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STATISTICAL PROPERTIES OF LINE CENTROID VELOCITIES AND CENTROID VELOCITY INCREMENTS IN COMPRESSIBLE TURBULENCE

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ABSTRACT

studying the intermittency in the interstellar medium, as an alternative to the line-shape approach. scale, non-Gaussian PDFs are observed in some cases. However, this is far from being the rule, and most of the distributions show relatively minor deviations from a Gaussian. By contrast, PDFs of cen-We have calculated probability density functions (PDFs) of centroid velocities and centroid velocity increments of line profiles computed from the output of a 512³ simulation of compressible turbulence. Subject headings: hydrodynamics — ISM: clouds vorticity in the flow and thus appear related to the phenomenon of intermittency. Investigations of PDFs of centroid velocity increments in non-star-forming regions thus seem a promising avenue for troid velocity increments clearly show non-Gaussian wings that are associated with regions of increased The PDFs of centroid velocities calculated over the whole data cube are roughly Gaussian. On a smaller ISM: kinematics and dynamics — turbulence

1. INTRODUCTION

son between the molecular line profiles of non-star-forming dense molecular clouds and those calculated from the output of a 512³ hydrodynamic code for compressible turbulence computed by Porter, Pouquet, & Woodward existence of regions of intermittent turbulent activity. In a subsequent study, Falgarone et al. (1994) made a compariclouds. One of the approaches for study of turbulence in the also, that non-Gaussian line profiles can be produced simply from a random velocity field with a Kolmogorov level that is weak compared to the contribution of the bulk (1994). Falgarone et al. (1994) found that the vorticity peaks nature of the gas flow within molecular clouds and of the resent a direct observational signature of the turbulent tive regions without associated star formation activity rep-They argued that the non-Gaussian CO line wings in inaclar line profiles as proposed by Falgarone & Phillips (1990) interstellar medium is the analysis of the shapes of molecuimportant role in the dynamics of interstellar molecular of the flow. Dubinski, Narayan, & Phillips (1995) showed features and wings of the line profiles, but at an intensity ascribed to intermittency contribute to the non-Gaussian There is considerable evidence that turbulence plays an

Turbulent activity and dissipation are known, from flow experiments and numerical simulations, to be highly concentrated in space and time. Finding the small regions undergoing such an intermittent activity in the interstellar medium might bring important clues to the understanding of its dynamical evolution. Our knowledge of the interstellar medium relies on observations that provide only average values of its physical properties. These average properties are not necessarily representative of the values of the gas characteristics (temperature, density, etc.) that are of relevance in describing the physical processes and the evolution of the medium. Indeed, the fluctuations of some properties can be so large that the average value provides inadequate information. For instance, a very rich and specific chemistry can be driven in atomic interstellar clouds in

the small regions transiently heated by intermittent turbulent dissipation (Falgarone & Puget 1995; Falgarone, Pineau des Forêts, & Roueff 1995). Intermittency also locally affects the relative velocities and possibly the size distribution of very small dust particles and large molecules. These changes, in turn, modify the thermal local properties of the gas, and may be the seed of major changes in the subsequent evolution of turbulent clouds.

and numerical simulations of incompressible turbulence of velocity increments and derivatives found in experiments often nearly exponential wings, similar to those in the PDFs imately Gaussian, most of them exhibit relatively centroid velocities in several star-forming molecular clouds. They concluded that, while some of the PDFs are approx-In a recent observational study, Miesch & Scalo (1995) analyzed probability density functions (PDFs) of the ¹³CO higher line moments are difficult from the observational but intermittency can probably be better found in a velocity-increment study, so centroid velocity increments increments. Falgarone & Phillips (1990) studied line wings moments and for differential measurements such as velocity is known that the effects are greater for the higher line of Porter et al. (1994). It is interesting to try to find improved ways to isolate the signatures of intermittency. It centroid velocity increments based on the simulation results here the statistical properties of the centroid velocity and evaluate the Miesch & Scalo method and results, we study the line-of-sight centroid velocity in turbulent flows, to help simulations considered the characteristics of the PDFs of Since none of the existing theoretical studies or numerical with very high signal-to-noise ratio. viewpoint, since they require mapping of extended regions provide a new window on the effect. Studies of

