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**Frequency-
dependent response
to extratropical wave
forcing**

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Analysis of the frequency-dependent response to wave forcing in the extratropics

A. J. Haklander^{1,2}, P. C. Siegmund², and H. M. Kelder^{1,2}

¹Eindhoven University of Technology (TUE), Department of Applied Physics, P.O. Box 513, 5600 MB Eindhoven, The Netherlands

²Royal Netherlands Meteorological Institute (KNMI), Climate Research and Seismology Department, Atmospheric Composition Division, P.O. Box 201, 3730 AE De Bilt, The Netherlands

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Correspondence to: A. J. Haklander (haklande@knmi.nl)

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Abstract

A quasigeostrophic model for the frequency-dependent response of the zonal-mean flow to planetary-wave forcing at Northern Hemisphere (NH) midlatitudes is applied to 4-D-Var ECMWF analysis data for six extended winter seasons. The theoretical response is a non-linear function of the frequency of the forcing, the thermal damping time α^{-1} , and a scaling parameter μ which includes the aspect ratio of the meridional to the vertical length scale of the response. Non-linear regression of the calculated response from the analyses onto the theoretical response yields height-dependent estimates for both α^{-1} and μ . The thermal damping time estimated from this dynamical model is about 2 days in the troposphere, 7–10 days in the stratosphere, and 2–4 days in the lower mesosphere. These estimates generally lie within the range of existing estimates, although the values we find for the troposphere are significantly smaller than those calculated in several radiative transfer modeling studies. At most levels, the estimates for μ are significantly lower than can be derived from scaling arguments that apply outside the forcing region. We illustrate with an example how the response of the meridional circulation inside the forcing area can have a higher aspect ratio than the effective response outside the forcing area.

1. Introduction

In NH midlatitude winter, planetary waves strongly interact with the zonal-mean flow. This interaction occurs at a broad range of timescales. For instance, the intense growth of a sudden stratospheric warming (SSW) event can occur in just a few days, its mature stage typically lasts a few weeks, and the total SSW cycle from preconditioning to recovery of the polar vortex can last a few months (e.g. Limpasuvan et al., 2004). Randel et al. (2002) found that the power spectrum of equatorial upwelling shows a broad maximum at periods between 10–40 days, and they argued that this is associated with episodes of planetary-wave activity at midlatitudes. The midlatitude zonal

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forcing by planetary waves also exhibits an annual cycle (e.g. Rosenlof, 1995). During winter, westerly stratospheric winds allow the vertical propagation of planetary waves emanating from the troposphere, whereas the summertime easterlies block the planetary waves. The angular momentum that is deposited by the waves is distributed between the relative and planetary reservoirs of angular momentum (e.g. Peixoto and Oort, 1992). This is expressed by the quasigeostrophic transformed Eulerian mean (TEM) zonal momentum equation,

$$\frac{\partial \bar{u}}{\partial t} - f \bar{v}^* = \bar{M}, \quad (1)$$

where the overbars denote zonal averages, \bar{u} is the zonal-mean zonal wind, f is the Coriolis parameter, \bar{v}^* is the meridional component of the residual circulation, and \bar{M} is $a \cos \phi$ times the wave-induced angular momentum deposition per unit mass (e.g. Holton et al., 1995). The tendency of the relative angular momentum is described by $\partial \bar{u} / \partial t$, that of the planetary angular momentum by $-f \bar{v}^*$. Garcia (1987) derived an expression for the frequency dependence of the $\partial \bar{u} / \partial t$ response to a given zonal wave forcing \bar{M} . According to this expression, the wave-induced angular momentum deposition at high frequencies is distributed about equally between the relative and angular momentum reservoirs. It was found that, away from the high-frequency limit, the rates of frictional dissipation and thermal relaxation toward radiative equilibrium determine the frequency dependence of the response. The timescale of thermal damping is important, since for non-zero $\partial \bar{u} / \partial t$ it determines how efficiently the meridional circulation is able to restore thermal-wind equilibrium through the adiabatic adjustment of the meridional temperature gradient. In the low-frequency limit, which defines the Brewer-Dobson circulation, the thermal response to the wave forcing is fully damped by thermal relaxation, implying that the angular momentum of the waves is deposited into the planetary reservoir only. Although Garcia's model provides valuable insights into the frequency dependence of the balance in Eq. (1), it has not been tested with real atmospheric data. In this study, we apply this model to wind and temperature analyses from the ECMWF model. Since the stratospheric diabatic heating during summer is

