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Performance Evaluation of Automatically Generated Data-Parallel Programs

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Abstract

In this paper- the problem of evaluating the perfor mance of parallel programs generated by data-parallel compilers is studied. These compilers take as input an application written in a sequential language aug mented with data distribution directives and produce a paral based on the species partition of the species partition of the species of the species of the species of t $data.$

A methodology for evaluating the relationships ex isting among the program characteristics- the data dis tribution adopted- and the performance indices mea sured during the program execution is described. It consists of three phases: a "static" description of the program under study- underweise verschiption-, tweed on the measurement and the analysis of its execution on a real system, when the sensor wenters of a working the construction of a workload model- by using workload characterization techniques Fol lowing such a methodology- decisions related to the selection of the data distribution to be adopted can be facilitated

The approach is exposed through the use of the Pana dore environment and executive for the execution of security quential programs on distributed memory parallel computers It is composed of a compiler, a runtime system. The present and tools for trace and profile generation. The results of an experiment explaining the methodology are pre sented

$\mathbf 1$ Introduction

Performance evaluation activities are required in many studies- involving the design and the tuning of α system-parameter as the debugging of its performance α Whatever is the ob jective of the study- the workloadthat is the set of programs submitted to the system-s one of the major components which determine system performance-that strict relationships exist between the strict relationships exist between the strict between \mathbb{R}^n the obtained performance and the hardware and soft

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> ware components of the system itself. Workload characterization is the basis of every performance evalua tion study-provides systematic methods systematic methods for the systematic methods for the systematic method a quantitative description of the load which which which are the load which and the load which are the load which with the systems are contracted as per coupled as performed as of the performance

In parallel environments- in particular- the perfor mance evaluation process is more crucial and difficult than in sequential ones. The analysis and characterization of the workload in parallel systems require special care because of their complex architectures, the large number of hardware and software compo \sim and the new programming paradigm \sim adopted

 i ed partitioning of data eg -
 and the property that problem problem of evaluations and problem of the ing the performance of parallel programs generated by data-parallel compilers. Such compilers that takes as input an application written in a sequential language augmented with data distribution directives like HPF and produce a parallel version-species on the species α

The "parallelizing" compiler represents one of the most important system's software component influencing the program execution \mathbf{f} the compact \mathbf{f} the compact \mathbf{f} the compact \mathbf{f} and $\$ piler manages in a transparent way code distributiondata distribution and communication among tasks, the parallelization decisions are definitively left to the user who specifies the partitioning of the data and their mapping onto the available processors These factors highly influence the performance attained by the system

The paper is organized as follows In Sect 2000 to the section of \sim motivations for such a study and the problems re lated to the selection of the appropriate data distri bution are presented. A methodology for the evaluation of the relationships existing between the work load characteristics and the obtained performance is

proposed in Section 1, the environment was the environment used for the section of \mathcal{L} tomatic generation of data parallel programs is briefly described to the providing to the p measurements of the program execution. Finally, an experiment showing the feasibility of the approach is presented in Sect

$\bf{2}$ Performance Evaluation of Data Parallel Programs

From the performance point of view- the ma jor characteristic of a data parallel program is the de pendence of the obtained performance from the spec is definite data distribution-distribution-distribution-distribution-distribution-distribution-distribution-distribution-distribution-distribution-distribution-distribution-distribution-distribution-distribution-distribut as well as communication activities Optimal system performance is obtained by balancing the computation activity among different processors but also by minimizing communication trac- and achieving a large degree of parallelism

As already pointed out- the user is still responsible for decisions related to data distribution Hence- due to the large number of distributions available and to the number of parameters aecting such decisions- an help in selecting the appropriate data decomposition which maximizes performance has emerged as an es sential requirement. This help can benefit to the user, who as the distribution of the distribution of the distribution of the distribution \mathcal{S} development of automatic data management in paral lelizing the sees of the compilers of the c

