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# Ultralong-ranged spatial correlations of the dynamics of jammed systems

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We introduce a dynamic light scattering method, termed Space and Time Resolved Correlation (STRC), which enables us to resolve the dynamics of soft materials in space and time. We demonstrate STRC by investigating the slow dynamics of two jammed systems, a quasi two-dimensional foam made of deformable bubbles and a rigid gel network formed by strongly attractive colloidal particles. We find the dynamics of both systems to be determined by intermittent rearrangement events. For the foam, the events extend over a few bubble sizes, but a small, finite dynamical correlation is observed up to macroscopic length scales. For the gel, rearrangement events involve correlated motion over surprisingly large distances, comparable to the system size. These results indicate that dynamical correlations in jammed systems can be extremely long-ranged and point to the key role of mechanical properties in determining dynamical correlations.

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The slow relaxation of molecular fluids, colloidal suspensions and granular materials becomes increasingly heterogeneous [1, 2, 3, 4, 5] as the glass [6] or jamming [7] transitions are approached. In these systems, structural relaxation can only occur through the correlated motion of clusters of particles, leading to spatial correlations of the local dynamics, in contrast to dilute systems where the dynamics of distinct particles are independent. Simulations [3] and experiments [1, 2, 4, 8, 9] on molecular and colloidal supercooled fluids show that the range of dynamical correlations is typically moderate, at most a few particle sizes close to the glass transition. Experiments in driven granular systems [5, 10] support similar conclusions for athermal systems approaching jamming. However, it has been recently argued [11] that in jammed materials any local rearrangement should propagate elastically over large distances, leading to long-ranged dynamical correlations.

Testing these ideas is a challenging task. Temporal fluctuations of the dynamics of a colloidal suspension close to random close packing have been recently attributed to system-size rearrangement events [12], but no direct measurements of the local dynamics were possible in these light scattering experiments. Spatial correlations of the dynamics can of course be investigated in simulations, but the linear size of the simulation box is typically limited to 10-20 particles. Optical or confocal microscopy of colloidal suspensions or imaging of 2-dimensional driven granular materials could in principle address this issue. In practice, however, the number of particles that can be followed is limited. This is because the spatial resolution is a fixed fraction of the field of view in conventional imaging techniques. Near jamming the particle displacements are very restrained, such that a high magnification has to be chosen to resolve them;

this consequently limits the field of view and thus the number of probed particles.

Here, we overcome these limitations by introducing a novel optical method that combines features of both dynamic light scattering [13] and imaging. The method, termed Space and Time Resolved Correlation (STRC) [14], decouples the length scale over which the dynamics is probed from the size of the field of view, thereby allowing long-ranged correlations to be measured. We demonstrate STRC by measuring the range,  $\xi$ , of spatial correlations of the dynamics in three systems: a diluted suspension of Brownian particles, and two jammed materials, a foam and a colloidal gel. As expected, we find no spatial correlations in the dynamics of the Brownian particles. By contrast, the foam and the gel exhibit extended dynamical correlations. For the foam consisting of deformable bubbles that can easily slip around each other,  $\xi$  is of the order of a few bubble sizes, but partially correlated motion is also observed on larger length scales. For the gel consisting of rigidly bounded hard colloids, the range of correlation is comparable to the system size, thousands of times larger than the particle size. These experiments demonstrate the existence of extended correlations of the dynamics in jammed systems and point to the key role of the system mechanical properties in determining their range.

The Brownian particles are polystyrene spheres of radius 265 nm, suspended in a mixture of water and glycerol at a volume fraction  $\varphi \sim 10^{-4}$ . The foam is a commercial shaving foam consisting of tightly packed, poly-disperse bubbles (gas fraction  $\approx 0.92$ ), a model system used to study intermittent dynamics in previous investigations [15]. To avoid multiple scattering, we confine the foam in a thin cell, of thickness 1-2 bubble layers. The foam coarsens with time: the data reported here

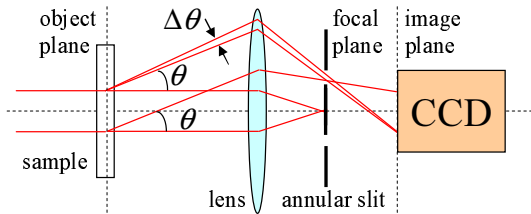


FIG. 1: (Color online) Schematic view of the low-angle, space-resolved light scattering apparatus.

