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# **Periodic and disordered polytypes of SiC: A dynamic model based on local deformations**

G. L. VIGNOLES

and

R. NASLAIN

Laboratoire des Composites ThermoStructuraux

3, Allée La Boétie – Université Bordeaux 1

F33600 PESSAC, France

[vinhola@lcts.u-bordeaux1.fr](mailto:vinhola@lcts.u-bordeaux1.fr)

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## ABSTRACT

Silicon carbide exists under a great variety of polytypes that can be described by a sequence of orientations of biatomic Si-C layers in a stacking direction. A **dynamical model** is proposed for the formation of polytypes during the layer-by-layer growth of the material that occurs in CVD/CVI. A recurrence law is determined for the sequence of layer deformations ; the orientation sequence is derived from it. The evolution of this law allows one to reproduce qualitatively the whole polytypism of SiC: short- or long-period periodic polytypes, as well as one-dimensionally disordered polytypes. A two-parameter bifurcation diagram has been studied : its fractal structure allows one to visualize various types of "roads to chaos".

## INTRODUCTION

Silicon carbide is used, among others, as matrix in ceramic matrix composites (CMC) owing to its high melting point ( $T_d \sim 2500^\circ\text{C}$ ), its stiffness ( $E \sim 450 \text{ GPa}$ ), its low density ( $\sim 3.2 \text{ g. cm}^{-3}$ ) and its excellent behavior in oxidizing atmospheres (passive regime). It is deposited chemically from a gaseous precursor (*e. g.* a mixture of  $\text{CH}_3\text{SiCl}_3$  (MTS) and hydrogen), in the pore network of a porous preform by the so-called chemical vapor infiltration (CVI) process, at a temperature (*i. e.*  $900\text{-}1100^\circ\text{C}$ ) much lower than the decomposition temperature of SiC /1-3/. The nature of silicon carbide in the matrix of SiC-based CMC has been the subject of very few studies /4,5/ and is still an open question.

Silicon carbide is known to display a great variety of crystallographic forms, called polytypes, differing only along a stacking direction of plane, compact, biatomic layers (hereby referred to as bilayers). There are more

than 170 known polytypes exhibiting periodic orientation sequences /6-8/. Some of these structures display very large spatial periods ; others illustrate the phenomenon of one-dimensional disorder /8,9/. This is frequently the case in chemical vapor deposition (CVD) or infiltration (CVI) processes. Direct observation of disordered polytypes in SiC samples synthesized by CVI from a gas mixture of  $\text{CH}_3\text{SiCl}_3$  (MTS) and hydrogen has been made using high resolution transmission electron microscopy (HRTEM) /4,5/ (fig. 1), showing an abundant random repartition of rotational twins along the growth axis, and Raman spectroscopy /5/, showing a roughly equal intensity for  $\alpha$ - and  $\beta$ -SiC phonon peaks. Although many attempts have been made to explain the occurrence of polytypism, no model accounting simultaneously for the growth of *both* ordered and disordered polytypes has been proposed /10-12/. As the process is such that the chemical system lies **far from thermodynamical equilibrium**, it is not attempted to model polytypism by means of a phase diagram, but rather to build a **dynamical model**. It will be shown how disordered polytypes can appear from deterministic growth mechanisms yielding also all the known polytypes.

## 1. STRUCTURE DESCRIPTION

Silicon carbide polytypes may be described as different stacking sequences of Si-C bilayers along a  $\langle 111 \rangle_\beta$  or the  $[0001]_\alpha$  direction of the corresponding cubic or hexagonal structures, which are also the only growth directions of interest to control polytypism /6,7,13/. Each bilayer displays a hexagonal arrangement perpendicular to the growth direction /14/. A schematic representation is shown in fig. 2. Every new layer has a choice in orientation as it settles itself up on the former one : it can be deduced from the former layer either by a simple translation, or by a translation plus a  $180^\circ$  rotation. These two options are respectively described by the letters **k** and **h** in Jagodzinski's "**h-k**" notation /15/. The choice leads to two unequivalent atomic environments : when the orientation of the new layer is **h**, its upper atoms are in eclipsed conformation with respect to the lower atoms of the former layer, while they are staggered in **k** orientation /16/. Any polytype can be described by an orientation sequence  $U_n$ ,  $n$  being the integer layer index.  $U_n$  is a boolean sequence since it has only two possible values (**h** and **k**). As an example, the 15R polytype, whose Zhdanov notation /17/ is  $(23)_3$ , will be denoted (**hkhkk**)<sub>3</sub>.

