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# A NEW EM ALGORITHM FOR UNDERDETERMINED CONVOLUTIVE BLIND SOURCE SEPARATION 

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#### Abstract

This paper presents a new statistical method for separating more than two sound sources from a two-channel recording. It is based on a probabilistic model of the Interchannel Level/Phase Difference presented in [1] and the model parameters are estimated using the maximum likelihood criterion and an Expectation-Maximization algorithm. The source separation task is achieved by soft time-frequency masking of the observation. These masks are derived from the estimated source position model. Algorithm performance is evaluated on the real and synthetic convolutive mixtures data of the first audio source evaluation campaign [2] as well as the Signal Separation Evaluation campaign (SiSEC) [10]. Promising results are obtained when comparing to the other methods presented in these two campaigns.


## 1. INTRODUCTION

Blind Source Separation (BSS) is a widely used technique that aims at recovering a set of $N$ original sources based only on their $M$ observed mixtures. This task is more difficult when the mixing model is not instantaneous but convolutive and gets even harder in the underdetermined case ( $N>$ $M)$. Indeed, when $N$ is larger than $M$, no algebraic linear solution can be found to separate the sources, even if the mixing matrix is identified. Still, with the source sparseness assumption, researchers have found a way to build non linear masks for the separation task.

Most of the BSS methods that consider the sparseness assumption deal with the two-channel case from which cues or features like Interchannel Level/Phase Difference (ILD/IPD) are used. In [3] a KMeans algorithm classifies these features in clusters and binary separating masks are estimated. In [4], rather than clustering the observed (ILD/IPD), the authors propose to model these features as Gaussian variables with the assumption of a dominant path. Then, after estimating the model parameters, soft separating masks have been derived. Nevertheless, in real-world situations, the underlying linear phase assumption deriving from the dominant path hypothesis reveals not applicable due to early reflections and reverberation. Also, the proposed Gaussian model, even if it facilitates the equation computation, does not have any theoretical background.

In this paper a Model Based Underdetermined (blind) Source Separation (MBUSS) is considered. In our previous work [1] a theoretical distribution for the $(\log (I L D) / I P D)$ features is presented, but no separation algorithm based on this distribution was explicitly provided. This paper, proposes an estimation procedure for this theoretical distribution parameters, based on an Expectation-Maximization (EM) algorithm where the Maximization step is speededup by a Quasi-Newton algorithm. Unlike [3], probabilistic soft masks are computed instead of binary ones, thus less
distortion and artifact are audible in the extracted sources. Unlike [4], separation is performed independently in each frequency band, therefore no linear phase assumption is made and wide band sources can be extracted even with the presence of frequency aliasing. Of course separating independently in each frequency band has the traditional permutation problem drawback. This permutation alignment is corrected using the ratio envelope of the extracted sources as in [5].

## 2. MODEL BASED SOURCE SEPARATION

We describe here briefly the $(\log ($ ILD $) /$ IPD $)$ probabilistic model that will be used in the separation task. For more detailed analysis, please refer to [1]. Consider the convolutive two-channel mixture model:

$$
\begin{equation*}
x_{j}(t)=\sum_{i=1}^{N} x_{j}^{(i)}(t)=\sum_{i=1}^{N} \sum_{k} a_{j i}(k) s_{i}(t-k) \tag{1}
\end{equation*}
$$

where $x_{j}^{(i)}(t)$ is the contribution of the $i^{\text {th }}$ source to the $j^{\text {th }}$ sensor. $s_{i}(t), i=1, . ., N$ are the sources and $a_{j i}(k)$ is the impulse response of the acoustic channel separating source $i$ from microphone $j$ with $j=1,2$. The time-domain observed signals $x_{j}(t)$ are converted into frequency-domain time-series signals using the Short-Time Fourier Transform (STFT):

$$
\begin{equation*}
X_{j}(t, \omega)=\sum_{k=0}^{L-1} w(k) x_{j}(t+k) e^{-j \omega k}=\sum_{i=1}^{N} X_{j}^{(i)}(t, \omega) \tag{2}
\end{equation*}
$$