are taken 6.1 h after producing the foam, when the average bubble radius is  $\sim 80\mu\text{m}$ . As an example of a system where jamming results from attractive interactions [16], we study a gel made of aggregated polystyrene particles of radius 20 nm at  $\varphi = 6 \times 10^{-4}$ , 32.3 h after the gel was formed. Details of the system can be found in [17, 18]; its average dynamics are representative of those of a wide class of soft glassy materials (see e.g. [19] and refs. therein). We express all time scales in units of  $\tau_r$ , the relaxation time of the average dynamics, defined by  $f(\tau_r) = e^{-1}$ , with  $f(\tau)$  the usual average dynamic structure factor. For the Brownian particles, foam, and gel,  $\tau_r = 42, 140,$  and  $5000$  s, respectively. For all samples, the dynamics are stationary on the time scale of the experiments.

The space-resolved dynamic light scattering apparatus is shown in Fig. 1. The sample cell of thickness  $L = 2$  or  $0.1$  mm for colloids and foams, respectively, is placed in a temperature-controlled bath (not shown in Fig. 1) and is illuminated by a collimated laser beam with a diameter of 8 mm and a wavelength of  $\lambda = 633$  nm. A lens with a focal length of 40 mm is used to form an image of the sample onto the detector of a CCD camera, typically with magnification 0.8-1.3, depending on the sample. We place an annular aperture of radius 9 mm in the focal plane of the lens, so that only light scattered within a small angular interval  $\Delta\theta/\theta \approx 0.1$  around  $\theta \approx 6.4$  deg contributes to the formation of the image. The CCD images have a speckled appearance [20], due to the coherence of the source. The electric field within any given speckle results from the sum of the contributions due to all scatterers within a small volume of the sample, of lateral extension  $\approx \lambda/\Delta\theta$  [20] and depth  $L$ . Our setup combines features of both imaging and scattering methods: similarly to imaging techniques and in contrast to usual scattering methods, each location on the CCD detector corresponds to a precise location in the sample. However, similarly to scattering methods and unlike conventional imaging, only light scattered at a chosen angle is collected by the detector, allowing one to probe the structure and the dynamics of the sample on a well defined length scale  $\sim q^{-1}$ , where  $q = 4\pi n/\lambda \sin \theta/2 \approx 1 \mu\text{m}^{-1}$  is the scattering vector, with  $n$  the sample refractive index.

In order to resolve the dynamics of our systems in space

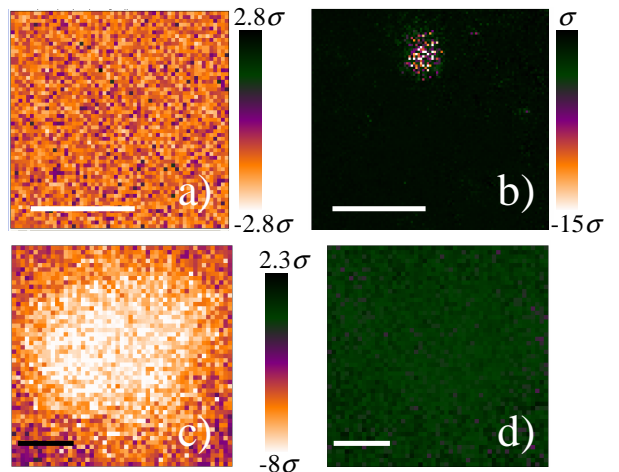


FIG. 2: (Color online) Dynamic activity maps. In each image, the bar corresponds to 2 mm. The color code indicates, in units of standard deviations  $\sigma$ , the fluctuations of the local  $c_I$  with respect to its temporal average. a): Brownian particles ( $\tau = 0.2$  s,  $\tau/\tau_r = 0.0048$ , with  $\tau_r$  the relaxation time of the spatially and temporally averaged dynamics); b) foam ( $\tau = 3$  s,  $\tau/\tau_r = 0.021$ ); c) and d): colloidal gel ( $\tau = 500$  s,  $\tau/\tau_r = 0.1$ ) during a rearrangement event and a quiescent interval, respectively.

