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Application of local singularity in prospecting potential oil/gas Targets

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Abstract. Together with generalized self-similarity and the fractal spectrum, local singularity analysis has been introduced as one part of the new 3S principle and technique for mineral resource assessment based on multifractal modeling, which has been demonstrated to be useful for anomaly delineation. Local singularity is used in this paper to characterize the property of multifractal distribution patterns of geochemical indexes to delineate potential areas for oil/gas exploration using the advanced GeoDAS GIS technology. Geochemical data of four oil/gas indexes, consisting of acid-extracted methane (SC_1), ethane (SC_2), propane (SC_3), and secondary carbonate (ΔC), from 9637 soil samples amassed within a large area of 11.2×10^4 km² in the Songpan-Aba district, Sichuan Province, southwestern China, were analyzed. By eliminating the interference of geochemical oil/gas data with the method of media-modification and Kriging, the prospecting area defined by the local singularity model is better identified and the results show that the subareas with higher singularity exponents for the four oil/gas indexes are potential targets for oil/gas exploration. These areas in the shape of rings or half-rings are spatially associated with the location of the known producing drilling well in this area. The spatial relationship between the anomalies delineated by oil/gas geochemical data and distribution patterns of local singularity exponents is confirmed by using the stable isotope of $\delta^{13}C$.

1 Introduction

As one of the direct techniques used to prospect for petroleum resources, oil/gas geochemical exploration, from a geochemical point of view, can delineate the effective spaces and ranges of the oil/gas reservoirs and then appraise the

oil/gas potential of study regions. Among various kinds of oil/gas geochemical exploration methods, hydrocarbon acidolysis and the ΔC technique have attracted a lot of interest from many petroleum geologists. The analytical method for acid-extractable hydrocarbons occluded on surface soils was developed in the 1930s (Horvitz, 1939, 1972, 1985) and ΔC in soils was believed to be an effective technique for oil/gas geochemical exploration (Duchscherer, 1988). By analyzing the association of surface geochemical indicators with a deep gas pool, one can obviously obtain large numbers of surface geochemical tracks from deep gas accumulations which are closely related to the type and scale of the deep gas accumulation area. Since their early uses, the hydrocarbon acidolysis method and ΔC technique have become common in surface geochemical exploration and plenty of data derived from the two methods have been accumulated throughout the world. Nevertheless, because of diverse interference factors, such as geographical conditions, sampling media, and variations of soil composition, some geochemical signatures are not considered to be distinguishable from background signals with current methods used by the industry (Abrams, 2005). This could be one of the reasons why geochemical hydrocarbon exploration remains an unconventional approach in the petroleum industry and did not result in widely used prospecting methods for oil/gas data processing although geochemical hydrocarbon exploration was systematically studied back in 1929 (Davidson, 1994; Saunders et al., 1999). To improve the application of these data to hydrocarbon prospecting, many researchers have studied various data-processing methods since the 1990s, including interference elimination and anomaly recognition. However, the methods for anomaly recognition and interference elimination based on classical statistics (Horvitz, 1985) can not be used effectively and still restrain the extraction of valuable information for oil/gas discovery because the data of interest can not meet the prerequisites of some typical statistic methods, such as normal distributions of multi-source data; and

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usually it is hard to separate background from anomalies by probability analysis.

In recent years, with the development of fractal theory, fractal and multifractal methods have become gradually regarded as effective and efficient means to analyze spatial structures in oil fields, except for extensive application in metallic geochemical systems. Christopher and Paul (1995) discussed the frequency-size distribution of oil fields and Xie (2005) and Bao (2004) and Xie et al. (2005) presented the multifractal distribution patterns of different hydrocarbons in Tarim Basin, China. The concentration-area (C-A) multifractal model (Cheng et al., 1994) has been applied to anomaly recognition based on wavelet analysis and it is believed techniques based on fractals and multifractals have greatly improved the prediction capability of the existing data (Zhang et al., 2006).

