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# Transpolar aurora: time evolution, associated convection patterns, and a possible cause 

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#### Abstract

We present two event studies illustrating the detailed relationships between plasma convection, field-aligned currents, and polar auroral emissions, as well as illustrating the influence of the Interplanetary Magnetic Field's ycomponent on theta aurora development. The transpolar arc of the theta aurorae moves across the entire polar region and becomes part of the opposite side of the auroral oval. Electric and magnetic field and precipitating particle data are provided by DMSP, while the POLAR UVI instrument provides measurements of auroral emissions. Ionospheric electrostatic potential patterns are calculated at different times during the evolution of the theta aurora using the KTH model. These model patterns are compared to the convection predicted by mapping the magnetopause electric field to the ionosphere using the Paraboloid Model of the magnetosphere. The model predicts that parallel electric fields are set up along the magnetic field lines projecting to the transpolar aurora. Their possible role in the acceleration of the auroral electrons is discussed.


Keywords. Ionosphere (Plasma convection; Polar ionosphere) - Magnetospheric physics (Magnetosphereionosphere interactions)

## 1 Introduction

The global distribution of the aurora has a qualitative as well as a quantitative dependence on the interplanetary magnetic field (IMF). For southward IMF the intense auroral activity is usually confined to the region known as the auroral oval, whereas for northward IMF considerable auroral activity is often encountered poleward of this region (e.g. Davis, 1963; Berkey et al., 1976; Lassen and Danielsen, 1978). The existence of auroral arcs at very high latitudes was established early on (e.g. Mawson, 1916; Davis, 1960; Denholm, 1961; Denholm and Bond, 1961; Eather and Aka-

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sofu, 1969). These arcs, variably referred to in the literature as "Sun-aligned arcs," "polar cap arcs," "high-latitude arcs," and "polar arcs," have been observed for many years using all-sky cameras (e.g. Lassen and Danielsen, 1978), and photometers on board low-altitude polar-orbiting spacecraft, such as ISIS and DMSP (e.g. Gussenhoven, 1982; Ismail and Meng, 1982; Hoffman et al., 1985). However, due to the limited view of all-sky cameras and photometers on low-altitude satellites, these arcs were considered relatively isolated features. It was not until imaging instruments were flown on high-altitude spacecraft, such as Dynamics Explorer 1 (e.g. Frank et al., 1982, 1986) and Viking (e.g. Murphree et al., 1987), that the existence of so-called transpolar arcs (TPAs), luminous features extending across the polar region linking the dayside aurora to the nightside oval, became clear. A comprehensive overview of observations related to polar arcs and their electrodynamics is found in Blomberg and Marklund (1993). Valladares et al. (1994) performed a comprehensive statistical study of the occurrence of high-latitude arcs and their dependence on the IMF. Recently, Kullen et al. (2002) extended the Gussenhoven (1982) classification of polar arcs and presented statistics of the different arc types based on three months of POLAR UVI observations. Several models have been created attempting to explain transpolar arcs (e.g. Chang et al., 1998; Newell et al., 1999; Kullen, 2000; Slinker et al., 2001; Kullen and Janhunen, 2004; Naehr and Toffoletto, 2004). However, since not all polar arcs are transpolar, care must be taken not to confuse the different types when discussing their occurrence, the corresponding magnetospheric topology, or the physical mechanisms causing them.

Transpolar arcs form, in the Northern Hemisphere, from an expanded dawnside (duskside) emission region when $B_{y}$ changes from negative to positive (positive to negative) (Cumnock et al., 1997, Cumnock et al., 2002). If the IMF remains sufficiently stable after the initial $B_{y}$ polarity change, the transpolar arc will usually migrate across the polar region, often in both hemispheres (Cumnock, 2005). The pattern commonly referred to as the theta aurora describes the
situation when a transpolar arc is aligned nearly along the noon-midnight meridian (Frank et al., 1986). The TPAs cross the noon-midnight meridian only when $B_{y}$ changes sign, resulting in a large $B_{z} /\left|B_{y}\right|$ ratio. The focus of the present paper is on moving transpolar arcs, i.e., large-scale arcs traversing the entire polar region in response to a $B_{y}$ change, forming a theta aurora when the arc is at highest latitude.

Ionospheric convection patterns observed during northward IMF generally contains regions of sunward flow at highest latitudes, in contrast to the antisunward flow prevailing for southward IMF. A variety of configurations have been used to explain these observations, including spatially dominant one-cell patterns and multiple-cell patterns. The number of cells seems to have a first-order dependence on the ratio of $B_{z}$ to $B_{y}$, resulting in an increasing number of cells and reverse convection at highest latitudes as the IMF becomes more strongly northward (Potemra et al., 1984; Reiff and Burch, 1985; Heelis et al., 1986; Cumnock et al., 1995; Cumnock and Blomberg, 2004, and references therein). Observations indicate that TPAs may be associated with either sunward or antisunward flow, as well as a variety of convection patterns, including a four-cell pattern (Frank et al., 1986; Gusev and Troshichev, 1990; Jankowska et al., 1990; Zanetti et al., 1990), a dominant one-cell (Hoffman et al., 1985), a three-cell ( Carlson et al., 1988; Zanetti et al., 1990; Jankowska et al., 1990), or a distorted two-cell (Robinson and Mende, 1990; Marklund et al., 1991). These studies are all based on isolated observations of single TPAs and thus represent different stages of theta aurora evolution relating to changing IMF $B_{x}$ and $B_{y}$ conditions during northward IMF.

Satellites have observed a variety of field-aligned current (FAC) configurations, including pairs of upward and downward field-aligned current sheets associated with the TPAs (e.g. Frank et al., 1986; Menietti and Burch, 1987; Marklund et al., 1991; Obara et al., 1993; Blomberg and Marklund, 1993; Blomberg and Cumnock, 2005). In addition, as the IMF becomes more northward both the Region 1 to Region 2 and the NBZ to Region 1 current ratios increase (e.g. Blomberg and Marklund, 1993).

The main purpose of this paper is to model the global potential patterns and to compare them to the convection predicted by mapping the magnetopause electric field to the ionosphere using the Paraboloid Model of the magnetosphere during the evolution of dawnside and duskside originating transpolar arcs. The present study follows up on the results of Cumnock and Blomberg (2004). Utilizing satellite data, the Royal Institute of Technology (KTH) numerical model provides the high-latitude global potential pattern. In addition, the magnetopause electric field predicted from IMF data is mapped to the ionosphere using Moscow State University's (MSU) Spherical and Paraboloid Models of the magnetosphere.

We model the entire evolution of the theta aurorae, and compare observations to the output of both models. In both events the transpolar arc moves across the entire polar region and eventually becomes part of the opposite side of the auroral oval.

