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framework for
aerosols and clouds,
Part 1**

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Kinetic model framework for aerosol and cloud surface chemistry and gas-particle interactions: Part 1 – general equations, parameters, and terminology

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Abstract

Aerosols and clouds play central roles in atmospheric chemistry and physics, climate, air pollution, and public health. The mechanistic understanding and predictability of aerosol and cloud properties, interactions, transformations, and effects are, however, still very limited. This is due not only to the limited availability of measurement data, but also to the limited applicability and compatibility of model formalisms used for the analysis, interpretation, and description of heterogeneous and multiphase processes. To support the investigation and elucidation of atmospheric aerosol and cloud surface chemistry and gas-particle interactions, we present a comprehensive kinetic model framework with consistent and unambiguous terminology and universally applicable rate equations and parameters. It allows to describe mass transport and chemical reactions at the gas-particle interface and to link aerosol and cloud surface processes with gas phase and particle bulk processes in systems with multiple chemical components and competing physicochemical processes.

The key elements and essential aspects of the presented framework are: a simple and descriptive double-layer surface model (sorption layer and quasi-static layer); straightforward flux-based mass balance and rate equations; clear separation of mass transport and chemical reactions; well-defined rate parameters (uptake and accommodation coefficients, reaction and transport rate coefficients); clear distinction between gas phase, gas-surface, and surface-bulk transport (gas phase diffusion correction, surface and bulk accommodation); clear distinction between gas-surface, surface layer, and surface-bulk reactions (Langmuir-Hinshelwood and Eley-Rideal mechanisms); mechanistic description of concentration and time dependencies; flexible inclusion/omission of chemical species and physicochemical processes; flexible convolution/deconvolution of species and processes; and full compatibility with traditional resistor model formulations.

Exemplary practical applications and model calculations illustrating the relevance of the above aspects will be presented in a companion paper (Ammann and Pöschl,

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2005). We expect that the presented model framework will serve as a useful tool and basis for experimental and theoretical studies investigating and describing atmospheric aerosol and cloud surface chemistry and gas-particle interactions. In particular, it is meant to support the planning and design of laboratory experiments for the elucidation and determination of kinetic parameters; the establishment, evaluation, and quality assurance of comprehensive and self-consistent collections of rate parameters; and the development of detailed master mechanisms for process models and the derivation of simplified but yet realistic parameterizations for atmospheric and climate models.

1. Introduction

Aerosols and clouds play central roles in atmospheric chemistry and physics, climate, air pollution, and public health. They influence the Earth's energy budget by scattering and absorption of radiation, they regulate the hydrological cycle, and they affect the abundance of trace gases via heterogeneous chemical reactions and other multiphase processes (Andreae and Crutzen, 1997; Ravishankara, 1997; Seinfeld and Pandis, 1998; Waibel et al., 1999; Finlayson-Pitts and Pitts, 2000; Ramanathan et al., 2001; Ramaswamy et al., 2001; Rudich, 2003; Mikhailov et al., 2004; Kulmala et al., 2004; Kanakidou et al., 2005; Lohmann and Feichter, 2005). Moreover, aerosols can cause respiratory, cardiovascular, and allergic diseases when inhaled and deposited in the human respiratory tract (Finlayson-Pitts and Pitts, 1997; Finlayson-Pitts and Pitts, 2000; Katsouyanni et al., 2001; Pope et al., 2002; Pöschl, 2002a; Bömmel et al., 2003; Gauderman et al., 2004; Franze et al., 2005; and references therein). The quantification of aerosol and cloud effects and the assessment of natural and anthropogenic influencing factors are among the key topics of current research on the environment and public health. The mechanistic understanding and predictability of aerosol and cloud properties, interactions, and transformation (chemical and physical aging) are, however, still very limited.

Atmospheric aerosols and clouds are complex multiphase systems consisting of a

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wide variety of organic and inorganic chemical compounds - multiple main components and hundreds of trace substances - in gaseous, liquid, and solid form (Seinfeld and Pandis, 1998; Finlayson-Pitts and Pitts, 2000; McMurry, 2000; Raes et al., 2000; Matta et al., 2003; Maßling et al., 2003; Pöschl, 2003; Sciare et al., 2003; Smolik et al., 2003; Schauer et al., 2003, 2004; Schneider et al., 2004; Putaud et al., 2004a, b).

Chemical reactions proceed both at the surface as well as in the bulk of solid and liquid particles, influencing atmospheric gas phase chemistry as well as the physicochemical properties and effects of the particles (Ravishankara, 1997; Atkinson et al., 1997; Seinfeld and Pandis, 1998; Finlayson-Pitts and Pitts, 2000; Pöschl et al., 2001; Sander et al., 2002; Ammann et al., 2003; Reid and Sayer, 2003; Rudich, 2003; and references therein). For example, they lead to the formation of reactive halogen species and depletion of ozone in the stratosphere and marine boundary layer (Austin et al., 2003; Sander et al., 2003; Pszenny et al., 2004), to the decomposition of N_2O_5 (Meilinger et al., 2002; Stewart et al., 2004), and have been extensively discussed as a source for HONO (Broske et al., 2004; and references therein). On the other hand, chemical aging of aerosol particles generally decreases their reactivity, increases their hygroscopicity and cloud condensation activity (Pöschl et al., 2001; Kumar et al., 2003; Rudich, 2003; Asad et al., 2004; Broekhuizen et al., 2004), and can change their optical properties (Gelencser et al., 2003). Heterogeneous oxidation and nitration reactions lead to the formation or degradation of hazardous aerosol components (Finlayson-Pitts and Pitts, 1997; Letzel et al., 2001; Pöschl, 2002a; Schauer et al., 2004; Franze et al., 2005), they cause artifacts upon sampling and analysis of air particulate matter (Finlayson-Pitts and Pitts, 2000; Schauer et al., 2003), and they play a major role in technical processes and devices for the control of combustion aerosol emissions (Su et al., 2004; Messerer et al., 2004, 2005¹).

Efficient investigation and description of these multiphase and multicomponent pro-

¹Messerer, A., Niessner, R., and Pöschl, U.: Comprehensive characterization of model and real diesel soot oxidation and gasification by nitrogen oxides and oxygen under diesel engine exhaust conditions, Carbon, submitted, 2005.

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cesses in laboratory, field, and model studies require consistent terminologies and universally applicable mathematical formalisms. Such formalisms have been presented and are widely applied for reactions occurring in the bulk of liquid atmospheric particles (Kolb et al., 1995; Sander, 1999; Finlayson-Pitts and Pitts, 2000; and references therein). The formalisms presented and applied for the description of particle surface reactions, however, generally have been limited to specific reaction systems and conditions: liquid water, water ice, acid hydrates, soot, or mineral dust; fresh or aged surfaces; low or high reactant concentrations; transient or (quasi-)steady-state conditions; limited numbers of chemical species and reactions; etc. (e.g. Jayne et al., 1990; Davidovits et al., 1991; Mozurkewich, 1993; Tabazadeh and Turco, 1993; Tabor et al., 1994; Davidovits et al., 1995; Kolb et al., 1995; Nathanson et al., 1996; Atkinson et al., 1997; Carslaw and Peter, 1997; Hanson, 1997; Jayne et al., 1997; Pöschl et al., 1998; Bertram et al., 2001; Clegg and Abbatt, 2001; Grassian, 2001; Katrib et al., 2001; Pöschl et al., 2001; Vesala et al., 2001; Adams et al., 2002; Hynes et al., 2002; Remorov et al., 2002; Sander et al., 2002; Smith et al., 2002; Worsnop et al., 2002; Ammann et al., 2003; da Rosa et al., 2003; Djikaev and Tabazadeh, 2003; Folkers et al., 2003; Reid and Sayer, 2003; Rudich, 2003; Strekowski et al., 2003; Frinak et al., 2004; Thornberry and Abbatt, 2004; and references therein). The different and sometimes inconsistent rate equations, parameters, and terminologies make it hard to compare and to extrapolate the results of different studies over the wide range of reaction conditions relevant for the atmosphere on the one hand, and for laboratory experiments and technical processes on the other.

To provide a basis for consistent description of chemical reactions and mass transport at the surface and in the bulk of liquid and solid atmospheric particles, we have developed a comprehensive model framework for aerosol and cloud surface chemistry and gas-particle interactions. In analogy to well-established formalisms of gas phase chemistry, it shall support the establishment and evaluation of comprehensive and self-consistent collections of rate parameters (Atkinson et al., 1997; Sander et al., 2002; Atkinson et al., 2004), the development of detailed master mechanisms (Saunders et

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al., 2003; Jenkin et al., 2003), and the derivation of simplified but realistic mechanisms and parameterisations for large scale atmospheric and climate models (Pöschl et al., 2000; von Kuhlmann et al., 2004; Spracklen et al., 2005).

5 The presented model framework builds on the basic kinetic theories of gases, condensed phases, and interfaces, and it combines concepts, rate equations, and rate parameters developed and applied in surface science and aerosol research. It is meant to be sufficiently general and flexible to allow efficient description of both simple and complex systems, to enable the inclusion of more elaborate concepts and formalisms of current and future atmospheric research and surface science, and to bridge the gaps
10 between atmospheric and technical processes as well as between modeling and experimental studies. Most likely not all of the rate parameters introduced below will be available for all species and systems of atmospheric relevance, but in analogy to the development of detailed master mechanisms of atmospheric gas phase chemistry they can be determined for certain model species and systems and extrapolated for others.
15 The presented terminology and formalisms shall help to develop a clear picture of the measurements, calculations, and assumptions which are required for a mechanistic description and prediction of aerosol surface chemistry and gas-particle interactions.

The general concept, terminology, and rate equations are outlined in the following sections of this manuscript. Exemplary practical applications including analytical and
20 numerical solutions for different systems under transient and (quasi-)steady-state conditions will be presented in a companion paper (Ammann and Pöschl, 2005).

2. Gas phase composition and processes

2.1. Gas kinetic fluxes and uptake coefficients

25 In atmospheric chemistry the net uptake of gases by aerosol and cloud particles is usually described by an uptake coefficient, which is defined as the number of gas molecules taken up by the particle divided by the number of gas molecules impinging

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onto the particle surface (here and below the term “molecule” includes atomic, ionic, and radical species). In terms of molecular fluxes, the uptake coefficient for a gas species X_i , γ_{X_i} , can be expressed as the ratio between the net flux of X_i from the gas phase to the condensed phase, J_{net,X_i} , and the gas kinetic flux of X_i colliding with the surface, J_{coll,X_i} (number of molecules per unit area and unit time):

$$\gamma_{X_i} = \frac{J_{\text{net},X_i}}{J_{\text{coll},X_i}} \quad (1)$$

Equation (1) is fully compatible with traditional verbal definitions of the uptake coefficient, but J_{net,X_i} and γ_{X_i} can assume negative values if the particle acts as a net source of X_i , which will be discussed below. For a list of symbols and SI units see Appendix A.

Based on gas kinetic theory, the flux of collisions of gas species X_i with a surface can be expressed as

$$J_{\text{coll},X_i} = [X_i]_{\text{gs}} \omega_{X_i} / 4 \quad (2)$$

$[X_i]_{\text{gs}}$ is the gas phase concentration of X_i close the surface, i.e. about one mean free path off the surface (see Sect. 2.2), and ω_{X_i} is its mean thermal velocity given by $\omega_{X_i} = (8RT/(\pi M_{X_i}))^{1/2}$, where M_{X_i} is the molar mass of X_i , R is the gas constant, and T is the absolute temperature.

Assuming that the gas phase concentration of X_i is homogeneous throughout the investigated system, the flux of surface collisions can be approximated by the average gas kinetic flux, $J_{\text{coll,avg},X_i} = [X_i]_{\text{g}} \omega_{X_i} / 4$, where $[X_i]_{\text{g}}$ is the average gas phase concentration of X_i . Under these conditions the net flux of X_i into the condensed phase can be approximated by $J_{\text{net},X_i} \approx \gamma_{X_i} [X_i]_{\text{g}} \omega_{X_i} / 4$. Significant net uptake, however, will lead to local depletion of X_i close to the particle surface ($[X_i]_{\text{gs}} < [X_i]_{\text{g}}$, $J_{\text{coll},X_i} < J_{\text{coll,avg},X_i}$), and gas phase diffusion will influence further uptake. Therefore it is useful to define an effective uptake coefficient γ_{eff,X_i} and a gas phase diffusion correction factor C_{g,X_i} :

$$J_{\text{net},X_i} = \gamma_{\text{eff},X_i} J_{\text{coll,avg},X_i} = \gamma_{\text{eff},X_i} [X_i]_{\text{g}} \omega_{X_i} / 4 = \gamma_{X_i} [X_i]_{\text{gs}} \omega_{X_i} / 4 \quad (3)$$

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$$C_{g,Xi} = \frac{\gamma_{\text{eff},Xi}}{\gamma_{Xi}} = \frac{J_{\text{coll},Xi}}{J_{\text{coll,avg},Xi}} = [X_i]_{\text{gs}} / [X_i]_{\text{g}} \quad (4)$$

$\gamma_{\text{eff},Xi}$ relates the net uptake of species X_i directly to its average gas phase concentration, which is usually the major observable in laboratory studies and the most relevant variable in atmospheric models. It is sometimes also referred to as the “apparent”, “measurable”, or “net” uptake coefficient. Note, however, that the term “net uptake coefficient” is not well suited to distinguish $\gamma_{\text{eff},Xi}$ from γ_{Xi} , because both quantities describe the same net flux of species X_i from the gas phase to the condensed phase and are just normalized to different gas kinetic reference fluxes (average gas kinetic flux or actual surface collision flux). $C_{g,Xi}$ describes the ratio between these fluxes, which is determined by the rates of uptake and gas phase diffusion and will be described in detail below (Sect. 2.2).

The net gas phase loss of X_i due to gas-particle interactions, $L_{g,p,Xi} - P_{g,p,Xi}$ (i.e. gross loss minus production; molecules per unit volume), can be conveniently calculated, when the particle surface concentration, $[PS]_{\text{g}}$ (area per unit volume), and the effective uptake coefficient are known:

$$L_{g,p,Xi} - P_{g,p,Xi} = J_{\text{net},Xi}[PS]_{\text{g}} = \gamma_{\text{eff},Xi}[PS]_{\text{g}}[X_i]_{\text{g}}\omega_{Xi}/4 = k_{g,p,Xi}[X_i]_{\text{g}} \quad (5)$$

Equation (5) allows to use an apparent first-order rate coefficient $k_{g,p,Xi} = \gamma_{\text{eff},Xi} [PS]_{\text{g}} \omega_{Xi}/4$ to calculate the net gas phase loss as a (pseudo-)first-order process with respect to average gas phase composition, which is usually the preferred way to handle heterogeneous reactions in atmospheric models.

Uptake coefficients for different types of gases and aerosol particles are usually determined in laboratory studies covering a limited range of experimental conditions. For a reliable extrapolation and application of the experimentally determined uptake coefficients to atmospheric conditions and in numerical models of the atmosphere, the uptake coefficients have to be deconvoluted into basic physicochemical parameters, which describe the multiple steps (elementary processes) that are usually involved in

aerosol surface reactions and gas-particle interactions and will be outlined in the following sections (transport and chemical reactions in and between gas phase, surface, and particle bulk).

For gas uptake by liquid droplets a widely used resistor model has been developed to deconvolute γ_{eff,X_i} under (quasi-)steady-state conditions. In this model gas phase diffusion to the particle surface, mass transfer from the gas phase into the liquid phase, and subsequent chemical reaction in the liquid are regarded as decoupled processes. These processes are described by individual resistance terms which can be added up to obtain $1/\gamma_{\text{eff},X_i}$ as the overall resistance in analogy to an electrical circuit consisting of serial resistors (Schwartz, 1986; Hanson et al., 1994; Kolb et al., 1995; Finlayson-Pitts and Pitts, 2000; and references therein):

$$\frac{1}{\gamma_{\text{eff},X_i}} = \frac{1}{\Gamma_{g,X_i}} + \frac{1}{\gamma_{X_i}} \quad (6)$$

$$\frac{1}{\gamma_{X_i}} = \frac{1}{\alpha_{X_i}} + \frac{1}{\Gamma_{b,X_i}} \quad (7)$$

α_{X_i} is the bulk accommodation coefficient of the investigated species, which is usually referred to as the “mass accommodation coefficient” and represents the probability or normalized rate of transfer of gas molecules across the surface (or gas-liquid interface) into the liquid. The “conductances” (inverse resistances) Γ_{g,X_i} and Γ_{b,X_i} represent normalized rates of gas phase diffusion and bulk diffusion and reaction, respectively. The most common formulae used to calculate these conductances are $\Gamma_{g,X_i} \approx 8D_{g,X_i} \omega_{X_i}^{-1} d_p^{-1}$ and $\Gamma_{b,X_i} \approx 4H_{\text{cp},X_i} RT \omega_{X_i}^{-1} (D_{b,X_i} k_{b,X_i})^{\frac{1}{2}}$, where D_{g,X_i} is the gas phase diffusion coefficient of X_i , d_p is the particle diameter, H_{cp,X_i} is the solubility or Henry’s law coefficient of X_i , D_{b,X_i} is the diffusion coefficient of X_i in the liquid, and k_{b,X_i} is its the first-order chemical loss rate coefficient of X_i in the liquid. The derivation and applicability of the resistor model equations and parameters will be addressed below (Sects. 2.2 and 4.3.2). Several studies have already set out to include surface reaction terms in the

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resistor model for gas uptake by liquid atmospheric particles and to extend it to solid particles. So far, however, the applicability of the published formalisms and terminologies was generally limited to specific types of aerosols and reaction conditions (e.g. Hanson, 1997; Smith et al., 2002; Worsnop et al., 2002; Ammann et al., 2003; Reid and Sayer, 2003; and references therein).

2.2. Gas phase diffusion

Mass transport by molecular diffusion from the gas phase to the surface of an aerosol or cloud particle depends on the flow regime, which is characterized by the Knudsen number Kn_{X_i} and determined by the particle diameter, d_p , and the mean free path of the investigated species X_i in the gas phase, λ_{X_i} . In the continuum regime ($d_p \gg \lambda_{X_i}$, $Kn_{X_i} \ll 1$) the transport flow is proportional to the gas phase diffusion coefficient and particle diameter, and in the gas kinetic or free-molecule regime ($d_p \ll \lambda_{X_i}$, $Kn_{X_i} \gg 1$) it is proportional to the uptake coefficient, molecular velocity, and particle surface area (Seinfeld and Pandis, 1998; and references therein). In the transition regime ($d_p \approx \lambda_{X_i}$, $Kn_{X_i} \approx 1$) mass transport can be influenced by both gas phase diffusion and surface uptake kinetics, which can be described by corrections of the continuum and gas kinetic flow equations as detailed below.

