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Maxwell Zimmerley, Pierre Mahou, Delphine Débarre, Marie-Claire Schanne-Klein, Emmanuel Beaurepaire. Probing ordered lipid assemblies with polarized third-harmonic-generation microscopy. Physical Review X, 2013, 3 (1), pp.11002. 10.1103/PhysRevX.3.011002. hal-00324248

HAL Id: hal-00324248

https://hal.science/hal-00324248

Submitted on 20 Nov 2013

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Probing Ordered Lipid Assemblies with Polarized Third-Harmonic-Generation Microscopy

Maxwell Zimmerley, Pierre Mahou, Delphine Débarre, Marie-Claire Schanne-Klein, and Emmanuel Beaurepaire Laboratory for Optics and Biosciences, École Polytechnique, CNRS UMR 7645, INSERM U696, 91128 Palaiseau, France (Received 4 August 2012; revised manuscript received 29 September 2012; published 14 January 2013)

Ordered lipid assemblies are responsible for important physiological functions including skin barrier and axon conductivity. However, techniques commonly used to probe molecular order such as X-ray scattering and nuclear magnetic resonance are not suited for *in-situ* tissue studies. Here, we identify and characterize a novel contrast mechanism in nonlinear optical microscopy which is sensitive to molecular ordering in multilamellar lipid vesicles (MLVs) and in samples obtained from human skin biopsy: polarized third-harmonic generation (P-THG). We develop a multiscale theoretical framework to calculate the anisotropic, nonlinear optical response of lipid arrays as a function of molecular order. This analysis reveals that conserved carbon-carbon bond and aliphatic tail directionality are the atomic- and molecular-scale sources of the observed P-THG response, respectively. Agreement between calculations and experiments on lipid droplets and MLVs validates the use of P-THG as a probe of lipid ordering. Finally, we show that P-THG can be used to map molecular ordering in the multilamellar, intercorneocyte lipid matrix of the stratum corneum of human skin. These results provide the foundation for the use of P-THG in probing molecular order and highlight a novel biomedical application of multiphoton microscopy in an optically accessible tissue relevant to monitoring lipid-related disorder.

DOI: 10.1103/PhysRevX.3.011002 Subject Areas: Biological Physics, Interdisciplinary Physics, Optics

I. INTRODUCTION

Ordered lipid assemblies are physiologically important structures participating in functions such as skin barrier and neuronal signaling. Although the supramolecular organization of lipid arrays is critical for proper function, it cannot be studied in situ and at the subcellular scale, however, using techniques such as x-ray scattering (XRS) and nuclear magnetic resonance (NMR). Recently, laserbased, coherent nonlinear optical microscopy (NLOM) has emerged as a possible approach for investigating molecular order in intact biological tissues. In addition, there has been an increased interest in characterizing the polarization-based optical response of ordered structures by using second-harmonic [1-7] and third-harmonic [8-10] generation (SHG and THG, respectively) and four-wave mixing [11] (FWM), which are all sensitive to the electronic properties of the material, as well as vibration-sensitive coherent-anti-Stokes-Raman-scattering (CARS) microscopy [12-15] and stimulated-Ramanscattering (SRS) [16] microscopy.

As in conventional polarized-light microscopy, polarization control in NLOM (P-NLOM) can be used to reveal material anisotropy and molecular ordering by determining the polarization dependence of the nonlinear optical (NLO)

Published by the American Physical Society under the terms of the Creative Commons Attribution 3.0 License. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI. signal. This approach couples the biocompatibility, three-dimensional (3D) signal localization, and specificity inherent in NLOM with the ability to probe molecular order, holding promises for advanced imaging studies of molecular arrays in tissues. In addition, while the theory describing multiscale, multiphoton light-matter interactions is complex, experimentally the typical NLOM setup need only be slightly modified by the simple incorporation of wave plates and polarizers.

In this study, we establish the sensitivity of P-THG to the orientation and ordering of lipids and thoroughly characterize this novel NLOM contrast for biomedical applications. This verification requires calculating the third-order nonlinear optical properties at each scale, followed by simulating the nonlinear light-matter interactions near the microscope focus. To that end, we first develop and validate a model for calculating the nonlinear optical response of individual lipid molecules and ordered lipid structures. We compare the calculated results to P-THG imaging experiments of multilamellar lipid vesicles (MLVs), establishing that polarization sensitivity correlates with molecular ordering, and validating the theoretical model. Finally, we present a biomedical application of P-THG toward monitoring lipid order in the outermost layer of human skin [called the stratum corneum (SC)] at the submicrometer scale of the intercorneocyte multilamellar matrix.

II. MODEL

On the molecular scale, the polarization-dependent, nonlinear optical response of third-order processes such as THG and CARS is described by the hyperpolarizability γ . γ is an 81-element tensor that maps three incident

^{*}Present address: Laboratory of Interdisciplinary Physics, Université Joseph Fourier, CNRS UMR 5588, 38402 Saint Martin d'Hères, France

electric fields to the induced molecular dipole moment $e\mathbf{r}^{(3)}$ according to [17]

$$er_i^{(3)}(\omega_4) \propto \sum_{jkl} \gamma_{ijkl}(-\omega_4; \omega_3, \omega_2, \omega_1)$$

$$\times E_i^{loc}(\omega_3) E_k^{loc}(\omega_2) E_l^{loc}(\omega_1) \qquad (1)$$

where e is the electron charge, i, j, k, l are any of the three Cartesian indices in the molecular frame, $\mathbf{E}^{\mathrm{loc}}(\omega_n)$ is the local electric field oscillating at frequency ω_n , and $\omega_4 = \omega_1 + \omega_2 + \omega_3$. For the THG process, $\omega_1 = \omega_2 = \omega_3$; for the CARS process, $\omega_2 < 0$, and $\omega_1 + \omega_2$ matches a vibrational eigenfrequency of the molecule.

In the approximately $1-\mu m^3$ excitation volume typical for NLOM, the detected signal reflects the averaged nonlinear optical response of the entire molecular ensemble located at the focus. At this scale, the induced nonlinear polarization $\mathbf{P}^{(3)}$ is

$$P_I^{(3)}(\omega_4) \propto \sum_{JKL} \chi_{IJKL}^{(3)}(-\omega_4; \omega_3, \omega_2, \omega_1)$$

$$\times E_J(\omega_3) E_K(\omega_2) E_L(\omega_1) \tag{2}$$

where the nonlinear susceptibility tensor $\chi^{(3)}$ is dependent on the molecular geometries and γ at the focus, and I, J, K, L are any of the Cartesian indices in the laboratory frame. The symmetry properties of $\chi^{(3)}$ can be determined experimentally from the magnitude and directionality of the P-NLOM response, revealing information on the local molecular organization. For example, when tuned to match the CH₂ stretch frequency, P-CARS images of lipid bilayers show a maximum nonlinear response for excitation fields oriented parallel to the bilayer surface [18], that is, parallel to the CH₂ moiety. The CH₂ vibrational modes determine the symmetry properties of the molecular vibrational hyperpolarizability $\gamma^{\rm vib}$ which, when averaged over the orientations found in a bilayer, produces an asymmetric vibrational $\chi^{(3)}$.

Conversely, we note that the carbon-carbon (CC) bonds forming the lipid backbone show an average directionality parallel to the bilayer normal. According to Kajzar and Messier [19], the average electronic hyperpolarizability of CC bonds $\langle \gamma^{\text{CC}} \rangle$ is approximately 6 times larger than that of CH bonds, hinting that this may be the source of a previously unnoticed asymmetric electronic $\chi^{(3)}$ that can be probed with P-THG. We later present experimental data on model lipid systems and human skin samples demonstrating that this is indeed the case. Before we do that, however, we derive the P-THG response from multilamellar lipid structures using a multiscale approach, summarized visually in Fig. 1. First, we calculate the electronic hyperpolarizability of a single lipid (1,2-Dimyristoyl-sn-glycero-3phosphorylcholine [DMPC]) molecule γ^{DMPC} from an energy-optimized structure calculated by Krishnamurty et al. [20]. Next, we use γ^{DMPC} to determine the electronic nonlinear susceptibility tensors $\chi^{(3)\mathrm{ML}}$ of liquid- and gelphase multilamellar (ML) DMPC arrays. Then, with the determined values of $\chi^{(3)\text{ML}}$, we perform numerical calculations to predict the expected P-THG signal at lipid interfaces.

