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I. Wohltmann, M. Rex. Improvement of vertical and residual velocities in pressure or hybrid sigma-pressure coordinates in analysis data in the stratosphere. *Atmospheric Chemistry and Physics Discussions*, 2007, 7 (5), pp.13401-13416. hal-00303097

HAL Id: hal-00303097

<https://hal.science/hal-00303097>

Submitted on 18 Jun 2008

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**Improvement of
vertical winds**

I. Wohltmann and M. Rex

Improvement of vertical and residual velocities in pressure or hybrid sigma-pressure coordinates in analysis data in the stratosphere

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Received: 6 September 2007 – Accepted: 11 September 2007

– Published: 13 September 2007

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Stratospheric vertical winds from analysis data in pressure (p) or hybrid pressure (σ - p) coordinates, for use in e.g. chemical transport models (CTMs) or trajectory models, often suffer both from excessive noise and errors in their mean magnitude, which in turn can introduce errors in important dynamical quantities like vertical mixing or constituent transport with the residual circulation. Since vertical velocities cannot be measured directly, they are inferred from other quantities, typically from horizontal wind divergence, that is the mass continuity equation. We propose a method to calculate the vertical wind field from the thermodynamic energy equation in p or σ - p vertical coordinates that substantially reduces noise and overestimation of the residual circulation. It is completely equivalent to the approach using potential temperature (θ) as a vertical coordinate and diabatic heating rates as vertical velocities, which has already been demonstrated to give superior results to the continuity equation. It provides a quickly realizable improvement of the vertical winds, when a change of the vertical variable would cause an inadequate effort (e.g. in CTMs). The method is only applicable for stably stratified regions like the stratosphere.

1 Introduction

Analysis and reanalysis data from e.g. the European Centre for Medium-Range Weather Forecasts (ECMWF) (Uppala et al., 2005), the United Kingdom Meteorological Office (UKMO) (Swinbank and O'Neill, 1994) or the NASA Goddard Earth Observation System (GEOS) (Schoeberl et al., 2003) often suffer from noisy and biased vertical winds based on the continuity equation in p coordinates. In turn, too much vertical dispersion and mixing or problems with the residual circulation and the mean age of air are introduced (e.g. Uppala et al., 2005). While there are promising developments in new datasets as the ERA-Interim reanalysis (Monge-Sanz et al., 2007), there is a need to improve the analysis data in these aspects.

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Vertical wind is an issue in CTMs, which use these data to run the dynamical part of the model. E.g., a too young age of air and a too rapid residual circulation are reported for CTMs using GEOS analysis data (and even General Circulation Model (GCM) data) in [Hall et al. \(1999\)](#) or for TM3 in [Bregman et al. \(2003\)](#) (ECMWF forecast data) and [van Noije et al. \(2004\)](#) (ECMWF ERA-40). Excessive vertical dispersion and problems with the age of air are reported in [Schoeberl et al. \(2003\)](#) for the GEOS Finite Volume Data Assimilation System (FVDAS) and UKMO. Models like SLIMCAT ([Chipperfield, 2006](#)) (UKMO or ECMWF) or IMATCH ([Mahowald et al., 2002](#)) are not affected in the same way, since they use θ coordinates and calculate vertical movements by diabatic heating rates. Indeed, a better performance of this θ coordinate approach in comparison to the continuity equation in p or σ - p coordinates has been demonstrated for trajectory calculations, CTMs and even for the internally consistent wind and temperature fields of GCMs ([Eluszkiewicz et al., 2000](#); [Mahowald et al., 2002](#); [Schoeberl et al., 2003](#); [Chipperfield, 2006](#)). These improvements carry over to the winds from the thermodynamic equation in p or σ - p coordinates, as we will show shortly. In addition to CTMs, there are many other studies, like trajectory calculations (e.g. [Fueglistaler et al., 2005](#)), which rely on vertical winds from analysis data and could benefit from improved vertical velocities.

The calculation of reliable vertical winds is a long-standing topic in numerical weather prediction (e.g. [Krishnamurti and Bounoua, 1996](#)). Several methods have been proposed to calculate vertical wind fields in p coordinates: The “kinematic” method (vertical wind w from the continuity equation), the “adiabatic” or “diabatic” method (w from the thermodynamic energy equation), the “vorticity” method (w from the vorticity equation) and the omega equation (a combination of several equations that avoids time derivatives). We choose the diabatic method here, since it is ideally suited for the stratosphere. In addition, it is possible to derive winds for analyses with a low upper boundary (e.g. the NCEP reanalysis, [Kistler et al., 2001](#)) if the radiative transfer above this boundary is sufficiently constant, which is difficult with the continuity equation.