2.1 Methodology

Generally-controlled on the objective of the study of and on the availability of the system-problem and the systems of the system ods can be applied for performance evaluation [11]. They range from the construction of models having an analytical solution-between \mathcal{A} solution-between \mathcal{A} els- to measurement based approaches The ma jor benefit in using performance modeling is when measurements are not available-relieved and the performance of the performance of \sim mance prediction studies or during design activities A number of studies have been done in the frame work of data-parallel compilers to statically estimate the performance of the generated parallel programs . Also in this case-time and the case-time and the case-time and the case-time and this case-time and the caseperformance measurement activity is required in order to test if the model is realistic-to-model is realistic-to-model is realistic-to-model in the validity the validity the validity of the validi of the parameterization of the model and to drive its input

when the system is available-to-control to the system is available-to-control tostudy is generally carried out; measurements represent the basis for the workload characterization process $s = 1$ and performances the performances of the performances of $s = 1$ of the real system are obtained: they contain also the influence of hardware and software components which would be otherwise difficult to capture even in a very

and terms are the measurement based approach make a measurement based approach make a measurement based approach detailed model. When dealing with programs generated by a particularity completely and particularly many are the decisions to be taken and the factors which in particularly suitable

> Thus- the approach that we propose is based on var ious statistical analyses of the data measured during the program execution. The aim is to relate the program characteristics with that of the data partition ing and mapping- in order to optimize performance The phases have been identified from the programmer in the p under study can be statically described by means of a few parameters the few parameters the descriptionbased on the measurement and the analysis of its ex ecution on a real system is obtained Finally-induced Finallyload characterization techniques are applied to the ob tained workload for constructing a model In what follows- the three phases are described in more detail

By statically analyzing the program structure- a workload description in terms of parameters that can affect the choice of the data distribution can be obtained. The attention has been focused on DO loops, and on array data structures-because the most part of the most part of the most part of the most part of the m scientific codes are based on loops working on data arrays- and the ma jor part of the parallelism inherent in an application residence in the matrix of the matrix of the matrix of the matrix of them Indeedhas to be generated especially for such structures; they form also the major source of performance degradation in numerical applications- due to communication

Parameters which are strictly related to the loop structure- and others which characterizes the whole the whole program have been detected as an example-of-control as an example-of-control as an example-of-control as an examplecan be defined by the size of each of the referenced arrays- by the order of the index in the nested loopsand by the depth of the loop. The selected data distribution- which can be identified by the size of blocks into which the data structures are partitioned, and the mapping strategy adopted are other parame ters characterizing the program Finally- the number of allocated processors can be chosen as a parameter reflecting the influence of the system hardware configuration

Note that the parameter selection is a critical point, in that they have to accurately describe the program characteristics

Once the program under study has been defined according to some of the previously described param eters- the second phase deals with the measurement and the analysis of its execution on a real architecture appropriate the trace the program executions of the propriate the second monitoring instrumentation is required see - Very low level data- related for example to the start and to the end of an event-to-the end of an event-to-the end of an event-to-the end of an event-to-the end of a tools and collected into trace files. The generally huge amount of data obtained makes them difficult to interprett and this point, if pre-laboration phase is needed at \sim recent in order to derive a more intuitive and compact de scription of the program behavior. Starting from measurements collected by the monitoring tools-by the monitoring tools-by the monitoring tools-by the monitoring toolshigherlevel parameters are identically described by the contract of the contra behavior of the program in terms of computation and communication activities Such parameters Such parameters dealexample-the number of messages exchanges exchanges exchanges the number of messages exchanges and the number of messages of the number of execution- computation and communication times

At the end of these two phases- the whole program execution can globally be represented by a set of n parameters-that is-the is-those related to its static structure in the static structure of the static structure and to the system condition-internal mass restricts restricting $\mathbf{q} = \mathbf{q}$ its dynamics definitions and is-

Each execution of the program is a workload com ponent-be represented as a point in a new point in a new dimensional space of the workload processed processed processed processed processed processed processed proces by the system is constituted by a collection of work load components- obtained varying the values of the parameters for example, the dimension of the dimension of the dimension of \mathcal{A} the blocks into which data have been distributed and the property of the state of \mathbb{R}^n mapping policy- or the problem dimension

