

Constraining tropospheric mixing timescales using airborne observations and numerical models

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Schlager

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Constraining tropospheric mixing timescales using airborne observations and numerical models

P. Good¹, C. Giannakopoulos¹, F. M. O'Connor², S. R. Arnold³, M. de Reus⁴, and H. Schlager⁵

¹National Observatory of Athens, Greece

²Centre for Atmospheric Science, Cambridge, UK

³School of the Environment, University of Leeds, UK

⁴Max-Planck-Institute for Chemistry, Atmospheric Chemistry Department, Mainz, Germany ⁵German Aerospace Center, Institute of Atmospheric Physics, Oberpfaffenhofen, Germany

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Correspondence to: P. Good (pgood@meteo.noa.gr)

Abstract

A technique is demonstrated for estimating atmospheric mixing time-scales from in-situ data, using a Lagrangian model initialised from an Eulerian chemical transport model (CTM). This method is applied to airborne tropospheric CO observations taken during seven flights of the Mediterranean Intensive Oxidant Study (MINOS) campaign, of August 2001. The time-scales derived, correspond to mixing applied at the spatial scale of the CTM grid. Specifically, they are upper bound estimates of the mix-down lifetime that should be imposed for a Lagrangian model to reproduce the observed small-scale tracer structure. They are relevant to the family of hybrid Lagrangian-Eulerian models, which impose Eulerian grid mixing to an underlying Lagrangian model. The method uses the fact that in Lagrangian tracer transport modelling, the mixing spatial and temporal scales are decoupled: the spatial scale is determined by the resolution of the initial tracer field, and the time scale by the trajectory length. The chaotic nature of lower-atmospheric advection results in the continuous generation of smaller spatial

- scales, a process terminated in the real atmosphere by mixing. Thus, a mix-down lifetime can be estimated by varying trajectory length so that the model reproduces the observed amount of small-scale tracer structure. Selecting a trajectory length is equivalent to choosing a mixing timescale. For the cases studied, the results are very insensitive to CO photochemical change calculated along the trajectories. The method
- is most appropriate for relatively homogeneous regions, i.e. it is not too important to account for changes in aircraft altitude or the positioning of stratospheric intrusions, so that small scale structure is easily distinguished. The chosen flights showed a range of mix-down time upper limits: 1 and 3 days for 8 August and 3 August, due to recent convective and boundary layer mixing respectively, and 7–9 days for 16, 17, 22a, 22c
- and 24 August. For the flight of 3 August, the observed concentrations result from a complex set of transport histories, and the models are used to interpret the observed structure, while illustrating where more caution is required with this method of estimating mix-down lifetimes.

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1. Introduction

Mixing has been identified many times as having significant influence on constituent evolution both in the stratosphere and troposphere, and some progress has been made in characterising its effects (e.g. Plumb and Ko, 1992; Plumb et al., 2000; Pierce et al.,

- ⁵ 1994; Haynes and Shuckburgh, 2000a,b; Tan et al., 1998; Wild et al., 1996; Methven et al., 2003; Lee et al., 2001; Morgenstern and Carver, 1999). Observation of long range tropospheric pollution transport has given some idea of for how long features can retain their identity in the troposphere. On the other hand many studies using Lagrangian trajectory models, which do not explicitly simulate mixing as a process, have shown success in reproducing observed high resolution structure when forced has a process.
- by analysed meteorology (e.g. Sutton et al., 1994; O'Neill et al., 1994; Plumb et al., 1994; Manney et al., 1995; Dragani et al., 2002; Methven and Hoskins, 1999; Methven et al., 2001; Evans et al., 2000), although Lagrangian transport does not always improve simulated small-scale structure (e.g. Fairlie et al., 1997; Dragani et al., 2002).
- ¹⁵ Dragani et al. (2002) in particular found that reverse domain filling trajectories showed significant improvement, over the use of analysed PV, in the simulation of in-situ stratospheric data, but only when there was small scale structure observed. They highlight the treatment of mixing as an area requiring further study.

A family of hybrid Lagrangian-Eulerian (e.g. Stevenson et al., 1998; Reithmeier and Sausen, 2002; Fairlie et al., 1999) and related (McKenna et al., 2002) models are emerging, which aim to use the advantages of the Lagrangian approach, but impose a form of Eulerian mixing between trajectories. The spatial scale of the mixing must be large enough to cover more than one trajectory. The imposed mixing time-scale is a free parameter in these models. Estimation of appropriate mixing time-scales is

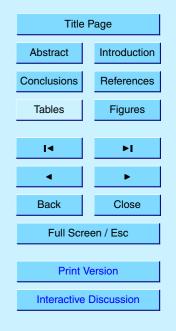
²⁵ difficult, because it depends on the unresolved small-scale tracer structure (see e.g. Nakamura, 1996, 2001). Some use shear-dependent parameterisations (Walton et al., 1988), but this has the disadvantage of enhancing mixing across wind jets such as the stratospheric vortex-dynamical features that are known to act as lateral transport

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barriers (e.g. Haynes and Shuckburgh, 2000a). Mostly, a mixing time-scale is chosen such that the model behaves reasonably. This work demonstrates one method for constraining mixing time-scales, using a Lagrangian model initialised from an Eulerian CTM to model in-situ CO observations taken over the eastern Mediterranean during
 the MINOS campaign of August 2001.