2. ANALYSIS

Our study of the statistical properties of the centroid velocities is based on the output of the 512³ hydrodynamic simulation computed by Porter et al. (1994). The simulation and its relevance to the interstellar medium is described in

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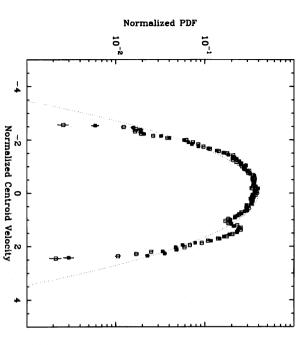


Fig. 1.—PDFs of the centroid velocity for 512^2 lines of sight on the face of the data cube. The velocity scale has been normalized so that the mean velocity $v_{\rm mean}=0$ and the dispersion $\sigma=1$. Filled and open squares correspond to uniformly weighted and density-weighted centroid velocities, respectively. The dotted curve represents a Gaussian distribution with $v_{\rm mean}=0$ and $\sigma=1$.

detail in Falgarone et al. (1994). The results presented here correspond to the simulation epoch that best represents the interstellar medium spectra ($t = 1.2 \tau_{ac}$, where the acoustic time, τ_{ac} , is the sound crossing time of the energy-containing scale). The power spectrum during this epoch is close to that predicted by Kolmogorov for incompressible turbulence [$E(k) \approx k^{-5/3}$], and the density contrast is $\rho_{max}/\rho_{min} \sim 40$. In the computations of the centroid velocities, (v_x) ,

In the computations of the centroid velocities, $\langle v_x \rangle$, where v_x is the line-of-sight velocity component, we treated all the 512² lines of sight on the face of the data cube as independent spectra. We used both density weighting, which is appropriate for optically thin lines, and uniform weighting, which is more appropriate for optically thick lines originating in a clumpy, supersonic medium. The average difference between the centroid velocities calculated with a uniform and density weighting is $\lesssim 3\%$ of the range in the centroid velocity and the maximum difference is $\lesssim 25\%$.

2.1. Probability Density Functions of Centroid Velocities and Centroid Velocity Increments

PDFs of the centroid velocities for all 512² lines of sight on the face of the data cube are shown in Figure 1. To facilitate the shape comparison, all the PDFs of the centroid velocities and the centroid velocity increments discussed here are normalized to a zero mean and a standard deviation of unity. A normalized Gaussian distribution is also shown as a dotted line. The PDFs based on centroid velocities calculated with uniform weighting and density weighting are plotted as filled and open squares, respectively. The error bars due to the limited number of points in a given histogram bin are also shown. The centroid velocity PDFs for the uniform and density weighting are similar and close to a Gaussian distribution; there is no evidence for the

presence of exponential wings. In order to determine whether such wings may arise on a smaller scale, we show in Figure 2 centroid velocity PDFs for 16 subcubes of the size 128 × 128 × 512. Although most of the distributions in Figure 2 do not diverge significantly from a Gaussian, in some cases non-Gaussian wings may be found. Only in one case (Fig. 2, *upper right panel*), an exponential wing is present on one side of the histogram.

flows (e.g., Anselmet et al. 1984; Gagne 1987) a numerical simulations of turbulence (e.g., Vincent & guzzi 1991) have demonstrated that broad, sidered all lines of sight with a separation $|r_1 - r_2|$ between $\Delta - 0.5$ and $\Delta + 0.5$ pixels. The resulting PDFs for a whole data cube (Fig. 3, solid gray line). ity increments calculated for the same separation over the much less pronounced than those in the PDFs of the velocabove the Gaussian distribution. However, these wings are the centroid velocity increments (Fig. 3) clearly show wings to the PDFs of the centroid velocities (Fig. 1), the PDFs of separation $\Delta = 5$ pixels are shown in Figure 3. In contrast $[\langle v_x \rangle (r_1) - \langle v_x \rangle (r_2)]$. For a given line of sight, r_1 , we convelocity increments between pairs of nearby lines of sight Gaussian. We therefore calculated PDFs of components built over the whole system are approximately increments and derivatives, while the PDFs of the velocity exponential wings Both experimental studies of laboratory and atmospheric are found in the PDFs 1984; Gagne 1987) and the the centroid of velocity Mene-