## 2. LOCAL DEFORMATIONS

A detailed study of the structures of various non-cubic polytypes shows that every crystallographic site displays a slight deformation of its coordination tetrahedron, due to atomic interactions. This feature has been evidenced for SiC by different methods. Careful X-ray analyses of 2H-SiC /18/ and 6H-SiC /19/ have allowed previous authors to estimate non-ideal bond lengths and angles.  $^{29}\text{Si}$  and  $^{13}\text{C}$  NMR studies /20/ reported the existence of 4 different kinds of sites in usual polytypes (3C,2H,4H,6H and 15R) ;

they have been related to the orientation of their layer and of the neighboring one /20,21/. *Ab initio* pseudopotential total-energy calculations on relaxation effects in the bulk structure of 5 simple polytypes /22/ have also been made : they are in reasonable agreement with the X-ray data.

The deformations are elongations of the coordination tetrahedra along the growth axis, *i. e.*, the bond lengths parallel to this axis, which are inter-bilayer bond lengths (hereafter denoted  $L_n$ ), are longer than the other ones, located inside the bilayers (denoted  $l_n$ ). The relative difference between them,  $\delta_n = (L_n - l_n)/l_n$ , is less than 1%. The bond angles do not vary significantly /16,22/. The deformations are variable according to the sites, a feature which leads to suppose that they play an important role in the local stabilization of a given orientation for every new atomic bilayer. If account is not taken of dangling bond rearrangements at the surface, there are only three characteristic geometrical variables at each layer :  $L_n$ ,  $l_n$ , and the angle  $A_n$ . However, the first two will be retained since  $A_n$  does not vary significantly.

The relation between bond lengths and orientations is sketched in fig. 3, where the lengths for each bilayer, as calculated by Cheng *et al.* /22/, are represented as a point in the  $(L_n, l_n)$  space. The data can be clearly divided into two groups : one of low deformation and of orientation **k**, and one of higher deformation and of orientation **h**. A direct relation between bond distortions and orientations thus appears. Moreover, as the points are roughly aligned along the dotted line, it is possible to restrict oneself to only one variable in order to describe the deformations, for example  $\delta_n$ , as defined above, which varies along this line.

Fig. 4 shows the repartition of the different bilayers on a  $\delta_n$  axis, associated to their orientation  $U_n$ . The distinction between the **h** and **k** groups is clear. Going further, they can be split further into four groups, according to the nature of the orientation  $U_{n+1}$  of the following layer. These groups fit exactly the NMR shift groups as defined in /20,21/. A further splitting on the criterion of  $U_{n+2}$  is possible. The ordering of the arising  $U_n U_{n+1} U_{n+2}$  sequences is strikingly regular : if **k** is replaced by 0 and **h** by 1, then they follow the ordering of binary numbers : 000 < 001 < 010 < ....

### 3. THE ITERATIVE MODEL

The deformations  $\delta_n$ , as well as the orientations, can be considered as forming a sequence. The description of this real sequence is achieved through the determination of the recurrence law, *i.e.* the function  $f$  so that  $\delta_{n+1} = f(\delta_n)$ . To perform this, one has simply to plot  $\delta_{n+1}$  as a function of  $\delta_n$ . Fig. 5 exhibits such a plot, as built using the computation results of Cheng *et al.* /22/. The fitted curves represent portions of the recurrence law  $f$ , also called first return map.  $f$  appears to be a once discontinuous function increasing on both sides of the discontinuity  $\delta^*$ , that is, a "sawtooth map" /23,24/. The presence of the discontinuity is related to the change of the layer  $n$  from **h** to **k**, and is consistent with the fact that the orientation choice is not based on the  $\delta_n$ , but on an energetic cri-

terion. Since  $\delta_n < \delta^*$  implies  $U_n = \mathbf{k}$  and  $U_n = \mathbf{h}$  for the converse case, the orientation sequence is directly deduced from the deformation sequence.

