

Optimizing networks
and model error

P. J. Rayner

Optimizing CO₂ observing networks in the presence of model error: results from TransCom 3

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Abstract

We use a genetic algorithm to construct optimal observing networks of atmospheric CO₂ concentration for inverse determination of net sources. Optimal networks are those that produce a minimum in average posterior uncertainty plus a term representing the divergence among source estimates for different transport models. The addition of this last term modifies the choice of observing sites, leading to larger networks than would be chosen under the traditional estimated variance metric. Model-model differences behave like sub-grid heterogeneity and optimal networks try to average over some of this. The optimization does not, however, necessarily reject apparently difficult sites to model. Although the results are so conditioned on the experimental set-up that the specific networks chosen are unlikely to be the best choices in the real world, the counter-intuitive behaviour of the optimization suggests the model error contribution should be taken into account when designing observing networks. Finally we compare the flux and total uncertainty estimates from the optimal network with those from the TransCom 3 control case. The comparison suggests that the TransCom 3 control case is robust.

1. Introduction

Atmospheric tracer inversions, in which the atmospheric transport operator is inverted to deduce net sources from atmospheric concentration observations, have been a widely-used tool in carbon cycle research in recent years, (e.g. Tans et al., 1990; Rayner et al., 1999; Bousquet et al., 2000; Rödenbeck et al., 2003). Several previous studies (Rayner et al., 1996; Gloor et al., 2000; Patra and Maksyutov, 2002) have sought to suggest optimal extensions or reconfigurations of the atmospheric sampling network used in such studies. The general method was to calculate some quantity representing the uncertainty in estimates of net source. This quantity is a function of the choice of observing network (among other things). The authors then used an opti-

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mization procedure to minimize their chosen quantity with respect to the network. The studies were generally interested in optimal extensions to the network and so were considering stations where no data had yet been gathered. They relied on the general property of linear inverse problems that posterior uncertainties in unknowns do not rely on the values of data but only their error statistics. These error statistics are hard to infer even with data to analyze since the separation of signal and noise requires a statistical model of the observations, often chosen ad hoc and a priori. Gloor et al. (2000) showed that this choice of error model had a great impact on the choice of desirable locations.

The network design studies have not yet been able to offer specific advice on observational sites although they have been instructive about the behaviour of the observing system. The reason is twofold. Firstly, the network returned by any optimization depends critically on the numerical quantity we optimize; the answer depends on the question. This was shown by Rayner et al. (1996) who performed optimizations of two apparently similar quantities and suggested completely different networks. Secondly, the results of the network optimization studies depend heavily on the prior knowledge input to the procedure. This was demonstrated by Gloor et al. (2000) through the importance of the error model for observations. It is clear, too, that regions with low prior uncertainty will not be improved as much by additional observations as those with large uncertainties.

The network design studies have generally sought to minimize some distillation of the posterior uncertainty in estimated fluxes but there is another source of uncertainty in atmospheric inversions. The atmospheric transport models used both in the inversion and network optimization studies have different properties and produce different simulations of atmospheric transport. Throughout the history of their use, there has been a concern that these models may produce different inverse flux estimates. In a series of studies to probe this, Law et al. (1996) and Denning et al. (1999) (studying the forward problem) and Gurney et al. (2002, 2003) (studying the inverse problem) have looked at the impact of differences in modelled atmospheric transport. Gurney et al. (2002)

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compared two measures of uncertainty of estimated fluxes. The first was the conventional posterior uncertainty estimate produced by error propagation from the prior flux uncertainty and data uncertainty via the inverse transport operator. The second was the variance of estimated fluxes across the ensemble of transport models. Following their nomenclature we refer to these as the “within model” and “between model” uncertainties respectively. A reasonable measure of the total uncertainty of estimated fluxes is the quadratic sum of these two error terms. This assumes the two types of error are statistically independent, an assumption we can neither verify nor contradict. We use this sum throughout this paper and refer to it henceforth as the “total uncertainty”.

