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# Opportunistic Localization Scheme Based on Linear Matrix Inequality

*Localization in Smart Environments* special session

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**Abstract**—Enabling self-localization of mobile nodes is an important problem that has been widely studied in the literature. The general conclusion is that an accurate localization requires either sophisticated hardware (GPS, UWB, ultrasounds transceiver) or a dedicated infrastructure (GSM, WLAN). In this paper we tackle the problem from a different and rather new perspective: we investigate how localization performance can be improved by means of a cooperative and opportunistic data exchange among the nodes. We consider a target node, completely unaware of its own position, and a number of mobile nodes with some self-localization capabilities. When the opportunity occurs, the target node can exchange data with in-range mobile nodes. This opportunistic data exchange is then used by the target node to refine its position estimate by using a technique based on Linear Matrix Inequalities and barycentric algorithm. To investigate the performance of such an opportunistic localization algorithm, we define a simple mathematical model that describes the opportunistic interactions and, then, we run several computer simulations for analyzing the effect of the nodes duty-cycle and of the native self-localization error modeling considered. The results show that the opportunistic interactions can actually improve the self-localization accuracy of a strayed node in many different scenarios.

## I. INTRODUCTION

When dealing with mobile networks, the knowledge of the position and trajectory of the nodes represents a precious information that can be exploited for many different purposes, such as communication protocols optimization, path planning, cooperative task design and so on. The accuracy of the localization estimation is strictly related to the environment and the technology used by the devices to localize themselves. A cheap and widespread technology like the Received Signal Strength Indicator (RSSI) is very poor for localization [1], while more expensive hardware can achieve better performance, for instance by comparing the Time-of-Arrival of radio signals or using acoustic or optical signals or a rather complex infrastructure [2], [3], [4].

Whereas most of the literature on localization focus on systems and algorithms explicitly designed to provide localization functionality to the nodes, in this paper we investigate how localization can be obtained through opportunistic interactions in systems that are not intended for providing such a service. An example of scenario that falls within this category is the

swarm of robots, in which few robots are natively capable of self-localization, whereas the others may infer their own position by exchanging data with their neighbors on an opportunistic basis. Another example is that of a tourist at his first visit to a city that may desire to estimate his own position by opportunistically exchanging data with the passing-by vehicles equipped with GPS-localization system. Yet another example is the case of a sensor node deployed on a given area that needs to infer its position by exchanging data with mobile nodes (vehicles, persons, robots) that cross the area for different purposes.

Such a vision offers a number of research challenges, such as the definition of efficient node-discovery and link-set up protocols in presence of heterogeneous and multi-interface devices, the design of suitable algorithms for performing the opportunistic data exchange and the related localization estimate, the analysis of the tradeoffs between different performance indexes (energy consumption and protocol overhead vs. localization accuracy), not mentioning the reliability, confidentiality and security issues.

In this paper we address only a very focussed subset of these problems. More specifically, we investigate the probability that an opportunistic data exchange can take place for different choices of some design parameters, such as the radio coverage range, the nodes speed, the percentage of time that nodes spend looking for opportunistic interactions with other nodes. Then, we apply the results of this preliminary analysis to a localization technique based on the Linear Matrix Inequality (LMI) and a simple barycentric algorithm that is run by a strayed node, unprovided with any native localization equipment.

The remaining of the paper is structured as follows. In Section IV we present a short survey of the state of the art on standard and cooperative localization. In Section II we formally state the problem and we describe the system model. Section III reports the performance figures obtained through simulation and comments the results. Finally, Section V draws some conclusions.

## II. MODELING

### A. Definitions and problem statement

We consider a system made of mobile *Nodes* equipped with a common communication device (WiFi, Bluetooth or ZigBee). We suppose one node, called *User*, is not capable of self-localization, whereas the other nodes, named *Peers*, can perform self-localization with a certain accuracy that, in general, varies in time. A given Peer  $i$  can maintain a list of past *self-positioning estimations*. The problem we address is how self-positioning estimations of Peers can be used by User to estimate its own position.

### B. Communication model

Every node in the network is equipped with a common wireless communication interface that is used for (opportunistic) data exchange. Radio propagation is described by means of a simple unit-disk model, according to which the radio transmission is always correctly received within a distance  $R$  (*coverage range*) from the transmitter, whereas it is not received at longer distances. Although the unit-circle model is known to be oversimplified, it permits to isolate the performance analysis from the characteristics of the radio interface that, at this stage of the work, is left generic.