#### 4.DYNAMICAL BEHAVIOR

In order to determine the possible dynamical behaviors of the model, an example of a family of maps similar to  $f$ , and of simpler analytic formulation, has been studied. This family is generated by varying two parameters  $\lambda_1$  and  $\lambda_2$  designed to tune the height of the two continuous parts of  $f$ :

$$f_{\lambda_1, \lambda_2}(x) = \begin{cases} 4\lambda_1 x(1-x) & \text{if } x \leq 1/2 \\ 1 - [4\lambda_2 x(1-x)] & \text{if } x > 1/2 \end{cases}$$

By variation of  $\lambda_1$  and  $\lambda_2$  and characterization of the permanent behaviour associated to every couple of parameters, a bifurcation diagram has been computed. By attributing a distinct color to each period between 1 and 256, one obtains the image in fig. 6. This picture has a fractal, *i. e.* self-similar appearance. The domains of dynamical stability of periodic behaviors are fish-like shaped regions obeying to two disposition rules ("fish reproduction rules") :

- Rule R1 : Between the "bodies" of two fishes of periodic sequences  $(A_1 A_2 \dots A_n)$  and  $(B_1 B_2 \dots B_m)$  lies a fish of sequence  $(A_1 A_2 \dots A_n B_1 B_2 \dots B_m)$ .

- Rule R2 : Between the "tails" of two fishes of sequences  $(A_1 A_2 \dots A_n)$  and  $(B_1 B_2 \dots B_m)$  lies a fish of sequence  $A_1 A_2 \dots \overline{A_n} B_1 B_2 \dots \overline{B_m}$ , where  $\overline{A_n}$  stands for  $\mathbf{h}$  if  $A_n = \mathbf{k}$  and reciprocally.

The nature of these laws (and consequently the structure of the diagram) has been demonstrated using the symbolic dynamics derived from the model, *i. e.* the dynamics of orientation sequences rather than the deformation sequences /24,25/. The basic feature lies in the above mentioned equivalence between the ordering of  $\delta_n$  and of the  $U_n U_{n+1} \dots$  sequences.

A consequence of rules R1 and R2 is that *any* imaginable orientation sequence, either periodic or chaotic, has a corresponding "fish" in the diagram of fig. 6. In particular, all known polytypes of length inferior to 50 have been attributed : they seem to lie in a restricted domain of the diagram, whose contour has been sketched.

The points corresponding to chaotic behavior in fig. 6 form a surface of fractal contour, whose noninteger dimension is roughly 1.6 : this means that chaos is a frequent possibility for the family of maps  $f_{\lambda_1, \lambda_2}$ . The symbolic approach allows to evidence the presence and the fractal structure of a frontier for topological chaos.

#### CONCLUSION

The above model, though minimal and very approximative, reproduces the richness of SiC polytypism. Its specificity is the ability to account for the formation of polytypes during SiC growth by CVD/CVI. The *same* physical bases (local interactions between bilayers) are used to describe the apparition of ordered (periodic) polytypes as well as disordered ones. It is possible to locate inside fig. 6 the disordered polytypic se-

quences present in SiC formed by CVD investigated by HRTEM /4,5/ - at least a finite sampling of them - with the help of the algebra of symbolic sequences derived from the iterative model.