Gurney et al. (2002) found that, for most regions, within-model uncertainty dominated between-model uncertainty. They drew the reasonable inference from this, that additional data would aid the constraint of estimated fluxes by reducing total uncertainty. It was not, however, the role of those studies to address this question directly. Any additional stations may have been so difficult to model that the between model uncertainty would increase more than the within model uncertainty was decreased. Investigating these possibilities is the role of the present paper.

The outline of the paper is as follows. In Sect. 2 we describe the combination of the genetic algorithm (GA) and synthesis inversion. Section 3 describes a series of networks optimized under different conditions, comparing them with the TransCom 3 network of Gurney et al. (2002). Section 4 compares the fluxes computed from the optimized network with those from Gurney et al. (2002).

2. Methodology

The network optimization procedure requires two components, an inversion algorithm to calculate the score for a given network under our chosen metric and an optimization procedure to minimize this quantity with respect to the choice of network. The inversion algorithm is exactly that of Gurney et al. (2003) and the same as for Gurney et al. (2002) with the addition of one extra transport model, making a total of 17. See those

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papers for details of participating models. The inversion is simple and computationally inexpensive since it estimates long-term mean sources from long-term mean data. This makes the set-up a good candidate for the genetic algorithm where many repeats of the scoring calculation must be performed.

5 We are interested in two quantities calculated by the inversion procedure,

within uncertainty = $\overline{\text{trace}(\mathbf{C}_S)}$ (1)

where \mathbf{C}_S is the posterior covariance matrix of source estimates for the 22 regions in the inversion and the overbar is the average across the ensemble of models,

between uncertainty = $\sum_{i=1}^{22} \text{Var}(S_i)$ (2)

10 where S_i is the posterior source estimate for region i and Var represents the variance over the ensemble of models. The total uncertainty is the sum of these two terms.

Genetic algorithms are one of the classes of stochastic optimization procedures used for nonlinear models. The term “model” here refers to any numerical algorithm which calculates an output as a function of inputs. In our case, the model calculates measures of uncertainty as a function of a set of station locations.

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Genetic algorithms seek to optimize their objective function not by improving a single solution but rather by improving an overall population. Improvements are made by seeking optimal combinations of members of this population and by adding random changes to this population. In this sense they duplicate the pairwise reproduction and mutation seen in many biological systems. For a short on-line introduction see <http://csep1.phy.ornl.gov/CSEP/MO/MO.html> and references contained therein. Genetic algorithms exist in many forms but have a few general features

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- the algorithm maintains a population of potential solutions
- a given member of the population is described by a list of parameter values. In our case these are integers referring to an indexed list of possible observing sites.

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There are 110 possible observing sites in this study so each member consists of a list of integers in the range 1–110.

- The population is initialized with a set of random lists.
- members of the population will
 1. Exchange parameter values pairwise (termed crossing-over).
 2. Have their parameter values randomly changed (mutate).
 3. Be culled or compete according to some fitness criterion based on the cost function we are optimizing.
 4. Be cloned or otherwise reproduce to rebuild the population after culling,
- The above four processes constitute one step of the genetic algorithm.
- the algorithm iterates allowing evolution of the population towards an optimum value of the fitness criterion.

Each of the four parts of the algorithm can be implemented in various ways. We detail the particular implementation of each step here. The probability of two members crossing over (analogous to breeding), mutation rates and the mechanism by which members of the population compete are all chosen by the implementer of the algorithm and choices depend on the properties of the cost function. In the simple implementation used here cross-over is implemented by first randomly pairing all members of the population then deciding whether to interchange information according to a random decision $x \in U(0, 1) < p_x$ where p_x is the cross-over probability and $U(0, 1)$ is the uniform probability distribution on $[0, 1]$. Once cross-over is chosen, the two original members are replaced with offspring that have pairwise random combinations of their parameters. For each parameter offspring 1 has the value from parent 1 or 2 with 50% probability and offspring 2 has the value from the other parent.

For the mutation step we examine each parameter in each member of the population. Again we choose a uniformly distributed pseudorandom number and, if less than the

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specified mutation rate, we replace the parameter value with a value chosen at random from the set of possible values.