## 2 Observations and model results

The Ultraviolet Imager (UVI) experiment (Torr et al., 1995) on the POLAR spacecraft provides global images of the aurora. The instrument is able to resolve 0.5 deg in latitude at apogee; thus, a single pixel projected to 100 km altitude from apogee is approximately $50 \times 50 \mathrm{~km}$. In the Lyman-BirgeHopfield mode (LBH) the instrument measures molecular nitrogen emissions in the $140-160 \mathrm{~nm}$ spectral region.

The Defense Meteorological Satellite Program's (DMSP) satellites provide measurements of precipitating particles and ionospheric plasma flows from three Northern Hemisphere passes during each of the two time periods of interest. DMSP F13 (Rich, 1994) passes in the dusk-to-dawn direction and DMSP F14 from about 21 MLT to 10 MLT in the Northern Hemisphere. The electrostatic potential distribution is derived by integrating the electric field $(\boldsymbol{E})$ along the satellite track, utilizing $\boldsymbol{E}=-\boldsymbol{v} \times \boldsymbol{B}$, where $\boldsymbol{v}$ is the measured transverse ion drift velocity and ( $\boldsymbol{B}$ ) is the model geomagnetic field. The electrostatic potential can then be used to determine which regions of sunward and antisunward flow may be connected by equipotential flow lines.

In order to analyse the global potential patterns during theta aurora evolution we utilize the KTH numerical model that assumes a field-aligned current distribution and a conductivity model and from these calculates the potential distribution. A detailed description of the model is found in Blomberg and Marklund (1991a). The model input (the fieldaligned current distribution) is qualitatively inferred from satellite UV images that give direct information about upward currents associated with electron precipitation. Downward currents are qualitatively inferred from statistical models. The currents are then quantitatively calibrated directly against satellite magnetometer data, as well as indirectly calibrated by comparing the calculated model potential pattern to satellite plasma flow data in an iterative manner. Data from one or more satellites can be used for the calibration, here DMSP F13 and F14 data were used.

The polar cap convection dependence on the IMF direction may be estimated by mapping the solar wind electric field to the polar ionosphere (Alexeev, 1986; Toffoletto and Hill, 1989). This approach assumes a very high conductivity along the magnetospheric magnetic field and thus magnetic field lines are equipoential. In this model, global reconfiguration of the magnetospheric magnetic field leads to modification of the polar cap convection (Belenkaya, 1998a, b; 2002).

The goal here is to reconstruct on a global scale the distribution of all auroral electrodynamic parameters during the evolving northward IMF conditions as a TPA moves across the entire polar region. Model inputs are the ionospheric conductivity and FAC distributions. The boundary condition used is that the potential is zero at $50^{\circ}$ magnetic latitude; in reasonable agreement with DMSP data. Model output is the ionospheric potential that can be compared with the potential calculated from electric field data along the DMSP satellite tracks. POLAR UVI provides information on the upward FAC distribution. For more details on UVI, DMSP
and the KTH numerical model for the events discussed here, see Cumnock and Blomberg (2004).

### 2.1 Spherical model of the magnetosphere

In the Moscow State University spherical model of the Earth's magnetosphere (Alexeev and Belenkaya, 1983), the magnetopause is approximated by a sphere of radius $R_{1}=10 R_{E}$ with the geomagnetic dipole located in its centre. At the magnetopause there are screening currents that create a uniform magnetic field antiparallel to the dipole moment. The magnetic field $\boldsymbol{b}$ that penetrates from the solar wind into the magnetosphere is $\boldsymbol{b}=k \boldsymbol{B}$, where $\boldsymbol{B}$ is the interplanetary magnetic field (IMF) and $k \approx 0.1$. The spherical model describes the general features of the interaction between the interplanetary and magnetospheric fields. In the dayside magnetosphere and in the polar caps the model output is consistent with observations.

The magnetic field associated with the magnetopause screening currents allows us to distinguish between two different types of reconnection, corresponding to southward and northward IMF (Alexeev and Belenkaya, 1983). For southward IMF ( $B_{z}<0$ ), two-dimensional reconnection takes place at the merging line on the spherical magnetopause. Figure 1 shows the meridional cross section of the spherical magnetosphere for southward IMF. The region marked 1 indicates closed field lines, the regions $2 a$ and $b$ (dotted) indicate open field lines of the northern and southern polar caps. For northward IMF ( $B_{z}>0$ ), three-dimensional reconnection occurs at the two neutral magnetic field points. Figure 2 shows the meridional cross section of the spherical magnetosphere for northward IMF. The region marked 1 indicates closed field lines, the regions 2 a and b (dotted) indicate open field lines of the northern and southern polar caps, and the shaded region indicates interplanetary magnetic field lines inside the magnetosphere. The neutral points and neutral lines are surrounded by diffusion regions where the conductivity is high but finite and where MHD breaks down. Magnetic field lines outside of the diffusion regions are assumed to be equipotential. This assumption, together with the boundary condition for the electric field component tangential to the magnetopause: $E_{t}=k E_{I M F}$, gives us the electric potential distributions in the open field line regions, where $\boldsymbol{E}$ is the fraction of the solar wind electric field $E_{I M F}$ that penetrates into the magnetosphere.

The spherical magnetospheric model was used to calculate distributions of the electrostatic potential in the open field line region in the northern ionosphere. The electrostatic potential distributions in the northern polar cap, predicted by the spherical model, are shown for southward IMF in Fig. 3 and for northward IMF in Fig. 4 (see also (Belenkaya, 1998a, b). For both cases $k=0.1$ was assumed. For northward IMF, the ionospheric convection pattern on the open field lines has two cells for $B_{x} \neq 0$ and one cell for $B_{x}=0, B_{y} \neq 0$. Reverse convection occurs near the cusp projection.

Figure 5 (derived from Fig. 9 of Cowley (1973)) illustrates the three-dimensional geometry of the superposition of the


Fig. 1. The meridional cross section of the spherical magnetosphere for southward IMF. The region marked 1 indicates closed field lines, the regions 2 a and b (dotted) indicate open field lines of the northern and southern polar caps.