## ACKNOWLEDGEMENTS

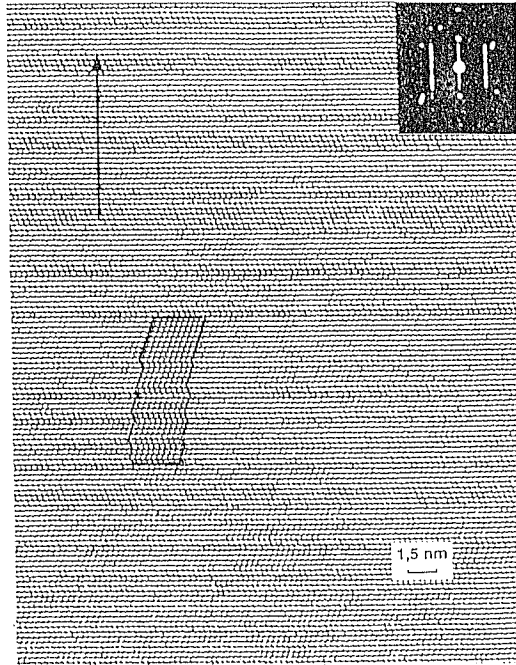
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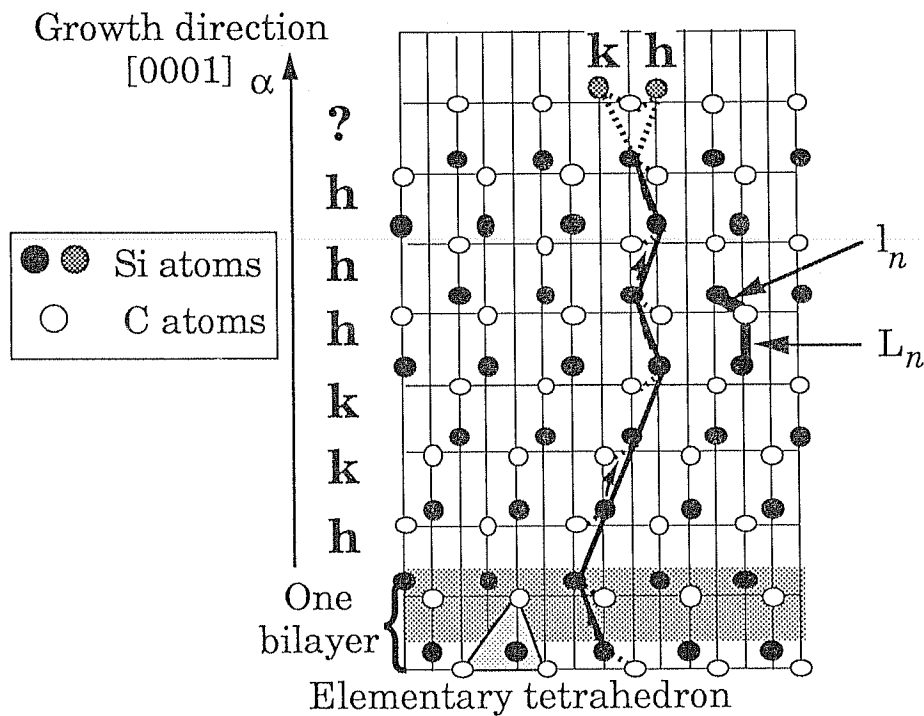
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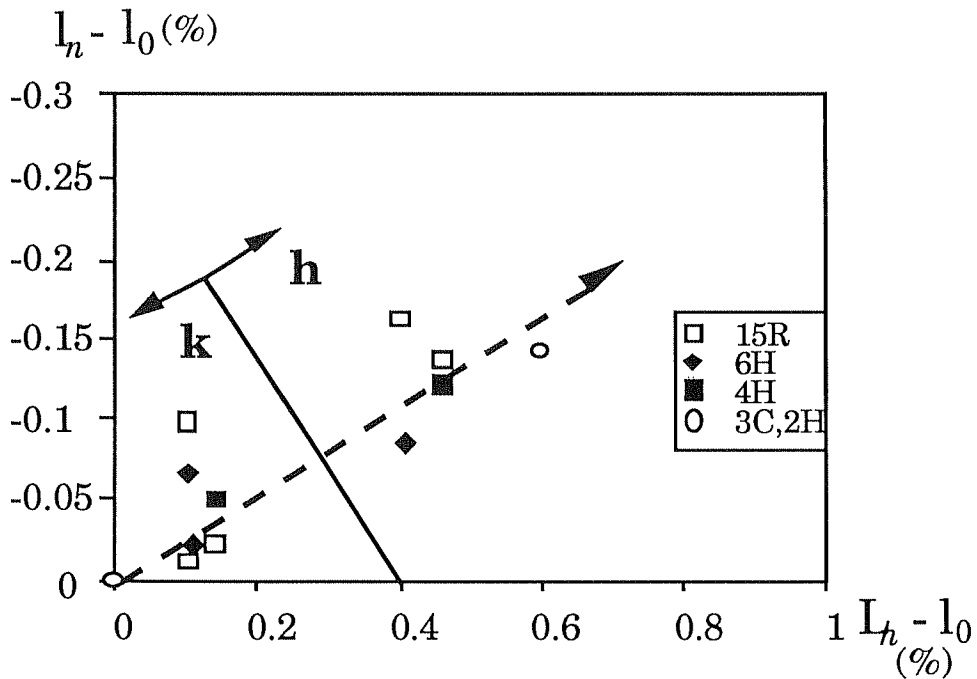




