

# Logic controllers dependability verification using a plant model

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**DESDES 2006**

**Rydzyzna, Poland; September 26-28, 2006**

**3<sup>rd</sup> IFAC Workshop on Discrete-Event System DESign**

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# Outline

**Context and objective of the work**

**DES modeling for verification purposes**

**Modeling complex plants**

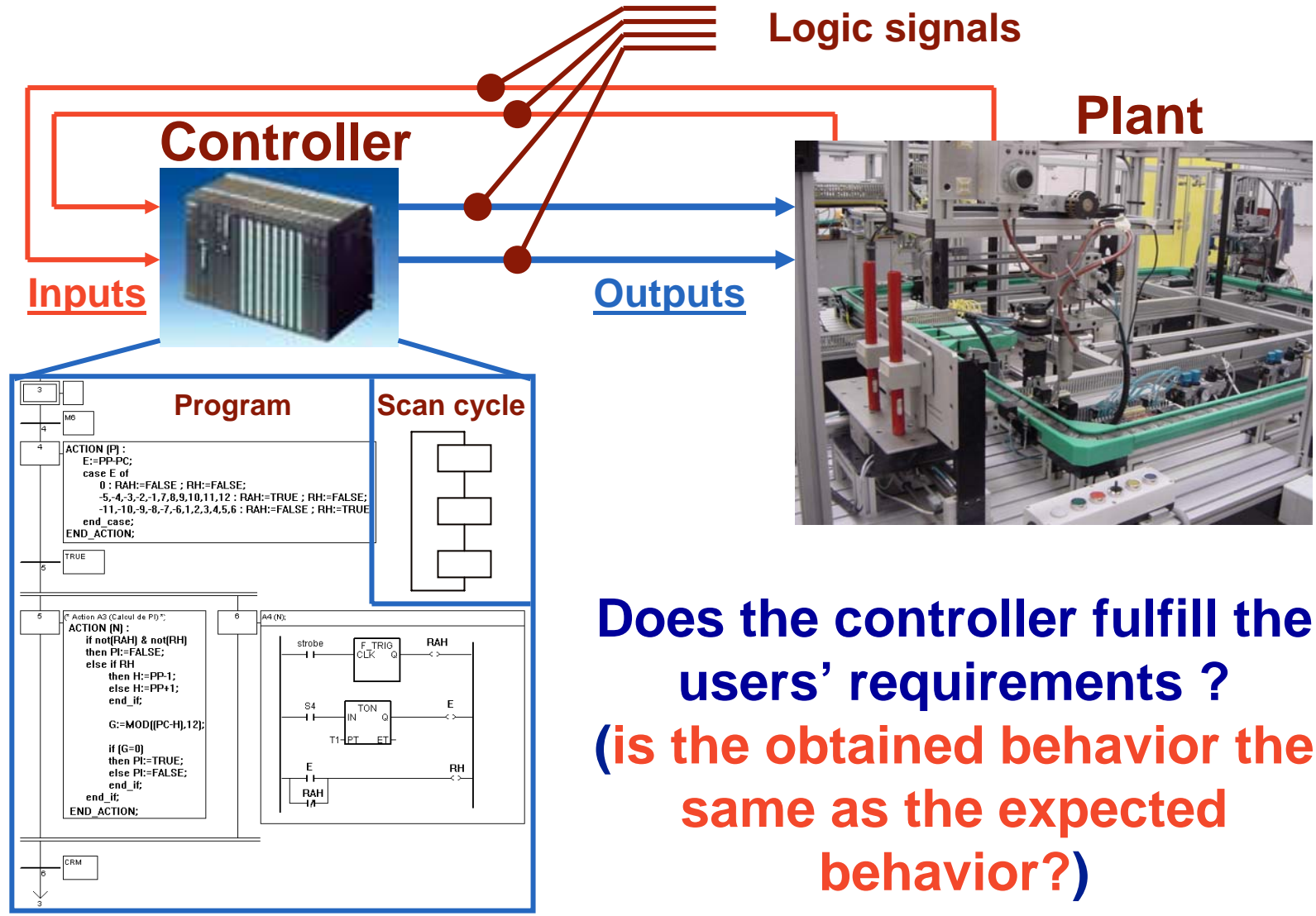
**Modeling closed loop DES**

**Case study**

**Formal verification results**

**Conclusions and prospects**

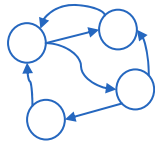
# Automated systems considered



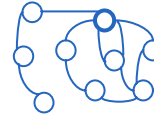
**Does the controller fulfill the users' requirements ?  
(is the obtained behavior the same as the expected behavior?)**

# Formal verification using model-checking

Formal  
representation  
of a system  
(DES model)

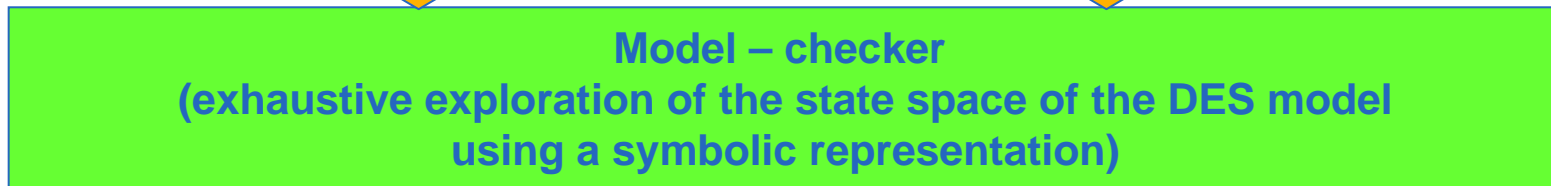


Satisfies ?



$AG (( dp\_head\_motor\_up ) =>$   
 $EF (!dp\_head\_motor\_up ))$

Formal  
representation  
of a property  
(temporal logic,  
observer automaton)



Property proved or counterexample  
in case of negative proof

The model to be verified is obtained either from the controller only  
(Non Model-Based approach) or from the whole system (Model-Based approach)

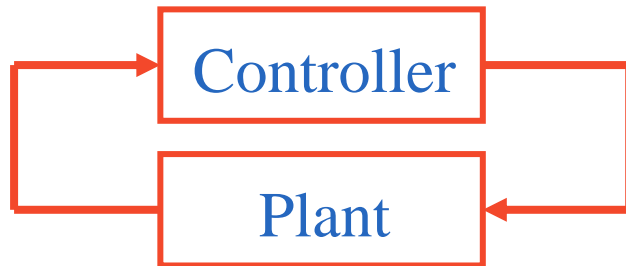
## Non Model-based and Model-based Model-Checking

- Non (Plant) Model Based (NMB) [Probst *et al.* 1997] [Bornot *et al.* 2000] [Mertke & Frey, 2001] [Rossi, 2004]



Focus is put on properties proof of the **isolated controller**

- (Plant) Model-Based (MB) [Kowalewski & Preußig, 1996] [Raush & Krogh, 1998] [Zaytoon & Carré-Ménétrier, 1999] [Mertke & Menzel, 2000] [Hanisch, 2006]



Focus is put on properties proof of the **closed loop system**

- Constraints-based approach: simplified version of MB

## Non Model-Based and Model-Based Model-Checking

### Which approach must be chosen ?

- NMB:
  - Properties are proved whatever the values of the controller inputs
  - All the plant behaviors (realistic and unrealistic) are considered
- MB:
  - Properties are proved only for realistic combinations of the controller inputs
  - An other model (plant model) is mandatory
  - Building a plant model is a difficult task for large scale industrial systems



**These approaches have never been compared**

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# DES modeling for verification purposes

