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The role of vibrationally excited nitrogen and oxygen in the ionosphere over Millstone Hill during 16–23 March, 1990

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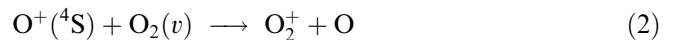
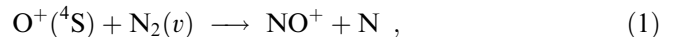
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Abstract. We present a comparison of the observed behavior of the F region ionosphere over Millstone Hill during the geomagnetically quiet and storm period on 16–23 March, 1990, with numerical model calculations from the time-dependent mathematical model of the Earth's ionosphere and plasmasphere. The effects of vibrationally excited $N_2(v)$ and $O_2(v)$ on the electron density and temperature are studied using the $N_2(v)$ and $O_2(v)$ Boltzmann and non-Boltzmann distribution assumptions. The deviations from the Boltzmann distribution for the first five vibrational levels of $N_2(v)$ and $O_2(v)$ were calculated. The present study suggests that these deviations are not significant at vibrational levels $v = 1$ and 2, and the calculated distributions of $N_2(v)$ and $O_2(v)$ are highly non-Boltzmann at vibrational levels $v > 2$. The $N_2(v)$ and $O_2(v)$ non-Boltzmann distribution assumption leads to the decrease of the calculated daytime NmF2 up to a factor of 1.44 (maximum value) in comparison with the $N_2(v)$ and $O_2(v)$ Boltzmann distribution assumption. The resulting effects of $N_2(v > 0)$ and $O_2(v > 0)$ on the NmF2 is the decrease of the calculated daytime NmF2 up to a factor of 2.8 (maximum value) for Boltzmann populations of $N_2(v)$ and $O_2(v)$ and up to a factor of 3.5 (maximum value) for non-Boltzmann populations of $N_2(v)$ and $O_2(v)$. This decrease in electron density results in the increase of the calculated daytime electron temperature up to about 1040–1410 K (maximum value) at the F2 peak altitude giving closer agreement between the measured and modeled electron temperatures. Both the daytime and nighttime densities are not reproduced by the model without $N_2(v > 0)$ and $O_2(v > 0)$, and inclusion of vibrationally excited N_2 and O_2 brings the model and data into better agreement. The effects of vibrationally excited O_2 and N_2 on the electron density and temperature are most pronounced during daytime.

Key words: Ionosphere (ion chemistry and composition; ionosphere-atmosphere interactions; ionospheric disturbances).

1 Introduction

The $O^+(^4S)$ ions that predominate in the ionospheric F2-region are lost in the reactions



with the loss rate

$$L = K[N_2] + \beta[O_2], \quad (3)$$

where $v = 0, 1, \dots$ is the number of the vibrational level of N_2 or O_2 , the effective rate coefficients of reactions (1), and (2) are determined as

$$K = \sum_{v=0}^{\infty} [N_2(v)]K_v/[N_2], \quad \beta = \sum_{v=0}^{\infty} [O_2(v)]\beta_v/[O_2], \quad (4)$$

K_v is the recombination rate coefficient of $O^+(^4S)$ ions with $N_2(v)$, β_v is the recombination rate coefficient of $O^+(^4S)$ ions with $O_2(v)$, $[N_2] = \sum_{v=0}^{\infty} [N_2(v)]$, $[O_2] = \sum_{v=0}^{\infty} [O_2(v)]$, $[N_2(v)]$ and $[O_2(v)]$ are the number densities of N_2 and O_2 at the v -th vibrational level.

Schmeltekopf *et al.* (1968) measured $K(T_v)$ over the vibrational temperature range 300–6000 K, and found the K_v/K_0 ratios from the measured $K(T_v)$ for $T_n = T_i = 300$ K where T_v is the vibrational temperature of N_2 , T_n is the neutral temperature, and T_i is the ion temperature. The fundamental results of Schmeltekopf *et al.* (1968) were confirmed by Ferguson *et al.* (1984). The measurements of K were given by Hierl *et al.* (1997) over the temperature range 300–1600 K for $T_n = T_i = T_v$. These results confirm the observations of Schmeltekopf *et al.* (1968), and show for the first time that the translation temperature dependencies of K_v are similar to K_0 .

In an earlier study, Richards *et al.* (1994) and Pavlov and Buonsanto (1997) compared the calculated electron densities and temperatures with the data for the 16–23 March, 1990, geomagnetic storm (Buonsanto *et al.*, 1992). Richards *et al.* (1994) and Pavlov and Buonsanto (1997) evaluated the effects of $N_2(v > 0)$ on the peak electron densities, NmF2, as about factors of 2–4 reductions in the daytime NmF2. Pavlov and Buonsanto (1997) found that the calculated distribution is highly non-Boltzmann at vibrational levels $v > 2$, and the Boltzmann distribution assumption results in the increase of 10–30% in calculated NmF2 during the storm-time periods. However, the calculations of Pavlov and Buonsanto (1997) were based on the translation temperature dependencies of K_v given by the theory of Van Zandt and O'Malley (1973), while Pavlov (1998b) and Pavlov *et al.* (1999) found that the $K(T_n)$ prediction of the Van Zandt and O'Malley (1973) theory do not agree with the recent measurements of $K(T_n)$ given by Hierl *et al.* (1997). In this study we examine the effects of $N_2(v)$, and the difference between Boltzmann and non-Boltzmann distributions of $N_2(v)$ on the electron density and temperature during the undisturbed and storm period of 16–23 March, 1990, by the use of the K_v/K_0 ratios given by Hierl *et al.* (1997), and the value of K_0 measured by Albritton *et al.* (1977).

Hierl *et al.* (1997) found a big difference between the high temperature flowing afterglow and drift tube measurements (McFarland *et al.*, 1973; Albritton *et al.*, 1977) of β as a result of the input of the reactions between the vibrationally excited O_2 and $O^+(^4S)$, and determined the dependence of β on the O_2 vibrational temperature, T_{vib} , over the temperature range 300–1800 for $T_{vib} = T_n = T_i$. The flowing afterglow measurements of β given by Hierl *et al.* (1997) were used by Pavlov (1998b) to invert the data to give the rate coefficients β_v for the various vibrational levels of $O_2(v > 0)$ for the model of the Boltzmann distribution of vibrationally excited molecular oxygen.

