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Performance Specifications and Analysis of a Variable Speed Synchronous Generator with a Diode Rectifier for the All Electric Aircraft Using the H∞ Control Approach

M. Sautreuil, O. Sename, D. Riu, N. Retière

Abstract—This paper deals with the modeling and control of an electrical source for the future "All Electric" aircraft. It is constituted by a rotor wounded synchronous generator and a diode rectifier feeding the DC power system. Using $H\infty$ control theory, this paper shows that usual disturbance rejection standards can not be met with such an electrical power source and new standards should be defined. Simulations on an exact nonlinear model of the power source are used for control validation.

I. INTRODUCTION

WITH the development of reliable and efficient power electronics converters, aircraft power networks have been considerably changed. First evolutions concerned the replacement of hydraulic and pneumatic devices by electrohydraulic and electro-pneumatic loads in the "More Electric" aircraft. In these aircrafts, the electrical power is distributed mainly through AC buses and includes many AC/DC/AC conversion stages to feed the motor loads. With the "All Electric" aircraft, AC/DC conversion stages are suppressed and the electrical power is distributed through a DC bus. This evolution was initiated with the European "Power Optimized Aircraft" project, followed by the current "More Open Electrical Technologies" project in which this work lies [2].

In [1], a first "All Electric" structure is studied from a DC voltage performance point of view. The electrical power source is directly derived from the "More Electric" structure and is shown in Fig. 1.

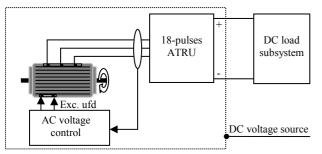


Fig. 1: Power source with Auto Transformer Rectifier Unit [1]

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The AC side voltage is controlled with a simple PI controller and the analysis in [1] shows that this simple control allows the respect of the disturbance rejection performances imposed by the standards on the DC side. However, the 18-pulses ATRU is a heavy device and other source structures are studied for the future "All Electric" aircraft.

In this paper, the authors study the control design of a lighter power source for the "All Electric" aircraft. It is constituted by a 209kVA synchronous generator with a diode rectifier feeding the DC load. The DC voltage is controlled through the excitation voltage of the synchronous generator (Fig. 2). The stator electrical frequency (fe) depends on the rotor speed, and varies from 360Hz to 800Hz. However, because the shaft speed varies slowly regarding electrical time constants, the system is assumed to be Time Invariant in this paper. Our aim is to evaluate if the usual disturbance rejection specifications can be met with this power source structure. If not, new standards should be proposed. The H∞ control theory is applied to obtain an optimal controller towards disturbance rejection control objectives. These objectives will have to be met for several operating conditions corresponding to the variable frequency operation of the generator.

The paper is organized as follows. In Section II, the linear model of the system is first derived. The control specifications are then defined. One of these specifications is the respect of the usual disturbance rejection standard. Section III proposes the design of a H∞ controller at a given operating point (fe=400Hz) and a performance analysis over all the operating conditions is performed. Section IV will conclude on the feasibility of a control for the performance specifications given in section II. It is shown that the standards, which impose the performances from a disturbance rejection point of view, should be modified if this source is finally used in the "All Electric" aircraft.

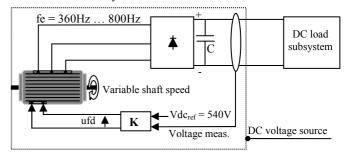


Fig. 2: Studied Power source

II. MODELING AND CONTROL SPECIFICATIONS

A. Modeling

1) The synchronous generator model

The generator equations are written in the (d,q,0) rotating frame using the Park transform described in the appendix. We make the assumption of a balanced three phase system, and 0 axis components are set to zero. The state space equations of the synchronous generator are given by:

$$uds = Rsids - we(Llsiqs + Lmq(iqs + ikq)) + \frac{d}{dt}(Llsids + Lmd(ids + ifd + ikd))$$

$$uqs = Rsiqs + we(Llsids + Lmd(ids + ifd + ikd)) + \frac{d}{dt}(Llsiqs + Lmq(iqs + ikq))$$

$$0 = Rkdikd + Llkd.\frac{dikd}{dt} + Lmd.\frac{d}{dt}(ids + ifd + ikd)$$

$$0 = Rkq.ikq + Llkq.\frac{dikq}{dt} + Lmq.\frac{d}{dt}(ikq + iqs)$$

$$ufd = Rfdifd + \frac{d}{dt}(Llfdifd + Lmd(ids + ifd + ikd))$$

$$(1)$$

(uds, uqs) are the stator voltages, (ids, iqs) the stator currents, (ikd, ikq) the damping windings currents, ifd is the excitation current and ufd the excitation voltage of the generator, we is the electrical pulsation. The parameters are defined in the appendix.