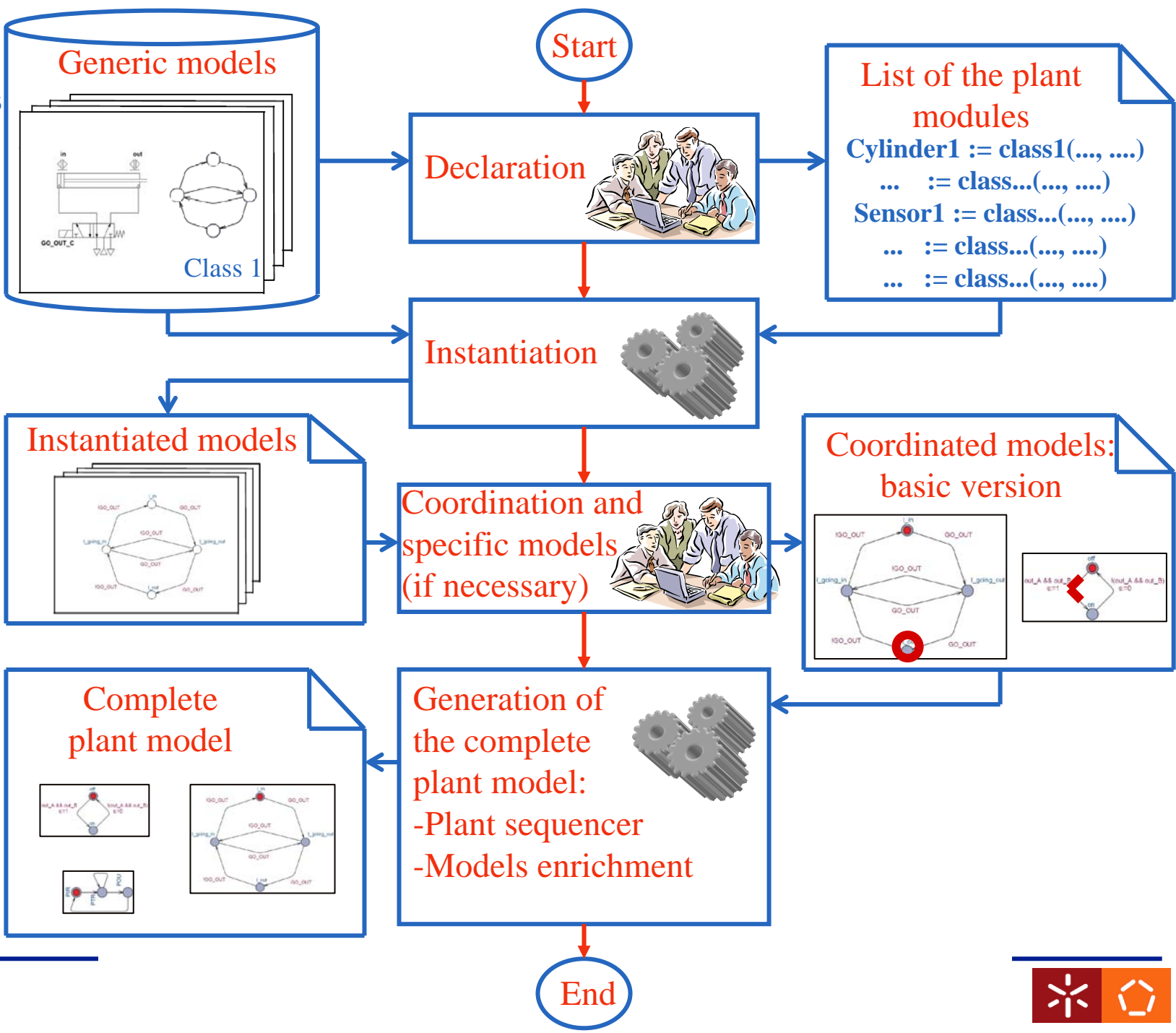
## Proposition of a method to build complex plant models

- Generic and modular
- As automated as possible
- Based on a suitable class of automata

## Proposition of algorithms to obtain the “ready-to-check” model of the closed-loop system

- Aim: to avoid constructing explicitly the model of the whole system by using automata products that always lead to combinatory explosion and often include unexpected behaviors
- Main feature: set of communicating sequencers (plant, controller and system sequencers)

# Building complex plant models

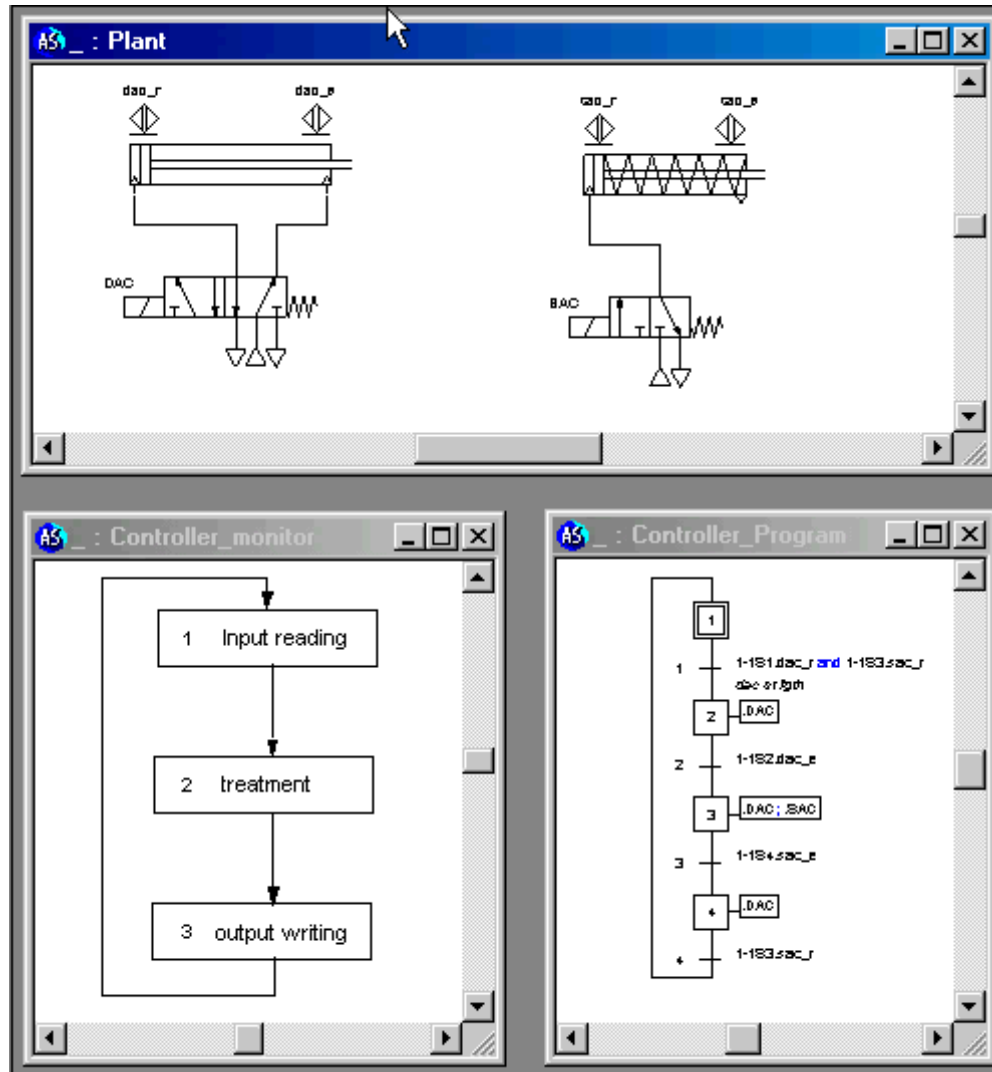




### Non deterministic and communicant automata (inspired by [Bengston and Yi, 2004])

- An automaton  $A$  is a triplet  $\langle N, n_0, \Sigma \rangle$  where :
  - $N$  is a finite set of states;
  - $n_0 \in N$  is the initial state;
  - $E \subseteq N \times \tau \times \Sigma \times N$ , is the set of transitions, with
  - $\tau$  being a set Boolean expressions defined on the set of logic variables  $V$ , and
  - $\Sigma$  a partition of the set of assignments on  $V$ ;
- An automata network  $\{A_1, \dots, A_n\}$  is a set of automata such as:
  - Boolean expressions  $\tau$  associated with the transitions are defined on the same set of logic variables  $V$ ;
  - Within the network the evolutions are asynchronous;
  - At each instant only one transition of one automaton can be fired;
  - Communication between automata is based on variable sharing.

