In-situ studies of ultracold atomic gases can yield invaluable information. Imaging on the one hand [1, 4, 5], and light-shift spectroscopy on the other hand [6, 7, 8] have independently proved successful in the investigations of cold neutral gases. In this paper, we present a light-shift tomography method combining in-situ absorption imaging and light-shift spectroscopy to yield an image, and/or the number, of atoms at constant potential-energy in an optical-dipole trap. It takes advantage of the strong light-shifts of the upper $5P_{3/2}$ level of the imaging transition of $^{87}\text{Rb}$ under the influence of our trapping laser at 1565 nm. This is due to quasi-resonances to higher excited states ($4D_{3/2}$ and $4D_{5/2}$) at 1529 nm. As a consequence, although the light-shift experienced by atoms in the ground state ($5S_{1/2}$), i.e. the trapping potential, is moderate, the shift of the imaging transition can be large compared to its natural linewidth. It thus allows us to perform spectrally-resolved imaging of the atomic cloud.

We use this technique for two different goals: (i) Mapping of the optical potential. Starting with a cold cloud with a smooth density profile, we suddenly switch on a trapping laser at 1565 nm, and immediately take an absorption image of the atoms in the presence of the trap, before any evolution of the atom density. By repeating this imaging at various probe laser frequencies, we obtain a map of the equal light-shift regions, i.e. we perform tomography of the trap potential. (ii) Measurement of the atom potential-energy distribution. Counting the number of atoms at a given probe detuning, we directly measure the potential-energy distribution of the cloud. This allows us to study the relaxation of a trapped atomic cloud from an initial out-of-equilibrium situation towards a thermal distribution, by monitoring the evolution of the energy distribution during the free-evaporation process.

As shown in Figure 1a, we image $^{87}\text{Rb}$ atoms using a probe resonant with the $5S_{1/2}$ ($F = 2$) to $5P_{3/2}$ ($F' = 3$) resonance transition at 780 nm ($D_2$), perturbed by the trapping laser at 1565 nm. In order to evaluate the light-shift of the ground and excited states of the $D_2$ imaging transition, we have computed the polarisabilities ($\alpha_g$ and $\alpha_e$, respectively) of these states for the 1565 nm laser excitation. The transitions giving the main contributions are shown in Figure 1b. The moderate detuning of the trapping laser with respect to the $5P$ to $4D$ transitions, compared to the $5S$ to $5P$, leads to a polarizability of the $5P_{3/2}$ state larger than the one of the ground state by a factor $\frac{\alpha_e}{\alpha_g} = 42.6$.

As the light-shifts of the energy levels are all proportional to the trapping-laser intensity, the light-shift of the ground state, i.e. the potential-energy of an atom in
shown in Figure 1b, by taking an potential-energy of the atoms in the trapping beams. As small compared to the light-shift $\Delta$ [11, 12].

The experimental setup is as follows: in a first vacuum chamber, $^{87}\text{Rb}$ atoms are collected from an atomic vapor created by a dispenser in a two-dimensional magneto-optical trap (2D MOT). Atoms are then transferred into a second chamber where they are trapped in a 3D MOT. The laser system for 2D and 3D MOT is based on tapered-amplified extended-cavity diode lasers, as described in [13]. The probe beam is generated by a dedicated, offset-locked laser, which can be detuned by $\delta\omega$ (neglecting gravity), is simply related to the light-shift of the imaging transition $\Delta$ by:

$$\hbar\Delta = \left(\frac{\alpha_g}{\alpha_p} - 1\right)E_p = 41.6 E_p.$$

(1)

As a consequence we can spectrally resolve the potential-energy of the atoms in the trapping beams. As shown in Figure 2, by taking an in-situ absorption image with a chosen detuning $\delta$ of the probe laser, we detect atoms situated at positions $r$ such that $U(r) = \frac{\hbar\Delta}{1+\sigma}$, where $U(r)$ is the trapping potential ($U = 0$ in free space). We thus directly obtain a map of the trapping potential $U(r)$. The energy resolution is related to the linewidth of the imaging transition, but, as a consequence of Eq. 1, enhanced by a factor of 41.6 (corresponding to $0.14 \text{MHz}$ or $7 \mu\text{K}$).

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The dipole-trap light is generated by a 50 W erbium-doped fiber-laser at 1565 nm (IPG ELR-50). This laser is focused to a $50 \mu\text{m}$ waist onto the atomic cloud through a lens that can be moved along the optical axis via a motorized translation stage (Aerotech ANT-50L), in order to be able to vary the beam diameter at the atomic position (much as in ref. [14]). Light is then refocused on atoms by a 1:1 telescope to create a crossed-beam configuration, with a crossing angle of $56^\circ$. The beam configuration is shown on Fig. 2. Throughout this paper, the movable lens is placed such that at the dipole trap crossing, the beam diameters are about $200 \mu\text{m}$. The optical power is controlled at the output of the laser by an electro-optic modulator and a Glan polarizer. The angle of incidence of the trapping beams with respect to the vacuum-chamber window is $28^\circ$, leading to astigmatism of the beams. We compensate this effect to first order on the first-pass beam using a tilted, glass plate.