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no longer slaved to the wave forcing, we base our analysis on NH winter (November to April) data only. For each of the three terms in Eq. (1), power spectra estimates are computed, using six winters of 12-hourly analysis data. Estimates for the vertical profiles of the thermal damping time and the high-frequency limit of the response are obtained, using a least-squares method to fit the theoretical frequency dependence of the response of $\partial \bar{u} / \partial t$ to \bar{M} onto the analyzed data.

2. Frequency-dependent TEM model

In the TEM model used by Garcia (1987), infrared cooling is parameterized by Newtonian cooling with thermal damping rate α , and gravity-wave drag is parameterized by Rayleigh friction with coefficient K_R . The forcing is assumed to be entirely due to the Eliassen-Palm (E-P) flux divergence of planetary waves, and thereby the forcing due to shortwave radiative heating is neglected. To study the frequency dependence of the zonal-mean flow response, a harmonic wave forcing at angular frequency ω is assumed, i.e., $\bar{M} = Re(\bar{M}_\omega e^{i\omega t})$. The zonal-mean zonal wind field can then be written as $\bar{u} = Re(\bar{u}_\omega e^{i\omega t})$. Garcia (1987) derived that the complex amplitude $i\omega \bar{u}_\omega$ of the zonal-mean zonal wind tendency Fourier component with angular frequency ω can be approximated as

$$i\omega \bar{u}_\omega \approx \mu \frac{(1 + \mu) + (\alpha/\omega)i}{(1 + \mu)^2 + (\alpha/\omega)^2} \bar{M}_\omega, \quad (2)$$

where μ is a real, non-dimensional scaling parameter defined as $\mu \equiv L_z^2 N^2 / (L_y f)^2$, which is typically $O(1)$ in the extra-tropics. N^2 denotes the square of the buoyancy frequency, and L_y and L_z denote the meridional and vertical scales of the response. Equation (2) is identical to the expression found by Garcia (1987, Eq. 14), but with K_R set to zero. Rayleigh friction introduces a non-physical momentum sink (e.g. Shepherd

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and Shaw, 2004), and it is difficult to argue that a linear drag such as Rayleigh friction is at all relevant in the stratosphere (Haynes, 2005). For these reasons, we have not adopted this parameterization in the present study. To compare the magnitudes of the Fourier components, we multiply both sides of Eq. (2) with their complex conjugate.

5 Subsequently taking the square root of both sides yields the response function r ,

$$\frac{|\partial \bar{u}_\omega / \partial t|}{|\bar{M}_\omega|} \sim r(\alpha, \mu, \omega), \text{ with } r(\alpha, \mu, \omega) \equiv \frac{\mu}{\sqrt{(1 + \mu)^2 + (\alpha/\omega)^2}}. \quad (3)$$

In the high-frequency limit Eq. (3) converges to $(1 + \mu^{-1})^{-1}$, and in the stationary limit it converges to zero. Garcia (1987) set $\mu = 1$, but we allow μ to be a function of height.

3. Data and method

10 For this study, we have used 12-hourly operational ECMWF four-dimensional variational (4-D-Var) analysis data for six NH winters (November to April) from 1999/2000 to 2004/2005. The wind and temperature fields were retrieved for a latitude-longitude grid of $1^\circ \times 1^\circ$ at 35 pressure levels: 1000, 925, 850, 700, 500, 400, 300, 250, 200, 150, 100, 70, 66.6, 54.6, 44.3, 35.8, 28.9, 23.3, 18.8, 15.2, 12.3, 9.9, 8.0, 6.4, 5.2, 4.2, 3.4, 2.7, 2.1, 1.6, 1.2, 0.8, 0.5, 0.3, and 0.1 hPa.