### C. Opportunistic interaction model

We assume that nodes can communicate only during a certain period of time, the so-called *Scan Phase*, which may correspond to an interlaced Inquiry/Scan phase of Bluetooth [5] or to the Active Scanning procedure of IEEE 802.11 systems [6]. The scan phase is repeated with period  $T$ , asynchronously and independently by each node, so that the offset between the scan phases of two nodes can be modeled as a random variable with uniform distribution in the interval  $(0, T)$ . The ratio between the scan phase and the entire cycle time  $T$ , is called *duty cycle* and denoted by  $\delta$ . Whereas the scan period  $T$  is the same for all the nodes, we suppose that each node can fix its own duty cycle depending on the requirements and the management policy of that node.

We suppose that opportunistic data exchange can occur (in a negligible time) only when the scan phases of the two nodes overlap in time. Furthermore opportunistic data exchange also requires the nodes to be mutually in range. We assume that opportunistic interaction immediately takes place as soon as both conditions are satisfied. Such an event is coined *rendez-vous*.

### D. Self-positioning model used by peers

We assume that peer nodes have “native” self-positioning capabilities, provided by some (non opportunistic) scheme. Accordingly, we denote by  $P_i$  and  $\hat{P}_i$  the real and the self-estimated position of peer  $\#i$ . Peers can be classified in different classes, depending on their native self-localization accuracy. For simplicity, we assume that the estimation error  $e_i = \|P_i - \hat{P}_i\|$  can be modeled as the module of a 2-dimensional Gaussian Random Variable  $[x(t) \ y(t)]$ , with zero mean and variance  $\sigma^2$ . The variance depends on the

localization class that for simplicity we assume to be the same for all nodes during simulations. Moreover, the error model considers two possible characteristics: correlation among consecutive estimations (considering a tracking-based technique) and degradation of the estimate in time, so that the positioning error is better modeled as a stochastic process  $e_i(t)$ , with the following characterization:

- At the time  $t = 0$ , the positioning error  $e_i(0)$  is the module of a zero mean 2-D Gaussian Random Variable  $[x(0) \ y(0)]$ , with standard deviation  $\sigma(0)$
- At the time  $t > 0$ ,  $e_i(t)$  is calculated from the two coordinates  $[x(t) \ y(t)]$  drawn according to the correlated Gaussian distribution:

$$f(x(t)|x(t-1); \rho) = \frac{\exp\left[-\frac{\bar{x}(t)^2 - 2\rho\bar{x}(t)\bar{x}(t-1) + \bar{x}(t-1)^2}{2(1-\rho^2)}\right]}{2\pi\sigma(t)\sigma(t-1)\sqrt{1-\rho^2}} \quad (1)$$

where  $\bar{x}(t) = \frac{x(t)}{\sigma(t)}$  and  $\bar{x}(t-1) = \frac{x(t-1)}{\sigma(t-1)}$ . The parameter  $\rho$  is the correlation coefficient, which can vary in the interval  $[0, 1]$ , where  $\rho = 0$  means independent samples and  $\rho = 1$  means completely correlated (equal) samples. The applies for the  $y$  coordinate.

The accuracy can degrade following the equation  $\sigma(t) = \sigma(0) + \alpha t$ , where  $\alpha$  is the drift of the estimation error.

During a rendez-vous, peer nodes send packets containing their estimated positions  $\hat{P}_i$  and the class of accuracy  $\sigma^2(t)$ . This information may then be used by the User node to estimate its own position by means of the opportunistic localization mechanism described below.

### E. Self-positioning model used by the user

As mentioned, the User node resorts to opportunistic localization to infer its geographical position. The opportunistic-positioning process requires the User to stop and stay at a fixed position for a given time interval  $W$ , during which the node collects the information opportunistically exchanged with passing-by Peer nodes. The localization time  $t$  is measured in number of scan periods, starting from  $t = 1$ . The opportunistic position estimation works in the following two stages.