2 Eulerian vertical winds

Usually, vertical wind is obtained from the continuity equation

$$\nabla \cdot (\rho_0 \mathbf{u}) = 0 \quad (1)$$

which describes the conservation of mass in p coordinates. $\mathbf{u}=(u, v, w)$ is the vector of zonal wind u , meridional wind v and vertical wind w in spherical coordinates. All following equations will use log-pressure height $z=-H \log(p/p_0)$ as vertical coordinate (p pressure, p_0 reference pressure, $H=RT_0/g$ scale height, R gas constant, T_0 reference temperature, g gravitational acceleration), for which $\rho_0=p_0/(RT_0) \exp(-z/H)$ is the air density. Solving for w gives

$$w(z) = \frac{1}{\rho_0(z)} \int_z^{z_\infty} \rho_0(z') \nabla_h \cdot \mathbf{u}_h(z') dz' \quad (2)$$

where $\nabla_h \cdot \mathbf{u}_h(z) = [\partial_\lambda u(z) + \partial_\varphi (v(z) \cos \varphi)] / (a \cos \varphi)$ is the horizontal wind divergence in spherical coordinates (λ longitude, φ latitude, a earth radius, ∂ Eulerian derivative). z_∞ is the log-pressure height of the highest given altitude level. The upper boundary condition is assumed to be $w(z_\infty)=0$ here. If u and v are given, w can be calculated.

However, the continuity equation is not the only conservation equation one can use to determine the vertical wind. At the same time, energy needs to be conserved by the first law of thermodynamics, expressed by the near conservation of potential temperature $\theta=T(p_0/p)^{2/7}$ (with T temperature), which can only be changed by radiative heating Q

$$\frac{D\theta}{Dt} = Q \quad (3)$$

D/Dt is the Lagrangian derivative. Solving for w gives

$$w = (Q - \partial_t \theta - \frac{u}{a \cos \varphi} \partial_\lambda \theta - \frac{v}{a} \partial_\varphi \theta) / \partial_z \theta \quad (4)$$

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If Q , T , u and v are given, w can be calculated. Q is obtained by a radiative transfer model, which needs T profiles as input data. Since we divide by the static stability $\partial_z \theta$, the equation can only be used in stably stratified regions like the stratosphere. For short time-scales, the diabatic component $Q/\partial_z \theta$ of the wind can usually be neglected, while it is the most important term on time-scales of several months.

In theory, Eqs. (2) and (4) obviously should give identical results. However, since u , v and T are measured quantities prone to errors and data are discretized and interpolated, Eqs. (2) and (4) will not be fulfilled at the same time in practice. This also means that mass is not conserved if Eq. (4) or the approach in the next section is used to calculate vertical winds. To ensure conservation of mass, a procedure similar to that presented in Weaver et al. (2000) can be used to correct the horizontal winds by adjusting the divergence to be zero while conserving the vorticity of the wind field. We do not follow this approach here, since the implied changes to the vertical wind are rather small.

3 Semi-lagrangian approach

Equation (4) substantially reduces noise in the vertical wind fields, but is not sufficient for long-time integrations and an accurate determination of the residual circulation. Since Eq. (4) basically represents an advection problem in an Eulerian framework, a criterion identical to the Courant-Friedrichs-Lewy criterion $u\Delta t \leq \Delta x$ applies as a necessary condition for a stable solution, where u is the advection velocity, Δx is the grid spacing and Δt is the time step of the analysis. Since the time step at which the data is obtained is typically 6 h and the grid spacing typically 2.5° , this condition is usually not fulfilled for available analysis data, especially at high latitudes (the time step and grid spacing of the underlying model of the analysis are usually much higher, but cannot be used due to computational constraints). Note also that since there is no exact constraint to a certain θ level as in an application with θ levels as vertical coordinate, the trajectories/air masses tend to drift away from the correct θ level even if only small

systematic errors are present in the vertical wind. Error sources are e.g. the approximation of derivatives by finite differences or interpolation errors. Hence, we use a Semi-Lagrangian approach, where we calculate forward and backward trajectories in a θ coordinate system starting/ending at the analysis grid points in the p or σ - p coordinate system and use the pressure difference between the start and end points of the trajectories (divided by the travel time of the trajectories) as a direct measure for the vertical wind.