As one new multifractal theory applied in geosciences, local singularity has been used to analyze the hydrothermal mineralization processes of elements and delineate the potential mineralization district in metallic geochemical fields (Cheng, 2006a), to map the distribution patterns of geochemical data analyzed from samples collected from surface media for mineral exploration (Cheng, 2000). As is generally known, metallic geochemical fields have some characteristics in common with petroleum regions, but there exist great discrepancies both in the mechanism of formation and in spatial structures between these two kinds of geochemical fields. What if we looked at the singularity patterns of oil/gas indexes and could the local singularity values help map the oil/gas anomalous trapping areas?

In this study, 9637 soil samples were taken from an area of 11.2×10^4 km² in the Songpan-Aba district, Sichuan Province, southwestern China, and four oil/gas geochemical indexes, i.e. acid-extracted methane (SC₁), ethane (SC₂), propane (SC₃), and secondary carbonate (Δ C), which are believed to be of great significance for oil/gas exploration (Duchscherer, 1988), were measured. The data was analyzed in order to recognize anomalous areas with the method of local singularity, which is available in an advanced GeoDAS system (Cheng, 2000). 119 isotope data ($\delta^{13}\text{C}$) were then used to characterize the relationship between chemical composition anomalies and distribution patterns of oil/gas indexes in surface soils.

2 Local singularity principle

Since the concept underlying the multifractals was originally introduced by Mandelbrot (1972, 1974), many kinds of fractal and multifractal models have been developed and applied in different scientific fields to characterize self-similar or self-affine measures (Schertzer and Lovejoy, 1991; Evertsz and Mandelbrot, 1992). Together with generalized self-similarity and fractal spectrum, local singularity has been introduced as one part of the new “singularity-similarity-

spectrum” (3S) principle and techniques for mineral resource assessment based on multifractal modeling, which has been demonstrated to be useful for singularity analysis and anomaly delineation (Cheng, 2006a,b).

Singularity can be defined mathematically as the point where conventional mathematical modeling breaks down. One example of a singularity in the geometry of space would be a “black hole”. From a geochemical point of view, singularity could be defined as one special phenomenon with the anomalous accumulation of materials and abrupt release of energy during a short period and within a narrow space, which could be characterized by multifractal models and could be quantitatively described as the following power-law relationship (Cheng, 2006b):

$$\mu_i(\varepsilon) \propto \varepsilon^{\alpha_i} \quad (1)$$

where \propto denotes proportionality and the measure $\mu_i(\varepsilon)$ denotes the total amount of material in the i -th box with box size ε ; and $\mu_i(\varepsilon)$ also could be expressed in an average density format as below (Cheng, 1999):

$$\mu_i(\varepsilon) \propto \varepsilon^2 \rho_i \quad (2)$$

and, the density of material in the space could be transformed as:

$$\rho_i = \varepsilon^{\alpha_i - 2} \quad (3)$$

where α_i is called the singularity exponent or local Hölder exponent (Evertsz and Mandelbrot, 1992), $\alpha_i - 2$ is the exponent of the power-law and value 2 in Eq. (2) and Eq. (3) is the Euclidean dimension of the 2-D boxes. As discussed above, when the material is evenly distributed in space, we will have $\alpha = 2$. Otherwise, for boxes relatively enriched with the material, $\mu_i(\varepsilon)$ will be larger than ε^2 . As we are mainly interested in the limit situation $\varepsilon \rightarrow 0$, we have $\varepsilon \ll 1$ and a larger $\mu_i(\varepsilon)$ means that local Hölder exponent α_i is less than 2. The smaller the α values are, the stronger the local enrichment of the materials is in corresponding boxes. That is to say, $\alpha < 2$ corresponds to local enrichment. Similarly, $\alpha > 2$ implies local depletion. Thus, if the singularity exponent values could be calculated and mapped, it will be very valuable to delineate the trapping areas of mineralization and oil/gas formation with association of spatial distribution patterns of singularity exponents. A method and the advanced GeoDAS GIS technical computer software has been developed (Cheng, 2000) to map the distribution of singularity based on geochemical data of samples collected from surface media such as soil, water, and till. The current paper will use GeoDAS to map the singularity distribution patterns and then to delineate the oil/gas potential areas for an oil/gas geochemical survey.

3 Geochemical data

Songpan-Aba Basin is situated in Southwest China, ranging $31^\circ 36' - 34^\circ 56'$ of latitude and $101^\circ - 105^\circ 10'$ of longitude,

Table 1. Table of basic descriptive statistics for geochemical oil/gas indexes in Songpa-Aba area, Sichuan Province, Southwestern China.

