



HAL
open science

Identification of the accretion rate for annually resolved archives

F. de Ridder, A. de Brauwere, R. Pintelon, J. Schoukens, F. Dehairs

► **To cite this version:**

F. de Ridder, A. de Brauwere, R. Pintelon, J. Schoukens, F. Dehairs. Identification of the accretion rate for annually resolved archives. *Biogeosciences Discussions*, 2006, 3 (2), pp.321-344. hal-00297794

HAL Id: hal-00297794

<https://hal.science/hal-00297794v1>

Submitted on 18 Jun 2008

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Biogeosciences Discussions is the access reviewed discussion forum of *Biogeosciences*

**Dating annually
resolved archives**

F. De Ridder et al.

Identification of the accretion rate for annually resolved archives

F. De Ridder^{1,2}, A. de Brauwere², R. Pintelon¹, J. Schoukens¹, and F. Dehairs²

¹Department of Fundamental Electricity and Instrumentation, Team B: System Identification and Parameter Estimation, Vrije Universiteit Brussel, Pleinlaan 2, 1050 Brussels, Belgium

²Department of Environmental and Analytical Chemistry, Vrije Universiteit Brussel, Brussels, Belgium

Received: 22 November 2005 – Accepted: 9 January 2006 – Published: 10 April 2006

Correspondence to: F. De Ridder (federid@vub.ac.be)

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Abstract

The past environment is often reconstructed by measuring a given proxy (e.g. $\delta^{18}\text{O}$) in an environmental archive, i.e. a species which gradually accumulates mass and records the current environment during this mass formation (e.g. corals, shells, trees, etc. . .). When such an environmental proxy is measured, its values are known as a function of distance. However, to relate the data to environmental variations, the date associated with each measurement, i.e. the time base, should be known. This is not straightforward solved, since species usually do not grow at constant rates. In this paper, we investigate this problem for annually resolved archives, which exhibit a certain periodicity. Such signals are often found in clams or corals. Due to variations in accretion rate the data along the distance axis have a disturbed periodic profile. A method is developed to extract information about the accretion rate, such that the original (periodic) signal as function of time can be recovered. Simultaneously the exact shape of the periodic signal is estimated. The final methodology is quasi-independent of choices made by the investigator. Every step in the procedure is described in detail and finally, the method is exemplified on a real world example.

1 Introduction

A problem often encountered in proxy-records is the reconstruction of the time-series, starting from measured distance series. Variations in accretion rate squeeze and stretch the distance series. This distortion results in the lengthening and shortening of individual features present in the signal, a broadening of spectral peaks, as well as the appearance of extraneous spectral peaks (see e.g. De Ridder et al., 2004). Such a distortion may occur during the recording (natural or artificial) of a signal or during its passage through certain kinds of filtering media. In some cases the accretion rate itself is of more interest than the recovered signal. In other cases it may be of interest to remove the distortion. Often, distortions of the type we are considering are removed

BGD

3, 321–344, 2006

Dating annually resolved archives

F. De Ridder et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

EGU

**Dating annually
resolved archives**

 F. De Ridder et al.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[I◀](#)
[▶I](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)

by correlating by eye. This, however, works only in the simplest cases, is not readily quantified and is generally limited to low resolution. What makes things worse is that two investigators, who are dating the same record with such an identical method, will come to different conclusions, because they may have selected different tuning points.

5 In the early '80s Martinson et al. (1982) proposed an inverse approach to signal correlating. They have presented a quantitative method for correlating a distance series with a given time series. In this paper, we go one step further and will estimate not only the accretion rate, but also the shape of the time series. To do so, we had to assume that the “true” time series is periodic. A second difference is that an automated model selection procedure is implemented, which chooses the model complexity using more objective, statistical rules. As will be shown, this allows us to extract the maximum amount of significant information from noisy data.

For the scope of this paper, we have assumed that when a measured proxy record is compared with a model, three types of errors occur:

- 15 1. *Stochastic noise*: models and data will never match perfectly. This has two reasons: (i) the measurements are disturbed by an unknown number of small effects, like instabilities in the measurement instrument etc. . . , and (ii) the modeled system can have a chaotic component. Fortunately, both effects can quite easily be described by an additional stochastic component in the model expression.

$$20 \quad s_n = s_{\text{model}}(t_n) + e \quad (1)$$

where n is the sample number, s the measured signal, s_{model} the model, t_n the date of observation n and e the error term, describing the difference between measurements and model. The main characteristics of this component are that it is zero on the average and that it can usually be described by a normal distribution with a standard deviation, σ .