and time, we take a time series of CCD images at a fixed rate. Each image is divided in regions of interest (ROIs), typically squares of side 10 – 20 pixels containing  $\sim 100$  speckles and corresponding to about  $50^2 - 150^2 \mu\text{m}^2$  in the sample. The local dynamics within a given ROI is quantified by a two-time degree of correlation [21]:

$$c_I(t, \tau; \mathbf{r}) = \frac{\langle I_p(t)I_p(t + \tau) \rangle_{\text{ROI}(\mathbf{r})}}{\langle I_p(t) \rangle_{\text{ROI}(\mathbf{r})} \langle I_p(t + \tau) \rangle_{\text{ROI}(\mathbf{r})}} - 1, \quad (1)$$

with  $\mathbf{r}$  the position of the center of the ROI,  $I_p(t)$  the intensity of the  $p$ -th pixel of the ROI at time  $t$ , and  $\langle \dots \rangle_{\text{ROI}(\mathbf{r})}$  the average taken over all pixels within the ROI. The space and time resolved dynamic structure factor is given by  $f(t, \tau; \mathbf{r}) = \sqrt{\beta^{-1}c_I(t, \tau; \mathbf{r})}$ , with  $\beta \lesssim 1$  an instrumental constant [13] and  $f(t, \tau; \mathbf{r}) = N^{-1} \sum_{j,k} \exp[i\mathbf{q} \cdot (\mathbf{r}_j(t) - \mathbf{r}_k(t + \tau))]$ , where the sum is over the  $N$  scatterers belonging to the sample volume associated to the ROI. The usual intensity correlation function  $g_2(\tau) - 1$  measured in traditional light scattering is the average of  $c_I(t, \tau; \mathbf{r})$  over both  $t$  and  $\mathbf{r}$ . By applying Eq. (1) to all ROIs, we build a “dynamical activity map” (DAM) showing the local degree of correlation, characterizing the change in configuration during the time interval  $[t, t + \tau]$ , as a function of the position in the sample.

We show in Fig. 2 representative DAMs for the three samples [for movies formed by a sequence of DAMs see [22]]. While previous works on dynamical heterogeneity have often dealt with the spatial correlation of the dynamics on a time scale comparable to the average

relaxation time  $\tau_r$  [5, 10, 23], here we focus on smaller time lags, for which individual rearrangement events are best visualized. As a control test, we show in Fig. 2a a DAM for a suspension of Brownian particles. The dynamics exhibit spatial fluctuations, without any obvious spatial correlation, consistent with the behavior expected for diluted, non-interacting scatterers. A typical DAM for the foam exhibiting an intermittent rearrangement event is shown in Fig. 2b. Contrary to the case of the Brownian particles, the dynamics is clearly inhomogeneous: the bright spot at the top of the field of view corresponds to an extended region with a large loss of correlation, while the rest of the sample experiences only a marginal change in configuration. Inspection of the full DAM movie [22] reveals that the foam dynamics is dominated by similar rearrangement events, which occur intermittently throughout the sample. We identify these events with the local bubble rearrangements driven by the accumulation of internal stress due to coarsening. Spatial maps of the dynamics of the colloidal gel are shown in Fig. 2c and d. Similarly to the foam, the dynamics is due to intermittent rearrangement events (c), separated by quiescent periods (d). These events, however, extend over strikingly large length scales, comparable to the system size, suggesting that any local rearrangement must propagate very far throughout the gelled network.

To better evaluate the spatio-temporal correlations of the dynamics, we compare in Fig. 3 the time evolution of the instantaneous degree of correlation  $c_I(t, \tau; \mathbf{r})$  in three ROIs, two of which are adjacent, while the third one is at least 3.1 mm apart from the first one. Data for the Brownian particles are shown in the top panel. The local dynamics fluctuates in a noise-like way and fluctuations in distinct ROIs appear to be uncorrelated, whatever the distance between ROIs. For the foam (middle panel), individual rearrangement events such as the one observed in Fig. 2b result in deep downward spikes, lasting  $\sim 3$  s, departing from the average value of  $c_I$  by several standard deviations. The  $c_I$  traces for adjacent ROIs appear to be strongly correlated, while the spikes in the trace of the third ROI, located at a distance  $\Delta r = 3.1$  mm from the first one, are almost completely uncorrelated, consistent with the typical event size inferred from the DAM of Fig. 2b. For the colloidal gel (bottom panel), we find that essentially all ROIs present strongly correlated  $c_I$  traces, suggesting that the ultra-long ranged rearrangement events depicted in Fig. 2c are indeed representative of the typical behavior of the gel. The duration of these events is of the order of  $10^3$  s.