A. Calculating the molecular hyperpolarizability

We calculate the elements of γ^{DMPC} using the bond-additivity model. We therefore assume that the nonlinear response of the molecule is a direct sum of the individual bond hyperpolarizabilities and that each bond hyperpolarizability is independent of the local electronic structure. To simplify the calculation, we relegate each bond type to having either a net isotropic (i) or polarization-sensitive (p) effect, and split up the hyperpolarizability [see Fig. 1(a)]:

$$\gamma^{\text{DMPC}} = \gamma^{i} + \gamma^{p}. \tag{3}$$

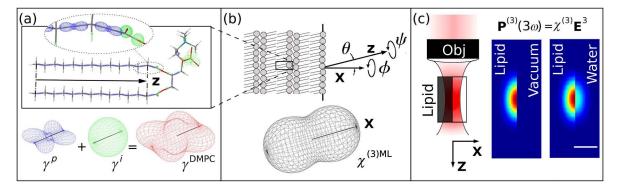


FIG. 1. Visual summary of calculations. (a) In the bond-additivity model, each bond contributes γ^{mol} . The non-CC bonds contribute isotropically while the CC-bond directions give rise to a directed $\chi^{(3)}$. The nonlinear dipole moment $|e\mathbf{r}^{(3)}(3\omega)|$ is calculated as a function of excitation angle [Eq. (1)] for γ^p (blue mesh), γ^i (green mesh), and γ^{DMPC} (red mesh). The black lines are the same length and indicate the molecular z axis. (b) The lipids within the bilayer rotate freely about ψ , ϕ and adopt a Gaussian distribution of angles relative to the bilayer normal (laboratory X axis). Averaging of γ^{DMPC} about these axes results in $\chi^{(3)\text{ML}}$. The grey mesh shows the lipid nonlinear polarization $|\mathbf{P}^{(3)}(3\omega)|$, and the black line indicates the bilayer normal. (c) Left: Simulated focal volume half-filled with ordered lipid (dark gray) and either vacuum or water (clear). Right: Focal distribution of induced $\mathbf{P}(3\omega)$ in each material at the focus (NA = 0.8, λ = 1180 nm, $n_{\omega} = n_{3\omega} = 1.33$, scale bar 500 nm).

Examination of the molecular structure of DMPC allows us to identify the PO, CN, and CO bonds as those contributing to γ^{i} . In the head group of the DMPC molecule, the four PO and four CN bonds are oriented in a tetrahedral geometry around the P and N atoms, respectively. For the CO bonds, the flexibility of the head group, the low cumulative directionality of the single CO bonds, and the CCto-double-CO-bond ratio of 29:2 all indicate that the anisotropic contributions of the CO bonds are negligible. Finally, while the number of CH bonds is approximately double the number of CC bonds, the orientation and low magnitude of $\langle \gamma^{CH} \rangle$ compared to $\langle \gamma^{CC} \rangle$ indicate that the CH bonds only increase the isotropy of the DMPC molecular hyperpolarizability, allowing us to relegate all non-CC bonds to γ^i . We may thus calculate the quantity γ^i as the direct sum of the various non-CC-bond hyperpolarizabilities $\langle \gamma^{AB} \rangle$:

$$\gamma^{i} = \sum_{AB \neq CC} N_{AB} \langle \gamma^{AB} \rangle, \tag{4}$$

where $N_{\rm AB}$ is the number of bonds of type AB in the molecule. For clarity, we present the average bond hyperpolarizabilities $\langle \gamma^{(AB)} \rangle$ in Table I, and refer the interested reader to Appendix A for the derivation of the exact values used. We briefly note here, however, that we lack experimental values for γ^{PO} corresponding to single and double bonds. We thus use the value for SiO single bonds, calculated from glass, and assume that the CC-to-PO bond ratio will minimize error (also potentially mitigating the error from assuming CH isotropy). Using these values for an isotropic DMPC liquid, we calculate $\chi^{(3)\text{DMPC}} = 3.68 \times$ 10⁻²² m² V⁻², i.e., a correct order of magnitude compared to the values 2.58 and 2.71 experimentally measured for triglycerides and vegetable oil, respectively [21]. While the agreement on absolute average values is only semiquantitative, we show later that this model accurately predicts the P-THG response observed in imaging experiments of multilamellar lipids.

To evaluate γ^p , we must first calculate the tensor elements of γ^{CC} . For this, we use the bond-charge model [22–25] in which the bonding electrons are viewed as point charges centered between two positively charged nuclei. In this model, the symmetry of the CC bond results in nine nonzero

TABLE I. Values used to compute γ^{DMPC} , $\chi^{(3)\text{ML}}$.

Bond type	$\langle \gamma angle^{ m a}$	Other	Value
СН	0.07 ^b	$\langle \gamma^{ ext{CC}} angle$	$0.45^{a,b}$
CO	0.34 ^b	$\gamma_\parallel^{ m CC}$	1.47 ^a
CN	0.27^{c}	$\gamma_\perp^{\rm CC}$	0.29^{a}
PO	2.00	V_{DMPC}	1100 ^d

 $^{^{}a}$ Units of 10^{-50} m⁵ V⁻².

tensor elements of $\gamma^{\rm CC}$, only two of which are unique: γ_{\parallel} and γ_{\perp} . For the CC bond, we calculate (in Appendix A) that $\gamma_{\parallel}=0.69$ and $\gamma_{\perp}=0.14\times 10^{-50}~\text{m}^5~\text{V}^{-2}$. We now calculate γ^p as a sum of the projections of all tensor elements of each CC bond onto the molecular frame:

$$\gamma_{ijkl}^{p} = \sum_{n=1}^{N_{\text{CC}}} \sum_{i'j'k'l'} (\mathbf{i} \cdot \mathbf{i}')(\mathbf{j} \cdot \mathbf{j}')(\mathbf{k} \cdot \mathbf{k}')(\mathbf{l} \cdot \mathbf{l}')\gamma_{i'j'k'l'}^{\text{CC}}, \quad (5)$$

where the first sum is over all CC bonds and the second sum is over the elements of γ^{CC} . Figure 1(a) depicts the polarization dependence of the nonlinear dipole $|e\mathbf{r}^{(3)}(3\omega)|$ calculated with Eq. (1) using either γ^p (blue), γ^i (green), or their sum, γ^{DMPC} (red, with values given in Appendix A). It can be seen from the blue and red meshes that the symmetries of γ^p result in lobed patterns in the induced nonlinear dipole which follow the orientation of the DMPC molecule. We now focus on determining the averaged macroscopic, nonlinear optical susceptibility $\chi^{(3)}$ of DMPC arrays from γ^{DMPC}

B. Calculating the nonlinear susceptibility

As discussed previously, the nonlinear susceptibility of multilamellar lipid arrays $\chi^{(3)\text{ML}}$ is related to the averaged molecular hyperpolarizability $\langle \gamma \rangle$, which depends on the orientation of the lipid molecules in the assembly. We define the molecular z axis as the line from the midpoint of the two terminal aliphatic carbons to the midpoint of the two carbonyl carbons [Fig. 1(a)] and define the laboratory X axis to be parallel to the surface normal of the multilamellar lipid structure [Fig. 1(b)]. Each lipid molecule in the array may freely rotate about both its own $z(\psi)$ and the laboratory X (ϕ) axes. Neglecting birefringence, and assuming that the molecule adopts a Gaussian distribution ρ of angles θ relative to the X axis [Fig. 1(b)], we can calculate the elements of $\chi^{(3)\text{ML}}$ as [17]

$$\chi_{IJKL}^{(3)\text{ML}}(\langle\theta\rangle,\sigma) = \frac{L_{\omega}^{3}L_{3\omega}}{NV} \sum_{ijkl} \gamma_{ijkl}^{\text{DMPC}} \int_{0}^{2\pi} d\psi \int_{0}^{2\pi} d\phi$$
$$\times \int_{0}^{\pi} d\theta \sin\theta \rho(\theta) T_{Ii} T_{Jj} T_{Kk} T_{Ll}, \tag{6}$$

where V is the average volume of DMPC [26] in a bilayer; L_{ω} , $L_{3\omega}$ are local field factors; N is a normalization constant; T_{nm} are elements of a 3D Euler matrix (see Appendix A); and

$$\rho(\theta) = \exp\{-(\theta - \langle \theta \rangle)^2 / 2\sigma^2\}.$$

The symmetry of stacked lipid bilayers (specifically, $C_{\infty V}$) leaves 21 nonzero tensor elements of $\chi^{(3)\text{ML}}$, only three of which are independent: $\chi^{(3)}_{XXXX}$, $\chi^{(3)}_{XXYY}$, and $\chi^{(3)}_{YYYY}$. Importantly, the $\chi^{(3)}$ elements parallel and perpendicular to the lipid surface are linked to the orientation distribution parameters ($\langle \theta \rangle$, σ) through Eq. (6); later, we determine how changes in these tensor elements affect the P-THG

bFrom Ref. [19]. Calculated from $\langle \gamma^{\text{mol}} \rangle$ of DMFA [19]. dIn Å³, bilayer volume of DMPC at 30 °C [26].

response from lipid-vacuum [27] and lipid-water interfaces [Fig. 1(c)].

We calculate $\chi^{(3)}$ elements for liquid-phase ($\langle \theta \rangle = 0^{\circ}$) and gel-phase ($\langle \theta \rangle = 30^{\circ}$) DMPC arrays spanning a range of disorder parameters $\sigma = 5.7^{\circ}$ to $\sigma = 74^{\circ}$ [Fig. 2(a) and 2(b)]. Of course, some of the states for which the calculation is done are not thermodynamically stable, but what we are particularly interested in here is the dependence of the optical modulation on the disorder parameter. In both systems, the tensor elements show a nonlinear relation with σ , which is decreasing for the element parallel to the bilayer normal χ_{XXXX} and the cross term χ_{XXYY} , and increasing for the perpendicular χ_{YYYY} . Note that, with higher σ , the systems approach isotropy; in this case, the $\chi^{(3)}$ tensor elements have the relation $\chi^{(3)}_{XXXX} = \chi^{(3)}_{YYYY} = 3\chi^{(3)}_{XXYY}$. Comparison between the two systems shows that disorder in the gel phase induces an optically isotropic system for lower disorder parameters than the liquid phase; however, both systems approach the same average value of $\langle \chi^{(3)\text{DMPC}} \rangle = 3.68 \times 10^{-22} \text{ m}^2 \text{ V}^{-2}.$

Using the calculated $\chi^{(3)}$, we can visualize the nonlinear polarization $|\mathbf{P}^{(3)}|$ for ordered lipid systems [Fig. 1(b)]. The elongation along the X axis shows that the ordering

information is retained even after averaging over the molecular configurations. While the displayed trace shows the behavior of a liquid-phase lipid system, a similar, slightly more spherical shape would be expected for the gel phase.

