 possibly indicate that due to unstable growth more energy was released than the actual required creating cracks in the GF2_1-4 material. The difference becomes much smaller for the other two lay-ups with the same of-axis layer thickness. Inverting the previous strain-crack density procedure, i.e. going from cycle maximum applied strain to crack density, the relationship between G_c and the applied strain is extracted. The results are presented in Fig. 6. All the experimental data resulting from the three different GF2 laminates are plotted to show that the results could be considered laminate lay-up insensitive, while the dependence is different for GF1 and GF2 composites. In other words, G_c is a material characteristic and does not vary with ply thickness.

As an alternative approach we use the measured stiffness degradation with strain and eq (11) to calculate G_c corresponding to the given strain level (more exactly for cracks developing at this strain level). In derivation of (11) the results of previous works [7, 26] on stiffness degradation with increasing crack density have been used. The model proposed by Lundmark and Varna [26] has been proved to provide a very accurate description of the

longitudinal Young's modulus relationship to the crack density. The G_c was calculated by eq (11) for every pair of points (ε , E_x). The necessary pair of points can be easily found experimentally, from the corresponding stress-strain curves using the unloading curve as described. The results are presented in Fig. 7. An average linear fitting is used for all results from the three different GF2 laminates since G_c is considered as a fracture characteristic of a material not depending on geometrical characteristics. The rather linear behaviour of G_c with applied strain, which was observed in the dissipated energy calculations, see Fig. 6, is also presented here for the two different materials examined. The numerical values obtained using these two different techniques are rather close. Linear fit to these data was used as the first approximation in the following modelling. Certainly, more refined (bi-linear or S-shape) approximation would account for more details and would improve the predictions. However the accuracy of the fitting has to be comparable with experimental differences between curves and the fact that G_c is considered as independent of the laminates lay-up.

G_c for the GF2_1-4 material calculated using the dissipated energy is used in order to develop an analytical method for simulation of the crack density corresponding to any applied strain level. Eq (10) provides the requested relationship and, thus, it was used to derive theoretically the crack density as a function of the applied strain for all materials under consideration. The results are presented in Fig. 8 in comparison to experimentally derived crack density versus maximum applied strain data for both materials systems under investigation. Since new damage modes (blunted cracks, delta cracks, curved cracks, local delaminations etc) start to be dominant at strains higher than the so called "saturation state", the described model for straight intralaminar cracks can not be used anymore. In order to extend the approach to this region these damage modes have to be classified, quantified and their effect on stiffness has to be modelled.

The experimental data, from the three different laminates manufactured using the GF2

material, are considered separately. The theoretical predictions appear to be in good agreement with the experimental data in the case of GF1 material. Considering the GF2 system three different predictions, with respect to the three different initial Young's moduli of the laminates are presented. The variation between the three different curves is not considerable, and all three are in agreement with the experimental data. Hence, in the crack density development the critical strain energy release rate can be treated as a material property to be calculated using macroscopically constructed stress-strain curves.

Conclusions

Critical strain energy release rate has been used as a mean for the analytical prediction of the crack density arising in cross-ply composite laminates as a consequence of the external applied strain level. Two different GFRP material systems (GF1 and GF2) were used. GF2 system was used in three different stacking sequences with varying layer thickness ratio. The energy dissipated during all loading-unloading cycles was calculated using the recorded stress-strain curves. Together with experimental crack density evolution data for a reference laminate it was used in order to derive the G_c as a function of a modified crack density. This dependence represents the statistical nature of the composite fracture toughness, G_c , distribution (first cracks are in positions with lower fracture toughness). Using the reference lay-up crack density data the G_c was recalculated versus the corresponding tensile applied strain. A linear relationship between G_c and the maximum applied strain level was observed for both materials systems. This experimental relationship was used for theoretical prediction of the crack density evolution with the applied strain in other laminates of the same material. An analytical model was used which requires only the material thermomechanical properties and the stiffness degradation law as a function of increasing crack density provided any appropriate model. The theoretical calculations of the crack density as a function of the

applied strain were compared to experimental data and a good agreement was found. It has been demonstrated that the energy dissipated during a loading –unloading cycle and the measured stiffness reduction can be used to determine G_c which can be treated as statistical material property and used in theoretical damage evolution models.