Stochastic errors can be reduced by

- (i) refining the measurement set-up, which is in general expensive;

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

(ii) repeated measurements, which is time consuming. Here the model and systematic errors are deterministic and will be identical in each measurement set, while the stochastic errors will differ from measurement set to measurement set and can thus be averaged out;

(iii) a parametric model, which can introduce additional model errors. The stochastic errors inherent in each measured sample will average out when the parameters are estimated. The improved precision is mainly determined by the ratio measured observation to number of parameters.

2. *Model errors* are non-stochastic components that are not described by the model and which are not hidden by the stochastic noise. Identifying these is possible only after analyzing the stochastic properties. Systematic errors can occur due to inaccurate measurements or by un-modeled effects in the studied system and can thus be avoided by improving the accuracy of the measurement or by refining the model.

3. A special type of systematic errors, which is specific for proxy records and sediment analysis are *dating errors* (Martinson et al., 1982; Paillard et al., 1996; Yu and Ding, 1998; Lisiecki and Lisiecki, 2002; Ivany and Wilkinson, 2003). In the scope of this paper, these are catalogued as a separated third class. In this paper a strategy to remove this type of errors systematically is proposed, by refining the model.

The methodology proposed is based on the next remarks: in the measurement set the values of the observations are given, but the corresponding dates are missing. On the other hand, we often have a model, containing time. However, notice that each model consists of some model parameters, which can only be tuned by matching the model on the measurement set. So, in this context neither the experimentalist, nor the modeler has enough information to work isolated. Here, both are combined. The focus is on annually resolved archives, which often have a clear periodic component, so the discussion can be limited to periodic

signal models. Still, in general even climate models (Martinson et al., 1982) or other signal models¹ can be used. First the signal and time base models are explained and next solutions are given for two particular problems, i.e.

- (i) gathering initial values for the parameters; and
- (ii) due to the parametric representation of the time base, neighboring observations can be altered, which would mean that the time is locally inverted. This artifact is circumvented.

The approach is finally illustrated on two proxy records measured in clams.

2 The signal and time base model

In this and the next paragraph the formal set-up of the methodology (i.e. the equations used) are briefly explained. The signal under investigation is assumed to be periodic, sampled along an equidistant distance grid. Formally, this translates to the assumption that the discrete-time signal, $s_{\text{model}}(t_n)$, is given by

$$s_{\text{model}}(t_n) = A_0 + \sum_{k=1}^h A_k \cos(k\omega t_n) + A_{k+h} \sin(k\omega t_n) \quad (2)$$

where t_n is the unknown time variable at sample position, $n \in \{1, \dots, N\}$, A_0 the offset, A_k and A_{k+h} are the unknown amplitudes of the k th harmonic, ω is the unknown fundamental angular frequency and h the number of harmonics, yet to be identified. Changing the number of harmonics will change the complexity of the model (Fig. 1). Although the samples are equidistantly spaced along the distance axis, the time instance between two subsequent samples is not constant, because of variations in the

¹A signal model is a black box or empirical (versus physical) model describing the variation of the proxy, e.g. a sinusoidal or polynomial model.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

accretion rate. These distortions of the time base are modeled by a function, δ_n , called the time base distortion (T.B.D.)

$$\delta_n = \sum_{m=1}^b B_m \phi_m(n) \quad (3)$$

where ϕ is a set of b basis functions, B is a vector of length b , yet to be identified, with the unknown time base distortion parameters. The parameter b defines the complexity of the time base (vide infra). Note that it is practically impossible to estimate the time base distortion directly, by comparing the measurements with the signal model (Eq. 2), because

- (i) the measured record is disturbed by stochastic noise, which would be propagated into the time base distortion; and
- (ii) the signal model's parameters and complexity are unknown (so we can only assume that it is periodic, without knowing its precise shape).

The first problem is circumvented by the introduction of basis functions. We have tested trigonometric functions, Legendre polynomials and splines as basis function (Abramowitz and Segun, 1968; Dierckx, 1995). The latter seems to work best.