Lagrangian tracer-advection models are generally described as including no mixing processes. However in most applications tracer mixing is implicitly included through their initialisation from low resolution gridpoint fields. That is, when a Lagrangian calculation is initialised with low-resolution, spatially averaged tracer fields, a form of mixing is automatically included in the final product of the calculation. Typical initialisations

are PV from analysed winds (e.g. O'Neill et al., 1994), satellite data (e.g. Sutton et al., 1994) and chemical transport models (e.g. Methven et al., 2001). The mixing spatial scale is determined by the initialisation, in particular by the resolution of the gridpoint fields. The mixing time-scale corresponds to the trajectory length. Thus choosing a
 trajectory length is equivalent to selecting a mix-down lifetime (Thuburn and Tan, 1997, discuss mix-down lifetimes).

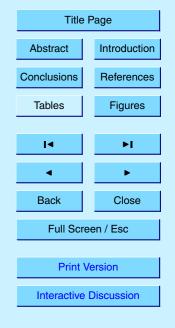
The approach suggested here is to choose a mix-down lifetime by comparing Lagrangian model results of varying trajectory durations with in-situ observations, for a long lived tracer. Since tracer advection continually produces smaller and smaller spa-

- tial scales, a trajectory duration, t_m , can be chosen such that the model reproduces the amount of small-scale structure in the observations. That is, for trajectories longer than t_m the model overestimates the small-scale structure, suggesting that t_m is the time-scale at which structure starts to lose its identity. The choice of t_m is made with most confidence if the region studied is relatively homogeneous, apart from the small-
- ²⁵ scale structure. That is, if neither accounting for changes in aircraft altitude, nor the positioning of stratospheric intrusions are too important, so that small scale structure is easily distinguished. Say the tracer initialisation is a reasonable low-resolution approximation to the real-atmosphere equivalent over the spatial scale d_m , where d_m is a vector defining the grid resolution of the tracer initialisation. In that case, t_m estimates

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the mix-down lifetime that should be imposed, over the spatial scale d_m , for a hybrid Lagrangian-Eulerian model to reproduce the amount of small-scale structure observed in the real atmosphere. If the advective dispersion of the trajectories is realistic, then the result is an estimate of mix-down lifetime in the real atmosphere.

Physical interpretation of the mix-down lifetime is restricted since the mechanism for mixing in the real atmosphere differs from that in the models described here. In the models, mixing is applied at the large scale, *d_m*, and is then stretched to small scale by Lagrangian advection. In the real atmosphere advection stretches large features, then mixing occurs at small scales. The numerical model approach of large scale mixing is dictated by computational limitations. However, it appears that this approach can be reasonable in some situations, since Lagrangian models initialised with coarse scale tracers have been used with success in reproducing observed small scale structure.

Carbon monoxide is used as the test tracer, because it has a relatively simple vertical profile, a long lifetime away from the continental boundary layer and is a common subject for model-measurement comparison. Ozone also has a relatively long lifetime in the upper troposphere, but the O₃ mixing ratio shows extremely large spatial curvature near the tropopause, which is difficult to model.

2. Model and measurements

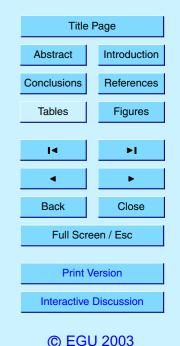
Carbon monoxide and ozone were measured aboard the German Aerospace Centre

- (DLR) Falcon aircraft, over the eastern Mediterranean during August 2001, as part of the MINOS campaign. CO was measured by Tunable Diode Laser Spectroscopy, with an accuracy of 2% and precision of 1.5% (Wienhold et al., 1998). O₃ was measured by UV-absorption spectroscopy, to an accuracy of 5% and precision of 2% (Schlager et al., 1997). This study uses measurements averaged over 15s intervals, which is about the period of a second to a sec
- ²⁵ 4 km in the horizontal, or equivalent to about 15 m in the vertical according to typical ratios of horizontal and vertical atmospheric scales (Haynes and Anglade, 1997). Lagrangian back trajectories, arriving at the Falcon flight tracks at one minute in-

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tervals, were calculated using the UK Universities Global Atmospheric Modelling program (UGAMP) offline trajectory model (Methven, 1997). The spacing of one minute corresponds to a horizontal resolution about one sixth of that of the meteological forcing. Methven and Hoskins (1999) showed that high-resolution advection can simulate

- ⁵ scales at least six times finer than the forcing resolution, when 6-hourly meteological analyses are used. Meteorological forcing was provided by T106 analyses from the European Centre for Medium Range Weather Forcasting (ECMWF). These trajectories were used as input to the Cambridge Tropospheric Trajectory model of Chemistry and Transport (CiTTyCAT) (Wild et al., 1996; Evans et al., 2000). CiTTyCAT models
- photochemical change following trajectories, with a detailed scheme for tropospheric photochemistry, including 90 chemical species and degradation of some hydrocarbons up to C-7, and parameterisations of surface deposition and boundary layer uptake of emissions. Mixing is included only implicitly in the initial tracer fields, and in a simple parameterisation for the vertical spread of surface emissions into the boundary layer.
- ¹⁵ Detail on the use of CiTTyCAT with the UGAMP trajectory model to simulate airborne observations is given by Methven et al. (2001).

Chemical initialisation for CiTTyCAT was provided by the TOMCAT 3d CTM, described by Law et al. (1998). The TOMCAT version used had a spatial grid corresponding to the T42 Gaussian grid in the horizontal, and 31 levels in the vertical. This

- is approximately 2.8° in the horizontal, and vertically 40 hPa in the mid-troposphere and 25 hPa near the tropopause. TOMCAT performs transport using the Prather second-order moments advection scheme (Prather, 1986), and includes a detailed tropospheric photochemistry scheme and parameterisations of boundary layer, convection and lightning processes. Tracer mixing ratios were interpolated to CiTTyCAT
- trajectory start points by linear spatial interpolation. Forcing is provided by 6-hourly 60-level ECMWF analyses, as for CiTTyCAT, except that for TOMCAT the analyses are truncated spectrally to T42, since there is no benefit in using forcing of resolution higher than that of the CTM. Vertical interpolation of the forcing to the model grid is performed in spectral space.