2) The diode rectifier model

The approach presented in this paper is a semi-analytical modeling method, which was originally proposed and validated in [3]. It consists in considering the diode rectifier as a voltage gain to calculate DC side voltage from AC side voltage, and a current gain to obtain AC side current from DC side current.

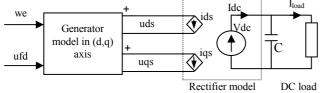


Fig. 3: Power source model [3]

The basic idea is to link the average values of the (d,q) variables of the AC side to the average values of the DC side voltage and current (2,3):

$$Vdc = kv_{\lambda}\sqrt{uds^2 + uqs^2} \tag{2}$$

$$Idc = ki.\sqrt{ids^2 + iqs^2} \tag{3}$$

In these equations, kv and ki are voltage and current gains, which are nonlinear and depend on the operating point of the system [3]. The resulting space vector diagram is shown in Fig. 4:

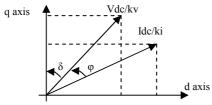


Fig. 4: space vector diagram for the rectifier model

From this diagram, the following equations are obtained:

$$Vdc = kv.\sqrt{uds^2 + uqs^2} \tag{4}$$

$$ids = (k_{\cos} uds + k_{\sin} uqs) \cdot \frac{Idc}{Vdc}$$
 (5)

$$iqs = (k_{cos}.uqs - k_{sin}uds).\frac{Idc}{Vdc}$$
 (6)

$$k_{\cos} = \frac{kv \cdot \cos \varphi}{ki}$$
 and $k_{\sin} = \frac{kv \cdot \sin \varphi}{ki}$ (7.8)

In (7) and (8), φ is the phase displacement between AC voltage and currents. To obtain the linear model of the rectifier, the above equations are linearized around the chosen operating point. The linear equations are given by:

$$Vdc = \frac{kv_{e} u ds_{e}}{\sqrt{u ds_{e}^{2} + u q s_{e}^{2}}} u ds + \frac{kv_{e} u q s_{e}}{\sqrt{u ds_{e}^{2} + u q s_{e}^{2}}} u q s$$
(9)

$$ids = \frac{k_{\cos_e} idc_e}{vdc_e} uds + \frac{k_{\sin_e} idc_e}{vdc_e} uqs + \frac{k_{\cos_e} uds_e + k_{\sin_e} uqs_e}{vdc_e} idc - \frac{ids_e}{vdc_e} vdc$$

$$iqs = \frac{-k_{\sin_e} idc_e}{vdc_e} uds + \frac{k_{\cos_e} idc_e}{vdc_e} uqs + \frac{k_{\cos_e} uqs_e - k_{\sin_e} uds_e}{vdc_e} idc$$

$$vdc_e$$

$$(11)$$

$$iqs = \frac{-k_{\sin_{e}}idc_{e}}{vdc_{o}}uds + \frac{k_{\cos_{e}}idc_{e}}{vdc_{o}}uqs + \frac{k_{\cos_{e}}uqs_{e} - k_{\sin_{e}}uds_{e}}{vdc_{o}}idc$$
 (11)

Index e denotes the equilibrium values of the variables. The following DC side equation is added to these equations:

$$idc = C.\frac{dVdc}{dt} + i_{load} \tag{12}$$

where iload is the load current.