where $w(k)$ is a window (e.g. Hanning) and $X_{j}^{(i)}(t, \omega)$ is the STFT of $x_{j}^{(i)}(t)$. Sparseness of the sources in the Time Frequency (TF) domain is the key assumption in solving the underdetermined separation problem. It means that each given source is non negligible on only a few number of TF slots. It generally implies that the sources have nearly disjoint supports in the TF domain in the sense that for each TF slot there can be at most one dominant source, and it is this last assumption that will be actually assumed [3]. If $q$ is the index of this dominant source at $(t, \omega)$, then the $j^{\text {th }}$ observation in eq.(2) can be approximated to $X_{j}(t, \omega) \approx X_{j}^{(q)}(t, \omega)$ and the ratio between the two observations at $(t, \omega)$ will then be:

$$
\begin{equation*}
R(t, \omega)=\frac{X_{1}(t, \omega)}{X_{2}(t, \omega)}=\frac{\sum_{i=1}^{N} X_{1}^{(i)}(t, \omega)}{\sum_{i=1}^{N} X_{2}^{(i)}(t, \omega)} \approx \frac{X_{1}^{(q)}(t, \omega)}{X_{2}^{(q)}(t, \omega)} \tag{3}
\end{equation*}
$$

The approximation $X_{j}^{(i)}(t, \omega) \approx A_{j i}(\omega) S_{i}(t, \omega)$, with $A_{j i}(\omega)$ as the Fourier transform of $a_{j i}(k)$, can be found in most of
the TF source separation methods. With it, the last term in (3) can be reduced to a constant in each frequency band $\omega$ and thus:

$$
\begin{equation*}
R(t, \omega)=\frac{X_{1}(t, \omega)}{X_{2}(t, \omega)} \approx \frac{X_{1}^{(q)}(t, \omega)}{X_{2}^{(q)}(t, \omega)} \approx \frac{A_{1 q}(\omega)}{A_{2 q}(\omega)} . \tag{4}
\end{equation*}
$$

The above ratio, being (approximately) time independent but frequency and source dependent, has been widely used as dominant source indicator in the TF binary masks approach. In [3], the modulus and argument of $R(t, \omega)$, which are no more than the well-known Interchannel Level Difference (ILD) and Interchannel Phase Difference (IPD), have been clustered by a KMeans algorithm. The cluster members define the binary separating mask and the cluster centers give an estimation of $A_{1 q}(\omega) / A_{2 q}(\omega)$. But does the above approximation (4) hold when dealing with a long tap impulse response, i.e with a reverberating environment?

### 2.1 One source Ratio STFT distribution model

To simplify the notations in this section, we will omit the $\omega$ parameter. From now, we implicitly work in given frequency band $\omega$. It has been demonstrated in [1] that, even if one source is observed, $R(t)$ is not constant in time. Fig. 1 plots the real and imaginary part of $R(t)$ for a 10 -second speech source placed in a moderate reverberant conditions ( $T_{60}=$ 250 ms ). This one source observed ratio should be considered as a (complex) random variable, the distribution of which has been derived in [1]. More precisely this paper provides the theoretical joint density of the real part and imaginary parts $x$ and $y$ of $\log R^{(q)}(t)=\log \left[X_{1}^{(q)}(t, \omega) / X_{2}^{(q)}(t, \omega)\right]:$

$$
x=\log \left|R^{(q)}(t)\right|=\log \operatorname{ILD}_{q}, \quad y=\arg R^{(q)}(t)=\operatorname{IPD}_{q}
$$

where $\operatorname{ILD}_{q} / \mathrm{IPD}_{q}$ are the ILD/IPD of $s_{q}$. Note that we did not considered the traditional feature $R^{(q)}(t)$ because it admits an infinite variance (see [1]). To estimate the joint density of $(x, y)$, we assume that $L$ is large enough so that, by the Central Limit Theorem, the pair $X_{1}^{(q)}(t)$ and $X_{2}^{(q)}(t)$ can be considered as Gaussian (complex circular) [1] with variance $\sigma_{1, q}^{2}(t)$ and $\sigma_{2, q}^{2}(t)$ and complex cross-correlation $\beta_{q}$. It has been demonstrated in [1] that the variance ratio $\sigma_{1, q} / \sigma_{2, q}$ and $\beta_{q}$ does not vary in time and may be considered as specific features for each source $s_{q}$, hence of the variable $\log R^{(q)}(t)$. Based on the complex gaussian circular assumption, the couple of variables ( $x, y$ ) admits the following joint density [1]:

$$
\begin{equation*}
p\left(x, y \mid r_{q}, \rho_{q}\right)=p_{\rho_{q}}\left(x-\log \left|r_{q}\right|, y-\arg r_{q}\right) \tag{5}
\end{equation*}
$$

where $r_{q}=\left(\sigma_{1, q} / \sigma_{2, q}\right) e^{i \arg \beta_{a}}, \rho_{q}=\left|\beta_{q}\right|$ and

$$
p_{\rho}(x, y)=\frac{1}{4 \pi} \frac{1-\rho^{2}}{(\cosh x-\rho \cos x)^{2}} .
$$