15 From above the planetary boundary layer to the upper stratosphere, the mechanical acceleration term \bar{M} in Eq. (1) is principally due to planetary-wave forcing. In the TEM framework, this forcing is well approximated by the divergence of the E-P flux,

$$\bar{M} \approx \frac{1}{a \cos \phi} \left[\frac{1}{a \cos \phi} \frac{\partial (F^\phi \cos \phi)}{\partial \phi} + \frac{\partial F^p}{\partial p} \right], \quad (4)$$

20 where p denotes pressure, and F^ϕ and F^p denote the two components of the E-P flux vector F (e.g. Peixoto and Oort, 1992). We performed our analysis at 60° N, since

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planetary-wave forcing is known to reach a maximum there (Christiansen, 2001), which increases the validity of our assumption that \bar{M} is well-represented by Eq. (4).

For each of the six November to April seasons, we have calculated the Fourier transforms of $\partial\bar{u}/\partial t$, $f\bar{v}^*$, and \bar{M} separately. The six independent power spectra estimates were subsequently averaged at each frequency. By taking the square root of the ratio between the power estimates for $\partial\bar{u}/\partial t$ and \bar{M} , an estimate was obtained for the frequency-dependent response of $\partial\bar{u}/\partial t$ to the wave forcing \bar{M} . Subsequently, we performed a least-squares fit of the theoretical response function r , defined in Eq. (3), to the ratios from the analyzed data. With this spectral analysis, estimates for both α^{-1} and $(1+\mu^{-1})^{-1}$ were obtained at all 35 pressure levels. The goodness of fit is expressed by the fraction R^2 of the variance of the ratio that is accounted for by the least-squares regression.

4. Results

Figure 1 shows the power spectrum estimates for the middle stratosphere at 9.9 hPa. This example is qualitatively representative for the stratosphere, with generally decreasing power for the forcing term \bar{M} and the Coriolis term $f\bar{v}^*$ as the frequency increases. At timescales of 10–40 days, a broad maximum is found in the power spectra, which agrees with the sub-seasonal variability in the tropical upwelling that was found by Randel et al. (2002). At all frequencies, the estimate of $|\partial\bar{u}_\omega/\partial t|^2 = \omega^2 |\bar{u}_\omega|^2$ is clearly smaller than that of the forcing, roughly following the maxima and minima of the spectral power estimates for $f\bar{v}^*$ and \bar{M} , as expected from Eq. (3). The symbols in Fig. 2 show the (non-smoothed) frequency dependence of the estimated ratios $|\partial\bar{u}_\omega/\partial t| / |\bar{M}_\omega|$ at 0.1 hPa, 9.9 hPa, and 1000 hPa. At all three levels, the ratio increases with increasing frequency, as expected from Eq. (3). The theoretical least-squares fits are based on the ratios at 45 angular frequencies, from $2 \times (2\pi) \text{ yr}^{-1}$ to $90 \times (2\pi) \text{ yr}^{-1}$, with steps of $2 \times (2\pi) \text{ yr}^{-1}$. Higher frequencies are not included, since inconsistencies between subsequent analyses lead to non-physical variability at high