In the culling step we first sort the population according to their generated values of the cost function. We then assign a fitness F to each according to

$$F = 1 - \frac{r - 0.5}{N} \quad (3)$$

where r is the ordinal ranking of the member and N is the population size. We then delete the member according to the rule

$$x \in U(0, 1) > F \quad (4)$$

Thus lower ranked members (with respect to the cost function) are more likely to be culled. It is noteworthy that no member is completely safe from culling since $F \neq 1$.

On average, each cull step will remove half the population and this must be replaced. For this we choose, at random, one of the remaining members of the population. If a random number from $U(0, 1)$ is less than the fitness calculated from Eq. (3) we copy this member to replace one of the culled members. This process continues until the population is refilled. Sampling is without replacement so that a member with high fitness may be copied several times.

In general the method requires a trade-off between strong enough selection to allow convergence to an optimal solution and maintaining enough diversity to avoid getting stuck in a local extremum. In our case this trade-off is performed by tuning the mutation rate. The other trade-offs are computational, the population size and the number of iterations. A larger population is always safer since it means higher diversity is maintained while still giving very fit members a chance to propagate (since for large N , $F \rightarrow 1$ for the fittest member). For our case we choose a population of 200 using 500 iterations. One optimization takes about six hours on a single Linux PC.

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2.1. Specific set-up

We assign each potential observing site an integer value. Sites considered are the 110 potentially used by Gurney et al. (2002). They chose 76 of these which met various criteria. The sites and data are taken from GLOBALVIEW-CO₂ (2001). Each population member therefore consists of a list of these integer values. Data values and uncertainties are constructed by the same algorithm as in Gurney et al. (2002). Importantly, one station can occur many times in an optimal list but we do not include the correction to data uncertainty to account for this as used by Gurney et al. (2002). Therefore the second station at a location contributes as much information as the first. We also wish to test the possibility that the current network is too large to optimize total uncertainty. We therefore add 20 “null” stations which have zero responses to sources from all regions.

Values for the tunable parameters in the GA are shown in Table 1.

p_m is of particular interest. Recall that it represents the probability of a given value being altered. A simple binomial probability calculation demonstrates that, for our control 76 station case, this value of p_m yields a probability of 54% that a given member will be altered in the mutation step and a 19% probability that a given member will have more than one value altered. This is much higher than usual implementations of a GA but our tests below found it to be an optimal value.

2.2. Testing the algorithm

Usually it is hard to design a test for a GA since we rarely know the optimal value. We could, however, construct a test here. The between-model case is uninteresting on its own but does provide a useful test. In a Bayesian inversion this metric will be minimized if the responses approach zero. The inclusion of the null stations in our potential network allowed us to test this. After 500 iterations the 76 station case produced a between-model variance of $0.01 \text{ (GtCy}^{-1}\text{)}^2$. There were still three real stations left, in the optimal lists, the rest all being null stations. We regarded this as acceptable and used this configuration throughout the real experiments.

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3. Experiments

We performed experiments with two different sized networks, the 76-station network as a comparison with the network of [Gurney et al. \(2002\)](#) and a 110-station network which is capable of covering the full list of available stations. In both cases we optimized separately for total uncertainty or within model uncertainty. The results are summarized in [Table 2](#) and the four optimized networks are shown in [Fig. 1](#) and [Fig. 2](#).

The first thing to note about the various optimal networks is their relatively small size, especially for the “within” cases. This is largely a function of the resolution of the sources. To constrain 22 regions it is required to have at least 22 independent measurements. There is a tendency therefore for the “within” optimizations to gravitate to a selection of 22 sites that best constrain the 22 regions. In tests with a single model this was almost achieved, with networks of 26 sites being a common outcome. The complication of multiple models is that optimal choices for one model may not hold for others so that the optimization will choose more sites to give the strongest average constraint across all models. This was noted by [Patra et al. \(2003\)](#) who also showed an increase in chosen sites when several models were considered. That study could not duplicate our result since the optimization technique was not allowed to choose sites multiple times and the study was of additions to the current network rather than construction of networks from scratch. That study did demonstrate the dependence of the size of the network on the resolution of the source description. They noted a spreading of stations as they moved from the 22 regions used in this study to a higher resolution description with 42 land regions rather than the 11 land regions used here.