The difference between the measurements of β given by Hierl *et al.* (1997) and the scaled drift tube data is decreased with the decrease in T_n . As a result, as for $N_2(v)$, the effects of the vibrational excitation of O_2 are expected to be more important during solar maximum than at solar minimum. First studies of the $O_2(v > 0)$ effects on NmF2 for the 6–12 April, 1990, storm (Pavlov, 1998b) and the 5–11 June, 1991, storm (Pavlov *et al.*, 1999) found that enhanced vibrational excitation of O_2 leads up to the 40% decrease in the calculated NmF2 at solar maximum. Here we study the effects of $O_2(v > 0)$ on NmF2 for the 16–23 March, 1990, geomagnetic storm which was at high solar-activity conditions (Buonsanto *et al.*, 1992). We examine also the effects of Boltzmann and non-Boltzmann distributions of $O_2(v)$ on the electron density and temperature during the March 1990 geomagnetic storm. We compare our results with previous modeling results given by Richards *et al.* (1994) and Pavlov and Buonsanto (1997) for the 16–23 March, 1990, period where the effects of $O_2(v > 0)$ on the electron density and temperature were not taken into account.

We also study the electron energy balance of the ionosphere at Millstone Hill during 16–23 March, 1990. The anomalous nighttime electron temperature events were observed over less than a third of the time studied in the fall and spring months over Millstone Hill (Garner *et al.*, 1994), and unusually high electron temperatures in the nighttime ionosphere over Millstone Hill were also observed during the periods 20–23 March, 1990, (Buonsanto *et al.*, 1992). The existence of anomalous nighttime temperature events in the fall and spring months argues against a simple relationship of these anomalous temperature enhancements to conjugate photoelectrons. The physical origin of these temperature events is still unclear. Following Balan *et al.* (1996) and Richards and Khazanov (1997), we believe that there is an additional heating rate of the electron in the plasmasphere, and we evaluate the value of this additional heating rate so that an agreement between the measured and modeled electron temperature is obtained during the studied period.

The thermal electron impact excitation of the fine structure levels of the 3P ground state of atomic oxygen is presently believed to be one of the dominant electron cooling processes in the F region of the ionosphere (Richards *et al.*, 1986; Richards and Khazanov, 1997). Pavlov (1998a, c) and Pavlov and Berrington (1999) have revised and evaluated the electron cooling rates by vibrational and rotational excitation of N_2 and O_2 , and the electron cooling rate by electron impact excitation of fine-structure levels of atomic oxygen. Pavlov and Berrington (1999) found that the role of the cooling rate of thermal electrons by electron impact excitation of fine structure levels of atomic oxygen is not significant at the F2-peak altitudes of the ionosphere for the geomagnetically quiet and disturbed period on 6–12 April, 1990, above Millstone Hill, and the energy exchange between the electron and ion gases and the electron cooling rates by vibrational excitation of O_2 and N_2 are the largest cooling rates above 160 km. The new analytical expressions for cooling rates given by Pavlov (1998a, c) and Pavlov and Berrington (1999) are applied to perform an examination the role of these electron cooling rates in the thermal balance of the ionosphere during the undisturbed and storm period of 16–23 March, 1990.

2 Theoretical model

The model used is the IZMIRAN model that we have steadily developed over the years (Pavlov, 1997; 1998a, b, c; Pavlov *et al.*, 1999; Pavlov and Berrington, 1999). Schematic illustration of the major input and output elements of the model code, and the flowchart of the solution are shown in Fig. 1. It is a one dimensional model that uses a tilted dipole approximation to the Earth's magnetic field and takes into account the offset between the geographic and geomagnetic axes. In the model, coupled time dependent equations of continuity and energy balance, and diffusion equations for electrons, and $O^+(^4S)$, H^+ , and He^+ ions are solved along a centered-dipole magnetic field line for the concentra-

THE MODEL OF THE THERMAL PLASMA IN THE IONOSPHERE AND PLASMASPHERE
 INPUT: LT, DATE, LATITUDE, LONGITUDE, 3 HOUR Ap INDICES, F10.7, <F10.7>
 OUTPUT: ELECTRON AND ION DENSITIES AND TEMPERATURES, $[N_2(v=1-5)]$, $[O_2(v=1-5)]$, $[O(^1D)]$

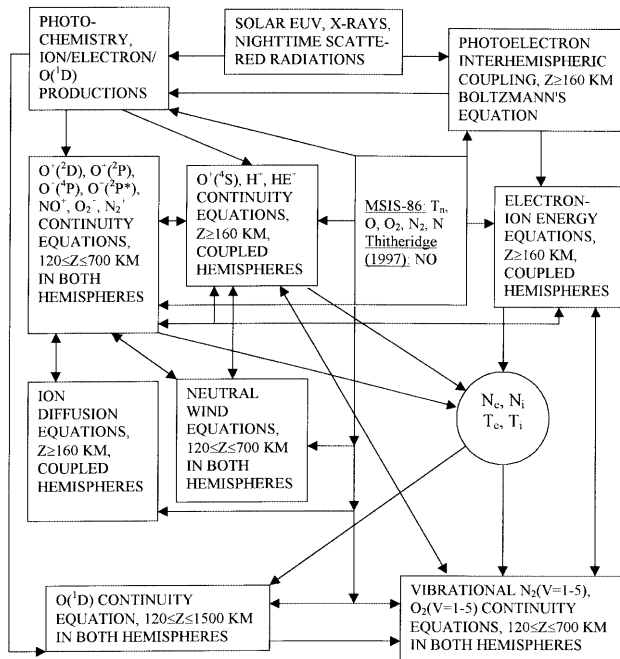


Fig. 1. Schematic illustration of the major input and output elements of the IZMIRAN model code and the flowchart of the solution