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frequencies. The dashed lines in Figs. 3a and b show the computed vertical profiles of, respectively, the thermal damping time α^{-1} and the high-frequency limit $(1+\mu^{-1})^{-1}$ of the response. The regression estimate of the thermal damping time is about 2 days in the troposphere (below 250 hPa), increasing to 7–10 days in the stratosphere and decreasing to 2–4 days in the lower mesosphere (above 1 hPa). The standard errors of these results are typically 4 days in the troposphere, 30 days in the stratosphere, and 10 days in the lower mesosphere. The standard errors become larger for longer thermal damping times, since the regression is then sensitive to the ratios at low frequencies, where the spectral resolution is relatively low. The sensitivity of R^2 (dotted line in Fig. 3b) to the thermal damping time estimate is clearly seen when comparing it with Fig. 3a. The solid lines in Figs. 3a and b show the profiles that only include points with $R^2 > 0.1$. The estimated stratospheric α^{-1} profile then becomes much smoother, whereas the $(1+\mu^{-1})^{-1}$ estimate is less sensitive. We first compare our estimates of α^{-1} from the frequency-dependent TEM model with those calculated by Newman and Rosenfield (Fig. 3, 1997; hereafter NR97), who used a radiative transfer model to derive thermal damping times as a function of latitude, height, and season. The damping times found in our study are generally shorter than their estimates for November to April at 60° N, but in the upper stratosphere, the agreement is quite good, especially considering the large stratospheric standard errors. In the lower stratosphere and troposphere however, our α^{-1} estimates are much smaller than those of NR97, who calculated wintertime damping times of 35–40 days at 100 hPa. Held and Suarez (1994) proposed a profile which for 60° N yields an α^{-1} of 26 days at 1000 hPa, linearly increasing to 40 days at 700 hPa and above. With our tropospheric α^{-1} estimates of about 2 days and a standard error of about 5 days, the differences can be called significant. Concerning tropospheric thermal damping times, little consensus exists in the literature. This was also acknowledged by Burde (1999), who stated that α^{-1} is typically set to be the order of several days in the troposphere. Prinn (1977) pointed out that, especially at low levels, thermal damping times will often be significantly overestimated if calculations do not include the effect of the conducting and radiating surface. Applying his analytical

expression for α^{-1} , tropospheric temperature perturbations with a vertical wavelength of about 3 km are thermally damped (mainly by water vapor) with α^{-1} as short as 0.7 to 2.0 days. Therefore, the tropospheric thermal damping times found in this study lie within the range of existing estimates.

5 The high-frequency limit of the response (Fig. 3b) is generally quite constant with height and has a standard error of approximately 0.2. In the stratosphere, at high frequencies, the ratio between $|\partial \bar{u}_\omega / \partial t|$ and $|\bar{M}_\omega|$ generally converges to 0.33–0.37. Alternatively, μ converges to 0.5–0.6, which is indeed $O(1)$ as stated by Garcia (1987). The $(1 + \mu^{-1})^{-1}$ profile has a remarkable maximum near 150 hPa. This suggests that
 10 in the lowermost stratosphere, the variability of $\partial \bar{u} / \partial t$ is less dominated by angular momentum deposition by planetary waves, and more by conservation of absolute angular momentum. Power spectrum estimates at 150 hPa (not shown) indicate that the variability of \bar{M} is indeed small compared to that of both $\partial \bar{u} / \partial t$ and $\bar{f} \bar{v}^*$. The rapid decrease of the $(1 + \mu^{-1})^{-1}$ estimate at the lowest levels is explained by the damping
 15 effect of surface drag on $|\partial \bar{u}_\omega / \partial t|$, which is not included in our calculation of \bar{M} .

5. Discussion and conclusions

In this paper, we have applied the frequency-dependent TEM model of Garcia (1987) to wind and temperature analyses from the ECMWF model. Six November–April seasons of 4-D-Var analysis data at 35 levels were used to derive power spectra for the planetary-wave forcing (E-P flux divergence), the zonal-mean zonal wind tendency, and the Coriolis acceleration associated with the residual meridional wind. We have
 20 used 4-D-Var data, since 3-D-Var analyses are known to yield a less realistic age of air in the stratosphere, which is mainly determined by the strength of the wave forcing (e.g. Scheele et al., 2005). We find that the theoretical response curve fits reasonably well onto the response derived from ECMWF analyses, with best agreement in the troposphere as well as in the upper stratosphere and lower mesosphere. Based
 25 on the least-squares fits, estimates were obtained for the vertical profile of the thermal

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damping time and the high-frequency limit of the response.

In this study, the scaling parameter μ is assumed to be a function of height only. However, Holton et al. (1995) argued from a scaling analysis of the vertical mass flux equation, that μ should have a particular frequency dependence, to allow for a non-zero vertical mass flux outside the forcing area. Based on their arguments, we obtain