It is, a priori, unclear what to expect when moving from optimizing within to total uncertainty. If there is strong disagreement among model transport fields then we may expect a further shrinking of the network as some sites, although offering strong constraint on the fluxes, give highly divergent results from one model to another. In fact we observe the opposite, with a growth in the size of the network for both the 76 and 110 station cases. It seems, in fact, that the optimization must counteract the model-model

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divergence caused by particular stations by averaging across a broader dataset. In that sense we may regard the model-model differences as some kind of heterogeneity. This is most clearly seen in Fig. 1 for Western Europe. Here the “within” optimization chose two sites while the “total” chose six. There is also some dispersal of sites around East Asia and the Pacific. From Table 2 it is clear that this dispersal produces a substantial reduction in “total” uncertainty without a large increase in “within” uncertainty. It would appear, therefore, that aggressive optimization of “within” uncertainty may expose one to substantial model-model variability. This is acceptable if one has a series of models with which to perform inversions but this will not, generally, be the case. The case holds, even more dramatically, for the 110-site network. Here the lowest “within” uncertainty in Table 2 corresponds to the largest “total” uncertainty. Although the specifics of these results will not, as discussed earlier, hold for a different set-up, we expect that this behaviour, with network diversity acting to reduce large model-model variations in flux estimates, is a general result.

It is important to note that optimal networks do not include any of the “null” stations. This demonstrates that, even for the larger network size, the available information content is not saturated. This is the direct test of the inference drawn by Gurney et al. (2002) that extra measurements would reduce uncertainty, even when that uncertainty included a component caused by model-model variations. This result would stand even more strongly if we tried to solve for sources at greater spatial resolution.

In general, the “within” optimizations choose sites within or near each region to minimize atmospheric diffusion and hence maximize signals. Where there are no nearby stations well-connected by atmospheric flow to a source region this can produce some surprising choices. For example, both the within-76 and within-110 optimizations heavily weight the upper levels of the Cape Grim aircraft profile. This site has the largest response to the South American source region of the available sites. The weakness of the constraint requires the optimization to invest many measurements at the site to simulate a high precision measurement, capable of seeing the small signals from such a distant source region. Rather than a comment on the utility of this site, such a choice

points out the deficiencies in the rest of the network, with no other measurement site providing a good constraint on South America.

The method we have used for the optimization of total uncertainty relies on the existence of real data at all potential observing sites. This is not particularly useful for planning a network. It is more useful if we can predict some of the impact of model-model variations using the properties of the response functions themselves. As an example, we consider three sites which are strongly favoured in the “within” optimization but do not appear in the “total” case. These are the Easter Island (EIC, 27° S, 109° W) (3 times), Izana, Canary Islands (IZO, 28° N, 16° W) (4 times) and Key Biscayne, Florida (KEY, 26° N, 80° W) (4 times) sites. These sites must contribute considerably to model-model differences in flux estimates. They can do this in one of two ways. Either their responses to the first-guess or presubtracted fields can vary widely or else their response functions can vary widely. To test the relative importance of these differences we calculate, for all sources at all sites, the standard deviation of the response functions across the ensemble of models.

For two of these stations the case is clear. EIC has the largest standard deviation in the response to the South Pacific source region among all the 110 potential sites. Thus it is quite likely to be removed when model-model differences influence the optimal choice of stations. Slightly less dramatically KEY has the largest standard deviation in its response to the North Atlantic source of any station included in the choices for the “within” optimization. It is, unsurprisingly, removed in the “total” optimization.

The case for the high-altitude site, IZO, is less clear. We analyzed the contribution to the “between” uncertainty from each region in the “within-76” network in an attempt to analyze the impact of this station. The largest contributions were made by the Tropical Africa and Temperate Eurasia regions. When we removed the IZO site from the network, the “between” uncertainty reduced considerably, almost entirely because of a reduction in the contribution from Tropical Africa. This is not simply related, as with the other sites, to the variation in the response to this region at IZO. This is actually relatively small. However the overall constraint on this region from the network is also

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small, leaving the inversion more susceptible to small model-model differences. It appears that, while the variation in model response at a site is a reasonable guide to its influence on model-model differences in inversions, we must keep in mind the potential moderating role of other sites. This highlights the risk of relying on single sites to constrain regions, consistent with the general findings of this study.

