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Building effective formal models to prove time properties of networked automation systems

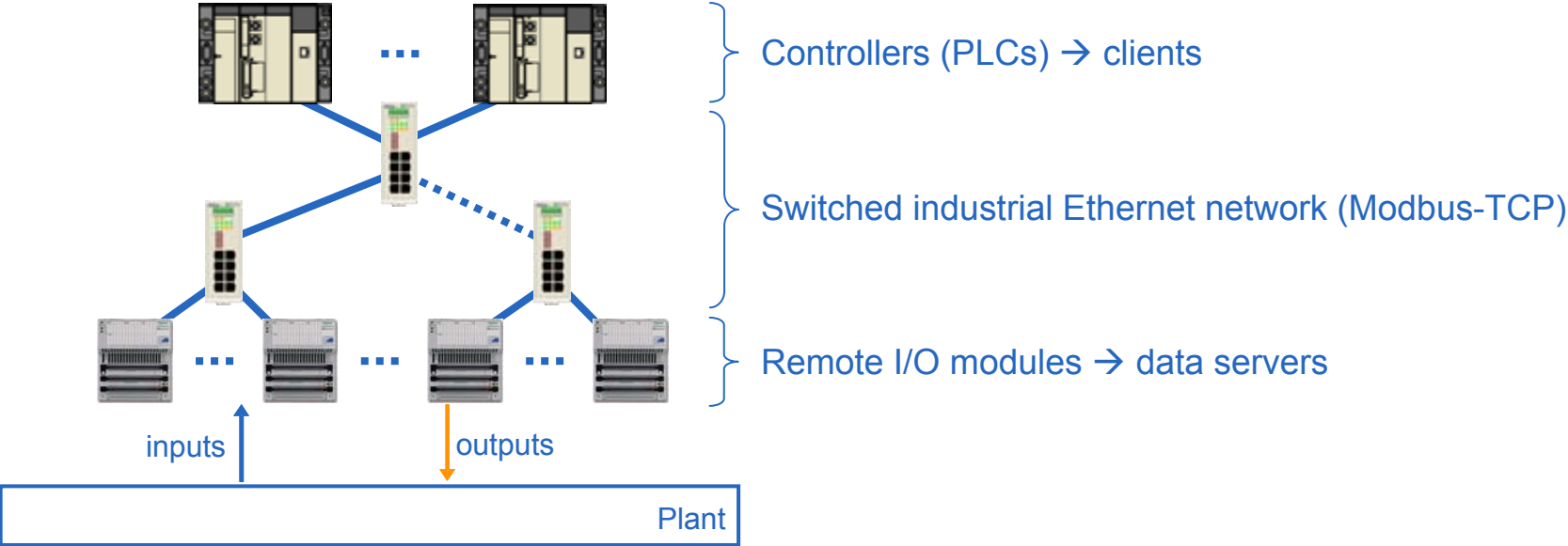
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and Jean-Marc Faure**

**LURPA, ENS de Cachan
France**

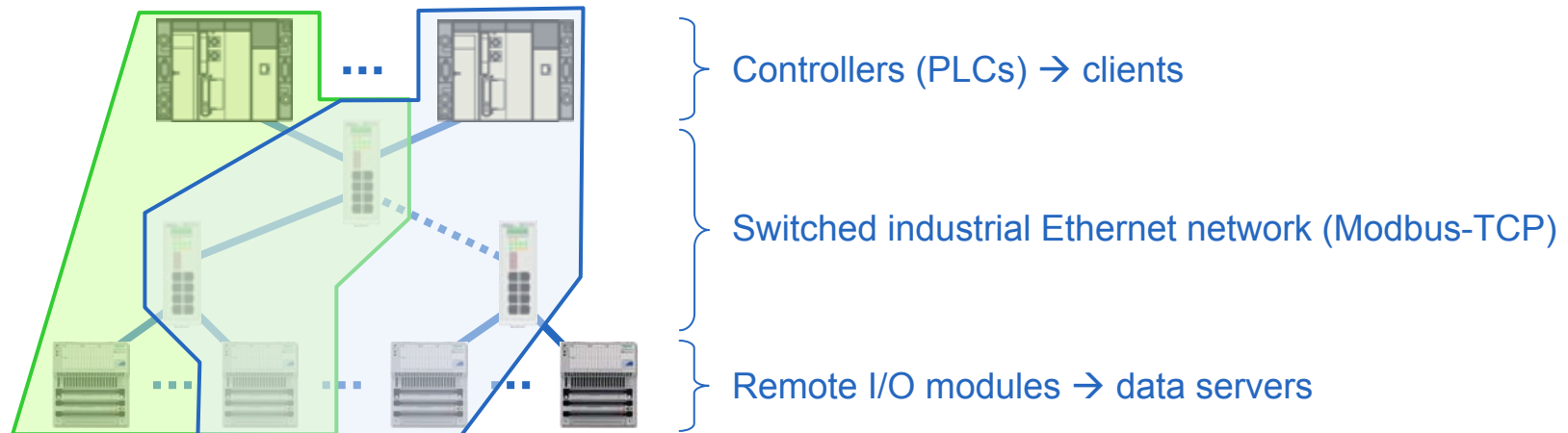
Outline

- **Time performances of networked automation systems**
- **Timed model-checking for time performances evaluation**
- **Building effective formal models**
- **Case study**
- **Conclusions and outlooks**

Considered class of NAS



Considered class of NAS



■ Main features

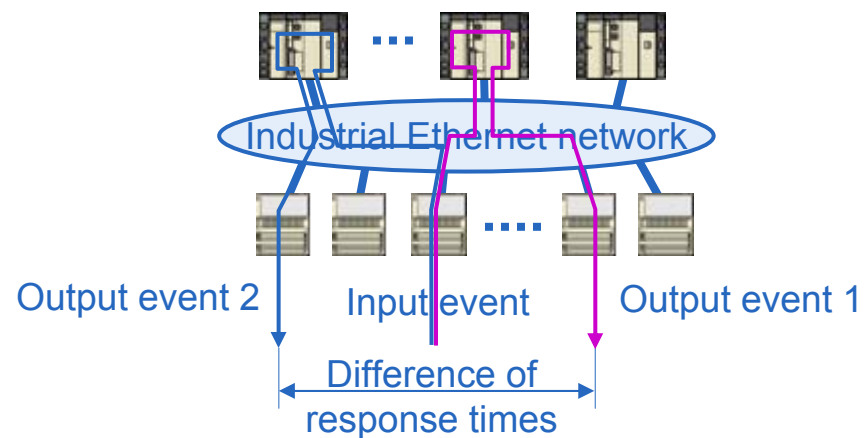
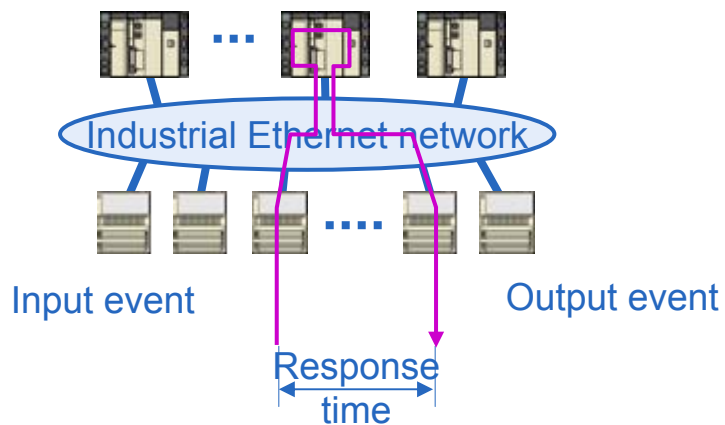
- Each PLC scans cyclically several RIOMs; PLCs scans are not synchronized.
- One RIOM may be scanned by several PLCs \Rightarrow **PLCs scans are concurrent processes.**