tions, temperatures, and field-aligned diffusion velocities of ions and electrons from a base altitude (160 km) in the Northern Hemisphere through the plasmasphere to the same base altitude in the Southern Hemisphere. Electron heating due to photoelectrons is provided by a solution of the Boltzmann equation for photoelectron flux. In the altitude range 120–700 km in the Northern and Southern Hemispheres the model solves time dependent continuity equations for $O^+(^2D)$, $O^+(^2P)$, NO^+ , O_2^+ , N_2^+ , $N_2(v=1, \dots, 5)$, and $O_2(v=1, \dots, 5)$, and vibrationally excited nitrogen and oxygen quanta $\alpha = \sum_v v[N_2(v)]/N_2$ and $\delta = \sum_v v[O_2(v)]/[O_2]$. An additional production of $O^+(^4S)$, $O^+(^2D)$, and $O^+(^2P)$ ions is that described by Pavlov (1998b), and obtained in the IZMIRAN model by inclusion of $O^+(^4S)$, and $O^+(^2P^*)$ ions. The model calculates $[O(^1D)]$ from a time-dependent continuity equation in the region between 120 and 1500 km in altitude in both hemispheres. The diffusion of ions and excited species are considered in continuity equations for NO^+ , O_2^+ , $O_2(v)$, $N_2(v)$, and $O(^1D)$, while densities of $O^+(^2D)$, $O^+(^2P)$, and N_2^+ are obtained from local chemical equilibrium. The updated IZMIRAN model uses the dissociative recombination rate coefficient for N_2^+ ions measured by Peterson *et al.* (1998). The revised electron cooling rates by vibrational and rotational excitation of O_2 and N_2 , and by electron impact excitation of fine structure levels of atomic oxygen given by Pavlov (1998a, c) and Pavlov and Berrington (1999) are included in the IZMIRAN model.

The full IZMIRAN model solves time dependent continuity equations for number densities $N_2(v=$

$1, \dots, 5)$ and $O_2(v=1, \dots, 5)$, and includes the option to use the model of the Boltzmann distribution of vibrationally excited molecular nitrogen and oxygen as

$$[N_2(v)]_B = [N_2(0)] \exp(-v E_1 T_v^{-1}), \quad (5)$$

$$[O_2(v)]_B = [O_2(0)] \exp(-v E'_1 T_{vib}^{-1}), \quad (6)$$

where $E_1 = 3353$ K and $E'_1 = 2239$ K are the energies of the first vibrational levels of N_2 and O_2 (Radzig and Smirnov, 1980), $[N_2(0)] = [N_2]\{1 - \exp(-E_1 T_v^{-1})\}$, $[O_2(0)] = [O_2]\{1 - \exp(-E'_1 T_{vib}^{-1})\}$, the values of the vibrational temperatures, T_v and T_{vib} , of N_2 and O_2 are calculated by solving the time-dependent continuity equations for vibrationally excited nitrogen and oxygen quanta given by Pavlov (1997, 1998b), and using the relationships $T_v = -E_1/\ln[\alpha(1+\alpha)^{-1}]$ and $T_{vib} = -E'_1/\ln[\delta(1+\delta)^{-1}]$ (see Pavlov and Buonsanto, 1997; Pavlov, 1997, 1998b).

The heating rate of the electron gas by photoelectrons is calculated along a centered – dipole magnetic field line using the numerical method of Krinberg and Tachilin (1984) for the determination of the photoelectron fluxes within a plasmaspheric field tube on the same field line grid that is used in solving for the temperatures. The updated IZMIRAN model solves the Boltzmann equation for photoelectron flux using the updated elastic and inelastic crosssections of the neutral components of the atmosphere. For O, the elastic cross section employed in the electron transport code was drawn from the work of Williams and Allen (1989) for energies below 8.7 eV, and, above 8.7 eV, we have adopted the elastic cross section of Joshipura and Patel (1993). The N_2 elastic cross section of Iticawa (1994) for electron energies is used in our model. The O and N_2 inelastic cross sections are given by Majed and Strickland (1997), and we employ these cross sections with some modification for N_2 . The N_2 vibrational excitation cross sections used by Majed and Strickland (1997) in calculations of the N_2 inelastic cross section were replaced by the N_2 vibrational excitation cross sections of Robertson *et al.* (1997) for vibrational levels $v = 1$ and 2, and those of Schulz (1976) for $v = 3-10$ with the normalization factor of 0.7 (see details in Pavlov 1998a). For O_2 , the elastic and inelastic cross sections are taken from Kanic *et al.* (1993).

The model uses the recombination rate coefficient of $O^+(^4S)$ ions with unexcited $N_2(0)$ and $O_2(0)$ (Albritton *et al.*, 1977; St.-Maurice and Torr, 1978) and vibrationally excited $N_2(v)$ and $O_2(v)$ (Schmeltekopf *et al.*, 1968; Hierl *et al.*, 1997; Pavlov, 1998b) as described in detail by Pavlov (1998b) and Pavlov *et al.* (1999). The energy balance equations for ions of the model consider the perpendicular component, E_\perp , of the electric field with respect to the geomagnetic field and the rate coefficients of such important ionospheric processes as the reactions of $O^+(^4S)$ with N_2 and O_2 , and N_2^+ with O_2 which depend on effective temperatures which are functions of the ion temperature, the neutral temperature and E_\perp (Pavlov, 1997, 1998b). The measured value of E_\perp can be used as an input parameter for our theoretical model.

The key inputs to the IZMIRAN model are the concentrations and temperature of the neutral constituents, the solar EUV fluxes, and the plasma drift velocity. The neutral temperature and densities are supplied by the MSIS-86 model of Hedin (1987) using 3-h A_p indices. To calculate the density of NO the model given by Titheridge (1997) is used. The solar EUV fluxes are supplied by the EUV97 model (Tobiska and Eparvier, 1998) for the model calculations. At night our model includes the neutral ionization by scattered solar 121.6, 102.6 and 58.4 nm fluxes (Pavlov, 1997). In the Northern Hemisphere instead of calculating thermospheric wind components by solving the momentum equations, the model calculates an equivalent neutral wind from the hmF2 measurements using the modified method of Richards (1991) described by Pavlov and Buonsanto (1997). For the Southern Hemisphere where we do not have observed hmF2 momentum equations for the horizontal components of the thermospheric wind are calculated in the altitude range 120–700 km to derive an equivalent plasma drift velocity, as described by Pavlov (1997).

4 Undisturbed period and storms of 16–23 March, 1990

The undisturbed conditions of 16–17 March, 1990, (A_p between 3 and 8) and the 18–23 March, 1990, magnetic storms (A_p between 14 and 73) were periods which occurred at solar maximum when the 10.7 solar flux varied between 180 on March 16 and 247 on March 23.