must be associated with high densities. by stretchings. Therefore, some of the high-vorticity regions vorticity is generated by shock interactions and amplified simulation we study. As discussed by Porter et al. (1994), partly due to shocks that are still present in the epoch of the compared to the bulk of the flow. This correlation may be increments are also characterized by an increased density PDFs have consistently more pronounced wings. This indicates that the lines of sight with the largest centroid velocity weighting is relatively small, although the density-weighted centroid velocities computed with uniform and density guzzi 1991). The difference between the PDFs built from in the PDFs of velocity increments (e.g., increasing separation. For separations $\Delta \gtrsim 40$ of PDFs are magnitude of the wings decreases monotonically increments with the separation Δ is shown in Figure 4. The very close to a Gaussian. This behavior is the same as seen The evolution of the PDFs of. the centroid velocity Vincent & Menewith

However, as the velocity power spectrum in a turbulent flow is steep, the spectrum of the centroid velocity is also separation Δ shown in Figure 4. For a given increment Δ scale" motions on the resulting PDFs. Figure 5 shows the centroid velocity of PDFs calculated from the filtered censistent with that in the observational study of Miesch & "systematic" motions. However, to make our analysis conoped compressible turbulence without gravity, star formaall wavenumbers above the lent to a high-pass filter, which, for a given value of β , passes of the centroid velocity. The moving filter average is equivabers around the wavenumber k_{Δ} from the power spectrum the increment method selects a narrow range of wavenumthe PDFs of the centroid velocity increments with the The evolution of these PDFs with β is comparable to that of troid map as a function of the size of the boxcar filter, 2β Scalo (1995), we examined the effect of filtering the "largetion, etc. The simulation of Porter et al. (1994) is for a fully develmotions on the resulting PDFs. Figure As a result, there is no need to filter any cutoff wavenumber

¹ The computations presented here were carried out using the Cray X-MP2E/232 supercomputer located at the Jet Propulsion Laboratory.

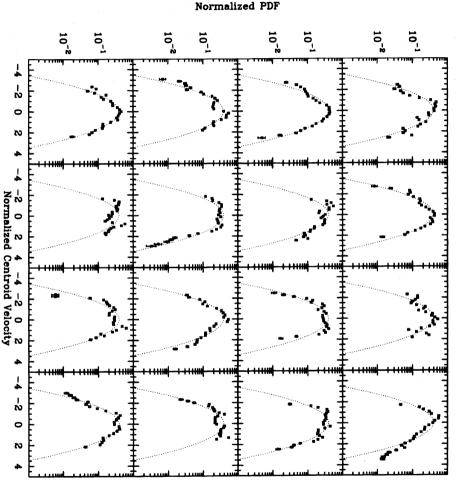


Fig. 2.—PDFs of the centroid velocity for 16 subcubes of size $128 \times 128 \times 512$. The velocity scale is normalized as in Fig. weighted centroid velocities are shown. 1. Only PDFs for uniformly

dominate the spectrum that goes through the high-pass steep. Thus wavenumbers close to the cutoff wavenumber k_{β} spectrum, filter. Accordingly, in a velocity field with a steep the two methods give similar results for power $\Delta = \beta$.

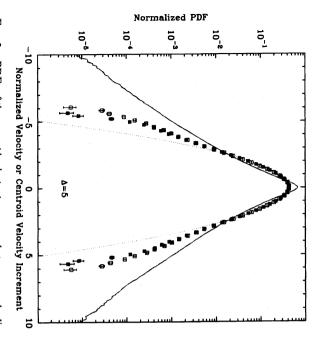


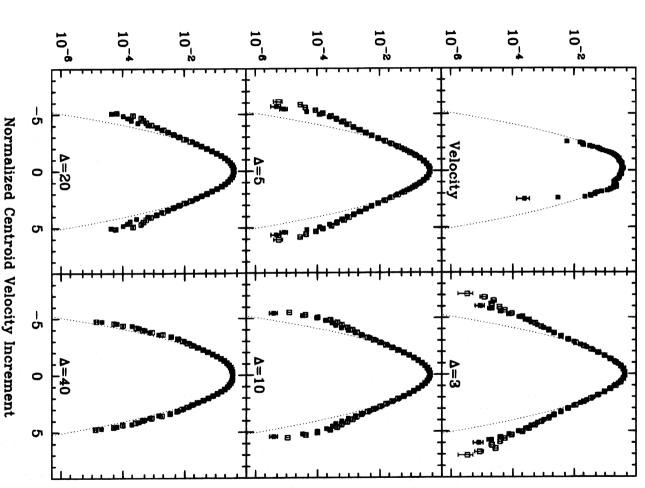
Fig. 3.—PDFs of the centroid velocity increments between nearby lines of sights, $\langle v_x \rangle (r + \Delta) - \langle v_x \rangle (r)$ for a separation $\Delta = 5$ pixels. Symbols are as in Fig. 1. The PDF of velocity increments, $v_x(x, y, z) - v_x(x, y + \Delta, z)$ calculated for the same separation over the whole data cube is shown as solid gray line