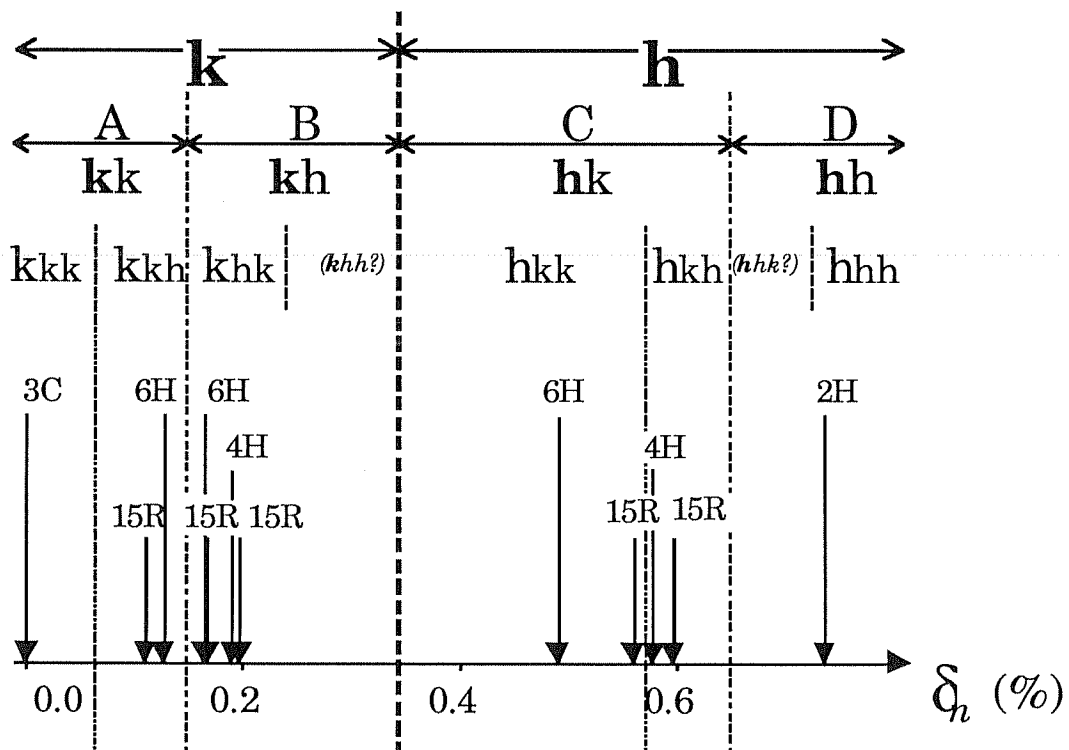
**Fig. 1 :** HRTEM photograph of a disordered SiC polytype observed along a  $\langle 11\bar{2}0 \rangle_\alpha$  direction. In the upper right corner, diffraction diagram showing disorder. In the middle left, superposition of a computed image. Image from /4/.