During the 16–23 March, 1990, period two geomagnetic storms took place with a gradual commencement time near 04:00 UT on March 18 (a minor storm) and with a sudden commencement time near 22:45 UT on March 20 (a major storm). The measured electron densities and temperatures, and the perpendicular electric fields (with respect to the magnetic field) used were taken by the incoherent scatter radar at Millstone Hill, Massachusetts (Buonsanto *et al.*, 1992).

4.1 Effects of vibrational excited oxygen and nitrogen on electron density and temperature

Figure 2 displays the measured (crosses) and calculated (lines) NmF2 (bottom panel), hmF2 (middle panel), and the electron temperature, T_{em} , at the F2 peak altitude (top panel) above Millstone Hill for the magnetically quiet and disturbed period 16–23 March, 1990. Solid lines show the IZMIRAN model results when the Boltzmann distribution of $N_2(v)$ and $O_2(v)$ is used. Dotted lines represent the results obtained from the IZMIRAN model with effects of $N_2(v > 0)$ and $O_2(v > 0)$ on the $O^+(^4S)$ loss rate and the heating rate of electrons due to the de-excitation reactions of vibrationally excited N_2 and O_2 using the non-Boltzmann populations of the first five vibrational levels of $N_2(v)$ and $O_2(v)$. The values of the deviations of $[N_2(v)]$ from $[N_2(v)]_B$ and $[O_2(v)]$ from $[O_2(v)]_B$ will be discussed later.

It can be seen from Fig. 2 that the modeled electron densities and temperatures are in reasonable accord with

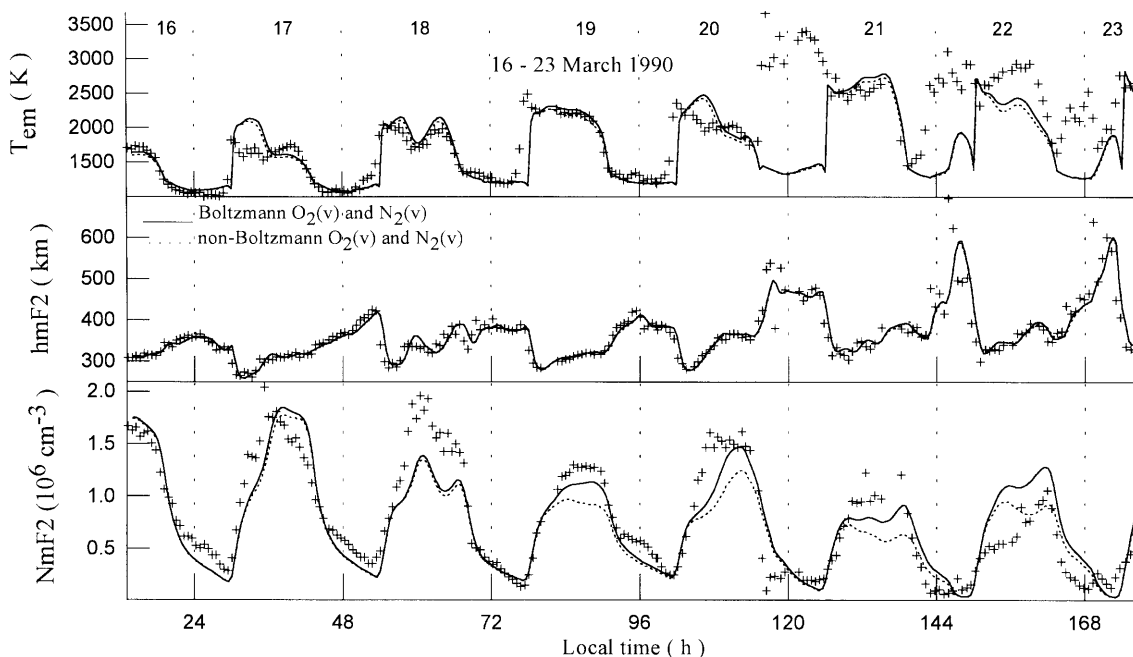


Fig. 2. The measured (crosses) and calculated (lines) NmF2 (bottom panel), hmF2 (middle panel), and the electron temperature, T_{em} , at the F2 peak altitude (top panel) above Millstone Hill for the magnetically quiet and disturbed period 16–23 March, 1990. Solid lines show the IZMIRAN model results when the Boltzmann populations of $N_2(v)$ and $O_2(v)$ are used. Dotted lines represent the

results obtained from the IZMIRAN model with effects of $N_2(v > 0)$ and $O_2(v > 0)$ on the $O^+(^4S)$ loss rate and the heating rate of electrons due to the de-excitation reactions of vibrationally excited molecular nitrogen and oxygen using the non-Boltzmann populations of the first five vibrational levels of $N_2(v)$ and $O_2(v)$. The local time start is 13:00

the observed values if the Boltzmann vibrational N_2 and O_2 distribution assumptions are used. It should be noted that the model results with the vibrational states of $N_2(v)$ and $O_2(v)$ included do not always fit the data. These discrepancies are probably due to the uncertainties in the model inputs, such as a possible inability of the MSIS-86 model to accurately predict the thermospheric response to this storm above Millstone Hill, and uncertainties in EUV fluxes, rate coefficients, and the flow of ionization between the ionosphere and plasmasphere, and possible horizontal divergence of the flux of ionization above the station.

The deviations of $[N_2(v)]$ from $[N_2(v)]_B$ and $[O_2(v)]$ from $[O_2(v)]_B$ in the F region of the ionosphere affect the recombination rate of $O^+(^4S)$ ions and the heating rate of electrons due to the de-excitation reactions of vibrationally excited molecular nitrogen and oxygen, and the result of these deviations is the difference between solid and dotted lines in Fig. 2. We found that the $N_2(v)$ and $[O_2(v)]$ Boltzmann distribution assumption leads to the increase of the calculated daytime NmF2 up to a factor of 1.44 and to the changes in T_{em} up to 686 K in comparison with NmF2 and T_{em} calculated by using of the non-Boltzmann vibrational distribution of N_2 and O_2 .

Our study shows the Boltzmann vibrational N_2 and O_2 distribution assumptions give better agreement between measured and modeled NmF2 and T_{em} than the non-Boltzmann vibrational distribution of N_2 and O_2 during 18–21 March. On 22 March only, the non-Boltzmann vibrational distribution model results agree better with the observations in comparison to the results from the model with the Boltzmann vibrational distribution of N_2 and O_2 . The Boltzmann and non-Boltzmann vibrational N_2 and O_2 distribution assumptions produce a comparable degree of agreement between modeled and measured electron density and temperature on 16 and 23 March.