■ Assumption

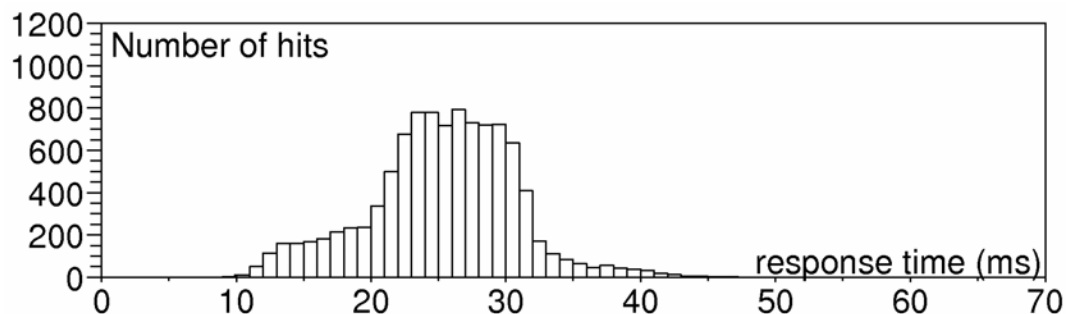
- No frame loss (full duplex switched Ethernet, large enough switches buffers, no perturbations due to electromagnetic fields, ...)

Definitions and measurement

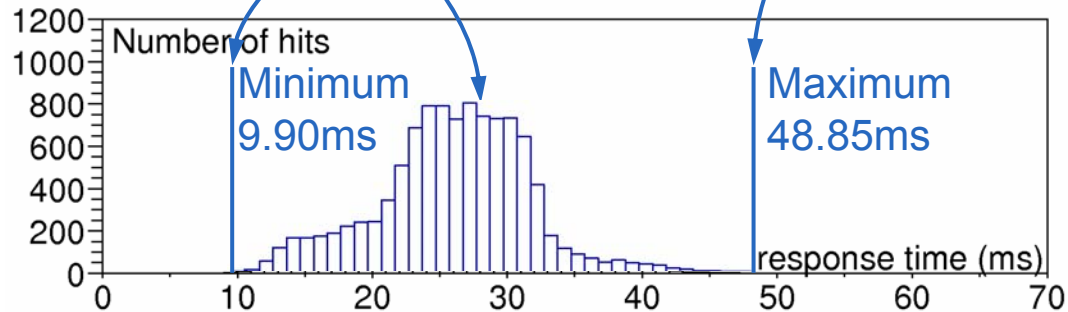
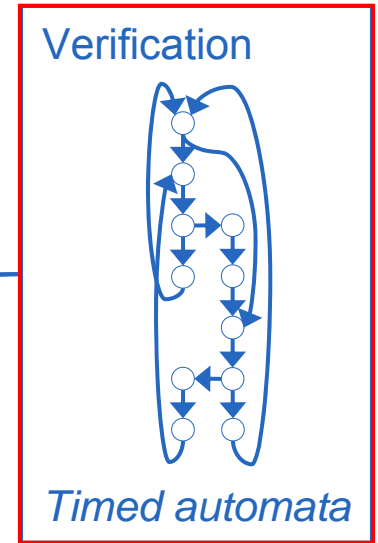
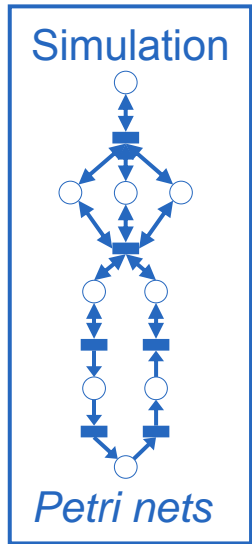
Response time and difference of response times



Experimental results: distribution of values



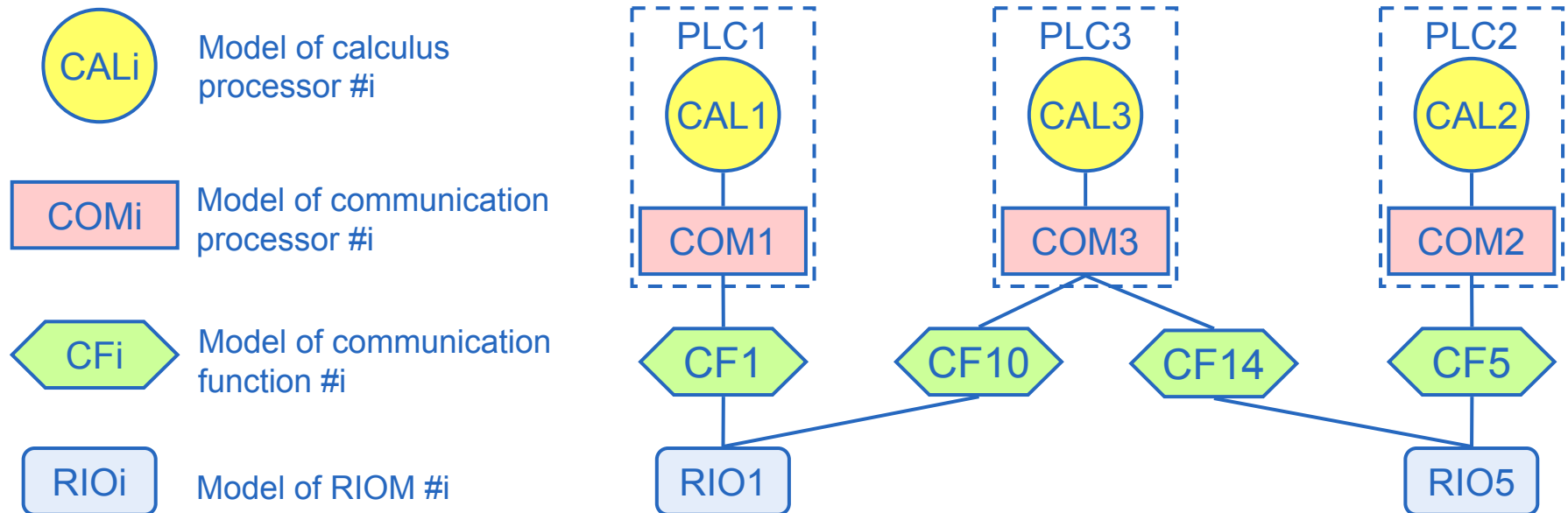
Off-line time performances evaluation using DES models



