HAL
open science

PRACTICAL QUANTIZE-AND-FORWARD SCHEMES FOR THE FREQUENCY RELAY CHANNEL

Brice Djeumou, Samson Lasaulce, Andrew G. Klein

▶ **To cite this version:**

Brice Djeumou, Samson Lasaulce, Andrew G. Klein. PRACTICAL QUANTIZE-AND-FORWARD SCHEMES FOR THE FREQUENCY RELAY CHANNEL. ICASSP 2008 - 33th IEEE International Conference on Acoustics, Speech and Signal Processing, Mar 2008, Las Vegas, United States. 5 p. hal-00361628

HAL Id: hal-00361628

https://hal.science/hal-00361628v1

Submitted on 16 Feb 2009

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

PRACTICAL QUANTIZE-AND-FORWARD SCHEMES FOR THE FREQUENCY RELAY CHANNEL

Brice Djeumou, Samson Lasaulce

LSS, CNRS - SUPELEC - Paris Sud
91190 Gif-sur-Yvette, France
{djeumou,lasaulce}@lss.supelec.fr

Andrew G. Klein

School of ECE, Worcester Polytechnic Institute
100 Institute Rd., Worcester, MA
klein@ece.wpi.edu

ABSTRACT

We consider static and quasi-static relay channels in which the source-destination and relay-destination signals are assumed to be orthogonal and thus have to be recombined at the destination. We propose cheap relaying schemes that are optimized from the knowledge of the signal-to-noise ratios (SNRs) of the source-relay and relay-destination channels at the relay. For this purpose the scheme under investigation is assumed to be scalar and have to minimize the mean square error between the source signal and its reconstructed version at the destination. We propose a quantize-and-forward (QF) scheme, which is a generalization of techniques based on joint source-channel coding. To further improve the receiver performance when the source-relay SNR is relatively poor we propose a Maximum Likelihood detector (MLD) designed for the QF protocol.

***Index Terms*—** Relay channel, quantize-and-forward, joint source-channel coding, ML detector.

1. INTRODUCTION

The channels under investigation in this paper are static and quasi-static orthogonal relay channels for which orthogonality is defined accordingly to [1]. Since the source-destination channel is assumed to be orthogonal to the relay-destination channel (i.e. the forward channel) the destination receives two distinct signals. For the channels under consideration there are at least two important technical issues: the relaying protocol and the recombination scheme at the destination. Three main types of relaying protocols have been considered in the literature: amplify-and-forward (AF), decode-and-forward (DF) and estimate-and-forward (EF). From the corresponding works, several observations can be made: (a) from information-theoretic studies like [1][2] it appears that the best choice of the relaying scheme depends on the source-relay channel (i.e. the backward channel) SNR and that of the relay-destination channel; (b) there are not many works dedicated to the design of practical EF schemes although the EF protocol has the potential to perform well for a wide range of relay receive SNRs (in contrast with DF which is generally more suited to relatively high SNRs).

One of the motivations for the work presented in the paper is precisely to propose low-complexity relaying schemes (comparable to the AF protocol complexity) that can be implemented in a digital relay transceiver (in contrast with the AF protocol) and use the knowledge of the SNRs of the forward and backward channels in order for the relay to optimally adapt to the forward and backward channel conditions. To achieve these goals, the main solution proposed is a QF protocol for which forwarding is done on a symbol-by-symbol basis and aims to minimize the mean square error (MSE) between the source signal and its reconstructed version at the output of the dequantizer at the destination. Some researchers have also referred to the classic Wyner-Ziv source coding scheme in [3] as QF [4][5]. Our practical approach, which ultimately aims to minimize the raw bit error rate (BER) at the destination for a fixed transmit spectral efficiency and does not exploit error correcting coding, differs from these information-theoretic works. It also differs from other practical studies on EF protocols, such as [6] and [7] where the authors consider the non-orthogonal half-duplex relay channel and focus on the achievable rate of the designed EF protocol. In [8], a practical wyner-ziv cooperation for the orthogonal half-duplex relay channel is proposed. It proceeds by forwarding a quantized version of the decoder soft outputs at the relay to the destination where the direct signal from the source serves as a side information for a modified decoder. This later scheme is not analytically optimized by taking the SNRs of the backward and forward channels into account. Rather, our work is based on the joint source-channel coding approach originally introduced in [9] for the Gaussian point-to-point channel where the authors extended the scalar version of the original iterative Lloyd's algorithm when the quantizer outputs (indexes) are passed through a channel before the dequantization. In this paper we further extend the iterative algorithm of [9] in the context of quasi-static orthogonal relay channels by taking into account both the forward and backward channels and providing a non-restrictive sufficient condition for convergence of the derived algorithm, similarly to [10].