The results of calculating $[N_2(v)]/[N_2(v)]_B$, $[O_2(v)]/[O_2(v)]_B$, T_{vib} , T_v , and T_n at hmF2 are presented in Fig. 3. The present study suggests that the deviations of $[N_2(v)]$ and $[O_2(v)]$ from the Boltzmann distributions of Eqs. (5) and (6) are not significant at vibrational levels $v < 3$ ($[N_2(1)]/[N_2(1)]_B = 0.72\text{--}1.07$, $[O_2(1)]/[O_2(1)]_B = 0.99\text{--}1.16$, $[N_2(2)]/[N_2(2)]_B = 0.88\text{--}1.46$, $[O_2(2)]/[O_2(2)]_B = 0.88\text{--}1.05$). The calculated distributions of $N_2(v)$ and $O_2(v)$ are highly non-Boltzmann at vibrational levels $v > 2$ ($[N_2(3)]/[N_2(3)]_B = 0.97\text{--}7.8$, $[N_2(4)]/[N_2(4)]_B = 0.9\text{--}49.0$, $[N_2(5)]/[N_2(5)]_B = 1.4\text{--}790$, $[O_2(3)]/[O_2(3)]_B = 0.59\text{--}1.00$, $[O_2(4)]/[O_2(4)]_B = 0.37\text{--}0.98$, $[O_2(5)]/[O_2(5)]_B = 0.23\text{--}0.99$). From the diurnal variations of the calculated vibrational and neutral temperatures shown in Fig. 3 it follows that $T_{vib} < T_n$ and $T_v < T_n$ are realized in the atmosphere for the nighttime periods where the production frequencies of $O_2(v)$ and $N_2(v)$ are low. This means that for these periods the populations of $O_2(v)$ or $N_2(v)$ are less than the populations for a Boltzmann distribution with temperature T_n . During daytime T_{vib} and T_v are larger than T_n due to the enhanced thermal excitation of O_2

and N_2 as a result of high thermal electron temperatures at F2-region altitudes. We found that $-50\text{ K} \leq T_{vib} - T_n \leq 358\text{ K}$ and $-99\text{ K} \leq T_v - T_n \leq 840\text{ K}$. The value of the vibrational temperature was not more than 1784 K for O_2 and 2334 K for N_2 . The calculations also showed that the O_2 and N_2 vibrational temperatures during the quiet periods are smaller than during the magnetic storm periods.

The excitation of N_2 and O_2 by thermal electrons provides the main contribution to the values of $O_2(v)$ and $N_2(v)$ vibrational excitations if the electron temperature is higher than about 1600–1800 K at F-region altitudes (Pavlov, 1988, 1997, 1998b; Pavlov and Namgaladze, 1988; Pavlov and Buonsanto, 1997). The values of $T_{vib} - T_n$ and $T_v - T_n$ increase with increasing the thermal electron production frequencies, $W(O_2)$ and $W(N_2)$, of the O_2 and N_2 vibrational quanta, correspondingly. Pavlov (1998a) found that the value of $W(N_2)$ increases with increasing T_e in the temperature range 300–6000 K, and due to this dependence, the value of T_v increases with increasing T_e . The value of $W(O_2)$ also increases with the increase of T_e (Pavlov, 1998c). However, unlike the dependence of $W(N_2)$ on T_e , this increase of $W(O_2)$ is small in the electron temperature range 2000–4000 K. As a result, $W(O_2) \approx \text{const. } N_e$, and this leads to $T_v > T_{vib}$.

Schmeltekopf *et al.* (1968) measured $K(T_v)$ over the vibrational temperature range 300–6000 K, and found the K_v/K_0 ratios from the measured $K(T_v)$ only for $T_n = T_i = 300\text{ K}$. The dependence of these rate coefficients on the neutral and ion temperatures was found for the first time by Hierl *et al.* (1997). The measurements of Hierl *et al.* (1997) have reduced the uncertainties in the temperature-dependent reaction rates for $O^+(^4S) + N_2(v > 0)$ and $O^+(^4S) + O_2(v > 0)$. Therefore, an accurate estimate of the role of $N_2(v > 0)$ and $O_2(v > 0)$ in the ionosphere can be made by comparing ionospheric model calculations with and without these species included.

Figure 4 shows the comparison between the measured (crosses) and calculated (lines) NmF2 (bottom panel), hmF2 (middle panel), and the electron temperature at the F2 peak altitude (top panel) above Millstone Hill for the magnetically quiet and disturbed period 16–23 March, 1990. Solid lines show the results obtained from the IZMIRAN model with effects of $N_2(v > 0)$ and $O_2(v > 0)$ on the $O^+(^4S)$ loss rate (see Eq. 3) using the Boltzmann populations of the first five vibrational levels of $N_2(v)$ and $O_2(v)$. Dotted lines represent the IZMIRAN model results when $N_2(v > 0)$ and $O_2(v > 0)$ are not included in the calculations of L . Dashed lines give the IZMIRAN model results when $O_2(v > 0)$ is included and $N_2(v > 0)$ is not included in calculations of L . Solid and dotted lines show the results obtained from the IZMIRAN model when the calculated Boltzmann populations of $N_2(v)$ and $O_2(v)$ are used in the heating rate of electrons due to the de-excitation reactions of $N_2(v)$ and $O_2(v)$.