The time instances, t_n , are given by

$$t_n = (n + \delta_n)T_s \quad (4)$$

where T_s is the average sample period.

In order to overcome the second problem, all the unknowns, the model parameters and the time base distortion, are represented by some unknown parameters. For fixed values of h and b , these can be grouped in a vector

$$\theta = [\omega, A^T, B^T]^T \quad (5)$$

The optimal set of parameters can be calculated by a numerical minimization algorithm, which minimizes a least squares cost function. For this task a Levenberg-Marquardt algorithm was implemented (e.g. Pintelon and Schoukens, 2001).

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

3 Starting value problem and optimization strategy

Minimizing this cost function will only be successful, if one can start from a reasonable set of initial values. Otherwise the local optimization method will possibly not be able to converge towards a good minimum. In order to minimize the risk of converging towards a bad local minimum, the optimization strategy is performed in five steps (for a structure of the algorithm, see Fig. 2):

1. Initializing the frequency, ω : a non-parametric time base distortion and the corresponding frequency can be gathered for periodic signal records, following the guidelines of (De Ridder et al., 2004);
2. Initialization of the T.B.D. parameters, B : initial values for the T.B.D. parameters can be gathered by matching Eq. (3) on the non-parametric T.B.D. This can easily be done, because Eq. (3) is linear in the parameters, B . Next, Eq. (4) is used to get more precise dates of the observations.
3. Initialization of the signal parameters, A : these are gathered by matching Eq. (2) on the observations employing the previously estimated time base. An efficient algorithm is described in (Pintelon and Schoukens, 1996).
4. Relaxation: alternating, the T.B.D. parameters and the signal parameters are optimized, while the other set is remained fixed. Note that optimizing the T.B.D. parameters, while the signal parameters are constant is, in fact, the parametric orbital tuning method proposed by Martinson et al. (1982). This relaxation algorithm is stopped when the largest relative variation in the parameter vector, θ , is lower than a numerical stop criterion (typically 10^{-3}). This step in the optimization is implemented to increase the calculation speed but it will not influence the final results.
5. Final estimation of parameters: all parameter values are estimated together employing a Levenberg-Marquardt.

BGD

3, 321–344, 2006

**Dating annually
resolved archives**

F. De Ridder et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

EGU

4 Local time reversal problem

The method seems to have a major weakness: it is sensitive to time reversal problems, especially when the number of time base distortion parameters is relatively high (an example is given in Fig. 3). This is not surprising, because the noise sensitivity is larger in this case. However, we know that such time reversals are physically impossible, so the algorithm has to be extended: to avoid this unrealistic behavior an inequality constraint optimization was implemented (e.g. Fletcher, 1991): in each step of the Levenberg-Marquardt algorithm a check is performed to verify if any time reversals have occurred: is the minimal sample period lower than 20% of the average sample period? If so, the constraints become active and the time base distortion at these samples is fixed at this minimum for this step of the optimization routine. The dotted line in Fig. 3 shows the result after the implementation of the inequality constraint optimization.

5 Model selection criterion

If we would stop developing the algorithm at this point, the complexity of the signal model and time base model, quantified by h and b , respectively, are still chosen by the user. Figure 4 shows the accretion rate and Fig. 5 the signal models, estimated from the same measurement record, with identically the same algorithm, but with different levels of complexity. So, two types of problems can occur:

- (i) if two investigators would process the same record with the same algorithm and based on the same assumptions, it is still possible that they come to different conclusions;
- (ii) Maybe the true time base and/or signal models are more complex than defined by the investigator. This would mean that not all useful information is extracted from

BGD

3, 321–344, 2006

Dating annually resolved archives

F. De Ridder et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

EGU

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

the data. On the other hand is the risk also present that the chosen complexity was too high. This would result in conclusions that are not supported by the data.

