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# Efficient multipoles modeling for linear magnetized beads manipulations

P. Kauffmann<sup>1,2</sup>, V. Haguët<sup>2</sup>, G. Reyne<sup>1</sup>, B. Delinchant<sup>1</sup>

<sup>1</sup>Grenoble Electrical Engineering lab, BP 46, 38402 Saint-Martin d'Hères, France

<sup>2</sup>Biopuces, CEA, Grenoble, France

benoit.delinchant@g2elab.grenoble-inp.fr

**Abstract** — Many Magnetic MEMS have been recently developed to manipulate spherical diamagnetic or superparamagnetic particles. Magnetic forces can be computed using the dipole method or the semi-numerical integral. However, these methods appear inaccurate or time consuming, respectively. This paper proposes a multipolar approach which provides a satisfying compromise between precision and rapidity to compute the magnetic force on linear magnetized beads. Gain in precision and CPU time will be detailed for water droplets levitating above micromagnets.

**Index terms** — Magnetostatics, analytical modeling, multipoles approach.

## I. INTRODUCTION

Micro-magnets and micro-coils have been recently developed to handle particles either by attraction or repulsion according to the magnetic susceptibility of the particle. Such devices could be used *e.g.* for providing contamination free digital microfluidics, cells micro-positioning and sorting or capturing molecules in a biological sample.

Complex micro-scale dynamic simulations with high magnetic gradients due to micro-magnets and micro-coils require specific modeling tools. A fast and precise model to compute energy and forces on linear magnetized spherical particles is presented. Thus moderate CPU time provides a precise simulation of diamagnetic, paramagnetic and superparamagnetic particles in a low magnetic field. Diamagnetic levitation of water microdroplets in air is used to demonstrate the efficiency of the method (fig. 1).

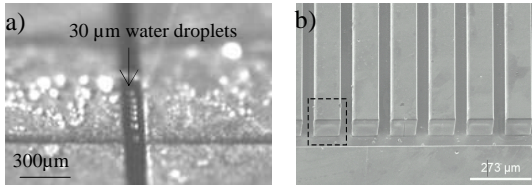


Fig. 1. a) 30 μm diamagnetic droplets levitating above a magnetic groove [1], b) 50 μm thick NdFeB micro-magnet deposit by sputtering.

## II. MULTIPOLAR MODELING TECHNIQUE

Magnetic force applied on a diamagnetic isotropic sphere depends on the susceptibility contrast  $\Delta\chi$  between the particle and its medium. This force is the integration of  $\nabla B^2$  over the sphere volume. It can also be computed through the integration of  $B^2$  over the sphere surface:

$$\vec{F} = \iiint_v \nabla U \cdot dv = \iint_s (U(s^+) - U(s^-)) \vec{n} ds \quad (1)$$

A magnetic multipoles model is presented. It is a transposition to magnetism of the multipoles approximation proposed by Jones for dielectrophoresis [2]. Eq. 2 details the 3 order multipolar development of the magnetic force:

$$F_i = 4\pi\mu_m R^3 \left( K^{(1)} \sum_{m=1}^3 H_m \frac{\partial H_i}{\partial x_m} + \frac{K^{(2)} R^2}{3} \sum_{n=1}^3 \sum_{m=1}^3 \frac{\partial H_n}{\partial x_m} \frac{\partial^2 H_i}{\partial x_m \partial x_n} + \frac{K^{(3)} R^4}{30} \sum_{o=1}^3 \sum_{n=1}^3 \sum_{m=1}^3 \frac{\partial^2 H_n}{\partial x_o \partial x_m} \frac{\partial^3 H_i}{\partial x_m \partial x_n \partial x_o} + \dots \right), \quad K^{(n)} = \frac{\mu_p - \mu_m}{n\mu_p + (n+1)\mu_m} \quad (2)$$

Successive derivatives of the magnetic field can be obtained by finite difference technique. However, it may supply noise during an optimization process where dimensions are varying. If analytical expressions of the magnetic field are available, symbolic differentiation can be used. Another solution consists in automatic code differentiation which will be presented in the full paper.

## III. VALIDITY RANGE OF MULTIPOLAR APPROXIMATION

Fig. 2 illustrates the validity range of the multipole method compared to the ratio between the radius of the droplet and the size of the magnetic groove (fig. 1).

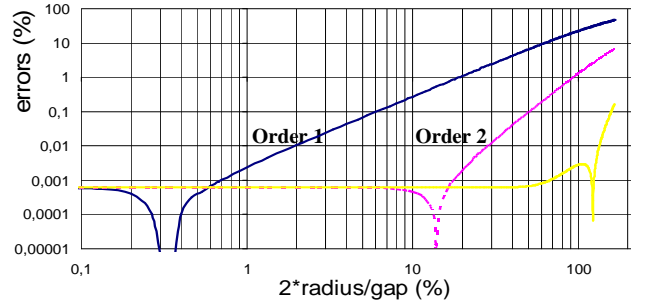


Fig. 2. Relative error due to the multipole approximation regarding droplet size relatively to the gap size between magnets.

From these results, constrained optimizations (detailed in the full paper) have been achieved very quickly for different specifications requirements. An optimization using our approach is in average about 250 times faster, keeping the same accuracy, than a numerical integration with the same gradient based algorithm.

## IV. REFERENCES

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