# Taking into account physical behaviors



Controller evolution faster than plant evolution

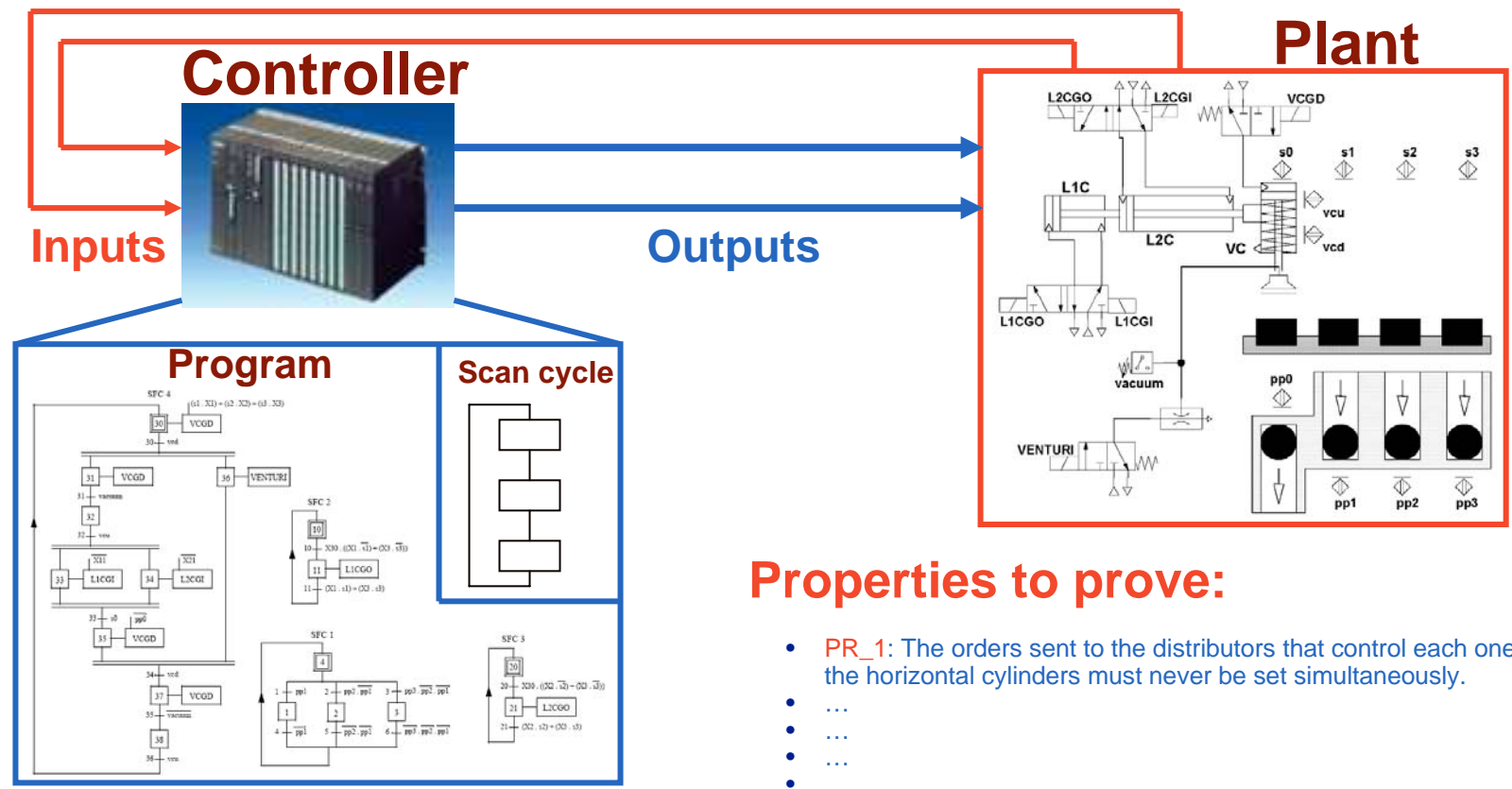
Asynchronous evolutions between controller and plant;

and

Synchronization between plant and controller during the inputs reading and outputs updating phases