This paper is organized as follows: in Sec. 2 the signal model for the orthogonal relay channel, main assumptions, and notation are given. In Sec. 3 the proposed QF scheme is provided and we propose a MLD in order to account for the quantization noise introduced by the relay. In Sec. 4 the proposed scheme is evaluated in terms of raw BER and compared with AF, which serves as a reference strategy. Concluding remarks are provided in Sec. 5.

2. SYSTEM MODEL

The source is assumed to be represented by a discrete-time unit-power signal x ($E[|x^2|] = 1$), which takes its value in the finite set of equiprobable symbols $\mathcal{X} = \{x_1, ..., x_{M_s}\}$. For sake of simplicity, square M_s-QAM symbols with independent real and imaginary parts are assumed. More importantly, the samples of the source, denoted by $x(n)$ where n is the time index, are assumed to be independent and identically distributed (i.i.d.) as in [9][10]. In the context of digital communications this assumption is generally valid because of interleaving, dithering or equivalent operations. In order to limit the relay and receiver complexity we will not exploit the interactions between the quantizer and the error correcting coders, possibly present

at the source and relay. Therefore the assumption made on the source samples and channel model (described just below) implies that there is loss of optimality by assuming *scalar* quantizers, i.e. symbol-by-symbol forwarding at the relay, instead of vector quantizers [**?**]. At each time instant n the source broadcasts the signal $x(n)$, which is received by the destination and relay nodes. The received baseband signals can be written:

$$\begin{cases} y_{sd}(n) &= h_{sd} \times x(n) + w_{sd}(n) \\ x_{sr}(n) &= h_{sr} \times x(n) + w_{sr}(n) \end{cases} \quad (1)$$

where w_{sd} and w_{sr} are zero-mean circularly symmetric complex Gaussian noises with variances σ_{sd}^2 and σ_{sr}^2 respectively. The source-destination and source-relay channels gains, h_{sd} and h_{sr} respectively, are unit reals when considering static channels and unit power complex circular random gaussian variables when considering quasi-static channels. In this paper, for simplicity of presentation, most of the derivations are conducted for static channels, so h_{sd} and h_{sr} are constant over the whole transmission. However, all the results provided easily extend to quasi-static channels. In this case, these quantities are assumed to be constant over a block duration and vary from block to block. In the simulation part both cases will be analyzed and Rayleigh block-fading will be assumed for modeling the channel gains in the case of quasi-static channels. The relay forwards the cooperation signal $x_r(n)$ to the destination. We assume memoryless and zero-delay relaying. Under these assumptions, $x_r(n)$, which satisfies the average power constraint $E[|x_r|^2] = 1$, is the result of a zero-memory quantization operation (denoted by $\mathcal{Q}$) on the sample $x_{sr}(n)$ followed by an M_r-QAM modulation (denoted by $\mathcal{M}$). Since the relay function and channels are memoryless, in the sequel we will at times omit the time index n from the signals. The cooperation signal received at the destination is written $y_{rd}(n) = h_{rd} \times x_r(n) + w_{rd}(n)$. Orthogonality between the received cooperation signal y_{rd} and direct signal y_{sd} can be implemented by frequency division (FD) and we assume that y_{sd} and y_{rd} have the same bandwidth.

At the destination, two types of combiners can be assumed. We will use either a conventional maximum ratio combiner (MRC) or a more sophisticated detector, namely the MLD, which will be derived in Sec. 3.2. The reason for introducing the latter combiner will be clearly explained in Sec. 3.2. Fig. 1 summarizes the system model. The notation $\mathcal{D}$ stands for decoder, which jointly incorporates the demodulation and de-quantization operations.

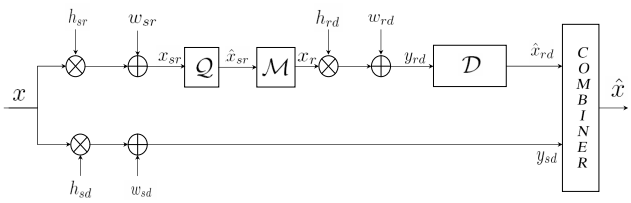

Fig. 1. System model for the quantize-and-forward protocol

.