Fig. 2. The meridional cross section of the spherical magnetosphere for northward IMF. The region marked 1 indicates closed field lines, the regions 2 a and b (dotted) indicate open field lines of the northern and southern polar caps, the shaded region indicate interplanetary magnetic field lines inside the magnetosphere.
dipole and the uniform magnetic fields for northward IMF. In the spherical model the uniform field is simply the sum of the penetrated portion of the IMF and the magnetic field resulting from the magnetopause currents screening the dipole field (both of them are also uniform fields). The surfaces A1 and A2 divide magnetic field lines of different topological types (open, closed, and interplanetary) and are called separatrix surfaces (see, for example, Siscoe et al., 2001). A1 is a boundary between open and interplanetary magnetic field lines, whereas A2 divides open and closed magnetic fluxtubes. Two magnetic field lines connecting the two neutral points $\left(\mathrm{O}_{S}\right.$ and $\left.\mathrm{O}_{N}\right)$ form a separator line $\left(\mathrm{C}_{1} \mathrm{C}_{2}\right.$, part $\mathrm{C}_{2}$ is not shown in Fig. 5). The separatrix surfaces intersect at the




$$
\mathrm{B}_{\mathrm{X}}<0, \quad \mathrm{~B}_{\mathrm{Y}}=0
$$

Fig. 3. Distribution of the electric equipotentials in the open field line region of the northern polar cap, in the spherical model, for southward IMF, $\boldsymbol{B}$, dependent on $b_{x}$ and $b_{y},(\boldsymbol{b}=k \boldsymbol{B}, k=0.1)$.


Fig. 4. Distribution of the electric equipotentials in the open field line region of the northern polar cap in the spherical model for northward IMF dependent on $b_{x}$ and $b_{y}$.
separator line. For southward IMF (not shown), the separator line is a quasi-neutral line, since at each point in the plane perpendicular to it, magnetic field lines have an X-type configuration, leading to two-dimensional reconnection. For northward IMF, there is no quasi-neutral line in the magnetosphere.

For northward IMF, the boundary of the northern open field line bundle, $\mathrm{A}_{1}$, converges to the northern magnetic


Fig. 5. Three-dimensional geometry of the superposition of the dipole and uniform (generated by the magnetopause currents and penetrated from the solar wind) magnetic fields for northward IMF (derives from Fig. 9 of Cowley (1973)).
null $\mathrm{O}_{N}$. The separatrix surface formed by the magnetic field lines originating from the boundary of the southern polar cap also converges to the northern magnetic null. From this null point and perpendicular to both separatrix surfaces, two singular magnetic field lines $\mathrm{B}_{1}$ and $\mathrm{B}_{2}$ diverge (these singular lines were called "stemlines" by Siscoe et al. (2001)). Along $\mathrm{B}_{2}$, the neutral point $\mathrm{O}_{N}$ maps to the ionospheric projection of the cusp ( $\mathrm{O}_{N}{ }^{\prime}$ ).

Alexeev and Belenkaya (1985) obtained an analytical expression approximating the NBZ currents on open field lines during northward IMF. NBZ currents flow out of (into) the ionosphere in the dawn (dusk) sectors. These field-aligned currents are each related to a convective vortice: the upward current with a clockwise one and the downward current with an anticlockwise cell. Figure 6 illustrates all field-aligned currents and ionospheric convection flows for $B_{z}>0$ (Clauer et al., 2001).

Let us assume for a moment that there are no parallel electric fields, and thus that each magnetic field line is an equipotential curve. Then, equipotential curves on the intersection of the southern magnetopause with the open field line bundle of the northern polar cap project to convection cells in the ionosphere. This is because the whole boundary of the open field line bundle converges to the neutral point $\mathrm{O}_{N}$ (see Fig. 5). Each equipotential crosses the open field line bundle boundary at two points. If projected to the ionosphere, these points all end up at $\mathrm{O}_{N}$, with the single exception being the projection of the equipotential contour which intersects at some point, $\mathrm{L}_{N}$, the singular southern magnetic field line $\mathrm{B}_{1}$. This contour has a potential $\Phi_{L N}$. By analogy, the singular equipotential contour on the magnetopause of the open field lines connecting to the southern polar cap, which intersects
the northern stemline $\mathrm{B}_{1}$ at $\mathrm{L}_{S}$ has the potential $\Phi_{L S}\left(\mathrm{~L}_{N}\right.$ and $\mathrm{L}_{S}$ are located at the intersections of the stemlines $\mathrm{B}_{1}$ with the magnetopause). The point $\mathrm{L}_{N}$ maps along the southern $\mathrm{B}_{1}$ to $\mathrm{O}_{S}$ and then along the southern $\mathrm{B}_{2}$ to $\mathrm{O}_{S}{ }^{\prime}$ and also along $\mathrm{A}_{2}$ to the open field line boundary of the northern polar cap. Thus, the boundary of the open field lines in the Northern Hemisphere has a potential $\Phi_{L N}$. The projection of the southern cusp $\mathrm{O}_{S}$ along the southern stemline $\mathrm{B}_{2}$ on the southern ionosphere $\left(\mathrm{O}_{S}\right.$ ') also has the potential $\Phi_{L N}$. Similarly, $\mathrm{O}_{N}$ and $\mathrm{O}_{N}$ ' have a potential $\Phi_{L S}$ which is also the potential of the open field line boundary in the southern polar cap. So, on the northern (southern) equipotential ionospheric boundary between open and closed field lines, a singularity exists, $\mathrm{O}_{N},\left(\mathrm{O}_{S}\right.$ '), where the potential macroscopically (on the MHD scale) is discontinuous. This exception determines the source function in the Poisson equation for the entire polar cap.

We now have magnetic field lines forming the boundary of the open field line bundles, all converging to the null points $\mathrm{O}_{N}$ or $\mathrm{O}_{S}$. For these lines the equipotentiality assumption for the magnetic field lines is invalid. Thus, an electric field component parallel to the magnetic field must exist (Greene, 1988) on the field lines of the cylindrical separatrix surfaces. All magnetic field lines of these separatrix surfaces tend to reach closer to the separator line $\left(\mathrm{C}_{1} \mathrm{C}_{2}\right)$ before veering off to the null points on the magnetopause (Siscoe et al., 2001).

The singular equipotential traversing the point $\mathrm{L}_{N}$ maps to the open field line region of the northern polar cap, which it divides into two vortices. Its projection has a potential $\Phi_{L N}$, except in the vicinity of $\mathrm{O}_{N}$, where the potential is $\Phi_{L S}$. This means that for $B_{y} \neq 0$ (for which $\Phi_{L N} \neq \Phi_{L S}$ ) field-aligned potential drops and consequently, strong fieldaligned currents should exist along those field lines which are topologically connected to the null points (Belenkaya, 2002). The locations of the ionospheric projections of the singular equipotentials $\left(\mathrm{L}_{N}{ }^{\prime} \mathrm{O}_{N}{ }^{\prime}, \mathrm{L}_{S}{ }^{\prime} \mathrm{O}_{S}{ }^{\prime}\right)$ dividing the polar caps into two vortices depend on the $B_{y}$ component of the IMF (see Fig. 4). For $B_{y}<0\left(B_{y}>0\right) \mathrm{L}_{N}{ }^{\prime} \mathrm{O}_{N}$ ' is in the dawn (dusk) sector of the northern polar cap.

