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# **To cite this version:**

Sébastien Angibaud, Damien Eveillard, Guillaume Fertin, Irena Rusu. Comparing Bacterial Genomes by Searching their Common Intervals. 1st International Conference on Bioinformatics and Computational Biology (BICoB 2009), 2009, New Orleans, United States. pp.102-113, 10.1007/978-3-642-00727-9 12. hal-00416466

# **HAL Id: hal-00416466 <https://hal.science/hal-00416466v1>**

Submitted on 15 Sep 2009

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# Comparing Bacterial Genomes by Searching their Common Intervals

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Abstract. Comparing bacterial genomes implies the use of a dedicated measure. It relies on comparing circular genomes based on a set of conserved genes. Following this assumption, the common interval appears to be a good candidate. For evidences, we propose herein an approach to compute the common intervals between two circular genomes that takes into account duplications. Its application on a concrete case, comparing E. coli and V. cholerae, is accurate. It indeed emphasizes sets of conserved genes that present high impacts on bacterial functions.

Keywords: comparative genomic, circular genome, common interval

#### 1 Introduction

The bacterial world is ubiquitous and shows a great diversity [21]. Interestingly, it is responsible for the major key biological processes, but it remains far from being well-understood. For a while, understanding the bacterial diversity was considered as a pointless area because of the complexity and the versatility of this bacterial world, and because of its dynamic nature. Recent efforts in highthroughput methods for analyzing bacterial genomes, confirm its dynamic but emphasize, as well, a more comprehensive picture of the structure of genomes [12]. It gives various insights for investigating the bacterial complexity [6]. In particular, Doolittle [7] suggests sets of genes as convenient descriptors for comparing two bacterial species. Following this assumption, comparing two bacterial genomes implies (i) comparing their genes for finding orthologs and (ii) finding their invariants, which indicates the genes that are conserved in both species. Furthermore, it highlights common biological properties shared by the compared bacteria.

Previous points raises several computational questions. The first one deals with the inherent complexity of comparing one gene of a bacterial genome with genes from another genome. In [4], Berglund et al. tackled this problem by using a clustering technique as implemented in the InParanoid software. The second one concerns the choice of an appropriate measure to compare genome structures. Based on a correct mapping of orthologs between species, various approaches propose a theoretical framework to compute a measure between genomes based on their structure similarities [5]. They particularly highlight the sets of genes that are conserved among the genomes.

When applied on prokaryotic world and its particular features, comparing genomes implies the use of a dedicated protocol. By nature, bacterial genomes are circular, which must be taken into account by a dedicated measure. In addition, experimental investigations show evidences of high rates of gene duplications in bacteria. Based on these assumptions, this paper depicts a in silico protocol for the bacterial genome comparison. We propose (i) to find bacterial homologies by using the InParanoid software. We then have to put forward (ii) a dedicated measure. It relies on comparing circular genomes based on a set of conserved genes (following the assumption detailed in [7] and mentioned above). In this purpose, we propose an adaptation of the common interval [20] with a special emphasis on the circularity and duplications.

The paper is organized as follows. We briefly give notations and definitions in Section 2. We show in Section 3 how to compute the number of common intervals between two circular genomes that takes into account duplications. Based on these theoretical features, we are able to define a complete approach to compare bacterial genomes. In Section 4, we propose its application on a concrete case: comparing Escherichia coli and Vibrio cholerae. These well-known  $\gamma$ -Proteobacteria appear as an appropriate benchmark for testing the measure (quantitively and qualitatively). Beyond the accuracy of the comparison, the measure emphasizes sets of genes that are conserved on genomes. These genes show particular functional properties and belong to operons, which reinforces the biological relevance of the common interval measure in comparative genomics.

## 2 Preliminaries

The following section gives some notations and definitions used in the paper.