3. QUANTIZE-AND-FORWARD

3.1. Optimum and uniform quantize-and-forward

The most natural way to estimate and forward the signal received by the relay is to quantize x_{sr} in order to minimize the distortion $D_{00} = E\left[|\hat{x}_{sr} - x_{sr}|^2\right]$, map the quantizer output onto a QAM modulation and send it to the destination. In the high cooperation regime (i.e $\frac{1}{\sigma_{rd}^2} \gg 1$) this strategy is almost optimal since it almost achieves the performance of a 1×2 single input multiple output (SIMO) system. On the other hand if x_{sr} is quantized with a reasonably high number of bits and sent through a bad cooperation channel, minimizing D_{00} is no longer optimal. This is why minimizing $D_{01} = E\left[|\hat{x}_{rd} - x_{sr}|^2\right]$ can be more efficient as shown by [9][10][11][12] in the context of the point-to-point Gaussian channel. In the context of the relay channel we know that the source-relay channel quality also plays a role in the receiver performance. Therefore we propose to minimize the MSE between the reconstructed signal $\hat{x}_{rd}$ and the original source signal x i.e $D_{11} = E\left[|\hat{x}_{rd} - x|^2\right]$ by assuming the SNRs of the forward and backward channels known to the relay.

Let us turn our attention to the quantizer itself. Since the signal to be quantized is complex, the quantizer is made of two "sub-quantizers" for the real and imaginary parts of x_{sr}. The quantization consists in mapping the signal x_{sr} into a pair of rational numbers belonging to $\mathcal{V}^R \times \mathcal{V}^I = \left\{v_1^R, v_2^R, ..., v_L^R\right\} \times \left\{v_1^I, v_2^I, ..., v_L^I\right\}$ where $L = 2^{\frac{b}{2}}$ and b is the total number of quantization bits. Note that the real and imaginary parts of the signal received by the relay are generally independent in practice, which allows us to design them independently. As a QAM modulation is assumed at the source we can restrict our attention to the sub-quantizer Q^R for the real part of x_{sr}. The sub-quantizer maps $\mathrm{Re}(x_{sr}) = x_{sr}^R$ onto the finite set $\left\{v_1^R, v_2^R, ..., v_L^R\right\}$. The mapping is done as follows: If $x_{sr}^R \in S_j^R$ then $\mathcal{Q}^R\left(x_{sr}^R\right) = v_j^R$ where $S_j^R = \left[u_j^R, u_{j+1}^R\right)$ for all $j \in \{1, 2, ..., L\}$ and $\{u_j\}_{j\in\{1,...,L\}}$ are called the transition levels. We will denote $\mathcal{U}^R = \left\{u_1^R, u_2^R, ..., u_{L+1}^R\right\}$. The same procedure is applied to the signal $x_{sr}^I = \mathrm{Im}(x_{sr})$. The quantizer output is then mapped onto the constellation. In [**?**] the author used the Kohonen learning algorithm to map, in ordered way, the N-dimensional input signal in which the representatives lie to the 2-dimensional space of modulation symbols. This mapping is done in such a manner that close representatives in the signal space are assigned to close symbols in the modulation space. Therefore, the most likely decision errors which appear in the neighborhood of the symbol associated with the input representative will result in a slight increasing of the distortion. In our case, the problem can be viewed as the mapping of a 2-dimensional (real and imaginary parts) input signal space onto a 2-dimensional signal space (i.e. the modulation set). Since the representatives set forms an ordered grid, it is straightforward to obtain a coherent correspondence between the signal space and the modulation space. Mapping the quantization representatives whose coordinates are $\left\{v_j^R, v_j^I\right\}$ onto the M_r-QAM constellation by using this approach leads to an ordered mapping such that a decision error in the neighborhood of the transmitted symbol results in a slight increase of the quantization error at the dequantizer output (i.e a small number of erroneous bits). Specifically, each centroid whose normalized and non-uniform coordinates are $(i, j) \in \mathbb{Z}^2$ in the quantization grid is mapped onto the QAM point having the same coordinates in the constellation. Note that, in contrast with conventional quantization the centroids are not necessarily located in the quantization cells they represent.

