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Crack closure and stress intensity factor measurements in nodular graphite cast iron using 3D correlation of laboratory X-ray microtomography images

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Abstract : 3D tomographic images of a nodular graphite cast iron obtained using a laboratory X-ray source were used to analyze the opening of a fatigue crack during *in-situ* mechanical loading. Direct image analysis and digital image correlation are utilized to obtain the 3D morphology and front location of the crack as well as the displacement fields in the bulk of the specimen. From DIC results, it is possible to extract the Crack Opening Displacement (COD) map in the whole sample cross-section and to compute Stress Intensity Factors (SIF) all along the crack front even for COD values that are less than the image resolution. The comparison of COD maps with local values of SIF enabled for an estimation of the opening SIF, K_{op} , equal to $6 \text{ MPa}\sqrt{\text{m}}$.

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1 Introduction

Fatigue crack closure was first described by Elber [1] more than 30 years ago. Although it is a critical issue for life time predictions through Paris' laws (with the use of effective stress

intensity factor ranges, ΔK_{eff}), there is still no unified method of measurement that reaches general consensus. Crack closure occurs when the crack surfaces come into contact before the minimum load of the fatigue cycle is reached. The underlying mechanisms are diverse and may operate simultaneously; the reader is referred to ref. [2] for a more complete description. For example, a growing crack leaves behind a plastically deformed zone that is adjacent to the crack faces. This plastic wake induces early closure of the crack during unloading via a mechanism called Plasticity-Induced Crack Closure (PICC). Furthermore, asperities on the crack faces may also result in premature contact and induce Roughness-Induced Crack Closure (RICC). This mechanism becomes significant near the fatigue threshold when crack paths are highly crystallographic or under mode II or III loading that favours asperity contacts; in this case, closure concentrates in regions where the crack changed its direction of propagation [3]. Therefore, ideally, to measure crack closure and identify the operative closure mechanism, one needs a way to measure precisely the crack mouth displacements or contact along the crack front knowing the topography of the crack. Measurements at the surface of a sample during a loading/unloading cycle have been performed using for example scanning electron microscopy [4]. Surface measurements allow one to visualize crack shapes and to analyze closure changes with the crack length [5]. However the relevance of this kind of measurement with respect to the bulk of the sample can be questioned. Bulk measurements of crack closure involve indirect observations from crack growth, e.g. with potential drop or acoustic emission, and with mechanical compliance curves [6]. This last method is the most widely used. The loss of linearity of the displacement-load curve recorded during unloading of the specimen delimits the closure load. However, the result may depend on the positioning of the displacement gauge, namely, at the crack mouth, at the back face of the specimen, behind the crack tip within the specimen (push-rod gauge) or near the crack tip at the surface [6]. With these techniques, no information on the relationship between crack topography and closure can be obtained as the detailed crack shape is not available.

Three-dimensional visualisation of cracks in optically opaque materials such as metals is now possible using high resolution X-ray tomography [7-13]. So far, synchrotron X-rays have been used for this kind of studies as crack detection is enhanced by the high spatial coherence of X-ray beams available at modern (third generation) synchrotron facilities [14]. However, the use of synchrotron radiation puts a strong limit on the number of experiments that can be carried out *in situ*.

3D tomography images can be used, in principle, to evaluate the 3D displacement field at the crack tip in a specimen under load. In practice, this can be achieved using two different methods, namely Particle Tracking (PT) and Digital Image Correlation (DIC). Particle Tracking consists in measuring the displacements of microstructural features or markers inside the material. These markers are first identified by their gravity centre. Then, they are individually tracked between 3D images of the same specimen under different loads in order to compute the global displacement field inside the specimen. The DIC method is well established for computing displacements and strains on the surface of samples or structures [15-17]. It consists in measuring displacement fields between image pairs of the same specimen at different loads. The displacement field is obtained, using the so-called brightness conservation, so that the image of the loaded sample is matched to the reference image when pixel locations are corrected for by the measured displacement field. Recent developments have made possible the extension of this Galerkin technique to 3D displacement measurements in the bulk of specimens using 3D tomography images [18]. The uncertainty level of the latter is usually smaller than that of the former.

Both techniques have been applied to very different materials (Table 1). For example, the architecture in a trabecular bone [19] or in an open-cell aluminium foam [20] has been proved a valid texture for 3D DIC while microporosity in an aluminium alloy has been successfully used for particle tracking [21; 22]. The resolution of both techniques depends directly on the presence of numerous and finely dispersed microstructural features inside the material and those features should not break nor deform heavily upon loading. If the material

does not possess a natural texture that meets these requirements, artificial markers may be added. For example, tungsten particles were added to an aluminium matrix [23; 24] and microholes were laser-drilled in a dispersion-strengthened copper alloy [25] to allow for strain mapping in tensile testing for strain values ranging from 3 [23; 25] to 22% [25]. However, the influence of artificial markers on the matrix behaviour is difficult to assess. Increasing the number of artificial markers enhances the spatial resolution of strain mapping via tracking methods but it may also reinforce their potential perturbation effect. Whenever possible, the use of a material that possesses a natural texture suitable for DIC/PT is thus preferable.

Measurement of crack closure has been carried out by manual tracking of microstructural features using high resolution synchrotron radiation (0.7 μm voxel size). It drew interesting results on the relationship between the crack shape and local values of the stress intensity factor [21]. However, this technique has the disadvantage that crack tip displacements are not measured automatically.

This paper is a first attempt to evaluate crack closure in a widely used structural material, *i.e.* a nodular graphite cast iron where the graphite nodules act as natural markers to determine 3D displacements and stress intensity factors by correlating images obtained with standard *laboratory X-ray tomography* equipment.

2 Material and experimental methods

2.1 Material

The material of this study is a ferritic cast iron whose composition is 3.4 wt% C, 2.6 wt% Si, 0.05 wt% Mg, 0.19 wt% Mn, 0.005 wt% S, and 0.01 wt% P. After casting and heat treatment (ferritization at 880 °C followed by air cooling) the microstructure obtained is a ferritic matrix (98 wt% ferrite and 2 wt% perlite; average grain size 50 μm) with a 14 % volume fraction of graphite nodules. Carbon (nodules) and iron (matrix) have atomic numbers that are different enough to give a strong X-ray attenuation contrast. Therefore, the spherical nodules, which

are homogeneously distributed inside the matrix, are easily imaged by tomography and they can be used as *natural markers* for image correlation in the 3D reconstructed images. The average nodule diameter of 45 μm is large enough to allow for a relatively low resolution voxel size to be used for tomography. This also enables one to observe millimetric samples, the only limitation for the sample size being the overall attenuation of the material that has to allow for, at least, a 10 % transmission of the incoming X-ray beam. The fatigue crack interactions with the microstructure gives a roughness of the crack path of the order of the grain / nodule size. The material Young's modulus, yield stress and Poisson's ratio are equal to 175 GPa, 315 MPa, and 0.27, respectively. More details on the microstructure and mechanical properties of the material can be found in ref. [26].