The parameters $r_{q}$ and $\rho_{q}$ are specific to the source $s_{q}$ position in space. Note that it is the source position in space which is modeled and not the source itself. Thus, this "'space"' position model can be applied independently from the source model (gaussian, laplacian, ...). More in details, $r_{q}$ corresponds to the mean of $\log R^{(q)}(t)$ and thus depends only on the source position in space where $\left|r_{q}\right|$ is equal to the $\mathrm{ILD}_{q}$ and $\arg \left(r_{q}\right)$ is equal to the $\mathrm{IPD}_{q}$. As for $\rho_{q}$, it will stand for the reverberation degree of the acoustic path separating $s_{q}$ from the set of microphones. This can be viewed from its definition as the modulus of the cross-correlation between the two observations where high reverberation causes low cross-correlation between microphones and vice-versa. For example, in free field conditions, i.e anechoic environment, the cross-correlation is maximum and $\rho_{q}=1$.


Figure 1: Ideal and observed (IPD, $\log (\mathrm{ILD})$ ) for a single source mixture at the 100 Hz center frequency

### 2.2 Mixture ratio STFT distribution model

Having the one source log ratio distribution model (5) and under the disjoint assumption, we are led to assume the following distribution model for the real and imaginary parts of the observed $\log$ ratio $\log [R(t, \omega)]$ :

$$
\begin{equation*}
p(x, y \mid \boldsymbol{\rho}, \boldsymbol{r}, \boldsymbol{\mu})=\sum_{i=1}^{N} \mu_{i} p_{\rho_{i}}\left\{x-\log \left|r_{i}\right|, y-\arg r_{i}\right\} . \tag{6}
\end{equation*}
$$

This model is given at the frequency $\omega$ for the set of considered time points $t \in T$ with $\boldsymbol{\rho}=\left[\rho_{1}, . ., \rho_{N}\right], \boldsymbol{r}=\left[r_{1}, . ., r_{N}\right]$ and $\boldsymbol{\mu}=\left[\mu_{1}, . ., \mu_{N}\right]$ where $\mu_{i}$ is an added parameter that denotes the a priori probability of the $i^{\text {th }}$ source in the considered frequency band. This parameter reveals necessary since all sources are not equiprobable in a given frequency band, depending for instance on the mean pitch of a person. Simulations with equiprobable hypothesis showed that the estimation of the model parameters $\rho$ and $\boldsymbol{r}$ is biased, hence producing degraded performance in terms of source separation.

### 2.3 Soft mask separation

The set of parameters $\boldsymbol{\rho}, \boldsymbol{r}$ and $\boldsymbol{\mu}$, which depend on the frequency band $\omega$, are the parameters of the mixture model and need to be estimated in order to separate the sources. Once the parameters of the probabilistic model given in (6) are estimated, the a posteriori probability that $i^{\text {th }}$ source is dominant at the TF point $(t, \omega)$ can be obtained directly as follows:

$$
\begin{equation*}
\pi_{i}(t)=\frac{\mu_{i} p_{\rho_{i}}\left[\log \left|R_{i}(t)\right|, \arg R_{i}(t)\right]}{\sum_{q=1}^{N} \mu_{q} p_{\rho_{q}}\left[\log \left|R_{q}(t)\right|, \arg R_{q}(t)\right]} \tag{7}
\end{equation*}
$$

where $R_{i}(t)=R(t) / r_{i}$. Then, source separation can be easily performed in each frequency band $\omega$ by applying these above probabilities to the observations. Note that sources are independently separated in each frequency band, thus permutation ambiguity remains and needs to be solved. In this paper, the correlation between the ratio envelope is used as in [5]. Note that other methods, based on linear phase assumption [6], can not be used due to reverberation. Fig. 2 shows the flow chart of the Model Based Source Separation approach where $M_{i}(t, \omega)$ refer to the masks that extract the $i^{\text {th }}$ source. $M_{i}(t, \omega)$ is constructed from the a posteriori probabilities (7) after correcting the permutation ambiguities. Thus, $M_{i}(t, \omega)=\pi_{\Pi_{\omega}(i)}$ with $\Pi_{\omega}=\left[\Pi_{\omega}(1), \ldots, \Pi_{\omega}(N)\right]$


Figure 2: Basic scheme of Model Based Source Separation Approach
the permutation alignment vector estimated by [5] in the frequency band $\omega$.