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3. Evaluation of TOMCAT CO fields

Comparisons between TOMCAT and observed CO for each MINOS flight are shown in Fig. 1. TOMCAT CO was interpolated linearly in space, at the model timestep closest to each observation point. TOMCAT results are coloured red for pressures greater than 700 hPa – in or near the PBL, and green otherwise. The relevant feature of the comparison is that, for pressures less than about 700 hPa, where TOMCAT CO shows a gradient, it will almost always have the correct sign and underestimate the magnitude of the observed gradient. The 700 hPa limit is required mostly due to errors in the model's planetary boundary layer (PBL) height and/or due to some overestimation of the PBL CO concentrations. Exceptions are for 1 August, the dip of 20 ppbv at about 10.6 UT (note times are given as decimal hours); and for 3 August, the slope from 8.10– 8.75 UT. The latter can be associated with numerical mixing of a stratospheric intrusion (the flight of 3 August is discussed further below). Some but not all of the gradient

- underestimation would be removed if TOMCAT was compared with real atmosphere CO mass averaged over the TOMCAT grid scale, rather than with in-situ flight data. Such a large-scale average is difficult to produce from the available data. The method described above estimates mix-down lifetimes using the structure generated when a trajectory model advects TOMCAT tracer fields. If the TOMCAT tracer gradients are too low, then CiTTyCAT will require longer trajectories, to generate structure of magnitude
- ²⁰ comparable to that observed, than if TOMCAT gradients were accurate. This leads to an over-estimation of mix-down lifetime. The conclusion is that for the purposes of this method, TOMCAT initialisation is useful, above the model PBL, for obtaining upper bound estimates of mix-down lifetimes.

Note that when TOMCAT CO gradients are referred to here, no mention is made of the spatial scale relevant to these gradients. This is because chaotic advection maintains a characteristic relationship between the energy in features of different scales of long lived tracers, above the dissipation scale (see e.g. Nakamura, 2001, and references therein). Also, a characteristic ratio is maintained between vertical and hor-

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izontal gradients (Haynes and Anglade, 1997). However, the smallest spatial scales generated by CiTTyCAT will result from stirring of features of the scale of a TOMCAT grid box, so when convection is not important, we are interested in the mix-down from the scale of the TOMCAT grid to the real atmosphere dissipation scale(s).

The approach below only tests the amount of structure in CiTTyCAT results, making no attempt to match specific features in model and data. This means that the assumptions about the CO initialisation (from TOMCAT) only concern the statistical distribution of gradient magnitudes. That is, neither the precise positioning of features nor the sign of gradients are important.

10 4. Results

4.1. Flight of 8 August 2001

Flight pressure, and ozone from measurements and TOMCAT model for 8 August are plotted in Fig. 2; similar plots for CO are earlier in Fig. 1. The ozone data in particular is quite homogeneous for two hours of the flight, from 11.5–13.5 UT. It is unusual for observed ozone to be so homogeneous over such a large region, so this suggests the possibility of relatively recent mixing. TOMCAT CO (Fig. 1) shows some structure in this region of a similar magnitude to the observations. In the data, relatively low values of O₃ (45–60 ppbv) and NO_y (0.5 ppbv, not shown) may be signatures of clean air mixed up from below. The CO is not low (100 ppbv), but the flight was planned to intercept air rich in biomass-sourced CO from monsoon regions; also, this is the only flight where observed CO is lower than in TOMCAT at these altitudes (Fig. 1). Either side, at lower altitudes (400-600 hPa), peaks in O₃ (Fig. 2) and NO_y (not shown) and a dip in CO (Fig. 1) show good evidence of a stratospheric intrusion, captured and positioned very well by the TOMCAT model.

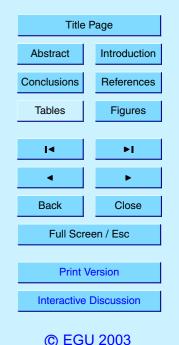
²⁵ Observed and CiTTyCAT model CO for 8 August are shown in Fig. 3. Initially, the measurements were available at 15 s intervals and CiTTyCAT results at one minute

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intervals. In order to intercompare structure fairly, the measurements and CiTTyCAT model results were sampled in two steps. First, the measurement frequency was reduced to that of the model, by selecting only those measurements nearest on the flight track to each model result. Second, in regions where measurements are missing, the

- ⁵ coinciding model results were discarded. Note that these plots also focus on only part of the flight – the high altitude central region, which is relatively homogeneous and so a good region for estimating a single mixing time-scale. The same procedure was applied for the other flights investigated below. Model calculations are shown for trajectory calculations initialised from TOMCAT fields at 18 UT on 7 August, 8 August and in the term of the other flights investigated below.
- ¹⁰ 10 August, trajectory lengths of less than one, two and four days. Each curve is plotted on a separate axis so that structure is clear.

The CiTTyCAT results show that even back trajectories of less than one day result in over-estimation of the structure in the data. Two- and four-day back trajectory results emphasise this. This suggests a mixdown lifetime, relative to the TOMCAT grid spatial

scale, of less than one day. Over this timescale the back trajectories originate from central north Africa; earlier, the air was brought rapidly from the east. The short mixing timescale and observed tracer concentrations are indicative of recent convection over north Africa, mixing relatively clean air up from below.

4.2. Flight of 3 August

Data and calculations for 3 August are shown in Figs. 4 and 5. CiTTyCAT model results are shown for trajectory calculations initialised from TOMCAT fields at 18 UT on 1 August, 31 July and 29 July, trajectory lengths of around 1.5, 2.5 and 4.5 days.