As Fig. 4 shows, there is a large increase in the modeled NmF2 without the vibrationally excited nitrogen and oxygen. Both the daytime and nighttime densities are not reproduced by the model without $N_2(v > 0)$ and

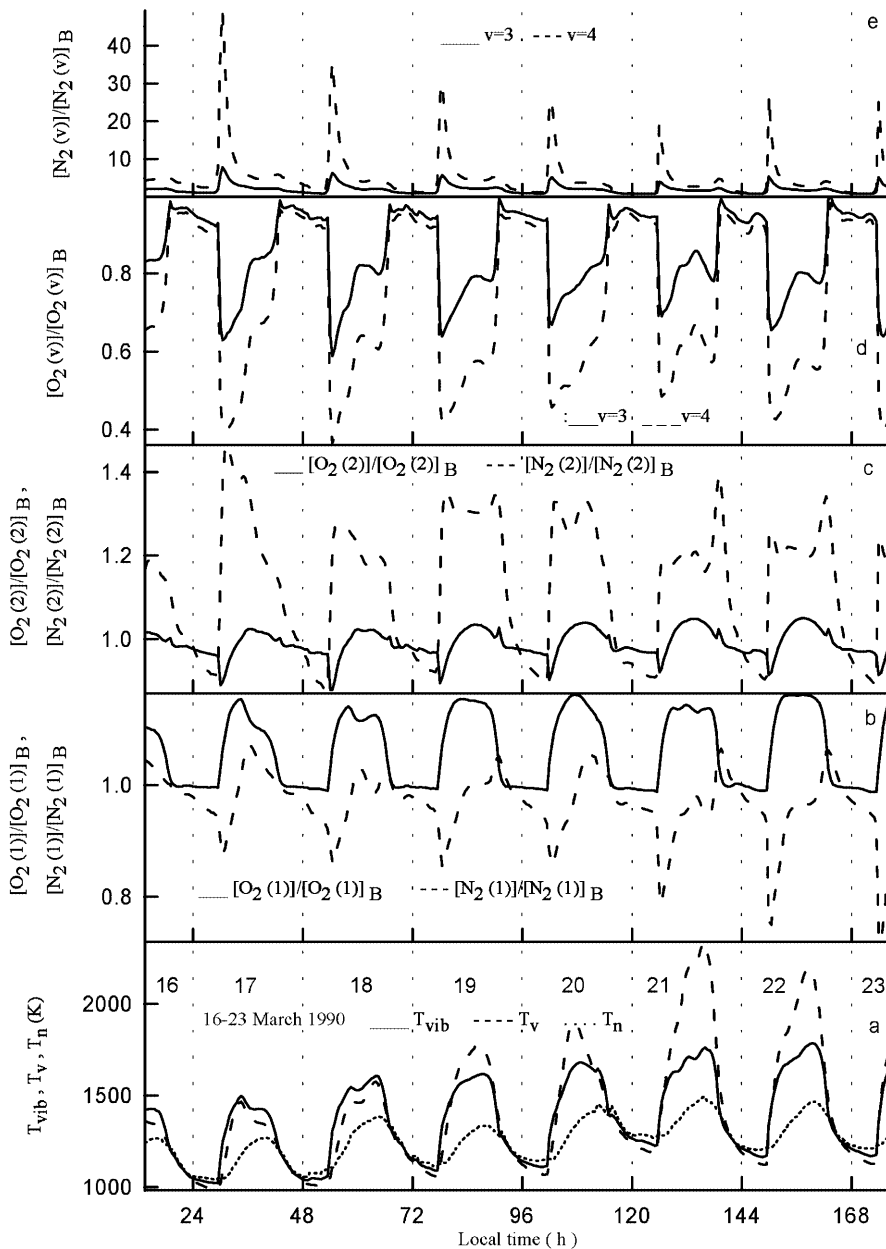


Fig. 3a-e. The time variations of the vibrational temperatures of $[N_2]$ and $[O_2]$, **a** and the neutral temperature, **b-e** and populations of the first five vibrational levels of $N_2(v = 1, 2, 3, \text{ and } 4)$ and $O_2(v = 1, 2, 3, \text{ and } 4)$ in comparison with the Boltzmann populations of Eqs. (5) and (6) during the 16–23 March, 1990, period at the F2 peak altitude. The *solid lines* show the modeled T_{vib} , $[O_2(1)]/[O_2(1)]_B$, $[O_2(2)]/[O_2(2)]_B$, $[O_2(3)]/[O_2(3)]_B$, and $[N_2(3)]/[N_2(3)]_B$. The *dashed lines* show the modeled T_v , $[N_2(1)]/[N_2(1)]_B$, $[N_2(2)]/[N_2(2)]_B$, $[N_2(4)]/[N_2(4)]_B$, and $[O_2(4)]/[O_2(4)]_B$. The *dotted line* shows the modeled T_n . The local time start is 13:00

$O_2(v > 0)$ in the loss rate of $O^+(^4S)$ ions, and inclusion of vibrationally excited N_2 and O_2 in L brings the model and data into better agreement. The comparison of solid and dashed lines in Fig. 4 shows that the increase in the $O^+ + N_2$ rate factor due to the vibrationally excited nitrogen leads to the decrease of the calculated daytime NmF2 up to a factor of 1.8. The comparison between dotted and dashed lines shows that the increase in the $O^+ + O_2$ loss rate due to vibrationally excited O_2 produces factors of 1.7 reductions in the daytime peak density. The resulting effect of $N_2(v > 0)$ and $O_2(v > 0)$ included in L on the NmF2 is the decrease of the calculated daytime NmF2 up to a factor of 2.8 for Boltzmann populations of $N_2(v)$ and $O_2(v)$, and up to a factor of 3.5 for non-Boltzmann populations of $N_2(v)$ and $O_2(v)$. The effects of vibrationally excited O_2 and N_2 on N_e are most pronounced during daytime.

The IZMIRAN model used was updated many times in comparison with the IZMIRAN model used by Pavlov and Buonsanto (1997). As a result, the discrepancies between the modeled and measured ionospheric parameters are less than those found by Pavlov and Buonsanto (1997).

Richards *et al.* (1994) compared observed values of NmF2, hmF2, and T_e at Millstone Hill with FLIP model results for the March 1990 storm. The FLIP model without $N_2(v)$ gives better agreement between the measured and modeled NmF2 on March 18–20 but worse agreement on March 21–23 than FLIP with $N_2(v)$ included. Although the FLIP and IZMIRAN models are similar in most respects, there are several differences between them (Pavlov *et al.*, 1999). We believe that the differences between the FLIP model used by Richards *et al.* (1994) and the IZMIRAN model in calculations of