C. P-THG as a probe of molecular ordering

In a microscope, THG signal can be induced (i) within birefringent media [8,28] or (ii) at an interface between two materials (isotropic or ordered) with either different values for $\chi^{(3)}$ or refractive indices. the signal due to $\chi^{(3)}$ mismatches between the two materials is proportional to their difference squared [29]:

$$I \propto |\Delta \mathbf{P}^{(3)}|^2 \propto (\chi_1^{(3)} - \chi_2^{(3)})^2,$$
 (7)

where indices 1 and 2 refer to the two materials, and, for simplicity, this expression neglects refractive-index variations and dispersion. If one of these samples is ordered, the polarization of light can be varied to probe different $\chi^{(3)}$ tensor elements, e.g., an X-polarized field produces an X-polarized THG signal $I_X \propto (\Delta \chi_{XXXX}^{(3)})^2$. Thus, a linearly-polarized electric field in the XY plane can be used to probe the three tensor elements of $\chi^{(3)\text{ML}}$ according to

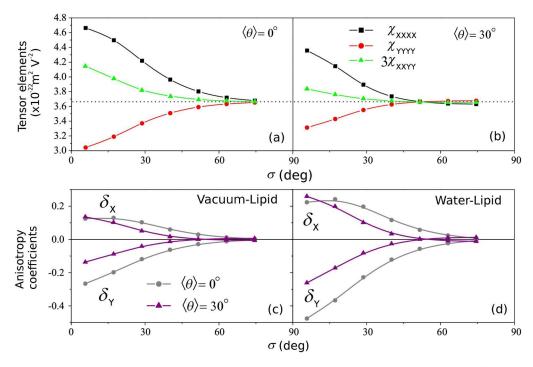


FIG. 2. Calculated nonlinear optical properties of multilamellar lipid structures and interfaces. The $\chi^{(3)\text{ML}}$ tensor elements of (a) liquid-phase ($\langle\theta\rangle=0^{\circ}$) and (b) gel-phase ($\langle\theta\rangle=30^{\circ}$) lipids as a function of disorder σ . Higher ordering results in greater $\chi^{(3)\text{ML}}$ anisotropy for the liquid phase; in the gel phase, optical isotropy is achieved at lower disorder. The elements are also shown to approach the same value of $\langle\chi^{(3)\text{ML}}\rangle$ (dotted line) as the system approaches isotropy. (c),(d) The anisotropy coefficients δ_X , δ_Y characterize the magnitude of the anisotropy-induced P-THG signal oscillation. Generally, for a pair of coefficients, $\delta_X>0$ and $\delta_Y<0$, and their magnitude is larger for liquid-phase interfaces (gray curves) relative to the gel-phase interfaces (purple curves). For an interface between two isotropic media, $\delta_X=\delta_Y=0$; thus, the gel-phase curves [corresponding to the tensor elements in (b)] cross at $\sigma\approx45^{\circ}$, and the liquid-phase curves [corresponding to (a)] cross at $\sigma\approx75^{\circ}$. Comparing the (c) vacuum-lipid and (d) water-lipid interfaces shows that $\chi^{(3)}$ matching of the second, isotropic material can potentially be used to enhance the P-THG contrast.

$$|\Delta \mathbf{P^{(3)}}|^2 \propto \begin{vmatrix} \cos(\Omega)(\Delta \chi_{\parallel}^{(3)}) \\ \sin(\Omega)(\Delta \chi_{\perp}^{(3)}) \\ 0 \end{vmatrix}^2, \tag{8}$$

where Ω is the direction of the field relative to the X axis, and

$$\Delta \chi_{\parallel}^{(3)} = (\Delta \chi_{XXXX}^{(3)}) \cos(\Omega)^2 + 3(\Delta \chi_{XXYY}^{(3)}) \sin(\Omega)^2,$$

$$\Delta \chi_{\perp}^{(3)} = (\Delta \chi_{YYYY}^{(3)}) \sin(\Omega)^2 + 3(\Delta \chi_{XYYY}^{(3)}) \cos(\Omega)^2$$

and \parallel and \perp are defined relative to the laboratory X axis. Because of the relationship between tensor elements discussed above, the differences between the elements of two isotropic materials are related as $\Delta \chi_{XXXX} = \Delta \chi_{YYYY} = 3\Delta \chi_{XXYY}$. Therefore, deviations from this ratio can be used to characterize anisotropy:

$$\delta_X = \frac{\Delta \chi_{XXXX}^{(3)}}{3\Delta \chi_{XXYY}^{(3)}} - 1, \qquad \delta_Y = \frac{\Delta \chi_{YYYY}^{(3)}}{3\Delta \chi_{XXYY}^{(3)}} - 1$$

where δ_X and δ_Y are termed the interface "anisotropy coefficients."

Importantly, δ_X and δ_Y depend on the $\chi^{(3)}$ of both materials. The disorder dependence of δ_X and δ_Y is plotted in Fig. 2(c) and 2(d) for lipid-vacuum and lipid-water interfaces. As can be seen, $\delta_X > 0$ and $\delta_Y < 0$ for most disorder parameters, but they approach zero as the system approaches isotropy. Comparing the two interface types shows that the anisotropy coefficients are larger for better $\chi^{(3)}$ -matched materials; we show later that this effect can greatly increase the sensitivity of P-THG to molecular ordering. The crossing of δ_X and δ_Y for larger disorder parameters reflects the change in the relative magnitude of the tensor components, indicating that disorder in the CC-bond orientation might reverse the P-THG contrast.

Rewriting Eq. (8) using the anisotropy coefficients, the THG signal can be expanded as

$$I \propto (3\Delta \chi_{XXYY}^{(3)})^2 \{ \delta_X^2 \cos(\Omega)^6 + \delta_Y^2 \sin(\Omega)^6 + 2[\delta_X \cos(\Omega)^4 + \delta_Y \sin(\Omega)^4] + 1 \}, \tag{9}$$

where we see the nonlinear, oscillatory dependence of the P-THG intensity on the material anisotropy coefficients. This equation provides a good starting point to describe the extraction of ordering coefficients from the P-THG response of lipid interfaces; however, a more rigorous treatment is needed for an analysis of P-THG microscope images, as we explain in the next section.

D. P-THG microscopy modeling

In practice, THG microscopy usually involves focusing a beam into the sample of interest with a high-numericalaperture (NA) objective lens. The simple field description assumed in the previous section is therefore insufficient. Importantly, the tight focusing of a linearly polarized laser produces a transverse asymmetry of the excitation field. This asymmetry in the focal electric field results in an additional P-THG modulation, expected even for interfaces between two isotropic media [9,30]. In simulations and imaging experiments of interfaces between isotropic lipids and water, we observe that this extra modulation is well fitted with a $\cos(\Omega)^2$ term with a magnitude related to the NA.

To ascertain that the measured response retains ordering information, we have performed numerical calculations [9] of P-THG induced by a linear beam focused at 0.8 NA onto lipid-water and lipid-vacuum interfaces, varying Ω . (For full details, see Appendix B.) In addition, from the P-THG angular profile, we define the modulation $M = (I_{\rm max} - I_{\rm min})/I_{\rm max}$, which, as we will show, allows us to characterize the molecular ordering even in the presence of focus asymmetry.

We have calculated $\chi^{(3)\text{ML}}(\langle \theta \rangle, \sigma)$ and the modulation for both liquid-phase ($\langle \theta \rangle = 0^{\circ}$) and gel-phase ($\langle \theta \rangle = 30^{\circ}$) DMPC arrays as a function of σ . Figures 3(a) and 3(b) depict the general trend predicted by the calculations for liquid-phase and gel-phase lipid arrays with lipid-water and lipid-vacuum interfaces: The optical modulation shows a nonlinear, monotonically decreasing relationship with the disorder parameter for all cases simulated. Comparing the lipid-vacuum interfaces (gray curves) and lipid-water interfaces (blue curves) shows the effect of $\chi^{(3)}$ matching on polarization contrast; as $\Delta \chi^{(3)}_{XXYY}$ decreases in Eq. (9), the anisotropy terms δ_X , δ_Y and the relative modulation increase. Thus, while $\chi^{(3)}$ matching usually reduces contrast in THG imaging [21], it increases contrast in P-THG microscopy of anisotropic structures. We also note that, as the system approaches isotropy, the modulation is nonzero due to the focus asymmetry as described above; however, we can interpret modulation higher than approximately 0.15 as reflecting the molecular arrangement of the lipids within the bilayer.

Also of interest is the full form of the THG intensity profiles as a function of Ω . The values obtained from the simulations are displayed as points in Figs. 3(c) and 3(d), color-coded to match Fig. 2(a). We find that a fitting function of the form of Eq. (10) (where A and B are the fitting parameters) provides an accurate approximation of the angular dependence of the P-THG signal. [See the continuous curves in Figs. 3(c) and 3(d).] Because of the relative magnitude of δ_X , δ_Y , δ_X^2 , δ_Y^2 , we find that a fit,

$$I(\Omega) = A + B(\langle \theta \rangle, \sigma, \text{NA}) \cos(\Omega - \Omega_0)^2$$
 (10)

[see curves in Figs. 2(c) and 2(d)], provides an accurate approximation of the numerical simulation [points in Figs. 2(c) and 2(d). We thus use this equation to fit experimental P-THG profiles from MLVs in the next section.