*Notations.* Let  $\mathcal F$  be a set of *genes*, where each gene is represented by an integer. A circular genome G is represented by an ordered sequence of signed elements (signed genes) from  $F$ , where we consider that the first gene and the last one are adjacent. Denote  $\eta_G$  the size of genome G. Let  $G[p]$ ,  $0 \leq p \leq \eta_G - 1$ , be the signed gene that occurs at position  $p$  on a genome  $G$ . For any signed gene g, let  $\overline{g}$  be the signed gene having the opposite sign. Let  $occ_G(g), g \in \mathcal{F}$ , be the number of occurrences of the gene q in  $G$ . Given a genome  $G$  without duplicates (i.e. without signed genes having the same absolute value) and two signed genes a, b, let  $G[a, b]$  be the set of unsigned genes located between genes a and b in G according to the circular order  $(G[0] \ G[1] \dots G[\eta_G-1] \ G[0] \dots)$  on G. We also note  $[a, b]_G$  the substring (i.e. the sequence of consecutive elements) of G starting by a and finishing by b.

For example, consider the set  $\mathcal{F} = \{1, 2, 3, 4, 5, 6\}$  and the circular genome  $G =$  $+3 - 2 + 6 + 4 - 1 + 5$  without duplicates. Then,  $G[4] = -1$  and  $\overline{G[4]} = +1$ ,  $G[-1, +3] = \{1, 3, 5\}$  and  $[-1, +3]$  $G = -1 + 5 + 3$ .

*Common intervals.* We define here the measure used in the paper. Let  $G_1, G_2$ be two circular genomes without duplicates and with a similar gene content. A common interval [20] of  $(G_1, G_2)$  is a substring of  $G_1$  such that  $G_2$  contains a permutation of this substring (not taking signs into account). For example, consider  $G_1 = +1 + 2 + 3 + 4 + 5$  and  $G_2 = +2 - 4 + 3 + 5 + 1$ . Then, substring  $[+3, +5]_{G_1}$  is a common interval of  $(G_1, G_2)$ . Note that the original definition of a common interval of [20] is extended here to consider circular sequences. Therefore, substring  $[+5, +1]_{G_1}$  is also a common interval.

Given a set  $\mathcal I$  of common intervals, a common interval  $I \in \mathcal I$  is called *maximal*, if there is no common interval of  $\mathcal I$  that strictly contains it. We call a *straight* interval, a maximal common interval for which the order and the signs of its genes are identical in  $G_1$  and  $G_2$ . On the contrary, the maximal interval is called reverse if the order and the signs of genes are reversed in  $G_1$  with respect to  $G_2$ . Finally, we call an *unstructured* interval, a maximal common interval that is neither straight nor reverse.

Genomes with duplicates. When genomes contain duplicates, we cannot directly compute the number of common intervals, because this measure is defined on permutations. A natural solution consists in i) finding a one-to-one correspondence (i.e. a matching) between signed genes of  $G_1$  and  $G_2$ , ii) using this correspondence to rename genes of  $G_1$  and  $G_2$ , and iii) deleting the unmatched signed genes in order to obtain two genomes  $G'_1$  and  $G'_2$  such that  $G'_2$  is a permutation of  $G'_{1}$ . Computing the measure becomes thus possible. Our study proposes to focus on two matching models: the *exemplar* model [15] and the *maximum* matching model [18].

- Exemplar model: for each gene g, we keep in the matching only one occurrence of g in  $G_1$  and in  $G_2$ .
- Maximum matching model: this model keeps the maximum number of signed genes in both genomes. In particular, we look for a one-to-one correspondence between signed genes of  $G_1$  and  $G_2$  that matches, for each gene g, exactly  $min(occ_{G_1}(g), occ_{G_2}(g))$  occurrences.

For a given model, among all possible matchings, we look for one that optimizes the number of common intervals. However, given two genomes  $G_1$  and  $G_2$ , the problem that consists in finding an exemplar (resp. a maximum matching) of  $(G_1, G_2)$  such that the number of common intervals is maximized, has been proved to be  $APX$ -Hard [1]. This complexity holds even when  $G_1$  does not contain duplicates and each gene appears at most twice in  $G_2$ .