4.2.1. Interpretation of observed features

This flight is a challenge to model, because it is a multi-level flight which includes a possible influence of asian biomass burning, a stratospheric intrusion, and very distinct but small-scale airmasses at low level. Indeed, this is the flight where TOMCAT has 3, 1213-1245, 2003

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the biggest differences from the data (Fig. 1). The CiTTyCAT trajectory model is able to help in interpretation.

The existence of a stratospheric intrusion seems clear: in the O₃, two main spikes at around 7.75 UT and 8.8 UT appear in both observations and TOMCAT (Fig. 4), colocated with dips in CO (Fig. 1). However, the less prominent structure at high altitude between these features is not reproduced. The 2.5 and 4.5-day CiTTyCAT runs (Fig. 5) reproduce rather detailed structure of the intrusion before 8 UT. The structure after 8.6 UT may be captured, albeit with some misplacement.

At lower altitudes, there are three observed O₃ peaks: at around 9UT, 9.4–9.6UT and 10.15–10.45UT (Fig. 4). The origin of the 9.5UT peak is discussed in detail. In the TOMCAT 3d CTM such a peak is reproduced with reduced magnitude (Fig. 4). The modelled feature corresponds to the very edge of a stratospheric intrusion. The CiTTyCAT Lagrangian model shows a much thinner ozone peak (not shown), due to pollutants uplifted from the top of the PBL. Differences between the models are prob-

- ably due to mixing in the TOMCAT 3d model broadening the intrusion, and to small differences in PBL height. Back trajectory calculations show the air passing over northern Turkey 1–2 days earlier; less than a day before that they pass in or near the PBL; 10 days before the flight they originate in the UTLS region. Observed CO between 9.4–9.6 UT is too high for a dominant stratospheric signature (Fig. 1), and elevated val-
- ²⁰ ues of shorter-lived hydrocarbons are also observed, suggesting that air of PBL origin was recently mixed in (Scheeren et al., 2003). On 1 August, around two days before the flight, considerable cloud-to-ground lightning activity over northern and western Turkey was detected by the sferics location system of the United Kingdom Meteorological Office (data is plotted by Wetterzentrale at http://www.wetterzentrale.de). This
- observation suggests convective mixing in the real atmosphere, uplifting PBL air. Trajectories arriving at the O₃ peak of 10.15–10.45 UT also pass over northern Turkey and so convective mixing is also implicated for this peak.

The low-altitude CO data also shows complicated structure (Fig. 1). There seem to be two CO populations: one of 110–120 ppbv (at around 09:10 and 10:00) and 140–

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160 ppbv (around 9.1 UT, 9.3 UT, 9.8 UT and after 10.5 UT). Back trajectories show the low-altitude air coming from the north, and earlier from northern Europe, remaining in the boundary layer. Very short CiTTyCAT integrations, initialised from the TOMCAT 3d CTM only 1.5 days earlier, improve the comparison, on average, with data (Fig. 5), sug-

- ⁵ gesting that TOMCAT was better away from the measurement site. For boundary layer air, the best comparison is obtained when CiTTyCAT is initialised with relatively "clean" air just north west of the European continent, suggesting that in this case CiTTyCAT does a better job of simulating the pick-up of pollution over Europe. For the data taken after 10.5 UT, the trajectories reside rather longer over northern Europe than those for
- ¹⁰ most of the other boundary layer observations, so the former show rather higher CO. This explanation may also apply to the other observed CO peaks over 140 ppbv, but the flight intercepts them too briefly for certainty. However, there is some hint that these peaks are reproduced, if slightly misplaced, at least in the 2.5-day integration.

4.2.2. Mixing timescales

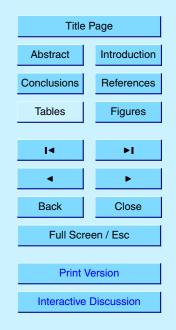
- Estimation of mix-down lifetime is done with caution here. The high altitude part of the flight before about 8.9 UT is not considered, because small misplacements of the stratospheric intrusion could cause problems. For the rest, some confidence is given by the fact that CiTTyCAT captures the main properties and even some fine structure of the data for runs of 2.5 and 4.5 days (Fig. 5), suggesting that their TOMCAT initialisation is reasonable, despite the fact that TOMCAT performs less well than usual at the actual
- measurement points. For the 2.5-day run, structure is seen that is not just large in amplitude, but also small in spatial scale compared to that in the data. An upper bound mixing lifetime of 2.5 days is chosen. This short time-scale is consistent with the evidence for recent mixing, either in the boundary layer or convection above. Note that
- this result is insensitive to photochemical evolution and surface exchange calculated along the trajectories.

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4.3. Flights of 16, 17, 22a, 22c and 24 August

5

Data and calculations for 17 August are shown in Figs. 6 and 7. Model results are shown for trajectory calculations initialised from TOMCAT fields at 18 UT on 12, 10, 9 and 7 August, trajectory lengths of around 5, 7, 9 and 11 days respectively. The 11-day trajectories originate from a broad region over the North Atlantic and North America, mostly between 100–600 hPa.

For this flight, we examine only the part of the flight for pressures lower than 700 hPa, between about 11.25 UT and 14 UT (Sect. 3). The situation is much simpler than for 3 August, and TOMCAT is able to capture the basic features of O_3 (Fig. 6) and the large scale gradient of CO (Fig. 1) quite well, albeit with an offset.