the statistics is greatly improved. increments is that the number of points used is larger and One advantage of forming the PDFs of the centroid velocity

directly to the fields studied by Miesch & Scalo star formation. lation of Porter et al. (1994) does not include gravity and the data processing. However, as discussed above, the simuwings should be enhanced if a smaller filter size their fields, our study suggests that the magnitude of these Scalo represent a signature of intermittency of turbulence in size was between 2 and 3.5. If the wings found be the square root of the total number of points) to the filter for which the asymmetric lobes were no longer discernible in the autocorrelation function of the residual centroid map. their study, when applying this method to the observational data. suggests that one should use the smallest possible filter size centroid velocity with the size of the boxcar filter (Fig. The ratio of the effective scale of the observations (taken to evolution of the Miesch & Scalo (1995) used the largest filter size Therefore, our results may not be applicable wings in the PDFs of the filtered by Miesch & is used in In S

2.2. Origin of the Wings in the PDFs of the Centroid Velocity Increments

distribution of the lines of sight contributing to these wings on the face of the data cube. Figure 6 shows the distribution found in the simulation for the PDFs of the centroid velocin the flow associated with intermittency, we studied the ity increments, are related to regions of increased vorticity In order to determine whether the non-Gaussian wings,



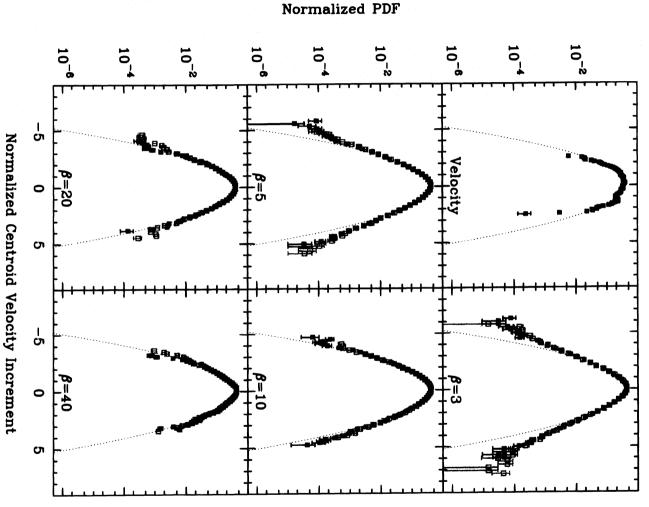
Normalized PDF

Fig. 4.—PDFs of the centroid velocity increments for separations $\Delta = 3$, 5, 10, 20, and 40 pixels. Symbols are as in Fig. 1. The magnitude of the non-Gaussian wings decreases with increasing Δ . For separations $\Delta \gtrsim 40$ pixels, the distribution is essentially Gaussian.

ponent perpendicular to the line of sight ($[\langle (\text{rot } v)_y \rangle^2 + \langle (\text{rot } v)_z \rangle^2]^{1/2}$, where $\langle (\text{rot } v)_y \rangle$ and $\langle (\text{rot } v)_z \rangle$ are the two vorticity components in the plane of the sky averaged along velocity field. The distribution of the average velocity comcross-derivatives of the line-of-sight component of the distribution of the two vorticity components, which involve they trace a filamentary structure, which is related to the velocity increments are not randomly distributed. Instead, sight contributing to the wings of the PDFs of the centroid (93% of the points overlap). Figure 6 shows that the lines of PDF (Fig. 3, open squares) have a very similar distribution tistics for the increments (Fig. ized PDF of the centroid velocity increments, for a separation $\Delta=5$ and uniform weighting. This threshold marks of the lines of sight above a threshold of 3.0 in the normaltransition between Gaussian contributing to the wings 3, filled squares). The lines of of the and non-Gaussian stadensity-weighted

the line of sight) is shown in Figure 7. The coincidence between the filaments in Figures 6 and 7 shows that the increment method can be used effectively to find the location of the maxima of the average vorticity component perpendicular to the line of sight.