The potential drop $\delta \Phi=\Phi_{L N}-\Phi_{L S}$ that exists between the two magnetic nulls for $B_{y} \neq 0$ also exists on the separator line $\left(\mathrm{C}_{1} \mathrm{C}_{2}\right)$ connecting the two magnetic neutral points. Siscoe et al. (2001) emphasized the significant role that $E_{\|}$ plays for the global magnetic reconnection. Greene (1988) also mentioned that $E_{\|}$arises due to the electric field singularity at the neutral points of the magnetic field. The potential of $L_{S}$ is
$\Phi_{L S}=\Phi_{O N}$.
By analogy, the potential
$\Phi_{L N}=\Phi_{O S}$.
We introduce $\delta \Phi$ as the potential drop between the null points
$\delta \Phi=\Phi_{L N}-\Phi_{L S}=\Phi_{O S}-\Phi_{O N}$.


Fig. 6. Field-aligned currents and convection in the polar cap for northward IMF. From high to lower latitudes: NBZ currents, Region I and II currents, currents near the cusp region on the closed field lines (Clauer et al., 2001).

For the spherical model $\Phi_{O S}-\Phi_{O N}=\delta \Phi_{p c} \sin \varphi_{m}$, where $\varphi_{m}$ is the angle between the x -axis and the projection of the IMFvector on the $x-y$ plane, and $\delta \Phi_{p c}$ is the potential drop across the polar cap in the spherical model for southward IMF. $\varphi_{m}$ is defined by:
$\sin \varphi_{m}=B_{y} / B_{l}, \cos \varphi_{m}=B_{x} / B_{l}$ where $B_{l}=\left(B_{x}^{2}+B_{y}^{2}\right)^{1 / 2}$.
For $B_{x}=0$ and $B_{y} \neq 0, \sin \varphi_{m}= \pm 1$ and the potential drop between the magnetic null points maximises and becomes equal to $\delta \Phi_{p c}$. This result agrees with that obtained by Siscoe et al. (2001): for azimuthal IMF the potential drop across the open field line bundle is equal to the potential drop applied to the separator line connecting the two neutral points.

Extending the singular equipotential onto the closed ionospheric field lines divides the two low-latitude vortices of the four-cell convection system existing for northward IMF. In Fig. 7 the corresponding convection patterns in the northern and southern ionosphere are shown. We see that for $B_{x}<0$, closed field lines going near the separator line $\mathrm{C}_{1} \mathrm{C}_{2}$ (thick curve) in the Northern Hemisphere are close to the singular equipotential on closed plasma sheet field lines. We assume that a field-aligned potential drop can exist only in the vicinity of $\mathrm{C}_{1} \mathrm{C}_{2}$. Low-latitude closed field lines located equatorward of the poleward edge of the auroral oval are not affected very much by the IMF. Thus, those lines do not approach $\mathrm{C}_{1} \mathrm{C}_{2}$ and, consequently, they are equipotential. We therefore expect the field-aligned potential drop to be on the singular equipotential on the plasma sheet closed field lines from the cusp projection up to the poleward edge of the auroral oval.

We suggest, following Belenkaya (2002), that the auroral emissions in transpolar auroral arcs are caused, largely, by the potential difference that exists between the northern


Fig. 7. Ionospheric convection patterns in the northern and Southern Hemispheres. Thick curves mark the location of magnetic field lines that come close to the separator line $\mathrm{C}_{1} \mathrm{C}_{2}$. Northward IMF with $B_{x}<0, B_{y}<0$.
and southern magnetic null points for IMF $B_{y} \neq 0$. On the local scale, the potential difference along a particular magnetic field line traversing the transpolar arc, determines the acceleration potential. The emission region should further be associated with the singular equipotential on the closed plasma sheet field lines from the cusp projection to the poleward boundary of the auroral oval (in the northern polar cap for $B_{x}<0$ and in the southern polar cap for $B_{x}>0$ ).

### 2.2 Paraboloid model of the magnetosphere

The magnetospheric plasma convection and the associated magnetospheric electric field are determined from the boundary conditions at the magnetopause (Alexeev, 1986; Kalegaev, 2000). The IMF penetrating the magnetosphere is connected to the undisturbed IMF upstream of the bow shock, $\boldsymbol{B}_{\mathbf{0}}$, by the relations: $b_{\perp}=k_{m p \perp} B_{0 \perp}$ and $b_{\|}=k_{m p \|} B_{0 \|}$, where $b_{\|}$and $b_{\perp}$ are the components parallel and orthogonal to the Sun-Earth line, respectively. For large magnetic Reynolds number $\left(R_{m} \gg 1\right)$ the magnetopause reconnection efficiency coefficients are $k_{m p \perp}=0.9 \chi^{1 / 2} R_{m}^{-1 / 4}$ and $k_{m p \|}=2 \chi\left(\pi \mathrm{R}_{m}\right)^{-1 / 2}$, they depend on $R_{m}$ and $\chi=\rho_{2} / \rho_{1}$ (Alexeev et al., 2003). Here $\rho_{1}$ is the solar wind plasma
density, $\rho_{2}$ is the magnetosheath plasma density downstream of the bow shock and $\chi=\rho_{2} / \rho_{1}$ determines the plasma compression at the bow shock. The magnetic Reynolds number $R_{m}=\mu_{0} \sigma \mathrm{~V}_{0} R_{1}$ is determined by the magnetopause subsolar distance, $R_{1}$, by the solar wind velocity $V_{0}$, and by the effective conductivity $\sigma$, of the solar wind plasma.

In contrast to the spherical model, the reconnection efficiency coefficients are different for the parallel and orthogonal components of the IMF. Both of them can be calculated self-consistently from the magnetosheath plasma flow solution (see Alexeev et al. (2003) for a more thorough explanation). We use both of the magnetospheric models because one of them (the spherical) enables a clear conceptual explanation of the TPA mechanism, and the other one (the paraboloid) gives quantitative results for ionospheric plasma convection patterns and auroral oval location that can be compared with the KTH numerical model and satellite observations.