4. TransCom 3 comparison

In Sect. 3 we saw that the conclusion of Gurney et al. (2002), that new measurements would provide a useful constraint on fluxes, was robust. We can also ask whether the particular flux distribution inferred in that paper was significantly different from one with minimum total uncertainty. Figure 3 shows such a comparison. Comparing, first, the error bars for both the optimal and TransCom 3 networks we notice relatively little reduction in total uncertainty. This is also evident from Table 2, which shows that the TransCom 3 network is nearly optimal with respect to total uncertainty. Note that, because the optimization is carried out for the globally summed uncertainty, there is no requirement that every region have its uncertainty reduced relative to the TransCom 3 case. Notwithstanding this, there are few regions where uncertainty is actually increased.

Comparison of the predicted fluxes themselves also yields only small differences between the two inverse calculations, especially if one normalizes the differences by the total uncertainty. This can be seen visually by considering the overlap of the error bars for each region. In most cases the error bars for each network include the central estimate for the other network. We should note that since the error bar represents one standard deviation we should expect some estimates to differ at this level. There are four regions of apparently significant difference: the Southern Ocean, Australasia, the West Pacific and the Tropical Indian Ocean. Most of these are due to removal of specific stations between the TransCom 3 and total-76 networks, e.g. the anomalous Darwin station. Sensitivity of the TransCom 3 inversion to this station has previously

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been noted by [Law et al. \(2003\)](#). One change is due to more systematic influences. The reduction of the Southern Ocean sink, already noted by [Gurney et al. \(2002\)](#), is strengthened in our optimal network. This occurs despite the great reduction in station density in this region. [Roy et al. \(2003\)](#) have noted that the reduction in Southern Ocean sink (relative to the prior) occurs even when almost all atmospheric observations are removed from the high southern latitudes. They conclude that the reduction in Southern Ocean sink is required to match large-scale atmospheric concentration gradients rather than particular local observations. The result of the present study suggests this result is also robust to the choice of atmospheric transport model.

5. Conclusions

We have extended previous network optimization studies to include the impact of model-model variations in transport on inversion estimates. We find that network optimizations generally choose quite small networks when optimizing only for the predicted uncertainty, concentrating on those sites that offer the strongest constraint. When model-model differences are considered, the optimization tries to average out some of the differences in transport by choosing more extensive networks, balancing the strength of constraint with the variations in transport. For the network sizes considered here the optimization always wishes to use as many sites as possible, confirming the conclusion of the TransCom 3 study that inversions are data not transport limited. We also find that the general distribution of fluxes predicted in that study is robust to our minimum uncertainty metric, and that the network used in the TransCom 3 study is quite good under this metric. Finally we find that model-model variations in responses at a particular site are a reasonable predictor of the suitability of a site under this total uncertainty metric however this breaks down when regions are very poorly constrained.

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TransCom 3 project and the global CO₂ measurement community who provided the various input data for this study.

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Table 1. Optimization parameters for genetic algorithm

Parameter	Description	Value
N_{pop}	Population size	200
p_x	Cross-over probability	0.2
p_m	Mutation rate	0.01
N_{iter}	Number of iterations	500

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Table 2. Uncertainty metrics in $(\text{GtCy}^{-1})^2$ for various optimized networks. The number at the end of the name is the possible number of sites in each network, the second column is the number of distinct sites chosen. In each case the bold-face number indicates the metric for which the network was optimized. The TransCom 3 control is also included for comparison.