Based on simple gas kinetic theory for hard sphere molecules of equal size and mass and on earlier studies of gas-particle interaction λ_{X_i} and Kn_{X_i} can be approximated by (Fuchs, 1964; Fuchs and Sutugin, 1971; Seinfeld and Pandis, 1998; and references therein):

$$\lambda_{X_i} = \frac{3 D_{g,X_i}}{\omega_{X_i}} \quad (8)$$

$$Kn_{X_i} = \frac{6 D_{g,X_i}}{\omega_{X_i} d_p} \quad (9)$$

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For air and most atmospheric gases the mean free path at standard temperature and pressure (STP, 0°C, 1 atm) is on the order of ~60 nm, and the particle size dependence of the Knudsen number can be approximated by $Kn_{X_i} \approx (10^2 \text{ nm})/d_p$.

In the continuum regime ($Kn_{X_i} \ll 1$), the flow of a trace gas species X_i , F_{g,X_i} (number of molecules per unit time), into a “perfectly absorbing sphere” ($\gamma_{X_i}=1$) under steady-state conditions is limited by gas phase diffusion and can be described by

$$F_{g,X_i} = 2 \pi d_p D_{g,X_i} [X_i]_g \quad (10)$$

A relation between the average gas phase concentration of X_i , $[X_i]_g$, and its gas phase concentration close to the particle surface, $[X_i]_{gs}$, can be obtained by matching the continuum flow of gas phase diffusion to the surface with the gas kinetic flow of net uptake at the surface. The formalism presented below has been derived by Fuchs (1964) for the coagulation of aerosol particles and is adopted here for the special case where one particle (molecule) is very small and moving much faster than the other one (quasi-static aerosol particle). Under these conditions, the average distance from which the molecule has a straight trajectory to the particle surface, Δ_{X_i} , can be approximated by λ_{X_i} for $Kn_{X_i} \gg 1$, $\lambda_{X_i}/2$ for $Kn_{X_i} \ll 1$, and values in between for $Kn_{X_i} \approx 1$:

$$\Delta_{X_i} = \frac{2}{3 d_p \lambda_{X_i}} \left\{ \left(\frac{d_p}{2} + \lambda_{X_i} \right)^3 - \left(\left(\frac{d_p}{2} \right)^2 + \lambda_{X_i}^2 \right)^{\frac{3}{2}} \right\} - \frac{d_p}{2} \quad (11)$$

By defining the gas phase concentration of X_i at the distance Δ_{X_i} from the surface as $[X_i]_{gs}$ the continuum flow of gas phase diffusion through a virtual particle envelope with diameter $d_p + 2\Delta_{X_i}$ can be expressed as

$$F_{g,X_i} = 2 \pi (d_p + 2\Delta_{X_i}) D_{g,X_i} ([X_i]_g - [X_i]_{gs}) \quad (12)$$

On the other hand, the gas kinetic expression for the net flow from the gas phase to the condensed phase is given by multiplication of J_{net,X_i} as defined in Eq. (3) with the

particle surface area, $d_p^2 \pi$, and for mass conservation the fluxes of diffusion to the surface and net uptake at the surface have to be equal:

$$2 \pi (d_p + 2 \Delta_{X_i}) D_{g,X_i} ([X_i]_g - [X_i]_{gs}) = \gamma_{X_i} \frac{\omega_{X_i}}{4} d_p^2 \pi [X_i]_{gs} \quad (13)$$

Rearrangement using the above definitions of Δ_{X_i} , λ_{X_i} , Kn_{X_i} , and C_{g,X_i} leads to

$$C_{g,X_i} = \frac{[X_i]_{gs}}{[X_i]_g} = \frac{d_p + 2 \Delta_{X_i}}{\frac{3 \gamma_{X_i} d_p^2}{8 \lambda_{X_i}} + d_p + 2 \Delta_{X_i}} = \frac{1}{1 + \gamma_{X_i} \frac{0.75}{Kn_{X_i} (1 + Kn_{X_i} \frac{\Delta_{X_i}}{\lambda_{X_i}})}} \quad (14)$$

Equation (14) can be further simplified by neglecting the size dependence of Δ_{X_i} and assuming $\Delta_{X_i} = \lambda_{X_i}$ as will be discussed and illustrated below (Fig. 1).

Fuchs (1964) expressed the result of flux matching as a correction factor β_F for the flow of a trace gas species X_i into a “perfectly absorbing sphere” under continuum conditions:

$$F_{g,X_i} = \beta_F 2 \pi d_p D_{g,X_i} [X_i]_g \quad (15)$$

$$\beta_F = \frac{\left(1 + Kn_{X_i} \frac{\Delta_{X_i}}{\lambda_{X_i}}\right) \gamma_{X_i}}{\gamma_{X_i} + \frac{4}{3} Kn_{X_i} \left(1 + Kn_{X_i} \frac{\Delta_{X_i}}{\lambda_{X_i}}\right)} \quad (16)$$

Fuchs and Sutugin (1971) proposed an alternative correction factor β_{FS} , which was derived from a numerical solution of the Boltzmann diffusion equation for neutron transfer to a black sphere and is thus characteristic for light molecules in a heavy background gas:

$$\beta_{FS} = \frac{(1 + Kn_{X_i}) \gamma_{X_i}}{\gamma_{X_i} + \frac{4}{3} Kn_{X_i} (Kn_{X_i} + 1 + 0.28 \gamma_{X_i})} \quad (17)$$

The applicability of β_{FS} for trace gases in air (including species with higher molecular mass) has been confirmed by good agreement with experimental data (Li and Davis, 1996; Widmann and Davis, 1997; Seinfeld and Pandis, 1998; Shi et al., 1999; Swartz et al., 1999; Qu and Davis, 2001; Worsnop et al., 2001).

- 5 By inserting β_{FS} instead of β_F in Eq. (15) and rearrangement using $F_{net,Xi}=d_p^2\pi J_{net,Xi}$ and the definition of Kn_{Xi} , $C_{g,Xi}$ can be flexibly adapted to the approach of Fuchs and Sutugin (1971):

$$\begin{aligned} J_{net,Xi} &= \beta_{FS} \frac{\omega_{Xi}}{3} Kn_{Xi} [X_i]_g = \\ &= \frac{Kn_{Xi}^2 + Kn_{Xi}}{Kn_{Xi}^2 + Kn_{Xi} + 0.283Kn_{Xi}\gamma_{Xi} + 0.75\gamma_{Xi}} \gamma_{Xi} \frac{\omega_{Xi}}{4} [X_i]_g \\ &= C_{g,Xi} \gamma_{Xi} \frac{\omega_{Xi}}{4} [X_i]_g \end{aligned} \quad (18)$$

$$C_{g,Xi} = \frac{1}{1 + \gamma_{Xi} \frac{0.75 + 0.283Kn_{Xi}}{Kn_{Xi}(1 + Kn_{Xi})}} \quad (19)$$

- 10 In the gas kinetic or free-molecule limit ($Kn_{Xi} \gg 1$) $C_{g,Xi}$ approaches unity, i.e. $[X_i]_{gs} \approx [X_i]_g$, and in the continuum limit ($Kn_{Xi} \ll 1$) Eqs. (14) and (19) both can be reduced to:

$$C_{g,Xi} = \frac{1}{1 + \gamma_{Xi} \frac{0.75}{Kn_{Xi}}} \quad (20)$$

- Figure 1 displays $C_{g,Xi}$ calculated as a function of Kn_{Xi} for $\gamma_{Xi}=0.01$, 0.1, and 1. The calculations have been performed with Eqs. (20), (19), (14), and with a simplified version of Eq. (14) assuming $\Delta_{Xi}=\lambda_{Xi}$. For $\gamma_{Xi} \leq 0.01$ the results of the different formalisms are essentially identical. For $\gamma_{Xi} \approx 0.1$ small differences occur in the transition regime but the relative deviations are less than 5%. Substantial deviations between the different formalisms occur only for $\gamma_{Xi} \approx 1$ and $Kn_{Xi} \approx 1$. Even under these conditions, however, the differences relative to Eq. (19) did not exceed +7% for Eq. (14), +10% for Eq. (14) with $\Delta_{Xi}=\lambda_{Xi}$, and -13% for Eq. (20), respectively. For many atmospheric process studies these differences are well within the general uncertainties. They should,
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however, not be neglected in high-precision measurements and model calculations of processes with $\gamma_{Xi} \approx 1$ and $Kn_{Xi} \approx 1$. The results of earlier studies suggest that Eq. (19) based on Fuchs and Sutugin (1971) is most appropriate under isothermal conditions (Li and Davis, 1996; Widmann and Davis, 1997; Seinfeld and Pandis, 1998; Shi et al., 1999; Swartz et al., 1999; Qu and Davis, 2001; Worsnop et al., 2001), whereas more elaborate formalisms may be required for non-isothermal processes (Qu et al., 2001).

To our knowledge, a gas phase diffusion correction factor similar to $C_{g,Xi}$ as defined in Eq. (4) and calculated in Eqs. (14), (19), and (20) has not been explicitly defined and introduced for the description of atmospheric gas-particle interactions before. At least within the kinetic model presented in the following sections, however, it proves to be the most useful, convenient, and descriptive way of representing the influence of gas phase diffusion on mass transport and chemical reaction at the surface of aerosol particles. In particular, it allows the flexible implementation of different models and corrections for gas phase diffusion effects in the transition regime without affecting the remainder of the kinetic model formalism.

The relation of $C_{g,Xi}$ with the gas phase diffusion conductances, $\Gamma_{g,Xi}$, of the traditional resistor model outlined above is straightforward, following from division of Eqs. (6) and (7):

$$C_{g,Xi} = \frac{\gamma_{\text{eff},Xi}}{\gamma_{Xi}} = \frac{1}{1 + \frac{\gamma_{Xi}}{\Gamma_{g,Xi}}} \quad (21)$$

with

$$\Gamma_{g,Xi} = \gamma_{Xi} \frac{C_{g,Xi}}{1 - C_{g,Xi}} = \frac{Kn_{Xi} (1 + Kn_{Xi} \Delta_{Xi} / \lambda_{Xi})}{0.75} \quad (22)$$

for the approach by Fuchs (1964), and

$$\Gamma_{g,Xi} = \frac{Kn_{Xi} (1 + Kn_{Xi})}{0.75 + 0.283 Kn_{Xi}} \quad (23)$$

for the interpolation by Fuchs and Sutugin (1971), respectively.

For the calculation of gas phase diffusion resistances in the continuum regime ($Kn_{X_i} \ll 1$) the above equations can be rearranged by inversion, multiplication with $(1 - Kn_{X_i})$, and omission of quadratic terms of Kn_{X_i} , which leads to

$$\frac{1}{\Gamma_{g,X_i}} \approx \frac{\omega_{X_i} d_p}{8D_{g,X_i}} - 0.38 \quad (24)$$

for the gas phase diffusion resistance term based on Fuchs (1964), and

$$\frac{1}{\Gamma_{g,X_i}} \approx \frac{\omega_{X_i} d_p}{8D_{g,X_i}} - 0.47 \quad (25)$$

for the resistance term based on Fuchs and Sutugin (1971), respectively.

The additive constants -0.38 and -0.47 on the right hand side of Eqs. (24) and (25), respectively, correspond to the correction term $-1/2$ in traditional resistor model formulations for the effect of gas phase diffusion in the continuum regime (Danckwerts, 1951; Finlayson-Pitts and Pitts, 2000; and references therein), which have been attributed to an effective doubling of the mean molecular velocity component directed towards the surface in case of high net uptake (distortion of Maxwellian flow; Motz and Wise, 1960). If, however, Kn_{X_i} is indeed more than an order of magnitude below unity, the additive constants contribute less than $\sim 5\%$ to the gas phase diffusion resistances and can be omitted from Eqs. (24) and (25), which become equivalent with Eq. (20).

3. Particle surface and bulk composition and processes

3.1. Double-layer surface model and surface mass balance

To describe the physicochemical processes at the gas-particle interface, we apply a simple double-layer surface model which comprises two monomolecular layers: a quasi-static surface layer consisting of (quasi-)non-volatile particle components Y_j

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(molecules, ions, or functional groups), and a sorption layer consisting of adsorbed volatile molecules X_i . Both the non-volatile particle components Y_j and the volatile molecules X_i can be reversibly transferred between the double-layer surface and the underlying particle bulk, in which they can undergo diffusion and reaction. The contribution of X_i to the chemical composition and physicochemical properties of the quasi-static surface layer, however, is assumed to be negligible. The description and effects of semi-volatile species which can significantly contribute to the composition of all model compartments (gas phase, sorption layer, quasi-static surface, particle bulk) will be addressed below (Sect. 3.7).

To describe surface-bulk mass transport and the potential influence of bulk composition on surface processes, it is useful to define the condensed phase directly adjacent to the quasi-static surface layer as the “near-surface particle bulk”. Depending on the chemical composition and physical state of the investigated particles, the near-surface bulk region can be pictured to extend one or a few molecular diameters or chemical bonds (~ 1 nm) from the quasi-static surface into the particle bulk. The chemical species present in the near-surface particle bulk are not directly exposed to the gas phase or sorption layer species, but they interact with the quasi-static surface layer and can influence its physico-chemical properties: e.g. electron donor-acceptor and charge-transfer interactions; hydrogen bonding networks (O’Hanlon and Forster, 2000); quasi-liquid or structurally disordered surface layers on ice (Delzeit et al., 1996; Girardet and Toubin, 2001). With respect to mass transport, the near-surface particle bulk is analogous to the near-surface gas-phase, i.e. the gas phase about one mean free path off the surface as discussed in the preceding section on gas phase diffusion. Both can be pictured as the region from which a molecule of the investigated species can directly interact and undergo exchange with the molecules in the double-layer surface.

Mass transport of the volatile species X_i and non-volatile species Y_j between the near-surface gas phase (gs), the sorption layer (s), the quasi-static surface layer (ss),

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and the near-surface particle bulk (bs) can be summarized by:



Compartments and transport fluxes in the double-layer surface model considering only volatile and non-volatile species are illustrated in Fig. 2. Combination of transport with chemical production and loss at the surface leads to the following surface mass balance equations for X_i and Y_j :

$$d[X_i]_s/dt = J_{\text{ads},X_i} - J_{\text{des},X_i} + P_{\text{s},X_i} - L_{\text{s},X_i} + J_{\text{b,s},X_i} - J_{\text{s,b},X_i} \quad (28)$$

$$d[Y_j]_{\text{ss}}/dt = P_{\text{ss},Y_j} - L_{\text{ss},Y_j} + J_{\text{b,ss},Y_j} - J_{\text{ss,b},Y_j} \quad (29)$$

$[X_i]_s$ is the concentration of X_i in the sorption layer (number per unit area), and $[Y_j]_{\text{ss}}$ is the concentration of Y_j in the quasi-static surface layer (number per unit area). All terms on the right hand side of Eqs. (28) and (29) are flux densities (number per unit area and unit time): J_{ads,X_i} and J_{des,X_i} stand for adsorption and desorption, i.e. reversible mass transport of from the near-surface gas phase to the sorption layer; $J_{\text{b,s},X_i}$ and $J_{\text{s,b},X_i}$ for mass transport from the near-surface bulk to the sorption layer and vice versa; P_{s,X_i} and L_{s,X_i} for production and loss of adsorbed X_i by chemical reaction at the surface; $J_{\text{b,ss},Y_j}$ and $J_{\text{ss,b},Y_j}$ for mass transport from the bulk to the quasi-static surface layer and vice versa; P_{ss,Y_j} and L_{ss,Y_j} for chemical production and loss of Y_j in the quasi-static surface layer. The mass transport flux densities, J_{ads,X_i} , J_{des,X_i} , $J_{\text{b,s},X_i}$, $J_{\text{s,b},X_i}$, $J_{\text{b,ss},Y_j}$, and $J_{\text{ss,b},Y_j}$, are determined by the chemical composition and physico-chemical properties of the surface (sorption layer and quasi-static layer), the near-surface gas phase, and the near-surface particle bulk. Molecular mechanisms and rate

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equations for the mass transport processes will be outlined below (Sects. 3.2 and 3.4). For chemical production and loss of X_i in the sorption layer ($P_{s,X_i} - L_{s,X_i}$) and of Y_j in the quasi-static surface layer ($P_{ss,Y_j} - L_{ss,Y_j}$), respectively, different reaction mechanisms have to be taken into account. Depending on the involved model compartments we distinguish between gas-surface reactions, surface layer reactions and surface-bulk reactions. The different types of chemical reactions and rate parameters are illustrated in Fig. 3 and will be described in detail below (Sect. 3.3).

3.2. Adsorption and desorption (gas-surface mass transport)

We define adsorption as the accommodation of gas molecules on the quasi-static particle surface, i.e. transport from the gas phase into the sorption layer on the quasi-static surface, and desorption as the reverse process. As indicated by the surface mass balance equations outlined above, the presented model framework aims at a clear distinction of transport processes (adsorption and desorption) from chemical reactions at the surface. We speak of adsorption or surface accommodation when the gas molecule colliding with the surface neither reacts nor bounces off immediately but stays within a distance on the order of a chemical bond ($\sim 10^{-10}$ m) for a duration on the order of or longer than the average duration of a (quasi-)elastic gas-surface collision or molecular scattering process. From gas kinetic theory this duration can be approximated by the ratio of the typical length of a chemical bond and the mean thermal velocity of the gas molecule ($\sim 10^2$ m s $^{-1}$), which is generally on the order of $\sim 10^{-12}$ s under ambient conditions in the lower atmosphere.