- 1) At every scan period  $t$ , the User collects self-positioning estimations  $\hat{P}_i(t)$  from each peer that are within radio range and whose duty cycles overlap the User’s duty cycle (rendez-vous). Let  $eb_i = \max_t(e_i(t))$  denote an upper bound on the error between exact and estimated position of Peer  $i$ , so that

$$\|\hat{P}_i(t) - P_i(t)\| \leq eb_i \quad \text{for } t \geq 1 \quad (2)$$

Furthermore, let  $P_u(t)$  be the exact position of User. Assuming that communication is feasible only when the nodes are within the coverage range  $R$ , we then have

$$\|P_u(t) - P_i(t)\| < R \quad (3)$$

Therefore, for each Peer  $i$  within the range of User at time  $t$ , inequalities (2) and (3) yield the following

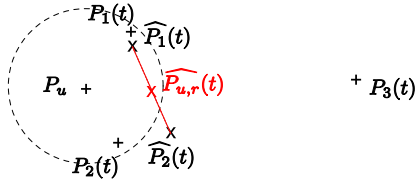


Fig. 1. Raw LMI-only estimation

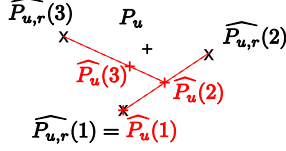


Fig. 2. LMI+barycentric estimation

triangular inequality

$$\|P_u(t) - \widehat{P}_i(t)\| \leq R + eb_i \quad (4)$$

Collecting the inequalities (4) for all the peers in the coverage range of User we get a Linear Matrix Inequality (LMI) that can be solved with standard techniques [7]. The resulting solution is used as a *raw (LMI) estimation*  $\widehat{P}_{u,r}(t)$  of the user position. Fig. 1 shows how  $\widehat{P}_{u,r}(t)$  is generated at cycle  $t$ , assuming that only  $P_1$  and  $P_2$  are within the User's range at time  $t$ .

- 2) When  $t > 1$ , the user can compute the barycenter of the primary estimations computed since  $t = 1$ . We define this barycenter as the self-positioning estimation of the user at time  $t$ :

$$\widehat{P}_u(t) = \frac{\sum_{k=1}^t w_k \widehat{P}_{u,r}(k)}{\sum_{k=1}^t w_k}, \quad t \geq 1 \quad (5)$$

where  $w_k$  is a weighting coefficient which is proportional to the number of Peers that have contributed to the  $k$ th raw LMI estimate.

This second stage is illustrated in Fig. 2, which shows how  $\widehat{P}_u(1)$ ,  $\widehat{P}_u(2)$  and  $\widehat{P}_u(3)$  are generated from  $\widehat{P}_{u,r}(t)$ ,  $t = 1, 2, 3$ , with all weights  $w_k$  equal to 1.

We have made numerous experiments with this model, and observed that in most cases, the self-positioning estimation improves over time. We therefore use the estimation only after a warm-up time denoted  $wu$  and measured in scan periods starting at  $t = 1$ .

### III. SIMULATION RESULTS

The models described in the previous section have been implemented using Matlab R2008b and its Robust Control Toolbox which provides an LMI solver. In this section we define a reference test case and study the impact of selected parameters, here the duty cycle  $\delta$ , the accuracy parameter

$\sigma(t)$  and the correlation parameter  $\rho$ . The impact of other parameters such as the number of peers within range, the range itself and the speed of peer nodes has been studied in other papers [8], [9] and will be briefly summed up.

#### A. Reference case

Our reference case involves  $N = 100$  peer nodes moving in a  $100 \text{ m} \times 100 \text{ m}$  square and one user node remaining at the center of this square. Peers and user share the same radio range  $R = 10$  meters, so that only a fraction of Peers are within range of the user at each time.

Peers and user also have the same scan period  $T = 1$  second and the same duty cycle  $\delta = 50\%$ , so that duty cycles are always partially overlapped. The scan period of the user starts at  $t = 0$  while the scan period of each peer starts with an offset uniformly distributed in  $(0, T)$ .

The self-positioning estimations of each peer are generated as follows. First, the trajectory is computed using the Random Pedestrian Mobility Model defined in [8]: this model is inspired by the Brownian movement, modified so that speeds are drawn from a Gaussian distribution  $N(1.2, 0.2)$  and at each time step the next direction is chosen in front of the pedestrian, *i.e.* in another Gaussian distribution centered on the previous direction, with a small standard deviation arbitrarily set to  $\sigma_{\text{dir}} = \pi/6$ . The trajectory is kept within the considered square area. Second, for each position a self-estimation is produced using the peer self-positioning model defined in Section II-D. In the reference case, the accuracy class of each peer has been set to  $\sigma = 1$  meter and it is assumed constant over time, *i.e.*  $\alpha = 0$  m/s. Furthermore, the self-positioning estimates are not correlated, *i.e.*  $\rho = 0$ . In practice, each peer self-position estimation at cycle  $t$  is randomly drawn in a disc centered around the exact position of the peer at cycle  $t$ , using a 2D Gaussian distribution;  $eb_i$  is the value such that  $[0, eb_i]$  is the 99 % confidence interval for the positioning error module  $e_i(t)$ . Different settings for the self-positioning model will be tried later in this section.