We now describe the quantizer optimization procedure. To find the optimal pair of sub-quantizers at the relay we minimize D_{11} as follows. The distortion can be written as:

$$D_{11} = \underbrace{E\left[(\hat{x}_{rd}^R)^2\right] - 2E\left[\hat{x}_{rd}^R x^R\right] + E\left[(x^R)^2\right]}_{D_{11}^R} + \underbrace{E\left[(\hat{x}_{rd}^I)^2\right] - 2E\left[\hat{x}_{rd}^I x^I\right] + E\left[(x^I)^2\right]}_{D_{11}^I}. \quad (2)$$

As D_{11}^R and D_{11}^I can be optimized independently and identically we focus, hence forth, on minimizing D_{11}^R. Given a number of quantization bits we now optimize the sub-quantizer Q^R by minimizing D_{11}^R with respect to the transition levels $\{u_\ell\}_{\ell\in\{1,...,L\}}$ and the representatives $\{v_\ell\}_{\ell\in\{1,...,L\}}$. For fixed transition levels the optimum representatives are the centroids of the corresponding quantization cells which are obtained by setting the partial derivatives of D_{11}^R to zero:

$$v_\ell^R = \frac{\sum_{k=1}^{\sqrt{M_s}} x_k^R p_k \sum_{j=1}^{L} P_{j,\ell}^R \int_{u_j^R}^{u_{j+1}^R} \phi\left(t - x_k^R\right) dt}{\sum_{k=1}^{\sqrt{M_s}} p_k \sum_{j=1}^{L} P_{j,\ell}^R \int_{u_j^R}^{u_{j+1}^R} \phi\left(t - x_k^R\right) dt}. \quad (3)$$

where $\forall k \in \left\{1, ..., \sqrt{M_s}\right\}$, $p_k = \Pr\left[X^R = x_k^R\right]$ (i.e. the channel input statistics), $\forall (j,\ell) \in \{1, ..., L\}^2$, $P_{j,\ell}^R = \Pr\left[\hat{x}_{rd}^R = v_\ell^R \,|\hat{x}_{sr}^R = v_j^R\right]$ (i.e. the forward channel statistics) and $\phi(t) = \frac{|h_{sr}|}{\sqrt{\pi}\sigma_{sr}} \exp\left(-\frac{|h_{sr}|^2 t^2}{{\sigma_{sr}}^2}\right)$ is the Gaussian pdf of the real noise component $\mathrm{Re}(w_{sr})$ of the signal received by the relay (i.e. the backward channel statistics). When the representatives are fixed it is not trivial, in general, to determine the transition levels explicitly as is the case of conventional channel optimized quantizers such as [10] for which the backward channel is not present. Determining the transition levels then requires the use of an exhaustive search algorithm. However, note that there are simple cases such as the 4-QAM at the source, which is used in the simulations in Section 4, where both the optimum representatives for fixed transition levels and optimum transition levels for fixed representatives can be found. For a 4-QAM constellation we have $\left(x^R, x^I\right) \in \{-A, +A\}^2$. For fixed transition levels, the representatives are obtained by replacing x_k^R by its values in (3). And, for fixed representatives we have

$$u_\ell^{R,*} = \frac{\sigma_{sr}^2}{2A} \ln\left[\frac{\sum_{k=1}^{L}\left(P_{\ell,k}^R - P_{\ell-1,k}^R\right)\left(A + \frac{1}{2}v_k^R\right)v_k^R}{\sum_{k=1}^{L}\left(P_{\ell,k}^R - P_{\ell-1,k}^R\right)\left(A - \frac{1}{2}v_k^R\right)v_k^R}\right]. \quad (4)$$