2.2 Fatigue pre-cracking

A notched fatigue specimen with cross-section $6 \times 4 \text{ mm}$ (see Figure 1a) was pre-cracked at room temperature using a maximum load of 3,217 N (stress ratio: 0.1, frequency 10 Hz). The specimen faces were mirror polished prior to the pre-cracking experiment and an optical travelling microscope was used to detect crack initiation and monitor crack propagation *in situ*. Fatigue testing was periodically interrupted and the specimen held at mean load to ease crack length measurement. When a crack longer than 350 μm was observed, a load-shedding technique was applied to maintain a maximum stress intensity factor, K_{max} , less than $12.8 \text{ MPa}\sqrt{\text{m}}$ in order to make sure that a small-scale yielding condition prevailed at the crack tip (estimated plastic zone size in plane strain: 170 μm). Fatigue cycling was stopped as soon as a 1.5 mm long crack was observed. For the tomography experiment, a smaller specimen with a square cross-section of $1.6 \times 1.55 \text{ mm}^2$ (Figure 1b) was cut by electro discharge machining in the larger sample (Figure 1a) so that it contains only a part of the total fatigue crack tip with a crack size greater than the grain / nodule size. One face of the small specimen used for the present study contains the crack tip that was at the surface of the larger sample while the other face contains the crack tip that was at the centre of the larger sample.

2.3 X-Ray Microtomography

The X-ray microtomography experiments were performed using a computed tomography system V-Tomex (Phoenix X-ray) fitted with a Nanofocus tube whose acceleration voltage can be adjusted from 10 to 160 kV. In the present work, a 95 kV acceleration voltage was selected to ensure a 10 % transmission of the X-ray beam through the $1.6 \times 1.55 \text{ mm}^2$ cross-section of the sample. The specimen was placed on a rotating stage in the tomography chamber between the X-ray source and an amorphous Si diode array detector of dimensions 1920×1536 voxels. A set of 900 radiographs (scan) were taken while the sample was rotating over 360° along its vertical axis. With an acquisition time per image of 500 ms, one scan lasted about 45 min. A miniature loading device¹ was used to load the specimen (see Figure 1c). The distance between the sample and the tube could thus be reduced to 15.9 mm resulting in an image voxel size of $3.5 \mu\text{m}$ (divergent beam). The specimen was loaded from 13 N up to 217 N in six incremental steps. A scan was started as soon as stability of the load was reached, *i.e.* at 13, 44, 82, 130, 185 and 217 N. Reconstruction of the tomographic data was performed with a filtered back-projection algorithm using `datos|x-` acquisition software developed by Phoenix. It provides a 3D image with a 16 bit greyscale colormap that is proportional to the X-ray attenuation coefficient. Definition of a Region Of Interest (ROI) that is focused on the crack reduced the image size to $500 \times 700 \times 480$ voxels; a 2D section of this image is shown in Figure 1b. For the sake of clarity, all the images are presented using the same coordinate system represented in Figure 1 with loading axis along *x*, crack propagation in the *y* direction and sample thickness along *z*.

2.4 Digital image correlation

A C8-DIC multiscale algorithm with eight node cubic element was used to compute the displacement fields in the loaded specimen. Details about the method can be found in ref. [18]. The image acquired at minimum load, *i.e.* 13 N, is used as the reference image of the computation (Figure 2). A ROI of $592 \times 416 \times 400$ voxels was centred on the original

image of $700 \times 500 \times 480$ voxels. 8-node cubic elements were used. A resolution analysis was performed to choose the relevant size of the element for correlation. Different displacement values in the [0,1]-voxel range are numerically prescribed to the reference picture. Then, the correlation algorithm is applied to this pair of images, thus allowing for an evaluation of the average error and uncertainty, which is equal to the standard deviation of the displacement about its mean value, for different sizes of elements (Figure 3). An increase in the element size results in a reduction of the mean error and standard uncertainty.

However, even though the displacement uncertainty is the lowest for large elements, the heterogeneity of the displacement prompts one to use small sizes. Therefore an element size of 16 voxels was chosen as good compromise resulting in a mean displacement error of 3.3×10^{-3} voxel and a standard uncertainty of 8.7×10^{-2} voxel.

The image of the loaded specimen corrected by the displacements measured with DIC gives the “corrected image” shown in Figure 2. The presence of a discontinuity, *i.e.* the crack itself, impedes perfect matching of the image of the deformed sample to the reference image when the deformed image is corrected by the estimated displacement field. The difference between the reference and the deformed-and-corrected images is the residual error map that provides valuable information about the crack geometry.

2.5 Stress Intensity Factors extraction

From the measured displacement field, it is proposed to extract SIFs. First, least squares techniques are implemented by using 2D solutions [27-30]. An alternative technique to determine SIFs is to evaluate directly the *J*-integral along a given contour [31]. However, only few measurement data are used and strains and stresses are to be computed. To avoid this drawback, interaction integrals [32] are used for extracting SIFs from a discrete displacement field [33; 34]. This last technique can be extended to the analysis of 3D cracks [35]. It will not be used in the following. Instead, the technique proposed by Hamam *et al.* [27] will be followed.

It is assumed that each of the node layers orthogonal to the mean direction of the crack front ((x,y) plane in Figure 2) can be treated separately. For each of these planes (nearly orthogonal to the crack front), the 3D displacement field is projected in a least squares sense onto a basis that includes 2D solutions for a cracked solid (mode I and mode II) as well as mode III asymptotic solutions. Following Williams [36], a closed-form solution for the in-plane displacements \underline{v} is derived from Kolossov-Muskhelishvili's potentials [37]

$$\underline{v}(r, \theta) = \sum_n [\omega_n \underline{\Omega}_n(r, \theta) + \nu_n \underline{Y}_n(r, \theta)] \quad (1)$$

where ω_n and ν_n are real numbers, n the number of terms of Williams' series. The reference field for mode I is

$$\underline{\Omega}_n = \frac{r^{n/2}}{2\mu\sqrt{2\pi}} \left[\kappa \exp\left(i\frac{n}{2}\theta\right) - \frac{n}{2} \exp\left\{i\left(2 - \frac{n}{2}\right)\theta\right\} + \left((-1)^n + \frac{n}{2}\right) \exp\left\{-i\frac{n}{2}\theta\right\} \right] \quad (2)$$

and for mode II

$$\underline{Y}_n = \frac{ir^{n/2}}{2\mu\sqrt{2\pi}} \left[\kappa \exp\left(i\frac{n}{2}\theta\right) + \frac{n}{2} \exp\left\{i\left(2 - \frac{n}{2}\right)\theta\right\} - \left((-1)^{n+1} + \frac{n}{2}\right) \exp\left\{-i\frac{n}{2}\theta\right\} \right] \quad (3)$$

where r and θ denote the in-plane coordinates associated to the usual crack tip frame, μ Lamé's shear modulus, and κ a dimensionless elastic (or Kolossov) coefficient related to Poisson's ratio ν according to $(3 - \nu) / (1 + \nu)$ for plane stress conditions or $3 - 4\nu$ for plane strain conditions (used in the sequel).

The factor $\sqrt{2\pi}$ is introduced to match the usual definitions of K_I and K_{II} SIFs [38], which are thus equal respectively to the amplitudes ω_1 and ν_1 associated with the fields $\underline{\Omega}_1$ and \underline{Y}_1 .