Because the NA-related modulation $f_{\rm NA}$ is present for any interface, we may assume that it is proportional to the material signal (that is, $f_{\rm NA}/(\Delta\chi^{(3)})^2 = {\rm const}$ for all materials). In addition, we make the assumption that the

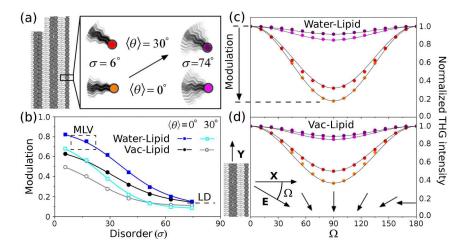


FIG. 3. Calculated P-THG response as a function of lipid order parameters. (a) The components of $\chi^{(3)\text{ML}}$ are determined by the physical distribution of lipid angles relative to the X axis. A low angle and low σ correlate with the highest P-THG modulation. The arrow points from the highest-modulation parameters to lowest. (b) Calculated modulation amplitude as a function of lipid parameters and interface type. Modulation is generally higher at lipid-water (blue curves) than at vacuum-lipid (grey curves) interfaces, showing the increased sensitivity to anisotropy due to the partial $\chi^{(3)}$ matching. The modulation is also consistently larger for the liquid-phase lipids (closed symbols) relative to the gel-phase (open symbols) lipids for a particular interface type. Experimental values for the modulation in the MLV and lipid droplet (LD) are indicated with dashed lines. (c),(d) The calculated angular profiles for four multilamellar lipids, color-coded to match (a). The P-THG signal is lowest when the excitation field is parallel to the bilayers. The fitting curves are of the form $I = A + B \cos(\Omega)^2$.

material and NA-related anisotropies are independent of one another. (See Appendix C for further discussion.) First, this allows us to rewrite Eq. (9) from the last section as

$$\begin{split} I & \propto (3\Delta\chi_{XXYY}^{(3)})^2 [\delta_X^2 \cos(\Omega)^6 + \delta_Y^2 \sin(\Omega)^6 \\ & + 2(\delta_X \cos(\Omega)^4 + \delta_Y \sin(\Omega)^4) + 1] + f_{\text{NA}} \cos(\Omega)^2. \end{split} \tag{11}$$

Second, we may separate the material-anisotropy and focus-asymmetry effects in the constant $B(\langle \theta \rangle, \sigma, \text{NA})$ of our fitting equation as follows: $B(\langle \theta \rangle, \sigma, \text{NA}) = B(\langle \theta \rangle, \sigma) + f_{\text{NA}}$. Using the definition of the modulation with both the fit equation (10) and Eq. (11) above,

$$M = \frac{B(\langle \theta \rangle, \sigma) + f_{\text{NA}}}{A + B(\langle \theta \rangle, \sigma) + f_{\text{NA}}}$$
(12)

$$=\frac{(\delta_X+1)^2-(\delta_Y+1)^2+f_{\rm NA}}{(\delta_X+1)^2+f_{\rm NA}},$$
 (13)

we can derive the relationship between δ_X , δ_Y and A, B as

$$A \propto [3\Delta\chi(3)_{XXYY}]^2 (\delta_Y + 1)^2,$$

 $B \propto [3\Delta\chi(3)_{XXYY}]^2 [(\delta_X + 1)^2 - (\delta_Y + 1)^2] + f_{NA},$

and the factor f_{NA} can be determined from the modulation at the interface of two isotropic materials $(\delta_X, \delta_Y = 0)$:

$$\frac{f_{\rm NA}}{(\Delta \chi^{(3)})^2} = \frac{M}{1 - M}.$$
 (14)

Importantly, Eq. (10) can be used to fit P-THG microscopy profiles from lipid interfaces, and Eqs. (11)–(14) can be used to quantify molecular ordering.

III. EXPERIMENTALLY MEASURING ORDERED LIPIDS

A. Microscopy

Multiphoton images of MLVs and skin are made with a custom-built, scanning, upright microscope (Fig. 4) utilizing a 20x 0.8 NA water-immersion objective (Olympus). Microscope resolution for THG imaging is estimated as the full width at half maximum of the THG profile from glasswater interfaces; we have determined the transverse (XY) and axial (Z) resolutions to be 0.5 μ m and 4.3 μ m, respectively. For MLVs, 8 images taken at a pixel rate of 400 kHz (pixel dwell time 2.5 μ s) are averaged for analysis. For the skin-biopsy samples, 4 images with 200 kHz pixel rate (pixel dwell time of 5 μ s) are averaged, taken approximately 30 μ m from the skin surface. THG imaging is performed using 1180 nm excitation pulses provided by a KTP-based OPO (APE, Germany) externally compressed to about 100 fs using dispersive prisms. CARS images are generated using longer pulses (150 fs pump, 400 fs Stokes) from a second Ti:S/OPO laser chain (Chameleon-OPO, Coherent, Inc.) with frequency difference tuned to the CH₂ stretch frequency (2840 cm⁻¹). For P-THG and P-CARS experiments, a polarizer and achromatic near-infrared half wave plate are placed just before the objective for polarization control. Polarization profiles

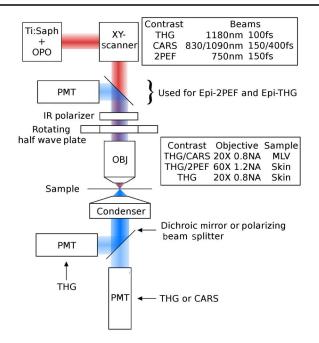


FIG. 4. Setup used for the various imaging experiments. OBJ = Objective, PMT = photomultiplier tube. The excitation path is represented by the red beam; blue beams indicate both the forward and the epi (backward) emission pathways. THG and CARS images are usually detected in the forward direction, while the 2PEF images are epidetected using a dichroic mirror. The general form of this setup is typical for any nonlinear optical microscope, with the inclusion of a polarizer and a half wave plate to guarantee accurate control of the polarization state at the focus.

of MLVs and skin samples are generated from 31 images covering a range of 0°-180°.

B. Ordering in multilamellar lipid vesicles

THG and CH₂-resonant CARS images of MLVs are shown in Fig. 5(a). As can be seen immediately, the two techniques provide complementary information: Not only are the polarization dependencies perpendicular to one another, but the THG contrast is highest at the water-MLV interfaces and weaker in the bulk, whereas the CARS signal is weaker on the surface and strongest in the bulk. This polarization complementarity may explain discrepancies between P-CARS imaging experiments of MLVs [12,13], which utilized the ratio of resonant-tononresonant CARS to quantify molecular order. As we have demonstrated here, γ^{DMPC} is oriented parallel to the hydrocarbon chains (and thus perpendicular to $\gamma^{\text{vib-CH}_2}$). We point out that nonresonant CARS and THG are both sensitive to the electronic nonlinear optical response; normalization to either of these signals would add modulation artefacts to any analysis. Conversely, we can predict the polarization dependence of THG from lipid interfaces. In addition, as we show later in skin samples, THG is a background-free and high-contrast imaging modality for interface detection, easily combined with SHG and/or 2PEF microscopy [31] (which is the gold standard in tissue fluorescence microscopy).

The MLVs generate THG by the two contrast mechanisms discussed earlier: (i) Away from the edge, phase matching is possible due to MLV birefringence, and signal is observed locally when the excitation field is oblique to each symmetry axis of the liquid crystal; (ii) At the MLV-buffer interface, the differences in $\chi^{(3)}$ and refractive indices both contribute to signal generation. Polarization-resolved-detection THG images [Fig. 5(a) and movie S1 in Ref. [32]) further show that the interface signal retains the same polarization as the excitation, while birefringence-related emission from the bulk is perpendicularly polarized, in agreement with Ref. [8]. Here, we focus on contrast mechanism (ii), which is most often met in biological imaging, and analyze the P-THG response at the MLV-water interface.

P-THG intensity profiles from the water-MLV interface are plotted in Fig. 5(b), along with the intensity profile of a plant oil droplet, in which lipids are randomly oriented. The difference in modulation between signals from the oil droplet (0.13 ± 0.02) and the MLV (0.73 ± 0.075) confirms that the polarization response in THG is sensitive to lipid ordering. The three MLV profiles compare different sampling sizes in the same region of the upper MLV interface. The experimental fits show relatively little change with an increase in sampling. Indeed, for the experimental conditions used in this study, we predict only a small gain in precision when averaging over more pixels. Our analysis (see Appendix D for a full discussion) indicates that we extract A, B, and Ω_0 with good precision even down to the limit of the excitation volume, with a detection of about 5000 photons per P-THG pixel (distributed over the 180° profile). Moreover, the agreement between the predicted modulation and the experimentally observed modulation validates our theoretical framework for constructing the $\chi^{(3)}$ of the lipid arrays. The nonuniform modulation measured along the surface of the MLV probably reflects ordering heterogeneity due to imperfect lipid packing. This interpretation is corroborated by our detecting heterogeneity within the MLV in the THG images.