# System overview

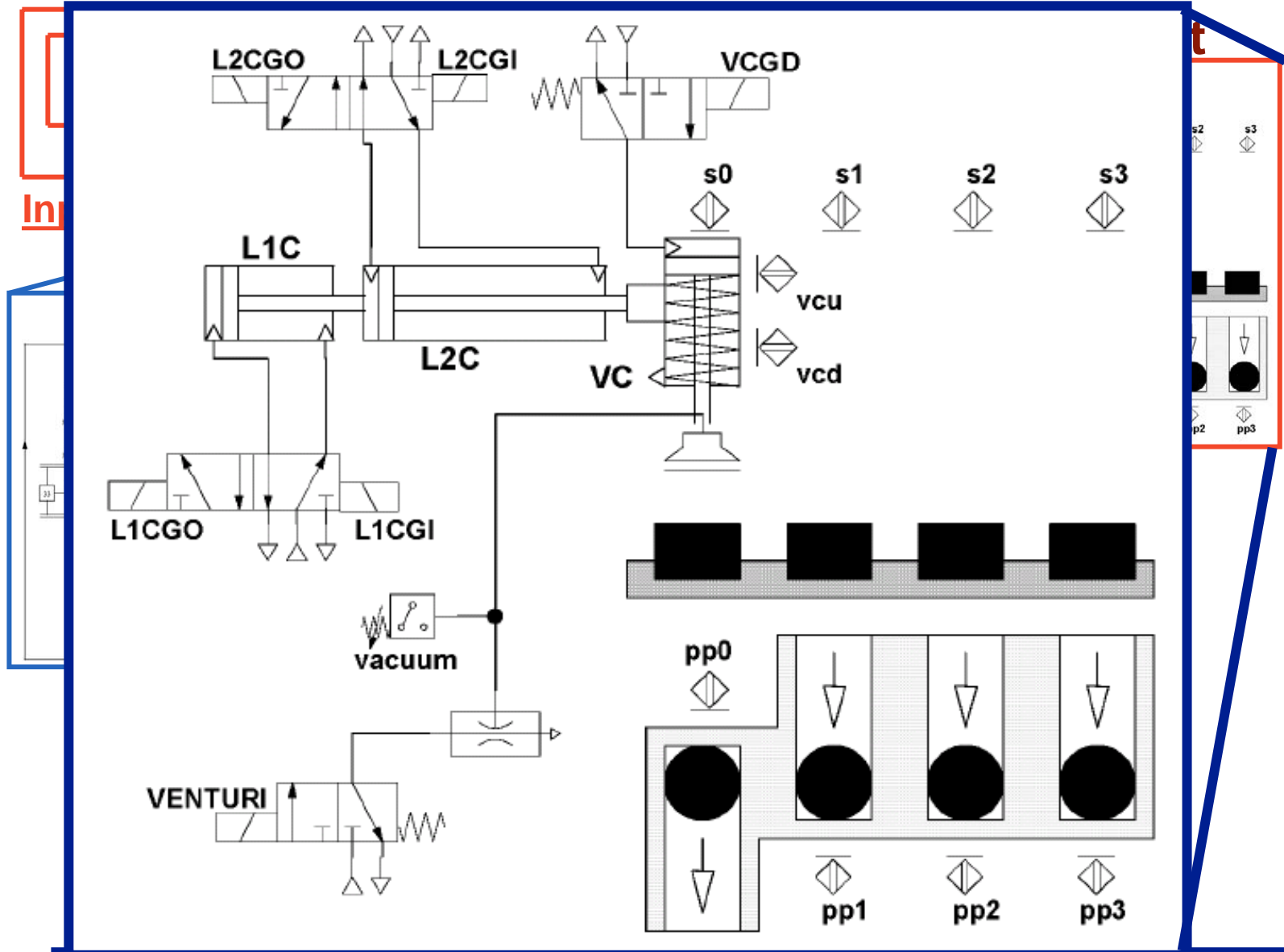


## Properties to prove:

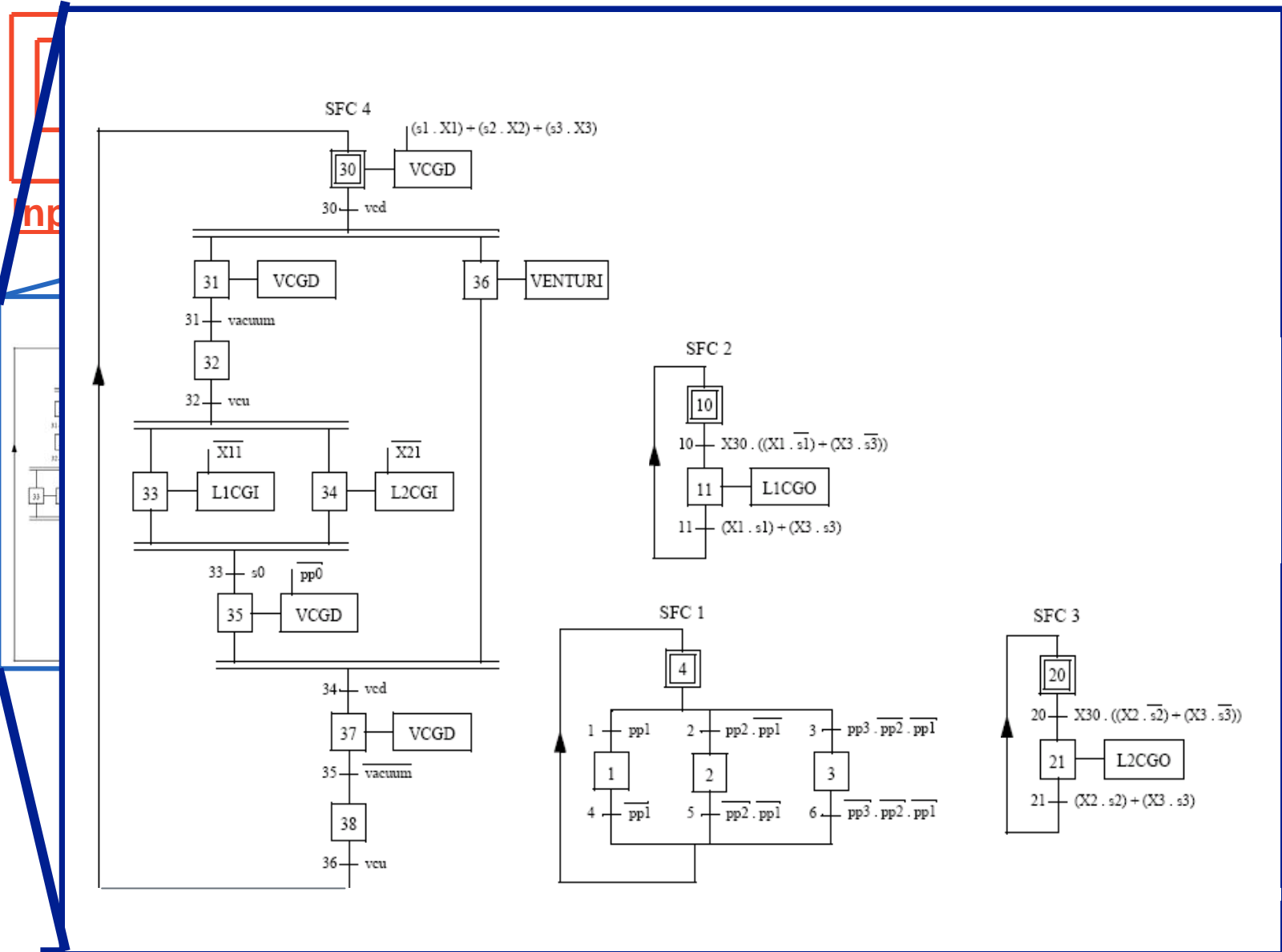
- PR\_1: The orders sent to the distributors that control each one of the horizontal cylinders must never be set simultaneously.
- ...
- ...
- ...
- ...
- ...
- PR\_7: If a part is detected by a sensor  $ppi$  ( $i \in [1,2,3]$ ), then, in the future, the rod of one of those cylinders will move outwards
- ...
- ...
- ...