Let us note first that the status of the fields $\underline{\Omega}_n$ and \underline{Y}_n is very different for n less than or greater than 1. For $n > 1$, the fields are called *subsingular*. They have no impact on the crack tip. Conversely, the attached stress fields increase with the distance to the crack tip. Such functions are thus useful to match the vicinity of the crack tip with the remote geometry, or

boundary conditions. However, since their impact on the crack tip process zone is negligible, one does not insist here on the structure of these fields. For $n < 0$, the fields are referred to as *supersingular*. Traditionally, the *supersingular* fields are ignored because their asymptotic behaviour near the crack tip is non-physical (*i.e.* diverging energy density). However, for the present purpose, since the crack tip process zone is cut out from the domain of analysis, one does not have to reject these solutions [27]. However, it makes no sense to extrapolate them *inside* the process zone. They rather characterize the (vanishing) influence of non-linearities present in the process-zone in the outer elastic domain.

Out of plane motions w induced by mode III displacements whose canonical field Ξ reads

$$\Xi = \frac{2}{\mu\sqrt{2\pi}} r^{1/2} \sin\left(\frac{\theta}{2}\right) \quad (4)$$

allow one to determine K_{III} .

Using least squares techniques, the measured displacement in each plane orthogonal to the crack front is projected onto the considered basis function. In practice, in-plane solutions are considered for n ranging between -3 and 5 . As mentioned above, negative n values correspond to *supersingular* solutions whose coefficients are related to a shift of the crack tip position in the plane with respect to the tip of the equivalent “elastic crack” for $n = -1$. By cancelling out its contribution, the equivalent crack tip position is estimated [27]. A length scale proportional to the process zone size [27] is obtained when ω_{-3} is related to $\omega_1 = K_I$. As all odd $n < 0$ functions lead to singular displacements at the crack tip, the displacement data at nodes whose distance to the crack tip (or respectively to the crack mouth) is less than 20 (resp. 16) voxels are not considered in the analysis.

A key feature of this study is to use a laboratory tomograph. Consequently, special care is to be paid to the post-processing of the displacement fields. For DIC applications, it is essential that the two images to be registered are directly comparable. Due to thermal expansion of the x-ray tube, the distance between the beam source and the specimen may vary by tiny

amounts during the experiment. The divergent beam geometry used for laboratory tomographs is such that this small distance change may result in significant (and spurious) image dilation. To decrease the voxel size and give a good crack description, the smallest possible sample / tube distance is used and even a modest thermal expansion in the tube results in an “apparent strain” of the order of 10^{-3} , *i.e.* comparable to elastic strain levels in most metals. This apparent strain should not be considered as a real one. Even though consequences of this artefact are limited in some cases (*e.g.* when large strain levels are observed [39]), it is not true in the present analysis. The strategy is to account for dilation by introducing the corresponding displacement field in the basis on which the DIC displacement is projected. The additional field varies linearly with the distance to the centre of the specimen and thus it is similar to a T-stress field. For conditioning purposes, the T-stress field is replaced by the dilation field and the least-squares analysis is performed with this modified basis. In other words, it is assumed that the actual T-stress is negligible as compared to the artifactual dilation to be extracted. The geometry of the mode I test used herein is consistent with this assumption.

2.6 X-FEM computation

An elastic eXtended-Finite Element Method using ELFE3-D software was performed to validate the results obtained with the SIF extractor described above. Details about X-FEM applications to tomographic images can be found in refs. [40; 41]. The computation was carried out using the true crack geometry described by level sets computed from the correlation residuals. The material model is elastic and defined by Young's modulus and Poisson's ratio reported in Section 2.1. From the previous analysis, an experimental displacement field is considered with rigid body and dilation corrections. The three components of this corrected displacement field are then used as a remote displacement on the top and the bottom face of the extended finite element model. From the resulting numerical displacement field, the same procedure as in Section 2.5 (except that the dilation correction is not searched for) is applied to extract SIFs.

3 Results

3.1 Identification of 3D crack shape

The grey level tomographic image of the cracked area can be thresholded in order to obtain a 3D rendering of the crack. However, for the cast iron used herein, similarity of grey values between the crack and the nodules makes it impossible to visualize the crack alone using this method (see Figure 4a). As reported in ref. [42], the growing crack is seeking out the nodules, which explains that the crack path deviates from a flat surface and that many nodules are embedded between the crack faces as shown in Figure 4a. To overcome this difficulty, the previously described residual error map was digitized on an 8 bit colormap and was thresholded using a 3D region growing algorithm from Amira software [43] to separate the voxels that belong to the crack from those that can be ascribed to noise such as computation error or image artefacts. Figure 4b shows the crack geometry as observed from the thresholded residual field under maximum load, *i.e.* at 217 N. The crack plane and tip position can be matched with those obtained from thresholding the tomographic image (Figure 4a) but the nodules are now erased so that the 3D topography of the crack is easier to observe. It is flat at a macroscopic scale but tortuous at the nodules scale. As this small sample was machined from one half of the larger pre-cracked specimen, the right-hand side of Figure 4 corresponds to the centre of the larger specimen, which underwent conditions close to plane strain during fatigue pre-cracking, while the other side corresponds to the free surface, *i.e.* closer to plane stress conditions. It is noticeable in Figure 4 that, due to tunnelling effect, the crack is longer in the former plane strain zone. For the sake of simplicity, left and right-hand sides of the specimen in Figure 4 will be referred to as *short crack side* and *long crack side* hereafter.

3.2 Crack tip position

The 3D rendering of the crack surface from the residual error map largely depends on the threshold value that is used for the region growing algorithm. A threshold value that is too small might result in noise embedded in the thresholded crack while a value that is too large might underestimate the crack front location especially at the crack tip where the thickness of the 3D object to threshold is the smallest. It is to be stressed that the residual field is markedly different along the crack path for a crack opening of order of half a voxel. Hence, the estimate of the crack front position is slightly underestimated as compared to its actual position where the crack opening displacement vanishes, and becomes undetectable by this procedure. For small crack opening (below 217 N), the crack tip visibility is better in the tomographic image than in the residual error probably because of some residual crack opening. Consequently, the crack tip was measured directly via visual inspection of the tomographic image in grey levels to check the position that can be deduced from the residual error field at maximum load (217 N) and validate the thresholding method. The methodology uses Image J software [44]. At a given load, the crack is viewed along the z direction and artificially coloured to enhance contrast between the crack and the cast iron matrix. A plug-in allows one to retrieve the (x,y) coordinates of the voxel that is manually selected at the crack tip. Thus, the crack tip position is determined in the thickness of the specimen and the resulting points are reported in Figure 5a. A rather large scatter of data is obtained at small loads when small crack opening results in limited crack tip visibility. This scatter is reduced at maximum load. Experimental points were fitted to analyse the variation of the apparent crack tip position, as observed via image analysis, with loading (Figure 5b). There is no visible evolution of the crack front between 13 and 44 N. Only at 82 N does the crack seem to go deeper inside the specimen. This level probably corresponds to a full opening of the crack front. The crack front positions measured at 82 N and above on both sides of the sample are consistent with the crack lengths of 636 and 1084 μm measured with an optical microscope.

It is also noticeable that the apparent crack “advance” is substantially higher on the *short crack* side than on the *long crack* side.