In the course of both events that are described below (8 November 1998 and 11 February 1999), the IMF strength and solar wind dynamic pressure were both above their respective average values. The Paraboloid Model takes into account not only the IMF influence on the structure of the magnetosphere, but also the dynamics of the subsolar distance and of the polar cap and auroral oval boundaries (see Alexeev et al., 2003). The Paraboloid model is here parametrised by solar wind data from the ACE spacecraft and by the geomagnetic indices $D_{s t}$ and $A L$ (obtained from the World Data Center in Kyoto).
The model calculations give us the polar cap potential distribution, the potential drop along the separator line, and the acceleration voltage of the auroral particles that create the TPA. For the paraboloid model the potential drop between the neutral points equals
$\delta \Phi=\Phi_{O S}-\Phi_{O N}=2 R_{1} k_{P} E_{I M F} \sin \varphi_{\mathrm{m}}$,
where $R_{1}$ is the distance to the subsolar magnetopause point ( $R_{1}=10 R_{E}$ ), $E_{I M F}$ is the interplanetary electric field, and $k_{p}$ describes the ratio of the ionospheric polar cap potential drop to the potential drop across the open field line bundle in the solar wind. For our two events $k_{P}=0.05$ was assumed.
The model results explain the correlation between TPA occurrence and the $B_{y}$ component of the IMF because the potential drop on the separator line, $\delta \Phi$, is proportional to $B_{y}$ (see Eq. (4)). They are also in agreement with the observed TPA motion from dawn to dusk or the opposite, with the change in sign of IMF $B_{y}$. The distribution of the fieldaligned potential difference $\delta \Phi_{\|}(s)$ along the ionospheric TPA curve is suggested to be proportional to $\delta \Phi s / S$, where $s$ is the ionospheric distance from the cusp projection and $S$ is the length of the TPA curve from the cusp projection to the poleward boundary of the auroral oval characterized by colatitude $\theta_{m}, S \sim R_{E} \sin \left(2 \theta_{m}\right)$.
It is not yet clear what magnetospheric feature corresponds to the poleward boundary of the auroral oval, and what drives the TPA at zero $B_{y}$ also remains an open question.


Fig. 8. Shown are magnetic field data from the ACE satellite which orbits the L1 Lagrangian point about $200 R_{E}$ sunward of the Earth. IMF GSM components are plotted for 8 November 1998, as a function of corrected universal time (UT plus the estimated propagation time from the satellite to GSM $X=0$ ); about 45 min . The thick vertical line marks the time when Polar UVI shows a TPA aligned along the noon-midnight meridian in the Northern Hemisphere. The three thin vertical lines mark the time when DMSP F13 reaches highest latitudes over the Northern Hemisphere. The thick horizontal line at the top denotes the time period when UVI data are available.

### 2.3 Event of 8 November 1998

In Fig. 8 we show magnetic field data from the ACE (Advanced Composition Explorer) spacecraft that orbits the L1 Lagrangian point approximately $200 R_{E}$ sunward of the Earth. IMF GSM components are plotted for 8 November 1998, as a function of corrected universal time (UT plus the estimated propagation time from the satellite to GSM $X=0$ ); in this event the correction is about 45 min . The thick vertical line marks the time when POLAR UVI observes a TPA aligned along the noon-midnight meridian in the Northern Hemisphere. The three thin vertical lines mark the time when DMSP F13 reaches highest latitudes over the Northern Hemisphere. The thick horizontal line at the top denotes the time period when UVI data is available.

IMF $B_{z}$ is positive for at least 3 h prior to and following a change in $B_{y}$. IMF $B_{x}$ is negative through the time period of interest. $B_{y}$ is small for 1 to 1.5 h while changing sign. ACE plasma measurements (not shown) indicate that during the time of the IMF $B_{y}$ change, solar wind ion density is about $20 \mathrm{~cm}^{-3}$ and solar wind velocity is approximately $550 \mathrm{~km} / \mathrm{s}$.

To map the solar wind electric field to the polar ionosphere using the Paraboloid Model, the $D_{s t}$ and $A L$ geomagnetic indices are needed. The event studied (see Fig. 9) corresponds to quiet or slightly disturbed time. $D_{s t}$ is about -50 nT and $A L$ is $-400,-69$, and -93 nT , respectively, for the three instants modelled. The model polar cap magnetic flux changed from 740 to 430 MWb during the evolution of the TPA.


Fig. 9. Left: Data shown from three DMSP passes on 8 November 1998 (12:17-12:41, 13:59-14:19, and 15:41-16:01 UT) that occur during the Polar UVI data period. DMSP F13 and F14 horizontal plasma flows, perpendicular to the satellite track, are plotted over a UV image taken at the time when F13 is at highest magnetic latitudes. Right: For the same 3 times are shown the modelled polar cap boundary, auroral oval, and polar cap convection generated by the solar wind electric field, as predicted by the Paraboloid Model. The model parameters for each case were calculated from solar wind data and geomagnetic indices. For UT=14:09:48 the TPA observed in the dusk sector may be explained by the time delay ( $\sim 20 \mathrm{~min}$ ) between the IMF turning and the ionospheric convection response (Clauer et al., 2001). At 13:49:48 UT IMF $B_{y}$ was slightly positive, which corresponds to the observed TPA location. Red curves show the electrostatic potential patterns ( 10 kV contour separation). See text for details.

POLAR UVI provides images in the Northern Hemisphere. In this event the transpolar arc originates on the duskside of the auroral oval and migrates across the entire polar region. Around 12:28 UT the duskside of the auroral oval has expanded poleward, as expected for positive $B_{z}$ and positive $B_{y}$, and has a bright poleward edge. IMF $B_{y}$ changes sign from positive to negative at approximately 14:00 UT then decreases approximately 14 nT at 14:45 UT. IMF $B_{x}$ is negative and $B_{z}$ remains positive (ranging from $13-26 \mathrm{nT}$ for the next 9 h ). During the next hour (14:00 to 15:00 UT) the TPA moves dawnward. At 15:01 UT, approximately 1 h after $B_{y}$ becomes negative/near zero and approximately 15 min after $B_{y}$ becomes more strongly negative, the transpolar arc
has moved to highest latitudes and is aligned along the noonmidnight meridian, forming what is commonly referred to as theta aurora. The dawnside of the auroral oval has expanded poleward, as expected for negative $B_{y}$. The arc continues its dusk to dawn motion and by 16:15 UT it has moved across the polar region and appears to be part of the dawnside auroral oval.

Figure 9 shows, in the left column, POLAR UV images in the Northern Hemisphere with DMSP F13 and 14 horizontal plasma flows are plotted over each UV image for the three Northern Hemisphere passes available during the TPA evolution. The data shown at the top occur during positive $B_{y}$ and northward IMF. DMSP F13 shows a spatially expanded duskside region of sunward flow that is bifurcated by a small antisunward flow region. This pattern has three sunward and two antisunward flow regions, producing four convection reversal boundaries (CRBs), where, for southward IMF, two CRBs are expected. The high-latitude convection pattern is dominated by sunward flow, some of which can be closed in the dawnside antisunward flow region, producing clockwise (negative potential) circulation in a cell located at highest latitudes on the dawnside of the polar region. The sunward flow associated with the TPA may be closed in the antisunward flow region equatorward, resulting in a local maximum in the negative potential region. In addition to an expanded duskside sunward flow region during positive $B_{z}$ and $B_{y}$, we expect an expanded duskside auroral oval.