User, placed in the center of the area, estimates its position using the opportunistic localization model defined in Section II-E. The opportunistic-localization time for the user is set to  $W = 2$  minutes and the warm-up time is set to  $wu = 30$  seconds. We will also see what happens for shorter and longer waiting times. The performance of the User's opportunistic-positioning scheme is evaluated in terms of distance between real and estimate position  $\|P_u - \widehat{P}_u(t)\|$ .

Table I sums up the parameter values used for the reference case.

*Accuracy of the reference case:* The reference case has been run 30 times with different random seeds. The *accuracy*  $A$  of each run is the average localization error after the warm-up time. The results, in terms of localization error of the user node, strongly differ from one run to the other, as illustrated by Fig. 3. The mean of the accuracy over 30 runs is  $\mu_A = 1.13$  m and the standard deviation is  $\sigma_A = 0.45$  m, while the worst case has an accuracy of 2.28 m. These wide variations are likely to be ascribed to the different trajectories of peers in

TABLE I  
REFERENCE CASE PARAMETERS

$N$	100 peers	$R$	10 m
$T$	1 s	$\delta$	50 %
$\mu_{\text{speed}}$	1.2 m/s	$\sigma_{\text{speed}}$	0.2 m/s
$\mu_{\text{dir}}(t)$	$\text{dir}(t-1)$	$\sigma_{\text{dir}}$	$\pi/6$
$\sigma_i$	1 m	$\alpha$	0 m/s
$\rho$	0	Square	$100 \times 100$ m
$wu$	30 s	$W$	120 s

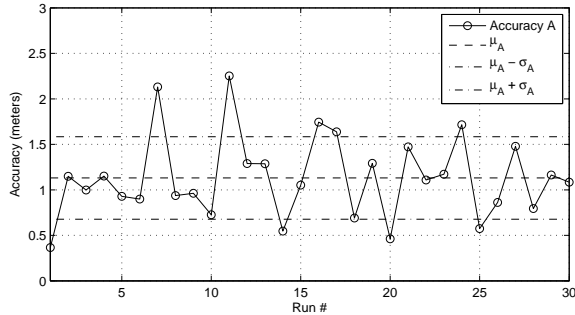


Fig. 3. Reference case runs

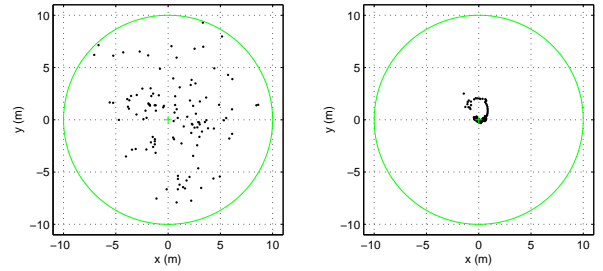
different runs. In fact, depending on the random seed of the run, peers may be widely spread in space, thus permitting good LMI-only localization and, in turn, good LMI+barycenter estimation, or they may be unevenly distributed in the area forming a small number of groups, a situation that yields to poor LMI-only localization and, consequently, to a degradation of LMI+barycenter performance.

To better understand the behavior of the protocol, we report in Fig. 4(a) the successive user's raw LMI estimations for a single run and in Fig. 4(b) the self-localization estimations of the user using LMI and barycenter algorithm. In Fig. 4(b), the oldest plots are "far" from the user position and gradually get closer, while in Fig. 4(a) old and new positions are equally distributed around the user position. The barycentric estimation clearly improves over time, and is better than the raw one. This is remarked in Fig. 4(c), where the reader can compare the evolution of the raw error  $\|P_u - \widehat{P}_{u,r}(t)\|$  and the error of the barycentric approach  $\|P_u - \widehat{P}_u(t)\|$ . The run-wide accuracy  $A$  is also plotted.

In most runs, the accuracy of the barycentric estimation tends to improve over time: each additional raw LMI estimation contributes to improve the estimation, since new information is added.