# 3 Maximizing the number of common intervals between two circular genomes

In [2], authors proposed three methods to compare two genomes that are modeled as linear sequences of genes. The first one is an exact algorithm based on transforming an optimization problem into a 0–1 linear program [16]. The second one is a heuristic based on the notion of Longest Common Substring  $(LCS)$  and the third method is an hybrid method that combines both previous approaches. An approach dedicated to the bacterial genome analysis implies to take into account the natural circularity of the input genomes. For that, we propose to show herein how to extend previous works.

#### 3.1 Exact approach

The principle of this approach is based on (1) transforming an optimization problem into a 0–1 linear program [16] and (2) run this program on a powerful solver (e.g. MiniSat+ [8]) in order to obtain optimal solutions. Given two circular genomes  $G_1$  and  $G_2$ , we detail the above transformation for both *exemplar* and maximum matching models.

Variables. We define two types of variables: the match variables and the interval variables. One match variable is defined for each possible pair of signed genes that can be matched together. Any such variable will be set to 1 if the pair of corresponding signed genes is matched, and 0 otherwise. Thus, we define the set of match variables as follows:

$$
X = \{x_j^i : 0 \le i < \eta_{G_1} \land 0 \le j < \eta_{G_2} \land |G_1[i]| = |G_2[j]|\}
$$
  

$$
\forall x_j^i \in X, x_j^i \in \{0, 1\}
$$

The interval variables correspond to the possible common intervals. Note that the whole genome  $G_1$  is necessarily a common interval. Hence, we do not consider these intervals in order to reduce the linear program generated. These variables are defined as follows:

$$
C = \{c_{j,m}^{i,n} : 0 \le i < \eta_{G_1} \land 0 \le j < \eta_{G_2} \land 0 \le n < \eta_{G_1} - 1 \land 0 \le m < \eta_{G_2} - 1\}
$$
  

$$
\forall c_{j,m}^{i,n} \in C, c_{j,m}^{i,n} \in \{0, 1\}
$$

A variable  $c_{j,m}^{i,n} \in C$  corresponds to the common interval that begins at the position i on  $G_1$  and that contains  $n+1$  signed genes. Its corresponding interval on  $G_2$  begins at the position j and contains  $m + 1$  signed genes.

Objective function. We want to maximize the number of common intervals between  $G_1$  and  $G_2$ . For that, we define the objective function as the sum of the interval variables:

$$
\text{maximize } \sum_{\substack{i,n\\ c_{j,m}^i \in C}} c_{j,m}^{i,n}
$$

Constraints. We define several constraints to insure that the assigned variables correspond to a valid matching, according to the considered model. For that, we first define two constraints to verify that each signed gene cannot be matched to more than one signed gene on the other genome:

$$
(C1.a) \ \forall i, 0 \leqslant i < \eta_{G_1}, \sum_{\substack{0 \leqslant j < \eta_{G_2} \\ |G_1[i]| = |G_2[j]|}} x_j^i \leqslant 1
$$
\n
$$
(C1.b) \ \forall i, 0 \leqslant j < \eta_{G_2}, \sum_{\substack{0 \leqslant i < \eta_{G_1} \\ |G_1[i]| = |G_2[j]|}} x_j^i \leqslant 1
$$

Then, for each gene, we count the number of signed genes that are matched in order to respect the definition of the model. For the maximum matching model, we must have:

$$
(C2)\ \forall g\in\mathcal{F},\sum_{0\leqslant i<\eta_{G_1}\atop{|G_1[i]|=g}}\sum_{0\leqslant j<\eta_{G_2}\atop{|G_2[j]|=g}}x_j^i=\min\{occ_{G_1}(g),occ_{G_2}(g)\}
$$

For the exemplar model, we must have:

$$
(C2')\ \forall g\in\mathcal{F}, \sum_{0\leqslant i<\eta_{G_1}\atop{|G_1[i]|=g}}\sum_{0\leqslant j<\eta_{G_2}\atop{|G_2[j]|=g}}x_j^i=\min\{1,\min\{occ_{G_1}(g),occ_{G_2}(g)\}\}
$$

In order to the interval variable validity, we introduce a new notation. For any  $q \in \{1,2\}$ , we let  $f_q(i,p) \equiv (i+p) \mod \eta_{G_q}$ . This notation is necessary for taking into account the common intervals that contain both  $G_q[0]$  and  $G_q[\eta_{G_q}$  – 1].