3.3 Displacements fields in the bulk of the specimen

Only a limited amount of information is made available by such “simple” image analysis while image correlation provides the full displacement fields in the bulk of the specimen. The discontinuity induced by the crack is clearly visible in the U_x displacement field (Figure 6) corresponding to mode I offering the possibility to study the crack opening change with load at a local scale. A slight discontinuity is also detectable in the U_y and U_z displacement fields, *i.e.* in Mode II and III. Mode II displacement or in-plane shear is localized on the right-hand side of Figure 4 where the crack deviates from the overall mean crack plane; the difference in U_y displacements between upper and lower crack faces remains less than 0.8 voxel (*i.e.* less than 3 μm) even under maximum load. Mode III displacement on both sides of the crack plane is distributed through the specimen thickness along the crack mouth with localization towards the *short crack* side at maximum load. U_z displacement is less than 1.4 voxel (*i.e.* 5 μm).

3.4 Crack opening displacement

The displacement field in mode I, U_x , is smooth and continuous away from the crack as shown in Figure 6. Thus, the displacement jump (ΔU_x) on the crack surface is estimated from the computed difference between the U_x values in two slices taken parallel to the average crack plane on both sides of the crack (Figure 6). The resulting COD map in the specimen cross-section is plotted for increasing load levels in Figure 7 with a colormap that is proportional to the value of crack opening. Values of ΔU_x greater than 3 times the standard uncertainty, *i.e.* 0.27 voxel or 1 μm , are assumed to correspond to a “real” crack opening so that black areas in Figure 7 correspond to crack faces still in contact. At 44 N, contact areas are still observed at the crack front. Only at 82 N and above does the crack fully open on the *short crack* side and a non-negligible value of ΔU_x is observed at the position of the crack tip

(depicted by a white line in Figure 7). Under maximum load, *i.e.* 217 N, the opening at the crack mouth amounts to 19 μm , *i.e.* more than five voxels, and it decreases towards the crack tip making the tip positions more difficult to assess. It is visible that at 130 and 217 N, the displacement jump goes farther than the crack tip position and that the opening values behind the crack tip are well above the opening level so that they could not be attributed to measurement noise only.

Profiles of ΔU_x from crack mouth to crack tip were extracted for each loading step on both sides of the specimen, *i.e.* along the dotted lines drawn in Figure 7, to obtain a more quantitative information. The resulting points are plotted in Figure 8 for the *short* and *long crack* side. Crack lengths reported in Figure 8 (indicated with arrows) were measured on the thresholded residual error map in Figure 4 so that they also correspond to the crack front position reported in Figure 7. They are shorter than the displacement jump extent by about 200 and 75 μm , respectively for the *short* and *long crack* side. At the smallest load (44 N), the crack is not completely open and ΔU_x shows variations from maximum values that are below the voxel size (3.5 μm) to zero. The values of COD measured should be a square root function of the distance to the crack tip if a linear elastic behaviour prevail at the vicinity of the crack tip [45]. Thus, the solid line curves in Figure 8 correspond to the best fit curves that could be obtained for each profile. Above 130 N, these fitted curves fail to represent experimental data close to the crack tip, probably because of the large plastic zone that develops at the crack tip at these load levels.

3.5 Estimation of the Stress Intensity Factors

The K_I SIF could be computed directly from the curves shown in Figure 8. However, this computation method does not give a full description of K_I values along the crack front and it does not exploit the full 3D displacement field information. Last, the dilation artefacts have to be incorporated. Therefore, the above mentioned extraction method (cf. Section 2.5) was used to measure SIF values along the crack front for the different loading steps. The results obtained for K_I , K_{II} and K_{III} are reported in Figure 9. The *short* and *long crack* sides

correspond to the left and right hand sides of Figure 9a to c respectively. In Figure 9a, the measured values of K_I on both sides of the sample emphasize the importance of the 3D effect. On the side where the crack is shorter, K_I is enhanced while it is reduced on the side where the crack is in advance due to the constraint exerted by the surrounding uncracked ligament. A 2D analysis would be unable to represent such an effect. The 3D X-FEM analysis predicts the same trend as the experimental values. Up to a 130 N load, an excellent match is obtained between the elastic X-FEM computation and the experimental points. Then, at 217 N, the computed curve rises slightly higher as plasticity develops. In Figure 9b, values obtained for K_{II} show fluctuations around 0 through the sample thickness, *i.e.* from about 1 to -1 MPa \sqrt{m} with K_{II} values that do not vary significantly with increasing load up to 130 N but do increase at 217 N. K_{III} has an almost zero value that tends to increase slightly with load as shown in Figure 9c. The X-FEM computation for K_{II} and K_{III} (using measured boundary conditions obtained from DIC analyses) shows a good agreement with experimental points. Although the specimen was macroscopically loaded in mode I, small mixed mode displacements occurred.

The position of the crack tip calculated with the SIF extractor is plotted in Figure 10 within the sample thickness. At 82 N and above, the calculated crack tip position in Figure 10 is in agreement with the crack tip position observed in the grey level images although the calculated position is about 80 to 120 μm deeper. In the SIF extractor, the crack length that is calculated corresponds to an equivalent elastic crack. Thus, the larger the plastic zone size at the crack tip, the longer the “equivalent elastic” crack as compared to the “real” or physical crack. Moreover, the manual procedure for estimating the crack front position (Figure 5) in the tomographic image is sensitive to the local crack opening displacement so that it tends to underestimate the crack front position. Both effects contribute to the observed differences.

4 Discussion

To the best of the authors' knowledge, this is the first time that crack opening displacement *fields* are measured at a local scale by applying DIC on 3D images obtained with a laboratory X-ray tomograph, an equipment which is becoming more and more widespread in materials science laboratories. A problem that is typical of this kind of equipment has arisen. The thermal expansion of the X-ray tube during tomographic data acquisitions results in artificial "dilation" of the sample. For the four studied load levels, spurious strains of the order of 10^{-3} , 1.7×10^{-3} , 1.6×10^{-3} , 2.7×10^{-3} , respectively, were measured. This dilation superimposes on the real displacement field inside the sample under tensile loading and biases the interpretation of DIC results. In the present study, this artefact was solved by a correction added to the above-mentioned SIF extraction method. In the near future, other solutions will be tested to solve the problem directly at its source by cooling of the X-ray tube. Provided this dilation artefact is corrected for, the use of a laboratory X-ray source instead of a synchrotron facility facilitates the kind of experiment presented herein.

The DIC method can however only be applied to materials with finely dispersed and resolvable microstructural features. The nodular graphite cast iron used in this study is a widely used material whose microstructure (with natural markers) is perfectly suited for image correlation. However, the present study would not have been possible for example with the 2024 aluminium alloy used by Toda *et al.* [21; 22] where the natural markers used (pores) have a low volume fraction and a typical size about twice the voxel size used in the present study.

The displacement uncertainty reported in Figure 3 appears to be higher than the levels reported for 2D images [46]. A possible source of this larger uncertainty lies in the nature of the images used. Tomography images are prone to "noise" because of reconstruction artefacts and improvement in reconstruction of tomographic data may help one to decrease the DIC uncertainty. It is to be noted that, for a given element size, coarsening the image resolution, e.g. from 12 to 36 μm per voxel, was reported to divide the DIC uncertainty by

more than 3 [20]. However, in the present study, a small voxel size (3.5 μm) was preferred in order to have an accurate mapping of the displacement field and of the crack morphology.