As said before, to build the soft separating mask, the $\mu_{i}, r_{i}$, and $\rho_{i}$ parameters need to be estimated for each source at each frequency band $\omega$. To do so, we propose to use as criterion the maximum of the log-likelihood of the data $\{\log |R(t)|, \arg R(t)\}, t \in T$. Under the independence assumption between the time set of observations, it is given by:
$L(\boldsymbol{\rho}, \boldsymbol{r}, \boldsymbol{\mu})=\sum_{t \in T} \log \left\{\sum_{i=1}^{N} \pi_{i} p_{\rho_{i}}\left[\log \left|R_{i}(t)\right|, \arg R_{i}(t)\right]\right\}$.
The above log-likelihood is hard to maximize. However, it may be recasted as the log-likelihood for a model with missing observations or hidden variables. These variables are the indexes that indicate which source is dominant at each $(t, \omega)$ point (here $\omega$ is fixed and hence not displayed). In this context the log-likelihood can be maximized by the well known Expectation Maximization (EM) algorithm [7].

## 3. THE EM ALGORITHM

This algorithm operates in two steps as described below.

### 3.1 The E-step

This step computes the conditional expectation of the full $\log$-likelihood given the data $\{\log |R(t)|, \arg R(t)\}, t \in T$. The expected log-likelihood will be computed at generic new parameters $\mu_{i}^{\prime}, r_{i}^{\prime}$ and $\rho_{i}^{\prime}$ and the conditional expectation is computed relatively to the model specified by the current parameters $\mu_{i}, r_{i}$ and $\rho_{i}$. The result can be shown to be:

$$
\begin{equation*}
\sum_{t \in T} \sum_{i=1}^{N} \pi_{i}(t) \log \left\{\mu_{i}^{\prime} p_{\rho_{i}^{\prime}}\left[\log \left|\frac{R(t)}{r_{i}^{\prime}}\right|, \arg \frac{R(t)}{r_{i}^{\prime}}\right]\right\} \tag{9}
\end{equation*}
$$

where $\pi_{i}(t)$ is the a posteriori probability given in (7) and computed at the current parameter $\mu_{i}, r_{i}$ and $\rho_{i}$.

### 3.2 The M-step

This step maximizes the above conditional expectation of the full $\log$-likelihood with respect to the generic parameters $\mu_{i}^{\prime}$, $r_{i}^{\prime}$ and $\rho_{i}^{\prime}$. The maximum point is then taken as the new parameter. It is easily seen that the maximization of (9) with respect to $\mu_{i}^{\prime}$ (under the constraint $\sum_{i=1}^{N} \mu_{i}^{\prime}=1$ ) and with respect to the set $\left(r_{i}^{\prime}, \rho_{i}^{\prime}\right)$ can be performed independently. The first maximization yields the new $\mu_{i}: \mu_{i}=\sum_{t \in T}\left[\pi_{i}(t)\right] /|T|$
where $|T|$ denotes the number of points in $T$. The second one is reduced to the maximization of:

$$
\begin{equation*}
C\left(r_{i}^{\prime}, \rho_{i}^{\prime}\right)=\sum_{t \in T} \pi_{i}(t) \log p_{\rho_{i}^{\prime}}\left[\log \left|\frac{R(t)}{r_{i}^{\prime}}\right|, \arg \frac{R(t)}{r_{i}^{\prime}}\right] \tag{10}
\end{equation*}
$$

for each $i=1, . ., N$ with respect to $r_{i}^{\prime}$ and $\rho_{i}^{\prime}$.