First, we must make sure that each extremity of a common interval is matched with the two following constraints:

$$
\begin{aligned} & (C3.a) \ \forall c_{j,m}^{i,n} \in C, 2c_{j,m}^{i,n} - \sum\limits_{\substack{0 \leqslant p \leqslant m \\ |G_{1}[i]| = |G_{2}[f_{2}(j,p)]|}} x_{f_{2}(j,p)}^{i} - \sum\limits_{\substack{0 \leqslant p \leqslant m \\ |G_{1}[f_{1}(i,n)]| = |G_{2}[f_{2}(j,p)]|}} x_{f_{2}(j,p)}^{f_{1}(i,n)} \leqslant 0 \\ & (C3.b) \ \forall c_{j,m}^{i,n} \in C, 2c_{j,m}^{i,n} - \sum\limits_{\substack{0 \leqslant p \leqslant n \\ |G_{1}[f_{1}(i,p)]| = |G_{2}[j]|}} x_{j}^{f_{1}(i,p)} - \sum\limits_{\substack{0 \leqslant p \leqslant n \\ |G_{1}[f_{1}(i,p)]| = |G_{2}[f_{2}(j,m)]|}} x_{f_{2}(j,m)}^{f_{1}(i,p)} \leqslant 0 \end{aligned}
$$

Then, we define constraints to insure that each signed gene of  $G_1$  inside a common interval  $I$  is correctly matched. For that, we consider two cases. If the corresponding interval of I on  $G_2$  does not contain both  $G_2[0]$  and  $G_2[\eta_{G_2} - 1]$ , we write:

$$
(C4.a) \ \forall c_{j,m}^{i,n} \in C, j+m < \eta_{G_2}, \forall 1 \leq p < n, \forall 0 \leq r < j,
$$
  

$$
|G_1[f_1(i,p)]| = |G_2[r]|, c_{j,m}^{i,n} + x_r^{f_1(i,p)} \leq 1
$$

$$
(C4.b) \ \forall c_{j,m}^{i,n} \in C, j+m < \eta_{G_2}, \forall 1 \leqslant p < n, \forall j+m < r \leqslant \eta_{G_2},
$$

$$
|G_1[f_1(i,p)]| = |G_2[r]|, c_{j,m}^{i,n} + x_r^{f_1(i,p)} \leq 1
$$

Else, if the corresponding interval of I on  $G_2$  contains both  $G_2[0]$  and  $G_2[\eta_{G_2}-1]$ , we write:

$$
(C4.c) \ \forall c_{j,m}^{i,n} \in C, j+m \geqslant \eta_{G_2}, \forall 1 \leqslant p < n, \forall f_2(j,m) < r < j,
$$
\n
$$
|G_1[f_1(i,p)]| = |G_2[r]|, c_{j,m}^{i,n} + x_r^{f_1(i,p)} \leqslant 1
$$

Finally, we also define the three symmetric constraints of  $(C4.a)$ ,  $(C4.b)$  and  $(C4.c)$  to consider each signed gene in  $G_2$ . Appendix ?? gives on overview of the whole 0–1 linear program.

#### 3.2 Non-exact approaches

IILCS heuristic. The IILCS heuristic proposed in [2] is a greedy algorithm based on the notion of Longest Common Substring (LCS). The program matches genes of an LCS of the two genomes, up to a complete reversal, and iterates this process until no gene can be matched (see [2] for more details). We easily modify this algorithm in order to compare circular genomes by identifying the LCS that may overlap the end and the beginning of the genomes.