An advantage of DIC is also that it allows for 3D rendering of the crack without resorting to threshold tomographic images. Compared to PT [21; 22], DIC is also a more automatic method. Although a robust and automatic particle tracking method is being developed to optimize the tracking efficiency [25], it has still not proved successful for cracked specimens. Besides, while application of PT to cracked specimens is restricted to the crack tip [21], DIC allows for an extended area to be studied, and the full 3D displacement field to be measured so that 3D maps of COD are accessible. Moreover, the exact position of the crack tip is not a pre-requisite to SIFs extraction. As explained in Section 2.5, SIFs are computed with respect to a calculated crack tip position (Figure 10) whose accurate position is not known *a priori*.

In the present study, different techniques allowed for the detection of crack opening during progressive loading of the specimen. Using direct image analysis to retrieve the crack tip position, an advance of the apparent crack tip position is observed in Figure 5b when the load increases from 44 to 82 N; it is not visible in the residual error field probably because of the medium spatial resolution of the DIC field. This apparent crack advance may be related to PICC that developed during pre-cracking of the larger sample. The larger advance observed on the *short crack* side would then be consistent with the size of the plastic zone inherited from the larger specimen. At the former free surface of the large sample, the plane stress condition created a plastic zone size that is theoretically about 3 times greater than that in plane strain, *i.e.* at the *long crack* side. Consequently, this larger plastic zone exerts its influence on a longer distance away from the crack tip. It is noticeable that the plane stress plastic zone seems to influence a large part of the crack front away from the former free surface. In thin specimens, Chermahini *et al.* [47] also reported that the opening load decreases slightly from the free surface towards the centre of the specimen whereas in thicker specimen, the region of higher opening load was restricted to a relatively narrow region near the free surface as expected. However, in the present study, this result should be

considered with caution as the cutting of the small tomography sample might induce stress relaxation so that the stress state that formerly existed inside the larger specimen might not be fully acting in the smaller specimen.

In the 3D images of the crack, a load of 82 N was sufficient to open the crack, and above this load level, the apparent crack tip position (Figure 5) did not vary significantly. However, non negligible values of COD are observed ahead of the crack tip location measured at maximum load (see Figure 8); they might be attributed to the presence of a plastic zone. At 217 N, the mean stress on the uncracked ligament is about 60 % of the monotonic yield strength.

Generalized plasticity is thus not expected. However, due to dissymmetry of the crack and the vicinity of the free surface, the plastic zone size at the crack front is likely to increase rapidly, especially on the *short crack* side, and the confined plasticity condition may be violated at the crack front. This hypothesis is in agreement with the fact that an elastic computation (see 'E' in Figure 9a) was unable to perfectly match the experimental points at 217 N, while a nearly perfect match was observed at 130 N and below.

Using the 3D displacement fields obtained from DIC, the SIF change along the crack front was obtained for the different load levels. K_{II} in Figure 9b varies around a zero value and a small positive value is measured for K_{III} in Figure 9c. Crack geometry and misalignment of the specimen inside the *in-situ* loading device and / or misalignment of the crack faces after fatigue pre-cracking of the large sample may explain some of this mixed mode displacement during tensile loading. However, mode II and III SIFs remain close to zero, and mode I is predominant, as expected from the prescribed "macroscopic" mechanical testing conditions. K_I is observed to increase from the *long crack* side towards the *short crack* side in Figure 9a. This is the result of the 3D shape of the crack, namely, a locally lagging crack front induces a higher value of SIF [48; 49].

By combining the results of Figure 7 and 9a it is possible to give an estimate of the value of opening SIF, K_{op} , assuming that mode I is the main opening mode and, also, that the crack actually opens when the measured ΔU_x equals 0.27 voxel. Around 82 N, the measured

values of K_I vary from 7.5 to 3.5 MPa \sqrt{m} from the *short crack* side (fully open) to the *long crack* side (crack locally closed). At 130N, K_I varies from 13 to 6 MPa \sqrt{m} and both sides of the crack are fully open. The value of K_{op} can thus be estimated close to 6 MPa \sqrt{m} . This level is in very good agreement with values reported in the literature by different authors on the same material but using mechanical compliance techniques [50-52]. This tends to indicate that DIC coupled with laboratory X-ray tomography can be trusted to assess crack closure in 3D studies of this type of material.

5 Conclusions

3D-DIC analyses on 3D microtomographic images obtained with a laboratory X-ray source were used to study fatigue crack closure in a nodular graphite cast iron. An *in-situ* testing machine enabled for progressive loading of the specimen in tension and 3D images acquired at different loading steps allowed for the detection of the opening load. The 3D images were further analyzed using 3D digital image correlation. The nodular graphite cast iron material is well adapted to the correlation technique with graphite nodules that act as natural markers. Compared to the tracking method used by Toda *et al.* [21; 22] to analyze crack closure in synchrotron X-ray microtomographic images, DIC is a more automatic method that provides the full displacement field inside the cracked sample. The measured displacement fields were then used to evaluate the COD maps in the specimen cross-section in order to visualize crack opening locally with an increased resolution compared to direct image analysis of the crack. A stress intensity factor extractor adapted for lab-CT, *i.e.* with correction for the artificial dilation induced by thermal expansion of the X-ray tube, permitted us to compute the stress intensity factor along the crack front from the 3D displacement fields. The confrontation of the COD maps with local SIF allowed for the estimation of a stress intensity factor for opening, K_{op} , equal to 6 MPa \sqrt{m} .

The method described herein could be potentially used to investigate the geometry of fatigue cracks in samples with a larger size (up to 5 mm with the present tomograph) relevant for

engineering applications and corresponding to more complex loading cases (e.g. tension / torsion loading). Besides, the tomography technique being non destructive, the same type of study can be performed *in situ* during fatigue crack propagation. Such experiments have been performed recently and are currently being analysed, they should allow to assess crack closure during mechanical cycling, and to correlate it to local crack growth.

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8 Figure captions

Figure 1 : Fatigue pre-cracking of (a) the large specimen from which a (b) small sample is obtained for (c) microtomography of *in-situ* loaded specimen.

Figure 2 : Extraction of the crack surface from Digital Image Correlation measurements.

Figure 3 : Displacement uncertainty and error expressed in voxel as functions of the element size when uniform sub-voxel displacements are prescribed.

Figure 4 : 3D rendering of the crack surface at maximum load from (a) the thresholded tomographic image and from (b) the residual error field.

Figure 5 : Position of the crack front for different load levels: (a) experimental points and (b) fitting curves.

Figure 6 : Displacement (expressed in voxels) fields in the specimen volume under maximum load (macroscopic load applied along x direction). The hatched planes drawn in the U_x field indicate the (y, z) planes used for COD mapping in Figure 7.

Figure 7 : Maps of ΔU_x displacement (COD) in the specimen cross-section with increasing load. The crack front is drawn in white and the dashed-lines along y direction indicate the location of the profiles plotted in Figure 8.

Figure 8 : Change with load of the crack opening displacement profile along crack depth (a) on the short and (b) long crack side; the dashed-line corresponds to 3 times the uncertainty in U_x and the arrow indicates the position of the crack front plotted in Figure 7. The solid lines correspond to the best fitting curves.