Index	SC ₁ ($\mu\text{l/kg}$)	SC ₂ ($\mu\text{l/kg}$)	SC ₃ ($\mu\text{l/kg}$)	ΔC (%)
No. of data	8951	8385	5837	8972
Mean	152.85	22.18	10.75	0.45
Medium	7.40	0.70	0.80	0.29
Minimum	0.40	0.10	0.10	0.04
Maximum	13073	5770	1998	6.26
Standard deviation	702.4	158.0	63.2	0.4
Skewness	9.46	15.92	13.70	3.31

**Fig. 1.** The landscape of different types of surface soils in Songpan-Aba district. Different shades of gray are representative of different sampling media: (1) Lacustrine deposits; (2) water-saturated marsh soil; (3) marsh soil; (4) Quaternary alluvial deposits; (5) poor soil overlying bed-rock; (6) forest or shrubby soil; and (7) fluvial deposits.

covering an area of $11.2 \times 10^4 \text{ km}^2$. South to the Sichuan basin, which is rich in natural gas, Songpan-Aba basin shares the same geological base with the Yangtze Platform and belongs to one part of the ancient Yangtze landmass. The basement of the Songpan-Aba basin consists of dark lithologic sequences of early Paleozoic age, over 5000 m in thickness, and a late Paleozoic carbonate landmass covered with marine sediments of the Triassic Period; and it is regarded as a new oil/gas prospecting area to be explored. The geographical features and hence the sampling media are quite diverse. On the basis of a detailed remote sensing interpretation, the sampling materials on the surface of the study area could be

classified into seven types: (1) lacustrine deposits; (2) water saturated marsh soil; (3) marsh soil; (4) Quaternary alluvial deposits; (5) poor soil over bed-rocks; (6) forest or shrubby soil; and (7) fluvial deposits (Fig. 1).

As one part of an ambitious oil/gas prospecting project, a surface geochemical survey had been conducted in the district in 2002 by the Training Center of Oil/Gas Geochemical Exploration in Hefei, China Petrochemical Corporation. Samples were taken on a grid of $1 \times 2 \text{ km}$ and 9637 were collected with 15 geochemical variables measured for each sample. Among these variables, acid-extractable methane (SC₁), ethane (SC₂), propane (SC₃), and secondary carbonate (ΔC)

are believed to be of great significance for oil/gas exploration (Duchscherer, 1988) and were used in this study to delineate the prospecting areas in this field. Since the concentrations of some indexes in certain samples are lower than the detection limit, the available data of various indexes are different and the basic statistic parameters of each index are listed in Table 1. It can be seen that the standard deviations of the four indexes are comparatively high and the maximum values are quite a lot larger than the medium and mean contents. This may be due to outliers of data existing in some samples.

4 Data processing

In Fig. 2 the minimum, medium, and maximum values of oil/gas indexes in different types of soils are displayed. The numbers in the abscissa represent the types of the soils and the vertical axis shows the contents of acid-extractable hydrocarbon. The value at the center of the small pane represents the medium content of each index, and the contents represented by the short lines above and below the pane stand for the maximum and minimum, respectively. The broken line is applied to show the content fluctuation of the index of interest by connecting the central dot in the small pane. It should be noted that different sampling media possess quite different contents of trapped light hydrocarbons. The highest medium values for all four hydrocarbons of study are from the water saturated marsh soils; and the contents of the indexes in the samples amassed from the marsh soils are also higher than the others except for those of the first type. But for the others, the content values are not so scattered but limited to narrow ranges. We do not present interpretation details here, but it can be seen that the characteristics within different types of soils are clearly different.