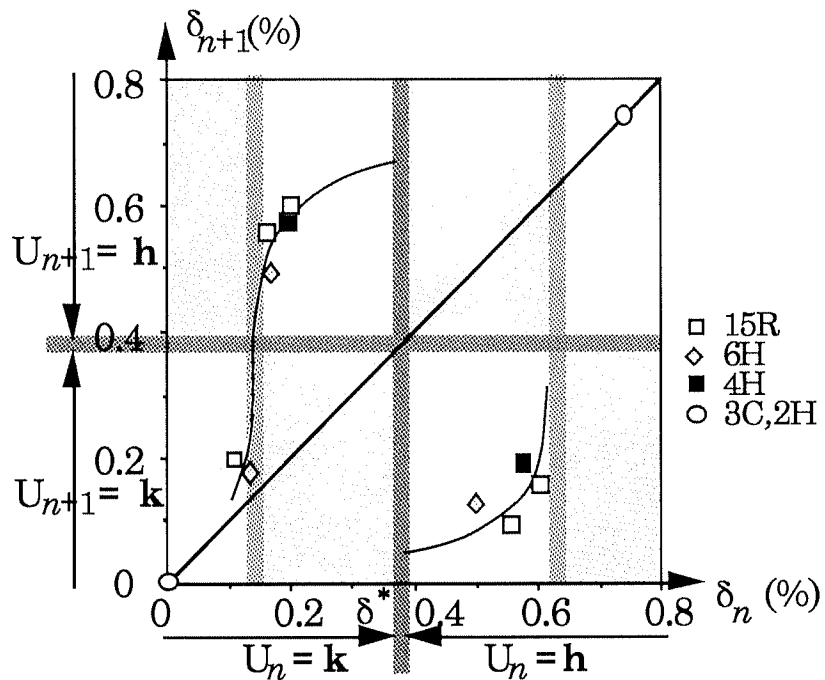
**Fig. 2 :** Schematic description of a disordered SiC polytype observed along a  $\langle 11\bar{2}0 \rangle_\alpha$  direction.



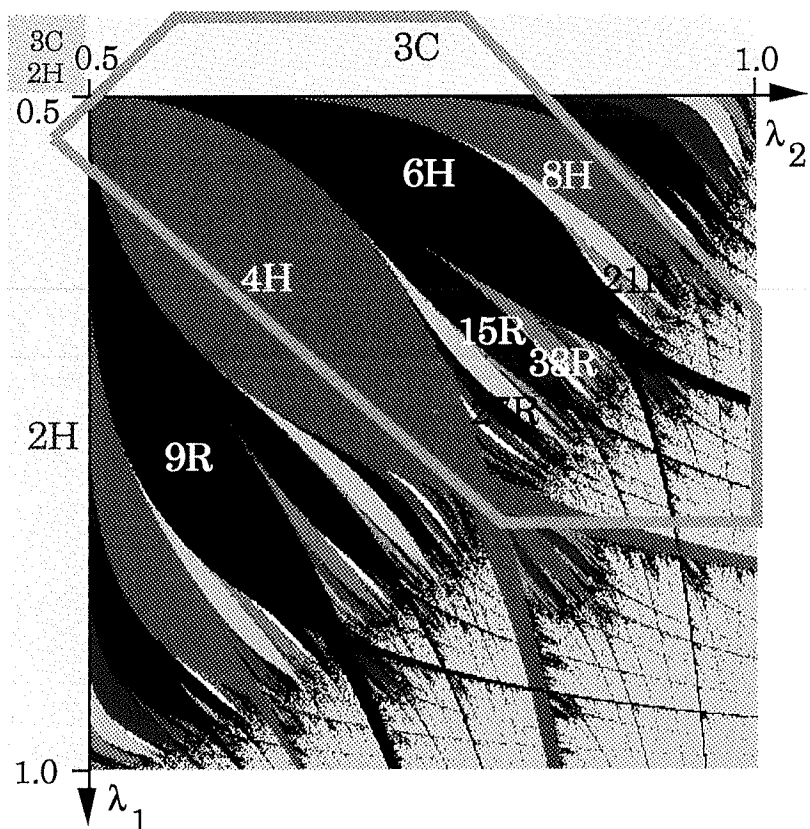
**Fig. 3 :** Representation of the layers of simple polytypes as points in the  $(L_n, l_n)$  space. The values are from /20/, and are given as differences with the ideal bond length  $l_0 (= L_0)$ .