Note that in (4) the strict positiveness of the argument of the natural logarithm insures the existence of the optimum transition levels. We are now in position to provide the complete iterative optimization procedure (**for a general modulation**, plutot pour la 4-QAM considérée ici car pour une modulation générale l'équation (4) n'existe pas). Let i and ϵ be the iteration index and the current value of the estimation error criterion of the iterative algorithm. The algorithm is said to have converged when ϵ reaches ϵ_{max}. **Step 1**: Set $i = 0$. Set $\epsilon = 1$. Initialize $\mathcal{V}^R$ and $\mathcal{U}^R$ with the sets (say $\mathcal{V}_{(0)}^R$ and $\mathcal{U}_{(0)}^R$) obtained from the algorithm in [10], which corresponds to a local optimum since the backward channel is not taken into account. **Step 2**: Set $i \to i+1$. For the fixed partition $\mathcal{U}_{(i-1)}^R$ use equation (3) to find the optimal codebook $\mathcal{V}_{(i)}^R$. For the fixed codebook $\mathcal{V}_{(i)}^R$ use equation (4) to obtain the optimal partition $\mathcal{U}_{(i)}^R$. If the realizability condition $u_1^R \le u_2^R ... \le u_L^R$ is not met stop the procedure and keep the transition levels provided by the previous iteration. **Step 3**: Update ϵ as follows: $\epsilon = \frac{\sum_{k=1}^{L}\left|v_{k(i)}^R - v_{k(i-1)}^R\right|}{\sum_{k=1}^{L}\left|v_{k(i)}^R\right|}$. If $\epsilon \ge \epsilon_{max}$ then go to Step 2; Stop otherwise.

As with other iterative algorithms (e.g. the EM algorithm) one cannot easily prove or insure, in general, the convergence to the global optimum. When the backward channel is not present the authors of [10] proved that the distortion obtained by applying the generalized Lloyd's algorithm is a non-increasing function of i and provide a sufficient condition under which the procedure is guaranteed to converge towards a local optimum. The corresponding condition is not restrictive since it can be imposed through the realizability constraint (u_ℓ must be an increasing function of ℓ) of the transition levels [10] to the iterative procedure without loss of optimality. It turns out a similar result can be derived in our context if one assumes a zero-mean channel input (i.e. $E[X^R] = 0$) and the backward channel to be an AWGN channel. This condition can be proved to be: $\forall \ell \in \{1, ..., L-1\},\ E[\hat{X}_{rd}^R | \hat{X}_{sr}^R = v_{\ell+1}^R] > E[\hat{X}_{rd}^R | \hat{X}_{sr}^R = v_\ell^R]$. If this condition is met the MSE will be a non-increasing function of the iteration index.

3.2. Maximum likelihood combiner for the QF protocol

As mentioned in section 2 the purpose of the combiner is to combine the source-destination signal y_{sd} and the dequantizer output $\hat{x}_{rd}$. If one decomposes the latter signal as $\hat{X}_{rd} = X + \hat{W}_{rd}$ it is obvious that the noise component $\hat{W}_{rd}$ is correlated with the useful signal component and is not Gaussian in general. Therefore maximizing the output SNR of a linear combiner is not optimum in terms of raw BER. In order to extract the best of the cooperation between the receiver and relay for all channel SNRs we propose to use a non-linear combiner namely the ML **combiner** (combiner $\to$ detector?). Assume that the symbol transmitted by the source is x and the $Q(x_{sr}) = v_i$. The likelihood $p_{ML} = p(y_{sd}, \hat{x}_{rd}|x)$ can be shown to factorize as: $p_{ML} = p(y_{sd}|x)p(\hat{x}_{rd}|x)$ where $p(y_{sd}|x) = \frac{1}{\pi\sigma_{sd}^2} \exp\left(-\frac{|y_{sd} - h_{sd}x|^2}{\sigma_{sd}^2}\right)$. For expanding the second term $p(\hat{x}_{rd}|x)$ one has to remind that $\hat{X}_{rd} \in \mathcal{V}^R \times \mathcal{V}^I = \{v_1, v_2, ..., v_{M_r}\}$ and makes use of the channel transitions probabilities $P_{k,\ell}$ between complex representatives (see section 3.1 where we have defined $P_{k,\ell}^R$ for the real part of complex representatives). We have:

$$\begin{aligned} p(\hat{x}_{rd} = v_i|x) &= \int_{x_{sr}} p(x_{sr}, \hat{x}_{rd} = v_i|x)\, dx_{sr} \\ &= \sum_{j=1}^{M_r}\left[\int_{x_{sr}\in S_j} p(x_{sr}|x)\, p(\hat{x}_{rd} = v_i|x_{sr})\, dx_{sr}\right] \\ &= \sum_{\ell=1}^{\sqrt{(M_r)}}\sum_{m=1}^{\sqrt{(M_r)}} P_{j,i} \times \\ &\quad \left[\int_{u_\ell^R}^{u_{\ell+1}^R} \phi\left(t - x^R\right) dt \int_{u_m^I}^{u_{m+1}^I} \phi\left(t' - x^I\right) dt'\right] \end{aligned}$$