What is happening? And can we do anything about it? The fact that the model and time base parameters can be optimized does not tell us anything about the significance of these parameters. It is very well possible that e.g. too much time base parameters are used, which would all be insignificant. These redundant parameters are only used to model the measurement noise. In this paragraph we tell how to find the optimal values for the number of harmonics, h , and for the number of T.B.D. parameters, b . To begin, we define the model complexity by the number of parameters, which are optimized. Increasing the model complexity will decrease the systematic errors, however, at the same time the model variability increases². Hence, it is not a good idea to select the model with the smallest cost function within the set because it will continue to decrease when more parameters are added. At a certain complexity the additional parameters no longer reduce the systematic errors but are used to follow the actual noise realization on the data. As the noise varies from measurement to measurement, the additional parameters increase only the model variability. However, usually we do not have repeated measurements and we would still like to draw conclusions from a model. For this reason, the cost function is extended with a model complexity term that compensates for the increasing model variability. Summarized, the model selection criterion, called MDL_c ³, should be able to detect undermodeling (= too simple model) as well as overmodeling (= too complex model). This model complexity term is dependent upon the signal-to-noise ratio and the availability of a noise model. In the examples of

²This means that if one would redo the measurement and match the same model, with the same model complexity again, the difference between the old and new model will be larger.

³We have followed the “minimum description length” nomenclature proposed by Rissanen (1978), which is also called the BIC criterion (Schwartz, 1978).

this paper the criterion to be minimized had the following expression

$$\text{MDL}_c(\hat{\theta}, n_\theta, n_c, N) = \frac{K(\hat{\theta})}{N} \exp p_c(n_\theta, n_c, N) \quad (6)$$

$$\text{with penalty } p_c(n_\theta, n_c, N) = \frac{\ln(N)(n_\theta - n_c + 1)}{N - (n_\theta - n_c) - 2}$$

with $K(\hat{\theta})$ the residual cost function, N the total number of observations and n_θ the number of parameters, reduced by the number of active constraints, n_c . Notice that introducing a model selection criterion eliminated interferences from the user, which makes the proposed method more objective and user independent.

Practically, the user chooses the maximum values for h and b , i.e. $(h, b)_{\max}$. Next, all models with a model complexity from $(h, b)=(0, 0)$ till this maximum are optimized and Eq. (8) is used to select the best model within this set (lowest MDL_c value). A detailed description of the model selection criteria can be found in (Akaike, 1974; Rissanen, 1978; Schwartz, 1978; De Ridder et al., 2005, de Brauwere et al., 2005).

6 Application: saxidomus giganteus

As an example, the $\delta^{18}\text{O}$ -signals measured in *Saxidomus giganteus* are processed. Two specimens were sampled from the West coast of the USA in Washington state, named Clam 1 and Clam 2. The large winter-summer variations are reflected in these signals (Figs. 6a and 7a) and this periodicity will be used to date the observations. The two clams lived under identical environmental conditions, so the correlation between the signals can be used to validate the method. In addition, the estimated accretion rates are compared.

To test the algorithm, the maximum model complexity was limited to $(h, b)_{\max}=(4, 20)$, i.e. four harmonics can be used to describe the signal model and 20 parameters can be used for the time base distortion. For some model complexities,

BGD

3, 321–344, 2006

**Dating annually
resolved archives**

F. De Ridder et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

EGU

the constraints became active. This was mostly the case when the number of time base distortion parameters, b , became high. The results are summarized in Table 1: the lowest model selection criteria, MDL_c , values were twice found for a signal model consisting of only one harmonic (see Figs. 6 and 7). Both samples were collected in 2001 and the most recent observation was dated as 1 April, so that annual maxima in $\delta^{18}O$ correspond to winter situations. The corresponding correlation between both records is 84% (see Fig. 8).

The accretion rates of both clams are shown in Fig. 9. Note that

1. Maybe annual variations in the accretion rate did occur, but such a time base distortion model was too complex according to the model selection criteria. So, the quality of the data is not sufficient to support annual variations in the time base distortion;
2. The estimated accretion rates decrease slowly with age, which can be expected;
3. most variation occurs at more or less the same moments in both clams. This is reflected in the correlation of 63% between the two accretion rate profiles. The mismatch between the two peaks around 1996 can be due to errors still present in the time base, which is used to construct and date the accretion rate. An alternative explanation can be found in the fact that the accretion rate is a non-linear function of the time base distortion parameters. Consequently, small errors on these parameters can have a large influence on the accretion rate than on the time base distortion itself.