The processes of adsorption and desorption are considered to include intermolecular interactions between molecules in the sorption layer and in the quasi-static surface layer (van der Waals interactions, hydrogen bonding, and similar electron donor-acceptor interactions; Goss, 2004) but no formation or cleavage of molecular chemical bonds (binding energies $\gg 100$ kJ mol $^{-1}$). Gas-surface interactions which lead to the formation or cleavage of chemical bonds in the involved gas phase or surface molecules (including so-called dissociative adsorption or desorption) are regarded ei-

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ther as (quasi-)elementary “gas-surface reactions” (Sect. 3.3.1) or as two-step processes of gas-surface mass transport and subsequent chemical reaction within the surface double-layer (“surface layer reactions”, Sect. 3.3.2). The conceptual distinction between adsorption, scattering (bounce), and immediate reaction of gas molecules colliding with a liquid or solid surface is supported by the results of molecular beam experiments and other advanced surface science studies revealing further details of gas-surface interactions on a molecular level (e.g. Masel, 1996; Nathanson et al., 1996; Rettner et al., 1996; Bartels-Rausch et al., 2002, 2005; and references therein).

In surface science the terms “physisorption” and “trapping” are frequently used to describe loose binding of adsorbed molecules to a surface (negative adsorption enthalpies typically $<50 \text{ kJ mol}^{-1}$), whereas “chemisorption” and “sticking” are used to describe strong binding (negative adsorption enthalpies typically $>50 \text{ kJ mol}^{-1}$; Masel, 1996). Within the kinetic model framework outlined in this manuscript, however, all of these terms are sub-summarized under the umbrella terms adsorption or surface accommodation, which comprise the full range from rather loose to relatively strong binding of molecules to the quasi-static surface, as long as no formation or cleavage of molecular chemical bonds is involved. This definition is in line with Langmuir’s understanding of adsorption (Langmuir, 1916) and aims at making the presented kinetic model framework with a limited number of rate equations and parameters consistently applicable for the wide variety of particles and trace gases interacting in the atmosphere. It is, however, not meant to constrain the distinction and application of different mechanisms and traditional categories of adsorption for detailed investigation and characterization of specific systems, from which the generalized rate parameters defined below can be determined and extrapolated to atmospheric conditions.

The flux of adsorption of gas molecules X_i can be described by multiplication of the flux of surface collisions, J_{coll,X_i} , with a surface accommodation coefficient or adsorption probability, S_{X_i} :

$$J_{\text{ads},X_i} = S_{X_i} J_{\text{coll},X_i} \quad (30)$$

S_{X_i} is defined as the probability that X_i undergoes neither scattering nor immediate

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chemical reaction upon collision with the particle but is accommodated in the sorption layer of the particle ($0 \leq S_{X_i} \leq 1$). In earlier studies of atmospheric aerosol surface chemistry similarly defined parameters have been called adsorptive mass accommodation coefficient (Elliott et al., 1991), (mass) accommodation coefficient (Jayne et al., 1990; Tabazadeh and Turco, 1993; Pruppacher and Klett, 1997), condensation coefficient (Pruppacher and Klett, 1997); sticking coefficient (Hanson, 1997), adsorption coefficient (Shi et al., 1999; Turco et al., 1989; Worsnop et al., 2002), or thermal accommodation coefficient (Li et al., 2001; Worsnop et al., 2002). For clarity and unambiguous distinction from bulk processes and from chemical reactions, however, we propose to use the term surface accommodation coefficient.

Inserting Eq. (3) in (30) leads to

$$J_{\text{ads},X_i} = k_{a,X_i}[X_i]_{\text{gs}} \quad (31)$$

with a first-order adsorption rate coefficient $k_{a,X_i} = S_{X_i} \omega_{X_i} / 4$, which has the dimensions “length time⁻¹” and can be regarded as a deposition velocity.

In Eqs. (30) and (31) all surface-specific parameters are lumped in the surface accommodation coefficient S_{X_i} , without making any a priori assumptions about the number and nature of sorption sites, surface coverage by competing adsorbate molecules, surface mobility and residence of adsorbate molecules, etc. The simplest way to estimate S_{X_i} is a Langmuir adsorption model in which all adsorbate species compete for a single type of non-interfering sorption sites with an overall concentration $[SS]_{\text{ss}}$ (number per unit area) on the quasi-static surface. In this case S_{X_i} is determined by the surface accommodation coefficient on a clean, i.e. adsorbate-free surface, S_{0,X_i} , and the sorption layer surface coverage, θ_s , which is given by the sum of the fractional surface coverages of all competing adsorbate species, θ_{s,X_p} :

$$S_{X_i} = S_{0,X_i}(1 - \theta_s) \quad (32)$$

$$\theta_s = \sum_p \theta_{s,X_p} \quad (33)$$

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Under the assumption of a single type and surface concentration of sorption sites for all adsorbate species, the fractional surface coverage of an individual species X_p is given by $\theta_{s,Xp} = [X_p]_s / [SS]_{ss}$.

In practice the nature of sorption sites at the surface of an aerosol particle is determined by its chemical composition, and the interaction between different adsorbates and specific surface sites (molecules, functional groups, atoms, or ions) may be highly variable. For such complex systems different types of sorption sites can be defined for different types of phase species interacting with the surface. For example, dual-site Langmuir formalisms have been applied to describe the interaction of carbonaceous particles with nitrogen oxides (Gray and Do, 1992). In principle, such formalisms are compatible with the model framework outlined in this manuscript, but they seem to be hard to generalize for atmospheric applications with a large number of interacting trace gases and their elaboration goes beyond the scope of this paper. Here we apply a simple approach assuming that the competition of different adsorbate species for different adsorption sites on the quasi-statistic particle surface can be described by assigning effective molecular cross sections to the adsorbate species and letting them compete for surface area rather than specific sites. In this case, the fractional surface coverage of individual species X_p can be calculated by

$$\theta_{s,Xp} = [X_p]_s / [X_p]_{s,max} = \sigma_{s,Xp} [X_p]_s \quad (34)$$

where $\sigma_{s,Xp}$ is the effective molecular cross section of X_p in the sorption layer, and the inverse of $\sigma_{s,Xp}$ is the maximum surface concentration of X_p , $[X_p]_{s,max}$.

Equations (31)–(34) describe a Langmuir-type adsorption process accounting for different competing adsorbate species. The influence of the (potentially changing) chemical composition of the quasi-static particle surface on adsorbate-surface interactions and thus on the surface accommodation coefficient can be taken into account by describing $S_{0,Xi}$ as a linear combination of the initial surface accommodation coefficients that would be observed on pure substrates made up by the different surface components Y_q weighted by their fractional surface area $\theta_{ss,Yq}$, i.e. their surface concentration

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$[Y_q]_{ss}$ multiplied by their effective molecular cross section $\sigma_{ss,Yq}$

$$S_{0,Xi} = \sum_q S_{0,Xi,Yq} \theta_{ss,Yq} \quad (35)$$

$$\theta_{ss,Yq} = [Y_q]_{ss} \sigma_{ss,Yq} \quad (36)$$

with $\sum_q \theta_{ss,Yq} = 1$.

5 If the surface accommodation process were significantly influenced not only by the quasi-static surface layer but also by the underlying condensed phase (e.g. by hydrogen bonding or other electron donor-acceptor interactions), the composition of the near-surface particle would also have to be taken into account. This could be achieved by expressing $S_{0,Xi,Yp}$ as a linear combination of the sticking probabilities $S_{0,Xi,Yp,Yq}$ which would be observed for X_i colliding with an adsorbate-free surface made up of pure Y_p on an underlying bulk of pure Y_q :

$$S_{0,Xi,Yp} = \sum_q S_{0,Xi,Yp,Yq} \phi_{Yq} \quad (37)$$

15 The weighting factor ϕ_{Yq} could be the mole, mass, or volume fraction of Y_q in the near-surface particle bulk. The latter appear to be more suitable for the representation of macromolecular particle components.

In this approach surface heterogeneities and interferences between adsorbate molecules which may lead to non-linear dependence of S_{X_i} on particle composition and sorption layer coverage, are assumed to be negligible or cancel out statistically. If this is not the case, appropriate corrections or alternative mathematical formalisms have to be applied. The investigated surfaces and underlying molecular layers have to be resolved into quasi-homogenous areas, or Monte-Carlo-type simulations have to be performed. Such approaches could be included in the presented model framework, but they would have to be designed specifically for different aerosol systems and are beyond the scope of this paper.

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Combining Eqs. (31) and (32) leads to

$$J_{\text{ads},Xi} = k_{\text{a},0,Xi}[X_i]_{\text{gs}}(1 - \theta_s) \quad (38)$$

with

$$k_{\text{a},0,Xi} = S_{0,Xi}\omega_{Xi}. \quad (39)$$

Equation (38) is consistent with standard textbook formulations for the flux of Langmuir adsorption (Langmuir, 1916; Laidler et al., 1940). The dependence of $S_{0,Xi}$ and thus of $k_{\text{a},0,Xi}$ on the composition of the quasi-static surface layer and near-surface particle bulk described in Eqs. (35)–(37), however, implies that even in the simple model of adsorption outlined above, the surface accommodation and adsorption rate coefficients may change over time if the particle components are transformed by chemical reactions (chemical aging).

In the Langmuir model of reversible adsorption, also the desorption process can be described by a first-order rate coefficient, $k_{\text{d},Xi}$, which is assumed not to depend on θ_s and can be regarded as the inverse of the desorption lifetime, $\tau_{\text{d},Xi}$, i.e. the mean residence time of the investigated species on the surface in the absence of chemical reaction and surface-bulk mass transport (Laidler et al., 1940):

$$J_{\text{des},Xi} = k_{\text{d},Xi}[X_i]_s = \tau_{\text{d},Xi}^{-1}[X_i]_s = \tau_{\text{d},Xi}^{-1}\sigma_{Xi}^{-1}\theta_s X_i \quad (40)$$

Under adsorption equilibrium conditions it is useful to combine the rate coefficients of adsorption and desorption into a Langmuir adsorption equilibrium constant $K_{\text{ads},Xi}$ (Sect. 4.2). In case of rapid chemical reaction or surface-bulk exchange, however, the actual mean residence time of X_i on the surface is shorter than its desorption lifetime, which can be taken into account in an effective adsorption equilibrium constant $K'_{\text{ads},Xi}$ for the description of adsorption-reaction steady-state conditions (Sect. 4.3). These special cases of equilibrium and steady-state conditions will be described and discussed in more detail below (Sect. 4) and illustrated by exemplary model calculations in a companion paper (Ammann and Pöschl, 2005).

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In analogy to Eqs. (35)–(37) for $S_{0,Xi}$, the influence of the chemical composition of the quasi-static surface layer and near-surface particle bulk can be taken into account by describing $\tau_{d,Xi}$ as a linear combination of the desorption lifetimes which would be observed on pure substrates made up by the different chemical components of the actual surface, $\tau_{d,Xi,Yp}$, or on surfaces of made up by pure Y_p on an underlying bulk of pure Y_q , $\tau_{d,Xi,Yp,Yq}$.

Since desorption is driven by thermal motion, the mean residence times and desorption rate coefficients are expected to exhibit a strong temperature dependence, which can usually be described by an Arrhenius equation involving the heat of adsorption and a pre-exponential factor on the order of the vibration frequency of the involved molecules and chemical bonds (Laidler et al., 1940; Baetzold and Somorjai 1976; Pöschl et al., 2001; and references therein). Of course the other rate coefficients of mass transport and chemical reaction introduced above and in the remainder of this manuscript can also exhibit more or less pronounced temperature dependencies, as will be discussed below (Sect. 4.1).

From heterogeneous catalysis it is known that almost all technically relevant surface reactions (except for single crystal surfaces) can be described by Langmuir-Hinshelwood or Eley-Rideal rate equations derived on the basis of a simple Langmuir adsorption model; even in systems where the actual adsorption process does not follow a simple Langmuir isotherm, reaction rates can often be described by a Langmuir-Hinshelwood rate equations based on the assumption of Langmuir adsorption (Sect. 4; Masel, 1996; Ammann et al., 2003; and references therein). Thus we expect that the above rate equations of adsorption and desorption will be suitable for the description of most relevant surface reactions on atmospheric particles, as indicated by multiple recent studies (Arens et al., 2001; Pöschl et al., 2001; Ammann et al., 2003; Rudich, 2003; Dubowski et al., 2004; Mmerekı et al., 2004; Sullivan et al., 2004; Ammann and Pöschl, 2005; and references therein).

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3.3. Chemical reactions at the surface

3.3.1. Gas-Surface Reactions (GSR)

We reserve the term gas-surface reactions exclusively for reactions which can be described by a single kinetic step of collision and reaction between gas phase and surface molecules, i.e. heterogenous elementary reactions in which one of the reactants comes directly from the gas phase without a separable step of surface accommodation prior to reaction. According to the above definition of surface accommodation, gas-surface reactions in the lower troposphere would have to occur within $\sim 10^{-12}$ s upon collision of the gas molecule with the surface. In the chemical engineering literature processes involving gas-surface reactions are commonly referred to as Eley-Rideal mechanisms.

In principle, sorption layer and quasi-static surface layer components X_i and Y_j can be formed upon reaction of any gas phase species X_p with any surface species X_q or Y_q , respectively. Net chemical production (i.e. gross production minus loss) of X_i and Y_j by elementary second-order gas-surface reactions can be described by the following generalized rate equations:

$$P_{s,g,X_i} - L_{s,g,X_i} = \sum_u \sum_p \sum_q C_{GSRu,s,X_i} J_{coll,X_p} (\gamma_{GSRu,X_p,X_q} \theta_{s,X_q} + \gamma_{GSRu,X_p,Y_q} \theta_{ss,Y_q} (1 - \theta_s)) \quad (41)$$

$$P_{ss,g,Y_j} - L_{ss,g,Y_j} = \sum_u \sum_p \sum_q C_{GSRu,ss,Y_j} J_{coll,X_p} (\gamma_{GSRu,X_p,X_q} \theta_{s,X_q} + \gamma_{GSRu,X_p,Y_q} \theta_{ss,Y_q} (1 - \theta_s)) \quad (42)$$

C_{GSRu,s,X_i} and C_{GSRu,ss,Y_j} stand for the stoichiometric coefficients (negative for starting substances and positive for reaction products) of surface species X_i and Y_j involved in the elementary gas-surface reaction $GSRu$ ($u=1, \dots, u_{\max}$ in a system with a total number of u_{\max} elementary gas-surface reactions). γ_{GSRu,X_p,X_q} or γ_{GSRu,X_p,Y_q} are

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defined as elementary gas-surface reaction probabilities, i.e. the probabilities that gas phase molecules X_p undergo an elementary gas-surface reaction GSR_u when colliding with an adsorbed volatile species X_i in the sorption layer or with a non-volatile species Y_j in the quasi-static surface layer, respectively.

- 5 Production and loss of X_i by elementary gas-surface reactions can involve volatile species in the sorption layer as well as non-volatile species in the uncovered fraction, $(1 - \theta_s)$, of the quasi-static surface layer:

$$P_{\text{g,gsr},Xi} - L_{\text{g,gsr},Xi} = \sum_u \sum_p \sum_q C_{\text{GSR}_u,\text{g},Xi} J_{\text{coll},Xp} (\gamma_{\text{GSR}_u,Xp,Xq} \theta_{s,Xq} + \gamma_{\text{GSR}_u,Xp,Yq} \theta_{ss,Yq} (1 - \theta_s)) \quad (43)$$

- 10 $C_{\text{GSR}_u,\text{g},Xi}$ stands for the stoichiometric coefficient of gas molecules X_i involved in the elementary gas-surface reaction GSR_u .

- Due to chemical interferences (activation or passivation by neighboring species, etc.), the reaction probabilities $\gamma_{\text{GSR}_u,Xp,Xq}$ and $\gamma_{\text{GSR}_u,Xp,Yq}$ may depend on surface composition and adsorbate coverage. As discussed in the above Langmuir adsorption model, non-linear interferences cannot be easily taken into account, but linear dependencies on surface and near-surface bulk composition could be accounted for by linear combination of the reaction probabilities that would be observed on pure substrates made up by the chemical components of the actual surface and near-surface particle bulk (in analogy to Eqs. 35–37). The same applies for the rate coefficients of surface layer reactions and surface-bulk reactions defined in the following sections.
- 20

3.3.2. Surface Layer Reactions (SLR)

- The term surface layer reaction is reserved for reactions which proceed within the surface double layer and involve only adsorbed species or components of the quasi-static surface layer. Such reactions can be influenced by surface heterogeneities and chemical interferences (local depletion or enrichment, activation or passivation by neighboring species, etc.), but for simplicity we assume that they exhibit a straightforward rate-
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dependence on the average surface concentration of the reactants and that deviations cancel out statistically. The same approach has been taken in early surface science (Laidler et al., 1940; Hinshelwood, 1940) and is widely applied in heterogeneous catalysis (Masel, 1996). In the chemical engineering literature processes involving surface layer reactions are commonly referred to as Langmuir-Hinshelwood mechanisms.

Assuming that all relevant surface layer reactions can be described by quasi-elementary steps following first- or second-order kinetics, the following generalized expressions can be used to describe net chemical production (i.e. production minus loss) of surface species X_i or Y_j by reactions within the sorption layer ($P_{s,s,X_i} - L_{s,s,X_i}$), between sorption layer and quasi-static surface layer ($P_{s,ss,X_i} - L_{s,ss,X_i}$, $P_{ss,s,Y_j} - L_{ss,s,Y_j}$), and within the quasi-static surface layer ($P_{ss,ss,Y_j} - L_{ss,ss,Y_j}$).

$$P_{s,s,X_i} - L_{s,s,X_i} = \sum_v \sum_p c_{SLRv,s,X_i} [X_p]_s \left(k_{SLRv,Xp} + \sum_q k_{SLRv,Xp,Xq} [X_q]_s \right) \quad (44)$$

$$P_{s,ss,X_i} - L_{s,ss,X_i} = \sum_v \sum_p \sum_q c_{SLRv,s,X_i} k_{SLRv,Xp,Yq} [X_p]_s [Y_q]_{ss} \quad (45)$$

$$P_{ss,ss,Y_j} - L_{ss,ss,Y_j} = \sum_v \sum_p c_{SLRv,ss,Y_j} [Y_p]_{ss} \left(k_{SLRv,Yp} + \sum_q k_{SLRv,Yp,Yq} [Y_q]_{ss} \right) \quad (46)$$

$$P_{ss,s,Y_j} - L_{ss,s,Y_j} = \sum_v \sum_p \sum_q c_{SLRv,ss,Y_j} k_{SLRv,Xp,Yq} [X_p]_s [Y_q]_{ss} \quad (47)$$

Here c_{SLRv,s,X_i} and c_{SLRv,ss,Y_j} stand for the stoichiometric coefficients (negative for starting materials and positive for reaction products) of species X_i and Y_j in reaction $SLRv$ ($v=1, \dots, v_{\max}$ in a system with a total number of v_{\max} (photo-)chemical reactions occurring on the surface of the investigated aerosol particles). $k_{SLRv,Xp,Yq}$, $k_{SLRv,Xp,Xq}$, and $k_{SLRv,Yp,Yq}$ are second-order reaction rate coefficients; $k_{SLRv,Xp}$ and $k_{SLRv,Yq}$ are first-order reaction rate coefficients, including photolysis frequencies (j-values).