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Figure Captions

FIGURE 1. A typical crack pattern in cross-ply laminates

FIGURE 2. Typical stress-strain curves for the two materials examined, (a) GF1, (b) GF2_1-4, (c) GF2_1-2 and (d) GF2_2-2.

FIGURE 3. Dissipated Energy as a function of cycle maximum applied strain for all the materials tested

FIGURE 4. The Dissipated Energy plotted against the modified crack density corresponding to each applied strain level for both materials systems

FIGURE 5. Critical strain energy release rate as a function of the modified crack density

FIGURE 6. Critical strain energy release rate as a function of applied strain. The data of the three different GF2 laminates are fitted by an average linear fitting curve

FIGURE 7. Theoretical evaluation of the G_c as a function of maximum applied strain. GF2 data are considered as one data-set

FIGURE 8. Theoretical prediction of the crack density corresponding to applied strain level in comparison with experimentally derived data. The results are presented for both materials systems used

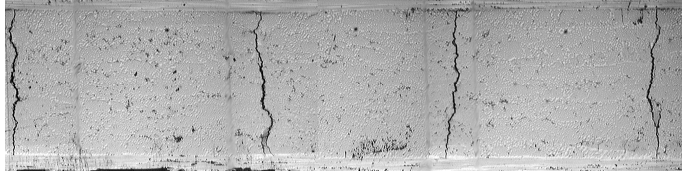


Figure 1

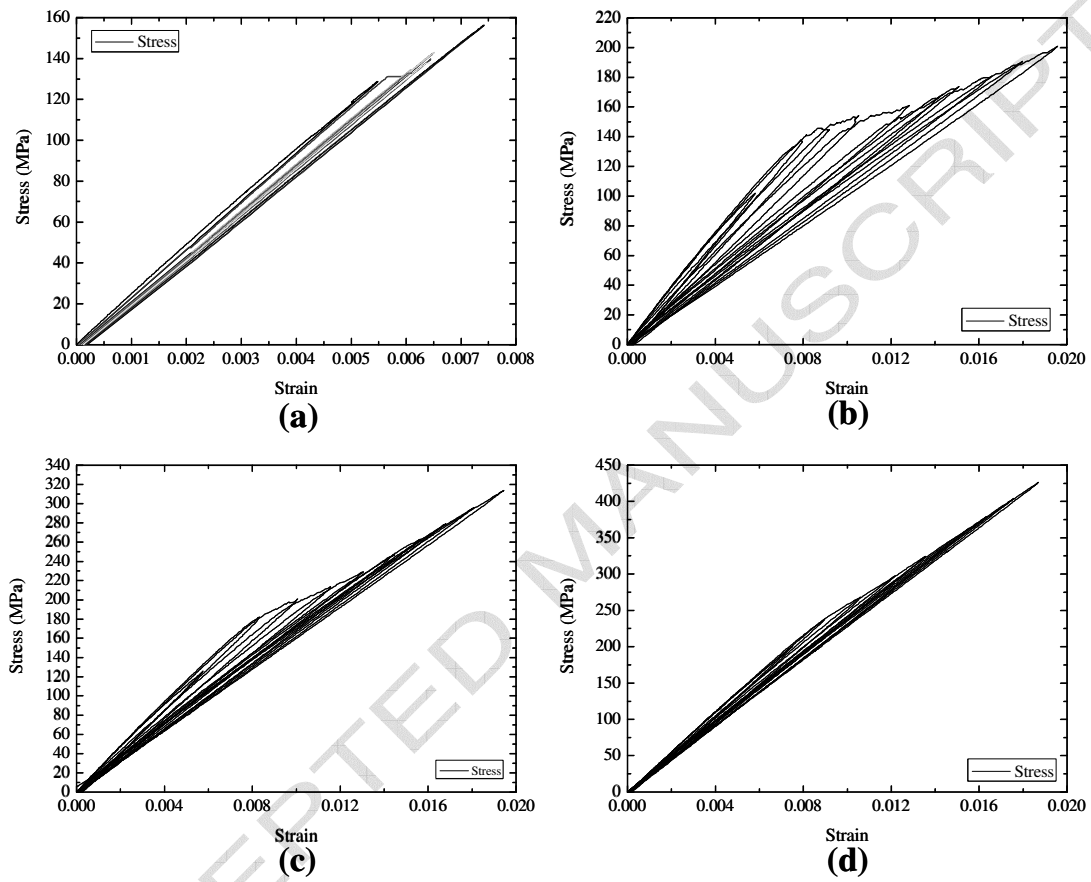


Figure 2