The relatively high correlation illustrates that these variations are relevant (do not reflect the stochastic noise) and that they are determined not only by the age of the specimens, but also by external forcing. Otherwise, accretion rate would decrease much smoother with age or in a random manner. Such precise estimations of the accretion rates open the possibility to use this information for climate reconstruction purposes.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

7 Conclusion

We have presented a new method to reconstruct the time base for periodic archives. It is based on (Martinson et al., 1982) and (De Ridder et al., 2004). The novelty of this approach is that it estimates the time base together with the signal, describing the time series. The method is build around an identification approach and which has several advantages:

- (i) it is combined with a statistically-based model selection criterion, to choose the most appropriate model complexity;
- (ii) which makes it is robust to overmodeling in the signal and time base model; and
- (iii) which makes it robust to undermodeling;
- (iv) it is robust to stochastic measurement errors, since parametric signal and time base models are used,
- (v) it is robust to non-sinusoidal periodic signals, because overtones are modeled too.

The combination of (i), (iv) makes it possible to separate largely the stochastic noise from the significant variations. The combination of (i), (ii) and (iii) allows the user to extract the maximum amount of significant information, hidden in the record. In addition all tuning is done by the algorithm, which makes the method user-friendly and more objective. On the other hand, the algorithm does assume that the “true” record is periodic, which may not be true. A violation of this assumption may bias the final result. Note that the strategy proposed here is not limited to this specific periodic signal model, although gathering initial values for arbitrary models can become a hard task.

The method has been exemplified on two records of $\delta^{18}\text{O}$, measured in clams. Both clams lived in the same environment, so the time series of $\delta^{18}\text{O}$ could be used to check the robustness of the method. After optimization, the correlation between both records

BGD

3, 321–344, 2006

Dating annually resolved archives

F. De Ridder et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

EGU

was 84%. Furthermore, the correlation between the independently estimated accretion rates was 63%. This could indicate that also the accretion rate is changing with varying environmental conditions in a deterministic manner.

A matlab version of the algorithm is available on request.

5 *Acknowledgements.* F. De Ridder and A. de Brauwere are researcher of the Flemish Fund for Scientific Research (FWO-Vlaanderen) and are grateful for their support. This work was also supported by the Belgian Government (IUAP V/22), the Flemish Government and the Vrije Universiteit Brussel (GOA22/DSWER4, GOA23-ILiNoS, and HOA9). We are grateful to D. P. Gillikin for providing data from the *Saxidomus giganteus* clams. Finally, we would like to
10 thank G. Munhoven and D. Paillard for their comments and critics on this work.

References

- Abramowitz, M. and Segun, I. A.: Handbook of Mathematical Functions with Formulas, Graphs, and Mathematical Tables, New York, Dover, 1968.
- Akaike, H.: A new look at the statistical model identification, IEEE T. Automat Contr., AC-19, 716–723, 1974.
- 15 de Brauwere, A., De Ridder, F., Pintelon, R., Elskens, M., Schoukens, J., and Baeyens, W.: Model selection through a statistical analysis of the minimum of a Weighted Least Squares cost function, Chemometr. Intell. Lab., 76, 163–173, 2005.
- De Ridder, F., Pintelon, R., Schoukens, J., Gillikin, D. P., André, L., Baeyens, W., de Brauwere, A., and Dehairs, F.: Decoding nonlinear growth rates in biogenic environmental archives, Geochem. Geophys. Geosy., 5(12), Q12015, doi:10.1029/2004GC000771, 2004.
- 20 De Ridder, F., Pintelon, R., Schoukens, J., and Gillikin, D. P.: Modified AIC and MDL model selection criteria for short data records, IEEE T. Instrum. Meas., 54(1), 144–150, 2005.
- Dierckx, P.: Curve and surface fitting with splines, Oxford Univ. Press, 1995.
- 25 Fletcher, R.: Practical methods of optimization, John Wiley and Sons Ltd., Chichester, 1991.
- Golub, G. H. and Van Loan, C. F.: Matrix Computations, Johns Hopkins University Press, Baltimore, MD, 1990.
- Ivany, L. C., Wilkinson, B. H., and Jones, D. S.: Using stable isotopic data to resolve rate and

BGD

3, 321–344, 2006

Dating annually resolved archives

F. De Ridder et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

EGU

duration of growth throughout ontogeny: an example from the Surf Clam, *Spisula solidissima*, *Palaios*, 18, 126–137, 2003.

Lisiecki, L. E. and Lisiecki, P.: Application of dynamical programming to the correlation of paleoclimate records, *Paleoceanography*, 17(D4), 1049–1061, 2002.