By fitting the profiles with Eq. (10), we generate corresponding average interface angle Ω_0 and modulation (M) images on a per-pixel basis [Figs. 5(c) and 5(d)]. Figure 5(c) is a hue-saturation-value rendering of the MLV in Fig. 5(a) where the hue is the extracted Ω_0 , saturation is 1, and the value or brightness depends on the relative error of the fit, where we have limited the processing to a sample-dependent intensity threshold. As can be seen, the fit accurately determines the angle of the bilayer normal which points radially outward. This sensitivity can be used to detect lipid orientation with sub- μ m spatial resolution in complex samples, such as the lipid aggregate shown in Fig. 5(e) and movie S2 in Ref. [32].

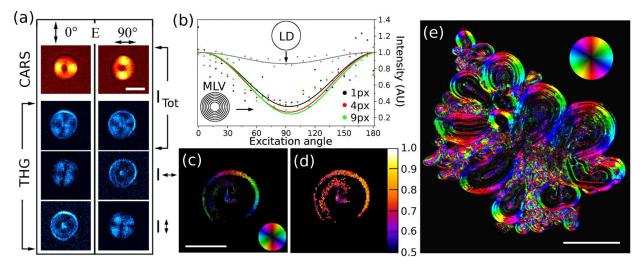


FIG. 5. P-NLOM imaging of ordered and amorphous lipid structures. (a) THG and CARS images of MLVs generated with two orthogonal polarizations (scale bar 15 μ m). The maximum CARS signal is obtained with excitation fields polarized parallel to the CH₂ moieties, i.e., to the MLV surface. Two types of THG signals are detected. The interface THG signal (analyzed in this study) is maximized for an excitation field polarized parallel to the CC bonds (i.e., to the surface normal) and retains the excitation polarization. The bulk THG signal is due to MLV birefringence and is polarized perpendicular to the excitation. (See also movie S1 in Ref. [32].) (b) Comparison between the polarization dependence of THG from the surface of a lipid droplet (isotropic lipids) and a MLV (with approximately 10^3 bilayers), clearly showing the sensitivity of P-THG to molecular ordering. The MLV data analyses indicate that pixel averaging is not necessary to retrieve accurate estimates of the interface angle and modulation amplitude. (c)–(e) Extraction of order parameters. On a per-pixel basis, the fits can be used to construct maps of (c) the lipids orientation and (d) modulation amplitude based on the interface THG signal (scale bar 15μ m). The same fitting procedure can accurately extract physical parameters in more complex systems, such as the large lipid aggregate in (e) (scale bar 15μ m; see also movie S2 in Ref. [32]).

C. Quantitative comparison with XRS

To compare P-THG to other methods for quantifying order, we correlate the MLV modulation amplitude, depicted in Fig. 5(d), to the disorder parameter σ . The modulation of the MLV signal in dilute buffer corresponds to $\sigma \approx 20^{\circ} \pm 8^{\circ}$ from the ordered lipid-water interface profile [Fig. 3(b)]. To relate this to x-ray scattering measurements, using our data, we calculate $\langle P_2 \rangle = 0.77$ [33,34] assuming $\langle \theta \rangle = 0$ (see Appendix E), and compare the result to $\langle P_2 \rangle \approx 0.4$ determined by Pan *et al.* [35] for DMPC (which correlates with $\sigma \approx 38^{\circ}$). This discrepancy of $\langle P_2 \rangle$ is likely due to the overestimation of $\langle \chi^{(3) \text{DMPC}} \rangle =$ $3.68 \times 10^{-22} \text{ m}^2 \text{ V}^{-2}$ calculated using the bond-additivity model. As noted earlier, the approximately 2.6×10^{-22} value for $\langle \chi^{(3)\text{Lipid}} \rangle$ measured by our group in a previous study [21] more closely matches that of water $(1.83 \times$ 10^{-22}) which, as we have shown, results in a higher modulation. If we uniformly scale the tensor elements of $\chi^{(3)\text{ML}}$ ($\langle \theta \rangle = 0$, $\sigma = 38^{\circ}$) by a factor of 0.63, we can calculate the experimentally observed modulation of 0.73 (Appendix E). This calculation results in $\langle \chi^{(3)\text{DMPC}} \rangle =$ $2.3 \times 10^{-22} \text{ m}^2 \text{ V}^{-2}$, in very good agreement with the expected value.

D. THG modulation in human skin stratum corneum

Ordered lipid assemblies play a key role in the hygroscopic nature of the skin SC [36], and their disruption is

associated with different skin diseases [37]. The SC, depicted in Fig. 6(a), can be viewed as a "brick-and-mortar" assembly [38] where dried, dead corneocytes form large, flat disks surrounded by stacked lipid bilayers (approximately 10 bilayers per intercorneocyte stack, with a total approximate thickness of 50 nm [39]) consisting of cholesterol, free fatty acids (FFAs), and ceramides [40]. Figures 6(b)–6(e) show the overlay of a THG and a two-photon excited fluorescence (2PEF) image of the skin stratum corneum along a fold, with THG signals anticorrelated relative to the endogenous fluorescence observed from the corneocytes. These maps explicitly show the physical separation of the signals and localize the THG signal to the ordered-lipid–disordered-corneocyte interface.

Figures 6(f) and 6(g) show P-THG images of the skin, taken with two orthogonal polarizations of the excitation field, demonstrating the structure-dependent variation of the signal. From a series of P-THG images, we construct the directional hue-saturation-value map of the lipid orientation of the intercellular skin lipids, shown in Fig. 6(h). In Fig. 6(i), it is interesting to note that the layers closer to the surface have the lowest modulation, approximately 0.6 compared to 0.75 for the layers further from the surface. This observation may reflect variations in lipid ordering for different layers of the SC. Importantly, as is evident in movie S3 in Ref. [32] (recorded at a depth of $35 \mu m$), P-THG still detects molecular order with high specificity even within complex tissue environments. Indeed, strong modulation is observed only from the stacked lipids in the

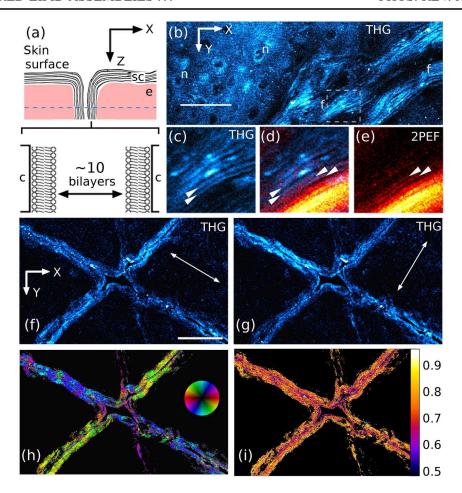


FIG. 6. Nonlinear optical imaging of samples from human skin biopsies. (a) Within the skin stratum corneum (labeled "SC"), stacked bilayers exist between the dead corneocytes (labeled "c"). Vertically oriented folds extending tens of microns deep into the epidermis (labeled "e") provide an optimal geometry for P-THG imaging (dashed blue line). (b) THG images of the skin highlight cell nuclei (labeled "n") as well as the folds ("f") (scale bar 50 μ m). (c)–(e) Subregion of the rectangular area indicated in (b). In human skin biopsies, endogenous 2PEF from the corneocytes alternating with THG signals (see white arrowheads) localizes the THG response to the intercellular lipid interfaces. (f),(g) THG images of a human skin biopsy approximately 25 μ m from the skin surface generated using two different polarizations, indicated by the straight doubleheaded arrows (scale bar 50 μ m). Note how the folds that are oriented perpendicular to the excitation polarization appear brighter than the ones with parallel orientations. As with the MLV, the P-THG signal can be fitted to extract the stacked lipids orientation (h) and modulation (i), to gain insight into the lipid ordering within the interfaces. Even within the tissue, a strong modulation is observed exclusively from ordered phases and not from other structures. See also the movie S3 in Ref. [32].

folds, whereas disordered structures produce only small, geometry-related modulation.

While we observe excellent qualitative agreement between the stratum corneum and the MLVs, quantitative correlations between modulation and lipid disorder require further characterization. The density, length, and angular distribution of CC bonds within SC bilayers is different than in the MLVs. In addition, the geometry of the lipids in the skin is better approximated by a thin slab within the focal volume, requiring a more accurate theoretical treatment. Still, because the THG polarization dependence in the SC is strong and specific, and because THG microscopy is background free, this method should be a sensitive probe to disruptions of the lipid layers integrity (e.g., from solvents or potentially from lipid-related diseases).

We finally note that scattering may alter polarization-based optical measurements in environments that exhibit large-scale anisotropy such as tendon [6]. However, such artifacts should generally not be present in standard tissues where scattering is not expected to cause major distortion in the focal-field distribution [41]. Ratiometric P-THG should therefore be a valid method for probing lipid order in various tissue contexts.

IV. CONCLUSION

We have identified a novel mechanism of nonlinear optical contrast sensitive to molecular ordering in lipid assemblies. We have presented a systematic, multiscale method for calculating the electronic nonlinear susceptibility of lipid arrays. Furthermore, we have derived a

simple expression relating $\chi^{(3)}$ tensor elements to the P-THG response, physically relevant for interfaces between isotropic materials and any multilamellar lipid structures (or other arrays with $C_{\infty V}$ symmetry).

The general agreement between numerical calculations and P-THG imaging experiments of MLVs validates the use of P-THG as a method to probe lipid ordering and facilitates the extraction of molecular distribution parameters with high precision even at the diffraction limit. P-THG imaging of human skin biopsy samples has led to the discovery of a remarkably strong probe of biological lipid ordering, and it is easily coupled to other multiphoton imaging modalities such as SHG and 2PEF. Importantly, P-THG is an experimentally simple technique requiring a single excitation beam, and skin is optically accessible [42] and amenable to *in-vivo* microscopy, potentially leading to biomedical applications.