### 3.3 Relaxing the M-step

Maximizing the above expression (10) is not easy and can not be done without using an iterative algorithm. In [8], we overcome this problem by replacing the theoretical density (5) in (10) with another similar and easier one to handle. Thus, we were able to maximize it analytically. In this work, as the theoretical density shall be used, we propose not to maximize the expected full log-likelihood (10) but to just make it increase. In fact, from the EM algorithm theory, increasing the expected likelihood (10) would be sufficient to increase, also, the marginal likelihood (8). Therefore, given the current parameters $r_{i}$ and $\rho_{i}$, we limit ourselves to finding the new parameters $r_{i}^{\prime}$ and $\rho_{i}^{\prime}$ that increase the objective function (10). Such new parameters can indeed be found analytically as described in the following basic step:

### 3.3.1 Basic step

Using Jensen's inequality, it can be easily proved that $C\left(r_{i}^{\prime}, \rho_{i}^{\prime}\right)-C\left(r_{i}, \rho_{i}\right)$ has the following lower bound:

$$
\begin{equation*}
-2 \zeta \log \sum_{t} \frac{w_{i}(t)\left\{\cosh \left[\xi_{i}(t)-\lambda_{i}\right]-\rho_{i}^{\prime} \cos \left[\phi_{i}(t)-\theta_{i}\right]\right\}}{\zeta\left(1-\rho_{i}^{\prime 2}\right)^{1 / 2} /\left(1-\rho_{i}^{2}\right)^{1 / 2}} \tag{11}
\end{equation*}
$$

where

$$
\begin{aligned}
w_{i}(t) & =\frac{\pi_{i}(t)}{\cosh \left[\log \left|R_{i}(t)\right|\right]-\rho \cos \left[\arg R_{i}(t)\right]} \\
& =\frac{2\left|R_{i}(t)\right| \pi_{i}(t)}{\left|R_{i}(t)\right|^{2}+1-2 \rho \Re\left[R_{i}(t)\right]}
\end{aligned}
$$

and $\zeta=\sum_{u} \pi_{i}(u), \xi_{i}(t)=\log \left|R_{i}(t)\right|, \lambda_{i}=\log \left|r_{i}^{\prime} / r_{i}\right|$, $\phi_{i}(t)=\arg R_{i}(t), \theta_{i}=\arg \left(r_{i}^{\prime} / r_{i}\right)$ and $\Re(z)$ is the real part of the complex number $z$. The maximum of the above equation (11), with respect to $\left(r_{i}^{\prime}, \rho_{i}^{\prime}\right)$, is strictly larger than zero (because it is equal to zero when $\left.\left(r_{i}^{\prime}, \rho_{i}^{\prime}\right)=\left(r_{i}, \rho_{i}\right)\right)$. Thus, the new couple ( $r_{i}^{\prime}, \rho_{i}^{\prime}$ ) that maximizes (11) will increase, at the same time, the objective function (10). Therefore, by a simple variable substitution, the problem of increasing the likelihood is now reduced to maximize (11) with respect to