The aim and the core of the methodology-the methodology-the methodology-the methodology-the methodology-the methodologypoint-the workload-that is to construct a model of the workload-that is-dea compact representation able to capture and repro duce the behavior of the system. Workload characterization techniques have to be applied- so that typi cal" behaviors of the program can be identified; multidimensional analysis techniques are required for this purpose A description of the techniques applied for workload characterization is presented in the next sec tion

2.2 Workload Characterization

The characteristics of the workload have to be stud ied by applying different statistical analyses. A complete description of workload characterization tech niques applied to performance evaluation studies of various system architectures-in - can be found in - can be found in - and -

The idea in our study is to find relationships among the system contains the system contains the system of the syst achieved performance

In order to reduce the number of parameters- and thus the complexity of the analysis- the correlation among

the parameters can be analyzed. The correlation matrix helps in selecting the most appropriate parame ters by expressing the dependencies among them a correlation index between two parameters close to one reflects an equivalent behavior. Just one parameter amongst the highly correlated parameters can then be considered for the description of the application of the application of the applicationreducing the dimension of the n -dimensional space.

clustering clustering and the set of the second very important the second second second and set of the second tant for the identification of workload components having similar behavior- and is most commonly ap plied to the workload characterization problem

The workload is considered as a set of points compo nents) in a space with a number of dimensions equal to the number of parameters used to describe each com ponent

Clustering algorithms partition the workload into clus ters-terms-components with similar characteristics with similar characteristics with similar characteristics w belong to the same cluster. These algorithms have to identify the partition which better represents the char acteristics of the original measurements The good ness of a partition is given by an optimality measure, based on a selected metric-type the electron part that a selectron

Then- according to some speci ed criteria- a few com ponents are extracted from every cluster and are con sidered as the representatives of the measured work load The centroid-centroid-centroid-centroid-centroid-center of Λ the clusters of the chosen and chosen all chosen and chosen and chosen and chosen and chosen and chosen and chos

The partitioning of the workload means that "typical" behaviors can be identified among the various program executions. This gives the possibility to relate the static parameters describing the program and the system contains the system contains the dynamic ones-with the dynamic ones-with the dynamic ones-with the dynamic onesis- with the performance indices Centroids represent a model of the workers and model is the static control to the static control of the static \mathbf{r} the program has been chosen-ch sponding performance indices can be "expected".

Furthermore- clustering algorithms provide an analysis of the behavior of the components belonging to a cluster Basic statistics, such as minimum-statistics, as minimumimum- average values and standard deviation give a first idea of the "average" behavior of the program. For example- when considering parameters related to communication activities- and the very high value of the very station-deviation-compared with the mean valueis a synonym of variabilities This means that unbal anced conditions due to uneven work or data distribu tion are detected

In Section of our methodology is a section of our methodology is a section of our methodology is a section of o

described through a test example

In the following section- the environment used for par allelizing the program and for monitoring its execution is presented

The Pandore Environment

PANDORE is an environment designed for the execution of sequential programs on distributed memory parallel computers $[1]$. It is composed of a compiler, a runtime system and tools for trace and profile generation

3.1 The Language

The PANDORE language is based on a sequential imperative language using a subset of C excluding pointers) as a basis. We have added a small set of simple and well-defined data distribution features in order to describe frequently used decompositions

A PANDORE program is a sequential program which calls distributed phases. The sequential part is in charge of all I/O operations and is executed on the host processor if exists or on one speci c node of the distributed computer. Each distributed phase is spread over the processors of the target machine and is executed in parallel according to the owner-writes

Distributed phases are declared like procedures pre ceded by the keyword dist To each formal parame ter of the distributed phase is assigned a distribution The distributed parameter list allows the specification of the partitioning and the mapping of the data used in the distributed phase

The array is the only data type that may be par tition are replicated the means to decomposition to decomposition and means to determine the means of the mean pose an array is to split it into blocks. The specification of the partitioning for a d -dimensional array is $\mathbb{R}^{r \times r}$ on construct block $\mathbb{R}^{r \times r}$ to the time time that $\mathbb{R}^{r \times r}$ cates the size of the blocks in the $i^{\,\cdots\,}$ dimension.