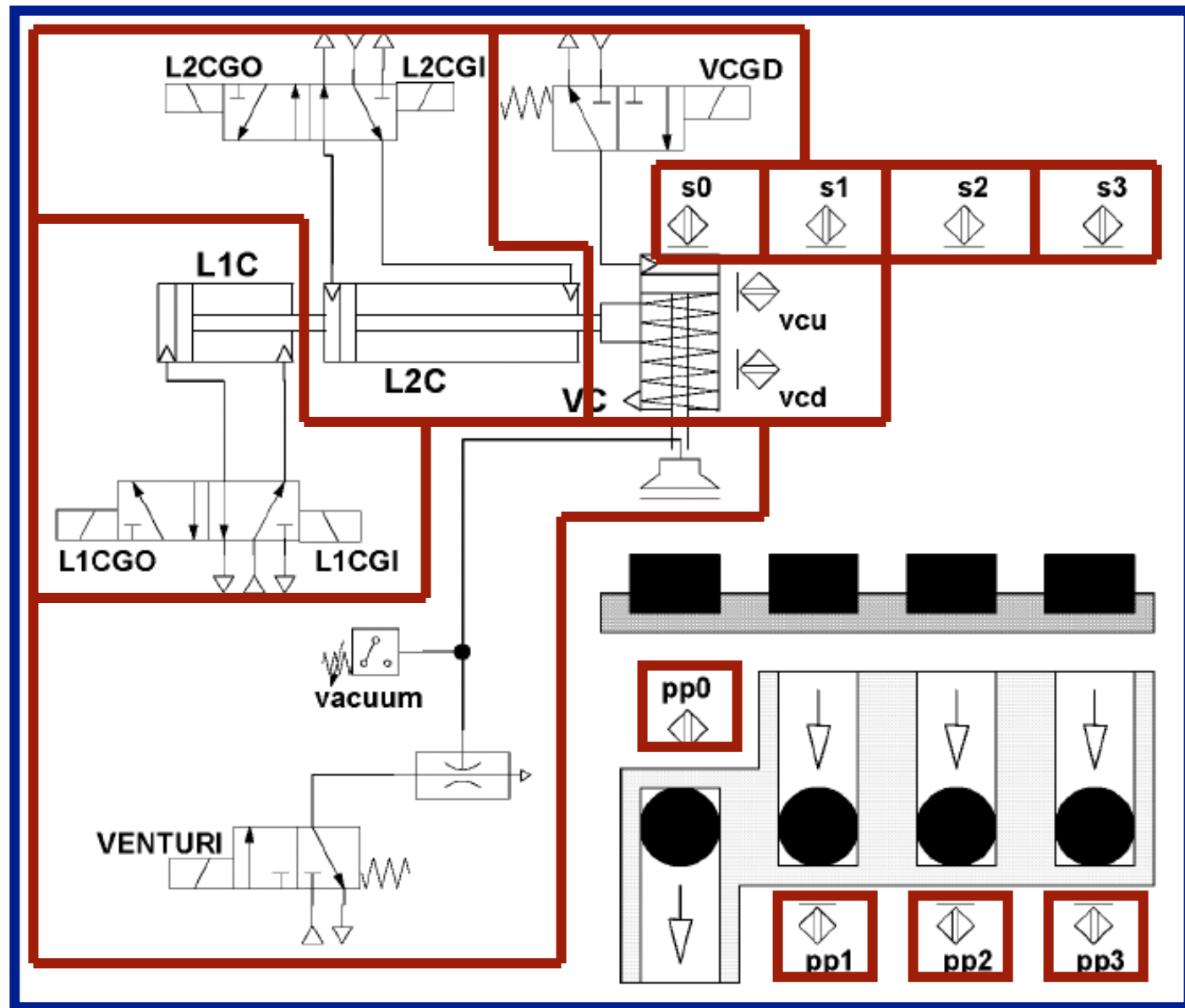
# Plant layout



# Controller program



## Modeling the plant: considered modules



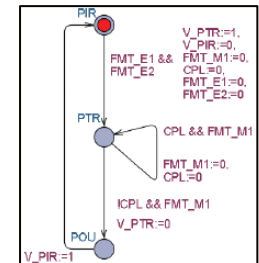
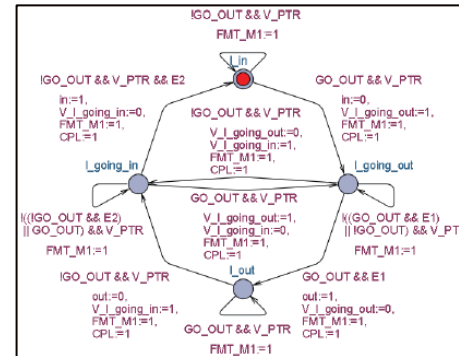
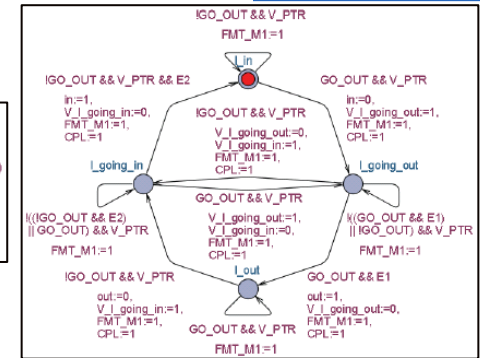
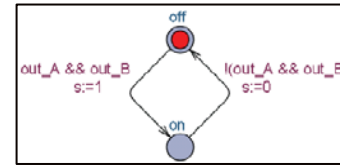
# Plant model construction

According to the 4 steps method presented above

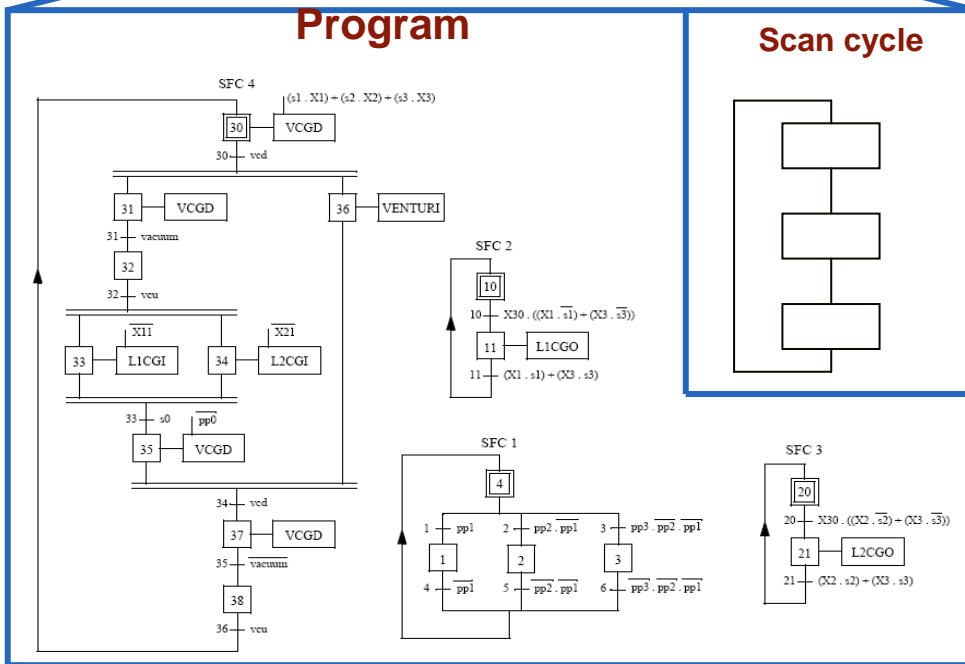
Result: a set of communicating automata and one plant model sequencer (automatically constructed)

Interest of this approach: no automata product is performed, only sequencing of automata is necessary

Extract of the plant model

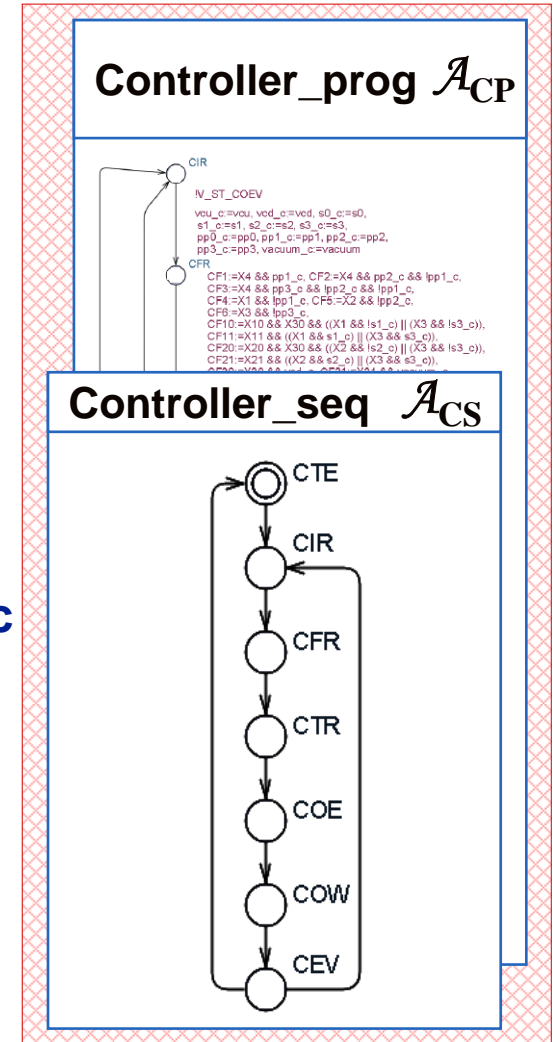


# Controller model



Automatic Translation

Via algebraic modeling





# Properties models

### Prop\_seq $\mathcal{A}_{PrS}$

### List of CTL and/or LTL formulae:

Pr\_1.1:  $AG \neg (L1CGO \wedge L1CGI \wedge (PEAC \vee PEAP))$

...