The back trajectory runs (Fig. 7) show very similar mean values to TOMCAT, with the same large-scale gradient – a consistency that gives some confidence. The relatively simple flight plan and observed air masses give a long time-series with plenty of small-scale structure to allow a reasonable mix-down lifetime estimate. Here, 5-day back

- ¹⁵ trajectories are required to get even close to the amount of structure observed. The 7-day run is better in this sense, with possibly a small overestimate, while the 11-day run clearly has too much fine-scale structure. As an indication of sensitivity, for these runs a 2 day difference in trajectory length is not very significant for the amount of structure generated, whereas a 4 day difference is significant. Hence, while the 7-day
- ²⁰ run seems reasonable, 9 days is chosen as a safer upper limit estimate of mix-down lifetime for the flight of 17 August. This longer lifetime is consistent with the trajectories remaining above the PBL, and there is no evidence of recent convection. Calculated photochemical change has no effect on the results, as is the case for all the flights studied in this work.
- Observations and CiTTyCAT model results for 16 August, the first and third flights of 22 August, and the flight of 24 August, are shown in Figs. 8, 9, 10 and 11. These are the remaining MINOS flights which featured measurements almost exclusively well above the PBL, and so are appropriate subjects for the above method. They all measured

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mid-upper tropospheric and some lower stratospheric air transported from the north Atlantic and northern America, in common with the flight of 17 August. Following the approach described above, mix-down lifetime upperbounds were chosen as follows: 9 days, 7 days, 9 days and 7 days for the flights of 16, 22a, 22c and 24 August,

respectively. Note that Fischer et al. (2002) found signatures of recent deep convection for short segments of flight c of 22 August, by looking at observed concentrations of multiple trace species. However, the flight segments for which they identify convective influence are of about 8, 3 and 2 min duration, which is much too short to be detected by the above method of estimating mixing timescales.

10 4.3.1. Tolerence with respect to initialisation errors

15

The above results are reliant on the CO initialisation, provided by the TOMCAT 3d CTM. The assumption is that TOMCAT CO spatial gradients underestimated the real atmosphere (see Sect. 3). Here, we test how much this assumption can be relaxed if a slightly less strong, general result is presented for the five similar flights (16, 17, 22a, 22c and 24 August). The question addressed is, if an upper bound of 11 days is proposed for these flights, what errors would TOMCAT CO have to to have for this result to be incorrect?

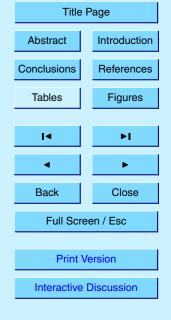
This was quantified using the data and 11-day model results as plotted in Figs. 7–11, ie. after the datasets had been sub-sampled as described above (Sect. 4.1). Each timeseries was de-trended, by applying a five minute boxcar average, and then subtracting the smoothed dataset from the original. The resulting residual distributions of data and 11-day model describe the small-scale structure – those features which grow strongly for longer model trajectories. For CiTTyCAT, the amplitude of this smallscale structure depends on the spatial gradients in the initialisation, since small-scale features are produced by stirring large-scale gradients.

The residual distributions for the measurements were then scaled by factors between one and six. The scale factor α which produced the best match between modelled and (scaled) measured residuals was found for each flight. If we propose that 11 days is

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the correct mix-down lifetime, and that the initialisation (taken from TOMCAT) is the only source of error, then α is the factor by which TOMCAT CO gradients would have to over-estimate those in the real atmosphere.

Comparison was done using the Kolmogorov-Smirnov (KS) numerical test (see applications by Fairlie et al., 1997; Dragani et al., 2002). Briefly, the KS test indicates whether two datasets come from the same statistical distribution. For the current application, this means that only the amount of structure is compared, so the timing of features along the flight-track has no effect on the result. Also, this test makes no assumption about the form of the statistical distribution. The KS test produces a P-value between 0 and 1, with higher numbers indicating a larger likelihood of a match between the distributions. Figure 12 plots these P-values for each flight as a function of the factor by which the measured residuals were scaled. This shows that scale factors

of at least two are required for the best match between modelled and scaled measured residuals. Hence, 11 days overestimates mix-down lifetime for these five flights, unless the spatial gradients in TOMCAT CO overestimate the real atmosphere by factors of at least two.

4.3.2. Discussion

Timescales of the order of a week or so are comparable to that of the observed cross-atlantic transport of Northern American boundary layer air reported by Stohl and Trickl
(1999). They are also consistent with evidence of ozone peaks, linked to stratospheric intrusions, surviving for more than 10 days (Bithell et al., 2000) in the troposphere. The tropopause ozone gradient is very large, and it is not clear how many e-folding lifetimes would be required for a particular stratospheric intrusion to lose its ozone signature. Note that the timescales reported in this work are for features to start to lose their identity, and not the time for a feature to vanish - in that sense they are something

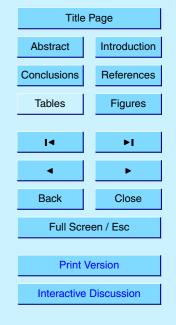
like an e-folding lifetime. The mixed Eulerian-Lagrangian models STOCHEM (Stevenson et al., 1998) and AT-TILA (Reithmeier and Sausen, 2002) are global 3d models. Their mixing timescales

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are chosen to achieve low numerical diffusivity rather than to accurately simulate smallscale structure. Numerical diffusivity is expected to vary as L^2/T , where *L* is the length scale of the mixing box, and *T* is the mixing lifetime. STOCHEM, has large mixing boxes to enable extremely long integrations and so needs a long mixing timescale – around 400 days. Note also that STOCHEM includes a convection scheme, which will

around 400 days. Note also that STOCHEM includes a convection scheme, which will introduce further tropospheric mixing. ATTILA, however, has mixing boxes comparable in size to those of this study, and uses a lifetime of 20 days in the troposphere.