ACKNOWLEDGMENTS

We thank Matthias Garten and Patricia Bassereau of the Université Pierre et Marie Curie for help with MLV synthesis, and Jean-Louis Martin, François Hache, Ana-Maria Pena, and Willy Supatto for helpful discussions. This work was partially supported by Agence Nationale de la Recherche under Contract Nos. ANR-07-RIB-010, ANR-09-PIRI-0013, and ANR-10-INBS-04.

APPENDIX A: DETERMINING THE PARAMETERS USED IN THE MULTISCALE MODEL

It is difficult to find comprehensive multiscale data and calculations in the literature, so we present a general guideline for determining the nonlinear optical susceptibility of dynamic systems. The calculation of $\chi^{(3)\text{ML}}$ is broken into parts, each pertaining to a progressively larger scale: First, calculation and determination of the bond hyperpolarizabilities γ^{AB} on the Ångstrom scale; next, calculation of the molecular hyperpolarizability γ^{DMPC} from the molecular structure on the nm scale; and, finally, averaging over molecular orientations to calculate the nonlinear susceptibility of multilamellar lipid structures $\chi^{(3)\text{ML}}$ on the 0.1–1- μ m scale. From experiment, we already have $\chi^{(3)\text{vac}} = 0$ and $\chi^{(3)\text{H}_2\text{O}} = 1.83 \times 10^{-22} \text{ V}^2 \text{ m}^{-2}$ [21].

1. The CH, CN, CO, and PO hyperpolarizabilities

We start from the work of Kajzar and Messier [19] for the experimental values of γ^{AB} that we use in this study. In their work, they measured the $\chi^{(3)}$ of various transparent liquids relative to the fused silica $\chi^{(3)glass}$, from which they calculated $\langle \gamma^{mol} \rangle$ for each liquid. By systematically measuring similar structures, they were able to estimate γ^{AB} for several bond types of interest to our study of DMPC; specifically, they presented values for γ^{CC} , γ^{CH} for single bonds and γ^{CO} for both single and double bonds.

At this point, we lack values for γ^{CN} and γ^{PO} single and double bonds. We obtain an estimate for γ^{CN} from Kajzar and Messier's experimentally determined molecular hyperpolarizability of N,N-dimethylformamide γ^{DMFA} , composed of seven CH bonds, one CO double bond, and three CN bonds. Because we could not find a tabulated reference value for γ^{PO} , we use the value for γ^{SiO} , calculated as half the molecular hyperpolarizability of γ^{SiO_2} [19]. While not ideal, we believe that this approximation is sufficient due to the ratio of PO to non-PO bonds in the DMPC molecule and the similarity between the electronic structures of Si and P.

While these numbers are a valuable starting point, more recent, similar THG experiments from our group have used a more accurate and significantly different value for $\chi^{(3)\text{glass}}$ [43]. Because all of the γ^{AB} by Kajzar and Messier were calculated relative to $\chi^{(3)\text{glass}}$, we need to update the values for this study. Fortunately, since both groups measured the same ratio $\chi^{(3)\text{H}_2\text{O}}/\chi^{(3)\text{glass}}$, we may simply multiply each value of γ^{AB} by the ratio of the measured $\chi^{(3)\text{H}_2\text{O}}$ to calculate the updated values presented in the main text.

2. CC hyperpolarizability

We make use of the bond-charge model to determine the ratio $\gamma_{\parallel}/\gamma_{\perp}$ of the elements of the CC-bond second hyperpolarizability. Originally, Van Vechten [22] derived simplified relations between the linear susceptibility $\chi^{(1)}$ and the band gap of a material E_g . The energy E_g has ionic C and covalent E_h components, each of which is dependent on the position of the electrons relative to the nuclei and was measured for many semiconductors. Based on this work, Levine [23] later noted that an induced polarization changed the electron positions $(\Delta \mathbf{r})$ and thus the bond energies. By expanding the expression for the electric-field-induced polarization to first order in $\Delta \mathbf{r}$, Levine was able to calculate the first hyperpolarizability β from atomic properties and crystal structure.

Following a similar path, Chemla *et al.* [25] derived expressions for the second-order expansion of the energy and for calculating the two independent tensor elements of γ^{AB} . Taking the z' axis as the bond axis, the nine nonzero elements of γ^{AB} are related to these two values according to

$$\begin{aligned} \gamma_{\parallel} &= \gamma_{z'z'z'z'}, \\ \gamma_{\perp} &= \gamma_{i'i'i'i'} = 3\gamma_{i'i'j'j'} = 3\gamma_{i'j'i'j'} = 3\gamma_{i'j'j'i'}, \\ i', j' &= x', y'; \quad i' \neq j', \end{aligned}$$

which shows that fields parallel (perpendicular) to the bond axis induce only parallel (perpendicular) dipoles $e\mathbf{r}^{(3)}(3\omega)$, respectively. While the bond-charge model itself provides an order-of-magnitude estimate of bond hyperpolarizabilities, the ratio of γ^i to γ^p determines the observed polarization dependence of the THG signal. Therefore, we limit the use of the bond-charge model to

calculating the ratio $\gamma_{\parallel}/\gamma_{\perp}$ and later couple this ratio to the experimentally measured $\langle \gamma^{CC} \rangle$.

For brevity, we present the calculation of $\gamma_{\parallel}/\gamma_{\perp}$ specific to the CC bond. For bonds in a diamond-type crystal (i.e., no ionic components, C=0),

$$\frac{\gamma_{\parallel}}{\gamma_{\perp}} = \frac{\frac{3}{2}(-0.25g_{1\parallel}^2 - 2h_{2\parallel}E_h)}{\frac{3}{4}(-2h_{2\perp}E_h)},\tag{A1}$$

where we explicitly use the notation set out by Van Vechten [22] for the homopolar energy E_h and the notation by Chemla *et al.* [25] for the factors g_1 and h_2 . This model was developed using the Gaussian system of units; here, we perform the calculation in this system and convert to *le Système international d'unités* (SI) at the end of the calculation. For a CC bond:

$$g_{1\parallel} = \frac{-be^2}{q} \left(\frac{2Z_c}{r_c^2}\right) \exp(-k_s r_c),$$
 (A2)

$$h_{2\parallel} = \frac{-40}{q^2} \left(\frac{E_h}{r_C^2}\right),$$
 (A3)

$$h_{2\perp} = \frac{-14.3}{q^2} \left(\frac{E_h}{r_C^2}\right),$$
 (A4)

$$E_h = 39.74(2r_C)^{-s}, (A5)$$

$$k_s = \sqrt{\frac{4k_f}{\pi a_0}}, \qquad k_f^3 = (3\pi^2)N, \qquad N = Z_C \frac{m}{\rho N_A},$$

where a_0 is the Bohr radius; $e = 4.803 \times 10^{-10}$ esu is the electron charge; r_C and Z_C are the covalent radius and number of valence electrons on carbon, respectively; the exponential constant s = 2.48 has been determined experimentally [22]; b is related to the average coordination number of the two atoms (and is generally between 1 and 2); k_s (k_f) is the Thomas-Fermi screening constant (wave number), respectively; N is the number of bonding electrons per diatomic volume for a compound with molar mass m and density ρ ; and N_A is Avogadro's number. Using the values presented in Table II, we calculate the ratio $\gamma_{\parallel}/\gamma_{\perp} = 5.08$.

The relationship between the average, isotropic hyperpolarizability $\langle \gamma \rangle$ of a collection of randomly oriented molecules and the molecular hyperpolarizability γ tensor elements is

TABLE II. Summary of the bond-charge calculation.

Input values		Calculated values		
\overline{b}	1.5	E_h	$2.182 \times 10^{-11} \text{ esu}$	
Z_C	4	k_s	$2.391 \times 10^{8} \text{ cm}^{-1}$	
r_C	$0.77 \times 10^{-8} \text{ cm}$	$\gamma_{\parallel}/\gamma_{\perp}$	5.08	
ρ	2.26 g/cm^3	γ"	$1.47 \times 10^{-50} \text{ m}^5 \text{ V}^{-2}$	
m	12.01 g/mol	$\gamma_{\perp}^{"}$	$0.29 \times 10^{-50} \text{ m}^5 \text{ V}^{-2}$	

$$\langle \gamma \rangle = \frac{1}{5} (\gamma_{xxxx} + \gamma_{yyyy} + \gamma_{zzzz}) + \frac{2}{5} (\gamma_{xxyy} + \gamma_{xxzz} + \gamma_{yyzz}).$$

We may apply this relation to a theoretical liquid made up of noninteracting single CC bonds to obtain

$$\gamma^{AB} = \frac{1}{5} (\gamma_{\parallel} + \frac{8}{3} \gamma_{\perp}), \tag{A6}$$

where we use $\gamma_{\perp} = \gamma_{xxxx} = \gamma_{yyyy} = 3\gamma_{xxyy}$, and $\gamma_{iizz} = 0$. With $\gamma_{\parallel}/\gamma_{\perp} = 5.08$ and with $\langle \gamma^{CC} \rangle = 0.21 \times 10^{-50} \text{ m}^5 \text{ V}^{-2}$ [19], we obtain $\gamma_{\parallel} = 0.69$, and $\gamma_{\perp} = 0.14 \times 10^{-50} \text{ m}^5 \text{ V}^{-2}$.