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In principle also higher-order reactions might occur in real systems and could be flexibly included in Eqs. (44)–(47). In analogy to the description of complex gas phase reactions in atmospheric chemistry, however, it should be possible to avoid excessive complexity and diversity of rate equations and to describe such reactions by formal first- or second-order rate equations with appropriate rate coefficients reflecting the influence of additional species (third-body reactions; Atkinson et al, 2004).

3.3.3. Surface-bulk reactions

The term surface-bulk reaction is reserved for elementary reactions between species in the quasi-static surface layer and in the near-surface particle bulk. For simplicity we assume that potential surface-bulk reactions proceed via quasi-elementary steps with straightforward second-order rate-dependence on the surface concentration of the reactant in the quasi-static surface layer and on the volume concentration of the involved species in the near-surface particle bulk.

Under these conditions the following generalized expression can be used to describe net chemical production of quasi-static surface layer species Y_j by surface-bulk reactions ($P_{ss,b,Y_j} - L_{ss,b,Y_j}$):

$$P_{ss,b,Y_j} - L_{ss,b,Y_j} = \sum_w \sum_p c_{SBRw,ss,Y_j} [Y_p]_{ss} \left(\sum_q k_{SBRw,Yp,Yq} [Y_q]_{bs} + \sum_r k_{SBRw,Yp,Xr} [X_r]_{bs} \right) \quad (48)$$

c_{SBRw,s,Y_j} stands for the stoichiometric coefficient (negative for starting materials and positive for reaction products) of surface species Y_j in the surface bulk reaction SBR_w ; $w=1, \dots, w_{\max}$ in a system with a total number of w_{\max} chemical reactions occurring between surface species and underlying condensed phase species on the surface of the investigated aerosol particles. $[Y_j]_{b,s}$ or $[X_i]_{b,s}$ are the volume concentrations of Y_j and X_i in the near-surface particle bulk (number per unit volume), and $k_{SBRw,Yp,Yq}$ and $k_{SBRw,Yp,Xr}$ are the second-order rate coefficients.

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On the other hand, the net chemical production of X_i and Y_j in the near-surface particle bulk due to surface-bulk reactions can be described by

$$P_{b,ss,Y_j} - L_{b,ss,Y_j} = \sum_w \sum_p c_{SBRw,b,Y_j} [Y_p]_{ss} \left(\sum_q k_{SBRw,Y_p,Y_q} [Y_q]_{bs} + \sum_r k_{SBRw,Y_p,X_r} [X_r]_{bs} \right) \quad (49)$$

$$P_{b,ss,X_i} - L_{b,ss,X_i} = \sum_w \sum_p c_{SBRw,b,X_i} [Y_p]_{ss} \left(\sum_q k_{SBRw,Y_p,Y_q} [Y_q]_{bs} + \sum_r k_{SBRw,Y_p,X_r} [X_r]_{bs} \right) \quad (50)$$

c_{SBRw,b,X_i} and c_{SBRw,b,Y_j} stand for the stoichiometric coefficients (negative for starting materials and positive for reaction products) of near-surface bulk species X_i and Y_j in the surface-bulk reaction SBR_w . For highly dynamic surfaces with rapid surface-bulk mass transport (low-viscosity liquid droplets), surface-bulk reactions can probably be neglected under most conditions. For non-volatile solid particles, however, they may play a significant role in the chemical aging of the surface and near-surface particle bulk.

3.3.4. Overall chemical production and loss of surface layer components

For conciseness, gross production and loss have not been separated in the above generalized rate equations for gas-surface, surface layer and surface-bulk reactions. For some considerations, however, this separation may be useful and it is easy to achieve by separate summation of the reaction rate terms with positive stoichiometric coefficients (production) and with negative stoichiometric coefficients (loss). Accordingly, the overall flux densities of gross chemical production and loss of adsorbed molecules X_i in the sorption layer and of non-volatile particle components Y_j in the quasi-static

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surface layer, respectively, can be expressed as follows:

$$P_{s,Xi} = P_{s,g,Xi} + P_{s,s,Xi} + P_{s,ss,Xi} \quad (51)$$

$$L_{s,Xi} = L_{s,g,Xi} + L_{s,s,Xi} + L_{s,ss,Xi} \quad (52)$$

$$P_{ss,Yj} = P_{ss,g,Yj} + P_{ss,s,Yj} + P_{ss,ss,Yj} + P_{ss,b,Yj} \quad (53)$$

$$L_{ss,Yj} = L_{ss,g,Yj} + L_{ss,s,Yj} + L_{ss,ss,Yj} + L_{ss,b,Yj} \quad (54)$$

To describe the influence of chemical reactions at the surface on the composition and mass balance of an aerosol particle surface, Eqs. (51)–(54) have to be inserted in Eqs. (28) and (29). Some of the reaction pathways and flux densities, however, which have been included for completeness and consistency of the above generalized rate expressions, are expected to be negligible under most atmospherically relevant conditions and will not be taken into account in the remainder of this manuscript (e.g. $P_{ss,ss,Yj}$, $P_{b,ss,Yj}$, $L_{b,ss,Yj}$, $P_{b,ss,Xi}$, $L_{b,ss,Xi}$).

3.4. Surface-bulk mass transport

3.4.1. Transfer of volatile species between sorption layer and near-surface particle bulk

For the mass transport of volatile species X_i between the sorption layer and near-surface particle bulk (solvation and desolvation, respectively), we assume a first-order dependence on sorption layer and near-surface bulk concentration, respectively:

$$J_{s,b,Xi} = k_{s,b,Xi}[X_i]_s \quad (55)$$

$$J_{b,s,Xi} = k_{b,s,Xi}[X_i]_{bs} \quad (56)$$

The surface-to-bulk transfer rate coefficient $k_{s,b,Xi}$ can be regarded as the inverse of the surface-bulk exchange lifetime, $\tau_{s,b,Xi}$, i.e. the mean residence time of the investigated species at the surface in the absence of chemical reaction and desorption. It

is expected to increase with increasing dynamic variability of the quasi-static surface and with decreasing viscosity of the near-surface particle bulk. In analogy to the desorption lifetime, the influence of the chemical composition of the quasi-static surface and near-surface particle bulk on the surface-bulk exchange lifetime could be taken into account by describing τ_{s,b,X_i} as a linear combination of the residence times that would be observed on pure substrates made up by the chemical components of the actual surface and near-surface particle bulk (in analogy to Eqs. 35–37). Moreover, the cluster-nucleation model proposed by Davidovits et al. (1991) and similar approaches of describing surface-to-bulk transfer could be used to determine and parameterize k_{s,b,X_i} .

The bulk-to-surface transfer rate coefficient k_{b,s,X_i} has dimensions of unit length per unit time and can be regarded as a transfer velocity, analogous to the deposition velocity (adsorption rate coefficient k_{a,X_i}) on the gas phase side. It is expected to be negligibly small for solid non-volatile materials and to increase with increasing mobility of X_i in the condensed phase. Based on kinetic theory of condensed phases and on the diffusion coefficient of X_i in the near-surface particle bulk, it should be possible to estimate the magnitude of k_{b,s,X_i} for different types of particles. A detailed discussion of this aspect, however, is beyond the scope of this paper, which is focused on surface reactivity rather than surface-bulk mass transport. As for the rate coefficients defined above, linear dependencies on surface and near-surface bulk composition could be accounted for by linear combination of the inverse rate coefficients that would be observed on pure substrates made up by the chemical components of the actual surface and near-surface particle bulk (in analogy to Eqs. 35–37).

3.4.2. Mass transport of non-volatile particle components between quasi-static surface layer and near-surface particle bulk

Mass transport of chemical species between the the quasi-static surface layer and the near-surface particle bulk, i.e. conversion of surface species into near-surface particle bulk species and vice versa, can proceed via two mechanisms: (a) coverage

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or exposure of near-surface bulk species by reactive transformation and size changes of the overlying quasi-static surface layer species (e.g. addition or loss of functional groups, partial volatilization); and (b) mutual exchange between surface and near-surface bulk species by thermal motion. We denote the transfer fluxes corresponding to the different mechanisms by J_{ss,b,rx,Y_j} and J_{b,ss,rx,Y_j} (reactive transformation) and by J_{ss,b,ex,Y_j} and J_{b,ss,ex,Y_j} (exchange), respectively.

a) Reactive transformation

Chemical transformations changing the molecular size of particle components in the quasi-static surface layer (e.g. addition or loss of functional groups, volatilization) will generally lead to the coverage of neighboring surface species or to the exposure of previously underlying near-surface bulk species. The overall process can be described by a pseudo-first-order “quasi-static surface transformation rate coefficient” $k_{ss,rx}$ calculated from the net production and effective cross section of all quasi-static surface species Y_p :

$$k_{ss,rx} = \sum_p (P_{ss,Y_p} - L_{ss,Y_p}) \sigma_{Y_p} \quad (57)$$

Negative values of $k_{ss,rx}$ describe the exposure of near-surface bulk species to the gas phase or sorption layer, which implies their transfer from the near-surface bulk to the quasi-static surface, J_{ss,b,rx,Y_j} . Positive values of $k_{ss,rx}$, on the other hand, describe the coverage of surface species which implies their transfer from the quasi-static surface to the near-surface particle bulk, J_{b,ss,rx,Y_j} .

By multiplication of the surface transformation rate coefficient with the surface concentration $[Y_j]_{ss}$ or with the near-surface bulk mole fraction and effective cross section of a non-volatile particle component Y_j , respectively, the corresponding surface-bulk mass transport fluxes can be approximated as follows:

$$J_{ss,b,rx,Y_j} = \frac{k_{ss,rx} + |k_{ss,rx}|}{2} [Y_j]_{ss} = k_{ss,b,rx,Y_j} [Y_j]_{ss} \quad (58)$$

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$$\begin{aligned}
 J_{b,ss,rx,Y_j} &= \frac{|k_{ss,rx} - k_{ss,rx}|}{2} \frac{\phi_{Y_j}/\sigma_{Y_j}}{\sum_p \phi_{Y_p}/\sigma_{Y_p}} \sigma_{Y_j}^{-1} \\
 &= \frac{|k_{ss,rx} - k_{ss,rx}|}{2} \frac{1}{\sigma_{Y_j}^2 \sum_p [Y_p]_{bs} \sum_p \phi_{Y_p}/\sigma_{Y_p}} [Y_j]_{bs} = k_{b,ss,rx,Y_j} [Y_j]_{bs}
 \end{aligned}
 \tag{59}$$

In Eq. (59) ϕ_{Y_q} stands for the mole fraction of Y_q in the near-surface particle bulk. If mass or volume fraction are used instead, the number concentrations $[Y_p]_{bs}$ have to be scaled by molar mass or partial molar volume, respectively. k_{b,ss,rx,Y_j} and k_{ss,b,rx,Y_j} are the pseudo-first-order rate coefficients for reactive bulk-to-surface and surface-to-bulk transfer of Y_j , respectively.

b) Mutual exchange

In analogy to the surface-bulk mass transport of volatile species, we assume that the mass transport fluxes of non-volatile particle components Y_j exhibit a first-order dependence on their surface and near-surface bulk concentrations, respectively:

$$J_{ss,b,ex,Y_j} = k_{ss,b,ex,Y_j} [Y_j]_{ss} \tag{60}$$

$$J_{b,ss,ex,Y_j} = k_{b,ss,ex,Y_j} [Y_j]_{bs} \tag{61}$$

Again the transfer rate coefficients can be expected to increase with increasing dynamic variability of the quasi-static surface and with decreasing viscosity of the near-surface particle bulk, and linear dependencies on surface and near-surface bulk composition could be accounted for by linear combination of the inverse rate coefficients for pure substrates.

In contrast to the mass transport of volatile species between bulk and sorption layer, however, the mutual exchange of non-volatile species between quasi-static surface layer and near-surface particle bulk has to be balanced at all times because $\sum_q \theta_{ss,Y_q} = 1$ by definition, i.e. the quasi-static surface has to be a monomolecular layer (Sect. 3.1, Eq. 36).

Since precise values for the transfer rate coefficients of all species present in real aerosol particles will hardly ever be available, practical application of Eqs. (60) and (61) for a comprehensive description of surface-bulk exchange will require a self-consistent normalisation formalism. The normalisation could be achieved in analogy to Eqs. (58) and (59) using an overall exchange rate coefficient instead of the transformation rate coefficient. The magnitude of such an overall exchange rate coefficient or of individual exchange rate coefficients for different species and different types of particles could be estimated based on diffusion coefficients and kinetic theory of condensed phases. A detailed discussion of this issue, however, is beyond the scope of this framework paper.

c) Overall transfer fluxes

Combining the above equations describing the two different transfer mechanisms, the overall transfer fluxes of non-volatile species Y_j between the quasi-static surface layer and the near-surface particle bulk, J_{ss,b,Y_j} and J_{b,ss,Y_j} can be expressed as

$$J_{ss,b,Y_j} = J_{ss,b,rx,Y_j} + J_{ss,b,ex,Y_j} = k_{ss,b,Y_j}[Y_j]_{ss} \quad (62)$$

$$J_{b,ss,Y_j} = J_{b,ss,rx,Y_j} + J_{b,ss,ex,Y_j} = k_{b,ss,Y_j}[Y_j]_{bs} \quad (63)$$

With pseudo-first-order transfer rate coefficients

$$k_{ss,b,Y_j} = k_{ss,b,rx,Y_j} + k_{ss,b,ex,Y_j} \quad (64)$$

and

$$k_{b,ss,Y_j} = k_{b,ss,rx,Y_j} + k_{b,ss,ex,Y_j} \quad (65)$$

3.5. Bulk reactivity and solubility

As outlined in Sects. 3.1–3.4 the concentrations of X_i and Y_j in the near-surface particle bulk, $[X_i]_{bs}$ and $[Y_j]_{bs}$, can influence the interaction between gas and surface molecules and can be changed by surface-bulk mass transport and reactions. On the other hand,

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the composition of the near-surface particle bulk is influenced by transport, solubility, and chemical reaction in the particle bulk, which will generally change over time (solubility saturation, depletion of reaction partners and change of diffusion coefficients due to chemical aging).

5 A detailed discussion of physico-chemical processes within the particle bulk is beyond the scope of this paper, which is focused on aerosol surface chemistry. Here we just include a couple of special cases which are also considered in traditional resistor model formulations.

3.5.1. Chemical reaction

10 Under steady-state conditions and if surface-bulk reactions are negligible, the net mass transport flux of X_i from the surface to the near-surface particle bulk, J_{s,b,net,X_i} , can be matched with the so-called reacto-diffusive flux of X_i in the particle bulk, J_{b,rd,X_i} :

$$J_{s,b,net,X_i} = J_{s,b,X_i} - J_{b,s,X_i} = J_{b,rd,X_i} \quad (66)$$

15 J_{b,rd,X_i} is the flux of X_i from the near-surface particle bulk towards the particle core which is driven by the consumption of X_i through chemical reaction. Assuming spherical geometry, a uniform pseudo-first-order loss rate coefficient k_{b,X_i} , and a uniform diffusion coefficient D_{b,X_i} of X_i in the particle bulk, the reacto-diffusive flux can be expressed as (Hanson, 1997):

$$J_{b,rd,X_i} = C_{b,rd,X_i} \sqrt{k_{b,X_i} D_{b,X_i}} [X_i]_{bs} \quad (67)$$

20 C_{b,rd,X_i} is the reacto-diffusive geometry correction factor (conversion from planar to spherical geometry) which is determined by the particle radius, r_p , and the so called reacto-diffusive length for species X_i , $l_{rd,X_i} = (D_{b,X_i}/k_{b,X_i})^{1/2}$:

$$C_{b,rd,X_i} = \coth\left(\frac{r_p}{l_{rd,X_i}}\right) - \frac{l_{rd,X_i}}{r_p} \quad (68)$$

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According to Eqs. (66), (67), (55), and (56) the concentration ratio $[X_i]_{bs}/[X_i]_s$ under steady-state conditions is given by

$$\frac{[X_i]_{bs}}{[X_i]_s} = \frac{k_{s,b,Xi}}{k_{b,s,Xi} + C_{b,rd,Xi} \sqrt{k_{b,Xi} D_{b,Xi}}} \quad (69)$$

and the net flux of surface-to-bulk mass transport can be expressed as a function of $[X_i]_s$ and a pseudo-first-order transfer rate coefficient $k_{s,b,net,Xi}$:

$$J_{s,b,net,Xi} = k_{s,b,net,Xi} [X_i]_s \quad (70)$$

$$k_{s,b,net,Xi} = \frac{k_{s,b,Xi} C_{b,rd,Xi} \sqrt{k_{b,Xi} D_{b,Xi}}}{k_{b,s,Xi} + C_{b,rd,Xi} \sqrt{k_{b,Xi} D_{b,Xi}}} = k_{s,b,Xi} \left(1 + \frac{k_{b,s,Xi}}{C_{b,rd,Xi} \sqrt{k_{b,Xi} D_{b,Xi}}} \right)^{-1} \quad (71)$$

Formalisms for the description of reactive transformation of the particle bulk composition by diffusion and chemical reaction as a function of gas-particle interaction time have been presented and applied in recent studies (Worsnop et al., 2002; Smith et al., 2002, 2003). Again a detailed discussion of such processes is beyond the scope of this paper, but it should be possible to flexibly include such formalismss in the model framework presented here. In fact, it is certainly more straightforward to include additional processes in the flux-based kinetic model framework presented here than in the traditional resistor model.