Construction of the model to check

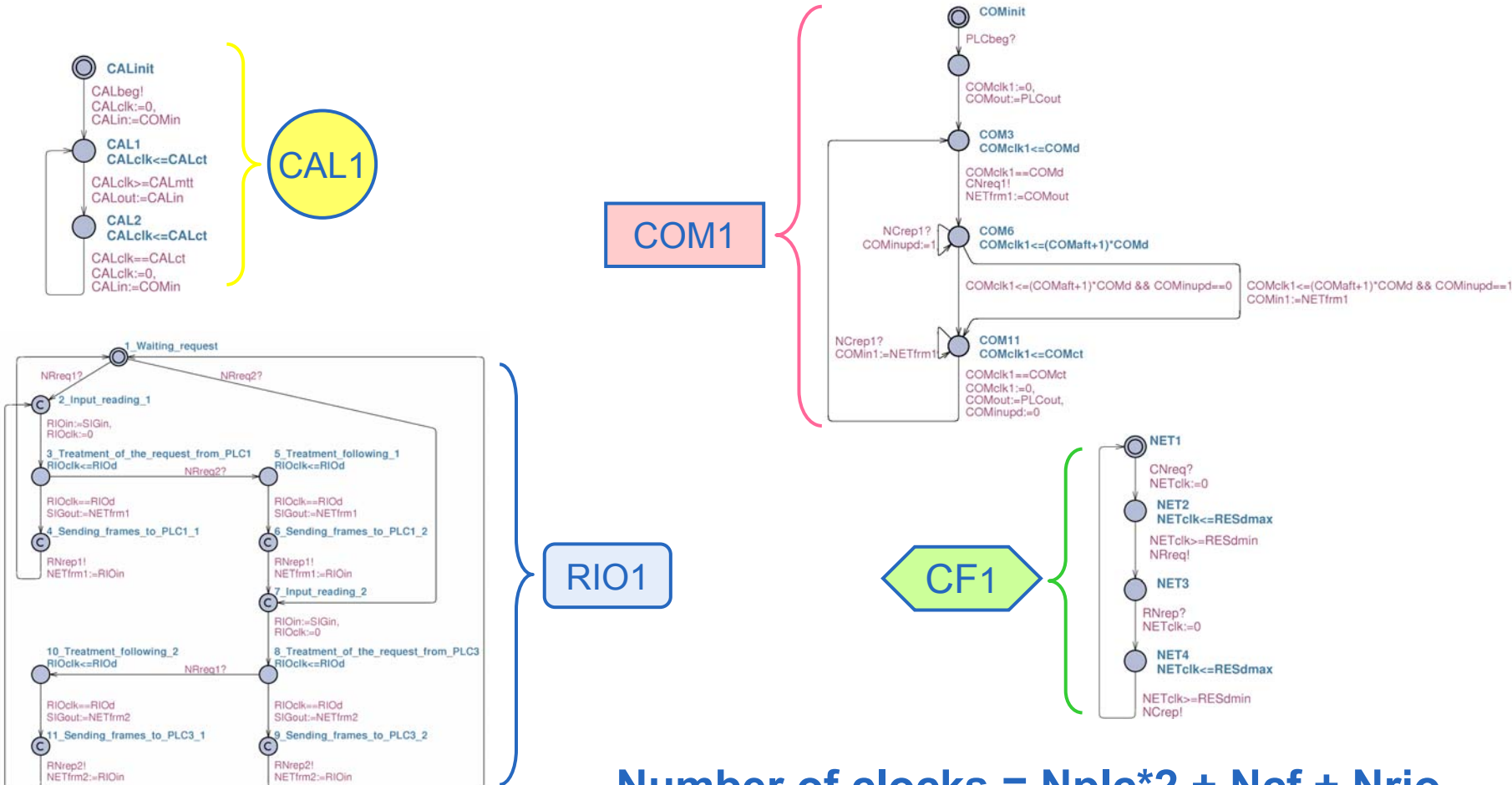
Structure of the NAS model: graph

- Nodes → components models
- Edges → communications between components models



Construction of the NAS model to check (continued)

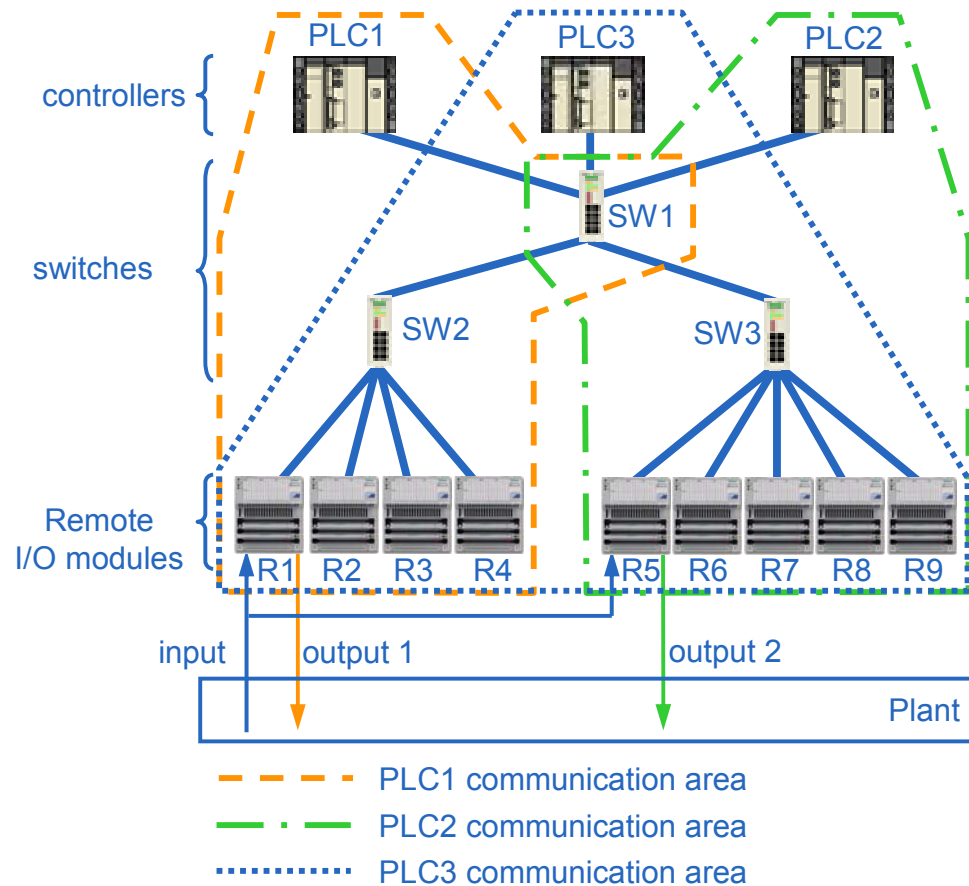
- Structure of the NAS model: graph
- Components models: timed automata