Then- the mapping of the blocks onto the architec ture will be achieved in a regular or cyclic way accord ing to the mapping parameters regular or wrapped In Pandore- we consider only one dimensional pro cessor arrays whose size is not specified in the source code but used as a parameter by the compiler. As we allow the mapping of multidimensional decompo sitions, it is needed to indicate the map the map the map order \mathcal{C} ping of blocks by providing an ordered list of dimen sion instance-of-columnation-column instance-of-column instance-of-column instancerst-states for row of row control to the state of the state

The last specification given in the parameter list concerns the transfer mode for values between the caller and the distributed phase allowed modes are IN- OUT and INOUT This speci cation is similar to the one found in Ada or Fortran

For example the formal parameter declaration

int A-N-N by blockN map wrapped mode INOUT

states that array A is decomposed into N lines mapped cyclically onto the processors The value of the ele ments of the array must be transferred from the host at the beginning of the distributed phase and must be sent back to it at the end of the phase

3.2 The Compiler and the Runtime Sys

From the source program- the Pandore compiler automatically generates a machine independent SPMD code according to the owner-writes rule: a processor modifies only the variables that have been assigned to it by the distribution specification.

Two compilation schemes are embedded in the com piler For reductions and parallel loops- the com piler applies an optimized scheme $[14]$ performing loop bounds reduction and message vectorization- based on static domain analysis. For statements that cannot be optimized and compiler relies on the well well and the well well as time resolution technique: masks and communication operations are introduced at the statement level to fetch distant data and select the processor responsible for the computation

An original distributed array management based on paging [15] has been developed to support both schemes. Each block of a distributed array is decomposed into pages so that the array is represented on a processor by a table of pages that contains both lo cal pages pages of the blocks owned by the processor and distant pages copies of pages owned by other pro cessors). Such a management leads to both efficient accesses and reasonable memory overhead

The code generated by the compiler is a SPMD C code containing calls to the runtime system The goal of the runtime system is to implement memory and process management, communication of data elements of data elements between processes- and distributed data accesses It is build upon a virtual machine that permits the execu tion of PANDORE programs on a wide range of parallel platforms

3.3 The Pandore Profiler

The PANDORE profiler allows the user to collect a number of quantitative measures on his program's execution with minimal intervention It may be com plemented by a trace generator for more qualitative measurements $[3]$. The use of profiling restrains the amount of storage needed; the number of counters to be updated is of the order of the number of variables declared in the source program. Sensors are inserted in modies of some runtime primitives- the some runtime primitives- the some runtime primitives- thus the some

the compiler generates a similar code whether an in strumentation is demanded or not. An enhancement of mere profiling is actually used: in addition to their occurrences-durations may also be currences-durations may also be currences may also be currences may also be mulated [13]. Measurements are performed on each node and counters are brought back to the host at the end of the execution and then written down into a file that can be exploited by appropriate tools

The links between the source and the evaluation results are established two different ways: first the user bounds fragments of the distributed phases he wants to be evaluated by defining some *instrumenta*tion zones-benefits and the second control of the second of the second control of the seco ures are associated with ob jects of the source program such as arrays- scalars or conditional statements

Twelve types of information are available that can be divided in two categories

Information relative to each instrumentation zone

For each distributed variable v and each couple α processors $\{P_1, P_2\}$, and manneer of messages from p to p-2 required for the assignment of value \sim is computed as well as the corresponding volume transferred and the cumulated waiting time on p- Identical information is collected for broad cast messages due to assignments to replicated scalars and due to the evaluation of conditional expressions

For the entire zone- the number of local accesses to a distributed array element and the number of accesses that required communication is com puted for each processor Identically- the number of purely local assignments and the number of as signments that required distant data is reported

The execution time for the zone is also given

Information relative to each distributed phase

For each distributed variable- the time spent re ceiving the corresponding initial value from the host is reported for each processor. The waiting part of this time is also given