3.5.2. Dissolution

Under mass transport equilibrium conditions (negligible chemical loss and production) the rate coefficients of gas-surface and surface-bulk transport can be combined to obtain the solubility or gas-particle partitioning coefficient, $K_{sol,cp,Xi}$, which describes the partitioning of a volatile species between gas phase and condensed phase (particle bulk). At infinite dilution, i.e. for ideal or at least highly dilute solutions, $K_{sol,cp,Xi}$ equals

the Henry's law coefficient for X_i in the investigated condensed phase, H_{cp,X_i} . Solubilities or Henry's law coefficients are usually given in molar concentration per unit pressure (index "cp"; Sander, 1999), but by multiplication with the gas constant, R , and absolute temperature, T , they can be converted into units of number concentration in the liquid phase per number concentration in the gas phase (dimensionless; index "cc"):

$$K_{sol,cc,X_i} = K_{sol,cp,X_i} RT = [X_i]_{b,sat} / [X_i]_{g,sat} \quad (72)$$

$[X_i]_{b,sat}$ and $[X_i]_{g,sat}$ are the equilibrium or solubility saturation number concentrations of X_i in the gas phase and condensed phase (particle bulk), respectively. Mass balance implies $k_{s,b,X_i} [X_i]_{s,sat} = k_{b,s,X_i} [X_i]_{b,sat}$ and $k_{d,X_i} [X_i]_{s,sat} = k_{a,X_i} [X_i]_{g,sat}$, which leads to

$$K_{sol,cc,X_i} = \frac{k_{s,b,X_i}}{k_{b,s,X_i}} \frac{k_{a,X_i}}{k_{d,X_i}} = \frac{k_{s,b,X_i}}{k_{b,s,X_i}} \frac{S_{X_i} \omega_{X_i}}{4k_{d,X_i}} \quad (73)$$

Equation (73) is equivalent to an expression previously derived by Hanson (1997), who also pointed out that the fractional surface coverage has to be taken into account in case of Langmuir-type adsorption with significant surface coverage but did not explicitly follow up on the implications. The direct proportionality between K_{sol,cc,X_i} and S_{X_i} , however, implies a gas phase composition dependence of the solubility, because S_{X_i} decreases with increasing surface and gas phase concentration of all competitively co-adsorbing species. This effect limits the applicability of solubilities or Henry's law coefficients determined for highly dilute solutions ($[X_i]_b \approx 0$, $\theta_s \approx 0$, $S_{X_i} \approx S_{0,X_i}$, $K_{sol,cc,X_i} \approx H_{cc,X_i}$). Surface saturation effects are expected to be important in case of high concentrations (laboratory studies) and viscous liquids with slow surface-bulk mass transport (e.g. liquid organic droplets or particle coatings; Marcolli et al., 2004). They may also affect atmospheric cloud droplets contaminated with organic surfactants as pointed out by Djikaev and Tabazadeh (2003). For such systems K_{sol,cc,X_i} and K_{sol,cp,X_i} , respectively, have to be deconvoluted into the underlying gas-surface and surface-bulk exchange rate coefficients in order to allow reliable application and

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extrapolation of solubilities or Henry's law coefficients to varying conditions in the atmosphere or laboratory experiments. Exemplary calculations of $K_{\text{sol,cc},X_i}$ as a function of $[X_i]_{\text{g}}$, S_{0,X_i} , k_{d,X_i} , $k_{\text{s,b},X_i}$, and $k_{\text{b,s},X_i}$ as well as the time dependence of solubility-driven, non-reactive gas uptake into liquids will be illustrated in a companion paper (Ammann and Pöschl, 2005). Note that the concentration dependence following from the kinetic model of gas-particle partitioning is consistent with the correction of thermodynamic Henry's law coefficients (limiting case for dilute solutions) by activity coefficients for concentrated solutions.

3.6. Overall gas uptake

Based on Eqs. (15) and (29) the overall flux of net uptake of a volatile species X_i by the condensed phase can be described by

$$J_{\text{net},X_i} = J_{\text{ads},X_i} - J_{\text{des},X_i} + L_{\text{g,gsr},X_i} - P_{\text{g,gsr},X_i} \quad (74)$$

with

$$J_{\text{ads},X_i} - J_{\text{des},X_i} = d[X_i]_{\text{s}}/dt - (P_{\text{s},X_i} - L_{\text{s},X_i}) - (J_{\text{b,s},X_i} - J_{\text{s,b},X_i}) \quad (75)$$

Accordingly, the uptake coefficient can be expressed as

$$\gamma_{X_i} = \gamma_{\text{sor},X_i} + \gamma_{\text{gsr},X_i} \quad (76)$$

with

$$\gamma_{\text{sor},X_i} = \frac{J_{\text{ads},X_i} - J_{\text{des},X_i}}{J_{\text{coll},X_i}} \quad (77)$$

$$\gamma_{\text{gsr},X_i} = \frac{L_{\text{g,gsr},X_i} - P_{\text{g,gsr},X_i}}{J_{\text{coll},X_i}} \quad (78)$$

The “sorption uptake coefficient”, γ_{sor,X_i} , and the “gas-surface reaction uptake coefficient”, γ_{gsr,X_i} , are limited to $\gamma_{\text{sor},X_i} \leq S_{X_i} \leq 1$, $\gamma_{\text{gsr},X_i} \leq 1$, and $\gamma_{\text{sor},X_i} + \gamma_{\text{gsr},X_i} \leq 1$, respectively.

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For values ≥ 0 , these uptake coefficients can be regarded as the probabilities that a collision of X_i with the surface leads to net uptake of X_i by adsorption (surface accommodation) and subsequent accumulation or reactive consumption at the surface or in the bulk of the particle (γ_{sor,X_i}), or by elementary gas-surface reactions (γ_{gsr,X_i}), respectively. Neither γ_{sor,X_i} nor γ_{gsr,X_i} , however, describe the probability for individual gas molecules X_i colliding with the surface to be taken up by or react with the condensed phase. In fact, γ_{sor,X_i} and γ_{gsr,X_i} can assume negative values if the particle acts as a source of X_i ($J_{\text{des},X_i} + P_{\text{g,gsr},X_i} > J_{\text{ads},X_i} + L_{\text{g,gsr},X_i}$), while at the same time the probability for an individual molecule colliding with the surface to be lost from the gas phase may still be larger than zero.

The probabilities for individual gas molecules colliding with the surface to be adsorbed or react at the surface are given by the following terms: S_{X_i} for adsorption (surface accommodation); $L_{\text{g,gsr},X_i}/J_{\text{coll},X_i}$ for elementary gas surface reactions; $S_{X_i}L_{\text{s},X_i}/(L_{\text{s},X_i} + J_{\text{des},X_i} + J_{\text{s,b},X_i})$ for adsorption and subsequent surface layer reaction. The probability for a gas molecule colliding with the surface to enter the bulk of the particle is given by:

$$\alpha_{X_i} = S_{X_i} \frac{J_{\text{s,b},X_i}}{J_{\text{s,b},X_i} + J_{\text{des},X_i} + L_{\text{s},X_i}} \quad (79)$$

In the atmospheric chemistry literature α_{X_i} is usually called “mass accommodation coefficient”, but we propose to call it “bulk accommodation coefficient” instead. This terminology helps to clearly distinguish the overall process of mass transport across the gas-particle interface, i.e. from the near-surface gas phase onto the particle surface and further into the (near-surface) particle bulk which is characterised by α_{X_i} (“bulk accommodation”), from its first (quasi-)elementary step characterised by S_{X_i} (“surface accommodation”). Note that S_{X_i} is the maximum value for α_{X_i} as well as for γ_{sor,X_i} but not for γ_{X_i} and γ_{gsr,X_i} , which can exceed S_{X_i} in case of significant gas-surface reactions.

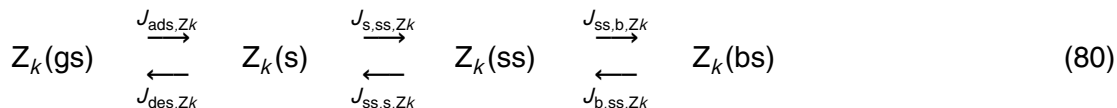
In this manuscript we have chosen the symbols S_{X_i} and α_{X_i} for surface and bulk accommodation coefficients, respectively, in order to support clear distinction of the sur-

face and bulk accommodation processes and compatibility with earlier publications on surface reactions in the atmospheric science community (e.g. Hanson, 1997; Worsnop, 2002; Ammann et al., 2003; Reid and Sayer, 2003; Rudich, 2003; and references therein). Nevertheless, we would like to point out that it might be beneficial for future developments to introduce the symbols α_{s,X_i} and α_{b,X_i} for surface and bulk accommodation coefficients, in order to maximize the self-consistency of terminology (greek letters for all quantities normalized by the gas kinetic flux) and to minimize the potential for confusion with related but differently defined quantities in surface science (sticking vs. trapping probabilities; Sect. 3.2).

The development of the model framework presented here has been targeted primarily at the description of aerosol surface chemistry. Nevertheless Eqs. (74) to (79) are equally applicable to systems where the rate of gas uptake is dominated by particle bulk processes (e.g. liquid droplets with reactive bulk components and highly dynamic surfaces). In such cases the above relations simplify to $\gamma_{X_i} \approx \gamma_{\text{sor},X_i} \approx (J_{s,b,X_i} - J_{b,s,X_i})/J_{\text{coll},X_i}$ and $\alpha_{X_i} \approx S_{X_i}$ as will be illustrated by exemplary model calculations in a companion paper (Ammann and Pöschl, 2005).

3.7. Semivolatile chemical species

Semivolatile species, Z_k , could be described and flexibly included in the double-layer model framework outlined above with the following relations:



$$d[Z_k]_s/dt = J_{\text{ads},Z_k} - J_{\text{des},Z_k} + P_{s,Z_k} - L_{s,Z_k} + J_{\text{ss},s,Z_k} - J_{s,\text{ss},Z_k} \quad (81)$$

$$d[Z_k]_{\text{ss}}/dt = J_{s,\text{ss},Z_k} - J_{\text{ss},s,Z_k} + P_{\text{ss},Z_k} - L_{\text{ss},Z_k} + J_{b,\text{ss},Z_k} - J_{\text{ss},b,Z_k} \quad (82)$$

$[Z_k]_s$ and $[Z_k]_{\text{ss}}$ are the concentrations of Z_k in the sorption layer and quasi-static surface layer, respectively (number per unit area). J_{ss,s,Z_k} and J_{s,ss,Z_k} are the flux densities

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of mass transport from the quasi-static surface layer to the sorption layer and vice versa (number per unit area and unit time). All other flux densities on the right hand side of Eqs. (81) and (82) are analogous to those described above for volatile and non-volatile species. The relevant processes are illustrated in Figs. 4 (transport) and 5 (chemical reaction).

Equations (80)–(82) should allow to describe also multilayer adsorption (Vinokurov and Kankare, 2002) and bulk condensation processes within the presented kinetic model framework. In the sorption layer, Z_k would competitively inhibit the adsorption of other semivolatile or volatile species as described for X_j in Sect. 3.2. In the quasi-static surface layer, on the other hand, Z_k would provide sorption sites (area) for gas molecules. The extent to which a semivolatile species at the particle surface acts as an adsorbate species or as a quasi-static surface component, i.e. its effective volatility and gas-particle partitioning, could be described by the ratio of the rate parameters governing the reversible transfer of Z_k between the two surface layers. Transfer from the quasi-static surface layer to the sorption layer is a (formal) kinetic step which can be pictured as a thermal activation process transforming a quasi-static surface component (with relatively low potential energy) into an adsorbate species (with relatively high potential energy) which can either desorb into the gas phase or return to the quasi-static surface (thermal deactivation). In principle, all species of aerosol and cloud systems could be treated as semivolatile species Z_k , the distinction between volatile species X_j and non-volatile species Y_j could be abandoned, and formalisms for the calculation of the flux terms on the right hand side of Eqs. (81) and (82) could be developed in analogy to the formalisms for volatile and non-volatile species presented above. $J_{ss,s,Zk}$ and $J_{s,ss,Zk}$ could be described in a similar way as $J_{b,ss,Yj}$ and $J_{ss,b,Yj}$ (Sect. 3.4.2). A detailed description of semivolatile species, multilayer adsorption, and bulk condensation processes is, however, beyond the scope of this manuscript.

For particles consisting of a semivolatile main component at steady-state (e.g. H_2O in liquid or solid cloud particles), the effects of continuous surface regeneration by condensation and evaporation of the semivolatile main component can be convoluted

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into the effective rate parameters describing the mass transport of volatile trace species across the gas-particle interface, and the semivolatile main particle component can be regarded as quasi-non-volatile. In fact, this is an implicit assumption of the traditional resistor model for the interaction of reactive trace gases with cloud droplets.

4. Model application and special cases

4.1. Composition, time, and temperature dependencies

The flux formalism and rate equations presented above allow to describe mass transport, chemical reaction and changing chemical composition in aerosol and cloud systems with multiple chemical species and competitive processes under transient conditions. For such systems the surface mass balance equations given in Sect. 3.1 lead to a set of coupled differential equations. These can be solved numerically by inserting the rate equations given in Sects. 3.2–3.5 or alternative/complementary mathematical descriptions of the involved physicochemical processes, provided that the initial concentrations and relevant mass transport and reaction rate coefficients are known or can be reasonably estimated. Exemplary practical applications and model calculations will be presented in a companion paper (Ammann and Pöschl, 2005).

In the rate equations of Sect. 3 gas phase diffusion effects are implicitly taken into account by considering gas phase concentrations close to the surface, $[X_i]_{gs}$, rather than average gas phase concentrations, $[X_i]_g$. As outlined in Sect. 2, $[X_i]_{gs}$ can be calculated by multiplication of $[X_i]_g$ with the gas phase diffusion correction factor $C_{g,Xi}$ which is determined by the uptake coefficient γ_{Xi} and the Knudsen number Kn_{Xi} .

For consistent analysis and interpretation of kinetic measurement data of aerosol and cloud surface chemistry and gas-particle interactions and for their application and extrapolation in atmospheric models it is important to recognize the (potential) dependence of rate parameters on the composition of the investigated system. In this respect the rate parameters introduced in the presented model framework (above and in the

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following sections) can be classified as follows:

1. Rate parameters which can be influenced by the gas phase, double-layer surface, and particle bulk composition of the investigated aerosol (alphabetical order): α_{Xi} , γ_{Xi} , $\gamma_{eff,Xi}$, $\gamma_{gsr,Xi}$, $\gamma_{sor,Xi}$, $\Gamma_{b,Xi}$, $\Gamma_{g,Xi}$, $\Gamma_{s,Xi}$, $\Gamma_{s,b,Xi}$, $C_{g,Xi}$, $k_{a,Xi}$, $k_{b,ss,rx,Yj}$, $k_{b,ss,Yj}$, $k_{g,p,Xi}$, $k_{ss,rx}$, $k_{ss,b,rx,Yj}$, $k_{ss,b,Yj}$, $k_{s,Xi}$, $k_{s,g,Xi}$, $k_{s,s,Xi}$, $k_{ss,Yj}$, $k_{ss,g,Yj}$, $k_{ss,s,Yj}$, $K'_{ads,Xi}$, $K_{sol,cc,Xi}$, $K_{sol,cp,Xi}$, S_{Xi} .
2. Rate parameters which are assumed to be independent of gas phase and sorption layer composition but can be influenced by the quasi-static surface layer and near-surface particle bulk composition: $\gamma_{GSRu,Xi,Xp}$, $\gamma_{GSRu,Xi,Yq}$, $\tau_{d,Xi}$, $\tau_{s,b,Xi}$, $H_{cc,Xi}$, $H_{cp,Xi}$, $k_{a,0,Xi}$, $k_{d,Xi}$, $k_{b,s,Xi}$, $k_{b,ss,ex,Yj}$, $k_{s,b,Xi}$, $k_{s,b,net,Xi}$, $k_{ss,b,ex,Yj}$, $k_{s,ss,Xi}$, $k_{ss,ss,Yj}$, $k_{SLRv,Xp}$, $k_{SLRv,Yp}$, $k_{SLRv,Xp,Xq}$, $k_{SLRv,Xp,Yq}$, $k_{SLRv,Yp,Yq}$, $k_{SBRw,Yp,Xr}$, $k_{SBRw,Yp,Yq}$, $K_{ads,Xi}$, $S_{0,Xi}$.
3. Rate parameters which are assumed to be independent of double-layer surface composition but depend on gas phase or particle bulk composition, respectively: $C_{b,rd,Xi}$, $D_{b,Xi}$, $D_{g,Xi}$, $k_{b,Xi}$, $I_{rd,Xi}$.

Characteristic composition dependencies, in particular the effects of varying gas phase concentrations, will be illustrated in a companion paper (Ammann and Pöschl, 2005).

In transient systems, composition-dependent rate parameters are likely to exhibit pronounced time dependencies, which may vary with the chemical nature and physical state of the aerosol and its components. Exemplary temporal evolutions of aerosol surface composition and rate parameters will be illustrated in a companion paper (Ammann and Pöschl, 2005).

Of course the rate parameters of mass transport and chemical reaction introduced above will exhibit more or less pronounced temperature dependencies, which can be described by appropriate mathematical formalisms like Arrhenius equations. This approach has already been introduced and applied for the description of selected adsorption and reaction processes in stratospheric aerosols at different temperatures (Elliott

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et al., 1991; Tabazadeh and Turco, 1993; Mozurkevich, 1993; Carslaw and Peter, unpublished manuscript, 1997), and for specific systems the required thermochemical data are available in the scientific literature of physical chemistry and chemical engineering (e.g. Masel, 1996; and references therein). For detailed and reliable models of atmospheric aerosol chemistry the temperature dependencies of rate parameters will have to be further explored and characterized in analogy to atmospheric gas phase reaction rate coefficients (Sander et al., 2002; Atkinson et al., 2004). Appropriate formalisms and parameters (Arrhenius equations and activation energies, etc.) can be flexibly included in the presented model framework, but a detailed treatment of this aspect would go beyond the scope of this paper.

In aerosol or cloud systems with insignificant chemical reactions at the particle surface ($P_{g,gsr,X_i}=L_{g,gsr,X_i}=P_{s,g,X_i}=L_{s,g,X_i}=0$), it is not necessary to resolve the elementary steps of gas-surface and surface-bulk transport, and the bulk accommodation coefficient is sufficient to describe mass balance at the gas-particle interface in accordance with classical formalisms of cloud microphysics.