3. DMPC hyperpolarizability

The determination of the tensor elements of the molecular hyperpolarizability is performed according to Eq. (5) in the main text. The tensor elements of $\gamma^{\rm DMPC}$ calculated in this study are summarized in Table III. Since we assume only Kleinman symmetry, there are 81 nonzero elements, 15 of which are independent. The independent tensor elements are related by the number of times a particular Cartesian axis appears in the subscript. Thus, (2x)yz refers to all elements such as γ_{xxyz} , γ_{xzyx} , etc., which are all equal. The only unique value of note is γ_{zzzz} , since an arbitrary rotation about the molecular z axis (defined in the main text) will change the elements with x and y indices, while reproducing the same macroscopic $\chi^{(3)\rm ML}$.

4. Lipid nonlinear susceptibility

The tensor elements of $\chi^{(3)\text{ML}}$ are determined by averaging γ^{DMPC} over all assumed molecular orientations. This calculation is performed according to Eq. (6) in the main text, where the factors L_{ω} , $L_{3\omega}$, and N are [17]

$$L_{\omega,3\omega} = \frac{n_{\omega,3\omega}^2 + 2}{3},$$

$$N = \int_0^{2\pi} d\psi \int_0^{2\pi} d\phi \int_0^{\pi} \sin\theta d\theta \rho(\theta,\sigma),$$

and the factors T_{nm} are obtained according to

TABLE III. Elements of γ^{DMPC} in units of 10^{-50} m⁵ V⁻².

General index type	Values			
4 <i>a</i>	10.43	уууу 10.10	zzzz 15.59	
$\overline{(3a)b}$	(3x)y -0.29	(3 <i>y</i>) <i>x</i> 0.01	(3x)z 0.17	
$\overline{(3a)b}$	$ \begin{array}{c c} (3z)x \\ -0.35 \end{array} $	(3y)z -0.32	(3z)y 0.46	
(2a)(2b)	(2x)(2y) 3.14	(2x)(2z) 2.73	(2y)(2z) 6.53	
$\overline{(2a)bc}$	(2x)yz -0.12	(2y)xz - 0.21	(2 <i>z</i>) <i>xy</i> 0.92	

$$T_{nm} = \begin{bmatrix} \cos(\theta)\cos(\phi)\cos(\psi) - \sin(\phi)\sin(\psi) & -\cos(\theta)\cos(\phi)\sin(\psi) - \sin(\phi)\sin(\psi) & \sin\theta\cos\phi \\ \cos(\theta)\sin(\phi)\cos(\psi) + \cos(\phi)\sin(\psi) & -\cos(\theta)\sin(\phi)\sin(\psi) + \cos(\phi)\cos(\psi) & \sin\theta\sin\phi \\ -\sin\theta\cos\psi & \sin\theta\sin\psi & \cos\theta \end{bmatrix}$$

where m is in the reference frame of the molecule and n is in the laboratory frame. We ignore the effects of both birefringence and dispersion in this study and use $n_X = n_Y = n_Z$ and $n_{\omega,3\omega} = 1.43$.

APPENDIX B: DETAILS OF P-THG MICROSCOPY SIMULATION

Once the $\chi^{(3)}$ tensor elements for all materials have been calculated, the P-THG microscopy simulation involves (1) calculating the 3D electric field near the focus, (2) simulating the induced nonlinear polarization $\mathbf{P}^{(3)}$ within the focal region, and (3) propagating it to the far field and coherently summing all the elementary contributions in the detection plane, taking into account their relative phase.

1. Field at the focus

We use the fairly straightforward approach laid out by Leutenegger *et al.* [44] for fast calculation of the focal-field distribution. Briefly, we simulate a linearly polarized Gaussian beam of light at 1180 nm incident on a 0.8-NA water-immersion objective with a filling factor 10/6.5. The focal volume is sampled at a size spanning $\pm 1.17~\mu m$ in the (lateral) X and Y directions and $\pm 3.94~\mu m$ in the (axial, parallel to beam propagation) Z direction, discretized into a $201 \times 201 \times 200~\text{grid}$. In our simulation, we assume a refractive index of 1.33 for the entire focal volume. Thus, we ignore the refractive index and birefringence effects related to THG signal generation and investigate solely the $\Delta \chi^{(3)}$ effects upon signal generation, as stated in the main text.

2. Sample geometry

For the geometry of the sample in focus, we create a grid the same size as the sampled focal volume and assign the localized $\chi^{(3)}$ for each 3D grid point. The geometry we choose emulates an idealized lipid-water or lipid-vacuum interface between two semi-infinite slabs. The interface is located at the X = 0 plane where all grid points with X < 0described by $\chi^{(3)\text{ML}}$ and $X \ge 0$ by $\chi^{(3)\text{H}_2\text{O}}$ or $\chi^{(3)\text{vac}}$. To simulate different field-interface angles (Ω) , we can recalculate either the sample geometry and $\chi^{(3)\text{ML}}$ or the focal-field distribution for each angle. Because of the simple geometry assumed, we find that recalculating the sample geometry is faster than recalculating the focal volume, so we choose the former. The nonlinear polarization $\mathbf{P}^{(3)}$ is then calculated at each grid point according to Eq. (2) in the main text; here, because we assume Kleinman-symmetry conditions are fulfilled, we use the d-matrix formalism as in Ref. [25].

3. Far-field THG signal

Plane waves oscillating at the TH wavelength (393.3 nm) are propagated to a far-field plane 10 cm from the focus and 25×25 cm (41 \times 41 grid points) in size using Green's functions [9,30] with a refractive index of 1.36. The intensity over the whole far field is integrated to obtain the THG signal. The THG signal is calculated with steps of size $\Delta\Omega=11.25^{\circ}$ ($\pi/16$) to determine the analytical form of the angular dependence shown in Figs. 2(c) and 2(d) of the main text.

APPENDIX C: FOCUSING RELATED P-THG MODULATION

In the main text, we assume that the polarization dependence of the focus transverse asymmetry (described by the factor $f_{\rm NA}$) can be separated from the material effects. Here, we justify that this assumption is reasonable for the DMPC arrays simulated here. To do so, we compare the modulation determined from the simulations

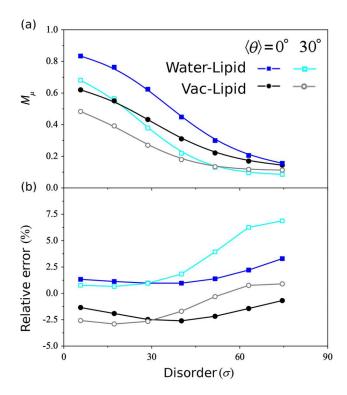


FIG. 7. Calculation of the signal modulation using the fast, approximate method. (a) Modulation as a function of the disorder parameter, similar to the predicted trend from the full numerical simulations. (b) Relative error between the two predictions, showing that the fast calculation is consistently within 10% (although generally even lower) of the numerical simulations.

presented in Fig. 3(b) (which we assume are the accurate or "true" modulations) with the modulation calculated according to Eq. (11) and using $f_{\rm NA}/(3\Delta\chi(3)_{XXYY})^2 = 0.15$. Figure 7(a) shows the predicted microscope modulation without the use of a full simulation as a function of disorder σ for liquid and gel phase, lipid-vacuum and lipid-water interface types. The relative difference $2(M_{\rm Ap}-M_{\rm Sim})/(M_{\rm Ap}+M_{\rm Sim})$ is plotted in Fig. 7(b). As is readily apparent, the anisotropy of the lipids prevents this approximation from perfectly predicting the P-THG modulation; however, the fast, approximate calculation is still within 10% of the full simulation for all values, and within 5% for the majority.

In addition, we determine an additive correction factor $F_{\rm NA}$ to the approximated modulation of Eq. (10) that may be used to calculate the expected modulation in the microscope:

$$M_{\mu} = M + F_{\text{NA}},\tag{C1}$$

$$F_{\text{NA}} = \frac{(\delta_Y + 1)^2 f_{\text{NA}} / (\Delta \chi^{(3)})^2}{(\delta_X + 1)^2 [(\delta_X + 1)^2 + f_{\text{NA}} / (\Delta \chi^{(3)})^2]}.$$
 (C2)

Importantly, this calculation allows us to predict the expected modulation in the microscope without performing the full P-THG simulation.