The equipotentials in the polar cap mapped from the magnetopause using the MSU paraboloid model are shown on the right. The MSU paraboloid model calculates the equatorward boundary of the auroral oval (thick grey curve), defined as the projection of the earthward edge of the magnetospheric tail current sheet. Also shown are the convection contours obtained by mapping the electric potentials from the magnetopause along open field lines into the ionosphere (negative potential, red curves). There is good agreement between the equatorward boundary of the auroral oval and the UV image. The negative potential dominates the polar region, with a potential difference of 103 kV at high latitudes in the KTH numerical model and 98 kV in the MSU paraboloid model. The model polar cap magnetic flux was calculated using its equality to the tail lobe magnetic flux. The assumption $E_{\|}=0$ allows us to calculate the ionospheric electric field from the known distribution of the electric potential at the magnetopause, in turn calculated by the method described by Alexeev et al. (2003).

By the time of the second DMSP pass (middle plot of Fig. 9), IMF $B_{y}$ has changed sign from positive to weakly negative. Both DMSP F13 and F14 reach higher magnetic latitudes than in the previous pass. On the dayside large antisunward and sunward flows are seen in what is traditionally the polar cap. Previously, the sunward flow was dominated by clockwise circulation (negative potential) in a dawn cell, whereas now it is dominated by counterclockwise circulation (positive potential) in a high-latitude dusk cell. The transpolar arc has moved to higher latitudes, and is still located on the duskside of the noon-midnight meridian. The arc re-
mains collocated with the duskside of the high-latitude sunward flow region, and both are now at higher latitudes than in the previous pass.

To the right, we show the corresponding equipotentials on open field lines projected to the ionospheric level. The polar cap potential drop is $\delta \Phi_{p c}=58 \mathrm{kV}$. The figure illustrates the location of the convection patterns relative to the noonmidnight meridian and explains the TPA location along it. However, the calculated polar cap size is smaller than the one estimated from POLAR data.

At the time of the observations shown at the bottom of Fig. 9, IMF $B_{z}$ is still positive and IMF $B_{y}$ has been negative (or weakly negative) for about 2 h . Both DMSP satellites have reached higher magnetic latitudes than in the previous orbit, with the F13 satellite track now aligned along the dawn-dusk meridian. The flow pattern has two main CRBs, the one located at highest latitudes is associated with a spatially expanded dawnside sunward flow region. The ionospheric convection pattern is still dominated by a counterclockwise circulating cell (positive potential) that is located at highest latitudes. The transpolar arc is located on the dawnside of the noon-midnight meridian but is still collocated with the duskward edge of the high-latitude sunward flow region.

The bottom right dial shows the polar cap convection at 15:51:04 UT on 8 November 1998, obtained from the Paraboloid Model. In this case the azimuthal component of the IMF, $B_{y}$, was negative and of the order of $B_{z}$. The polar cap potential drop of $\delta \Phi_{p c}=95 \mathrm{kV}$ is larger than that $(73 \mathrm{kV})$ obtained by the KTH model.

Figure 10 shows on the left model field-aligned current patterns for each of the DMSP passes on 8 November 1998, and on the right the electrostatic potential patterns generated by the KTH model. Upward and downward FACs are shown in red and blue, respectively, positive potentials are shown in blue and negative in red. The black line denotes zero potential. In the top left of Fig. 10, the TPA FACs reflect the motion of the TPA, first on the duskside of the auroral region, then at higher latitudes near the noon-midnight meridian, then finally the TPA has moved to the dawnside of the noon-midnight meridian. POLAR UVI (not shown) tracks the continued dawnward motion of the TPA. Table 1 lists the model input values for the FACs.

The maximum and minimum values of the electrostatic potentials are shown in Table 2. The last two columns show the values of the polar cap potential drops in the KTH and Paraboloid Models, respectively.

The Paraboloid Model gives the potential drop across the polar cap $\delta \Phi_{r}$ as
$\delta \Phi_{r}=b v \Delta y$.
Here $b=k_{b} B$ is the IMF penetrating the magnetosphere, $v=k_{v} V$ is the plasma velocity at the open field line bundle boundary near the magnetopause, and $\Delta y$ is the width of the open magnetic field line bundle at the magnetopause.

Table 1. Modelled field-aligned current values (MA) for 8 November 1998.

| Event | Dusk |  | Polar Region |  |  |  | Dawn |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | R2 $\downarrow$ | R1 $\uparrow$ | NBZ $\downarrow$ | TPA $\downarrow$ | TPA $\uparrow$ | NBZ $\uparrow$ | R1 $\downarrow$ | R2 $\uparrow$ |
| 8 November 1998-1 | 0.50 | 0.72 |  | 0.06 | 0.005 | 0.85 | 1.05 | 0.20 |
| 8 November 1998-2 | 0.15 | 0.55 | 0.55 | 0.10 | 0.05 | 0.30 | 0.60 | 0.60 |
| 8 November 1998-3 | 0.23 | 0.80 | 0.55 | 0.30 | 0.27 |  | 0.40 | 0.50 |

Table 2. Local potential extrema (kV) for 8 November 1998.

| Event | Dusk | Noon-midnight <br> Meridian |  | Dawn | $\delta \Phi_{K T H}$ | $\delta \Phi_{\text {pc-parab }}$ |
| :--- | :--- | :--- | :--- | ---: | ---: | :---: |
| 8 November 1998-1 | -45 |  | -90 | +13 | 103 | 98 |
| 8 November 1998-2 | -13 | +45 | -8 | +8 | 58 | 58 |
| 8 November 1998-3 | -25 | +48 |  | +9 | 73 | 95 |

To calculate $\delta \Phi_{p c}$, the transpolar potential drop, we take into account the saturation effect (Siscoe et al., 2002):
$\delta \Phi_{p c}=\delta \Phi_{r} \delta \Phi_{s} /\left(\delta \Phi_{r}+\delta \Phi_{s}\right)$.
The coefficient $k_{b}=0.2$ for the magnetic field was determined based on the results of Alexeev et al. (2003). The coefficient $k_{v}$ was determined as 0.4 . The saturation potential value $\delta \Phi_{s}=158 \mathrm{kV}$ was determined based on Siscoe et al. (2002). Equations (6) and (7) give, for the case of 8 November 1998, 14:09:48 UT (when $B_{y}=0$ ), a polar cap potential drop of 58 kV , which is in good accordance with the KTH model result $\sim 58 \mathrm{kV}$ (see Table 2), as well as with the DMSP F13 ion drift observations. These values of the coefficients in Eqs. (6) and (7) correspond to an $8 \%$ ratio of the ionospheric transpolar potential drop to the potential drop across the open field line bundle in the solar wind. From an analysis of the polar cap potential drop dependent on the IMF, Reiff et al. (1981) estimated this ratio as $10-20 \%$. Kelley et al. (2003) determined the ratio of the dawn-dusk electric field measured by ground-based radars at the equatorial ionosphere to the interplanetary electric field registered by ACE to be $7 \%$.