$$\text{Number of clocks} = N_{plc} * 2 + N_{cf} + N_{rio}$$

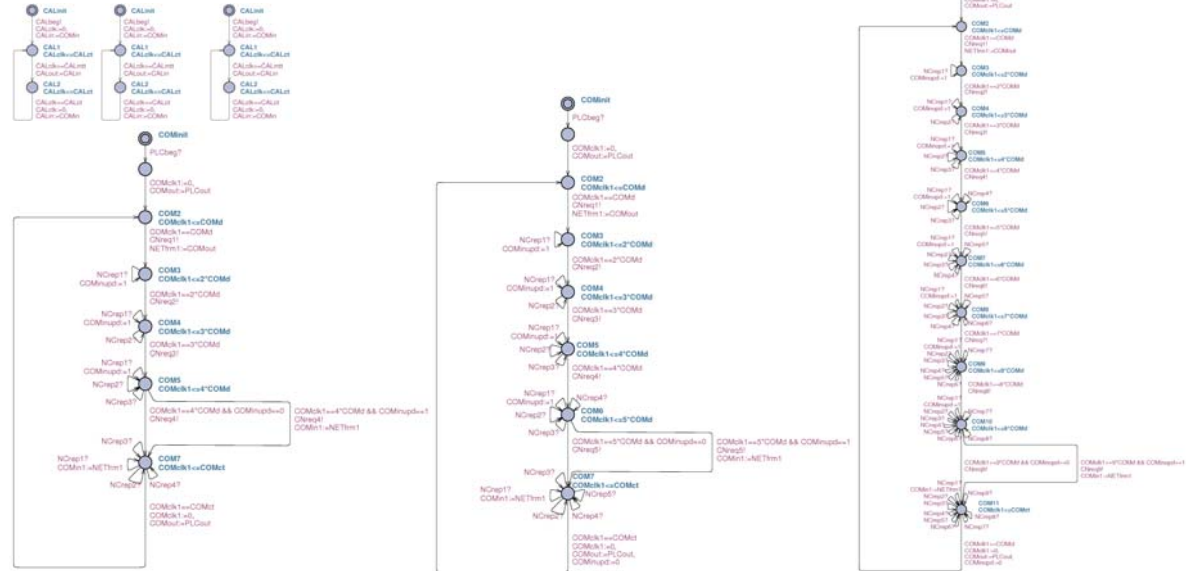
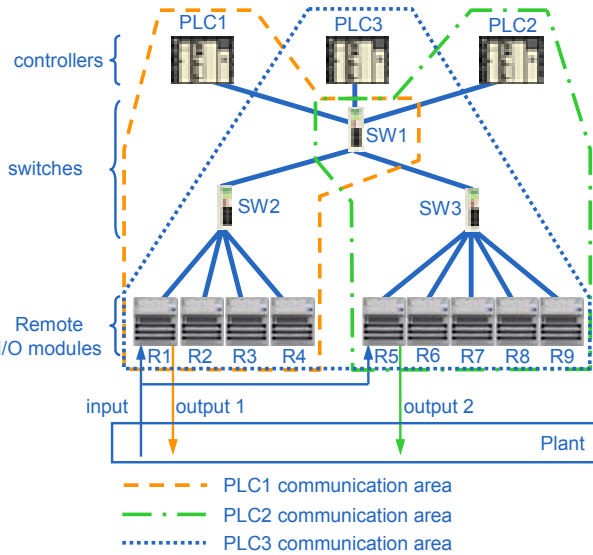
Testing scalability of the approach

■ Small example



Testing scalability of the approach

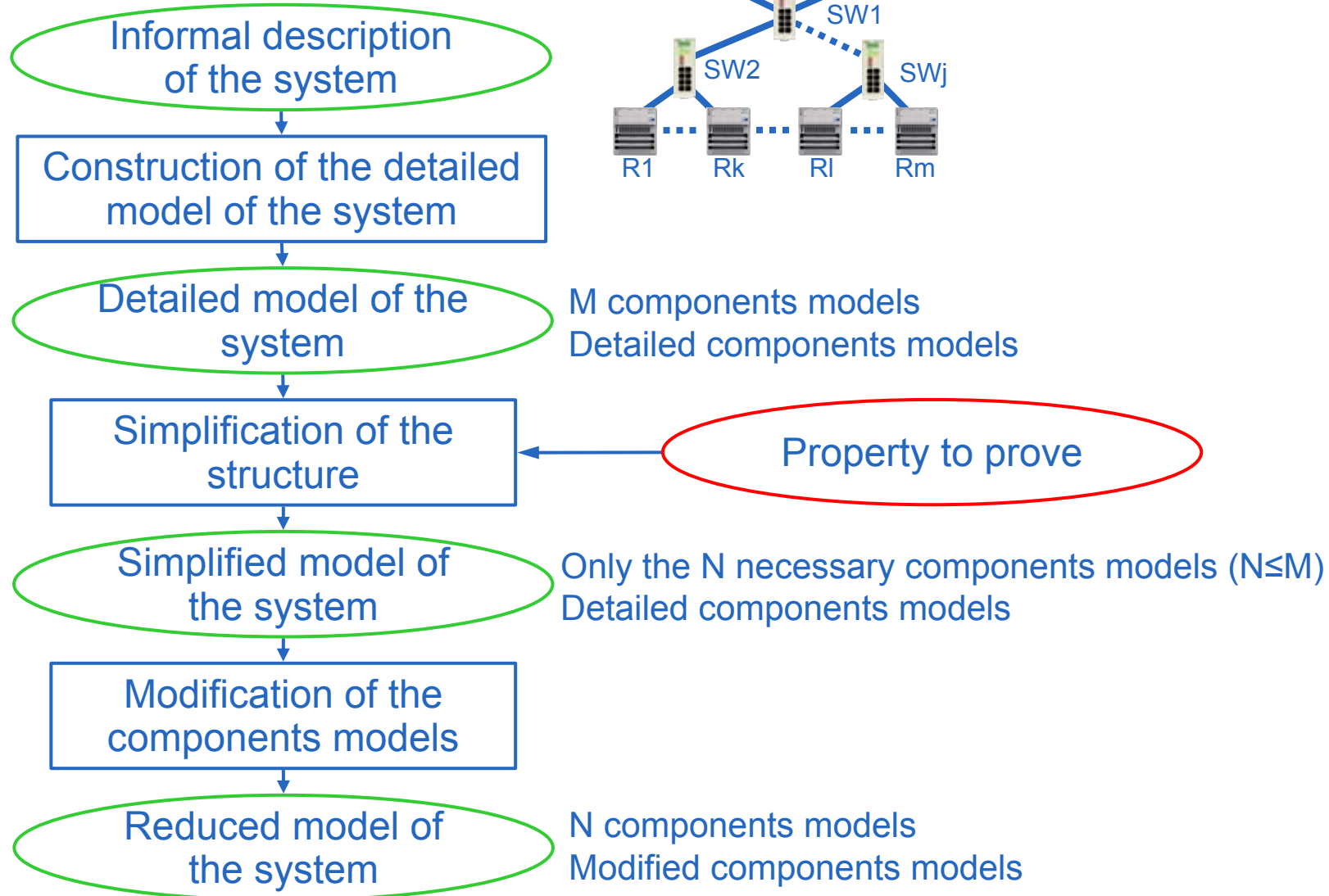
■ Small example → Out of memory in few minutes