Name	$N_{distinct}$	Within	Between	Total
Total-76	40	6.26	1.96	8.22
Within-76	35	5.33	6.11	11.44
Total-110	46	5.77	2.10	7.87
Within-110	38	4.66	7.20	11.86
TransCom 3	62	7.05	3.27	10.32

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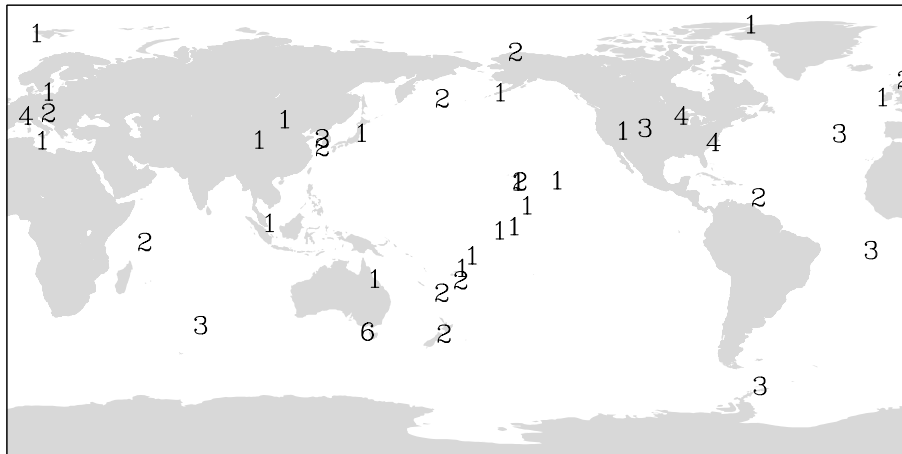
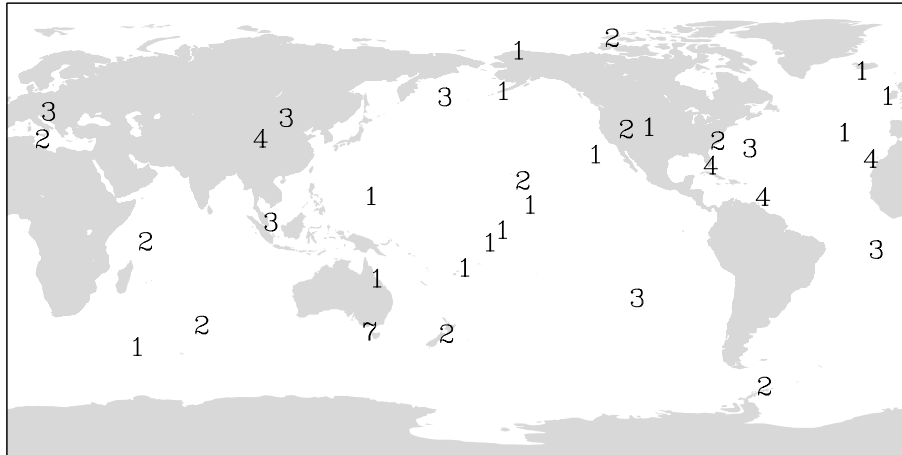


Fig. 1. Optimized networks for within-model **(a)** and total **(b)** uncertainty for a 76-site network. Numbers indicate the number of times the site is included.