3) State-space equations of the synchronous generator with diode rectifier system

To develop the model of the synchronous generator with the diode rectifier, the generator equations are associated to the rectifier equations. The load current is an input of the system and will be considered as the system disturbance for control design. The following representation is finally obtained:

$$V.U = E.X + F.X$$

with U the input vector, and X the state vector:

$$U = \begin{bmatrix} i_{load} & ufd \end{bmatrix}^T$$

 $L_{21} + L_{22}L_{13} = 0$

 $X = [ids \ ifd \ ikd \ iqs \ ikq \ Vdc]^T$

Matrix V, E and F are given by:

$$V = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 0 \\ L_{31} + L_{32}L_{13} & 0 \\ 0 & 0 & 0 \\ L_{13} & 0 \end{bmatrix}$$

$$E = \begin{bmatrix} Rs - L_{20} - L_{22}L_{11} & 0 & 0 & -weLq - L_{22}L_{12} & -weLmq & -L_{23} - L_{22}L_{10} \\ 0 & Rfd & 0 & 0 & 0 & 0 \\ 0 & 0 & Rkd & 0 & 0 & 0 \\ weLd - L_{32}L_{11} & weLmd & weLmd & Rs - L_{30} - L_{32}L_{12} & 0 & -L_{33} - L_{32}L_{10} \\ 0 & 0 & 0 & 0 & Rkq & 0 \\ -L_{11} & 0 & 0 & -L_{12} & 0 & -L_{10} \end{bmatrix}$$

$$(12)$$

$$F = \begin{bmatrix} Ld & Lmd & Lmd & 0 & 0 & 0 \\ Lmd & Lf & Lmd & 0 & 0 & 0 \\ Lmd & Lmd & LD & 0 & 0 & 0 \\ 0 & 0 & 0 & Lq & Lmq & 0 \\ 0 & 0 & 0 & Lmq & LQ & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

$$(14)$$

Coefficients L_{ij} are quite complex and are not given in this paper. Then, the open-loop state-space representation of the system is obtained:

$$\dot{X} = A.X + B.U \tag{15}$$

Y = C.X

with:

$$A = -F^{-1}.E$$
, $B = F^{-1}.V$, and $C = [0 \ 0 \ 0 \ 0 \ 1]$ (16)

B. Control specifications

1) Disturbance rejection

Following a load current step on the DC side of the rectifier, the standards usually impose that the DC voltage remains in a transient envelop defined by Fig. 5, as presented in [1].

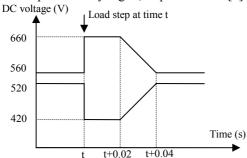


Fig. 5: Assigned transient envelop after a load step at Point Of Regulation

These specifications should be met for all operating conditions, which is a robust performance criterion.

2) Limitations on the excitation voltage

To avoid control saturation, the minimum / maximum amplitude of the excitation should be limited. Saturation limits are ufd = 0V (the excitation voltage can not be negative) and ufd = 48V (upper limit of saturation). The bandwidth of the control should also be limited for noise attenuation. In this application, the noise on the DC voltage measurement is the harmonic content of the DC voltage due to the 6-pulses rectification. This harmonic content is at frequency fn = 6*fe, with fe the frequency of the AC voltage. Consequently it varies from 2160Hz (fe=360Hz) to 4800Hz (fe=800Hz).

III. $H\infty$ control of the generator with diode rectifier system at the nominal 400Hz operating point

In this section, the first part is devoted to a background on the $H\infty$ control approach. The second one concerns the application of $H\infty$ control theory to the system introduced in section II at the nominal operating condition of the system defined by fe=400Hz. The performance of this $H\infty$ controller will finally be evaluated for various operating conditions.

A. Some background on $H\infty$ control

The H ∞ control problem relies on the general control configuration (Fig. 6), where P(s) is the generalized plant model. v are the control variables, y the measured variables, w the exogenous signals and e the controlled output variables. Given γ , a pre-specified attenuation level, a suboptimal H ∞ control problem is to design a controller that internally stabilizes the closed-loop system and ensures:

$$||N_{ew}(s)||_{\infty} \le \gamma \tag{17}$$

where $N_{\rm ew}$ is the closed-loop transfer matrix from e to w. Weights are considered to take the performance specifications in the frequency domain into account. In Fig. 6, G is the plant model and $W_{\rm i/o}$ the frequency domain weights.

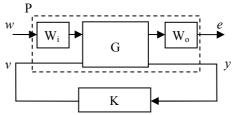


Fig. 6: General control configuration [4]

The $H\infty$ suboptimal control problem (17) is solved using the Riccati equations or LMI, allowing to get the minimal value of gamma. The details can be found in [4].