When only reversible adsorption and surface layer reactions of volatile species but no gas-surface and surface bulk reactions or surface-bulk transfer are considered ($P_{g,gsr,X_i}=L_{g,gsr,X_i}=P_{s,g,X_i}=L_{s,g,X_i}=J_{b,s,X_i}=J_{s,b,X_i}=0$), the formalisms outlined above are equivalent to classical Langmuir-Hinshelwood reaction mechanisms. If on the other hand only elementary gas-surface reactions of volatile species but no surface-layer reactions and surface-bulk reactions or surface-bulk transfer are considered ($P_{s,s,X_i}=L_{s,s,X_i}=P_{s,ss,X_i}=L_{s,ss,X_i}=J_{b,s,X_i}=J_{s,b,X_i}=0$), they are equivalent to classical Eley-Rideal reaction mechanisms. For these two types of reaction mechanisms a wide range of special cases with different rate limiting steps (adsorption, desorption, or chemical reaction) and different types of interacting species have been described in the scientific literature of chemical engineering and catalysis (Masel, 1996). The rate equations for chemical surface reactions following these mechanistic schemes can be readily inserted into the presented model framework.

Characteristic effects of reversible adsorption and particle aging on the

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concentration- and time-dependence of uptake coefficients in simple Langmuir-Hinshelwood reaction systems have already been presented by Ammann et al. (2003). Further exemplary model systems and calculations involving multiple chemical species, reactions, and mass transport processes under transient and steady-state conditions will be presented and discussed in a companion paper (Ammann and Pöschl, 2005).

In the following sections we present rate equations and equivalent resistor model formulations derived from the general formalisms presented above for several special cases involving reversible adsorption and reactions at the particle surface as well as surface-bulk transfer processes under (quasi-)steady-state conditions. They are based on the assumption of constant gas phase and particle composition (quasi-steady-state approximation, QSSA), which is generally applicable to describe chemical kinetics on short time-scales and can be extended to longer time-scales by iterative calculations as will be illustrated in a companion paper (Ammann and Pöschl, 2005).

In Sect. 4.2 we consider “adsorption equilibrium” conditions where the surface concentration of volatile species is determined by reversible adsorption which proceeds much faster and can be regarded as fully decoupled from all other involved processes. In Sect. 4.3 we consider “adsorption-reaction steady-state” conditions where the surface concentration of volatile species is determined by reversible adsorption, surface reactions, and surface-bulk exchange which proceed at rates of comparable magnitude and have to be treated as coupled processes.

4.2. Adsorption equilibrium conditions

4.2.1. Surface concentration of X_i

At steady state ($d[X_i]_s/dt=0$) and when the rates of adsorption and desorption are of similar magnitude and much higher than the rates of all other processes affecting the surface concentration of a species X_i and its particle-related gas phase loss, X_i can be assumed to be in adsorption equilibrium and $[X_i]_s$ can be approximated by equating

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the fluxes of adsorption and desorption:

$$J_{\text{ads},X_i} \approx J_{\text{des},X_i} \gg P_{\text{g,gsr},X_i} + L_{\text{g,gsr},X_i} + P_{\text{s},X_i} + L_{\text{s},X_i} + J_{\text{b,s},X_i} + J_{\text{s,b},X_i}, \quad (83)$$

Combining relations (33)–(34) and (38)–(40), and introducing a (Langmuir) adsorption equilibrium constant K_{ads,X_i} leads to

$$K_{\text{ads},X_i}[X_i]_{\text{gs}} = \frac{\theta_{\text{s},X_i}}{1 - \theta_{\text{s}}} = \frac{\theta_{\text{s},X_i}}{1 - \sum_p \theta_{\text{s},X_p}} \quad (84)$$

with

$$K_{\text{ads},X_i} = \frac{\sigma_{X_i} k_{\text{a},0,X_i}}{k_{\text{d},X_i}} = S_{0,X_i} \frac{\sigma_{X_i} \omega_{X_i}}{4k_{\text{d},X_i}} \quad (85)$$

If all other competitively adsorbing species X_p are assumed to be in adsorption equilibrium as well, their fractional surface coverages can be substituted by $\theta_{\text{s},X_p} = \theta_{\text{s},X_i} K_{\text{ads},X_p} [X_p]_{\text{gs}} / (K_{\text{ads},X_i} [X_i]_{\text{gs}})$, and the surface concentration of X_i as well as the overall fractional surface coverage θ_{s} can be expressed as a function of gas phase concentrations and adsorption equilibrium constants:

$$[X_i]_{\text{s}} = \sigma_{X_i}^{-1} \frac{K_{\text{ads},X_i} [X_i]_{\text{gs}}}{1 + \sum_p K_{\text{ads},X_p} [X_p]_{\text{gs}}} \quad (86)$$

$$\theta_{\text{s}} = \frac{\sum_p K_{\text{ads},X_p} [X_p]_{\text{gs}}}{1 + \sum_p K_{\text{ads},X_p} [X_p]_{\text{gs}}} \quad (87)$$

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4.2.2. Surface and bulk accommodation and net uptake of X_i

The surface and bulk accommodation coefficients under adsorption equilibrium conditions follow from relations (32)–(33), (79), (83), (85) and (87):

$$S_{X_i} = \frac{S_{0,X_i}}{1 + \sum_p K_{\text{ads},X_p} [X_p]_{\text{gs}}} \quad (88)$$

$$\alpha_{X_i} = S_{X_i} \frac{k_{\text{s,b},X_i}}{k_{\text{s,b},X_i} + k_{\text{d},X_i}} \quad (89)$$

Jayne et al. (1990) derived similar expressions to describe the dependence of SO_2 uptake into aqueous solution droplets on gas phase concentration and surface coverage. Relations equivalent to (89) have also been derived by Davidovits et al. (1995) and Hanson (1997), but they did not explicitly account for competitive adsorption and assumed S_{X_i} to be the maximum value not only for α_{X_i} but also for γ_{X_i} , neglecting the possibility of gas-surface reactions (Eqs. 74–79).

The net flux of X_i from the gas phase to the condensed phase under adsorption equilibrium conditions can be calculated from

$$J_{\text{net},X_i} = L_{\text{g,gsr},X_i} - P_{\text{g,gsr},X_i} + L_{\text{s},X_i} - P_{\text{s},X_i} + J_{\text{s,b},X_i} - J_{\text{b,s},X_i}. \quad (90)$$

By inserting Eq. (86) into the formulae presented in Sects. 3.3 and 3.4 all terms on the right hand side of Eq. (90) and J_{net,X_i} can be expressed as explicit functions of the near-surface gas phase concentrations of all competitively adsorbing volatile species and of the surface and near-surface bulk concentrations of non-volatile particle components. In the same way γ_{sor,X_i} , γ_{gsr,X_i} , and γ_{X_i} can be expressed and calculated according to Eqs. (74)–(78).

From relations (74)–(78) and (83) follows $\gamma_{\text{sor},X_i} \ll 1$, $\gamma_{\text{gsr},X_i} \ll 1$, and $\gamma_{X_i} \ll 1$. Provided that the particle diameter is not much larger than the mean free path of X_i and according to Eqs. (4), (14), (19), and (20), $\gamma_{X_i} \ll 1$ implies $C_{\text{g},X_i} \approx 1$, $[X_i]_{\text{g,s}} \approx [X_i]_{\text{g}}$, and

$Y_{X_i} \approx Y_{\text{eff},X_i}$. Thus the average gas phase concentration $[X_i]_g$ can be used instead of $[X_i]_{g,s}$ under these conditions.

4.2.3. Surface concentration of Y_j

For non-volatile particle components Y_j the rate of surface concentration change, $d[Y_j]_{ss}/dt$, is given by Eq. (29). Under adsorption equilibrium conditions all terms on the right hand side of Eq. (94) can be expressed as explicit functions of the near-surface gas phase concentrations of the competitively adsorbing and reacting volatile species and of the surface and near-surface bulk concentrations of non-volatile particle components by inserting Eq. (86) into the formulae presented in Sects. 3.3 and 3.4. In case of significant transformation of particle components by chemical reaction (chemical aging of the particle), their change of surface and near-surface bulk concentration changes can feed back into the calculation of surface reaction rates and adsorption equilibrium constants via Eqs. (85), (35) for S_{0,X_i} , and analogous equations for other rate parameters. Under these conditions the calculation of surface and near-surface bulk concentrations has to be iterated for both volatile and non-volatile species in order to maintain the quasi-steady-state approximation (assumption of constant chemical composition) on which Eqs. (86)–(90) are based.

4.2.4. Special Case A: “adsorption equilibrium and negligible chemical production at the surface”

20 *Net uptake of X_i*

For a species X_i with negligible chemical production at the particle surface ($P_{g,gsrX_i} + P_{s,X_i} \ll L_{s,X_i} + J_{s,b,X_i} + J_{b,s,X_i}$), Eq. (90) can be reduced to

$$J_{\text{net},X_i} = L_{g,gsr,X_i} + L_{s,X_i} + J_{s,b,X_i} - J_{b,s,X_i}. \quad (91)$$

Based on the formulae of Sect. 3.3, the chemical loss terms L_{g,gsr,X_i} and L_{s,X_i} can be described as a pseudo-first order processes with the following rate equations and

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parameters:

$$L_{g,gsr,Xi} = \gamma_{gsr,Xi} \omega_{Xi} / 4 [X_i]_{gs} \quad (92)$$

$$L_{s,Xi} = k_{s,Xi} [X_i]_s \quad (93)$$

$$\begin{aligned} \gamma_{gsr,Xi} = - \sum_u C_{GSRu,g,Xi} \left(\sum_p \gamma_{GSRu,g,Xi,Xp} \frac{K_{ads,Xp} [X_p]_{gs}}{1 + \sum_q K_{ads,Xq} [X_q]_{gs}} + \right. \\ \left. \sum_r \gamma_{GSRu,g,Xi,Yr} \sigma_{Yr} [Y_r]_{ss} \frac{1}{1 + \sum_q K_{ads,Xq} [X_q]_{gs}} \right) \end{aligned} \quad (94)$$

$$k_{s,Xi} = k_{s,g,Xi} + k_{s,s,Xi} + k_{s,ss,Xi} \quad (95)$$

$$k_{s,g,Xi} = -\sigma_{Xi} \sum_u \sum_p C_{GSRu,s,Xi} \gamma_{GSRu,Xi,Xp} \frac{\omega_{Xp}}{4} [X_p]_{gs} \quad (96)$$

$$k_{s,s,Xi} = - \sum_v C_{SLRV,s,Xi} \left(k_{SLRV,Xi} + \sum_p k_{SLRV,Xi,Xp} \sigma_{Xp}^{-1} \frac{K_{ads,Xp} [X_p]_{gs}}{1 + \sum_q K_{ads,Xq} [X_q]_{gs}} \right) \quad (97)$$

$$k_{s,ss,Xi} = - \sum_v \sum_q C_{SLRV,s,Xi} k_{SLRV,Xi,Yq} [Y_q]_{ss} \quad (98)$$

$k_{s,Xi}$ is the overall pseudo-first-order rate coefficient for the chemical loss of X_i in the sorption layer. $k_{s,g,Xi}$, $k_{s,s,Xi}$, and $k_{s,ss,Xi}$ are individual pseudo-first-order loss rate coefficients for gas-surface reactions and surface layer reactions within the sorption layer or between sorption layer and quasi-static surface layer, respectively.

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According to Sect. 3.5.1 the net surface-bulk transfer of X_i under steady-state conditions can also be described as a pseudo-first-order process with a rate coefficient k_{s,b,net,X_i} . Combining Eqs. (70), (77), (86), and (93) leads to

$$\gamma_{sor,X_i} = S_{X_i} \frac{k_{s,X_i} + k_{s,b,net,X_i}}{k_{d,X_i}} \quad (99)$$

5 The overall uptake coefficient for X_i is given by the sum of γ_{gsr,X_i} and γ_{sor,X_i} (Eq. 76).

Surface concentration of Y_j

Assuming that there is no or negligible chemical production, surface-bulk reaction, and surface-bulk transport of a non-volatile particle component Y_j , its surface concentration change over time can be described by

$$10 \quad d[Y_j]_{ss}/dt = -(L_{ss,g,Y_j} + L_{ss,s,Y_j} + L_{ss,ss,Y_j}) = -k_{ss,Y_j}[Y_j]_{ss} \quad (100)$$

with an overall pseudo-first-order loss rate coefficient $k_{ss,Y_j} = k_{ss,g,Y_j} + k_{ss,s,Y_j} + k_{ss,ss,Y_j}$ that comprises individual pseudo-first-order rate coefficients for gas-surface reactions and surface layer reactions within the quasi-static layer or between sorption layer and quasi-static layer, respectively:

$$15 \quad k_{ss,g,Y_j} = -\sigma_{Y_j} \sum_u \sum_p C_{GSRu,ss,Y_j} \gamma_{GSRu,X_i,Y_j} \frac{\omega_{X_p}}{4} [X_p]_{gs} \quad (101)$$

$$k_{ss,s,Y_j} = - \sum_v \sum_p C_{SLRV,ss,Y_j} k_{SLRV,X_p,Y_j} \sigma_{X_p}^{-1} \frac{K_{ads,X_p}[X_p]_{gs}}{1 + \sum_q K_{ads,X_q}[X_q]_{gs}} \quad (102)$$

$$k_{ss,ss,Y_j} = - \sum_v C_{SLRV,ss,Y_j} \left(k_{SLRV,Y_j} + \sum_q k_{SLRV,Y_q,Y_j} [Y_q]_s \right) \quad (103)$$

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4.3. Adsorption-reaction steady-state

When the rates of reaction at the surface or surface-bulk exchange of a volatile species X_i are of comparable magnitude as the rate of adsorption, no general explicit analytical expression like Eq. (86) can be derived to describe the surface concentration of volatile species as a function of their gas phase concentration. At steady-state, however, the surface mass balance of all competitively adsorbing and reacting volatile species X_p ($p=1 \dots i_{\max}$) can be described by a set of i_{\max} algebraic equations in the general form

$$J_{\text{ads},Xp} - J_{\text{des},Xp} + P_{s,Xp} - L_{s,Xp} + J_{b,s,Xp} - J_{s,b,Xp} = 0. \quad (104)$$

After inserting the rate equations and rate coefficients defined in Sects. 3.2–3.4, the near-surface gas phase concentrations of all competitively adsorbing volatile species and the surface and near-surface bulk concentrations of non-volatile particle components, Eq. (104) can be solved for the surface concentrations $[X_p]_s$, and the uptake coefficient γ_{X_i} can be calculated according to Eqs. (74)–(78).

In case of significant net consumption of particle components Y_q by chemical reaction (chemical aging of the particle), their surface and near-surface bulk concentration changes feed back into the calculation of mass transport and reaction rates at the surface. Under these conditions the calculation of surface and near-surface bulk concentrations has to be iterated for both volatile and non-volatile species in order to maintain the quasi-steady-state approximation (assumption of constant chemical composition) on which Eq. (104) is based.

In general Eq. (104) has to be solved numerically; only under restricted conditions explicit analytical expressions for $[X_p]_s$, γ_{Xp} , and $d[Y_j]_{ss}/dt$ can be derived as outlined above for general adsorption equilibrium conditions.

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4.3.1. Special Case B: “adsorption-reaction steady-state and negligible chemical production at the surface”

Surface concentration of X_i

For a species X_i with negligible chemical production at the particle surface
 5 $(P_{s,X_i} \ll J_{\text{des},X_i} + L_{s,X_i} + J_{s,b,X_i} + J_{b,s,X_i})$, the surface mass balance Eq. (104) can be reduced to

$$J_{\text{ads},X_i} = J_{\text{des},X_i} + L_{s,X_i} + J_{s,b,X_i} - J_{b,s,X_i}. \quad (105)$$

Inserting Eqs. (38), (40), (70), and (93) into (105) leads to

$$k_{a,0,X_i}[X_i]_{\text{gs}} \left(1 - \sum_p \theta_{s,X_p} \right) = \theta_{s,X_i} \sigma_{X_i}^{-1} (k_{d,X_i} + k_{s,X_i} + k_{s,b,\text{net},X_i}) \quad (106)$$

10 By introducing an effective adsorption equilibrium constant, K'_{ads,X_i} , Eq. (106) can be further rearranged to

$$K'_{\text{ads},X_i}[X_i]_{\text{gs}} = \frac{\theta_{s,X_i}}{1 - \theta_s} = \frac{\theta_{s,X_i}}{1 - \sum_p \theta_{s,X_p}} \quad (107)$$

with

$$K'_{X_i} = \frac{\sigma_{X_i} k_{a,0,X_i}}{k_{d,X_i} + k_{s,X_i} + k_{s,b,\text{net},X_i}} = S_{0,X_i} \frac{\sigma_{X_i} \omega_{X_i}}{4(k_{d,X_i} + k_{s,X_i} + k_{s,b,\text{net},X_i})} \quad (108)$$

15 If the assumption of negligible production by surface reaction can be extended to all competitively adsorbing species X_p (or at least to the species dominating the total sorption layer coverage), their fractional surface coverages can be substituted by

$\theta_{X_p} = \theta_{X_i} K'_{\text{ads},X_p} [X_p]_{\text{gs}} / (K'_{\text{ads},X_i} [X_i]_{\text{gs}})$, and $[X_i]_{\text{s}}$ as well as θ_{s} can be expressed as a function of gas phase concentrations and effective adsorption equilibrium constants:

$$[X_i]_{\text{s}} = \sigma_{X_i}^{-1} \frac{K'_{\text{ads},X_i} [X_i]_{\text{gs}}}{1 + \sum_p K'_{\text{ads},X_p} [X_p]_{\text{gs}}} \quad (109)$$

$$\theta_{\text{s}} = \frac{\sum_p K'_{\text{ads},X_p} [X_p]_{\text{gs}}}{1 + \sum_p K'_{\text{ads},X_p} [X_p]_{\text{gs}}} \quad (110)$$

5 Surface accommodation, bulk accommodation, and net uptake of X_i

For the surface and bulk accommodation coefficients under adsorption-reaction steady-state conditions follows

$$S_{X_i} = \frac{S_{0,X_i}}{1 + \sum_p K'_{\text{ads},X_p} [X_p]_{\text{gs}}} \quad (111)$$

$$\alpha_{X_i} = S_{X_i} \frac{k_{\text{s,b},X_i}}{k_{\text{s,b},X_i} + k_{\text{s,X}_i} + k_{\text{d},X_i}} \quad (112)$$

- 10 Based on Eq. (109) and in analogy to Special Case A (Sect. 3.2.1, Eqs. 91–99) the following expressions can be derived for the gas-surface reaction uptake coefficient, the pseudo-first-order rate coefficient for reactive loss within the sorption layer, and the sorption uptake coefficient:

$$\gamma_{\text{gsr},X_i} = - \sum_u c_{\text{GSRu},g,X_i} \left(\sum_p \gamma_{\text{GSRu},X_i,X_p} \frac{K'_{\text{ads},X_p} [X_p]_{\text{gs}}}{1 + \sum_q K'_{\text{ads},X_q} [X_q]_{\text{gs}}} + \right.$$

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$$\sum_r \gamma_{\text{GSR},u,X_i,Y_r} \sigma_{Y_r} [Y_r]_{\text{ss}} \frac{1}{1 + \sum_q K'_{\text{ads},X_q} [X_q]_{\text{gs}}} \quad (113)$$

$$k_{\text{s},\text{s},X_i} = - \sum_v C_{\text{SLR},v,\text{s},X_i} \left(k_{\text{SLR},v,X_i} + \sum_p k_{\text{SLR},v,X_i,X_p} \sigma_{X_p}^{-1} \frac{K'_{\text{ads},X_p} [X_p]_{\text{gs}}}{1 + \sum_q K'_{\text{ads},X_q} [X_q]_{\text{gs}}} \right) \quad (114)$$

$$\gamma_{\text{sor},X_i} = S_{X_i} \frac{k_{\text{s},X_i} + k_{\text{s},\text{b},\text{net},X_i}}{k_{\text{s},X_i} + k_{\text{s},\text{b},\text{net},X_i} + k_{\text{d},X_i}} \quad (115)$$

5 k_{s,X_i} , $k_{\text{s},\text{g},X_i}$, $k_{\text{s},\text{ss},X_i}$, and $k_{\text{s},\text{b},\text{net},X_i}$ are defined in analogy to Special Case A, Eqs. (95), (96), (98), and (71). Again the overall particle-related gas phase loss is given by the sum of γ_{gsr,X_i} and γ_{sor,X_i} .