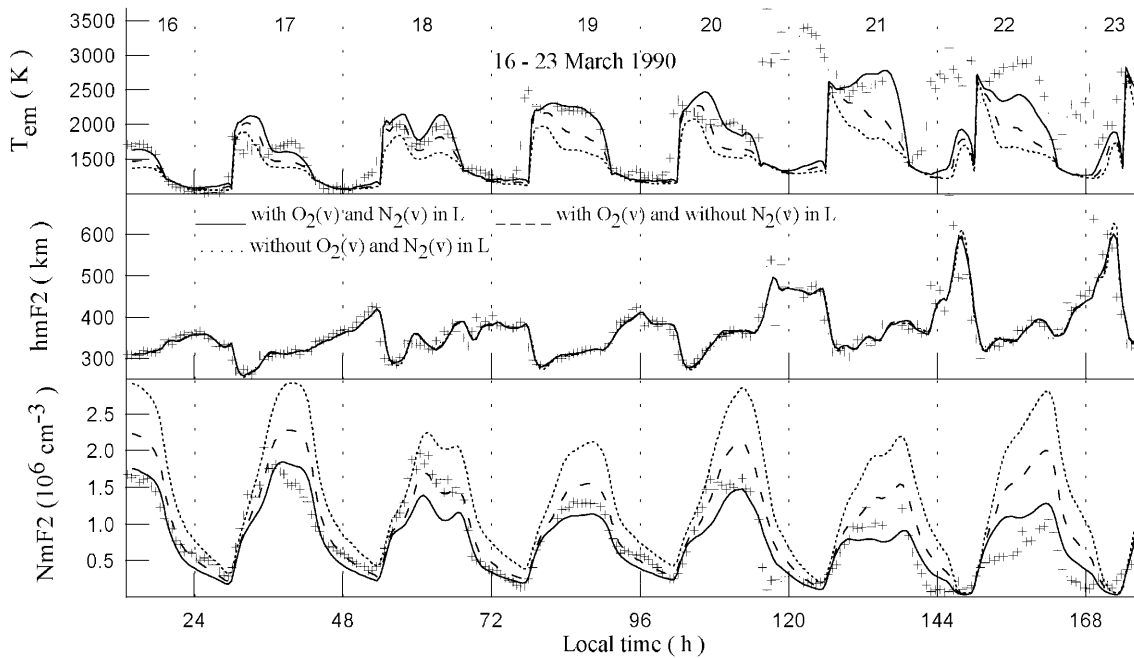


Fig. 4. Observed (crosses) and calculated (lines) NmF2 (bottom panel), hmF2 (middle panel), and the electron temperature, T_{em} , at the F2 peak altitude (top panel) above Millstone Hill for the magnetically quiet and disturbed period 16–23 March, 1990. Solid lines show the modeled results obtained with effects of $N_2(v > 0)$ and $O_2(v > 0)$ on the $O^+(^4S)$ loss rate, L , (see Eq. 3) using the Boltzmann populations of the first five vibrational levels of $N_2(v)$ and $O_2(v)$.

Dotted lines represent the IZMIRAN model results when $N_2(v > 0)$ and $O_2(v > 0)$ were not included in the calculations of L . Dashed lines give the IZMIRAN model results without effects of $N_2(v > 0)$ on L when $O_2(v > 0)$ was included in the calculations of L . The value of hmF2 from the IZMIRAN model is a fit to data using the modified method of Richards (1991) described by Pavlov and Buonsanto (1997) (see Sect. 2). The local time start is 13:00

the loss rate of $O^+(^4S)$ ions, cooling rate of thermal electrons, and the model of solar flux (see also Pavlov and Buonsanto, 1997) determine the differences between the IZMIRAN and FLIP model results for the March 1990 magnetic storm.

4.2 Electron temperature

The top panel of Fig. 4 shows the diurnal variations of the measured and modeled electron and ion temperatures at the F2-peak altitude. As can be seen, the effects of adding $N_2(v)$ and $O_2(v)$ on T_e are largest during the day, with increases in T_e accompanying the decreases in NmF2. We found that the resulting effect of $N_2(v > 0)$ and $O_2(v > 0)$ included in L on the electron temperature at the F2 peak altitude is the decrease of the calculated daytime electron temperature up to about 1040 K for Boltzmann populations of $N_2(v)$ and $O_2(v)$ and up to about 1410 K for non-Boltzmann populations of $N_2(v)$ and $O_2(v)$. The effects of vibrationally excited O_2 and N_2 on T_e are most pronounced during daytime.

It should be noted that the modeled electron temperature is very sensitive to the electron density, and, as a result, there is a large decrease in the modeled electron temperatures without the vibrationally excited nitrogen and oxygen in the model (see upper panel of Fig. 4). Including of vibrationally excited N_2 and O_2 in the loss rate of $O^+(^4S)$ ions which brings the measured and modeled electron densities into better agreements

tends to give close agreement between measured and modeled electron temperatures.

The relative magnitudes of the cooling rates are of particular interest for understanding the main processes that determine the electron temperature. We found that the energy exchange between electrons and ions, and the electron cooling rates by vibrational excitation of N_2 and O_2 are the dominant cooling channels above 180 km during daytime. We found that the contribution of the cooling of electrons by low-lying electronic excitation of $O_2(a^1\Delta_g)$ and $O_2(b^1\Sigma_g^+)$, by excitation of O to the 1D state, and by rotational excitation of O_2 can be neglected above 160 km altitude as they are not more than 1% of the total cooling rate during the quiet and geomagnetic storm period 16–23 March, 1990. The atomic oxygen fine structure cooling rate of thermal electrons is not the dominant electron cooling process in agreement with the conclusions of Pavlov and Berrington (1999).

During the period 16–23 March the agreement between the measured and modeled electron temperatures is good except for the nighttime periods 20–23 March when high electron temperatures were observed at F2 peak altitudes. A detailed statistical study of the nighttime electron temperature enhancements over Millstone Hill has been published by Garner *et al.* (1994), who found that the anomalous nighttime temperature events are observed over less than a third of the time studied in the fall and spring months. There is a close relationship between electron temperature and electron

density at night. However, Fig. 4 shows that even when the IZMIRAN model accurately reproduces the electron density, it does not always reproduce the observed electron temperature.

The IZMIRAN model solves the Boltzmann equation for photoelectron flux along a centered – dipole magnetic field line to calculate the heating rate of the electron gas by photoelectrons using the numerical method of Krinberg and Tachilin (1984). The energy lost by photoelectrons in heating the plasma in the plasmasphere is calculated using the analytical equation for the plasmaspheric transparency, $P(E)$, (Krinberg and Matafonov, 1978; Krinberg and Tachilin, 1984) that determines the probability of the magnetically trapped photoelectrons with an energy, E , of entering the magnetically conjugated ionosphere. The transparency depends mainly on a single parameter proportional to the Coulomb cross section and the total content of electrons in the plasmasphere magnetic flux tube (the transparency approaches unity as photoelectrons pass through the plasmasphere without significant absorption, and $P(E) = 0$ if photoelectrons are absorbed by the plasmasphere).