Pr\_7.1:  $AG((pp1 \wedge (PEAC \vee PEAP)) \Rightarrow EF(V P6 \wedge (PEAC \vee PEAP)))$

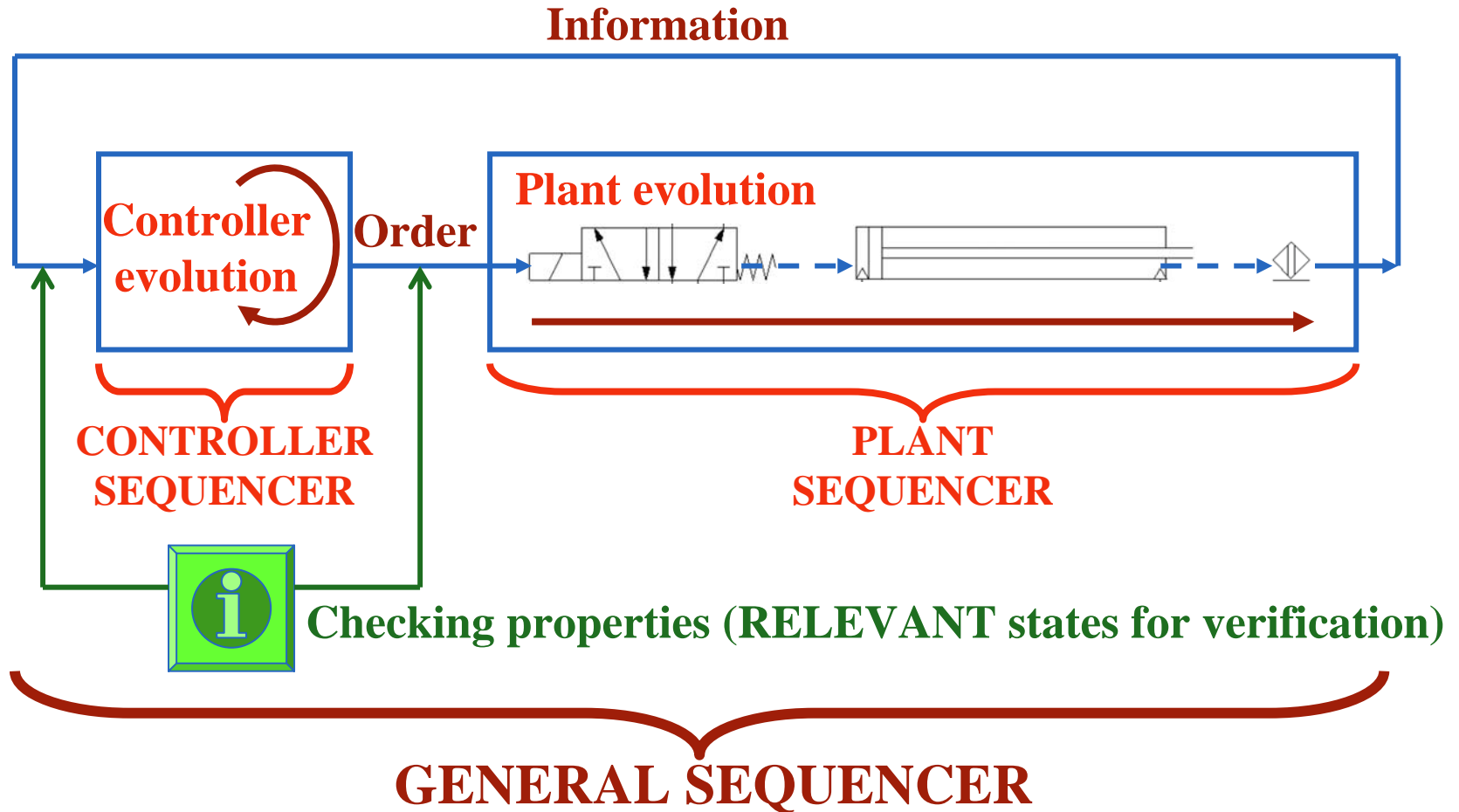
...

### PR\_4 $\mathcal{A}_{Pr_4}$

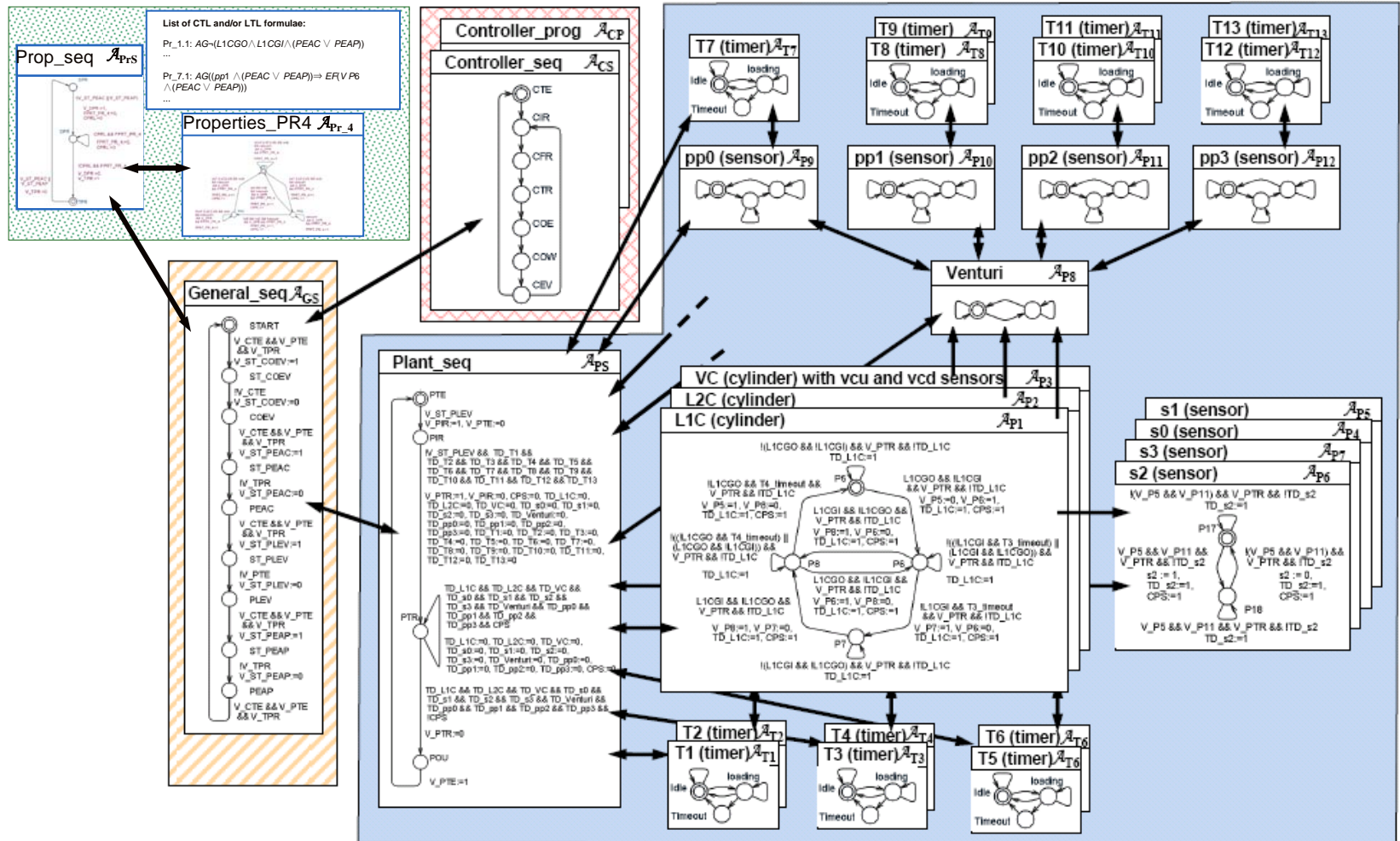
## Two kinds of properties: Safety and Liveness properties