Figure 3a shows a geochemical contour map of original (non-preprocessing) contents of secondary carbonate (ΔC) performed by Surfer 8.0, using kriging with an exponential semivariogram model. Comparing Fig. 3a with Fig. 1, it is quite clear that the main anomalous area of high values shown in Fig. 3a approximately coincides with the areas where the second and third types of soils are distributed (Fig. 1). The other three indexes used in the study also show the same kind of distribution tendency. This kind of difference is significantly influenced by the physical and chemical characteristics of the soils and it is hard to ascertain the relationship between the anomalous area and the meaningful microseepage from underlying potential oil/gas reservoirs. In fact, many studies have indicated that soil interference with its hydrocarbon content is quite common and results from the dilution by sand in soils or from condensation in clays or carbonates (Horvitz, 1985; Ruan and Cheng, 1992). From this perspective, the original data set is not sufficient to characterize the true spatial structures of any underlying oil/gas pool and some sort of category normalized data preprocessing seems necessary.

In order to eliminate the medium interference related to the oil/gas geochemical field, a procedure of categorized standardization is employed in relation to each type of soil sample. The transformation of the original data set x_{ij} consists of the following two steps:

The first is to reduce the discrepancy among different types of soil samples by normalization. On the basis of the soil classification, each type of soil sampling data has been transformed by Eq. (4):

$$x'_{ij} = \frac{x_{ij} - \bar{x}_j}{s_j} \quad (4)$$

where x_{ij} is the value of variable j (content of a certain hydrocarbon) in sample i , \bar{x}_j and s_j represent the average value and standard deviation of variable j in each type of soil.

The second task is to eliminate negative values. Since the preceding transformation procedure generates a new data set x'_{ij} with some negative values, we therefore apply another standardization procedure to avoid negative data before log-transformation necessary for the calculation of local singularity exponents in the next sections. The standardization is achieved by:

$$x''_{ij} = \frac{x'_{ij} - x'_{j\min}}{x'_{j\max} - x'_{j\min}} \quad (5)$$

where $x'_{j\max}$ and $x'_{j\min}$ are the maximum and minimum values of the data set x'_{ij} for variable j in all samples, respectively; and the value which equals 0 was deleted directly. After this preprocessing, the subsequent data are all positive.

The contour map generated with the same procedure was also employed for the analysis of the new data set x''_{ij} for ΔC . Unexpectedly, a similar trend of geochemical distribution was obtained and is shown in Fig. 3b. The anomalies with high values of acid-extractable hydrocarbons are also located in the northern part of the study area. But it seems that the highly anomalous areas are smaller and the data distribute more evenly on the contour map of Fig. 3b, which may reflect that data preprocessing has removed some outliers from the data and has eliminated some kind of interference related to the soil compositions.

5 Results and discussion

The transformed values of acid-extractable methane (SC_1), ethane (SC_2), propane (SC_3), and secondary carbonate content (ΔC) from the soil samples were used for calculating and mapping of local singularities with the advanced GeODAS system. The half-window size r of each square window used for the calculation was set from 0.75 to 30.75 km with an interval of 1.5 km. As for edge effects, the local singularity exponents in the corners of every side of the area in study can not be calculated unless we would apply Kriging