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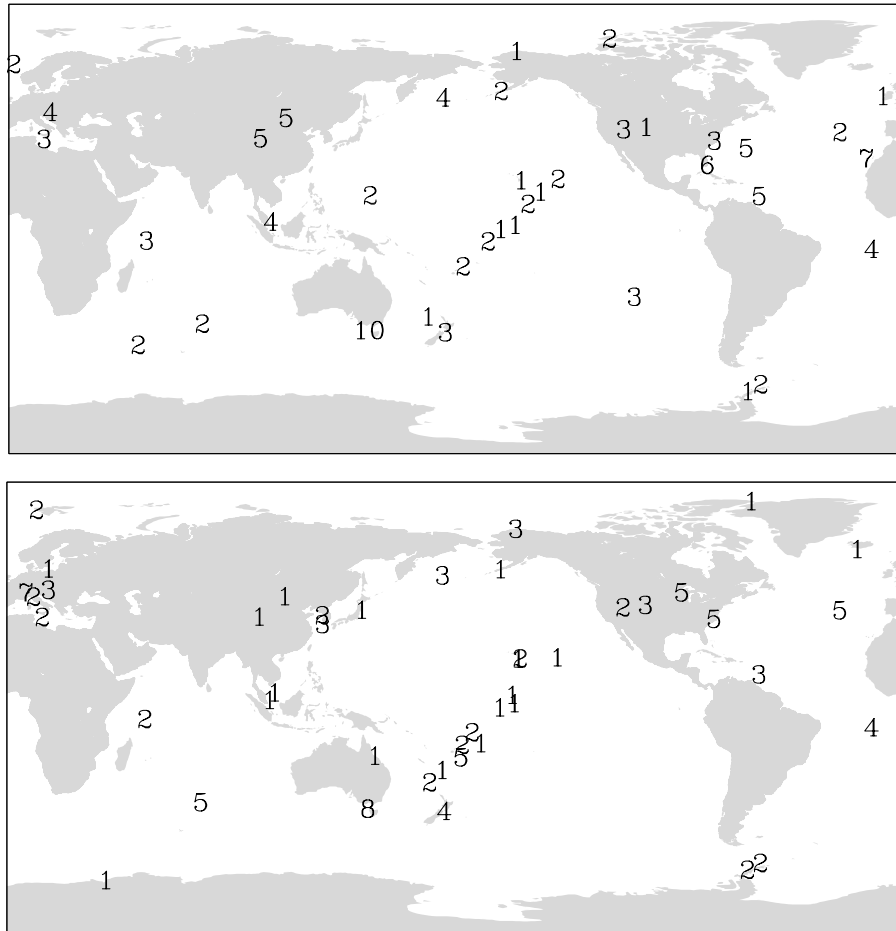


Fig. 2. Optimized networks for within-model (a) and total (b) uncertainty for a 110-site network. Numbers indicate the number of times the site is included.

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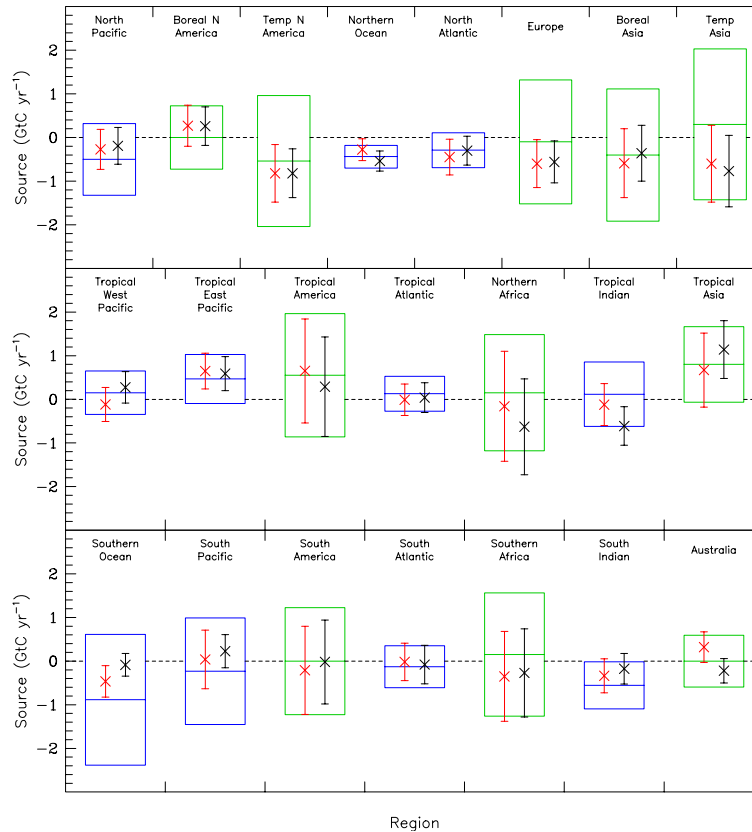


Fig. 3. Estimated fluxes and “total” uncertainty (GtC yr^{-1}) for the TransCom 3 (left) and total-76 (right) networks. The box shows the prior uncertainty, the horizontal bar the prior estimate. For each network the cross shows the predicted estimate and the error bar the one standard deviation total uncertainty.

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