|  |  | 4 Men Speech |  |  |  |  | 4 Women Speech |  |  |  |  | 3 Music, No drums |  |  |  | 3 Music, with drums |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | S1 | S2 | S3 | S4 | Mean | S1 | S2 | S3 | S4 | Mean | S1 | S2 | S3 | Mean | S1 | S2 | S3 | Mean | OVAP |
|  | SDR | 3,91 | 2,68 | 3,71 | 4,17 | 3,61 | 4,46 | 3,40 | 4,37 | 5,27 | 4,37 | 2,42 | 5,80 | 4,81 | 4,34 | 1,65 | 3,49 | 0,35 | 1,83 | 3,61 |
| new | ISR | 6,17 | 5,99 | 6,52 | 6,87 | 6,39 | 6,58 | 7,28 | 7,07 | 7,52 | 7,11 | 4,27 | 8,61 | 8,61 | 7,16 | 1,76 | 6,38 | 0,40 | 2,85 | 6,00 |
| MBUSS | SIR | 5,75 | 2,62 | 5,37 | 6,89 | 5,16 | 6,75 | 3,45 | 6,77 | 10,13 | 6,78 | 4,07 | 8,80 | 6,57 | 6,48 | 13,38 | 6,15 | 11,88 | 10,47 | 7,04 |
|  | SAR | 6,21 | 5,52 | 6,19 | 6,08 | 6,00 | 7,78 | 7,44 | 6,82 | 7,72 | 7,44 | 5,50 | 11,24 | 8,96 | 8,56 | 15,90 | 9,73 | 7,56 | 11,06 | 8,05 |
|  | SDR | 3,25 | 1,97 | 3,69 | 4,11 | 3,25 | 4,43 | 3,84 | 4,44 | 5,50 | 4,55 | 1,69 | 5,87 | 5,19 | 4,25 | 1,64 | 3,02 | 0,34 | 1,67 | 3,50 |
| MBU | ISR | 6,14 | 4,17 | 6,87 | 7,21 | 6,10 | 6,34 | 8,03 | 7,89 | 8,65 | 7,73 | 4,31 | 8,30 | 10,50 | 7,70 | 1,80 | 7,16 | 0,42 | 3,12 | 6,27 |
| [8] | SIR | 3,73 | 2,21 | 5,20 | 6,27 | 4,35 | 8,45 | 5,35 | 7,24 | 9,53 | 7,64 | 3,15 | 9,78 | 7,15 | 6,69 | 14,85 | 6,94 | 11,94 | 11,24 | 7,27 |
| [8 | SAR | 5,99 | 5,04 | 6,25 | 6,17 | 5,86 | 6,78 | 6,95 | 6,68 | 7,29 | 6,93 | 5,60 | 11,26 | 9,00 | 8,62 | 11,59 | 6,09 | 6,01 | 7,89 | 7,19 |
|  | SDR | 3,50 | 2,24 | 3,16 | 3,57 | 3,12 | 4,03 | 3,10 | 3,77 | 5,22 | 4,03 | 1,82 | 5,58 | 5,15 | 4,19 | 1,72 | 4,62 | 0,36 | 2,23 | 3,42 |
| Kmeans | ISR | 7,64 | 5,90 | 7,38 | 8,65 | 7,39 | 6,16 | 10,55 | 9,20 | 10,06 | 8,99 | 5,29 | 8,00 | 10,28 | 7,86 | 1,82 | 8,75 | 0,42 | 3,66 | 7,15 |
| [3] | SIR | 7,01 | 4,62 | 6,36 | 7,08 | 6,27 | 12,51 | 5,52 | 8,04 | 9,81 | 8,97 | 4,13 | 8,49 | 7,05 | 6,55 | 14,73 | 7,77 | 13,68 | 12,06 | 8,34 |
|  | SAR | 4,58 | 2,40 | 4,24 | 4,54 | 3,94 | 4,69 | 5,65 | 5,53 | 6,31 | 5,54 | 7,34 | 11,27 | 9,68 | 9,43 | 16,26 | 10,92 | 7,75 | 11,64 | 7,22 |

Table 1: Results for synthetic recording with a 5 cm microphone spacing and two different types of sources: speech and music. the overall performance OVAP of the source separation is presented in the last column. All figures are given in dBs
$\theta_{i}, \lambda_{i}, \rho_{i}^{\prime}$. By developing the numerator terms $\cosh \left[\xi_{i}(t)-\lambda_{i}\right]$ and $\cos \left[\phi_{i}(t)-\theta_{i}\right]$, the maximum is obtained when

$$
\begin{aligned}
\lambda_{i} & =\tanh ^{-1} \frac{\sum_{t} w_{i}(t) \sinh \xi_{i}(t)}{\sum_{t} w_{i}(t) \cosh \xi_{i}(t)} \\
\theta_{i} & =\arg \sum_{t} w_{i}(t) \operatorname{sign}\left\{R_{i}(t)\right\} \\
\rho_{i}^{\prime 2} & =\frac{\left[\sum_{t} w_{i}(t) \cos \phi_{i}(t)\right]^{2}+\left[\sum_{t} w_{i}(t) \sin \phi_{i}(t)\right]^{2}}{\left[\sum_{t} w_{i}(t) \cosh \xi_{i}(t)\right]^{2}-\left[\sum_{t} w_{i}(t) \sinh \xi_{i}(t)\right]^{2}}
\end{aligned}
$$

where $\operatorname{sign}\{z\}=z /|z|=e^{i \arg z}$. Finally, to increase (10), we are led to assume the following one iteration basic step:

$$
r_{i} \leftarrow r_{i} \sqrt{a_{i} / b_{i}} \operatorname{sign} c_{i}, \quad \rho_{i} \leftarrow\left|c_{i}\right| / \sqrt{a_{i} b_{i}}
$$

where $a_{i}=\sum_{t} \chi_{i}(t)\left|R_{i}(t)\right|^{2}, b_{i}=\sum_{t} \chi_{i}(t)$, and $c_{i}=$ $\sum_{t} \chi_{i}(t) R_{i}(t)$ with $\chi_{i}(t)=\frac{1}{2} w_{i}(t) /\left|R_{i}(t)\right|$.