We use light-shift tomography of the optical-dipole trap to map the potential landscape, using atoms as local probes of the potential. About $10^8$ $^{87}\text{Rb}$ atoms are collected in the 3D MOT with a magnetic field gradient of $12.5 \text{G.cm}^{-1}$ and a detuning of the cooling laser of $2.5 \Gamma$. The 3D MOT is then compressed down to $200 \mu\text{m}$ (rms radius) by increasing the detuning of the cooling laser up to $10 \Gamma$. The cooling beams are switched off, and the dipole trap laser is switched on 1 ms later. After another millisecond an absorption image is taken with a $50 \mu\text{s}$ pulse at the chosen probe detuning. A re-pumping laser resonant with the free space $F = 2$ to $F' = 3$ transition is applied together with the imaging laser. At resonance, atoms scatter about 100 photons during the imaging pulse and the atomic density has no time to evolve.

Examples of absorption images are shown in Fig. 3. At

FIG. 2: Beam configuration of the dipole trap and the probe. (color online)

FIG. 3: Absorption images taken immediately after switching on the optical-dipole trap, showing the equipotentials of the trap. By choosing the probe laser detuning with respect to the free-space imaging transition ((a): -40 MHz, (b): -80 MHz, and (c): -100 MHz, corresponding to a light-shift of the ground state of 45 $\mu\text{K}$, 91 $\mu\text{K}$, and 115 $\mu\text{K}$ respectively) we observe the distribution of equal laser-intensity regions i.e. equipotentials of the trap. The probe laser propagation axis is inclined by $45^\circ$ with respect to the crossed dipole trap plane. Images insets (b) and (c) show cuts along the horizontal axis.
moderate probe detuning (-40 MHz), we see open equipotentials (Fig.3), which means that we probe atoms which will be able to escape along the directions of the two beams. In this image, we can detect an asymmetry of the trapping potential between the two arms of the dipole trap, which is related to intensity imbalance and residual astigmatism. The decrease of the contrast at the edges of the image is due to the vanishing atomic density. For larger detunings (-80 MHz), the images (Fig.3b) show closed equipotentials with an elliptic contour. As we go deeper in the trap (-100 MHz), we reach the bottom, where the equipotentials merge into a spot (Fig.3c).

This tomographic method allows us to determine in-situ the trap characteristics. The potential landscape at the bottom of the trap yields the trap frequencies (110 ± 10 Hz, 110 ± 10 Hz, and 150 ± 10 Hz), and the detuning at which we observe the change from closed to open equipotentials yields the trap depth (57 µK in our experiment). We observe that the shape of the crossed region as probed by tomography is very sensitive to the overlap of the two arms, which provides us with a direct and accurate alignment method [13].

We evaluate the spatial resolution of the potential mapping as follows: in a place where the trapping potential gradient is \( \nabla U \), the resolution associated with the linewidth \( \Gamma \) of the probe transition is \( d = \frac{\hbar}{\alpha_e - \alpha_g |\nabla U|} \approx 1/41.6 \mu m \). In our experimental conditions, at the places of steepest gradients, \( d = 10 \mu m \), whereas the resolution of our imaging setup is 7 µm. The widths of the peaks in the insets of figures 3b and c are explained by the convolution of the two effects. Actually, \( d \) could be made smaller than the resolution of the imaging system, either by increasing the light-shift gradients or by using a narrower transition [14,17].

We now turn to the measure of the potential-energy distribution of the atomic cloud. For each value of the probe detuning, i.e. of the potential-energy (Eq.1), we count the number of atoms by integration of the optical density in the corresponding in-situ absorption image (any spatial information is lost). Repeating this measurement at various values of the detuning, we obtain the atomic potential-energy distribution convoluted with our energy resolution lineshape. As in our case the measured atom number varies smoothly at the scale of the resolution (7 µK), it is simply proportional to the atomic potential-energy distribution.

Using this technique, we follow the evolution of an optically-trapped cloud under the effect of free evaporation. Experimentally, we load atoms in a compressed MOT, we then turn off the cooling laser, and load the atoms in the dipole trap [18,19,20,21,22]. We then wait for a given time, and image in-situ the trapped cloud at various detunings.