where the index j corresponds to the symbol of the relay al-

phabet (i.e. $\{1, ..., M_r\}$) associated with the pair of representatives (v_ℓ^R, v_m^I). Now, by denoting $\underline{s} = (s_1, ..., s_N)$ the vector of bits associated with the source symbol x allows us to express the log-likelihood ratio for the nth bit:

$$\lambda(s_n) = \log \left[\frac{\sum_{\underline{s} \in S_1^{(n)}} p\left(y_{sd}|x\right) p\left(\hat{x}_{rd}|x\right)}{\sum_{\underline{s} \in S_0^{(n)}} p\left(y_{sd}|x\right) p\left(\hat{x}_{rd}|x\right)} \right] \quad (5)$$

where the sets $S_1^{(i)}$ and $S_0^{(i)}$ are defined by: $S_1^{(n)} = \{(s_1, \ldots, s_N) \in \{0,1\}^N | s_n = 1\}$ et $S_0^{(n)} = \{(s_1, \ldots, s_N) \in \{0,1\}^N | s_n = 0\}$. If $\lambda(s_n) > 0$ then $\hat{s}_n = 1$ and $\hat{s}_n = 0$ otherwise.

4. SIMULATION ANALYSIS

We assume a 4-QAM at the source and focus on the raw BER versus $SNR_{sr} = \frac{1}{\sigma_{sr}^2}$. Because of the lack of space we limited ourselves to a few scenarios but will also briefly comment simulations that cannot be provided here. For static channels, Fig. 2 compares the optimum QF with the conventional AF in a typical scenario where: $SNR_{sr} = SNR_{sd} + 10$ dB, $SNR_{rd} = 10$ dB and the number of quantization bits is 6 (i.e. $\frac{b}{2}$ bits per sub-quantizer). At the destination, the MRC is used for all relaying schemes. The QF solution provides a significant gain over the AF protocol. On the figure, the clipped AF protocol is a modified AF protocol where the received signal at the relay x_{sr} is optimally clipped to minimize the end-to-end distortion. Other simulations have shown that, depending on SNR_{sr} and SNR_{rd} this gain typically ranges from 0.5 dB to 1.5 dB. For quasi-static rayleigh fading channel, many simulations showed that the receiver performs quite similarly no matter which relaying protocol (AF or optimum QF) is used, provided that the preferred combining scheme is employed (i.e. the MRC is used for AF and MLD is used for optimum QF): exemple of Fig. 3. And for low and medium transmit or cooperation powers the optimum QF provides the best performance whereas the performance loss in the high cooperation regime is always small, which means that the SIMO bound is almost achieved by optimum QF in the latter regime. Fig. 3 also depicts the influence of the combining scheme on the receiver performance. In both "good" and "bad" relay scenarios, the MLD brings a significant performance gain, especially when b is small.

5. CONCLUSION

We have proposed a low-complexity quantize-and-forward scheme, which exploits the knowledge of the SNRs of the source-relay and relay-destination channels. In static channels it generally performs close to or better than the conventional AF protocol. Over Rayleigh block-fading channels we have seen that the optimum QF protocol, provided it is associated with an ML detector, it has generally similar performance to the conventional AF protocol, whatever the simulation scenario. The following comment can be made: since the optimum QF protocol is both scalar, simple and generally performs closely to the AF protocol, this shows that the proposed solution can be seen as a way of implementing a channel optimized AF-type protocol in a digital relay transceiver. Now, if the relay and receiver complexity can be relaxed the proposed approach can be improved by vector quantization or exploiting the structure inherent to channel coding, which can be seen as an *extension* of this work.