Hybrid method. This approach uses both previous methods. First, a partial matching is obtained by running IILCS until the size of any LCS is smaller than a given parameter k, chosen by the user. Then, a  $0-1$  linear program is generated in order to match the remaining unmatched genes. Since both previous methods have been extended for taking into account genome circularity, the hybrid method is hence adapted to circular genomes.

### 4 Comparing bacterial genomes: a practical application

Based on the previous theoretical framework, we are now able to propose a practical comparison of proteobacterias. Here, we first define the protocol used and, secondly, put forward a precise analysis of biological results obtained.

#### 4.1 Protocol

The different steps of our comprehensive approach might be described as follow (see also Figure 1 for illustration).

Step 1. Input data. One selects on the NCBI website two genomes  $G_1$  and  $G_2$ and transforms the corresponding data into two files in the FASTA format, one for each genome. These files contain the list of genes, each of which is described by a label followed by its protein sequence.



Fig. 1. Step by step description of the bacterial genome analysis.

Steps 2 and 3. Homologies detection. We call the InParanoid software [13], which clusters orthologs and inparalogs genes based on a Blastp (step 2). The output file contains the clusters of the homologous genes. According to these sets, we tag these homologous genes with a similar label. It hence builds two intermediate genomes  $G'_{1}$  and  $G'_{2}$  (step 3).

Steps 4, 5 and 6. Measure computation. We use one of the approaches described in Section 3 to obtain a matching between the two genomes (step 4). In this purpose, two parameters must be specified:

- The model: exemplar or maximum matching model (see Section 2).
- The method: the exact method based on a pseudo-boolean programming  $(PSB)$ , the IILCS heuristic or the hybrid method with a parameter k bounding the size of the LCS (see Section 3).

We generate the list of gene pairs that are matched. Thus, we rename the genes according to this matching and remove the unmatched genes to construct two genomes  $G''_1$  and  $G''_2$  without duplications and with the same gene content (step 5). We then compute the common intervals of  $(G''_1, G''_2)$  (step 6).

Filtering relevant common intervals. Among the set  $\mathcal I$  of common intervals we have obtained, we select the relevant common intervals as follows:

1. We remove common intervals that contain all matched signed genes (the whole genome being a trivial common interval).

- 2. Since genomes are circular, for each common interval  $I \in \mathcal{I}$ , there exists a unique common interval  $I' \in \mathcal{I}$ , such that  $I'$  contains all matched signed genes that do not belong to I. The pair  $(I, I')$  will be called a *complementary* pair. Given any complementary pair  $(I, I')$ , we assume that the smallest interval  $I_s \in \{I, I'\}$  (i.e., the one that contains less signed genes) is the most biologically informative, and thus we choose to keep only  $I<sub>s</sub>$  in our set.
- 3. However, an interval that contains only one gene carries no biological information. We thus remove such intervals from our set.

#### 4.2 Practical application

We apply our method on a benchmark composed of proteobacteria's genomes (Escherichia coli and Vibrio cholerae). Table 1 lists the considered set of genomes and Table 2 shows quantitative details concerning common intervals under the maximum matching model. Note that the computational time of InParanoid is much longer than the one needed to obtain the matching. However, for the longest sequences (NC\_000913 vs  $NC_{-002505}$  or  $NC_{-000913}$  vs  $NC_{-009457}$ ), only the IILCS heuristic gives results in an acceptable amount of time. Note also the distribution of straight, reverse and unstructured intervals (see Table 2). On average, 41% of maximal common intervals are straight, 49% are reverse and 10% are unstructured.

$\overline{\text{NCBI label}}$	Name
NC_000913	Escherichia coli K12
	NC_002505 Vibrio cholerae 01 biovar eltor str. N16961 chromosome I
	NC_002506 Vibrio cholerae 01 biovar eltor str. N16961 chromosome II
$NC_009456$	<i>Vibrio cholerae</i> 0395 chromosome I
NC_009457	<i>Vibrio cholerae</i> 0395 chromosome II

Table 1. Set of genomes analyzed.