- the two opposite commands of the horizontal cylinder must never be simultaneously set
- the manipulator takes the part at the picking position and doesn't release it until the placing position is reached

# Modeling the closed-loop system



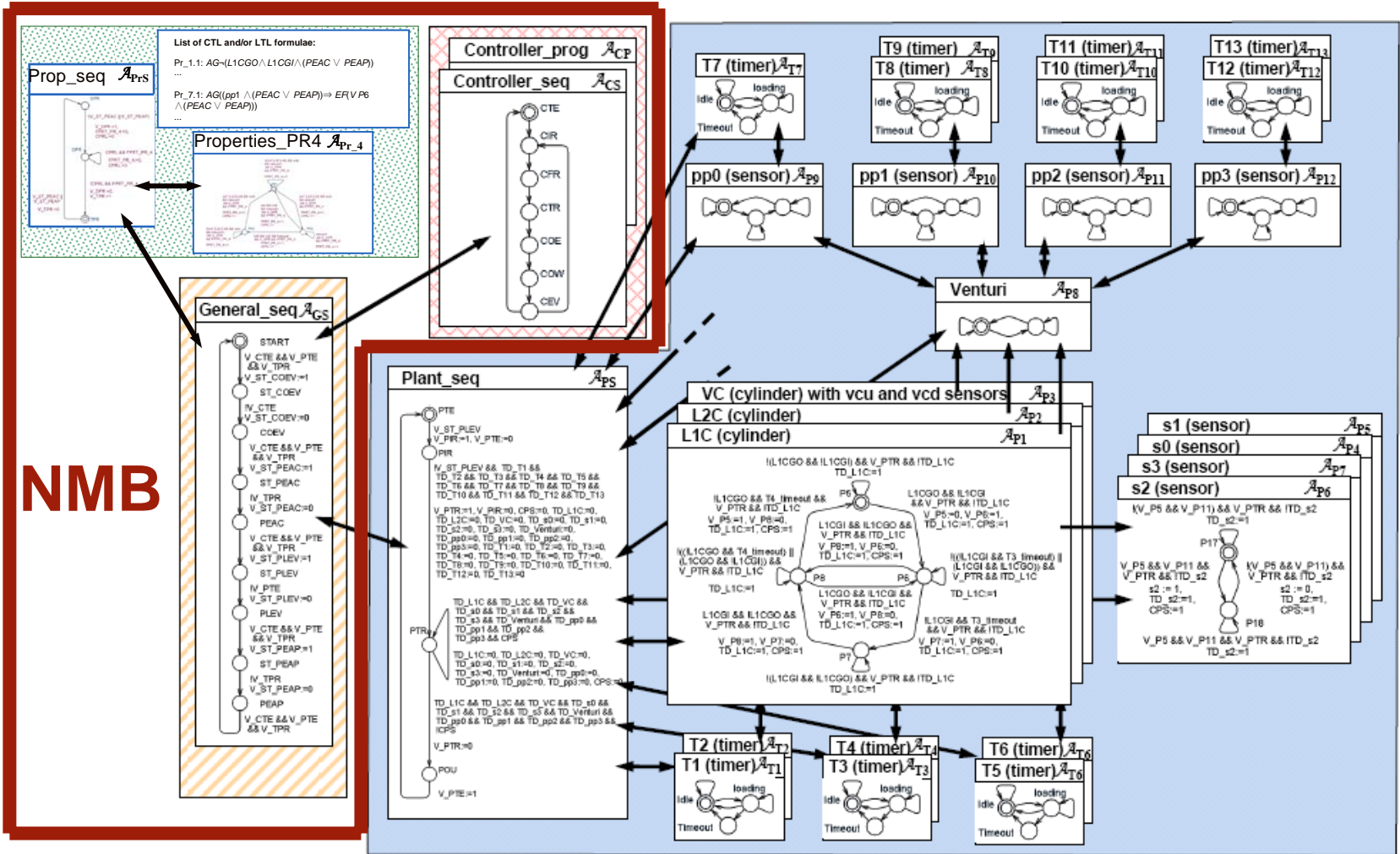
# Overall model



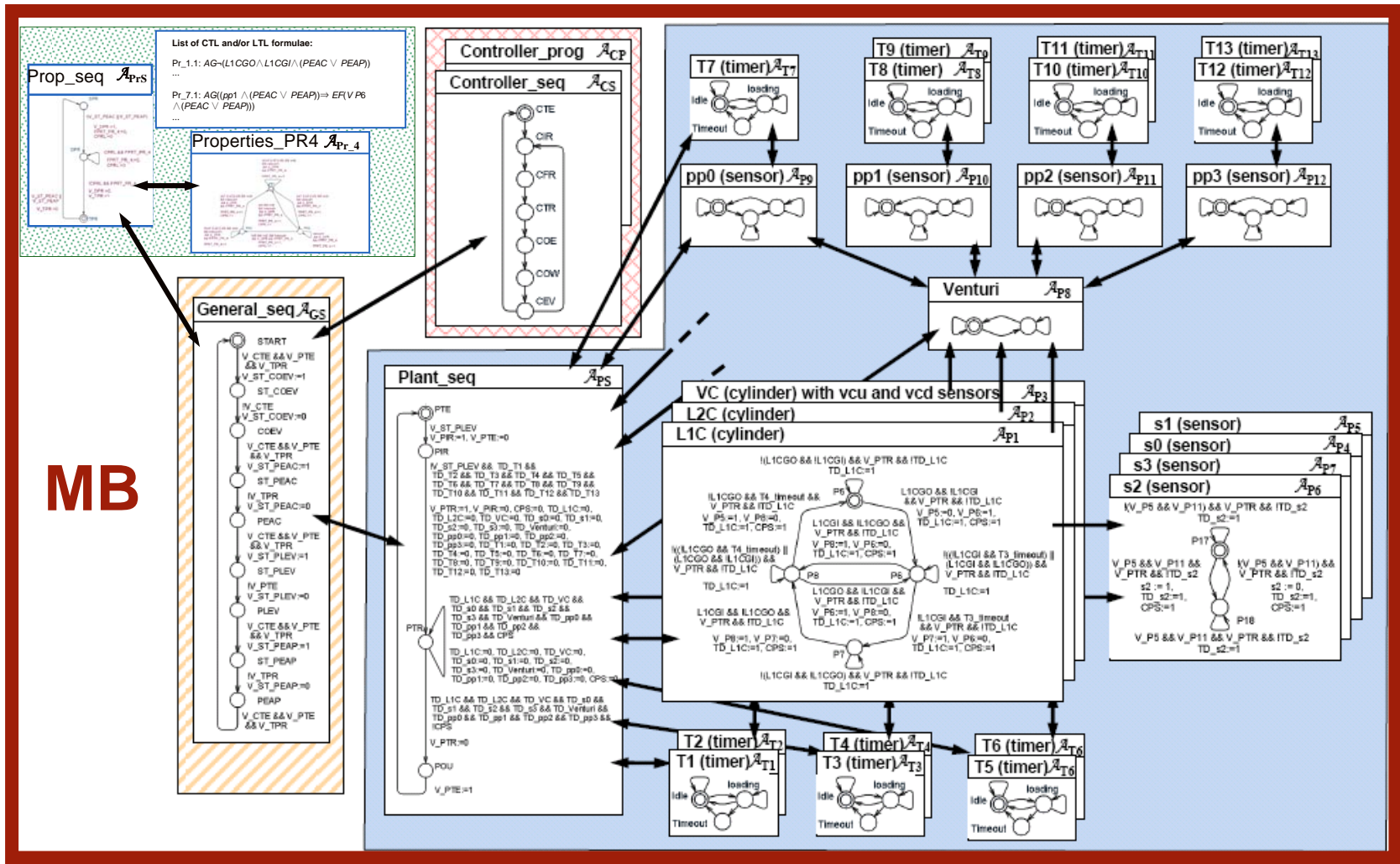
42 safety and liveness properties have been verified with NuSMV running on a computer with a P4 CPU at 2.54GHz and 2GB RAM



