A level set approach for brittle damage

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In this paper, we present a model for damage evolution. It is well know that fracture mechanics alone, despite all the advances in numerical technics to represent cracks, can not represent easily the initiation process or the changes of topology in the crack shape, like branching or merging of cracks. To model properly such phenomena, damage mechanics models are more adapted. But damage model have their own weaknesses. Damage models are usually written locally for a given material, which cause well known spurious numerical localization and force the use of complex technics, be it averaging the local material law over a region or using second gradient model. Recently, new type of descriptions appeared, that we see as means to bridge the gap between damage and fracture mechanics. In Bourdin, Francfort and Marigo (1), brittle damage is regarded as a minimization problem on a crack field and the mechanical fields. The crack field represent the crack position by a continuous function over the full domain, whose value is 0 close to the crack and 1 far from it. The physics community (2) developed an other model, the so called "phase field approach". Here, the phase field, represent the damage and a global phase equation is coupled to the mechanical equations to describe the damage evolution. A level set technic was proposed by Salac (3), where a level set function is used to separate the fully damaged zone from the undamaged one. The damage front in this model advance, if a driven force reaches a critical value. The first two descriptions force to solve a global equations on the full computation domain, in the last approach, only a front velocity need to be computed and the level set advance can take advantage of narrow-band technics to improve efficiency. Inspired by Nguyen (4) and Salac model, we propose a new model that might improve the previous one. In our model, a level set is used to separate the undamaged zone from the damaged one. The iso-zero of the level set is the damage front that moves according to a Kuhn Tucker type relation, on each point of the front :

$$v_n \ge 0 \quad f = e - \left(Y_c + \frac{\gamma_c}{\rho}\right) \le 0 \quad fv_n = 0 \tag{1}$$

where v_n is the normal velocity of the damage front, *e* the free energy and ρ the radius of curvature of the front and *f* play the role of the driving force that moves the front. Y_c and γ_c are parameters of the model, and respectively represent a critical bulk energy and a critical surface energy. Note that, $\gamma_c/Y_c = l_c$ introduce a natural lenght scale in the model, lenght scale that should prevent spurious localisation and allow for size effect in the model.

The algorithm to compute new position of the front verifying the above Kuhn Tucker relation will be described and some results in the frame work of planar linear elasticity for the undamaged zone, including branching and merging of cracks will be discussed (figure 1).

References

^[1] The variational approach to fracture, B. Bourdin, G. Francfort, and J.-J. Marigo, Springer, 2007.

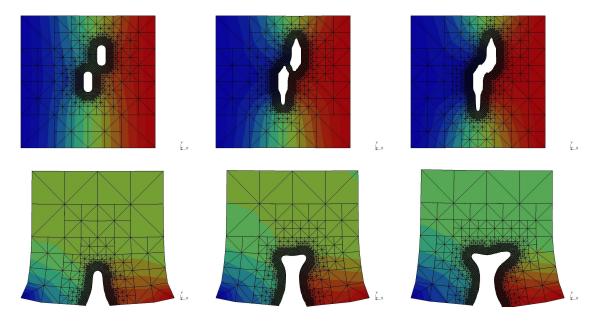


Figure 1: Top : Merging of two damaged zone, Bottom: Branching of a crack encountering a stiffer material.

- [2] *Phase-field model of mode III dynamic fracture*, A. Karma, D. Kessler, H. Levine, Physical Review Letters, 8704 (4), 2001.
- [3] A level set approach to model directed nanocrack patterns, D. Salac, W. Lu, Computational Materials Science, 39 (4), 849-856, 2007.
- [4] *Sur une loi de propagation régularisante en rupture et endommagement fragile*, Q. S. Nguyen, R.M. Pradeilles, C. Stolz, compte rendus de l'académie des sciences, 309, 1515-1520, 1989.