Different times are measured globally for the phase the time for the triggering of the phase by the time for the time for the time for the time \mathcal{L}_1 from the time for time for time for \mathbf{f} the state time for executing the state time for executing the state \mathbf{f} ments of the phase and the time for transferring OUT variables back to the host

$\overline{4}$ Experiments

In order to test the feasibility of the proposed methodology- a few experiments have been carried out based on data obtained using the profiler integrated

into the Pandore environment- described in the pre vious section. An $iPSC/2$ with 32 nodes has been chosen as target architecture As a test program-Jacobi algorithm has been considered see Fig Following the methodology presented in Sect. 2.1 raw data collected by the problem and collected between \mathcal{D} applying various statistical techniques

The algorithm has been statically described as fol lows the size of the array Size has been chosen for the designation of the stap, which the modern of the number cated processors and the number of blocks and the number of blocks and the number of blocks and the number of b into which the array are partitioned represent the data distribution policy

Different runs of the algorithm have been executed, and monitored using the Pandore produce the Pandore ing 32 components for the workload. Each workload component has been obtained by executing the algo rithm varying from 2 to 16 the number of allocated processors- the problem size- and the number of blocks allocated per processor

At the beginning- parameters have been ex tracted from the measurements for the description of the achieved performance They are they mean number of messages exchanged between a cou ple of pleases and variety time the most process of the state of the waiting the state of th execution time for the time $\frac{1}{2}$ and $\frac{1}{2}$ the time for the $\frac{1}{2}$ the time the phase \mathbf{f} the time \mathbf{f} for transferring variables from the host Tin and back \mathbf{T} to the number relations related to the number relations relations relations relations relations relations relations of \mathbf{r} ber of accesses NRL- NRD- NAD- NAR

```
256
#define N
define P 
  \ddotscdist jacobien (distribute BN by by and the (fight) of the second party of the second party of the second party
                                                  map wrapped

                                                  mode INOUT
                      \lambdae double Annual Communications and the communications of the communi
\mathcal{L}
 int i,j;for (i=1; i<(N-1); i++)for (j=1; j<(N-1); j++) {
             A[i][j] = (B[i-1][j] + B[i+1][j] +B[i][j-1] + B[i][j+1] ) +
                                   V * B[i][j];
        }
}
```
Figure 1: The Jacobi algorithm considered.

The pre-analysis phase dealt with the definition of the relevant parameters able to capture the parallel

characteristics of the loads and component-componenthas been represented in a 11-dimensional space.

The aim of the experiments was to analyze the av erage behavior of the program; the value of the parameters for each component have been computed by averaging the values on all the processors on which the data have been distributed

 \mathcal{A} -matrix \mathcal{A} -matrix correlated parameters have been discovered. In the further analysis-benefits-benefits-benefits-benefits-benefits-benefits-benefits-benefits-benefits-benefits-ben the array processors are number of blocks the size-size-size-sizeper processor, and messages- the straining and messages- π execution times- times-time- $\frac{1}{\alpha}$, a consider the IO times-time consideration of the IO times- $\mathcal{L} = \mathcal{L} = \mathcal{L} = \mathcal{L} = \mathcal{L} = \mathcal{L}$

Cluster analysis yield an optimal partition of the workload into the contraction of the statistics are statistics are shown in the statistics are shown in the sta Fig As can be seen- cluster contains the ma jor part of the worker of the worker of the workload components-in the workload components-in the workload componentsby low execution times and number of exchanged mes sages

Looking at the composition of each cluster- we can see that-independently on the allowable to the the state of the allowed the allowed the allowed the allowed the state of the allowed the state of the state o cated processors- cluster in the category contract the contract of \mathcal{C} problem size and high number of blocks per processor Then- we can conclude that the performance obtained when executing the jacobi algorithm with high problem size and a partitioning of the data in small blocks are independent on the number of allocated proces sors

5 Conclusions and Future Work

A methodology for evaluating the relationships ex isting among the program characteristics- the data dis tribution adopted and the measured performance in dices has been presented. The results of an experiment in which the Jacobi algorithm has been analyzed- have been shown

Following such methodology- decisions related to the selection of the data distribution to be adopted can be facilitated

The methodology has to be tested on real applica tion programs Then- a more detailed description of the loop and the studies and the studies of the studies are statements and the state statements of the statements of the state of the state of the state of the state o representing the influence that such factors have on the selected data distribution. If different experimentations are carried out while varying the data distribu tion-the data mapping and the problem description-the problem description-the problem descriptiongroups of programs with similar performance behavior

can be identified the program description of the program description of the program description of the program tion- a prediction of the performance can be obtainedbased on the specified data distribution.