Figure 9 : SIF values along the crack front for (a) Mode I, (b) Mode II and (c) Mode III; Measured ('FF') values of SIF (symbols) are compared to computed ('E') values (lines); the hatched area in (a) corresponds to the K_{op} range obtained from literature data.

Figure 10 : Crack tip position of the equivalent "elastic crack" based on the SIF extractor method (symbols); the solid lines correspond to the crack tip positions reported in Figure 5b (visual inspection of tomographic images and smoothed by curve fitting).

¹ Courtesy of W. Ludwig – MATEIS/ESRF

Table 1

Reference	X-Ray source	Crack	Voxel size in μm	Method	Material	Displacement uncertainty (in voxels)	Section of analysis (mm) [subvolume in voxels]	Deformation range (%)
[19]	laboratory	no	35	DIC	Trabecular bone	3.5×10^{-2}	$\varnothing 15$	0.4 – 1.8
[22]	synchrotron	yes	0.7	Manual tracking	Al2024-T351 with 800 pores $7.2 \mu\text{m}$ in \varnothing	5×10^{-1}	0.8×0.9	Elastic
[21]				Tracking		10^{-1} (on COD)		
[23]	synchrotron	no	1.5	Tracking	Aluminium with added (5000) W markers $10 \mu\text{m}$ in \varnothing	2×10^{-1}	0.45×0.45	2.7 – 9.5 (plastic)
[20]	laboratory	no	36 (20,12)	DIC	Open-cell aluminium foam	5×10^{-2}	5×5 [28 \times 16 \times 26]	No loading
[24]	synchrotron	no	1.5	Tracking	Al/AlO ₂ with added (~38000) W markers	5×10^{-1} (on markers' position)	$\varnothing 1$ [67 ³]	10 (plastic)
[25]	synchrotron	no	0.474	More automatic tracking	Copper alloy with 188 artificial pores $15 \mu\text{m}$ in \varnothing	1 (on markers' position)	0.25×0.3	3.5 – 22 (plastic)
[18]	synchrotron	no	4.91	DIC	Polypropylene solid foam	3×10^{-1} - 3×10^{-2}	$\varnothing 15$ [400 ³]	10 – 30

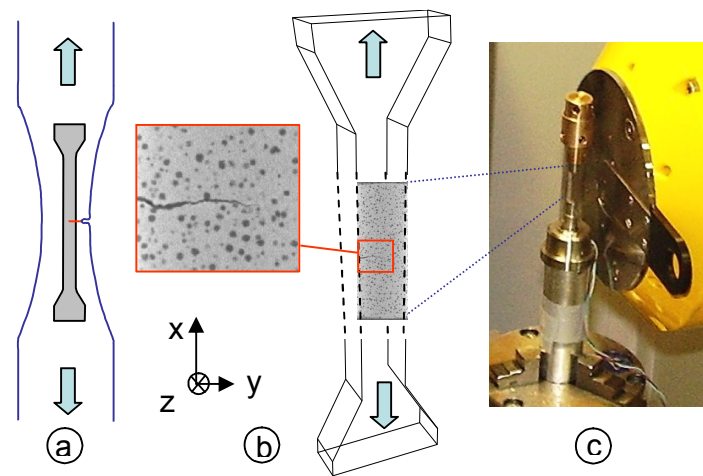


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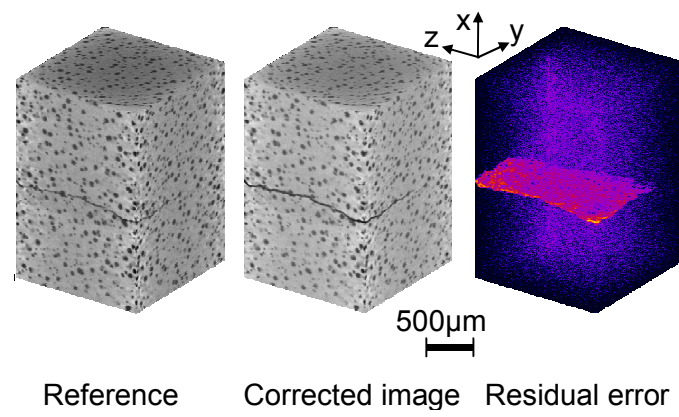


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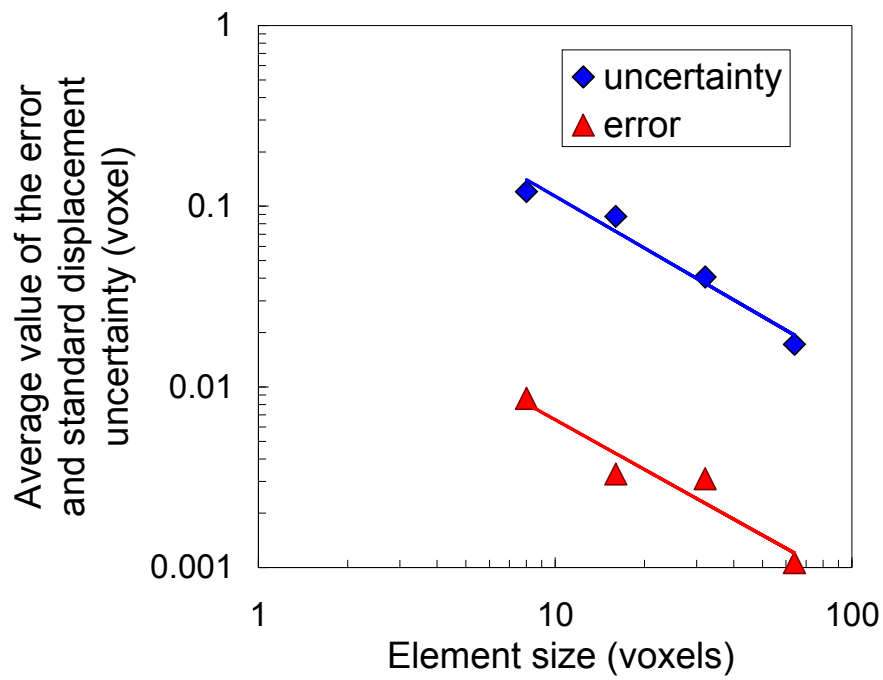


Figure 3 : Displacement uncertainty and error expressed in voxel as functions of the element size when uniform sub-voxel displacements are prescribed.

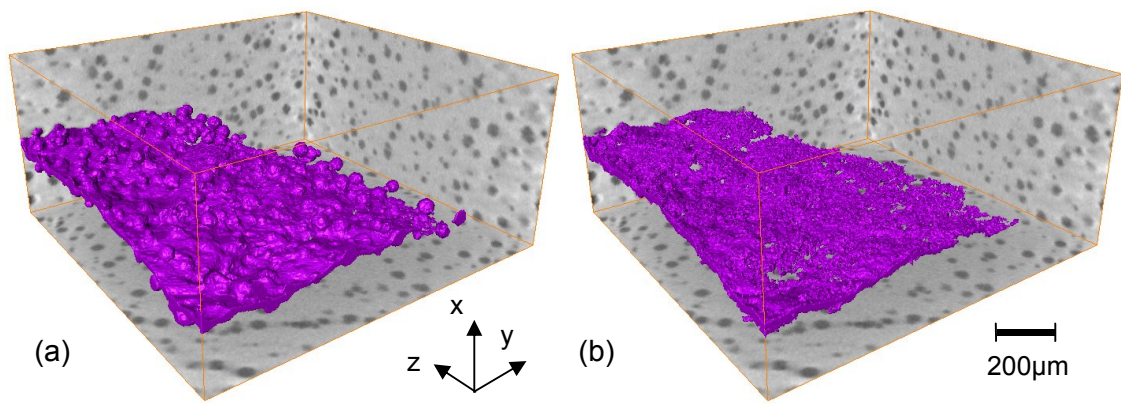


Figure 4 : 3D rendering of the crack surface at maximum load from (a) the thresholded tomographic image and from (b) the residual error field.