The disagreement between the measured and modeled electron temperature could be due to uncertainties of the IZMIRAN model in the amount of the energy deposited in the plasmasphere by ionospheric photoelectrons. However, changing the value of $P(E)$ we have found that the heating provided by trapped photoelectrons cannot account for the observed nighttime high electron temperatures at F2 peak altitudes during the 20–23 March period.

The possible additional sources of the electron gas heating in the plasmasphere, such as wave-particle interactions, which can cause increased photoelectron scattering, and Coulomb collisions between ring current ions and plasmaspheric electrons and ions could be the most plausible mechanisms to explain the observed electron temperature enhancements. The heating could also be caused by heated flux tubes drifting past Millstone Hill due to plasma convection. To model this transfer of plasma, caused by some plasmaspheric electric field (usually of magnetospheric origin), consideration of the perpendicular (with respect to the magnetic field) divergence contribution in the ion equations of continuity arising from perpendicular plasma gradients is needed, and a model of this electric field is required or must be created. The IZMIRAN model cannot take into account the drift of flux tubes because it is a one dimensional model. This is the reason of possible errors of the model.

As a result, following Pavlov (1996, 1997) and Richards and Khazanov (1997), we use a fitting approach. We assume that an additional heating rate, q , should be added to the normal photoelectron heating in the electron energy equation in the plasmasphere region above 5000 km along the magnetic field line to explain these anomalous electron temperature enhancements. We do not know the real time dependence of additional heating, and we can only evaluate the value of q from the comparison of the modeled and measured

electron temperatures. We found that good agreement between the measured and modeled nighttime electron temperatures is obtained if $q = 0.9 \text{ eV cm}^{-3} \text{ s}^{-1}$ from 20:54 UT on 20 March to 8:54 UT on 21 March, $q = 0.5 \text{ eV cm}^{-3} \text{ s}^{-1}$ from 23:54 UT on 21 March to 09:54 UT on 22 March, and $q = 0.7 \text{ eV cm}^{-3} \text{ s}^{-1}$ from 24:54 UT on 22 March to 03:54 UT on 23 March. The model electron heating due to photoelectrons is less than this required additional heating above 5000 km during the time periods with the additional heating in the model. The values of q used by the IZMIRAN model between 5000 km and 12077 km are less than the values of an equatorial high-altitude heat source found by Balan *et al.* (1996) in this altitude range.

5 Conclusions

The model results were compared to the Millstone Hill incoherent-scatter radar measurements of electron density and temperature for the geomagnetically quiet and disturbed period on 16–23 March, 1990. The model used is an enhanced and updated version of the IZMIRAN model we have steadily developed over the years. The updated model uses the revised electron cooling rates by vibrational and rotational excitation of O_2 and N_2 , and by electron impact excitation of fine structure levels of atomic oxygen given by Pavlov (1998a, c) and Pavlov and Berrington (1999) in calculations of the electron temperature, and the updated elastic and inelastic cross sections of the neutral components of the atmosphere to solve the Boltzmann equation for photoelectron fluxes.

The deviations from the Boltzmann distribution for the first five vibrational levels of N_2 and O_2 were calculated. The present study suggests that the deviations from the Boltzmann distribution are not significant at the first and second vibrational levels of N_2 and O_2 , and the calculated distributions of $\text{N}_2(v)$ and $\text{O}_2(v)$ are highly non-Boltzmann at vibrational levels $v > 2$. The calculations also showed that the O_2 and N_2 vibrational temperatures during the quiet periods are less than during the magnetic storm periods. During daytime the high vibrational temperatures stem from the enhanced thermal excitation of O_2 and N_2 as a result of high thermal electron temperatures at F2-region altitudes.

We found that the $\text{N}_2(v)$ and $\text{O}_2(v)$ Boltzmann distribution assumption leads to the increase of the calculated daytime NmF2 up to a factor of 1.44 and to the changes in T_{em} up to 686 K in comparison with NmF2 and T_{em} calculated by using of the non-Boltzmann vibrational distribution of N_2 . Our study shows that the Boltzmann vibrational $\text{N}_2(v)$ and $\text{O}_2(v)$ distribution assumption gives better agreement between measured and modeled NmF2 and T_{em} than the non-Boltzmann vibrational distribution of $\text{N}_2(v)$ and $\text{O}_2(v)$ during 18–21 March. On 22 March only, the $\text{N}_2(v)$ and $\text{O}_2(v)$ non-Boltzmann vibrational distribution model results agree better with the observations in comparison to the results from the IZMIRAN model with the $\text{N}_2(v)$ and $\text{O}_2(v)$ Boltzmann vibrational distribution. The

Boltzmann and non-Boltzmann vibrational N_2 and O_2 distribution assumptions produce a comparable degree of agreement between modeled and measured electron density and temperature on 16 and 23 March.

The resulting effect of $N_2(v > 0)$ and $O_2(v > 0)$ included in L on the NmF2 is the decrease of the calculated daytime NmF2 up to a factor of 2.8 for Boltzmann populations of $N_2(v)$ and $O_2(v)$ and up to a factor of 3.5 for non-Boltzmann populations of $N_2(v)$ and $O_2(v)$. The modeled electron temperature is very sensitive to the electron density, and this decrease in electron density results in the increase of the calculated daytime electron temperature up to about 1040–1410 K at the F2 peak altitude. Both the daytime and nighttime densities are not reproduced by the model without $N_2(v > 0)$ and $O_2(v > 0)$, and inclusion of vibrationally excited N_2 and O_2 brings the model and data into better agreement. The effects of vibrationally excited O_2 and N_2 on the electron density and temperature are most pronounced during daytime.

We have examined the thermal electron energy budget in the mid-latitude ionosphere at solar maximum in March 1990 and evaluated the value of the additional heating rate that should be added to the normal photoelectron heating in the electron energy equation in the plasmasphere region above 5000 km along the magnetic field line to explain the anomalous electron temperature enhancements during the nighttime periods 20–23 March, 1990. This additional heat source of electrons in the plasmasphere might arise from wave-particle interactions and Coulomb collisions between ring current ions and plasmaspheric electrons and ions. The heating could also be caused by heated flux tubes drifting past Millstone Hill.

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