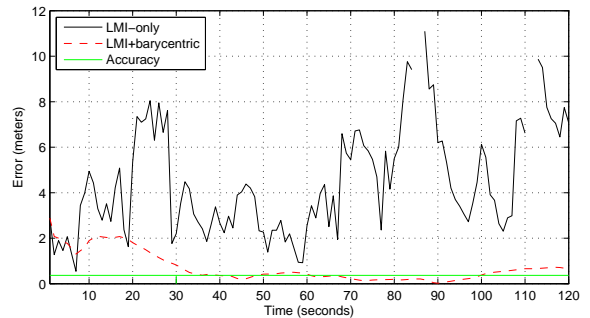
### B. Duty cycle impact

In this section we measure the impact of the duty cycle length. There is clearly a trade-off between rendezvous probability (long duty cycle) and energy consumption (short duty cycle). We have run the simulation 30 times for two additional values of duty cycle  $\delta$ : 20 % and 40 %, the other parameters being the same as for the reference case above. The results are summed up in Table II, where the last line is a reminder of the test case.



(a) LMI-only est

(b) LMI+bary est



(c) Error comparison

Fig. 4. Reference case run #1/30.

TABLE II  
DUTY CYCLE IMPACT

$\delta$	$\mu_A$	$\sigma_A$	retained
20 %	2.40 m	1.18 m	1.13 peers
40 %	1.54 m	0.54 m	2.38 peers
50 %	1.13 m	0.45 m	3.01 peers

As expected, accuracy improves when the duty cycle increases thanks to the higher number of peer self-positioning estimations that improves the performance of the raw LMI location estimation scheme and, in turn, the barycentric estimation.

### C. Peers self-positioning impact

In this section we measure the impact of the self-positioning model characterizing peers. To this end, we consider three different parameters: first, the correlation coefficient  $\rho$  among successive self-positioning estimations of each peer; second, the self-positioning accuracy class  $\sigma$  of peers; third, the accuracy drift  $\alpha$  of peers. The other parameters are set to the values of the reference case.

Table III gathers all the results. As it can be observed, the parameters have negligible impact on the accuracy of the opportunistic localization scheme that, hence, proves to be rather robust to localization errors of Peers. This is likely due to the fact that, despite the errors, the positions provided by the Peers form a uniform "cloud" of points around the User. Then, applying the barycentric scheme, the User always localizes itself near the center of such a cloud. To verify this conjecture, however, we plan to consider in future work other error models



TABLE III  
CORRELATION IMPACT

$\rho$	$\sigma_i$	$\alpha$	$\mu_A$	$\sigma_A$
0.4	1 m	0 m/s	1.14 m	0.46 m
0.9	1 m	0 m/s	1.15 m	0.48 m
0.99	1 m	0 m/s	1.19 m	0.48 m
0	3 m	0 m/s	1.18 m	0.49 m
0	5 m	0 m/s	1.24 m	0.54 m
0	1 m	0.01 m/s	1.14 m	0.45 m
0	1 m	0.03 m/s	1.15 m	0.46 m
0	1 m	0.1 m/s	1.23 m	0.48 m
0	1 m	0.3 m/s	1.62 m	0.62 m
0	1 m	0 m/s	1.13 m	0.45 m

for peers estimation, such as model for pedometers, or for MEMS-based inertial navigation systems, or for RSS-based landmarks.

#### D. Other parameters

In previous papers [8], [9], we also studied the impact of other parameters; we showed that the accuracy of the user self-positioning scheme degrades when: the amount of peers within range ( $N$ ) decreases, the range threshold  $R$  increases or the peers mean speed  $\mu_{\text{speed}}$  decreases. We re-evaluate these parameters and others quickly here.

For the setup used here, using 50 peers give a mean accuracy of 1.76 m while 200 peers give a mean accuracy of 0.77 m (this is not as overcrowded as it may seem, if you think of a station, a big mall or a conference room for instance: in a  $100\text{m} \times 100\text{m}$  square, this gives  $50 \text{ m}^2$  per peer). Of course, the more peers there are with random trajectories, the more communication opportunities there are, and the more information are fed to the LMI system, which induces better estimations.

Another way to improve the accuracy is to increase the waiting time of the user: 5 minutes lead to an accuracy of 0.91 m. In that case, the barycentric estimation takes into account more and more raw LMI estimations, thus giving less weight to bad raw estimations. On the contrary, reducing to 1 minute degrades the accuracy to 1.67 m.

We also changed the radio coverage range. A 5 m range leads to an accuracy of 1.01 m, while a 20 m range leads to an accuracy of 1.86 m. This is not an intuitive result, since a larger range would mean more opportunities for sharing information. However, these additional positions are more far away from the user, which increase both the raw LMI error and the barycentric error.