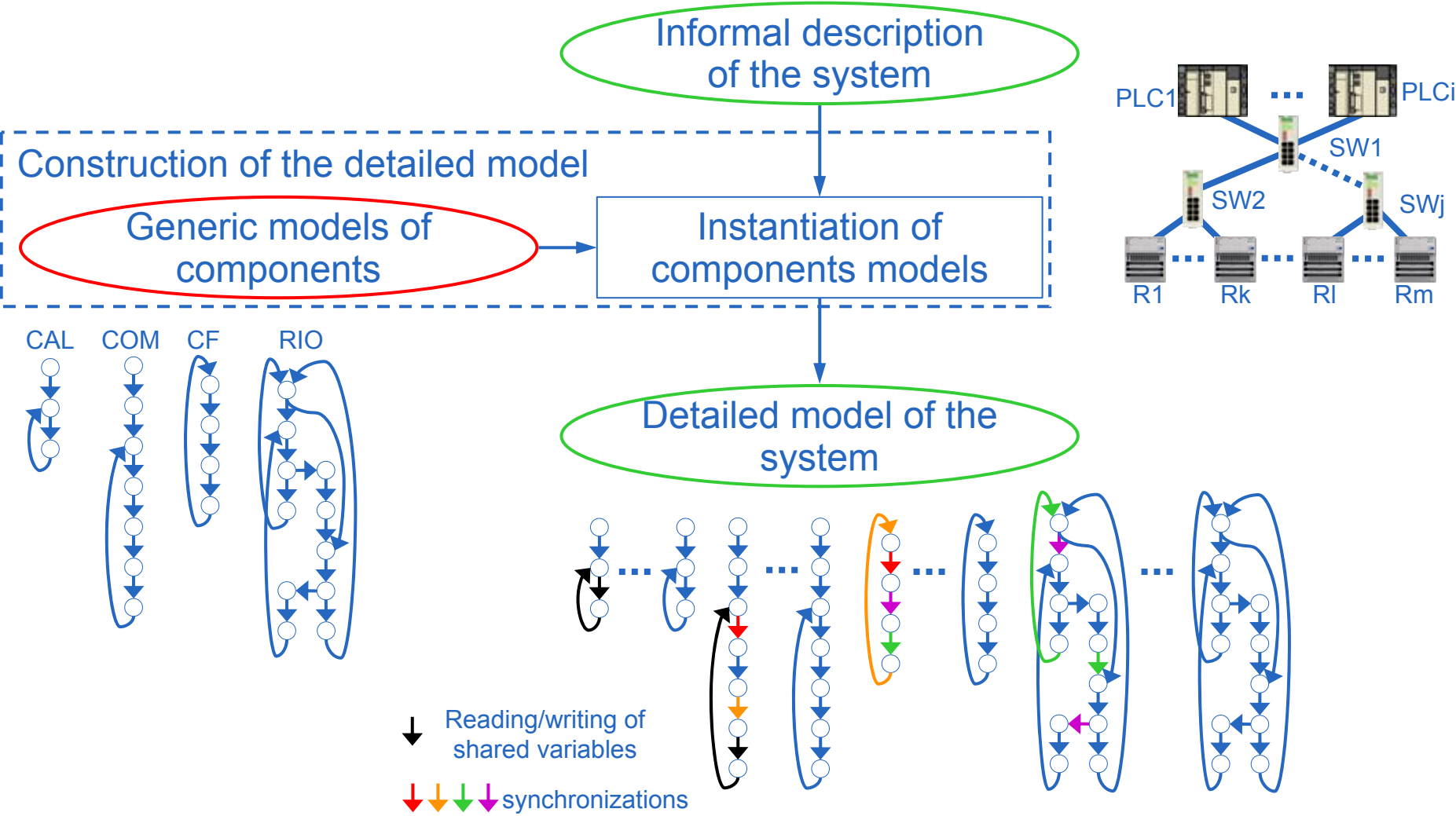
A method to build effective formal models is required

- **This method must yield abstract models that are tractable by existing model-checkers.**
- **Proof results on these models must be trustworthy.**

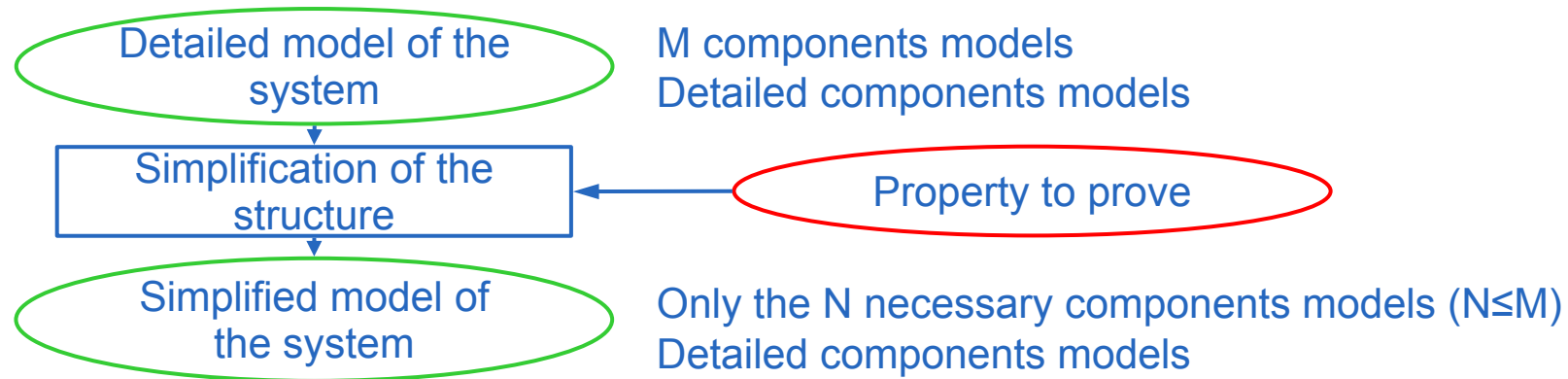
Method overview



Step 1: construction of the detailed model



Step 2: simplification of the structure



■ Principle

- Keep only the components models which generate, modify or propagate data that depend on the input or output events
- **Interpretation abstraction** similar to 'cone of influence' in symbolic model-checking, or 'localization reduction' for integrated circuits verification

■ Step automation: analysis of the structure of the model (graph)

- Search of the **shortest path** from the considered input to the considered output that goes through the calculus processor that computes the value of the output event