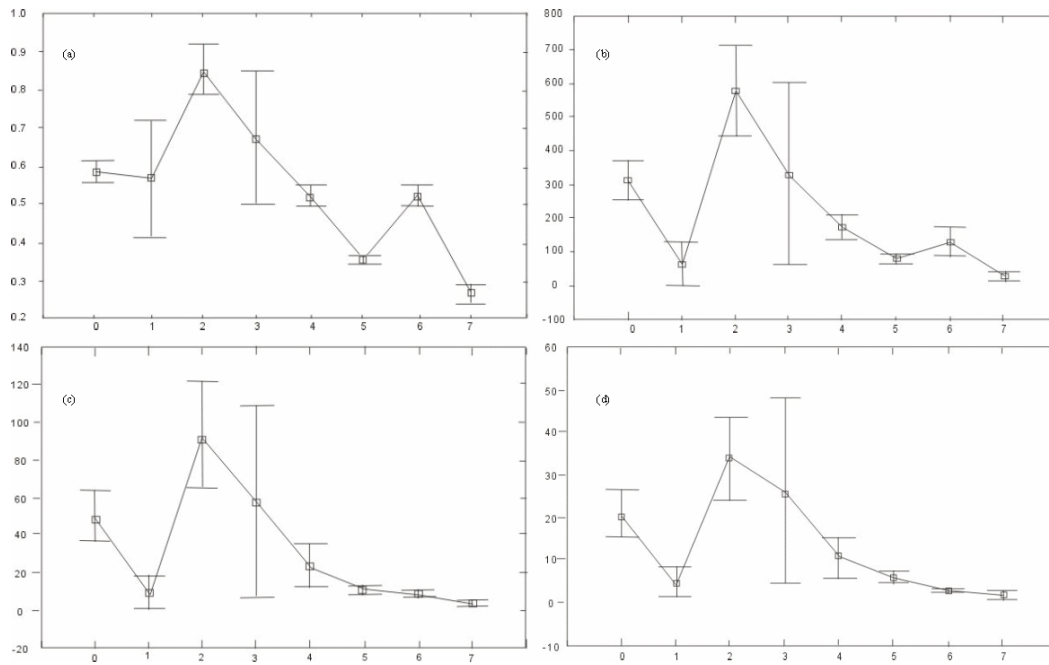


Fig. 2. The variations in abundance of oil/gas geochemical indexes in different types of soil: 0- Non-classified soil samples; 1- lacustrine deposits; 2- water saturated marsh soil; 3- marsh soil; 4- Quaternary alluvial deposits; 5- poor soil overlying bed-rock; 6- forest or shrubby soil; and 7- fluvial deposits. **(a)** ΔC ; **(b)** SC_1 ; **(c)** SC_2 ; **(d)** SC_3 . The numbers along the abscissa represent the types of the soils and the vertical axis shows the contents of acid-extractable hydrocarbon.

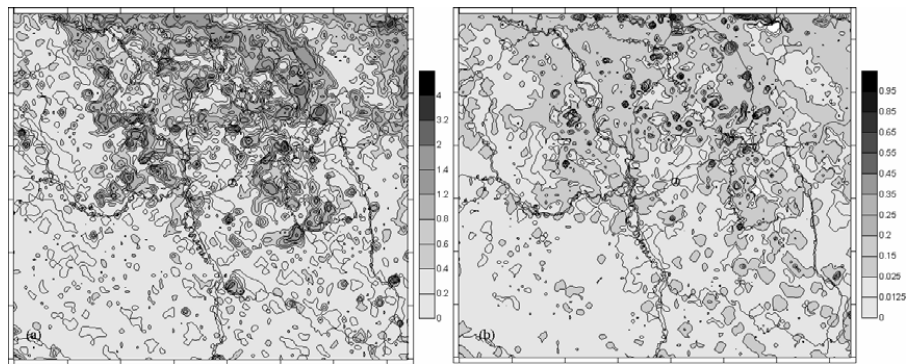


Fig. 3. 2-D structural contour map of secondary carbonate (ΔC) contents. **(a)** The contour map of ΔC with original data; **(b)** the isoline map of ΔC with categorization-standardized data. Black solid lines are the regional boundaries of different counties within the area of study. The small circle with triangle inside it near the center is location of the drilling well, Hongcan 1#.

or other data processing methods. Here we only used the real data measured from the samples and so every side of the original area was reduced by 30.75 km. Consequently, the area for which local singularity exponents were estimated is smaller than that in Figs. 2 and 3.

Figure 4 is the raster map of local singularities estimated by means of the windows-based method for the four oil/gas indexes of the study. The shades in Fig. 4 go from black to offwhite. The areas with α -value < 2 are shown as jet black pixels, the areas with an α -value larger than 2 as offwhite

pixels, and those with medium levels of α -value close to 2 as gray pixels. Mostly inside the areas with dark color, a dashed line has been drawn on the map that shows a ring-shape anomalous zone of NW-SE orientation, which can be divided into separate cinctures. The offwhite pixel areas compose first central cincture, the center of which is close to the site of the commercial drilling well, Hongcan 1#. The smaller α -value area outside the dashed line with jet black pixels was delineated as the outermost cincture, and the intermediate zone is between the off white central cinctures