### 3.3.2 Combining with the Quasi Newton step

The basic step could lead to a slower convergence of the algorithm as the obtained increase of the expected log-likelihood (10) can be much less than the maximum achievable. To overcome this problem we will consider a Quasi-Newton (Q$\mathrm{N})$ algorithm. In fact, when the old parameter $r_{i}$ and $\rho_{i}$ are close to the maximum solution of (10), the Quasi-Newton algorithm would have a quadratic convergence to the point maximizing (10). Therefore, the algorithm should converge within one single Q-N iteration. However, in contrast to the basic step, the Q-N step does not guarantee the increase of the expected log-likelihood. It does not even guarantee the new $\rho_{i}^{\prime}$ to be in the interval $(0,1)$. Thus, the following strategy is adopted in the M-step:

- Compute the new parameter $\rho_{i}^{\prime}$ and $r_{i}^{\prime}$ based on the basic step as in section 3.3.1
- Compute the other new estimation of $\hat{\rho}_{i}^{\prime}$ of the $\mathrm{Q}-\mathrm{N}$ step and test if it belongs to the interval $(0,1)$
- If not, adopt the new parameter $\rho_{i}^{\prime}$ and $r_{i}^{\prime}$ of the basic step, otherwise compute the other new parameter $\hat{r}_{i}^{\prime}$ of the Q-N step and test if it and $\hat{\rho}_{i}^{\prime}$ of the Q-N step lead to a larger increase of the expected log-likelihood than the basic step; if so, adopt these parameter $\hat{r}_{i}^{\prime}$ and $\hat{\rho}_{i}^{\prime}$ otherwise adopt those of the basic step $\rho_{i}^{\prime}$ and $r_{i}^{\prime}$.
Computations (not detailed here) show that the Q-N step is given by:

$$
\begin{aligned}
\hat{\rho}_{i}^{\prime} & =\rho_{i}-\frac{\rho_{i}\left(a_{i}+b_{i}\right)-2 \Re\left(c_{i}\right)}{\sum_{t} \chi^{2}(t)\left\{\left[\left|R_{i}(t)\right|^{2}+1\right]^{2}-4 \Re\left[R_{i}(t)\right]^{2}\right\} / \pi_{i}(t)} \\
\hat{r}_{i}^{\prime} & =r_{i} \exp \left[(3 / 2)\left(a_{i}+b_{i}\right) /\left(a_{i}-b_{i}\right)\right] \operatorname{sign}\left[3 c_{i}-\Re\left(c_{i}\right)\right]
\end{aligned}
$$

Note that these formula involve the already computed quantities $a_{i}, b_{i}, c_{i}$.

### 3.4 EM Initialization and Stop Criteria

A simple way to initialize our algorithm is to choose randomly N times points $t_{1}, . ., t_{N}$ and initialize $r_{i}$ by $r_{i}=R\left(t_{i}\right)$, $i=1 . . N$. The a posteriori probability $\pi_{i}(t)$ can be initialized by formula (7) using the density (5) with $\rho_{i}$ set to one, leading to:

$$
\pi_{i}(t)=\frac{d\left[R(t), r_{i}\right]}{\sum_{i=1}^{N} d\left[R(t), r_{i}\right]}
$$

where $d\left[R(t), r_{i}\right]=\cosh \log \left[R(t) / r_{i}\right]-\cos \arg \left[R(t) / r_{i}\right]$. Since the log-likelihood increases monotonically at each EM iteration, the EM iteration process is stopped when the increase of log-likelihood becomes insignificant(e.g $\left.10^{-6}\right)$.

## 4. EXPERIMENTS AND RESULTS

In order to evaluate our algorithm, we simulated speech and music mixtures in a reverberant noise-free environment by convolving speech and music samples with filter impulse responses coming from the first audio source separation campaign [2]. Also, it was recently tested in the Signal Separation Evaluation Campaign (SiSEC) [10] where results showed that our algorithm compares favorably with the others presented in this campaign in most of the real and synthetic convolutive situation. As these results can be accessed at [10], only the results for the first audio source separation campaign will be presented. Signals are 16 kHz -sampled and have a 10 s duration. Four types of mixtures were generated: 4 female speakers, 4 male speakers, 3 musics with one of them is drums and 3 other musics (no drums). Two different sets of source positions are used, one for speech and another for music mixtures. Angles and distances of these positions are given in Table 2. Our algorithm uses Hanning windowed 2048 sample frames, and reconstruction is achieved using the overlap and add method with $75 \%$ overlap.