5. Conclusions

A technique has been demonstrated for estimating mixing time-scales from in-situ data, using a Lagrangian model initialised from an Eulerian CTM. This method was applied to airborne CO observations taken during the MINOS campaign. The time-scales derived are applicable to the family of hybrid Lagrangian-Eulerian models, which perform Lagrangian advection and impose Eulerian mixing between trajectories. Such models have a mix-down lifetime as a free parameter, so it is important to find ways of estimating this parameter independently.

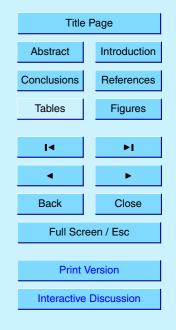
Lagrangian tracer-advection models are generally described as including no mixing processes, however in most applications tracer mixing is implicitly included through their initialisation from low resolution gridpoint fields. The mixing spatial scale is determined by the initialisation, in particular by the resolution of the gridpoint fields. The mix-

- ing time-scale corresponds to the trajectory length. Thus choosing a trajectory length is equivalent to selecting a mix-down lifetime. This choice can be made by comparing Lagrangian model results with in-situ observations, for a long lived tracer. If the tracer initialisation is a reasonable low-resolution approximation to the real-atmosphere equivalent, then the result estimates the mix-down lifetime required for a hybrid Lagrangian-
- ²⁵ Eulerian model to reproduce the amount of small-scale structure observed in the real atmosphere. Further, if the advective dispersion of the trajectories is realistic, then the result is an estimate of mix-down lifetime in the real atmosphere.

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The method is most appropriate for relatively homogeneous regions, so that smallscale structure is easily distinguished. More confidence is given in the result when reasonably broad regions are examined, so that plenty of small-scale structure is generated in the model.

- ⁵ Physical interpretation of the mix-down lifetime is restricted since the mechanism for mixing in the real atmosphere differs from that in the models described here. In the models, mixing is applied at the large Eulerian grid scale and is then stretched to small scale by Lagrangian advection. In the real atmosphere advection stretches large features, then mixing occurs at small scales. The numerical model approach of large scale mixing is dictated by computational limitations. However, it appears that this approach can be reasonable in some situations, since Lagrangian models initialised
- with coarse scale tracers have been used with success in reproducing observed small scale structure.
- Carbon monoxide was chosen as the test tracer, because it has a long photochemi-¹⁵ cal lifetime and is a common subject for model-measurement comparison. Ozone also has a relatively long lifetime in the upper troposphere, but is unsuitable for the above estimates because the O₃ mixing ratio shows extremely large spatial curvature near the tropopause, which is difficult to model. An advantage of the method is that for the flights studied above, with CO as the test tracer the results are very insensitive to photochem-²⁰ ical change calculated along the trajectories. Thus, errors in model photochemistry are
- unlikely to affect the conclusions.

In the experiments described above, the TOMCAT 3-d CTM provided CO initialisation. The MINOS campaign featured flights of the DLR falcon aircraft. The variety of flight configurations allowed tests of the TOMCAT CO tracer gradients, which are un-

derestimates above the model planetary boundary layer. For this reason, the mix-down lifetimes derived above are treated as upper bound estimates only.

Seven flights were examined, with mix-down lifetime upper bounds of 1 day for 8 August, 2.5 days for 3 August and 7–9 days for the five flights of 16, 17, 22a, 22c and 24 August. Recent convective and boundary layer mixing are likely explanations of the

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short time-scales of the first two examples.

For the flight of 3 August, the observed air shows much complexity. It shows considerable structure due to a stratospheric intrusion, PBL air uplifted by convection and/or advection, and different PBL air histories. Here, the models are used more generally to interpret the data in support of MINOS, and illustrate where more caution is required

with the above method of estimating mix-down lifetimes.

For the five flights with similar mix-down lifetimes, of 7–9 days, the sensitivity to errors in the CO initialisation was tested. Numerical comparisons were made of the small-scale structure in the observations and in model results for 11 day trajectories.

- It was shown that the slightly weaker upper bound of 11 days overestimates mix-down lifetimes for these five flights unless the spatial gradients in TOMCAT CO are too large by factors of at least two. These lifetimes are consistent with observed long-range transport across the Atlantic. Existing mixed Lagrangian-Eulerian models use longer lifetimes in order to limit numerical diffusivity.
- Realistic and representative mixing time-scales are difficult to estimate. The approach presented above offers some possibility to assist characterizing atmospheric mixing times. Further development work will aim to further constrain the errors in initilisation, and to test the applicability of simple mixing with these timescales for the CiTTyCAT photochemical transport model. It may be necessary to use smaller mixing grid boxes, to limit numerical diffusivity. The timescales in this work can be scaled roughly according to the stretching timescale of 3.3 days reported by Methven et al. (1999) for trajectories over northern Europe. That is an e-fold reduction of mixing grid
- length-scale would be expected to require a reduction of the mix-down lifetime by about 3 days.
- 25 *Acknowledgements.* The authors would like to thank A. Badopoulou for support in the execution of this work.