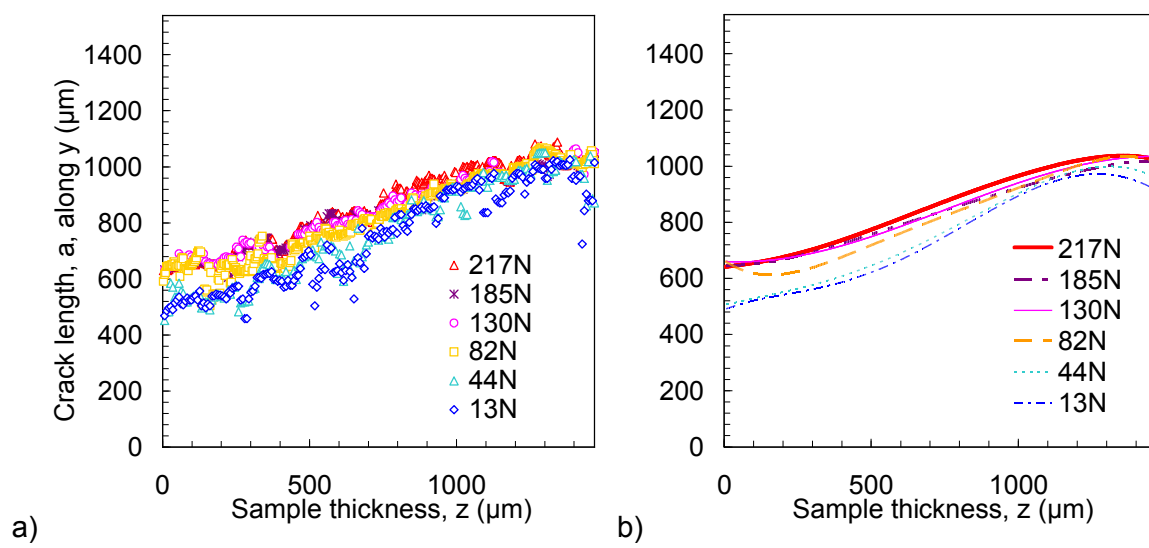


Figure 5 : Position of the crack front for different load levels: (a) experimental points and (b) fitting curves.

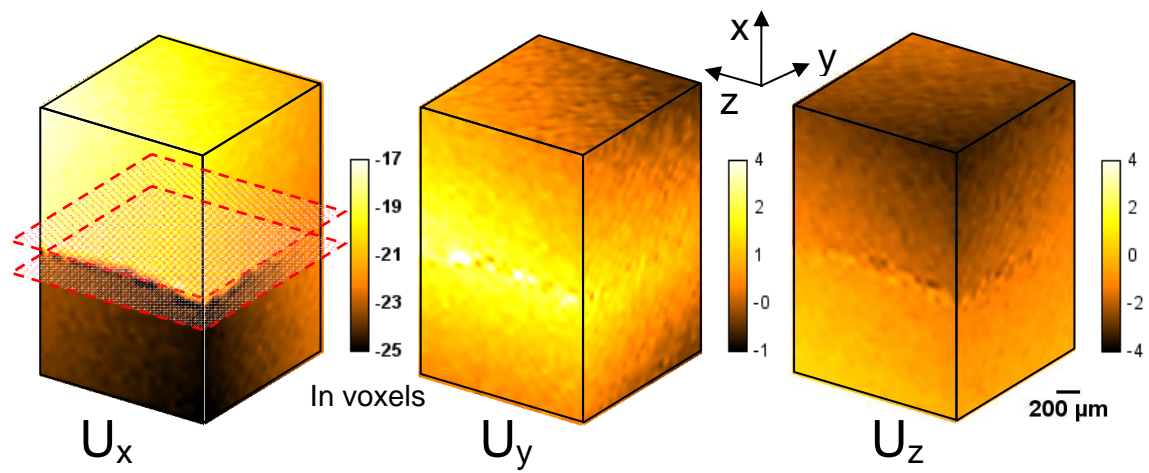


Figure 6 : Displacement (expressed in voxels) fields in the specimen volume under maximum load (macroscopic load applied along x direction). The hatched planes drawn in the U_x field indicate the (y, z) planes used for COD mapping in Figure 7.