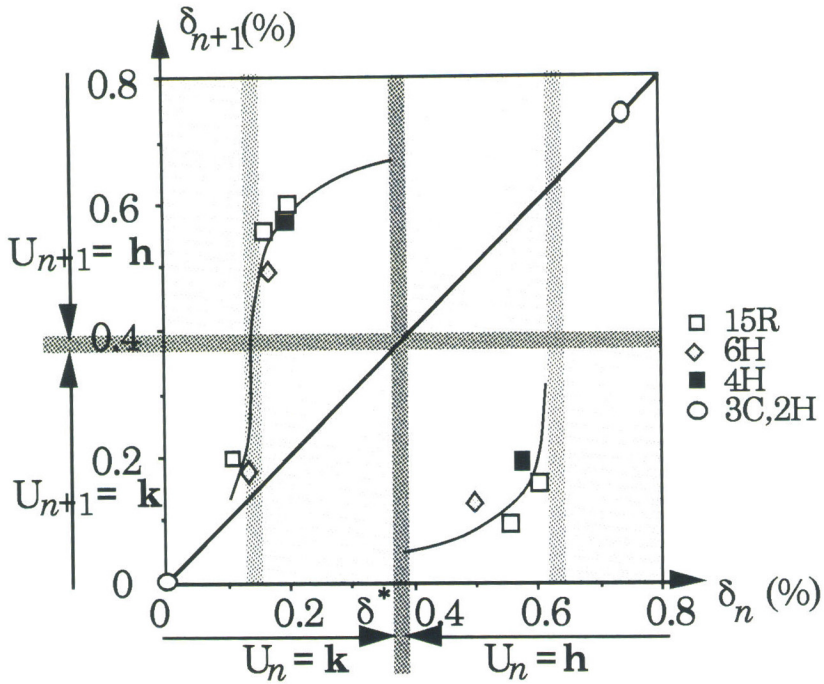
**Fig. 4 :** Correspondence between deformations  $\delta_n$ , orientation sequences in terms of **h** and **k** symbols and NMR shift groups (A, B, C and D).



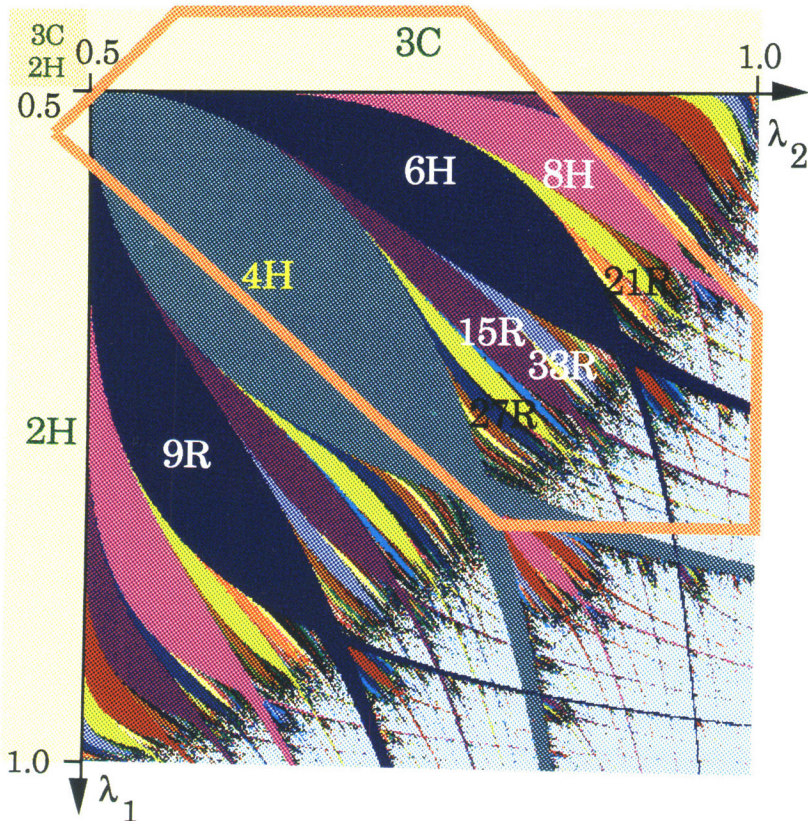
**Fig. 5 :** First return map of the deformations. The full line is a guess of the recurrence function  $f$ .



**Fig. 6 :** 2-parameter bifurcation diagram of the sawtooth map. The sketched contour "contains" all known polytypes of length  $\leq 50$ .



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