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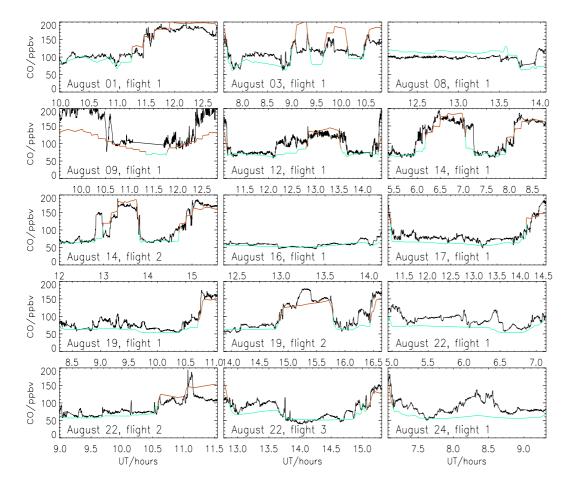


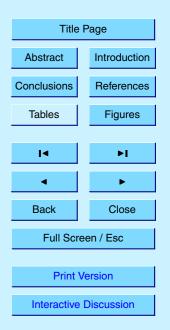
Fig. 1. Observed (black) and TOMCAT model (green and red) CO for each MINOS flight-track. TOMCAT results are coloured red for pressures greater than 700 hPa – in or near the PBL, and green otherwise (see text for explanation).

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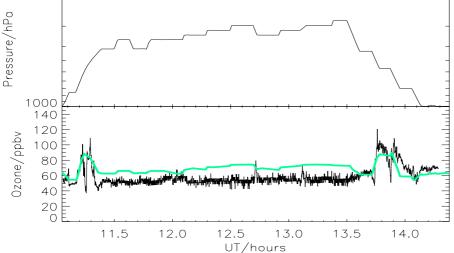
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Fig. 2. Flight-track pressure, and ozone from measurements and TOMCAT model for 8 August.

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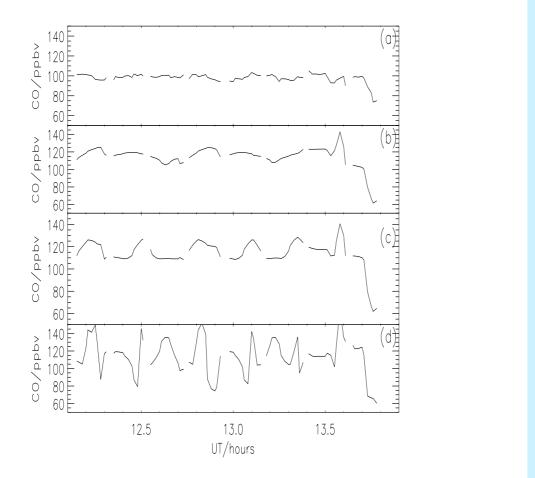
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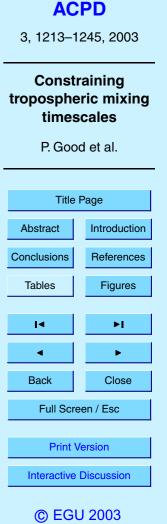


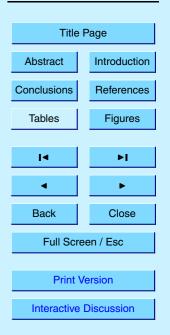
Fig. 3. CO from measurements **(a)** and CiTTyCAT model **(b–d)** for 8 August. Model and measurements are sampled at the same temporal frequency, for fair inter-comparison of structure (see text for details). Model results are shown for trajectory lengths of about 1 (b), 2 (c) and 4 (d) days.

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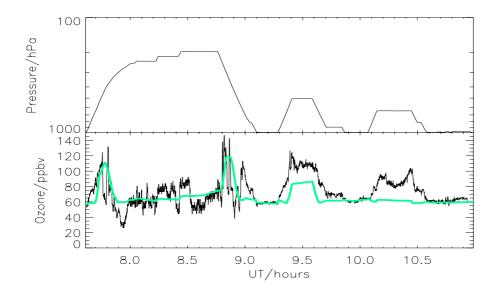
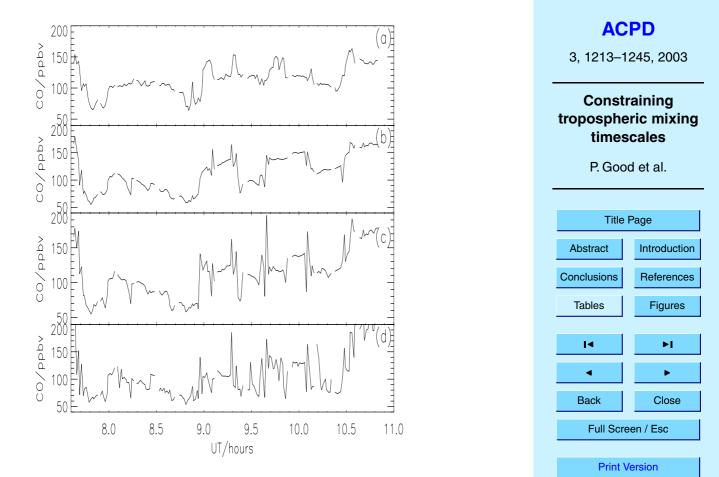
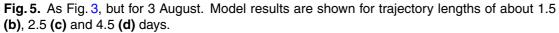


Fig. 4. As Fig. 2, but for 3 August.





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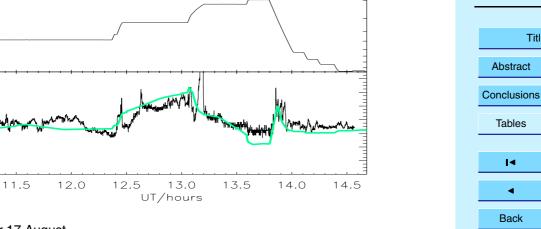


Fig. 6. As Fig. 2, but for 17 August.