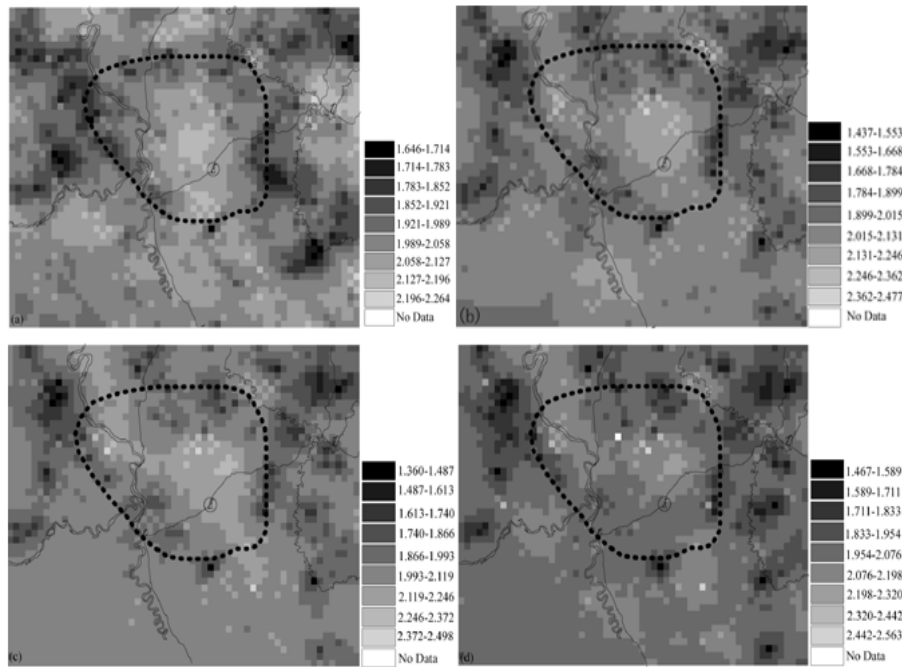


Fig. 4. Estimated singularity α -values by the windows-based method with GeoDAS: (a) ΔC ; (b) SC_1 ; (c) SC_2 ; (d) SC_3 . Dark colored patterns represent low values. Polygons enclosed by the dashed line represent the favored target area delineated by local singularity values. The small circle included in the center is the location of the drilling well, Hongcan 1#.

and the dashed line. The three cinctures change gradually outward from the center, as indicated by the shades of gray. This kind of α -value distribution pattern can be called a ring-shaped anomaly in surface geochemical exploration for oil and gas (Zhang et al., 1995). The inner cincture of the ring-type anomalous area is of stronger singularity (lower α -values) than outside the perimeter of the anomalous area. As explained above, strong singularity (lower α -values) may reflect strong accumulation of material, and on the contrary, relative depletion of material may show weak singularity (higher α -values). For major petroleum indicators in the oil/gas geochemical field, from the center to the border of the ring-shaped anomalous zone, the α -values decrease gradually.

$\delta^{13}C$ values of methane from 119 samples in the Songpan-Aba ring-type anomalous area (Fig. 5) range from -58.6 to 92.39% , with -20.60% on average, which is heavier than the $\delta^{13}C$ values of methane originating from both the Earth's surface and those associated with a biogenic gas contribution. Generally speaking, methane from the metamorphic reactions and degassing of the Earth's mantle typically shows a considerably heavier isotopic signature and the relative content of the $\delta^{13}C$ value is heavy, amounting to -40% , whereas the contents of supergenic and biogenic methanes will contain relatively lighter isotopic compositions and their $\delta^{13}C$ values would range from -70 to -60% on average (Stevens and Rust, 1982; Stevens and Engelkemeir, 1988; Kadir et al., 2005). In the central part of the anomalous area, the $\delta^{13}C$

values are mainly between -60 and -40% (Fig. 5); while in the marginal parts, they are greater than -40% . As for the non-anomalous area, there is not any obvious concentration range. In brief, mainly lighter value dots of $\delta^{13}C$ fall around the vicinity of Hongcan 1# and the center of the anomalous ring; and the dots on Fig. 5 with $\delta^{13}C$ values higher than -40% area distributed in a scattered fashion around the margin of the ring.