B. $H\infty$ control design at the nominal 400Hz frequency.

In this part, the authors apply the $H\infty$ control theory to the proposed power source. The operating point is set to fe=400Hz at the maximum power point (150kW, i_{load} =270A). The studied control configuration is presented in Fig. 7.

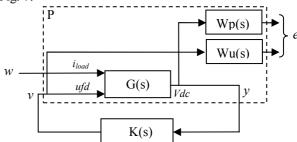


Fig. 7: the control scheme with the weights

It includes the plant model G(s), the controller to be designed K(s) and the weighting functions Wp(s) and Wu(s). Wp(s) is the frequency domain weight representing the required disturbance rejection performances. Wu(s) is the weight linked to the excitation voltage limitations explained upper. They are chosen as follows.

Wp: The inverse of the function Wp defines the template of the transfer function Vdc/i_{load} . This template should guarantee that after a load current step, the DC voltage remains in the envelop defined in Fig. 5. A maximum load current step of 135A is considered (which corresponds to a

50% load power step). The weighting function is given by:

$$Wp(s) = \frac{s / Ms + wb}{s + wb \cdot \varepsilon s}$$
 (18)

with Ms = 120/135, wb = 75 rad/s and $\varepsilon s \approx 0$.

Wu: The control input ufd is limited beyond 1000Hz in order to avoid noise sensitivity. For fe = 400Hz, noise occurs at 6*400 = 2400Hz. Moreover, the amplitude of Wu is limited before 1000Hz to avoid excitation voltage saturation. The weighting function Wu is given by:

$$Wu(s) = \frac{s + wbu/Mu}{\varepsilon u.s + wbu}$$
 (19)

The H ∞ problem has a solution. This means that the control objectives are met at the operating point corresponding to fe=400Hz. The amplitudes of the obtained closed-loop transfer functions Vdc/i_{load} and ufd/i_{load} are respectively given in Fig. 8 and Fig. 9 and compared to the templates 1/Wp and 1/Wu.

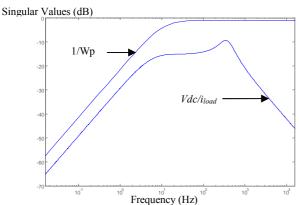


Fig. 8: Amplitude of the closed-loop transfer function *Vdc/i_{load}* and template 1/Wp.

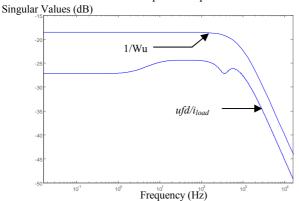


Fig. 9: Amplitude of the closed-loop transfer function ufd/i_{load} and template 1/Wu.

The controller performances are now evaluated at different operating conditions, for fe varying from 360Hz to 800Hz. The closed-loop transfer function Vdc/i_{load} and ufd/i_{load} are plotted for fe=360Hz, 400Hz, 500Hz, 600Hz, 700Hz and 800Hz (Fig. 10 and 11).

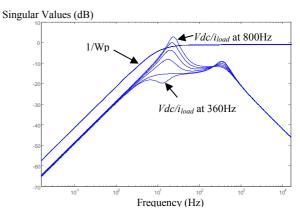


Fig. 10: Amplitude of the closed-loop transfer function Vdc/i_{load} for operating frequencies from 360Hz to 800Hz and 1/Wp.

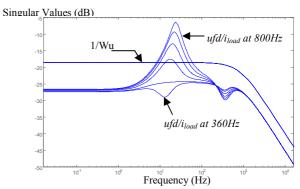


Fig. 11: Amplitude of the closed-loop transfer function ufd/i_{load} for operating frequencies from 360Hz to 800Hz and template 1/Wu.

The analysis of Fig. 10 and Fig. 11 shows that the required performances are not met for all the operating conditions of the system. It can also be concluded that the "worst" operating point is at high shaft speed, i.e. for fe=800Hz. As a conclusion, a $H\infty$ controller synthesized at 800Hz that would meet the performances specifications would also meet the specifications for lower operating frequencies. In the next section, the authors look for such a controller.