$\mu \approx \sqrt{1 + \alpha^2 / \omega^2} \max [1, L_z / H]$, where $H \approx 7$ km is the mean scale height. This yields an aspect ratio of $L_y / L_z \leq N / f$ for all frequencies, whereas we find an aspect ratio that is in general about 35% larger than N / f . Only in the lower stratosphere, where the forcing $|\hat{M}_\omega|$ is relatively weak, we find $L_y / L_z \leq N / f$. Our results therefore suggest that the aspect ratio scaling argument of Holton et al. (1995) is not applicable well inside the forcing region. For instance, the net meridional response may actually consist of multiple shallow meridional cells. This would yield a larger aspect ratio inside the forcing region, and a lower “effective” aspect ratio outside the forcing area, which still satisfies the condition $(L_y / L_z)_{\text{eff}} \leq N / f$. Furthermore, substituting μ in Eq. (2) leads to non-physical behavior at low frequencies, since the stationary limit $\omega \rightarrow 0$ yields a non-zero response between $\frac{1}{2}\sqrt{2}$ and 1. Therefore, we have not applied these scaling arguments to μ , although we have allowed it to vary with height instead of assuming a constant aspect ratio of N / f , as was assumed by Garcia (1987).

Although the agreement between our estimates of the thermal damping time and those of NR97 is quite good at higher levels, we found significantly shorter thermal damping times in the lower stratosphere and troposphere. However, our results still lie within the broad range of tropospheric thermal damping times found in the literature. Garcia’s model for the frequency-dependent response of the zonal-mean flow to wave forcing is therefore found to be applicable to NH midlatitude wintertime conditions.

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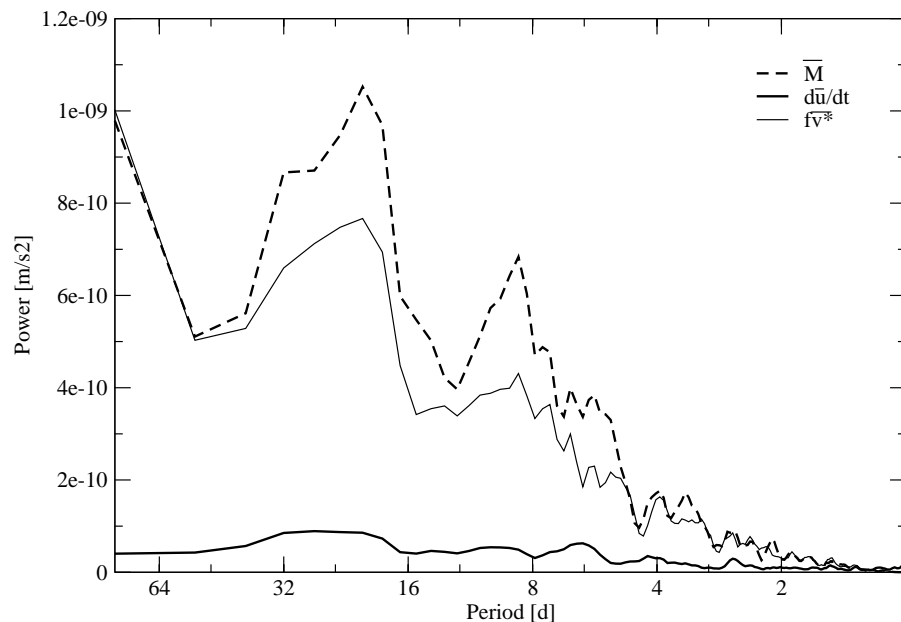


Fig. 1. Power spectrum estimates for the November–April season at 60° N for $\partial\bar{u}/\partial t$ (thick solid line), $f\bar{v}^*$ (thin solid line), and \bar{M} (dashed line) at the 9.9 hPa level. The spectral estimates have been smoothed using five-point averages.