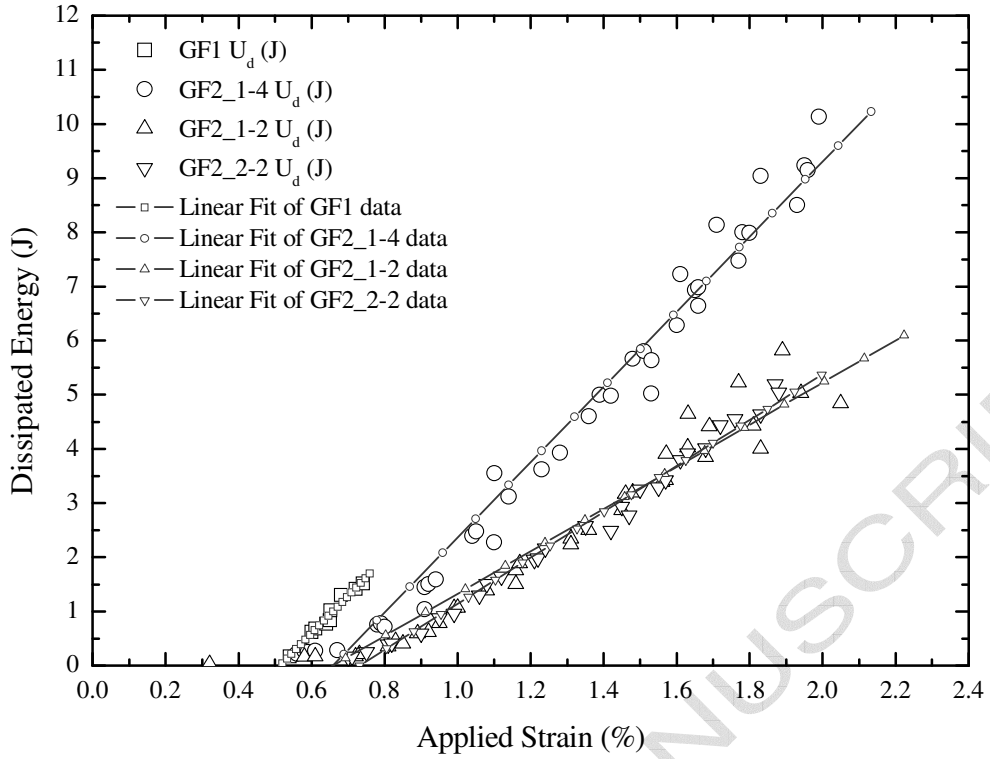


Figure 3

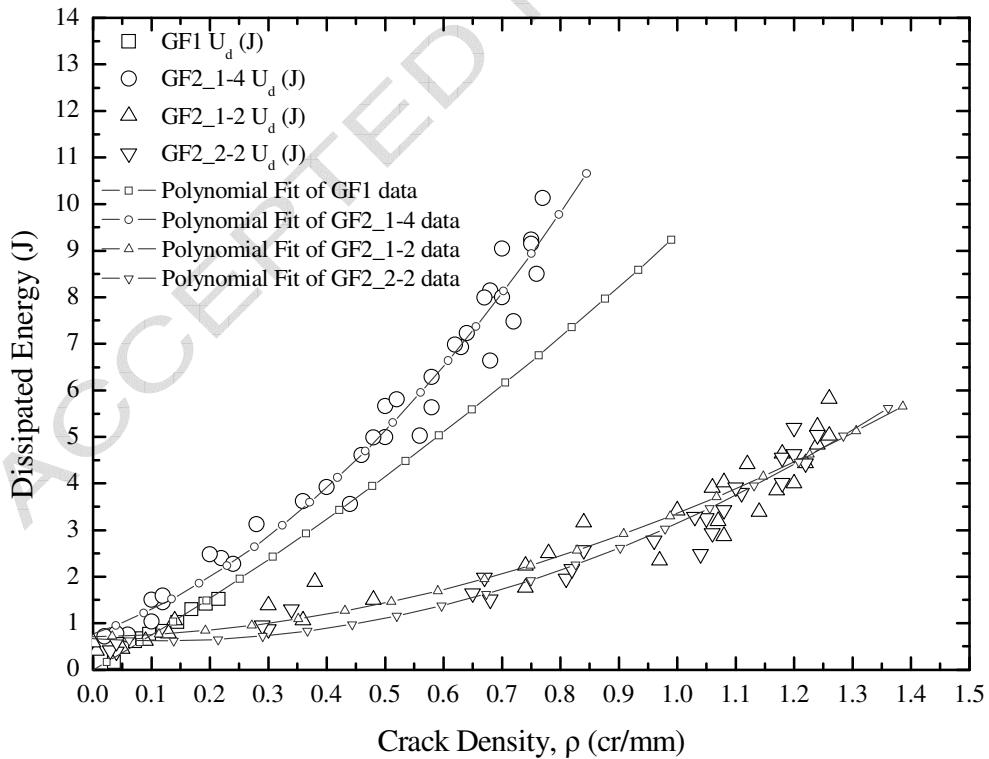


Figure 4

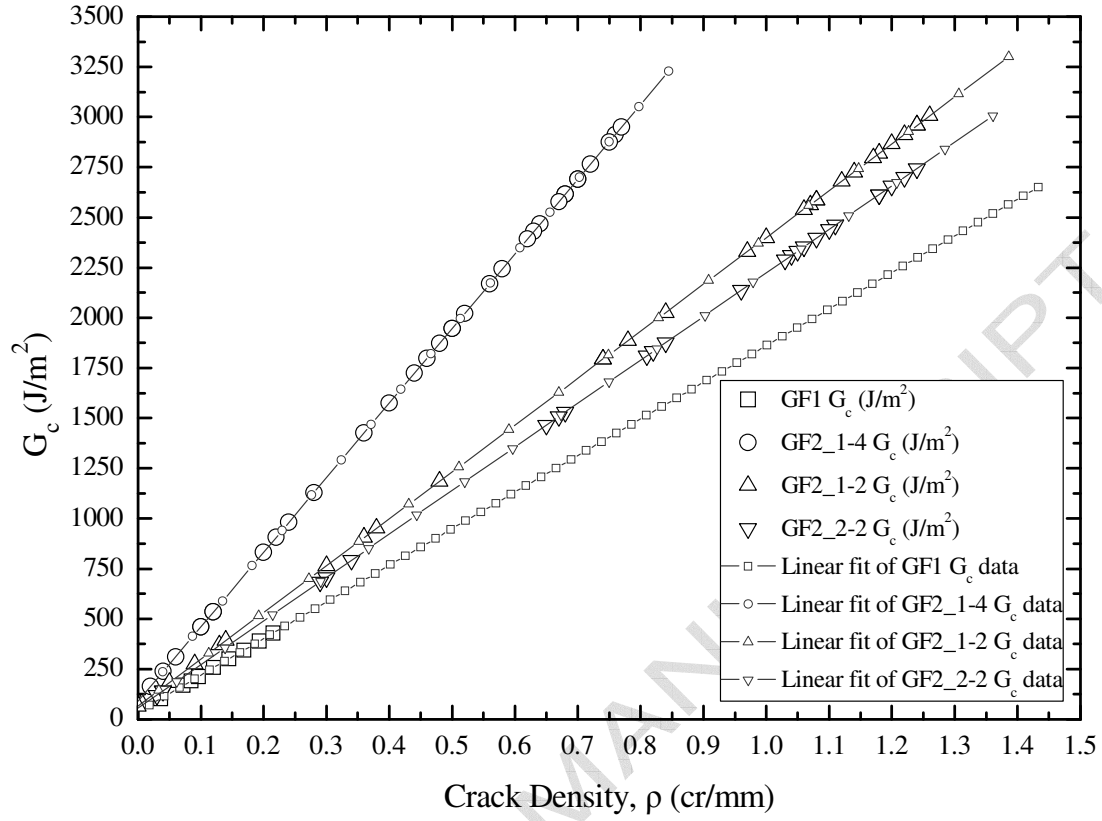


Figure 5

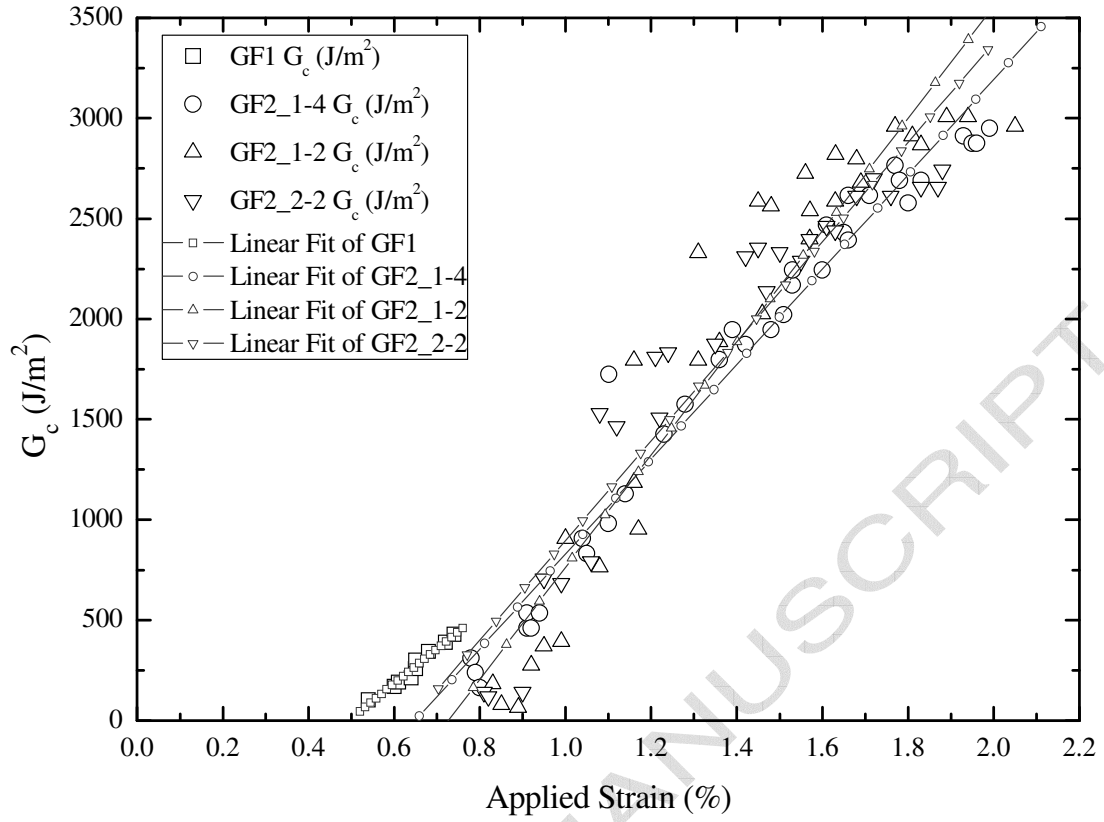


Figure 6

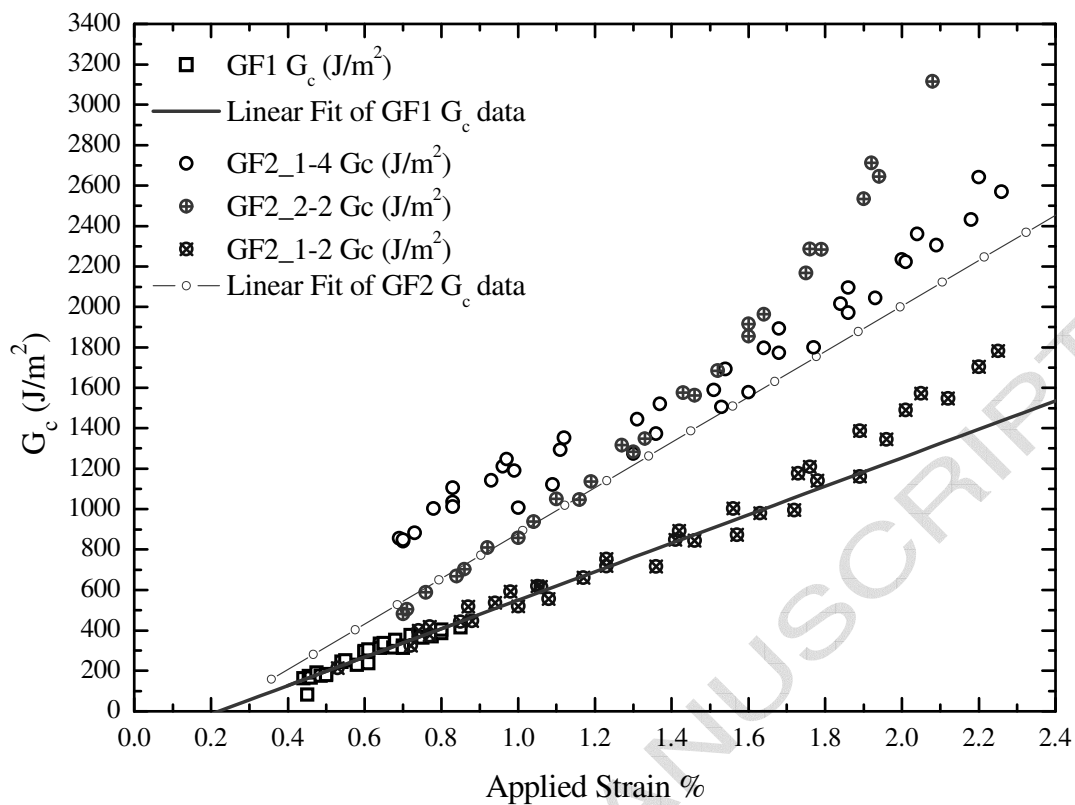


Figure 7

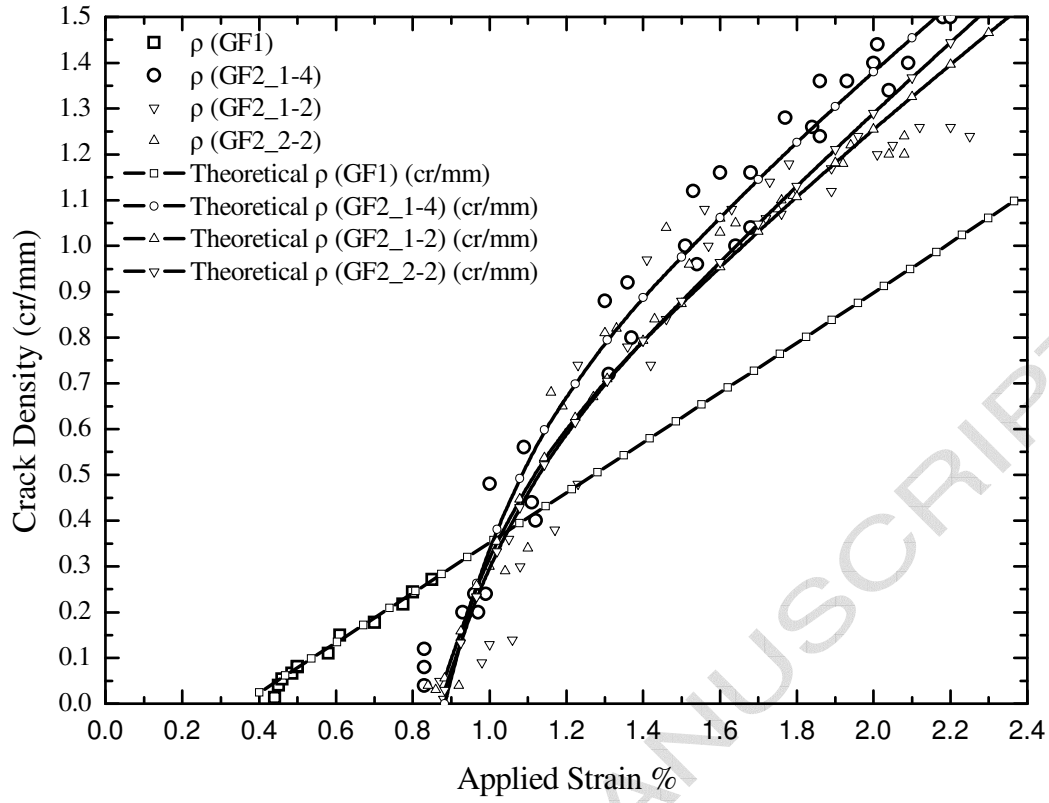


Figure 8