### 2.4 Event of 11 February 1999

In Fig. 11 we show magnetic field data from ACE at L1. IMF GSM components are plotted for 11 February 1999, as a function of corrected universal time; here the correction is about 1 h . The thick vertical line marks the time when Polar UVI shows a TPA aligned along the noon-midnight meridian in the Northern Hemisphere. The three thin vertical lines mark the time when DMSP F13 reaches highest latitudes over the Northern Hemisphere. The thick horizontal line at the top denotes the time period when UVI data are available.

ACE plasma measurements (not shown) indicate that during the time of the IMF $B_{y}$ change, solar wind ion density is about $30 \mathrm{~cm}^{-3}$ and solar wind velocity is about $430 \mathrm{~km} / \mathrm{s}$.

The event studied (see Fig. 12) corresponds to quiet time. $D_{s t}$ is 11 nT and $A L$ is $9.2,34.6$, and 21.8 nT , respectively, for the three instants modelled. The model polar cap magnetic flux is about 420 MWb . Similar to Fig. 9, both auroral oval boundaries and predicted TPA positions are shown.

In this event UVI observed a transpolar arc originating on the dawnside of the auroral oval and subsequently migrating across the entire polar region. Between approximately 19:15 and 20:00 UT (not shown) the dawnside of the auroral oval expands poleward, as expected for negative $B_{y}$ and positive $B_{z}$. Between approximately 20:00 and 21:30 UT, $B_{y}$ is weakly positive while changing sign from negative to positive. During this time the TPA appears to begin separating from the dawnside auroral oval and is clearly separated by 20:40 UT. As expected for positive $B_{y}$, the duskward migration of the TPA is accompanied by a poleward expansion of the duskside oval (21:40 UT). In this case an arc forms at the poleward edge of the duskside auroral oval and appears to separate by 22:00 UT. At 22:20 UT the dawnside originating TPA is aligned along the noon-midnight meridian, about 140 min after $B_{y}$ becomes positive/near zero and about an hour after $B_{y}$ becomes more strongly positive. At 22:40 UT the TPA is located just on the duskside of the noon-midnight meridian and is clearly attached to the dayside auroral oval. By 00:45 UT on 12 February 1999 the dawn originating TPA has merged with the duskside oval.

The top plot of Fig. 12 shows data from the first DMSP pass when IMF $B_{z}$ is northward, IMF $B_{y}$ is changing from negative to weakly positive and IMF $B_{x}$ is changing from positive to negative. DMSP F13 shows a spatially expanded


Fig. 10. Shown on the left, modelled field-aligned current patterns $\left(0.1 \mu \mathrm{~A} / \mathrm{m}^{2}\right.$ contour separation) for each of the DMSP passes on 8 November 1998; and on the right, the electrostatic potential patterns ( 3 kV contour separation) generated by the KTH model. Upward and downward FACs are shown in red and blue, respectively; positive potentials are shown in blue and negative in red. The black line denotes zero potential. See text for more details.
dawnside region of sunward flow that is bifurcated by small antisunward flow regions. The sunward flow associated with the TPA may be closed in the antisunward flow region equatorward, resulting in a local minimum in the positive potential region. This pattern is similar to the first pass of the first event (8 November 1998), except that the expansion is from the dawnside, as expected for negative $B_{y}$. The high-latitude convection pattern is dominated by sunward flow, some of which can be closed in the duskside antisunward flow region producing anticlockwise (positive potential) circulation in a cell located at highest latitudes on the duskside of the polar region.

By the time of the second DMSP pass, shown in the middle plot of Fig. 12, IMF $B_{y}$ has become more strongly positive. DMSP F13 passes at lower latitudes on the dayside than in the previous orbit. Convection is now dominated by clockwise circulation (negative potential), as expected for positive $B_{y}$. The TPA appears to have separated from the dawnside auroral oval and a second arc has formed at the poleward edge of the duskside auroral oval co-located with the sunward plasma flow.


Fig. 11. Shown are magnetic field data from the ACE satellite which orbits the L1 Lagrange point about $200 R_{E}$ sunward of the Earth. IMF GSM components are plotted for 11 February 1999, as a function of corrected universal time (UT plus the estimated propagation time from the satellite to $\operatorname{GSM} X=0$ ); about 1 h . The thickest vertical line marks the time when the TPA is aligned along the noonmidnight meridian. The thick horizontal line at the top denotes the time period when UVI data are available.

By the last DMSP pass for this event (bottom plot of Fig. 12), IMF $B_{z}$ is still positive and $B_{y}$ has been positive for about 3 h . The dawnside originating TPA has migrated to the duskside and faded. DMSP F13 is located at lower magnetic latitudes than in the previous pass, passing again through the poleward edge of the dayside auroral oval. Spatially expanded duskside sunward flow can be closed in a strong antisunward flow region, resulting in a large clockwise circulating (negative potential) cell dominating the dayside region. The right-hand column in Fig. 12 shows the convection patterns on open field lines projected using the Paraboloid Model.

Figure 13 shows, on the left, model field-aligned current distributions for each of the DMSP passes on 11 February 1999, and on the right, the electrostatic potential patterns generated by the KTH model. Upward and downward FACs are shown in red and blue, respectively, and positive potentials are shown in blue and negative in red. The black line denotes zero potential. The TPA FACs reflect the dawn to dusk motion of the TPA. Table 3 lists the model input values for the FACs.

The maximum and minimum values of the electrostatic potentials are shown in Table 4. The last column shows the values of the polar cap potential drops in the Paraboloid Model, $\delta \Phi_{p c-\text { parab }}$, (see Sect. 2.5).