Figure 3 shows the observed atomic potential-energy distribution after various evolution times, averaged over 4 images per data point. At short evolution times (<50 ms), the measurement is blurred by the untrapped atoms falling from the magneto-optical trap. After 50 ms, the atom distribution extends far into the anharmonic region of the trap, in particular into the two arms where atoms can escape. The fact that we can observe atoms with a potential-energy larger than the trap depth is a signature of the non-ergodicity of the free-evaporation process: atoms have enough energy to escape but temporarily remain in the trapping region. Not all the available regions of phase-space are explored in the time scale of the experiment [19]. The bottom of the trap is at -115 µK. Atoms detected below this value reflect the finite linewidth of the imaging transition [15].

As the thermalisation proceeds, the number of atoms located in regions of high potential-energy diminishes faster than the number of atoms at the bottom of the trap. This process results in a lower mean potential-energy of the remaining atoms. To characterize our results better, we fit our data with the theoretically predicted atom number \( N(\delta) \) at a given probe detuning, in the case of \( N_{\text{tot}} \) classical atoms at thermal equilibrium in a harmonic trap, taking into account the finite linewidth of the imaging transition:

\[
N(\delta) = \frac{4N_{\text{tot}}}{\sqrt{\pi}} \int_{0}^{\infty} \frac{u^2 e^{-u^2} du}{1 + 4(\delta + v - tu^2)^2}
\]

where \( t = \hbar \Gamma \omega_0 (\omega_0 - 1) \), \( v = \frac{U(v=0)}{\hbar \Gamma} \) and \( \delta = \frac{\omega_0 - \omega}{\Gamma} \) (\( \omega_0 \) is the unshifted probe transition frequency) are normalized temperature, minimal potential-energy and detunings respectively. The fit is unexpectedly good given the
fact that the trap is harmonic only close to the bottom of the trap. The fitted temperatures are, to within 10% uncertainty consistent with complementary measurements of the velocity distribution obtained by the time-of-flight method.

Inset in Figure 1 shows the evolution of the temperature with the free evaporation time. We first observe a rapid decrease of the temperature in 100 ms, which we attribute to a simple loss of atoms with an energy larger than the trap depth. It takes a few trap periods for the energetic atoms to find their path to escape along one of the two trapping beams. At longer time, we observe a slower decrease of the temperature. It is consistent with collision-induced evaporation as we estimate the initial collision rate in our trap to be of the order of 3 s⁻¹. The lifetime in this experiment is limited to 2 s by background gas collisions and we nevertheless measure an increase in phase-space density by a factor of 5 between the loaded cloud at 50 ms and the thermal, trapped cloud at equilibrium after 1 s.

In conclusion we have presented a method to directly map the potential created on ⁸⁷Rb by an erbium doped fiber-laser at 1565 nm and to directly measure the atomic potential-energy distribution. The energy resolution (7 μK) could be improved using a trapping laser closer to the 1529 nm transition and an appropriate probe polarization. This method is not specific to ⁸⁷Rb, and could be generalized to other alkali gases which have strong transitions from the nF₃/₂ state to higher excited states in the mid-infrared (e.g. Cs at 1469 nm, K at 1252 nm).

The potential-energy resolution of this technique is independent of the spatial resolution of the imaging setup. For a rapidly spatially-varying light field, this technique could achieve sub-wavelength resolution. For example, in a three-dimensional, cubic, optical lattice, the detuned probe laser would be resonant with atoms situated in spherical shells centered on each lattice site, the radius of which being related to the probe-laser detuning. Light-shift tomography, allowing in-situ local probing, is likely to be useful in the the context of both quantum gas studies and quantum information processing using cold atoms.

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References:
[11] The tensor polarizability leads to a difference of the polarizability of the various magnetic sublevels of the 5F₃/₂ (F' = 3) state of about 20% [14]. Due to the orthogonal polarizations of the two arms of the crossed dipole trap, the polarization of the trapping laser is ill defined in the trap, and we assume a uniform distribution of the atoms over the various magnetic sublevels of the ground level 5S₁/₂ (F = 2). The broadening of the probe transition is then evaluated by taking equal polarization components for the probe beams. This results into an intensity-dependant broadening that can be as large as 12% of the shift of the transition, which adds to the natural linewidth (6.1 MHz).
[15] Using the potential mapping, we can evaluate in-situ the aberrations created on the trap beam by the vacuum chamber windows, by measuring the real beam waist, and extracting the beam quality factor M².
[18] The strong red-shift of the cycling transition raises specific problems in the loading process from a MOT or an optical molasses. Here we address this problem by rapidly alternating the optical dipole trap and the cooling lasers (10 kHz). Efficient loading of an optical-dipole trap at 1565 nm will be described in a further publication.