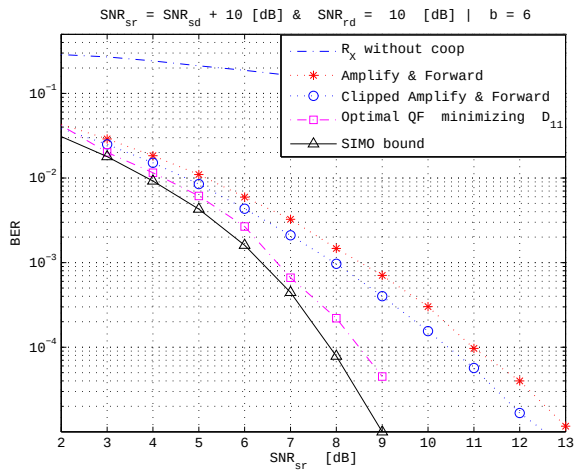

Fig. 2. QF versus AF and clipped AF with static channel

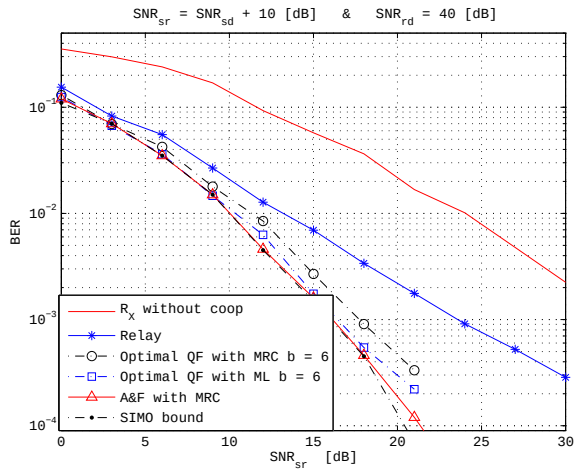

Fig. 3. QF versus AF and ML versus MRC with quasi-static channel

Acknowledgment

The authors would like to thank Prof. Pierre Duhamel for many constructive and critical comments.

6. REFERENCES

[1] A. A. El Gamal, M. Mohseni and S. Zahedi, "Bounds on capacity and minimum energy-per-bit for AWGN relay channels", *IEEE Trans. on Information Theory*, Vol. 52, Issue 4, Apr. 2006, pp. 1545–1561.

[2] J. N. Laneman and D. N. C. Tse and G. W. Wornell, "Cooperative Diversity in Wireless Networks: Efficient Protocols and Outage Behavior", *IEEE Trans. on Info. Theory*, Vol. 50, Issue 12, Dec. 2004, pp. 3062–3080.

[3] T. M. Cover and A. A. El Gamal, "Capacity theorems for the relay channel", *IEEE Trans. Inform. Theory*, Vol. 25, Issue 5, Sep. 1979, pp. 572–584.

[4] M. A. Khojastepour, A. Sabharwal and B. Aazhang, "Lower bounds on the capacity of Gaussian relay channel", *Proc. of CISS*, Mar. 2004, pp. 597–602.

[5] M. Katz and S. Shamai, "Relaying protocols for two colocated users", *IEEE Trans. Inform. Theory*, Vol. 52, Issue 6, Jun. 2006, pp. 2329–2344.

[6] Z. Liu, V. Stankovic and Z. Xiong, "Wyner-Ziv coding for the half-duplex relay channel", *IEEE Proc of. ICASSP*, Mar. 2005, pp. 1113-1116.

[7] A. Chakrabarti, A. De Baynast, A. Sabharwal and B. Aazhang, "Half-Duplex Estimate-and-Forward Relaying: Bounds and Code Design", *IEEE Proc. of ISIT*, Jul. 2006, pp. 1239–1243.

[8] R. Hu and J. Li, "Practical Compress-Forward in User Cooperation: Wyner-Ziv Cooperation", *Proc. of ISIT*, Jul. 2006, pp. 489–493.

[9] A. Kurtenbach and P. Wintz, "Quantizing for noisy channels", *IEEE Trans. on Comm.*, Vol. 17, Apr. 1969, pp. 291–302.

[10] N. Farvardin and V. Vaishampayan, "Optimal quantizer design for noisy channels: An approach to combine source-channel coding", *IEEE Trans. on Information Theory*, Vol. 33, Issue 6, Nov. 1987, pp. 827–837.

[11] V. Vaishampayan and N. Farvardin, "Joint design of block source codes and modulation signal sets", *IEEE Trans. on Information Theory*, Vol. 38, Jul. 1992, pp. 1230–1248.

[12] F. H. Liu, P. Ho and V. Cuperman, "Joint source and channel coding using a non-linear receiver", *IEEE Proc. of ICC*, 1993, pp. 1502–1507.