In the examples given here, vertical winds are calculated for every grid-point in longitude, latitude and time, but for a staggered grid in the p coordinate, with the new grid points centered in log-pressure between the old levels, which greatly improves the long-term stability of the trajectories in the vertical direction. At every four-dimensional grid-point, a 12 h forward and a 12 h backward trajectory in θ coordinates are started. The pressure difference between the latest date of the forward trajectory and the earliest date of the backward trajectory divided by 24 h is the vertical wind at the grid-point. Potential temperature on the isentropic forward and backward trajectories is only allowed to change by radiative heating.

The isentropic trajectory model uses a 4th order Runge-Kutta method for integration with a 10 min time step. Spherical coordinates are used, but poleward of 85° , the projection is switched to a polar projection to avoid the singularities at the poles. Wind and temperature values are interpolated linearly in longitude, latitude, the logarithm of θ and time to the position of the trajectory. Pressure is determined from the interpolated temperature and θ by solving $\theta = T(p_0/p)^{2/7}$ for p .

4 Results and discussion

The left panel of Fig. 1 shows a vertical wind field derived from the continuity equation, as provided by the ECMWF ERA-40 reanalysis (50 hPa taken from the standard pressure levels, horizontal $2.5^\circ \times 2.5^\circ$ grid, 1 January 2000 averaged over 0–24 h UTC). The right panel shows the field calculated from the thermodynamic equation with the

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Semi-Lagrangian method that most closely simulates the wind field in the left panel (calculated with ERA-40 temperature and wind data at the same day at 12 h UTC with 12 h back- and forward trajectories, staggered level between 30 and 50 hPa). It is obvious that the right panel is considerably less noisy.

5 It could be argued that the scatter is real and that the left panel is the correct one. However, the vertical winds in the left panel would correspond to heating rates of several K/day after subtraction of the part of the wind that is caused by adiabatic movements. Such heating rates can be ruled out as unphysical (see also [Eluszkiewicz et al., 2000](#)). In addition, the vertical mixing caused by these winds would be much larger than
10 observed (see discussion of diffusion coefficients below).

The method is now tested with ERA-40 σ - p model level data (60 levels) with a horizontal resolution of $2^\circ \times 2^\circ$. After calculating the Eulerian vertical winds with the Semi-Lagrangian method using these ERA-40 data, the original vertical winds from ERA-40 are replaced on a staggered grid, while keeping the horizontal winds and temperature.
15 This data set is used to drive several test runs with a trajectory model using the pressure of the model levels as coordinate (THERMO-P hereafter, red dots in the following figures). In addition, results are compared with trajectory runs with the original vertical winds from the continuity equation in the same coordinate system (CONT-P, blue dots) and with the potential temperatures of the model levels as the coordinate and heating
20 rates as vertical velocities (Q-THETA, green dots).

As a first example we start forward trajectory runs at the equator. For all runs, 1440 trajectories are started at 0° N on 1 January 2000 (00 h UTC), equally spaced in longitude in 0.25° steps at the 475 K isentropic level. Trajectories are integrated for 20 days.

25 To test the long-term stability of the method first, we run this setup with a prescribed artificial constant heating rate of 0 K/day. Results after 20 days show an average of 475.5 K and a standard deviation of 3.4 K over all trajectory end-points. A run with 1 K/day heating shows an average of 495.7 K and a standard deviation of 3.2 K. Integration periods of up to 100 days show similar results. This demonstrates the stability

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of the method.

Figure 2 (left) shows results for the three combinations of vertical coordinates and velocities described above. Heating rates are obtained directly from the ERA-40 archive and are based on the radiative transfer model in use by ECMWF (Morcrette et al., 1998), which uses climatological ozone and prognostic water vapor profiles in the stratosphere. Note that there are known temperature biases and fluctuations compared to measurements in ERA-40 data (Uppala et al., 2005), which could affect the heating rates.

The Lagrangian mean over the difference of the vertical start and end positions of the trajectories is a direct measure for the vertical residual velocity of the tropical upward branch of the Brewer-Dobson circulation (Andrews et al., 1987). Results are shown in Table 1. The difference between the continuity equation and the thermodynamic equation is noticeable. The mean upward velocity is 15.5K in 20 days for CONT-P and 10.2K in 20 days for THERMO-P. Q-THETA shows a change of 8.9K, comparable to THERMO-P. The table also contains calculations based on standard pressure level data instead of model level data (everything else being the same). The difference between the continuity and thermodynamic equation is much less pronounced here, which demonstrates that many other parameters, like the number of levels, can significantly influence the results.