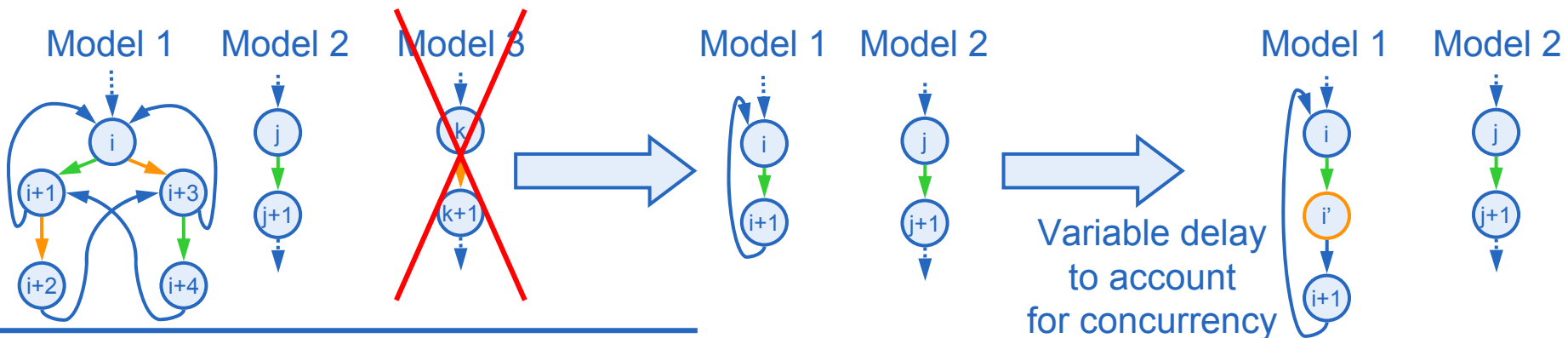
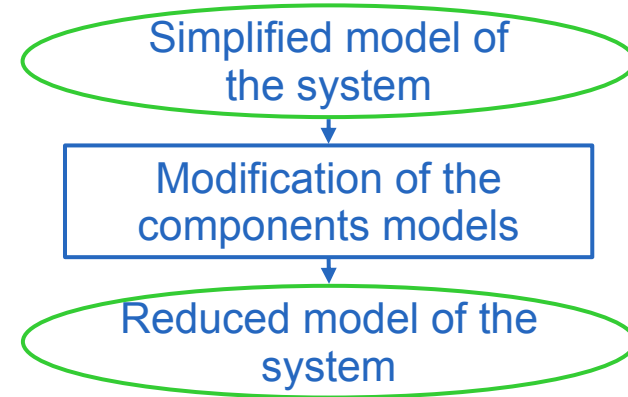
Step 3: modification of the components models

■ Consequence of the previous step

- Loss of possible behaviors in remaining components models

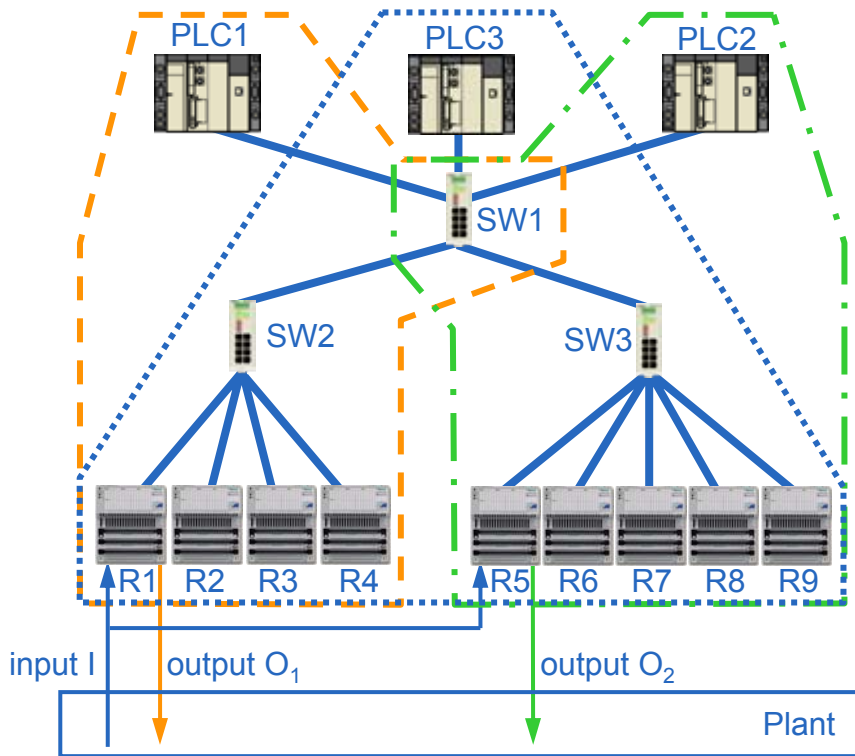
■ In all remaining components models

- Remove useless transitions and locations
- Insert variable duration (from 0 to Worst Case Waiting Time) locations to account for concurrency



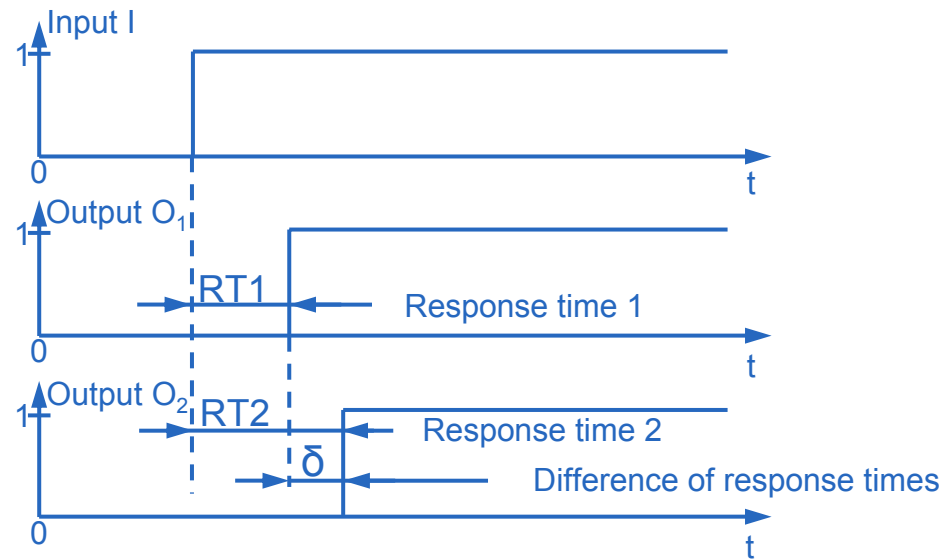
Objective of the study

Studied system



- PLC1 communication area
- . - PLC2 communication area
- PLC3 communication area