Finally, we also changed the mean peer speed. If peers are slow (0.6 m/s) the accuracy degrades to 2.14 m. If peers are fast (3 m/s) the accuracy improves to 0.68 m. When the speed increases, positions taken into account will largely vary between two successive LMI-only estimations. This diversification of spatial information improves the behavior of the barycentric estimation.

## IV. RELATED WORK

Self-localization problem has been investigated in a number of papers. Most common localization methods consist in

measuring the power of the received RF signal (RSSI), the Time of Arrival (ToA) or the Angle of Arrival (AoA) of the RF signals from the beacons. In this way, every node estimates a set of distances from the beacons and, then, guesses its position by means of lateration and triangulation techniques [10], [11] or by using statistical estimation methods [12]. Overviews of localization techniques based on RSSI and ToA measurements can be found in [13], [14], [15]. Multi-step localization techniques, which involve a number of successive refinement phases, have been proposed by Savarese [16] and Savvides [11]. Other solutions leveraging on specialized and complex hardware and infrastructure are given in [3], [2], [4]. When nodes (either static or mobile) can detect each other, then it is possible to devise cooperative position estimate techniques, which are very well studied in robotics. In [17] the authors utilize Markov localization for self-localize nodes and, then, probabilistic methods to synchronize robots estimate when they have a contact. Collective localization based on a distributed Kalman Filter is proposed in [18], whereas an anchor-free approach where robots infer their position estimate on the basis of the only information exchanged among them is proposed in [19].

In [7] Doherty et al. pioneered the use of semidefinite programming (SDP) methods in the localization problem. The problem is considered as a bounding problem containing several convex geometric constraints mathematically represented as linear matrix inequalities (LMI). The mechanism proposed in this paper is based on this approach, taking into estimation errors and introducing a barycentric improvement over time.

The Centroid localization method [20] is developed to estimate the user's location by computing the barycenter of all the positions received from those fixed beacon nodes. To find the optimum deployment of those beacon nodes for a given application may consume a lot of labor.

In the APIT method [21], a user chooses three beacon nodes around him as the triangle vertex point and uses the APIT algorithm to test if he is lying in the triangle. If the APIT test can be passed, i.e., at least one node's signal is becoming barycenter of the triangle will be taken as the location estimation of the user. Continuously, another different three nodes will be chosen to face the APIT test again. If the new test can also be passed, the barycenter of the intersection of the triangles will be used. By analogy, the user will repeat this APIT test until all combinations are exhausted or the satisfying accuracy is achieved. It is noticeable that since the APIT test is used under the condition of static beacon nodes, accomplishing it is still not an easy thing. Additionally, the APIT test may fail in less than 14% of the cases [21].

Other research works jointly solve the time synchronization and localization problems. For instance, Enlightness [22] relies on the availability of beacon nodes (at least 5% of the nodes) providing absolute time and space information, like the GPS in outdoor environments. Enlightenment combines recursive positioning estimation [23] with a clock offset estimation scheme based on the measure of beacon packet delays and

timestamps.

In [24], an advanced integration of 802.11b equipments and Inertial Navigation System (INS) is used to enhance the performance of the indoor positioning system. As a result, a system performance close to the meter accuracy can be achieved with a low density of access points in the environment, provided that users carry inexpensive INS equipment.

## V. CONCLUSION AND FUTURE WORK

In this paper, we propose an algorithm in which a still user infers localization information using the positions of other passing-by nodes. The opportunistic interaction is modeled by considering several parameters that permit to compare the performance of the scheme in different scenarios.

In all the cases considered in this study, we obtained a localization error lower than 2.5 meters that can be reduced to less than 1 meter with an accurate tuning of the system parameters. In particular, the duty cycle of the opportunistic-scan phase has been observed to have a significant impact on the user self-positioning estimation: the shorter the duty cycle the less the rendezvous probability with peers and, in turn, the lower the localization accuracy. Furthermore, we observed that the proposed opportunistic localization scheme is rather robust to the self-positioning error model for Peers. In fact, the correlation, the standard deviation and the drift of the self-positioning error do not significantly affect the localization accuracy, provided that the algorithm is performed over the data gathered with a large enough number of opportunistic exchanges.

In order to complete this work, some improvements will be done. We will try to define a more realistic set-up involving different types of peer nodes, e.g. access points with well-known positions but only partial coverage and mobile peers carrying cheap INS systems which accuracy drifts over time. We will also implement the opportunistic meeting model defined in [25] that applies to peer meetings. It is also possible to take into account different self-localization models and opportunistic update.

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