surements of the centroid velocity increments may be connot cancel out in the interstellar medium, therefore the written as $\langle (\text{rot } \mathbf{v})_i \rangle = \partial_i \langle v_x \rangle$ of a vorticity component i in the points selected using the increments method with the taminated and the correlation between the distribution of because of periodic boundary conditions. This term does bution of the vorticity that disappears in the simulation term on the right-hand side is simply a cross-derivative of increment method). The second term is a large-scale contri-It can be shown analytically that the line-of-sight average centroid velocity (the quantity the plane of the $+ [v_i(0)]$ we $-v_i(L)]/L$ sample sky can with the



5.—PDFs of the filtered centroid velocity after subtracting a smooth image calculated using a boxcar filter with size 2β . Symbols are as in Fig. 1.

The term due to the boundary conditions may not be negvelocity field do not have a significant effect on our results. boundary conditions due to the turbulent component of the the line of sight, instead of 512). This suggests that the formed over a fraction of the data cube (128 points along of the sky does not change when the calculations are distribution of the average vorticity component in the plane selected with the increment method and the filaments in the ences relative to the large-scale ones. We have also verified mittency further smaller than the small-scale contribution. In addition, intervorticity filaments may not be as good as in the simulation correlation between the distribution of the points large-scale contribution of the vorticity is much in Kolmogorov turbulence presence of large-scale rotation. However, enhances the small-scale velocity differ $\Delta v/\Delta l \sim \Delta l^{-2/3}$ per-

> thus be separated easily from the fluctuating term due turbulence the rotation term will vary slowly with position and can

uniform weighting (Fig. centroid velocity increments for a separation $\Delta = 5$ and increment method (Fig. increased line-of-sight-averaged vorticity modulus, the are not observed. However, the lines of sight selected using the two velocity components in the line of sight, since the vorticity modulus depends also on (filled circles and squares, respectively) in the PDF PDFs for the lines of sight above thresholds of 3.0 and 4.0 pared to the bulk of the flow. Figure 8 shows the vorticity with the maxima in the vorticity modulus averaged along The distribution of the increment method 6) does not correlate equally well 3, filled squares). The overpopuare lines of sight selected with the also the plane of the sky which characterized coman

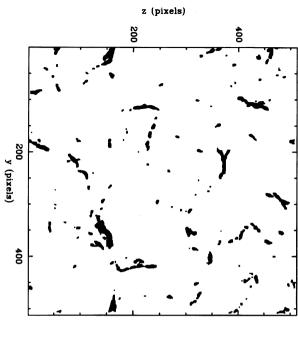
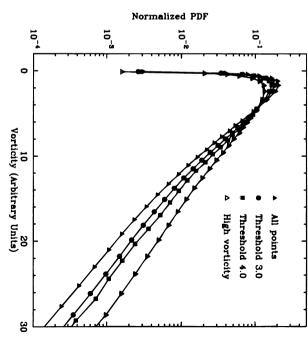


Fig. 6.—Spatial distribution of points with a centroid velocity increment greater than 3.0 in the PDF corresponding to $\Delta = 5$ with uniform weighting (Fig. 3, filled squares; density weighting leads to a very similar distribution).

ity increments, compared to the average for the whole data contributing to the wings in the PDF of the centroid veloccube (filled triangles), suggests that these wings are associlation of the tail of the vorticity PDFs for the lines of sight



olds of 3.0 and 4.0, respectively (see Fig. 3). Open triangles sh ticity PDF for the lines of sight with the average modulus greater than 6. separation $\Delta = 5$ pixels. Filled circles and squares correspond to threshnon-Gaussian wings in the PDF of the centroid velocity increments for a FIG. 8.—Comparison of the vorticity PDF for the whole data cube (filled triangles) with that for the lines of sight that contribute to the Open triangles show the vor-

using the increment method is less to intermittency (e.g., Porter, Pouquet, & Woodward 1992) The tail in the vorticity PDF for the lines of sight selected ated with some of the zones of increased vorticity assignable pronounced than for