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1000 140 120

> 100 80

Pressure/hPa

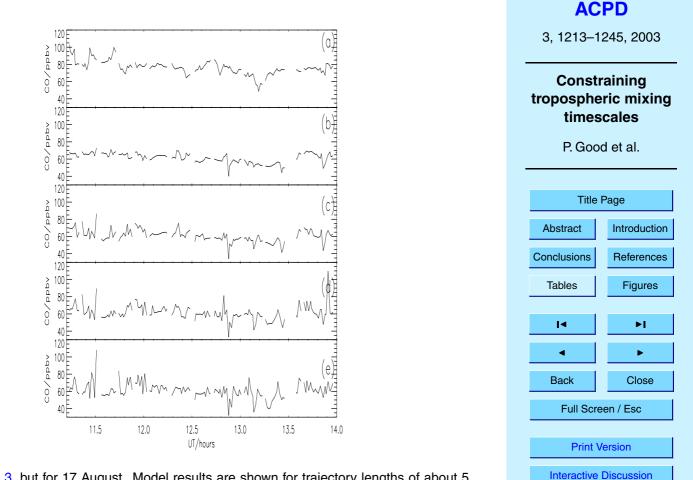
Ozone/ppbv

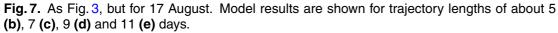
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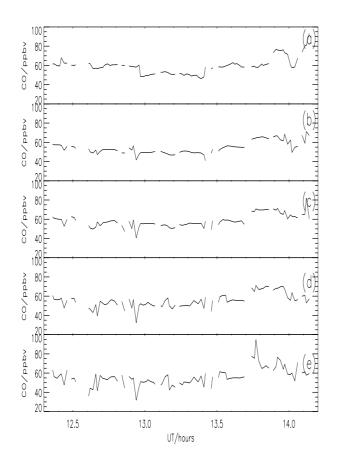
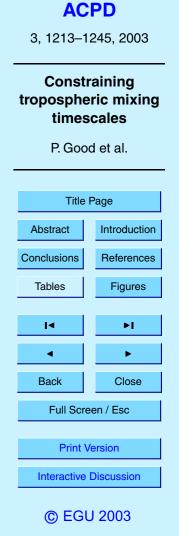
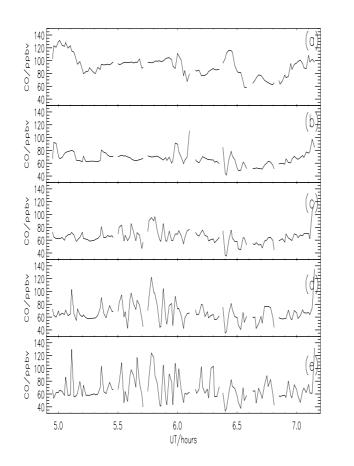
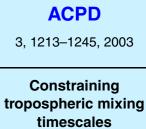


Fig. 8. As Fig. 7, but for 16 August.







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Fig. 9. As Fig. 7, but for 22a August.

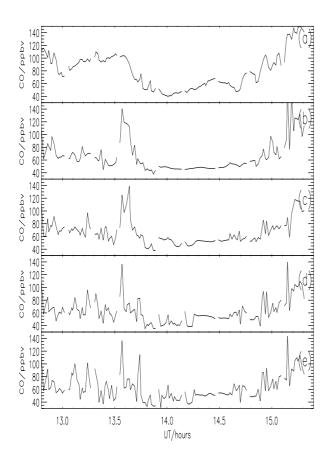
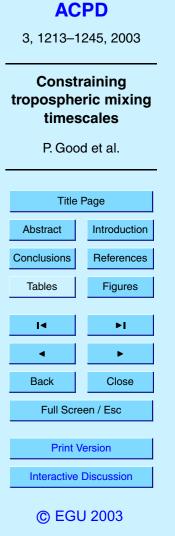


Fig. 10. As Fig. 7, but for 22c August.



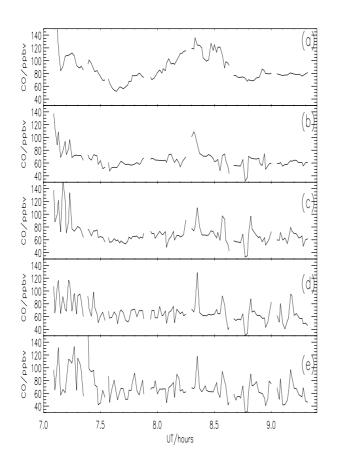
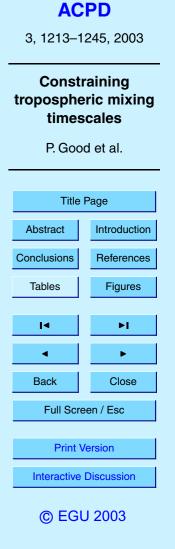


Fig. 11. As Fig. 7, but for 24 August.



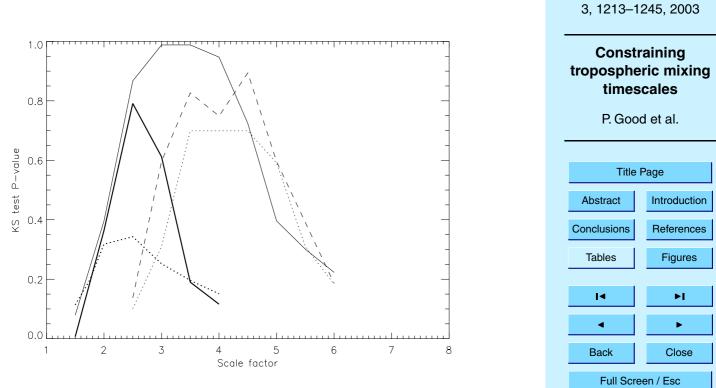


Fig. 12. KS test results comparing residual distributions for 11-day model results and scaled observations. The abscissa is the scaling factor applied to the observed residual distribution (see text for details).

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