5 Paillard, D., Labeyrie, L., and Yiou, P.: Macintosh program performs time-series analysis, *Eos Transactions AGU*, 77(39), 379, 1996.

Martinson, D. G., Menke, W., and Stofa, P.: An inverse approach to signal correlation, *J. Geophys. Res.*, 87(B6), 4807–4818, 1982.

10 Pintelon, R. and Schoukens, J.: An improved Sine-Wave Fitting Procedure for Characterizing Data Acquisition Channels, *IEEE T. Instrum. Meas.*, 45(2), 588–593, 1996.

Pintelon, R. and Schoukens, J.: *System Identification A Frequency Domain Approach*, IEEE PRESS, New York, 2001.

Rissanen, J.: Modeling by shortest data description, *Automatica*, 14, 465–471, 1978.

Schwarz, G.: Estimating the dimension of a model, *Ann. Stat.*, 6(2), 461–464, 1978.

15 Yu, Z. W. and Ding, Z. I.: An automatic orbital tuning method for paleoclimate records, *Geophys. Res. Lett.*, 25, 4525–4528, 1998.

BGD

3, 321–344, 2006

Dating annually resolved archives

F. De Ridder et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

EGU

Table 1. Summary of the selected models used in the *Saxidomus giganteus* examples.

	Clam 1	Clam 2
Residual cost function (per mil) ² , $K(\hat{\theta})$	3.48	4.64
Automated model selection criterion (per mil) ² , MDL_c	0.045	0.048
Number of observations, N	133	123
Selected number of harmonics, h	1	1
Selected number of T.B.D. parameters, b	9	10

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

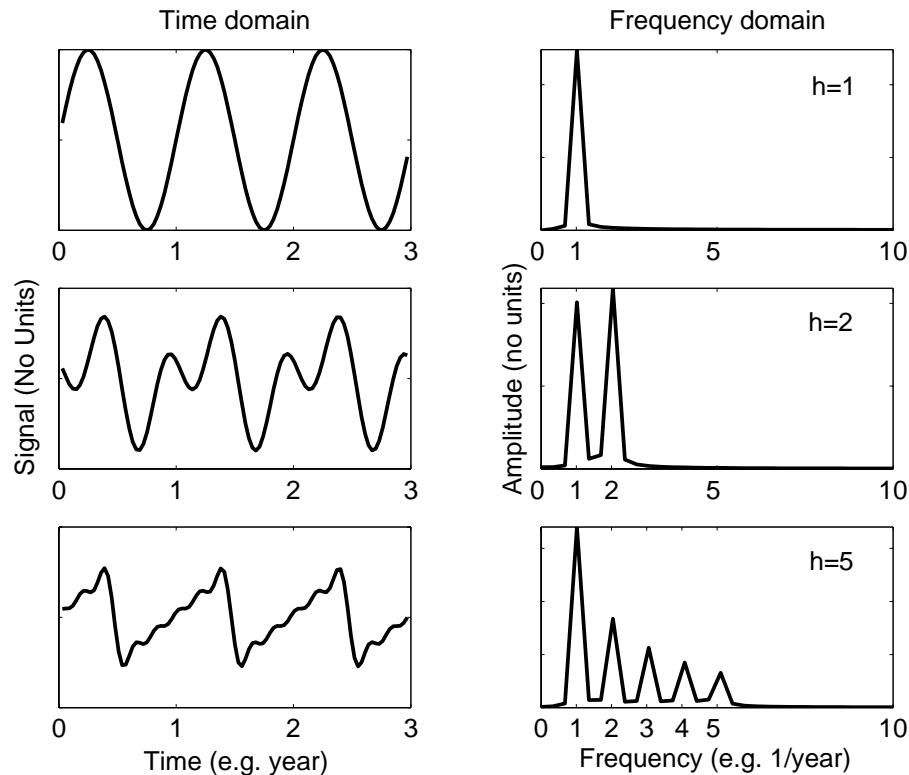


Fig. 1. Several signals are shown in the time and frequency domain. All signals are periodic, which is best seen in the frequency domain: the only non-zero amplitudes are found at integer frequencies. Notice further that with only one harmonic, $h=1$, the time signal is sinusoidal, while more complex periodic signals can be described using multiple harmonics.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