|  | Speech Sources |  |  |  | Music Sources |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | S1 | S2 | S3 | S4 | M1 | M2 | M3 |
| Distance (m) | 1,2 | 1,1 | 1 | 0,8 | 1,1 | 0,9 | 1 |
| Angle (deg) | 50 | -15 | -45 | 15 | 45 | -30 | 5 |

Table 2: Source positions from the set of microphone

### 4.1 Comparison Algorithm and performance measurement

The proposed algorithm (referred to as new MBUS) is compared with two other algorithms: the first one (referred to
as old MBUS) is our previous method based on the same model-based EM approach, but with a simplifying probability distribution of the couple of variable (IPD, $\log (\mathrm{ILD})$ ) [8]. The second one (referred to as Kmeans) is the KMeans underdetermined source separation presented in [3], in which the ILD/IPD observations are grouped into $N$ clusters using a KMeans algorithm: each cluster center gives an estimation of the mixing matrix and the cluster point sets give the binary TF separating masks. The separation performance was evaluated for each estimated source $i$ by the same criteria used in SiSEC: Signal to Interference Ratio $\left(\mathrm{SIR}_{i}\right)$, Image to Signal Ratio ( $\mathrm{ISR}_{i}$ ), Signal to Distortion Ratio $\left(\mathrm{SDR}_{i}\right)$ and Signal to Artifact Ratio $\left(\mathrm{SAR}_{i}\right)$. For a detail description of these criteria and of their computation, the reader may refer to [10].

### 4.2 Results

Detailed performance are given in Table 1 whereas the mean of each case and the overall performance OVAP (mean performance on all mixture types) are plotted in Figure 3. When looking at the SDR which computes the global separation performance, OVAP column, the proposed MBUSS gives the best results as compared to the others. It shows a slight advantage for the new MBUSS 3.61 dB compared to the old one 3.5 dB and a more efficient as compared to KMeans 3.42 dB . Furthermore, the intermediate errors show that the compromise operated by the algorithms is different.

Comparing the new MBUSS to the old one, results show that the proposed algorithm gives better results in terms of SAR (SAR $=8.05$ and 7.19 respectively) and, almost, the same in terms of SIR (SIR=7.04 and 7.27 respectively), which justifies the use of the theoretical distribution and not the approximated one as in [8]. Comparing the new MBUSS with the KMeans, Fig. 3 (a),(b) and (c) show that the MBUSS method performs better for speech mixture, whereas KMeans performs better on music ones. One explanation could lie in the nature of the signal themselves: music sources are very resonant, hence the energy is highly concentrated on some (usually harmonic) frequencies, which ensures a quasi-disjoint spectro-temporal supports between instruments. Thus, hard masking would be more suitable filter for this type of mixtures than a soft filter. The OVAP on Fig. 3 (d) also shows that the KMeans algorithm favors weak interferences $(\operatorname{SIR}=8.34)$ to the cost of more degraded separated speech ( $\mathrm{SAR}=7.22$ ), in contrast to our method that presents stronger interference $(\operatorname{SIR}=7.04)$ but with a clearer separated speech signal ( $\mathrm{SAR}=8.05$ ).

These results are confirmed by informal listening tests: less audible artifact are noticed in the proposed MBUSS, at the expense of more interference, which reveals nicer to listen to since our auditory system is very sensitive to artifact (gurgling noise) and less to interference. One explanation (partially) lies in the nature of the mask: as compared to the binary mask used in the KMeans method, the soft mask slightly smooths the output, limiting the isolated errors (the artifact like musical noise), but favoring the presence of interference.Note that the mask is used "as is": we are inclined to think that some "wise" smoothing (linear or nonlinear) could give better objective and subjective results, reducing even more the artifact.

## 5. CONCLUSION

In this paper, a new method to solve the underdetermined blind separation of audio mixtures problem has been presented. It is based on the sparseness assumption and on a theoretical model for the interchannel cues (log(ILD),IPD) given in [1]. By an EM algorithm, we were able to estimate the parameters of this model and then build the time frequency separating masks. The algorithm demonstrated its


Figure 3: (a),(b),(c) presents respectively the SDR, SAR and SIR performance for each type of mixture; (d) presents the OVAP
ability to separate undetermined reverberant mixtures where in terms of objective criteria it gives the best results in terms of artifact and distortion. Nevertheless, more studies need to be done, especially on the robustness of the model over the source positions and room reverberation.

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