APPENDIX D: FITTING ERROR AS A FUNCTION OF SIGNAL STRENGTH

Here, we discuss the precision with which we can determine optical parameters from the P-THG measurements, using an approach to error analysis similar to the one found in Ref. [45]. The fitting function defined in the main text [Eq. (10)] was used because of the simple relationship between the nonlinear susceptibility elements and the fit parameters A, B, and Ω_0 . Here, we use a different fitting function f for the P-THG signal, which can be related to the fit parameters discussed in the main text but which allows for a simpler derivation of measurement precision:

$$f = I(\theta) = A\{1 + M[\cos 2(\theta - \theta_0)]\},$$
 (D1)

where $A = \langle I \rangle$ is the signal average amplitude, -1 < M < 1 is the modulation depth of the signal as a function of polarization, and θ_0 is identical to Ω_0 defined in Eq. (10). The function is measured at N different points $\{\theta_i\}_{i=1...N}$, and the measurement yields the values $\{I_i\}_{i=1...N}$. First, we note that the residual error for a least-square fit if there is zero noise on the signal and an error δA , δM , $\delta \theta_0$ on the parameters can be written as

$$\epsilon \approx \sum_{i=1}^{N} [\delta A + 2AM\delta\theta_0 \sin 2(\theta_i - \theta_0) + (A\delta M + M\delta A)\cos 2(\theta_i - \theta_0)]^2, \quad (D2)$$

assuming that $\delta\theta_0 \ll \pi$, which is reasonable if we investigate the measurement error, and considering only the first order in infinitely small quantities δA , δM , $\delta\theta_0$. If we also assume that the N points $\{\theta_i\}_{i=1...N}$ are evenly spaced between 0 and π , the residual error reduces to

$$\epsilon = N(\delta A)^2 + 2N(AM)^2(\delta \theta_0)^2 + \frac{N}{2}(M\delta A + A\delta M)^2.$$
(D3)

Second, we now evaluate the residual error ϵ' purely due to shot noise in the signal. Here, we assume that the fitting parameters are perfectly known ($\delta A = \delta B = \delta \theta_0 = 0$), so that the difference between the measured values $\{I_i\}_{i=1...N}$ and the fit values $\{I(\theta_i)\}_{i=1...N}$ is due only to the shot noise. Because this noise is on average equal to the square root of the intensity, the statistical mean of the total error can be expressed as

$$\langle \epsilon' \rangle = \sum_{i=1}^{N} (\sqrt{I_i})^2 = N \langle I \rangle,$$
 (D4)

where $\langle I \rangle$ is the average number of photons over the *N* measurements.

Last, the fitting parameter precision can finally be estimated by assuming that the residual error due to the fitting parameters is comparable to the residual error due to the shot noise, that is, $\epsilon = \epsilon'$. For instance, for the statistical error in the fitting parameter A, we solve the equation [45]

$$\sum_{1}^{N} \left[\left(\frac{\partial f}{\partial A} + \frac{\partial f}{\partial M} \frac{\partial M_{m}}{\partial A} + \frac{\partial f}{\partial \theta_{0}} \frac{\partial \theta_{0m}}{\partial A} \right) dA \right]^{2} = N \langle I \rangle. \quad (D5)$$

The quantities M_m , θ_{0m} are the values that minimize ϵ in Eq. (D3); specifically, $\partial M_m/\partial A$, $\partial \theta_{0m}/\partial A$ are determined from the partial derivative of ϵ with respect to δM and $\delta \theta_0$, respectively. Here, we assume that there is no change in A or M with respect to changes in θ_0 (and vice versa). Following this scheme, we obtain the following values for the statistical error in the fitting parameters:

$$\delta A = A^{1/2} = \langle I \rangle^{1/2}, \qquad \delta M = \frac{1}{\sqrt{2 + M^2} \langle I \rangle^{1/2}},$$
$$\delta \theta_0 = \frac{1}{\sqrt{2} M \langle I \rangle^{1/2}}.$$

As expected, the errors for M and $\delta\theta_0$ decrease as the square root of the signal (a typical behavior in the presence of shot noise) and with the modulation depth M. (The greater the modulation, the more information in the measured values.)

For the curve presented in Fig. 3(b) of the main text, the numbers are as follows: typical maximum signal of approximately 1 photon per 10 pulses (i.e., twice below photon-counting saturation); pixel dwell time of 2.5 μ s; 8 images per orientation; and 31 orientations, resulting in a typical total signal of about 5000 photons per P-THG pixel. The modulation depth M as defined above is around 0.6, which yields

$$\frac{\delta A}{A} \approx 7.9\%, \qquad \delta M \approx 0.051,$$

 $\delta \theta_0 \approx 0.093 \text{ rad} \approx 5.3^\circ.$

For comparison, the error should be reduced threefold when averaging the signal over nine pixels. Because this error is low, we can assume that the measured difference for 1 and 9 pixels is of the order of the statistical error, and we find indeed from the curves that $\delta\theta_0\approx 3-4^\circ$ and $\delta M\approx 0.08$, which are the right order of magnitude for the expected error.

APPENDIX E: COMPARING XRS AND P-THG

In this study, we assume that the lipid tails adopt a Gaussian range of angles θ relative to the bilayer normal centered at either 0° or 30° for the fluid and gel phase, respectively. To compare this value to XRS measurements, we calculate the second-order Legendre polynomial $\langle P_2 \rangle$, as described in Refs. [33,34]:

$$\langle P_2 \rangle = \frac{\int_0^{\pi/2} d\theta \sin(\theta) P_2[\cos(\theta)] \exp\{\frac{-(\theta - \langle \theta \rangle)^2}{2\sigma^2}\}}{\int_0^{\pi/2} d\theta \sin(\theta) \exp\{\frac{-(\theta - \langle \theta \rangle)^2}{2\sigma^2}\}}, \quad (E1)$$

where $P_2[\cos(\theta)] = \frac{1}{2}[3\cos(\theta)^2 - 1]$. A disorder-free $(\sigma = 0)$ distribution of lipids with $\langle \theta \rangle = 0^\circ$ corresponds to $\langle P_2 \rangle = 1$, with $\langle P_2 \rangle \to 0$ for a completely isotropic distribution.

We assume that the MLVs were in the fluid phase (above the transition temperature), resulting in $\langle\theta\rangle=0$. The MLV modulation measured in the MLVs for the liquid-phase lipid-water interface correlates with $\sigma=20^\circ$ as predicted in our multiscale model. Using this value for disorder in the calculation just described, we calculate $\langle P_2\rangle=0.77$, as noted in the main text. This result is much different than the value 0.4 (which in our model correlates with $\sigma\approx38^\circ$) measured for DMPC using XRS [35]. We attribute this difference to the inaccuracy in the calculated lipid-water $\chi^{(3)}$ ratio. As we have shown through the comparison between lipid-vacuum and lipid-water interfaces, the modulation increases when the $\chi^{(3)}$ ratio approaches 1.

To validate this explanation, we calculate the scaling factor (s) which, when multiplied by each tensor element of $\chi^{(3)\text{ML}}(\langle\theta_0\rangle=0,\,\sigma=38^\circ)$ predicts the experimentally observed modulation (M=0.73) at the MLV-water interface. More simply, we solve the expanded form of Eq. (13) (as we have access to the explicit tensor elements) for s:

$$M = 0.73 = \frac{(s \cdot \chi_{YYYY}^{(3)ML} - \chi^{(3)H_2O})^2}{(s \cdot \chi_{XXXX}^{(3)ML} - \chi^{(3)H_2O})^2 + f_{NA}},$$
 (E2)

where we also scale $f_{\rm NA}$. Using the modulation M=0.13 from the lipid droplet, Eq. (14) gives $f_{\rm NA}=0.15 (s\cdot \langle \chi^{(3)\rm ML}\rangle - \chi^{(3)\rm H_2O})$. The tensor elements of $\chi^{(3)\rm ML}(\langle \theta_0\rangle = 0,\,\sigma=38^\circ)$ calculated according to Eq. (6) in the text are

$$\chi_{XXXX}^{(3)\text{ML}} = 4.05, \qquad \chi_{YYYY}^{(3)\text{ML}} = 3.50, \qquad 3\chi_{XXYY}^{(3)\text{ML}} = 3.78.$$

Solving Eq. (13) using these values leaves s=0.63, which results in $\langle \chi^{(3)\text{ML}} \rangle = 2.32 \times 10^{-22} \text{ m}^2 \text{ V}^{-2}$. This value is much closer to the values measured previously (difference of approximately 0.35 compared to about $1.0 \times 10^{-22} \text{ m}^2 \text{ V}^{-2}$), indicating that the discrepancy between the P-THG and XRS data can be attributed in great part to the uncertainty in the isotropic $\chi^{(3)\text{ML}}$ value, and that accurate values for the modulation can be measured when a correct isotropic $\chi^{(3)\text{ML}}$ value is used. Specifically, increased accuracy could come from better estimates for γ^{PO} as well as the ability to determine the degree of anisotropy of the γ^{CH} contribution.

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- [32] See Supplemental Material at http://link.aps.org/ supplemental/10.1103/PhysRevX.3.011002 for movies S1, S2, and S3. Movie S1: Multiphoton images of MLVs. The rotating bar (left) indicates the polarization of the exciting fields used to generate the CARS or THG images. Driving fields induce maximal CARS intensity when aligned parallel to the average CH2 moiety and maximal THG intensity when aligned parallel to the average CC bond direction. The P-THG images with polarization-resolved detection illustrate two different THG mechanisms. The THG signal due to birefringence is emitted perpendicular to the excitation field, while the interface signal retains the same polarization direction. Scale bar = 15 μ m. Movie S2: P-THG imaging of a large multilamellar lipid aggregate. P-THG sensitivity to lipid ordering is clearly visible in this image series of an aggregate of multilamellar objects with varying sizes. THG signals obtained at interfaces and within ordered regions exhibit a strong, easily observed polarization dependence. The rotating bar indicates the excitation polarization and is 50 µm in length. Movie S3: P-THG imaging of a human skin biopsy recorded approximately 35 μ m below the surface. Left: Raw THG images recorded as the driving polarization is rotated. The rotating bar indicates the polarization incident on the sample. Top right: Modulation image. A strong, order-related modulation is observed specifically from the folds containing multilamellar lipid phases, whereas other cellular structures exhibit only weak, geometry-related modulation (see text). Bottom right: Extracted orientation image. The average orientation of lipid molecules in the multilamellar phases is consistently found to be perpendicular to the folds.
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