IV. $H\infty$ control design at the "worst" operating condition

A. Performance specifications

A controller designed at the "worst" operating condition (fe=800Hz) would also meet the performance specifications for lower frequencies. As explained upper, the voltage measurement noise directly depends on the DC voltage harmonic level, which is caused by the 6-pulses rectification. It explains that the noise frequency varies from 2160Hz to 4800Hz, according to the operating AC side frequency. To guarantee noise rejection at all operating frequencies, the control should not be sensitive to the noise which occurs at the frequency 6*360 = 2160Hz. For this, the cut off frequency in Wu is chosen to reject 2160Hz noise. The required disturbance rejection performances are the same and the Wp parameters are not changed (18).

B. $H\infty$ control design at the "worst" operating condition

The results are plotted in Fig. 12 and 13. The amplitudes of the closed-loop transfer functions Vdc/i_{load} and ufd/i_{load} are compared to the templates 1/Wp and 1/Wu.

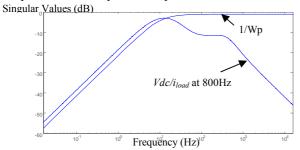


Fig. 12: Amplitude of the closed-loop transfer function Vdc/i_{load} at the worst operating frequency (800Hz) and 1/Wp.

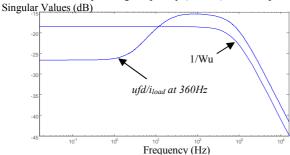


Fig. 13: Amplitude of the closed-loop transfer function ufd/i_{load} at the worst operating frequency (800Hz) and template 1/Wu.

As shown on Fig. 12 and 13, the performance specifications are not met. From Fig. 12, it is concluded that a disturbance can not be rejected as fast as required. From Fig. 13, we notice that the resulting controller is sensitive to noise and exhibits saturation after a load step. This is a very important result because it shows that the performance requirements can not be simultaneously met for the "worst" operating condition. In other words, conflicting objectives were defined in the $H\infty$ control problem (17). On one hand, from the analysis of the closed-loop transfer functions in Fig. 12 and 13, we conclude that the bandwidth and amplitude limitations on the excitation voltage are not compatible with the required disturbance rejection speed. On the other hand, the performance specifications on the excitation voltage can not be released for controller practical implementation reasons.

C. Towards new performance specifications

1) Considerations on control achievability for usual disturbance rejection standards

Other control solutions could be performed, for example a gain-scheduling control which would adapt the controller parameters to the AC side frequency. But it could be shown that at the operating 800Hz condition, with the maximum admissible bandwidth on 1/Wu (chosen to reject noise at 6*800 = 4800Hz), no solutions can be found. Moreover, in more classical source structures [1], a simple PI control of the generator exhibits satisfying disturbance rejection performances and the standards are easily met. From these considerations, we conclude that the usual disturbance

rejection standards are not suitable if the synchronous generator + diode rectifier source is chosen. In the next section, a new disturbance rejection standard is proposed. For this, the best performances achievable by an $H\infty$ controller for all the operating conditions are sought.

2) Best achievable performances by $H\infty$ control for all the operating conditions

Wu is not changed (template of 1/Wu in Fig. 13) because they guarantee an adequate operation of the controller on the real plant (no noise sensitivity and no saturation). Only Wp is changed. We choose to keep almost the same requirements on over-voltage / under-voltage after the load step. But the required time response is extensively modified until the $H\infty$ problem has a solution. The obtained closed-loop transfer functions are given in Fig. 14 and 15.

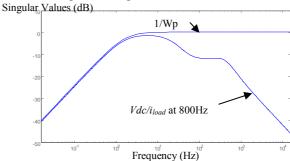


Fig. 14: Best achievable performance in 1/Wp and closed-loop transfer function Vdc/i_{load} (Amplitudes).

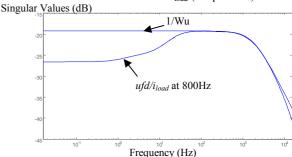


Fig. 15: Amplitude of the closed-loop transfer function ufd/i_{load} and 1/Wu

To find a solution to the $H\infty$ problem, the cut-off frequency wb of the 1/Wp template has been divided by 7,5 and the Ms factor in (18) was increased from 120/135 to 140/135. In other words, in the time domain the required time response is 7,5 times larger than with the classical requirements, and an overshoot of 140V is allowed after a 135A load step.