These quantitative results are computationnaly relevant. We therefore propose to go further by investigating their qualitative properties. In particular, we focus on the comparison of the chromosome pair composed by *Escherichia*  $\text{coli}$  (NC<sub>-000913</sub>) and *Vibrio cholerae* (NC<sub>-009457</sub>), for which the quantitative results are given in Table 2. We consider their comparison as an appropriate benchmark for testing the biological properties highlighted by the common interval measure. As shown in Figure 2, it emphasizes three kinds of common intervals:

Straight intervals. They show a perfectly conserved gene arrangements like in Figure 2 a). Based on experimental knowledges refered in EcoCyc[11], CcmA, CcmB, CcmC, CcmD, CcmE, CcmF, CcmG and CcmH are the genes that encode for proteins that are sub-units of the cytochrome C complex. These genes

	genome size			time		computational relevant common intervals cardinality				
$\sim$ ئ genome	coli E.	$\zeta_2^2$	method	$\overline{\mathbf{e}}$ Inparanoid	$\odot$ matching	number	maximal	straight	reverse	unstructured
$NC\_002505$ 4243		2742	IILCS	1144	62			3710 275 117 (43%)	134(48%)	$24(9\%)$
$NC\_002506$ 4243		1093	PSB	638	23	123	50	$18(36\%)$	$23(46\%)$	$9(18\%)$
$NC$ 009456 4243		1133	PSB	651	22	132	55	17(31%)	$27(49\%)$	$11(20\%)$
$NC\_009457$ 4243		2742	$\it{IILCS}$	1199	59			$ 3602 278 114(41\%) 141(51\%)$		23(8%)

Table 2. Relevant common intervals obtained under the maximum matching model by comparing *Escherichia coli* (NCBI label NC<sub>-000913</sub>) with four *Vibrio* cholerae chromosomes (NC 002505, NC 002506, NC 009456 and NC 009457).

belong to the same operon promoted by  $\operatorname{cmAp}[17]$ . In particular, experimental studies show that mutants of one of these genes are deficient in the ability to produce c-type cytochromes [19]. Their presence into a unique straight common interval, emphasizes the fact that these genes are conserved by their DNA sequence (i.e. homology shown using InParanoid), but also by their arrangement on the bacterial genomes (i.e. determination of the common interval). This result confirms the interest to find highly functionnal genes into a single common interval.

Reverse intervals. They show sets of genes that presents a conservation between two genomes in a reverse order, like the one in Figure 2 b). This particular interval depicts the pilus gene clusters that encode for extracellular pilus structures. They are common among bacteria and have been involved in several colonization functions, like those involved in the intestinal mucosa colonization. For clinical motivations, the homology of these genes is already shown between V. cholerae and Vibrio fisheri [14]. In [9], Fullner and Mekalanos depict the organization of the pilus assembly operon with 7 genes. The reverse common interval shown in Figure 2 b) suggests a conservation of 3 genes only, which is not fully accurate with the experimental assumption. Nevertheless, note that EcoCyc [10] not shows neither high-quality evidences of a common transcriptionnal unit for the seven genes, which not invalidates our method.

Unstructured intervals. They represent common intervals which are neither straight nor reverse. Figure 2 c) illustrates this case. Like in a), this particular interval also describes the arrangement of four genes that belong to the same operon:  $hisJp$  operon. It is activated by Hns and repressed by ArgR. It products a subunit of an ABC Transporter. Note again that  $ArgR$  that encodes ArgR belongs, with mdh, to a single reverse common interval (see Figure 2 d)). mdh produces Mdh that is a subunit of a malate dehydrogenase. It interacts in several



Fig. 2. Illustration of the three kinds of common intervals observed between E. coli (NC 000913) and V. cholerae (NC 009457). Each representation indicates the gene indexes (e.g., GI16130131), the genes position (e.g., 2121), the available labels of genes (e.g.,  $CcmH$ ), the gene orientation. Homologies are summarized using colors.