Note that the possibility of second order reactions within the sorption layer (adsorbate cross and self reactions) leads to a mutual interdependence of the effective adsorption equilibrium constant K'_{ads,X_i} and the pseudo-first-order surface loss rate coefficients k_{s,X_i} and $k_{\text{s},\text{s},X_i}$ as defined in Eqs. (108), (94), and (114): $k_{\text{s},\text{s},X_i}$ which is required for the calculation of k_{s,X_i} and K'_{ads,X_i} depends itself on the surface concentration of all adsorbed species $[X_p]_{\text{s}}$ and thus on K'_{ads,X_i} . As a consequence no explicit algebraic expression for K'_{ads,X_i} can be derived, and in general the surface concentrations and reaction rates have to be determined numerically. Only when second order sorption layer reactions are negligible against the overall surface reactivity ($\sum_p C_{\text{SLR},v,\text{s},X_i} k_{\text{SLR},v,X_i,X_p} [X_p]_{\text{s}} \ll k_{\text{s},X_i}$) or when surface reactivity is negligible against mass transport ($k_{\text{s},X_p} \ll k_{\text{d},X_p} + k_{\text{s},\text{b},\text{net},X_p}$), the effective adsorption equilibrium constant K'_{ads,X_i} can be expressed explicitly as a function of volatile species gas phase concentrations $[X_p]_{\text{gs}}$, non-volatile particle component surface concentrations $[Y_q]_{\text{ss}}$, and basic rate coefficients.

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Surface concentration of Y_j

The surface concentration change of a particle component Y_j with negligible chemical production, surface-bulk reaction, and surface-bulk mass transport can be calculated according to Eq. (100) with the same rate coefficients k_{ss,g,Y_j} and k_{ss,ss,Y_j} as in Special Case A, but with a modified pseudo-first-order surface reaction rate coefficient k_{ss,s,Y_j} and replacement of $K_{ads,Xp}$ by $K'_{ads,Xp}$:

$$k_{ss,s,Y_j} = - \sum_v \sum_p c_{SLRv,ss,Y_j} k_{SLRv,Xp,Y_j} \sigma_{Xp}^{-1} \frac{K'_{ads,Xp}[X_p]_{gs}}{1 + \sum_q K'_{ads,Xq}[X_q]_{gs}} \quad (116)$$

Effects of reversible and competitive adsorption

Reversible and competitive adsorption on a quasi-static surface implies that the surface accommodation coefficient of every species X_i decreases with increasing surface concentration and thus with increasing gas phase concentration of all competitively adsorbing species. Consequently all rate parameters proportional to S_{X_i} , including bulk accommodation, sorption uptake, and Henry's law coefficients, will also exhibit a dependence on gas phase composition which can only be neglected when the total sorption layer surface coverage is much less than unity ($\theta_s \ll 1$). For systems in Langmuir adsorption equilibrium or in adsorption-reaction steady-state with negligible surface production of volatile species, the condition $\theta_s \ll 1$ is fulfilled when the sum of the products of (near-surface) gas phase concentration and effective adsorption equilibrium constant of all volatile species X_p (including X_i) is much less than unity:

$$\sum_p K'_{ads,Xp}[X_p]_{gs} \ll 1. \quad (117)$$

Under these conditions S_{X_i} can be replaced by S_{0,X_i} , and the relation between gas phase and surface concentration of X_i becomes quasi-linear, as assumed by Han-

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son (1997):

$$[X_i]_s \approx \sigma_{Xi}^{-1} K'_{ads,Xi} [X_i]_{gs}. \quad (118)$$

Relations (117) and (118) may often be valid under atmospheric background conditions. For the modeling of highly polluted air masses (e.g. fossil fuel combustion or biomass burning plumes; Pöschl, 2002b; von Glasow et al., 2003; Hobbs et al., 2003; Jost et al., 2003; Meilinger et al., 2005) and for the analysis and extrapolation of laboratory experiments with relatively high trace gas concentrations, however, non-linear gas phase concentration dependencies of rate parameters caused by reversible and competitive adsorption can play an important role. (e.g. Pöschl et al., 2001; Ammann et al., 2003; and references therein). Exemplary model calculations and parameter variations will be illustrated in a companion paper (Ammann and Pöschl, 2005).

4.3.2. Resistor model formulation of Special Case B

To re-formulate the flux equations describing net gas uptake in Special Case B (adsorption-reaction steady-state and negligible chemical production at the surface) in terms of the traditional resistance model, Eq. (115) can be inverted to

$$\frac{1}{\gamma_{sor,Xi}} = \frac{1}{S_{Xi}} \left(1 + \frac{k_{d,Xi}}{k_{s,Xi} + k_{s,b,net,Xi}} \right) \quad (119)$$

All parameters in Eq. (119) are defined in the same way as in Sect. 3.2.1, and by inserting Eq. (71) for $k_{s,b,net,Xi}$ it can be further rearranged to

$$\frac{1}{\gamma_{sor,Xi}} = \frac{1}{S_{Xi}} + \frac{1}{S_{Xi} \frac{k_{s,Xi}}{k_{d,Xi}} + \frac{1}{\frac{1}{S_{Xi} \frac{k_{s,b,Xi}}{k_{d,Xi}}} + \frac{1}{S_{Xi} \frac{k_{s,b,Xi}}{k_{d,Xi}} \frac{C_{b,Xi} \sqrt{k_{b,Xi} D_{b,Xi}}}{k_{b,s,Xi}}}} \quad (120)$$

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and

$$\frac{1}{\gamma_{\text{sor},Xi}} = \frac{1}{S_{Xi}} + \frac{1}{\Gamma_{s,Xi} + \frac{1}{\frac{1}{\Gamma_{s,b,Xi}} + \frac{1}{\Gamma_{b,Xi}}}} \quad (121)$$

with

$$\Gamma_{s,Xi} = S_{Xi} \frac{k_{s,Xi}}{k_{d,Xi}} = \frac{4k_{a,Xi}}{\omega_{Xi}} \frac{k_{s,Xi}}{k_{d,Xi}} \quad (122)$$

$$5 \quad \Gamma_{s,b,Xi} = S_{Xi} \frac{k_{s,b,Xi}}{k_{d,Xi}} \quad (123)$$

$$\Gamma_{b,Xi} = S_{Xi} \frac{k_{s,b,Xi}}{k_{d,Xi}} \frac{C_{b,Xi} \sqrt{k_{b,Xi} D_{b,Xi}}}{k_{b,s,Xi}} = \frac{4}{\omega_{Xi}} K_{\text{sol,cp},Xi} N_A R T C_{b,Xi} \sqrt{k_{b,Xi} D_{b,Xi}} \quad (124)$$

Equation (121) is equivalent to earlier resistor model formulations (Hanson, 1997; Davidovits et al., 1995; Worsnop et al., 2002; Smith et al., 2003; Reid and Sayer, 2003; and references therein), in which the processes of surface reaction, surface-bulk transfer, and bulk diffusion and reaction are represented by the “conductance terms” (inverse resistances) $\Gamma_{s,Xi}$, $\Gamma_{s,b,Xi}$, and $\Gamma_{b,Xi}$.

In Eq. (121) and in most previous resistor model formulations, however, the possibility of elementary gas-surface reactions has not been taken into account. To account for such processes and to obtain a comprehensive expression for the uptake coefficient γ_{Xi} , $\gamma_{\text{gsr},Xi}$ as defined in Eq. (113) has to be added and Eq. (121) has to be extended to

$$15 \quad \gamma_{Xi} = \gamma_{\text{gsr},Xi} + \frac{1}{\frac{1}{S_{Xi}} + \frac{1}{\Gamma_{s,Xi} + \frac{1}{\frac{1}{\Gamma_{b,Xi}} + \frac{1}{\Gamma_{s,b,Xi}}}}} \quad (125)$$

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Even though this aspect tends to be obscured by resistance model formulations such as Eqs. (121) and (125), the gas-surface reaction probability γ_{gsr,X_i} is the only parameter in Eq. (125) which is independent of the surface accommodation coefficient S_{X_i} . Surface layer and bulk reactions are coupled to the surface accommodation process, and the conductance terms Γ_{s,X_i} , $\Gamma_{\text{s,b},X_i}$, and Γ_{b,X_i} are directly proportional to S_{X_i} as shown by Eqs. (122)–(124).

Only when the rates of elementary gas-surface reactions and surface-layer reactions are negligible against uptake into the particle bulk, i.e. when $\gamma_{\text{gsr},X_i} \ll \gamma_{\text{sor},X_i}$ and $k_{\text{s},X_i} \ll k_{\text{s,b,net},X_i}$, the terms γ_{gsr,X_i} and Γ_{s,X_i} can be omitted from Eq. (125). In this case the resistances $1/S_{X_i}$ and $1/\Gamma_{\text{s,b},X_i}$ can be convoluted into a “bulk accommodation resistance” $1/\alpha_{X_i}$ to obtain the traditional resistance model formulation for gas uptake by liquid droplets, Eq. (7), and the bulk accommodation coefficient α_{X_i} is given by Eq. (89).

5. Conclusions and outlook

Among the major obstacles on the way to full mechanistic understanding and reliable prediction of aerosol and cloud properties and effects on the atmosphere, climate and public health are not only the limited availability of measurement data, but also the limited applicability and compatibility of model formalisms used for the analysis, interpretation, and description of aerosol and cloud interactions and transformation. In particular, the kinetics of heterogeneous reactions and multiphase processes (concentration, time, and temperature dependencies) are usually not well characterized and most experimental and modeling studies involve system- and method-specific rate equations and parameters, which are hard to compare and extrapolate.

Comprehensive investigations of atmospheric aerosol and cloud effects, however, need to include a consistent description of a wide range of components and processes: multiple condensed phases (solid/liquid, surface/bulk, homogeneous/heterogeneous, internal/external mixing); multiple chemical species (volatile/semi-volatile/non-volatile, reactive/non-reactive); multiple competing physical and chemical processes (particle

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formation/transformation, gas uptake/release, mass transport, phase transition, chemical reaction, reversible/irreversible).

For this purpose we have developed and presented a kinetic model framework with consistent and unambiguous terminology and universally applicable rate equations and parameters, which allow to describe mass transport and chemical reactions at the gas-particle interface and to link aerosol and cloud surface processes with gas phase and particle bulk processes. The key elements and essential aspects of the kinetic model framework can be summarized as follows:

- (a) simple and descriptive double-layer surface model (sorption layer and quasi-static layer, near-surface gas phase and particle bulk);
- (b) straightforward flux-based mass balance and rate equations;
- (c) clear separation of mass transport and chemical reaction;
- (d) well-defined rate parameters (uptake and accommodation coefficients, reaction probabilities, reaction rate coefficients and mass transport rate coefficients);
- (e) clear distinction between gas phase, gas-surface, and surface-bulk transport (gas phase diffusion correction, surface and bulk accommodation);
- (f) clear distinction between gas-surface, surface layer, and surface-bulk reactions (Langmuir-Hinshelwood and Eley-Rideal mechanisms);
- (g) mechanistic description of concentration and time dependencies for all relevant interaction processes and conditions;
- (h) flexible inclusion/omission of chemical species and physicochemical processes depending on the complexity of the investigated systems and applied models;
- (i) flexible convolution/deconvolution of species and processes depending on the experimental or theoretical possibilities and requirements for their separation;

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(j) full compatibility with traditional resistor model formulations.

Exemplary practical applications and model calculations illustrating the relevance of the above aspects will be presented in a companion paper (Ammann and Pöschl, 2005). We hope that the presented model framework will serve as a useful tool and common
5 basis for experimental and theoretical studies investigating and describing atmospheric aerosol and cloud surface chemistry and gas-particle interactions. In particular, it is meant to support

- (a) the planning and design of laboratory experiments for the elucidation and determination of rate parameters (mapping of most insightful experimental conditions; identification and characterization of relevant concentration and time dependencies);
10
- (b) the establishment, evaluation, and quality assurance of comprehensive and self-consistent collections of rate parameters (in analogy to existing evaluated data bases of gas phase reaction rate coefficients);
- 15 (c) the development of detailed master mechanisms for process models and the derivation of simplified but yet realistic parameterizations for atmospheric and climate models (in analogy to existing master mechanisms and condensed mechanisms of atmospheric gas phase chemistry).

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Appendix A: List of symbols

Symbol	Meaning	SI Unit
α_{X_i} (α_{b,X_i})	bulk accommodation coefficient of X_i	
β_F	gas phase diffusion correction factor based on Fuchs (1964)	
β_{FS}	gas phase diffusion correction factor based on Fuchs and Sutugin (1971)	
Y_{X_i}	uptake coefficient of X_i (normalized by gas kinetic flux of surface collisions)	
Y_{eff,X_i}	effective uptake coefficient of X_i (normalized by average gas kinetic flux)	
$Y_{GSRu,Xp,X_i}, Y_{GSRu,Xp,Y_j}$	gas-surface reaction probabilities for X_p colliding with	
Y_{sor,X_i}	sorption uptake coefficient of X_i	
Y_{gsr,X_i}	gas-surface reaction uptake coefficient of X_i	
r_{b,X_i}	resistor model conductance of particle bulk diffusion and reaction of X_i	
r_{g,X_i}	resistor model conductance of gas phase diffusion of X_i	
r_{s,X_i}	resistor model conductance of surface reaction of X_i	
r_{s,b,X_i}	resistor model conductance of surface-bulk transfer of X_i	
Δ_{X_i}	average distance from which X_i gas molecules have a straight trajectory to the particle surface	m
λ_{X_i}	Mean free path of X_i in the gas phase	m
θ_s	sorption layer surface coverage	
θ_{s,X_p}	fractional surface coverage by X_p (sorption layer)	
θ_{ss,Y_q}	fractional surface area of Y_q (quasi-static layer)	
σ_{s,X_p}	molecular cross section of X_p in the sorption layer	m ²
σ_{ss,Y_q}	molecular cross section of Y_q in the quasi-static layer	m ²
Φ_{Y_q}	fractional concentration of Y_j in the near-surface particle bulk (mole, mass, or volume fraction)	
τ_{d,X_i}	desorption lifetime of X_i	s
τ_{d,X_i,Y_p}	desorption lifetime of X_i on a surface composed of Y_p	s
τ_{d,X_i,Y_p,Y_q}	desorption lifetime of X_i on a surface composed of Y_p on a particle bulk composed of Y_q	s
τ_{s,b,X_i}	surface-bulk exchange lifetime	s
ω_{X_i}	Mean thermal velocity of X_i in the gas phase	m s ⁻¹
C_{GSRu,g,X_i}	stoichiometric reaction coefficient of gas phase X_i in the gas-surface reaction GSRu	
$C_{GSRu,s,X_i}, C_{GSRu,ss,Y_j}$	stoichiometric reaction coefficients of surface X_i and Y_j in the gas-surface reaction GSRu	
$C_{SLRv,s,X_i}, C_{SLRv,ss,Y_j}$	stoichiometric reaction coefficients of surface X_i and Y_j in surface layer reaction SLRv	
C_{SBRw,ss,Y_j}	stoichiometric reaction coefficients of surface Y_j in surface-bulk reaction SBRw	
$C_{SBRw,b,X_i}, C_{SBRw,b,Y_j}$	stoichiometric reaction coefficients of bulk X_i and Y_j in surface-bulk reaction SBRw	
C_{b,rd,X_i}	reacto-diffusive geometry correction factor of X_i	
C_{g,X_i}	gas phase diffusion correction factor of X_i	
d_p	particle diameter	m
D_{b,X_i}	particle bulk diffusion coefficient of X_i	m ² s ⁻¹
D_{g,X_i}	gas phase diffusion coefficient of X_i	m ² s ⁻¹