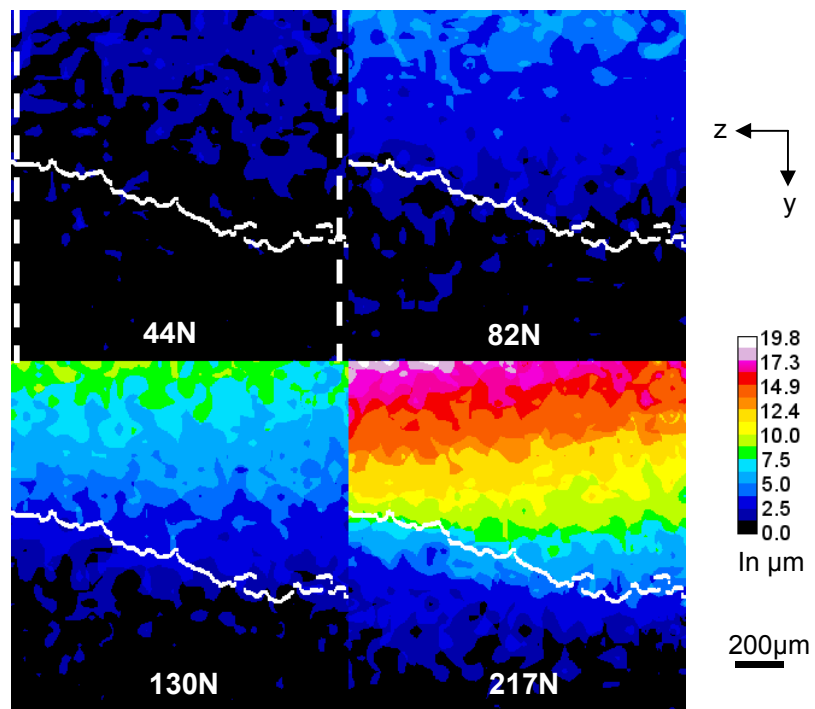


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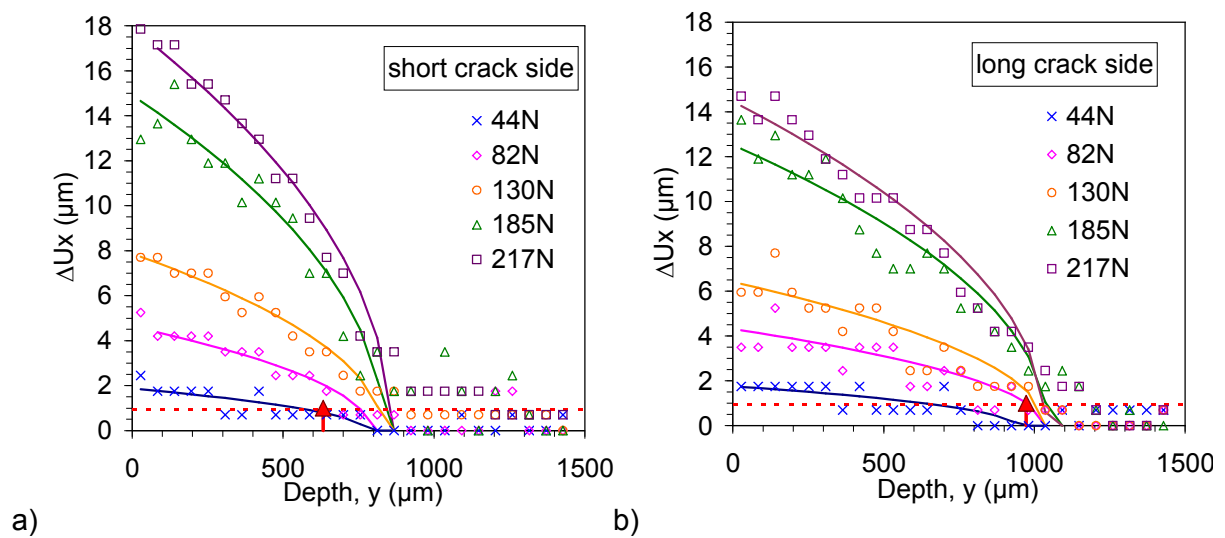


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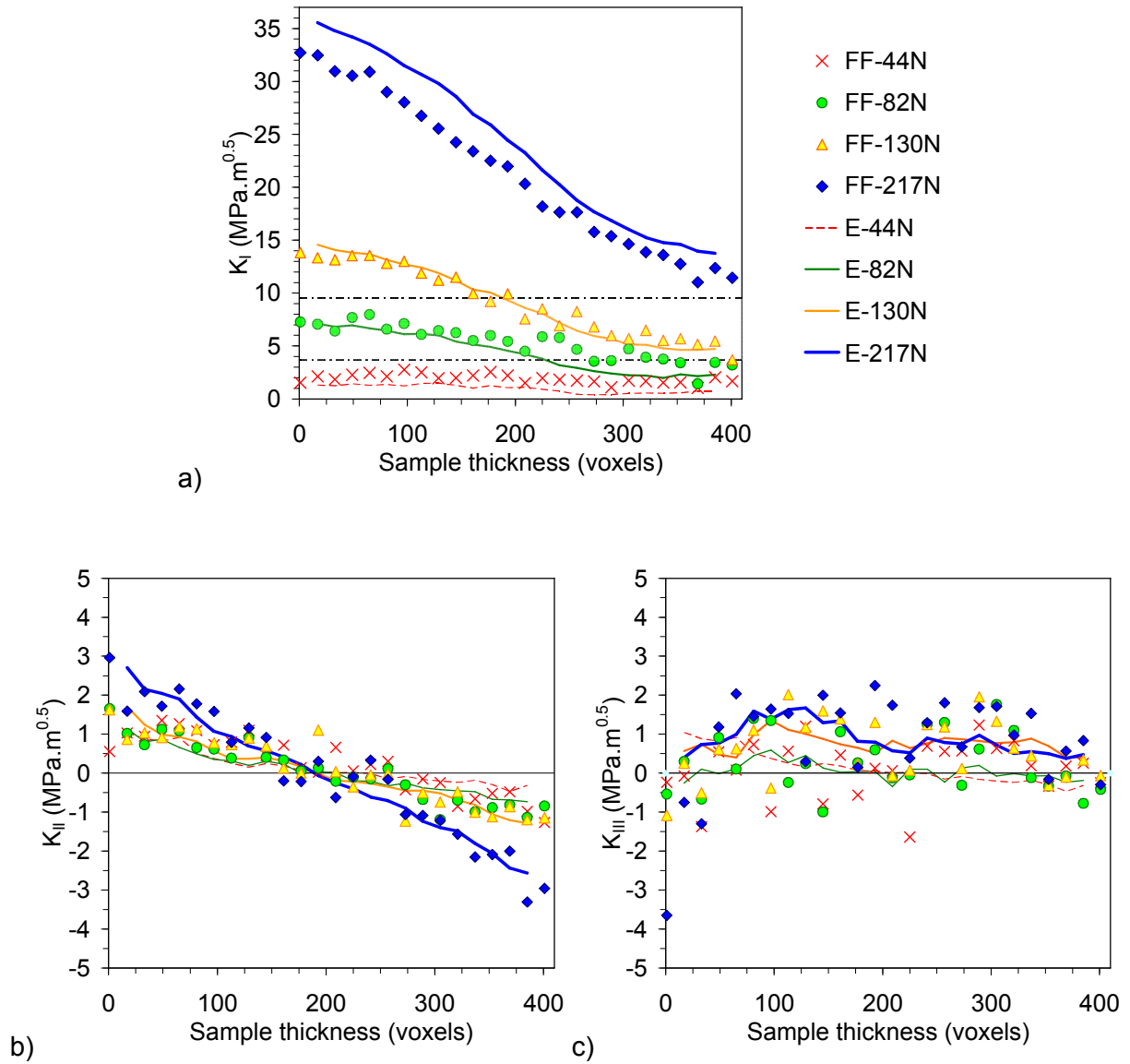


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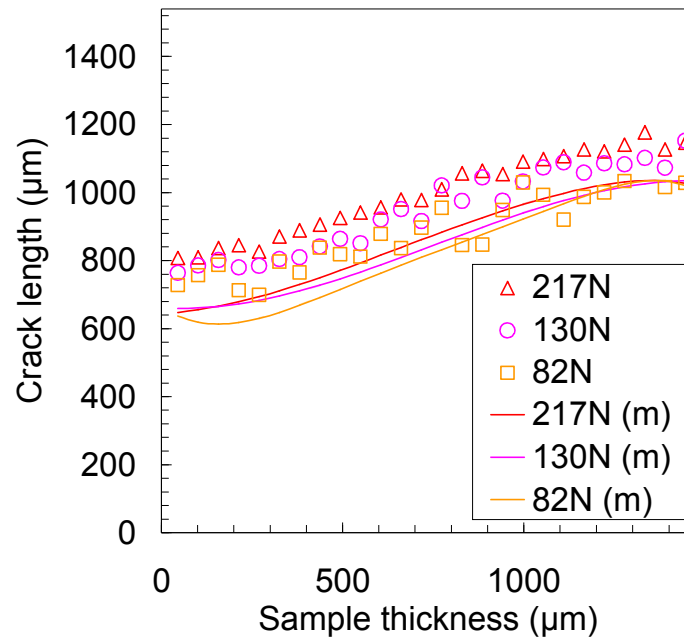


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