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	Npr	Size	NB1	NM	Wait	Tex	Tin	Tout	NRL	NRD	NAD
Npr	1.00	0.00	0.00	0.04	0.49	0.44	-0.59	0.45	-0.58	0.04	-0.58
Size	0.00	$1.00\,$	0.00	0.38	0.35	0.44	0.58	0.49	0.58	0.38	0.58
NB1	0.00	0.00	1.00	0.87	$0.42\,$	0.45	0.01	0.33	-0.01	0.87	0.00
NM	0.04	0.38	0.87	$1.00\,$	0.62	0.68	0.18	0.55	0.16	$1.00\,$	0.18
Wait	0.49	0.35	0.42	0.62	$1.00\,$	0.99	-0.21	0.83	-0.21	0.62	-0.20
Tex	0.44	0.44	0.45	0.68	0.99	1.00	-0.14	0.83	-0.14	0.68	-0.12
Tin	-0.59	0.58	0.01	0.18	-0.21	-0.14	$1.00\,$	-0.04	0.99	0.18	0.99
Tout	0.45	0.49	0.33	0.55	0.83	0.83	-0.04	$1.00\,$	-0.05	0.55	-0.04
NRL	-0.58	0.58	-0.01	0.16	-0.21	-0.14	0.99	-0.05	1.00	0.16	$1.00\,$
NRD	0.04	0.38	0.87	1.00	0.62	0.68	0.18	0.55	0.16	1.00	0.18
NAD.	-0.58	0.58	0.00	0.18	-0.20	-0.12	0.99	-0.04	$1.00\,$	0.18	$1.00\,$

Figure 2: Correlation matrix.

Npr	Size	N _B	NΜ	Tex	Tin	Tout	
16	128	1	236.25	2960.40	77.02	63.85	
16	128	$\overline{2}$	488.25	6961.27	95.80	2115.51	
16	128	4	992.25	14693.36	42.19	2472.90	
16	128	8	1984.50	19382.80	42.29	2162.21	
16	256	1	476.25	13169.92	152.69	151.59	
16	256	$\overline{2}$	984.25	30699.33	180.96	7571.21	
16	256	4	2000.25	64488.50	134.20	8231.70	
16	256	8	4032.25	131149.64	137.57	8556.59	
8	128	1	220.50	2024.08	81.45	148.48	
8	128	2	472.50	4124.83	100.27	1212.01	
8	128	4	976.50	8086.10	125.39	1475.52	
٠							

Figure 3: Workload components.

 $\overline{}$

	1 th cluster of 2	n. of observations = 23,0000						
param.	center	min	max	st dev				
Npr	7.130	2.000	16.000	5.286				
Size	166.957	128.000	256.000	60.220				
N _{Bl}	3.043	1.000	8.000	2.549				
NΜ	796.457	126.000	1984.500	608.624				
Tex	7370.958	1411.711	19382.811	5579.477				
Tin	257.511	42.192	946.695	248.937				
Tout	1231.401	63.854	3622.539	872.672				
	2 th cluster of 2 n. of observations = 9.0000							
param.	center	min	max	st.dev				
Npr	8.444	2.000	16.000	6.064				
Size	256.000	256.000	256.000	0.000				
N _{Bl}	5.556	2.000	8.000	2.404				
NΜ	2712.861	984.250	4032.250	1208.181				
Tex	44796.430	7039.291	131149.641	38947.316				
Tin	441.284	134.206	964.395	328.209				
				2654.015				

Figure 4: Statistics of the two clusters obtained. $\;$