D. Proposition of a new disturbance rejection standard

Considering the results presented in this paper, the author propose to use the following disturbance rejection standard.

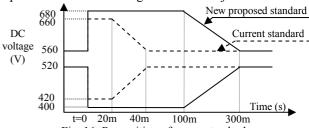


Fig. 16: Proposition of a new standard.

This new performance specification is the translation of the frequency domain template 1/Wp into time domain performances.

E. Validation by non-linear simulation

Our approach is validated using the non-linear simulation tool SABER®. The topological model presented in Fig. 2 is simulated, where the DC load is an ideal constant power load, which is a typical aircraft electrical load [1]. At t=0,5s, a load decrease from 150kW (the nominal generator power) to 75kW is simulated.

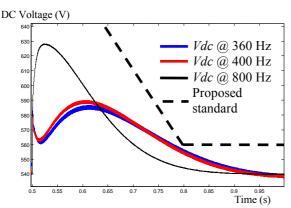


Fig. 17: DC voltage transient after a load power step from 150kW to 75kW

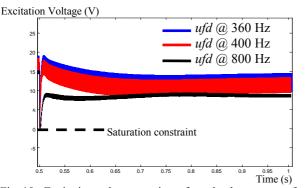


Fig. 18: Excitation voltage transient after a load power step from 150kW to 75kW

As a conclusion, the new standard we propose in Fig. 16 is met. Moreover, no saturation appears after the load step and the maximal distortion of the excitation voltage is about 30% of the average value of *ufd*. This can be considered as being a maximum admissible value and lower noise desensitization performances would have been unacceptable. This supposes that the weighting function Wu was appropriately chosen from a practical implementation point of view.

V. CONCLUSION

This paper has dealt with the use of optimal $H\infty$ control theory to prove that usual disturbance rejection standards can not be met for the studied aircraft power source. The best achievable frequency domain performances have then been found and translated in the time domain. This leads to the proposition of a new standard for aircraft power systems. This standard should be used if the synchronous generator + rectifier source is chosen for the future "All Electric"

aircraft. This source has the advantage to be lighter than the power source studied in [1]. But using a more "relaxed" standard could lead to oversize other power elements (for example the breakers). Then the weight gain obtained by the use of the proposed power source may be compensated by an increase in other power elements weight. That is why other power sources will be studied in future publications. In particular, sources with less stringent bandwidth should be studied as a controlled rectifier, for example. For these other power sources, the best achievable performances will be searched from a H∞ control point of view and compared together.

APPENDIX

The Park transform is defined by:

$$\begin{bmatrix} x_d \\ x_q \\ x_0 \end{bmatrix} = 2/3 \times \begin{bmatrix} \cos wt & \cos(wt - 2\pi/3) & \cos(wt + 2\pi/3) \\ \sin wt & \sin(wt - 2\pi/3) & \sin(wt + 2\pi/3) \\ 1/2 & 1/2 & 1/2 \end{bmatrix} \begin{bmatrix} x_a \\ x_b \\ x_c \end{bmatrix}$$

where (x_a, x_b, x_c) are the AC variables and (x_d, x_q, x_0) the rotating frame variables. The parameters of the power source are given in Table I:

TABLE I System parameters

Symbol	Description	Value
Rs	Stator windings resistor	11mΩ
Lls	Stator (d,q) axis leakage inductance	25,1μH
Lmd	Stator d axis magnetizing inductance	737μΗ
Lmq	Stator q axis magnetizing inductance	659μΗ
Rkd	Resistance of d axis damper windings seen	$33 \mathrm{m}\Omega$
	from stator	
Rkq	Resistance of q axis damper windings seen	$44 \mathrm{m}\Omega$
	from stator	
Rfd	Resistance of exciter windings	$3,6$ m Ω
Llkd	D axis damper leakage inductance	50,2μH
Llkq	Q axis damper leakage inductance	14,9μΗ
Llfd	Field winding leakage inductance	159μΗ
C	Output capacitor of the diode rectifier	2mF
Sn	Nominal power of the generator	209 kVA

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