Results for the vertical residual velocity from the trajectory calculations are compared to observed vertical velocities in geopotential height (Mote et al., 1998) and potential temperature (Hall and Waugh, 1997) inferred from the tape recorder signal in tropical stratospheric water vapor mixing ratios. Typical heating rates in the tropical stratosphere are in the order of 10 K in 20 days (e.g. Hall and Waugh, 1997). Comparison with Mote et al. (1998) is only possible for standard pressure levels, since the model level data contains no geopotential. CONT-P shows a mean change of 378 gpm in geopotential height, while THERMO-P shows a change of 397 gpm and Q-THETA shows a change of 342 gpm. Mote et al. (1998) give long-term mean vertical speeds of 0.2 mm/s at altitudes of about 20 km for HALOE data, corresponding to 345 gpm in

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20 days. Niwano et al. (2003) also suggests a value near 0.2 mm/s. All values agree roughly within the uncertainties of the observations and our calculations.

The runs can also be used to derive the vertical eddy diffusion coefficient K_z , since K_z and the standard deviation σ of the end-points of the trajectories are related by $K_z = \sigma^2 / (2t)$, where t is the integration time (this follows from Fick's law with a delta function as initial condition). Table 1 shows observed values derived from the tape recorder signal in comparison to the values inferred from the trajectory runs. The vertical diffusion coefficients derived from the continuity equation are more than two orders of magnitude larger than observed and are clearly outside the possible range of K_z values compatible with the observed tape recorder signal (Hall and Waugh, 1997; Mote et al., 1998). The diffusion coefficients from the isentropic and thermodynamic runs are much closer to reality. They somewhat underestimate the observed values, perhaps due to missing sub-grid processes.

Figure 2 (right) shows results of backward trajectory runs in the polar vortex as a second example. For all runs, trajectories are initialized on a $2.5^\circ \times 2.5^\circ$ grid inside the polar vortex at the 450 K isentropic level. The polar vortex is defined as the area inside the 20 PVU contour of Lait's modified potential vorticity ($\theta_0 = 420$ K) (Lait, 1994). Trajectories start on 5 March 2000 (12 h UTC) and run for 100 days until 26 November 1999. The winter 1999/2000 is selected because it is one of the few winters in which tracer measurements are available for comparison.

The plot shows the position of the trajectories on 26 November 1999 (12 h UTC) as a function of modified PV and θ . Only trajectories inside the 20 PVU contour on 1 January 2000 and inside the 15 PVU contour on 26 November 1999 are shown (basically trajectories that stayed inside the vortex). The trajectories show a much larger vertical dispersion in the case of the continuity equation again.

The Lagrangian mean over the difference of the vertical start and end positions of all trajectories is now a measure for the vertical residual velocity of the polar downward branch of the Brewer-Dobson circulation. The mean downward velocity from 26 November 1999 to 5 March 2000 shows large differences between the two isobaric

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runs ($\Delta\theta=187$ K for CONT-P, $\Delta\theta=44$ K for THERMO-P). Results for the averaged vertical velocity are compared to descent rates inferred from tracer measurements of N_2O (Greenblatt et al., 2002). N_2O tracer measurements conducted around 26 November 1999 (solid black line, $\theta=513$ K) and around 5 March 2000 (dashed black line, $\theta=450$ K) give a change of $\Delta\theta=63$ K. In comparison to this value, the value from the THERMO-P run is far more realistic than the value from the CONT-P run, which overestimates the descent rates by a factor of 3. The Q-THETA run ($\Delta\theta=48$ K) compares well with the THERMO-P run, but both runs show values slightly too small compared to the observations. Again, there are noticeable differences if standard pressure level data is used in all runs (Table 1).

This article was inspired by the question in how far the use of vertical wind fields from continuity affected water vapor transport into the stratosphere in Fueglistaler et al. (2005). Figure 3 shows results of backward trajectory runs started on 29 February 2000 at 400 K on a $2^\circ \times 2^\circ$ grid between 30° N/S and run until they reached the 365 K level for all three wind fields discussed above. The upper panel shows position and temperature of the coldest point along each trajectory while the lower panel shows the distribution of residence times of the trajectories between 365–375 K. While the cold point locations remain relatively unaffected (small change in the stratospheric water vapor obtained by freeze drying), mean residence times differ by a factor of 2, which directly affects chemical and microphysical processing.