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Symbol	Meaning	SI Unit
F_{g,X_i}	Flow of gas phase diffusion of X_i	s^{-1}
H_{cp,X_i}	Henry's law coefficient of X_i (concentration/pressure)	$mol\ m^{-3}\ Pa^{-1}$
H_{cc,X_i}	dimensionless Henry's law coefficient of X_i	
i_j, p, q, r, u, v, w	counting variables	
J_{ads,X_i}, J_{des,X_i}	flux of adsorption and desorption of X_i	$m^2\ s^{-1}$
J_{b,rd,X_i}	reacto-diffusive flux of X_i in the particle bulk	$m^2\ s^{-1}$
J_{b,s,X_i}, J_{s,b,X_i}	flux of bulk-surface and surface-bulk transfer of X_i (sorption layer)	$m^2\ s^{-1}$
$J_{b,ss,Y_j}, J_{ss,b,Y_j}$	flux of bulk-surface and surface-bulk transfer of Y_j (quasi-static layer)	$m^2\ s^{-1}$
$J_{b,ss,ex,Y_j}, J_{ss,b,ex,Y_j}$	flux of exchange bulk-to-surface and surface-to-bulk transfer of Y_j (quasi-static layer)	$m^2\ s^{-1}$
$J_{b,ss,rx,Y_j}, J_{ss,b,rx,Y_j}$	flux of reactive bulk-to-surface and surface-to-bulk transfer of Y_j (quasi-static layer)	$m^2\ s^{-1}$
J_{coll,X_i}	gas kinetic flux of X_i colliding with the surface	$m^2\ s^{-1}$
J_{coll,avg,X_i}	average gas kinetic flux of X_i	$m^2\ s^{-1}$
J_{net,X_i}	net flux of X_i from the gas phase to the condensed phase	$m^2\ s^{-1}$
J_{s,b,net,X_i}	net flux of surface-bulk transfer of X_i	$m^2\ s^{-1}$
k_{a,X_i}	first-order adsorption rate coefficient of X_i	$m\ s^{-1}$
$k_{a,0,X_i}$	first-order adsorption rate coefficient of X_i on an adsorbate-free surface	$m\ s^{-1}$
k_{b,X_i}	pseudo-first-order rate coefficient for chemical loss of X_i in the particle bulk	s^{-1}
k_{b,s,X_i}	first-order rate coefficient for bulk-to-surface transfer of X_i	$m\ s^{-1}$
k_{b,ss,Y_j}	first-order rate coefficient for bulk-to-surface transfer of Y_j	$m\ s^{-1}$
k_{b,ss,ex,Y_j}	first-order rate coefficient for bulk-to-surface transfer of Y_j by mutual exchange	$m\ s^{-1}$
k_{b,ss,rx,Y_j}	pseudo-first-order rate coefficient for bulk-to-surface transfer of Y_j by reactive transformation	$m\ s^{-1}$
k_{d,X_i}	first-order desorption rate coefficient of X_i	s^{-1}
k_{g,p,X_i}	pseudo-first-order rate coefficient for gas phase loss of X_i due to gas-particle interactions	s^{-1}
k_{s,X_i}	pseudo-first-order rate coefficient for chemical loss of X_i in the sorption layer	s^{-1}
k_{s,b,X_i}	first-order rate coefficient for surface-to-bulk transfer of X_i	s^{-1}
k_{s,b,net,X_i}	pseudo-first-order rate coefficient for net surface-to-bulk transfer of X_i	s^{-1}
$k_{s,g,X_i}, k_{s,s,X_i}, k_{s,ss,X_i}$	pseudo-first-order rate coefficients for chemical loss of X_i in the sorption layer by gas-surface reactions and surface layer reactions within the sorption layer or between sorption and quasi-static layer, respectively	s^{-1}
k_{ss,Y_j}	pseudo-first-order rate coefficient for chemical loss of Y_j in the quasi-static surface layer	s^{-1}
k_{ss,b,Y_j}	first-order rate coefficients for surface-bulk transfer of Y_j	s^{-1}
k_{ss,b,Y_j}	first-order rate coefficients for surface-bulk transfer of Y_j	s^{-1}
k_{ss,b,ex,Y_j}	first-order rate coefficients for surface-bulk transfer of Y_j by mutual exchange	s^{-1}

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Symbol	Meaning	SI Unit
k_{ss,b,rx,Y_j}	pseudo-first-order rate coefficients for surface-bulk transfer of Y_j by reactive transformation	s^{-1}
k_{ss,g,Y_j} , k_{ss,s,Y_j} , k_{ss,ss,Y_j}	pseudo-first-order rate coefficients for chemical loss of Y_j in the quasi-static layer by gas-surface reactions and surface layer reactions within the quasi-static layer or between sorption and quasi-static layer, respectively	s^{-1}
$k_{ss,rx}$	pseudo-first-order rate coefficient for reactive transformation of the quasi-static surface	s^{-1}
k_{SBRw,Y_p,Y_q} , k_{SBRw,Y_p,X_r}	second-order rate coefficients for surface-bulk reactions of Y_p with Y_q , and Y_p with X_r , respectively	$m^3 s^{-1}$
k_{SLRv,X_p} , k_{SLRv,Y_q}	first-order rate coefficients for surface layer reactions of X_p and Y_q , respectively	s^{-1}
k_{SLRv,X_p,X_q} , k_{SLRv,X_p,Y_q} , k_{SLRv,Y_p,Y_q}	second-order rate coefficients for surface layer reactions of X_p with X_q , X_p with Y_q , and Y_p with Y_q , respectively	$m^2 s^{-1}$
K_{ads,X_i}	Adsorption equilibrium constant of X_i	m^3
K'_{ads,X_i}	Effective adsorption equilibrium constant of X_i	m^3
K_{sol,cp,X_i}	solubility or gas-particle partitioning coefficient of X_i (concentration/pressure)	$mol m^{-3} Pa^{-1}$
K_{sol,cc,X_i}	dimensionless solubility or gas-particle partitioning coefficient of X_i	
Kn_{X_i}	Knudsen number for X_i	
l_{rd,X_i}	reacto-diffusive length for X_i in the particle bulk	m
M_{X_i}	molar mass of X_i	$kg mol^{-1}$
N_A	Avogadro constant	mol^{-1}
P_{b,ss,X_i} , L_{b,ss,X_i}	chemical production and loss of X_i in the near surface bulk by surface-bulk reactions	$m^{-2} s^{-1}$
P_{b,ss,Y_j} , L_{b,ss,Y_j}	chemical production and loss of Y_j in the near surface bulk by surface-bulk reactions	$m^{-2} s^{-1}$
P_{g,gsr,X_i} , L_{g,gsr,X_i}	chemical production and loss of gas phase X_i by gas-surface reactions	$m^{-2} s^{-1}$
P_{g,p,X_i} , L_{g,p,X_i}	Gas phase production and loss of X_i due to gas-particle interactions	$m^{-3} s^{-1}$
P_{s,X_i} , L_{s,X_i}	chemical production and loss of X_i in the sorption layer	$m^{-2} s^{-1}$
P_{s,g,X_i} , L_{s,g,X_i}	chemical production and loss of X_i in the sorption layer by gas-surface reactions	$m^{-2} s^{-1}$
P_{s,s,X_i} , L_{s,s,X_i} , P_{s,ss,X_i} , L_{s,ss,X_i}	chemical production and loss of X_i in the sorption layer by surface layer reactions (reaction partner in sorption or quasi-static layer, respectively)	$m^{-2} s^{-1}$

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Symbol	Meaning	SI Unit
$P_{ss,Yj}, L_{ss,Yj}$	chemical production and loss of Y_j in the quasi-static surface layer	$\text{m}^{-2} \text{s}^{-1}$
$P_{ss,b,Yj}, L_{ss,b,Yj}$	chemical production and loss of Y_j in the quasi-static surface layer by surface-bulk reactions	$\text{m}^{-2} \text{s}^{-1}$
$P_{ss,g,Yj}, L_{ss,g,Yj}$	chemical production and loss of Y_j in the quasi-static surface layer by gas-surface reactions	$\text{m}^{-2} \text{s}^{-1}$
$P_{ss,s,Yj}, L_{ss,s,Yj}, P_{ss,ss,Yj}, L_{ss,ss,Yj}$	chemical production and loss of Y_j in the quasi-static layer by surface layer reactions (reaction partner in sorption or quasi-static layer, respectively)	$\text{m}^{-2} \text{s}^{-1}$
$[\text{PS}]_g$	particle surface concentration	$\text{m}^2 \text{m}^{-3}$
R	gas constant	$\text{J K}^{-1} \text{mol}^{-1}$
r_p	particle radius	m
$S_{X_i}(\alpha_{s,X_i})$	surface accommodation coefficient of X_i	
$S_{0,X_i}(\alpha_{s,0,X_i})$	surface accommodation coefficient of X_i on an adsorbate-free surface	
$S_{0,X_i,Y_p}(\alpha_{s,0,X_i,Y_p})$	surface accommodation coefficient of X_i on an adsorbate-free surface composed of Y_p	
$S_{0,X_i,Y_p,Y_q}(\alpha_{s,0,X_i,Y_p,Y_q})$	surface accommodation coefficient of X_i on an adsorbate-free surface composed of Y_p on a particle bulk composed of Y_q	
$[\text{SS}]_{ss}$	sorption site surface concentration	m^{-2}
T	absolute temperature	K
$u_{\max}, v_{\max}, w_{\max}$	Total number of gas-surface, surface-layer, and surface-bulk reactions, respectively	
X_i	volatile molecular species	
$[X_i]_b$	particle bulk number concentration of X_i	m^{-3}
$[X_i]_{bs}$	Near-surface particle bulk number concentration of X_i	m^{-3}
$[X_i]_{b,\text{sat}}$	saturation particle bulk number concentration of X_i	m^{-3}
$[X_i]_g$	gas phase number concentration of X_i	m^{-3}
$[X_i]_{gs}$	Near-surface gas phase number concentration of X_i	m^{-3}
$[X_i]_{g,\text{sat}}$	saturation gas phase number concentration of X_i	m^{-3}
$[X_i]_s$	surface number concentration of X_i (sorption layer)	m^{-2}
$[X_i]_{s,\text{max}}$	maximum surface number concentration of X_i (sorption layer)	m^{-2}
Y_j	non-volatile molecular species	
$[Y_j]_{ss}$	surface number concentration of Y_j (quasi-static layer)	m^{-2}
$[Y_j]_b$	particle bulk number concentration of Y_j	m^{-2}
$[Y_j]_{bs}$	Near-surface particle bulk number concentration of Y_j	m^{-2}
Z_k	Semi-volatile molecular species	
$[Z_k]_s$	surface number concentration of Z_k (sorption layer)	m^{-2}
$[Z_k]_{ss}$	surface number concentration of Z_k (quasi-static layer)	m^{-2}

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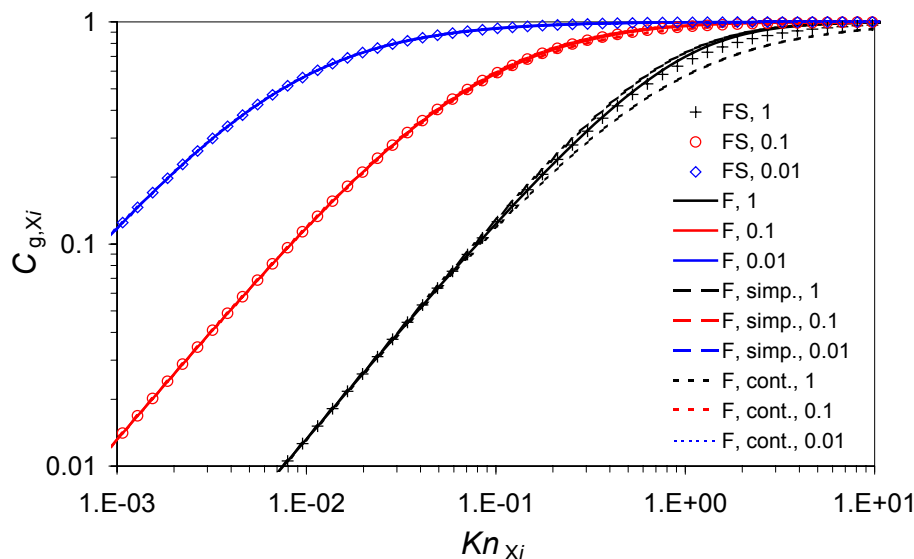


Fig. 1. Gas phase diffusion correction factor $C_{g,Xi}$ plotted against Knudsen number Kn_{Xi} for different uptake coefficients and transition regime flux matching approaches: $\gamma_{Xi}=1$ for black lines and symbols; $\gamma_{Xi}=0.1$ for red lines and symbols; $\gamma_{Xi}=0.01$ for blue lines and symbols; FS (symbols): Eq. (20) based on Fuchs and Sutugin (1971); F (solid lines): Eq. (14) based on Fuchs (1964); F, simp. (dashed lines): Eq. (14) with $\Delta_{Xi}=\lambda_{Xi}$; F, cont. (dotted lines): Eq. (20).

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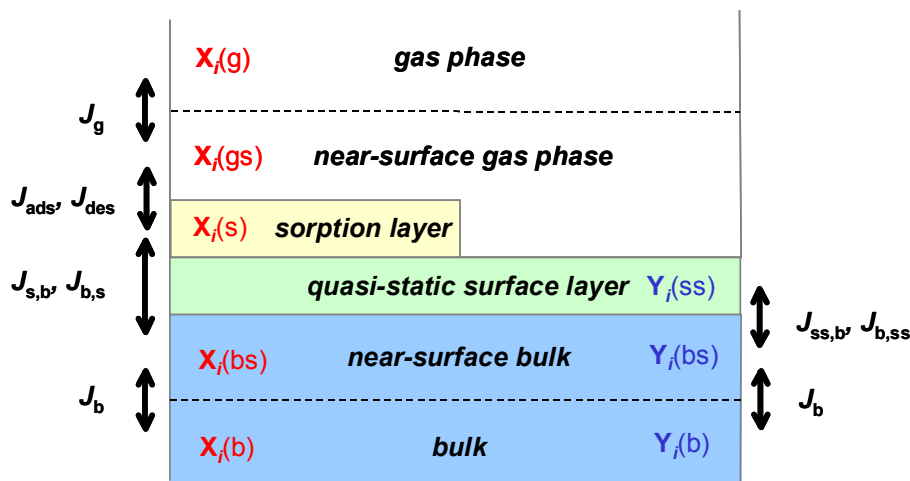


Fig. 2. Double-layer surface model compartments and transport fluxes for volatile species X_i (left) and non-volatile species Y_i (right).

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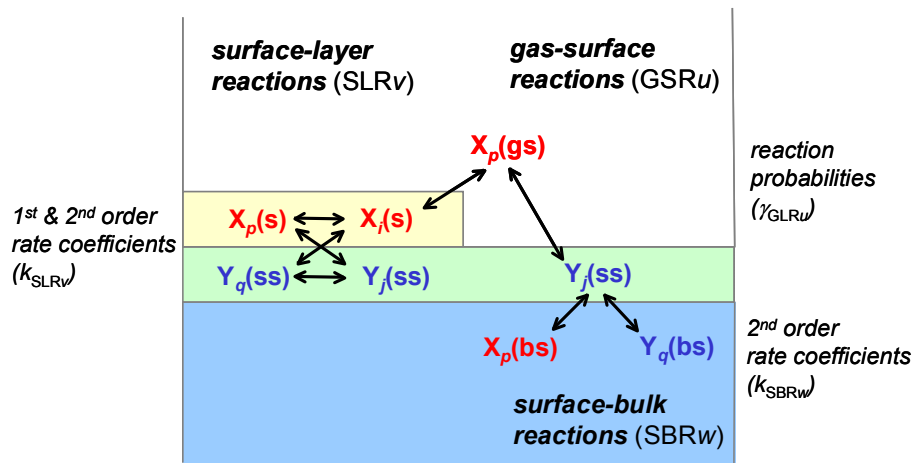


Fig. 3. Classification of chemical reactions between volatile and non-volatile species at the surface.

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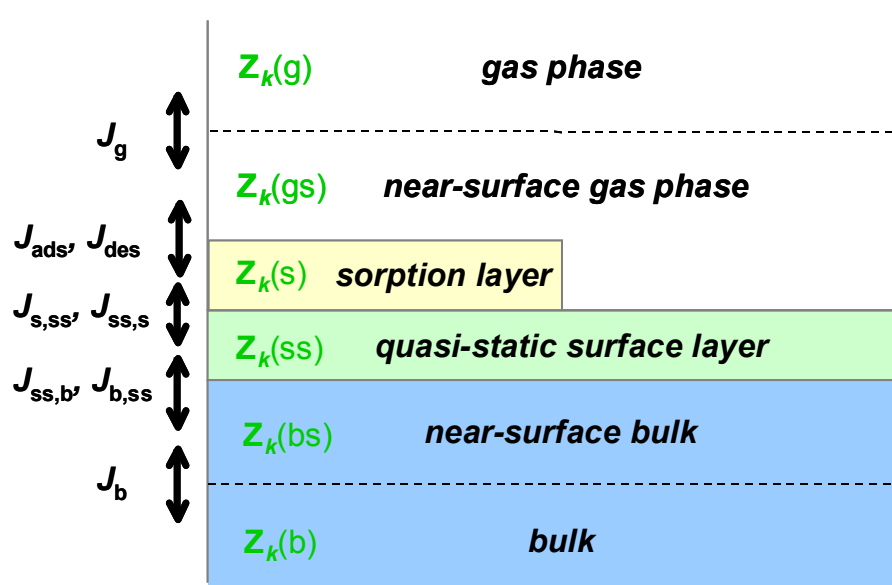


Fig. 4. Double-layer surface model compartments and transport fluxes for semi-volatile species Z_k .

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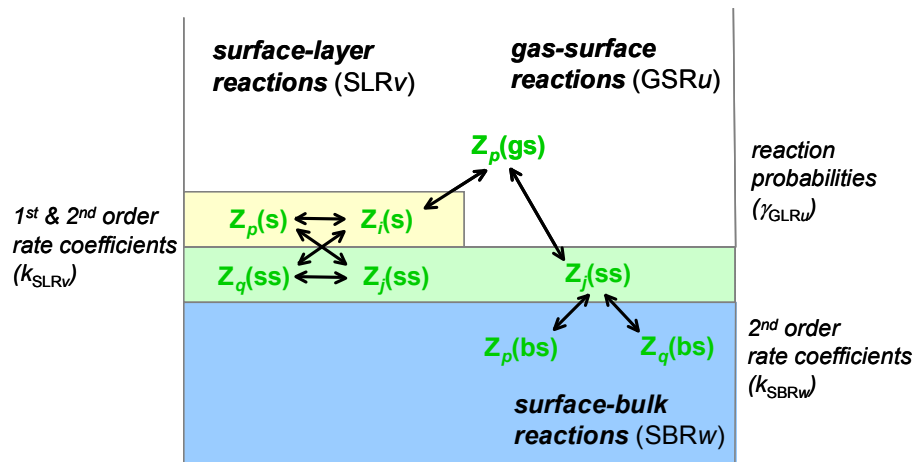


Fig. 5. Classification of chemical reactions between semi-volatile species at the surface.

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