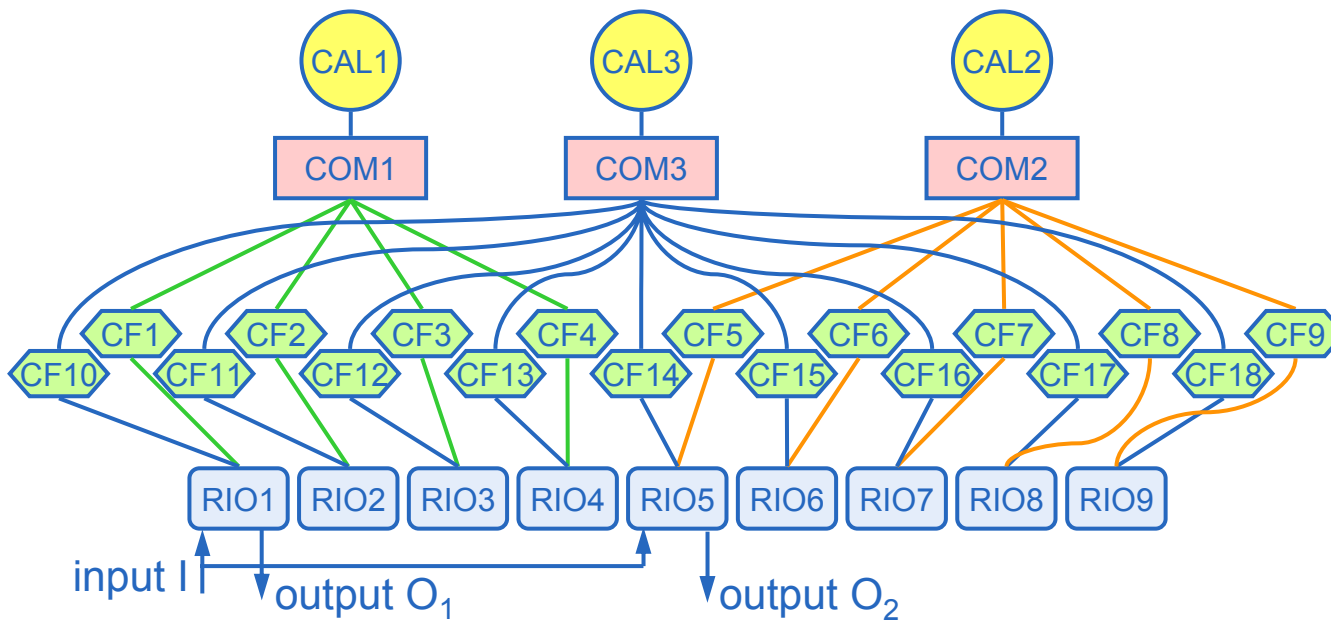
Studied time performance



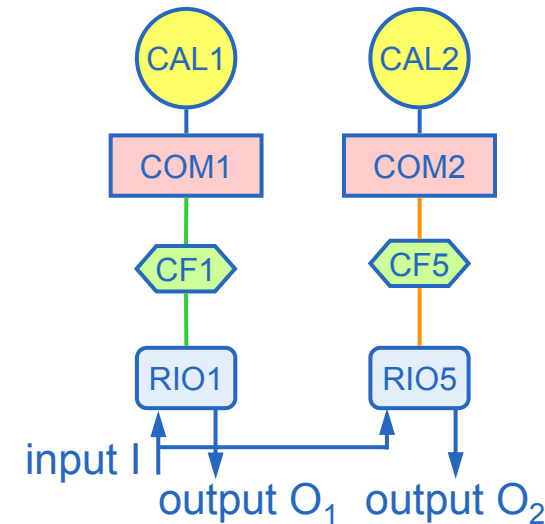
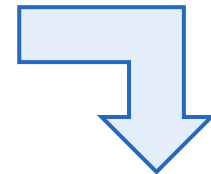
Upper bound of δ ($\text{Max}(\delta)$)?

Simplification of the NAS model structure

- Initial and final system models



Graph analysis

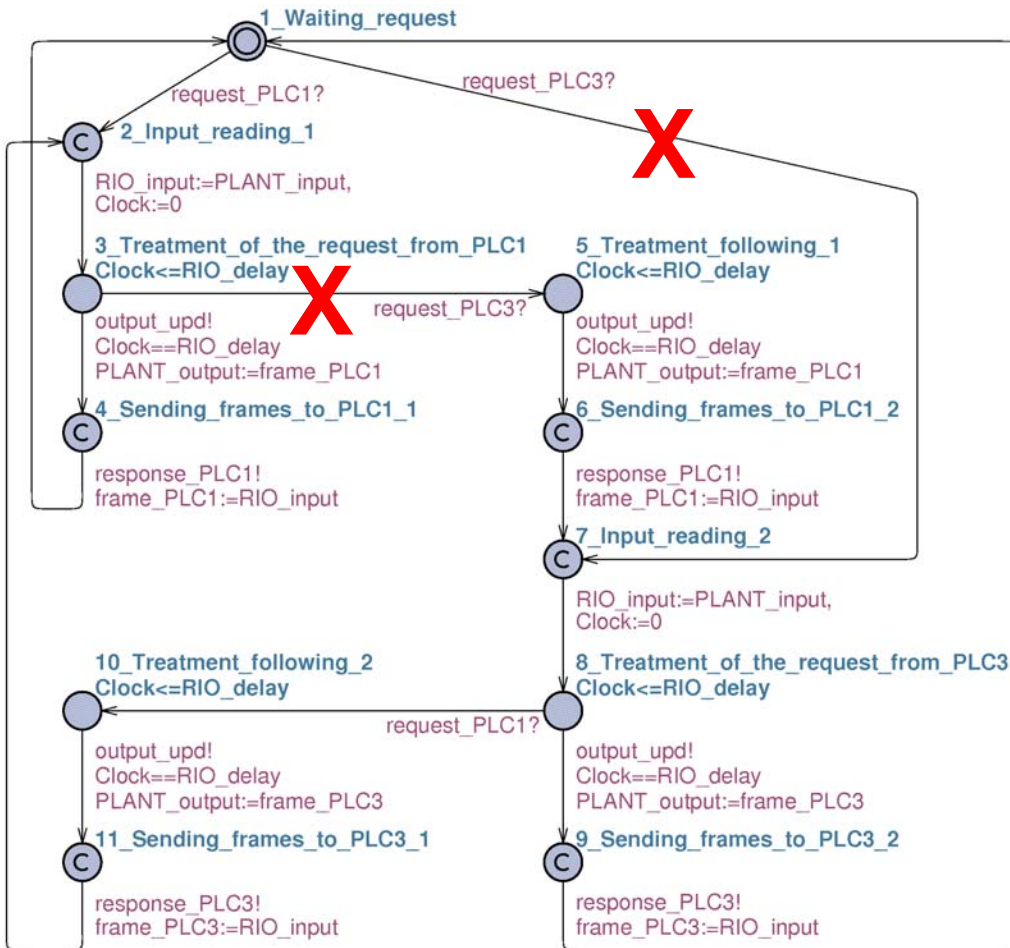


Possibility to determine separately the lower and upper bounds of RT1 and RT2 (RT1m, RT1M, RT2m, RT2M)

$$\rightarrow \text{Max}(\delta) \leq \text{MdRT} = \text{Max}((\text{RT1M}-\text{RT2m});(\text{RT2M}-\text{RT1m}))$$