We quantify the spatial correlation of the dynamics by introducing a “four point” correlation function  $\tilde{G}_4(\Delta r, \tau)$  that compares the dynamical activity in two small regions separated by  $\Delta r$  over a time interval  $\tau$ . We define  $G_4$  as

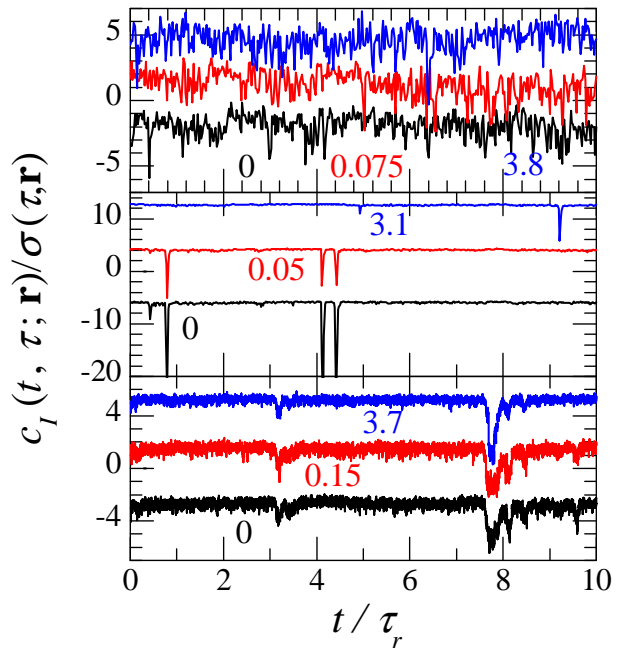


FIG. 3: (Color online) Instantaneous degree of correlation  $c_I(t, \tau, \mathbf{r})$ , normalized by its standard deviation  $\sigma(\tau, \mathbf{r})$ , measured at three different locations in the sample, as a function of reduced time  $t/\tau_r$  (for the sake of clarity, the curves are offset along the vertical axis and only a limited portion of the data is shown). Data have been corrected for instrumental noise as explained in Ref. [24]. For each sample, curves are labeled by the distance in mm with respect to the location for the black curve. Top: Brownian particles; middle: foam; bottom: colloidal gel. For all samples,  $\tau/\tau_r$  is as in Fig. 2.

the crosscorrelation of the local dynamics [3, 5, 10, 23]:

$$\tilde{G}_4(\Delta r, \tau) = \left\langle \frac{\langle \delta c_I(t, \tau; \mathbf{r}_1) \delta c_I(t, \tau; \mathbf{r}_2) \rangle_t}{\sigma(\tau, \mathbf{r}_1) \sigma(\tau, \mathbf{r}_2)} \right\rangle_{|\mathbf{r}_1 - \mathbf{r}_2| = \Delta r}. \quad (2)$$

Here,  $\delta c_I(t, \tau; \mathbf{r}) = c_I(t, \tau; \mathbf{r}) - \langle c_I(t, \tau; \mathbf{r}) \rangle_t$  and  $\sigma(\tau, \mathbf{r}_1) = \sqrt{\langle \delta c_I(t, \tau; \mathbf{r})^2 \rangle_t}$ , with  $\langle \cdot \cdot \cdot \rangle_t$  an average over time. Figure 4 shows  $\tilde{G}_4$  for the Brownian particles (blue squares). The spatial correlation decays nearly completely over one ROI size, confirming that the dynamics of diluted Brownian particles are spatially uncorrelated. The spatial correlation of the dynamics of the foam and the gel are shown in Fig. 4 as red triangles and black circles, respectively. Here, a slightly different normalization has been chosen: as discussed in Ref. [24],  $c_I$  contains a noise contribution stemming from the finite number of speckles. The noise of distinct ROIs is uncorrelated and thus does not contribute to the numerator of Eq. (2); however, it does add an extra contribution for  $\Delta r = 0$ . We thus plot only data for  $\Delta r > 0$  and define  $G_4(\Delta r, \tau) = b \tilde{G}_4(\Delta r, \tau)$ , with  $b \gtrsim 1$  chosen so that  $G_4(\Delta r, \tau) \rightarrow 1$  for  $\Delta r \rightarrow 0$ .