The ring-shaped anomaly is a special kind of phenomenon that commonly occurs in soils above many reservoirs (Ruan, 1992). In these reservoirs, hydrocarbons will migrate upwards in different ways, and the speed and strength of the migration changes according to their structural position. Together with the data of $\delta^{13}C$ values, the generating mechanism for the ring-shaped singularity anomaly shown in Fig. 4 can be depicted as follows:

At the initial stage of vertical seepage of oil/gas ingredients, representing the channel of hydrocarbon migration, pores in the porous media are nearly empty. With time, on top of the oil/gas reservoir, massive hydrocarbon compounds enter into an oxidization belt through vertical seepage and release of CO_2 , which will then react with calcareous minerals in the cap rock to form carbonates (Duchscherer, 1988). With the continuous accumulation of secondary carbonates, the channel for vertical migration will become jammed by the carbonates and some pores will be filled with oil and gas. Consequently, water will be driven out to the edge of the oil/gas reservoir. Usually, oil/gas diffuses upwards to the

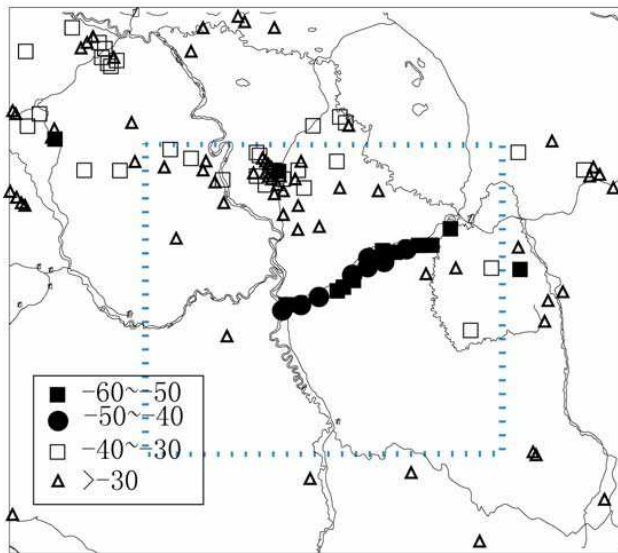


Fig. 5. The distribution of $\delta^{13}\text{C}$ values in Songpan-Aba district. The area delineated by the dashed line is as large as the area in Fig. 4.

surface due to differences in concentration. Under this condition, hydrocarbons migrate upwards to the surface with lower diffusion speed and accordingly the kinetic fractionation effect of isotopes will be stronger (Zhang et al., 1995), which results in lower $\delta^{13}\text{C}$ at the surface of the soil on top of the reservoir; i.e., the central part of the ring. As displayed in Fig. 5, the site where the lowest $\delta^{13}\text{C}$ value occurs is close to Hongcan 1#. The slow exchange of material will correspondingly lead to stronger fractionation of hydrocarbons with higher singularity (Fig. 4) in oil/gas/water systems.

Whereas at the margins of the reservoir, corresponding to the anomalous marginal zone, except diffusion, hydrocarbons and other oil/gas ingredients will continuously traverse the pores of the bedrocks and then migrate toward the surface together with oil-field water. In this case, the fast migration of hydrocarbons will result in weaker fractionation of isotopes and weaker singularity of hydrocarbons (Fig. 4). Thereby, often nearly reaching the surface, the carbon isotope composition of the highly concentrated methane will change slightly compared with its premigrated state, and thus the $\delta^{13}\text{C}$ values at the margins of the anomalous ring will be heavier than those at the ring center (Fig. 5).

In such a case, the hydrocarbon anomaly areas of lower α -values may be exactly at the edge of the underlying oil/gas reservoir, and the center of the anomaly ring's perimeter may coincide with the position of the oil/gas deposit. Therefore, Hongcan 1# is of great importance in the oil/gas prospecting in this area and we believe drilling close to it will bring success; and the delineated areas could be considered as favorable for detailed drilling and geological survey.

6 Conclusions

The application of the local singularity method to the oil/gas geochemical data demonstrates that the new multifractal theory has overcome some disadvantages of traditional spatial methods and therefore constitutes a powerful tool for extracting local hidden spatial information from oil/gas geochemical data and for predicting undiscovered natural resources. Through the technique of local singularity analysis using the advanced GeoDAS system, one can extract new local information from the patterns concerned and try to characterize the tendency of enrichment and depletion of oil/gas indexes defined by underlying hydrocarbons. The center of the anomalous area delineated by the local singularity method in the current paper coincides with the producing drilling well.

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