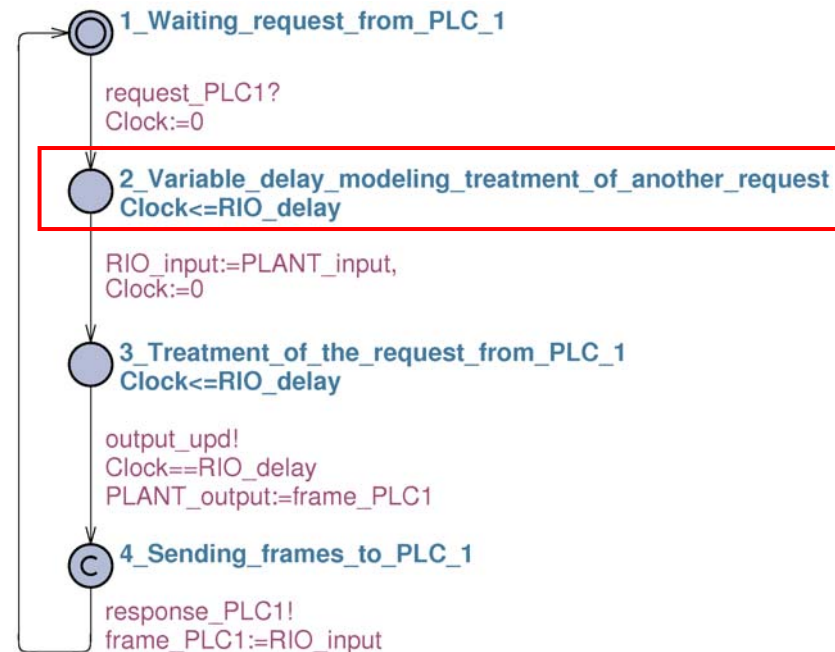
Modification of the components models (RIO model)

▪ Detailed model



▪ Modified model

- Locations 1, 3 and 4 unchanged
- New location (variable duration) added to account for PLC3 requests



Obtained results

| | Experiment 1 | Experiment 2 | Experiment 3 |
|--------------------------|---|---|--|
| Model | Detailed | Reduced | Reduced |
| Performance | Max(δ) | Max(δ) | MdRT |
| Calculus duration | Impossible (not enough memory) | 28 hours | 1 second |
| Obtained values | | Max(δ) = 21.4 ms | MdRT = 21.4 ms → Max(δ) ≤ 21.4 ms |

■ Comparison

- Experiment 3 leads to a very short calculus duration
- Experiment 3 gives an overestimation of the upper bound of the difference of response times
- Experiment 2 gives the upper bound of the difference of response times

Conclusions

- **Time performances evaluation of real systems using model-checking requires to “pre-process” detailed models**
- **Modeling method to build abstract formal models of networked automation systems based on:**
 - Simplification of the structure of the system model
 - Modification of the components models
- **Formal models obtained**
 - Are tractable by existing proof tools
 - Proofs on these models are meaningful and trustworthy

Outlooks

■ Technical improvements

- Automation of the different steps of the method
 - Set up of a components models library to automate step 1
 - Automatic modification of components models (step 3) from shortest path search results (results of step 2)
- Larger case studies to assess the limits

■ Further investigations

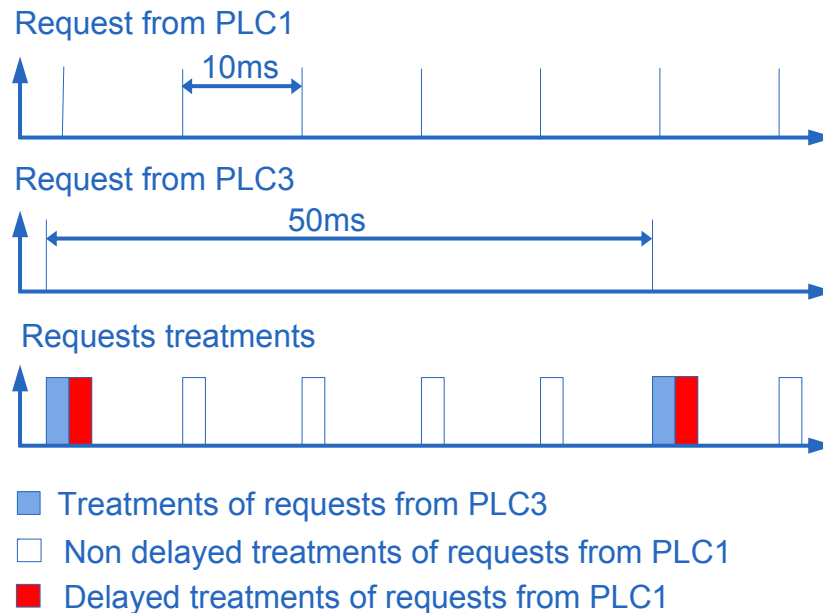
- More complex models that account for other communications (data exchange between PLCs, between PLCs and upper levels (SCADA, maintenance, production management systems, ...))
- Parametric model-checking so as to find sets of parameters of NAS that guarantee specified time performances bounds

Thank you for attention.

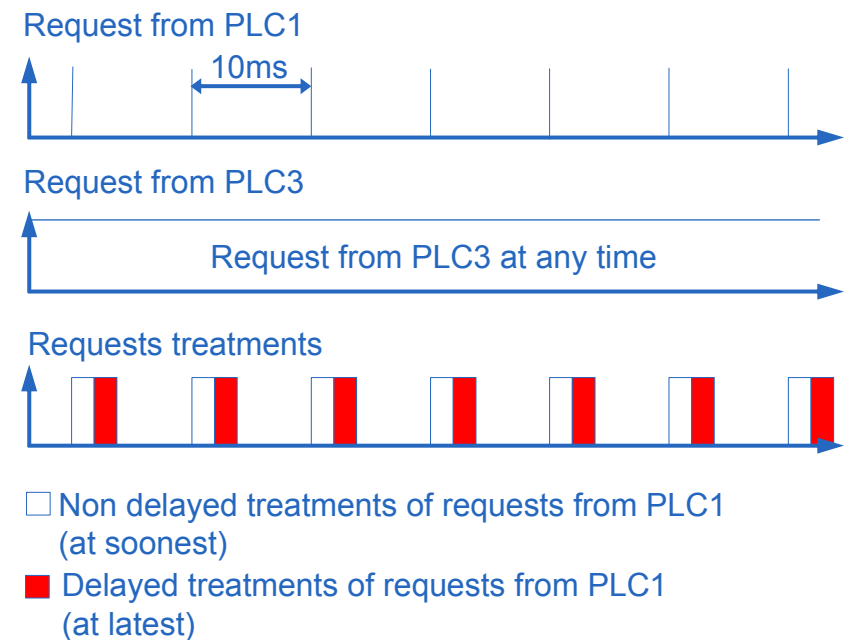
Questions ?

Behavior evolution

■ Initial behavior



■ Abstract behavior



■ With the abstract model, all requests might be delayed or not

- Adding unexpected behaviors
- Worst case model