Table 3. Modelled field-aligned current values (MA) for 11 February 1999.

| Event | Dusk | Polar Region |  |  |  |  | Dawn |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | R2 $\downarrow$ | R1 $\uparrow$ | NBZ $\downarrow$ | TPA $\downarrow$ | TPA $\uparrow$ | NBZ $\uparrow$ | R1 $\downarrow$ | R2 $\uparrow$ |
|  |  |  |  |  |  |  |  |  |
|  |  | 0.52 | 0.01 | 0.02 |  | 0.50 | 0.50 |  |
| 11 February 1999-1 | 0.20 | 0.69 | 0.52 |  |  |  |  |  |
| 11 February 1999-2 | 0.25 | 0.64 | 0.63 | 0.10 | 0.23 | 0.60 | 0.55 | 0.10 |
| 11 February 1999-3 | 0.55 | 0.65 |  | 0.12 | 0.02 | 0.70 | 0.95 | 0.35 |

Table 4. Local potential extrema (kV).

| Event | Dusk | Noon-midnight <br> Meridian |  | Dawn | $\delta \Phi_{K T H}$ | $\delta \Phi_{\text {pc-parab }}$ |
| :--- | :--- | :--- | ---: | ---: | ---: | :---: |
| 11 February 1999-1 | -20 | +41 |  | +20 | 61 | 74 |
| 11 February 1999-2 | -17 | +29 | -53 | +5 | 82 | 67 |
| 11 February 1999-3 | -20 |  | -63 | +9 | 72 | 75 |

## 3 Discussion and conclusions

This paper addresses the class of high-latitude aurora that involves moving transpolar arcs forming theta aurora as they traverse the highest latitudes. Theta aurorae were first observed on a global scale by Frank et al. (1982) from Dynamics Explorer 1 images. Before that a multitude of localised observations of high-latitude aurora had been made (e.g. Mawson, 1916; Davis, 1960; Denholm, 1961; Denholm and Bond, 1961; Davis, 1963; Eather and Akasofu, 1969; Berkey et al., 1976; Lassen and Danielsen, 1978), but because of the limited field of view of imagers located on the ground or onboard low-altitude spacecraft, the global nature of some of these arcs was not recognised.

Valladares et al. (1994) performed a comprehensive statistical study of the occurrence of high-latitude arcs and their dependence on the IMF, based on all-sky images. They also investigated the motion of the arcs and found the same kind of IMF dependence of the direction of motion that has later been established for transpolar arcs (e.g. Cumnock et al., 1997), although many of the arcs in their study belonged to different classes of high-latitude aurora.

Several models have been developed that attempt to explain transpolar arcs (e.g. Chang et al., 1998; Newell et al., 1999; Kullen, 2000; Slinker et al., 2001; Kullen and Janhunen, 2004; Naehr and Toffoletto, 2004; and references therein), although none of them producs arcs that reach the dayside oval. Others (e.g. Maynard et al., 2003) address additional types of auroral arcs at high latitudes during northward IMF. When trying to relate the occurrence of high-latitude auroral arcs, the corresponding magnetospheric topology, and the physical mechanisms causing them, to models and simulations, we must carefully consider the domain of validity of each model. Whereas some features may
be common to the different types of arcs, it is certainly not a valid assumption that all features are common. For example, Maynard et al. (2003), relate midnight originating Sunaligned arcs to high-pressure channels in the distant plasma sheet. Whereas their results are certainly interesting in relation to midnight originating arcs, their applicability to the class of arcs that we are addressing is not at all clear.
In the spherical model it was shown that when $B_{y}$ changes sign, the line dividing the two polar convection cells and the corresponding auroral emissions, aligned along the noonmidnight meridian, should drift in either the dawn or dusk direction. When $B_{y}$ changes from negative to positive (positive to negative) it moves from dawn to dusk (from dusk to dawn), in good agreement with our observations and also with earlier reports (e.g. Cumnock et al., 1997, 2002; Cumnock and Blomberg, 2004).

In the Paraboloid model, in contrast to the Spherical model, the reconnection efficiency coefficients are different for the parallel and orthogonal components of the IMF, and both of them can be calculated self-consistently from the magnetosheath plasma flow solution (see Alexeev et al. (2003) for a thorough explanation). We use both of the magnetospheric models because one of them (the spherical) enables a simple and clear explanation of the TPA mechanism, whereas the other one (the paraboloid) gives quantitative results for ionospheric plasma convection patterns and auroral oval location that can be compared with the KTH model and satellite observations.

The TPA (associated with closed field lines) originates as part of the dawn or dusk side auroral oval. As it moves to higher latitudes it is surrounded by regions void of ions and filled with polar rain electrons (associated with open field lines). The TPA then continues to move across the polar region and becomes part of the opposite oval from where it


Fig. 12. Left: Data shown from three DMSP passes on 11 February 1999 (19:46-20:06, 21:29-21:49, and 23:10-23:30 UT) that occur during the Polar UVI data period. DMSP F13 horizontal plasma flows, perpendicular to the satellite track are plotted over a UV image taken at the time when F 13 is at highest magnetic latitudes. Right: For the same 3 times are shown the model calculations of the polar cap boundary, auroral oval, and polar cap convection generated by solar wind electric field, all derived from the Paraboloid Model. The model parameters for each case were calculated from solar wind data and geomagnetic indices. See text for details.
originated. This separation implies a highly distorted and dynamic magnetotail configuration.

Model calculations give us the polar cap electric field potential drop as well as the parallel potential difference applied to the separatrices and the acceleration of the auroral particles which creates the TPA. The model results explain the correlation between TPA occurrence and the $B_{y}$ component of the IMF because the potential drop on the separatrix, $\delta \Phi$, is proportional to $B_{y}$. They support the observed TPA motion from dawn to dusk or opposite with the change in sign of IMF $B_{y}$. In accordance with observations, the TPA region is collocated with sunward ionospheric convective flow. Additional study is needed to explain why the model gives a smaller polar cap size than the size of the visible dark area in the polar region. It is not yet clear what the magnetospheric field feature is that corresponds to the poleward boundary of the auroral oval. Also, the model does not account for the existence of a TPA when IMF $B_{y}=0$.


Fig. 13. Shown on the left, modelled field-aligned current patterns $\left(0.1 \mu \mathrm{~A} / \mathrm{m}^{2}\right.$ contour separation) for each of the DMSP passes on 11 February 1999; and on the right, the electrostatic potential patterns ( 3 kV contour separation) generated by the KTH model. Upward and downward FACs are shown in red and blue, respectively; positive potentials are shown in blue and negative in red. The black line denotes zero potential. See text for more details.

We suggest that the auroral emissions in transpolar auroral arcs are caused, on a global scale, by the potential difference that exists between the northern and southern magnetic null points for IMF $B_{y} \neq 0$. On the local scale, for the potential difference along a particular magnetic field line traversing the transpolar arc the acceleration potential is determined by the electric potential at the ionospheric footpoint of each field line and the fact that all boundary field lines share a common potential at their magnetospheric end. Thus, we should expect auroral emissions at the boundary between the two cells in the open field line regions in the polar caps for northward IMF. The emission region should be associated with reverse convection.

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