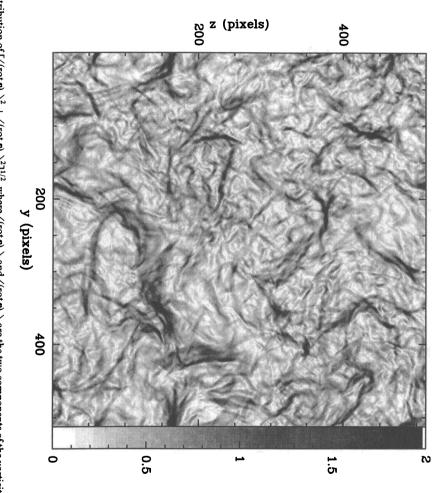


Fig. 7.—Spatial distribution of $[\langle (\text{rot}\, v)_y \rangle^2 + \langle (\text{rot}\, v)_z \rangle^2]^{1/2}$, where $\langle (\text{rot}\, v)_y \rangle$ and $\langle (\text{rot}\, v)_z \rangle$ are the two components of the vorticity in the plane of the sky averaged along the line of sight.

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8, open squares). As discussed above, this is related to the fact that we observe only one component of the velocity those with the highest average modulus of the vorticity (Fig.

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2.3. Relevance to the Interstellar Medium

field does not destroy the phenomenon of intermittency in the velocity field, as revealed by the non-Gaussian wings in the PDFs the velocity increments. Non-Gaussian wings in the PDFs missing effects may be important in varying degrees in interstellar molecular clouds of different types. In addition, the of the centroid velocity increments may possibly be attribwhen trying to extrapolate our results to the interstellar medium. Complications due to star formation can be tistically homogeneous. Therefore, one should be cautious velocity field in molecular clouds is, in general, not stagravity, magnetic fields, and star formation. All those selected by the increment method is a solid prediction of the uted to effects other than the intermittency of turbulence private communication) show that the existence of magnetic (e.g., Biskamp, Welter, & Walter 1990; M. Rieutord 1995, turbulence with comparable magnetic and kinetic energies and three-dimensional numerical simulations of MHD itself in the interstellar medium. For instance, recent twothe velocity field is so fundamental that it should manifest present work that can be tested observationally. However, the filamentary distribution of the lines of sight latitude clouds. We believe that the effect of intermittency of largely avoided by studying inactive regions, like high-Our results are based on a simulation of decaying supercompressible turbulence, which does not include

3. SUMMARY

and gravitationless simulation shows the following: Our study of the statistical properties of the line centroid velocity in a turbulent, compressible but non-star-forming

although deviations from a Gaussian are present on smaller of sight on the face of the data cube is close to a Gaussian, The PDF of the centroid velocity calculated for all lines

> whole data cube found in PDFs of velocity increments calculated over the tion, the magnitude of these wings is smaller than those decreases with increasing separation Δ . For a given separashow non-Gaussian wings. The magnitude of these wings The PDFs of the centroid velocity increments clearly

velocity field with a steep power spectrum, this approach is partially equivalent to calculating centroid velocity increments. However, the increment method gives much filtered out by subtracting a smooth image. In a turbulent 3. Non-Gaussian wings also appear in PDFs of the centroid velocity after "large-scale" motions have been better statistics.

line-of-sight component of the velocity field. two vorticity components involving cross-derivatives of the filamentary structure, which follows the distribution of the wings of the PDFs of centroid velocity increments trace 4. The lines of sight contributing to the non-Gaussian а

origin in the phenomenon of intermittency. sight with increased average vorticity compared to the bulk of centroid velocity increments thus appear to have their velocity component). The non-Gaussian wings in the PDFs which cannot be localized with observations of only one of the flow (although not those with the highest vorticity, 5. The increment method allows for selecting lines of

should be applicable to non-star-forming quiescent molecphysics and chemistry of the interstellar medium and for studying the effects of intermittency of turbulence on methods discussed in this paper provide a useful new tool these results to the interstellar medium, we believe that the Although one has to be cautious when extrapolating

and by the JPL Superconducting Project, which is sponsored by JPL and the NASA Office of Space Science and ward for providing us with the result of their hydrodynamic simulation. This research has been supported by NSF grant Applications. AST 93-13929 to the Caltech Submillimeter Observatory We thank D. H. Porter, A. Pouquet, and P. R. Wood-

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