biological processes (carbohydrate metabolism, gluconeogenesis, glycolysis, tricarboxylic acid cycle, tricarboxylic acid cycle intermediate metabolism, malate metabolism, fermentation, anaerobic respiration, glyoxylate catabolism, carbohydrate catabolism). Again, these results confirm that common intervals might be associated with operons, but moreover, like in this case, with a set of genes that controls operons. Assuming that a common interval emphasizes a biological function conservation over compared genomes, regulatory function appears as important as other metabolic functions. Like in this case, common interval shows a specific regulatory unit that controls distinct biological processes via distinct operons. It is particularly interesting for studying genomes and their comparisons from a functionnal viewpoint.

A close look at these qualitative results highlights that common intervals (either straight, reverse or unstructured) may indicate the presence of functional components within bacterial genomes. Such an information is particularly valuable for investigating the bacterial functional diversity, in particular in an environmental context for which the genomic data remain the corner stone for a better understanding.

# 5 Extension of the method to conserved intervals

Apart of the common intervals, Bergeron and Stoye introduced in [3] the notion of conserved intervals. Given two circular genomes  $G_1$  and  $G_2$  with same gene content and without duplication, consider two signed genes  $a$  and  $b$  of  $G_1$ , with possibly  $a = b$ . Substring  $[a, b]_{G_1}$  is called a *conserved interval* of  $(G_1, G_2)$  if  $[a, b]_{G_1}$  is a common interval and if it satisfies one of the two following properties: either a and b appear in  $G_2$  and  $G_1[a, b] = G_2[a, b]$ ; or  $\overline{a}$  and  $\overline{b}$  appear in  $G_2$ and  $G_1[a, b] = G_2[\overline{b}, \overline{a}]$ . For example, if  $G_1 = +1 + 2 + 3 + 4 + 5$  and  $G_2 =$  $-5 - 4 - 2 + 3 - 1$ , substrings  $[+4, +5]_{G_1}$  and  $[+4, +1]_{G_1}$  are two conserved intervals of  $(G_1, G_2)$ .

Our previous approach (see Section 3) can be adapted to compute the conserved intervals instead of the common intervals. Concerning the exact approach, since a conserved interval is also a common interval with restrictions on its extremities, an additional filter on interval variables suffices to consider the number of conserved intervals. In that case, we change the set  $C$  of variables such that

$$
C = \{c_{j,m}^{i,n} : 0 \leq i < \eta_{G_1} \land 0 \leq j < \eta_{G_2} \land 0 \leq n < \eta_{G_1} - 1 \land 0 \leq m < \eta_{G_2} - 1\} \land \newline \newline \quad \left(\begin{array}{c} (G_1[i] = G_2[j] \land G_1[f_1(i,n)] = G_2[f_2(j,m)] \end{array}\right) \lor \newline \left(\begin{array}{c} G_1[i] = \overline{G_2[f_2(j,m)]} \land G_1[f_1(i,n)] = \overline{G_2[j]} \end{array}\right)
$$

For IILCS and hence for the hybrid method, the process remains the same in the greedy phase. However, the intervals computation is modified to count only conserved intervals, which does not affect the complexity of the algorithm.

### 6 Conclusion

In this paper, we have presented a comprehensive method to find sets of genes that are conserved between two circular genomes. We present for that an approach to compute or approximate the number of common intervals between two circular genomes. Each resulting interval can be considered as a set of genes that is conserved between the two genomes during the evolution process. Our method was tested on Escherichia coli and four chromosomes of Vibrio cholerae. From these experimentations, the results strongly suggest that common intervals is a measure that provide useful information on bacterial genomes and help the user to focus on specific sets of genes that possess functionnal and regulatory properties. It confirms the interest of the common interval measure for giving more functionnal insights in comparative genomics studies. A thorough biological analysis of each maximum common interval, along with tests on larger benchmarks, are planned in the very next future.

Acknowledgment: the authors thank Dr. Richard A. Long for the fruitful discussions that initiated this work.

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