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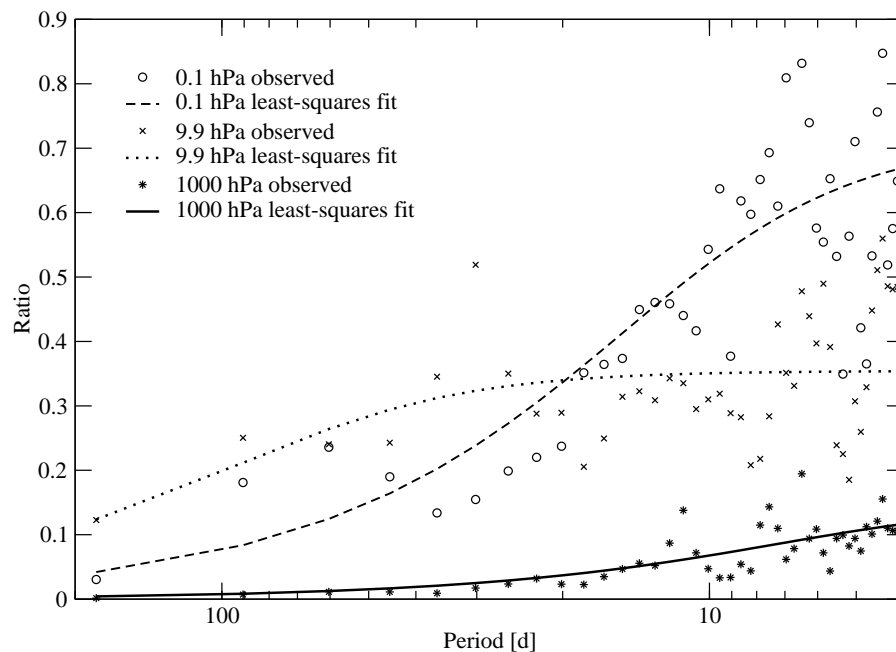


Fig. 2. Estimates (symbols) for the Nov-Apr season at 60° N for the ratio $|\partial \bar{u}_\omega / \partial t| / |\bar{M}_\omega|$ at 0.1 hPa, 9.9 hPa, and 1000 hPa. Each line represents the least-squares fit of the theoretical response function to the observed ratios.

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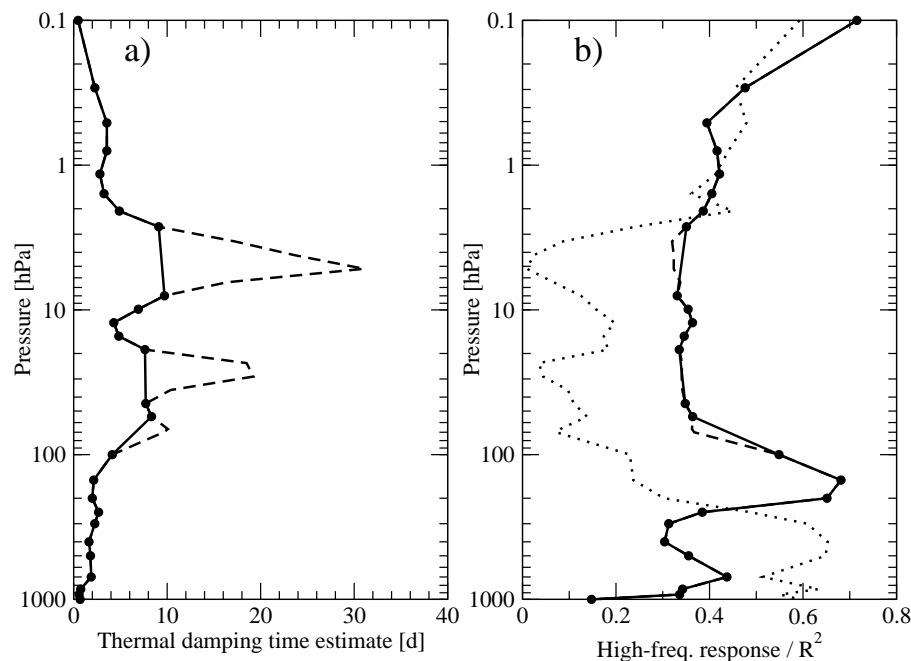


Fig. 3. Estimates for the November–April season at 60°N for **(a)** the thermal damping time α^{-1} and **(b)** the high-frequency limit of the response $(1+\mu^{-1})^{-1}$, as a function of pressure. The dashed lines show the estimates at all levels, the solid lines only show the estimates at the levels where R^2 , the fraction of the variance of $|\partial \bar{u}_\omega / \partial t| / |\bar{M}_\omega|$ that is accounted for by the least-squares regression, exceeds 10%. The dotted line in (b) shows R^2 for the least-squares theoretical fit.

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