These examples show the importance of a correct representation of vertical wind fields in modelling studies, which will remain an issue in the future.

Acknowledgements. We thank P. Haynes for helpful suggestions. We thank ECMWF for providing reanalysis data. This work is supported by the European Community through the SCOUT-O3 project.

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Table 1. Performance of different representations of the vertical wind field. Vertical velocities are derived from the continuity equation (CONT-P) in pressure coordinates, the thermodynamic equation (THERMO-P) in pressure coordinates or from heating rates (Q-THETA) in θ coordinates (all coordinates are interpolated both from standard pressure levels p or model levels σ - p). Second column: Mean descent (26 November 1999 to 5 March 2000) in the polar vortex in potential temperature (from Fig. 2, right). 3rd and 4th column: Mean ascent (1–21 January 2000) in the tropics based on geopotential height or potential temperature (from Fig. 2, left). 5th and 6th column: Eddy diffusion coefficients K_z based on geopotential height or potential temperature (from Fig. 2, left). All values are compared to observations: ^aGreenblatt et al. (2002), ^bHall and Waugh (1997), ^cMote et al. (1998).

	Descent vortex (K)	Ascent tropics (K)	Ascent tropics (m)	K_z tropics (K ² /d)	K_z tropics (m ² /s)
Observed	63 ^a	10 ^b	345 ^c	0.3 ^b	0.02 ^c
CONT-P p	205.7	9.8	378.2	37.3	0.47
CONT-P σ - p	186.6	15.5	–	54.7	–
THERMO-P p	91.4	11.7	396.9	0.24	0.001
THERMO-P σ - p	44.0	10.2	–	0.25	–
Q-THETA p	73.1	10.0	342.4	0.009	0.002
Q-THETA σ - p	47.5	8.9	–	0.04	–

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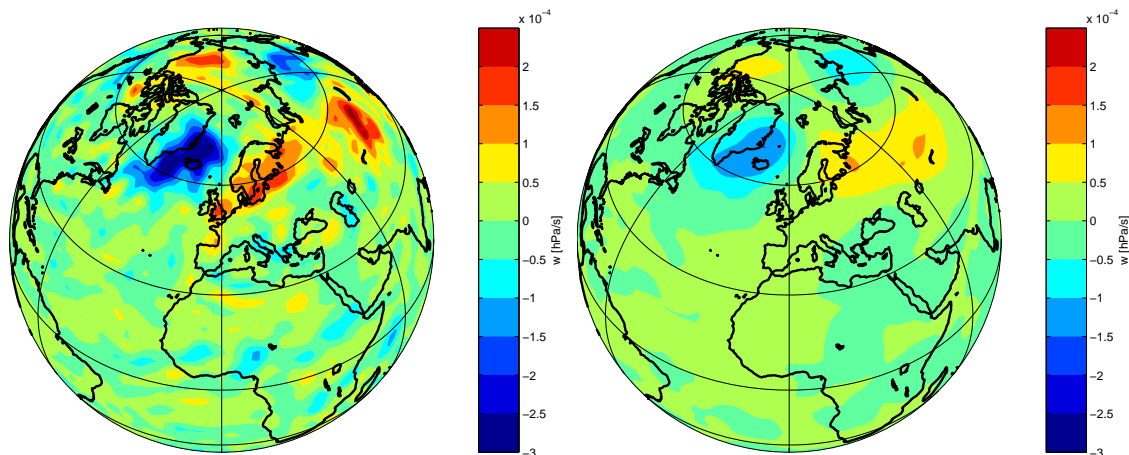


Fig. 1. Vertical wind from ERA-40 reanalysis data on standard pressure levels, calculated with two different methods. Left panel: Vertical wind field at 50 hPa from the continuity equation as provided by ECMWF, averaged over 1 January 2000 0–24 h (UTC) (to compare better with the right panel). Right panel: Vertical wind field from the thermodynamic equation and the Semi-Lagrangian approach for the staggered level between 30 and 50 hPa and 1 January 12 h (UTC).