For the foam, most of the decay of  $G_4$  is well described by a slightly compressed exponential,  $G_4 = \exp[-(\Delta R/\xi)^p]$ , with  $p = 1.27$  and  $\xi = 0.6$  mm, cor-

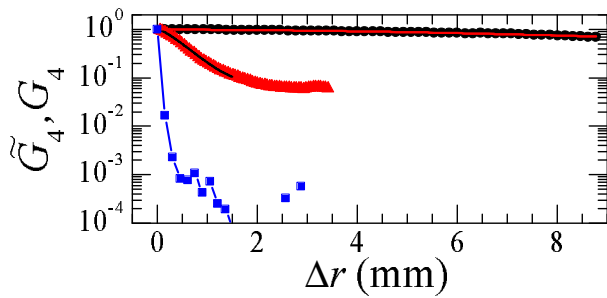


FIG. 4: (Color online) Spatial correlation of the dynamics for diluted Brownian particles ( $\bar{G}_4$ , blue squares), for a foam ( $G_4$ , red triangles), and for a colloidal gel ( $G_4$ , black circles). The lines are stretched exponential fits to the decay of  $G_4$ , yielding  $\xi = 0.6$  and  $16.4$  mm for the foam and the gel, respectively. For all samples,  $\tau/\tau_r$  is as in Fig. 2.

responding to 8 bubble radii (black line), denoting the size of rearrangement events, in agreement with previous estimates [15]. Interestingly, this decay is followed by a plateau  $G_4 \approx 7 \times 10^{-2}$  that extends over the full field of view,  $\Delta r \lesssim 4$  mm. This indicates that, although the spatial correlations of the dynamics are dominated by the typical size of rearrangements such as that shown in Fig. 2b, these local events have also a small impact on the rest of the sample, arguably because of the foam elasticity. By contrast, elastic strain propagation has a dramatic effect in the gel, where the range of dynamical correlation is strikingly large:  $G_4$  only decays by about 25% over 8 mm. A compressed exponential fit of  $G_4$  (red line) yields  $p = 1.8$  and  $\xi = 16.4$  mm, demonstrating that the dynamics are strongly correlated over distances far larger than any relevant structural length scale: the particle diameter is 20 nm and the gel is formed by fractal clusters of size  $\approx 20 \mu\text{m}$ . The differences observed in the spatial extent of correlated dynamics of our two jammed systems can be understood considering their distinct mechanical properties. The foam consists of deformable bubbles, for which the resistance to sliding around each other is relatively small. Thus, the motion of one bubble mostly occurs with the displacement of only a limited number of nearby bubbles. In the colloidal gel, by contrast, the motion of one strand sets a long-ranged strain field, because both the particles and the bonds between them are rigid and do not allow for a localized reorganization.

Our experiments show that the dynamics of jammed systems can exhibit surprisingly long-ranged spatial correlations, which exceed by far those reported in previous works on molecular and colloidal glass formers and in driven granular media. The technique introduced here should provide a flexible and valuable tool to test the generality of these findings. Using a modified version of the setup with  $\theta = 90$  deg, we have probed dynamical spatial correlations in other glassy soft materials (a Laponite suspension [25] and jammed multilamellar vesicles

[14, 26]), finding similar results. Finally, STRC could also be extended to different kinds of radiation, to probe, e.g., molecular glass formers. For example, in Fluctuation Electron Microscopy (FEM) [27] an optical layout similar to that of Fig. 1 is used and the STRC method could be adopted to analyze the FEM speckle images to monitor the dynamics with spatial resolution.

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