This document must be cited according to its final version which is published in a conference proceeding as: S. Bhartiya, P. Dufour, F.J. Doyle III, "Thermal-hydraulic digester model using a higher order numerical method", American Institute of Chemical Engineers (AIChE) Fall meeting, Reno, Nevada, USA, november 5-7, 2001.

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Thermal-Hydraulic Digester Model Using A Higher Order Numerical Method

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http://fourier.che.udel.edu/~Agenda2020

AIChE Annual Meeting Reno, Nevada



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Motivation

- Chip level control
 - Digester endpoint Kappa # (Amirthalingam & Lee, 2000)
- Grade transition control
 - Hardwood/softwood swings
- Process monitoring and fault diagnosis

Development of a fundamental model based on mass, heat and momentum conservation

Literature Overview: Fundamental Continuous Digester Models - Purdue Model	
1974 —	Smith and Williams Series of CSTRs, 3 phase system, kinetic parameters
1982 —	Christensen et al. Optimal kinetic parameters, specie rate multiplier, mass transfer data
1986 —	Maras et al. Thermal balance for wood and liquor
1996 —	Kayihan <i>et al.</i> 2-vessel model
1997 —	Wisnewski et al. Improved defns. of mass conc. and volume fractions
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Model





Summary of Assumptions

• Radial property gradients neglected (P,M)

P - Purdue M - Michelsen

- Solid/entrapped phase in thermal and dynamic equilibria (M)
- Stratified, incompressible flow (*P*,*M*)
- Liquor-wall resistance neglected (correlation/experimental data) (M)
- Acceleration of liquor negligible (simplified) (M)
- Constant cross-sectional area (M)
- Pulping chemistry based on McKibbins (1960)
- Hydraulic constitutive laws based on Härkönen (1987)



Mass Continuity

Solid Phase

$$\frac{\partial \rho_{si}}{\partial t} = -v_c \, \frac{\partial \rho_{si}}{\partial z} + \hat{R}_{si}$$

Bulk flow Reaction

Entrapped Liquor Phase

$$\frac{\partial \rho_{ei}}{\partial t} = -\frac{\rho_{ei}}{\varepsilon} \frac{\partial \varepsilon}{\partial t} + -\frac{v_c}{\varepsilon} \frac{\partial (\varepsilon \rho_{ei})}{\partial z} + D(\rho_{fi} - \rho_{ei}) + \hat{R}_{ei}$$

Bulk flow Diffusion Reaction

Free Liquor Phase

$$\frac{\partial \rho_{fi}}{\partial t} = -v_c \frac{\partial \rho_{fi}}{\partial z} - D\varepsilon \frac{(1-\eta)}{\eta} (\rho_{fi} - \rho_{ei}) \pm \rho_{fi,ext} \frac{\dot{V}_{ext}}{\delta V_f}$$

Bulk flow Diffusion External flows

recirculation/extracts



Volume Continuity

Chip Phase Volume Continuity

$$\frac{\partial \eta}{\partial t} = \frac{\partial}{\partial z} \left[(1 - \eta) v_c \right]$$

Overall Digester Volume Continuity

$$\nabla_z (\dot{V_c} + \dot{V_f}) = 0$$

Space not occupied by chips must be filled with liquor



Momentum Conservation



Liquor Phase

$$\frac{\partial p_f}{\partial z} = -v_f \frac{\partial}{\partial z} \left[\rho_f v_f \right] - \eta v_f \frac{\partial \rho_f}{\partial t} + \rho_f g + \frac{F_{\Lambda}}{\eta}$$

Gravity Chip/liquor flow resistance



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Energy Conservation

Chip Phase

$$(C_{Ps}M_{s} + C_{Pe}M_{e}\varepsilon)\frac{\partial T_{c}}{\partial t} = -T_{c}\left(C_{Ps}\frac{\partial M_{s}}{\partial t} + C_{Pe}\frac{\partial (M_{e}\varepsilon)}{\partial t}\right) - v_{c}\frac{\partial}{\partial z}\left[(C_{Ps}M_{s} + C_{Pe}M_{e}\varepsilon)T_{c}\right] + \Delta H_{R}\sum_{i=1}^{5}\hat{R}_{si} + U(T_{f} - T_{c}) + D\varepsilon D_{E}$$
 Diffusive energy
Bulk Heat of reaction Interphase heat transfer
iquor Phase
$$C_{Pf}M_{f}\frac{\partial T_{f}}{\partial t} = -T_{f}\frac{\partial}{\partial t}(C_{Pf}M_{f}) \mp v_{f}\frac{\partial}{\partial z}(C_{Pf}M_{f}T_{f}) - U\frac{(1 - \eta)}{\eta}(T_{f} - T_{c}) + \frac{D\varepsilon D_{E}}{\eta} \pm \frac{\dot{V}_{ext}M_{ext}T_{ext}}{\delta V_{f}}$$

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Phenomenological Interactions





Computational Issues

Staggered Grid (Patankar, 1980)



- 96 control volumes (CVs)
- Height: 0.29 m /CV
- 2213 states
- All variable properties vary linearly

Simulation Time

80 hr sim time - 25 min. real time Sun Sparc Ultra 10 - 333Mhz



Production Rate Change

- Simultaneous chip feed and blow rate change
- Flow rate change of $\approx 11\%$ from nominal value
- Step change filtered using first order filter with 13 min. time constant







Transient Response





Near-Fault Scenario

• Step increase in white liquor flow





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initial

final



Contraction of the second seco

Enhanced Approximations For Plug Flow Using Finite Differences

1) Increase number of CSTRs

• increases number of model states

2) Use higher order information for approximation

$$\frac{du_i}{dz} = \frac{-u_{i-3} + 6u_{i-2} - 18u_{i-1} + 10u_i + 3u_{i+1}}{12}$$

• For the same volume, plug flow reactor shows higher conversion than CSTR

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Higher Order Numerical Method

• Better approximation of plug flow leads to lower Kappa



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Conclusions & Future Work

- A hydraulic extension of Purdue Model is presented
- Momentum transfer impacts K # and compaction profiles
- Simulation examples demonstrate coupling between momentum transfer and pulp quality profile
- A hybrid first/fourth order finite difference approximation shows increased conversion

Hardwood/softwood grade transition model extension
Kappa profile control in a continuous pulp digester



Acknowledgements

US Department of Energy

Westvāco



University of Delaware Process Control and Monitoring Consortium



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