# Using the overall model for formal verification



# Using the overall model for formal verification



## Case of identical answers

Prop	Type	NMB	MB
PR_1	Safety	<u>true</u>	<u>true</u>
PR_2	Safety	<u>true</u>	<u>true</u>
PR_3	Safety	false	true
PR_4	Safety	false	true
PR_5	Safety	X	true
PR_6	Liveness	<u>true</u>	<u>true</u>
PR_7.1	Liveness	X	true
PR_7.2	Liveness	X	true
PR_7.3	Liveness	X	true
PR_8.1	Liveness	<u>true</u>	<u>true</u>
PR_8.2	Liveness	<u>true</u>	<u>true</u>
PR_8.3	Liveness	<u>true</u>	<u>true</u>
PR_9	Safety	X	true

The approach  
that yields the  
more  
meaningful  
results  
must be chosen

X means 'absence of answer'

## Case of contradictory answers for safety properties

Prop	Type	NMB	MB
PR_1	Safety	true	true
PR_2	Safety	true	true
PR_3	Safety	<u>false</u>	<u>true</u>
PR_4	Safety	<u>false</u>	<u>true</u>
PR_5	Safety	X	true
PR_6	Liveness	true	true
PR_7.1	Liveness	X	true
PR_7.2	Liveness	X	true
PR_7.3	Liveness	X	true
PR_8.1	Liveness	true	true
PR_8.2	Liveness	true	true
PR_8.3	Liveness	true	true
PR_9	Safety	X	true

Requires  
complementary  
analysis

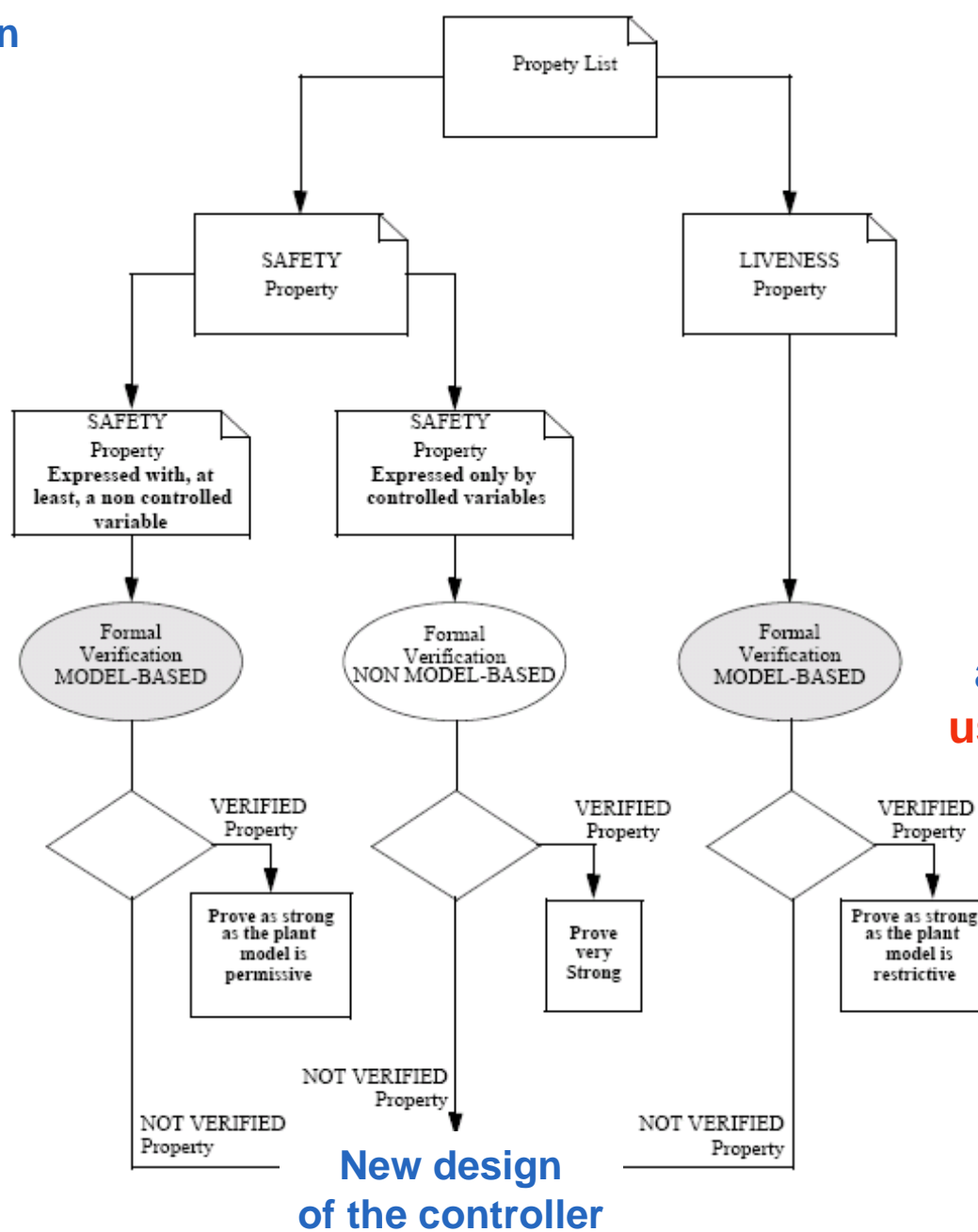
## Absence of answer with the NMB approach

Prop	Type	NMB	MB
PR_1	Safety	true	true
PR_2	Safety	true	true
PR_3	Safety	false	true
PR_4	Safety	false	true
PR_5	Safety	<u>X</u>	<u>true</u>
PR_6	Liveness	true	true
PR_7.1	Liveness	<u>X</u>	<u>true</u>
PR_7.2	Liveness	<u>X</u>	<u>true</u>
PR_7.3	Liveness	<u>X</u>	<u>true</u>
PR_8.1	Liveness	true	true
PR_8.2	Liveness	true	true
PR_8.3	Liveness	true	true
PR_9	Safety	<u>X</u>	<u>true</u>

The property can be proved only by taking into account the plant behavior



# Formal verification results



**PROPOSITION:**  
Decision tree taking into account the kind of properties and the variables used in the property



## Conclusions and prospects

Proposition of a **method** to build complex plant models

Proposition of **algorithms** to obtain the “ready-to-check” model of the closed-loop system without combinatory explosion nor unexpected behaviors

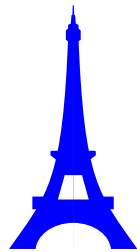
Proposition of a decision tree to choose the most appropriate approach (NMB/MB)

To apply these techniques to timed systems (using the UPPAAL model-checker)

To introduce faulty behaviors in the plant model so as to check controller behavior in the presence of plant faults



1<sup>st</sup> IFAC Workshop on  
**Dependable Control of Discrete Systems**



**DCDS'07**

June 13-15, 2007  
Paris - Cachan, France

The aim of this workshop is to provide the communities of safety/reliability analysis and of DES with an opportunity to exchange and to discuss new developments in the field of **dependable control** of discrete event systems