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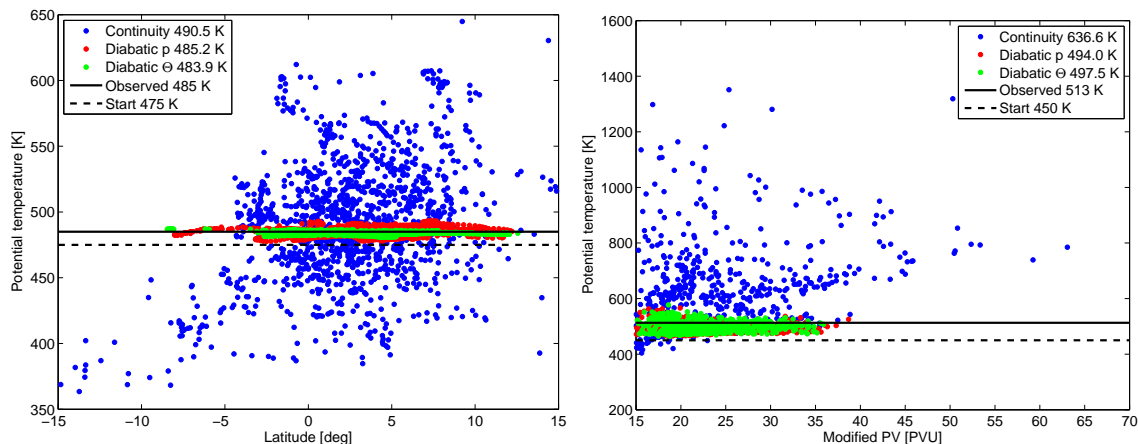


Fig. 2. Trajectory runs driven with different vertical wind fields. Left: Position of 1440 forward trajectories started at 1 January 2000 (00 h UTC) on the equator after 20 days, for winds from the continuity equation in pressure coordinates (blue dots), from the thermodynamic equation in pressure coordinates (red dots) and from heating rates in θ coordinates (green dots). Right: Position of backward trajectories on 26 November 1999 (12 h UTC) started at 450 K inside the polar vortex on a 2.5° grid on 5 March 2000 (12 h UTC).

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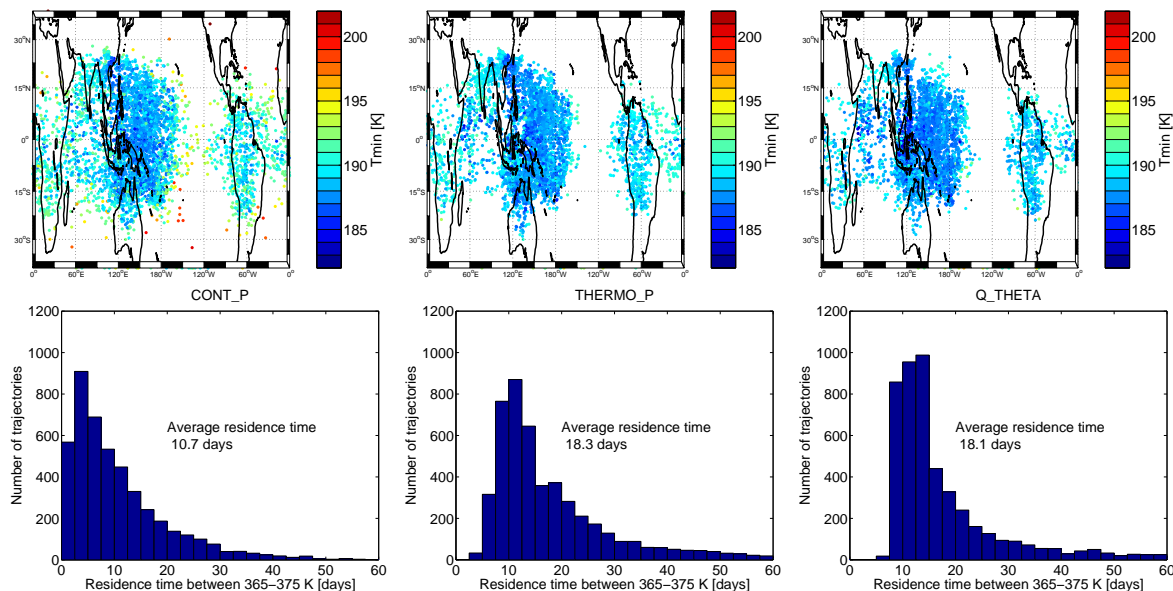


Fig. 3. Upper panel: Cold point locations and temperatures for the CONT-P, THERMO-P and Q-THETA winds and backward trajectories started on 29 February 2000 at 400 K on a $2^\circ \times 2^\circ$ grid between 30° N/S. Lower panel: Distribution of residence times between 365–375 K for the same winds.

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