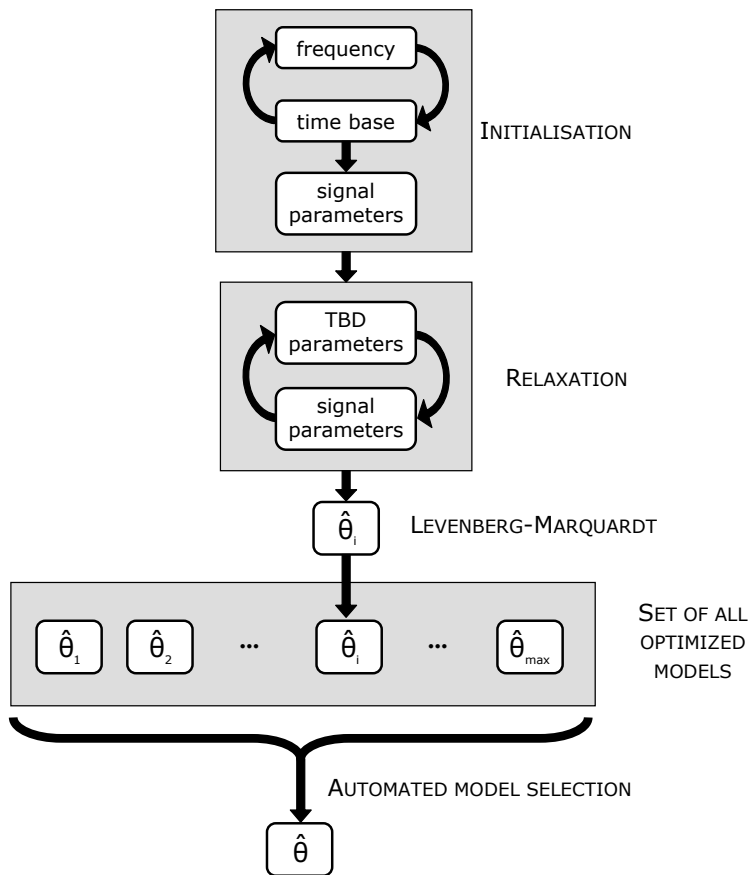


Fig. 2. Structure of the algorithm.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

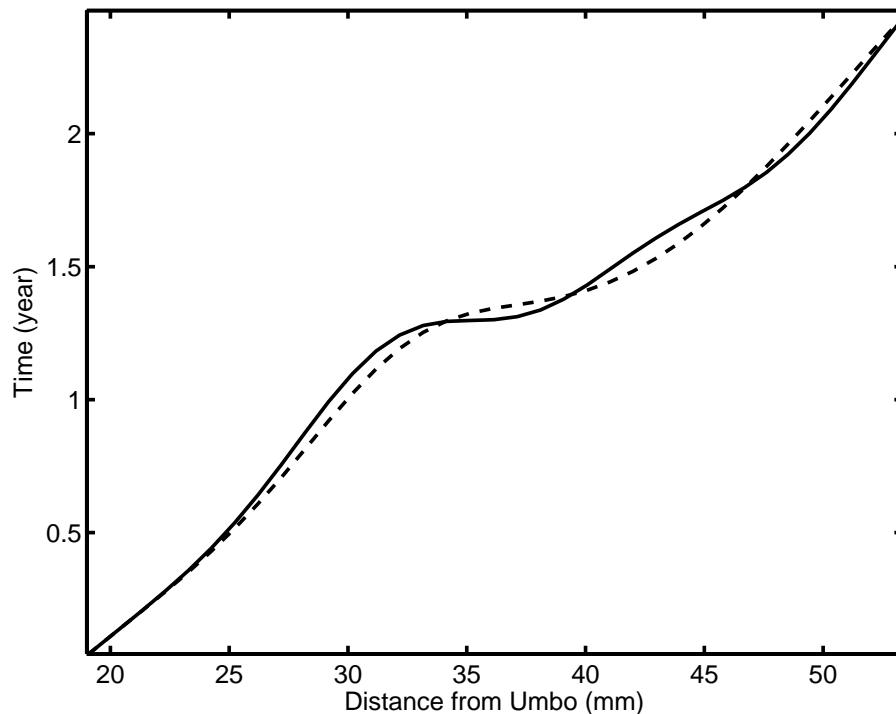


Fig. 3. Around 35 mm from the Umbo, the estimated time is constant (full line), which would correspond to an infinite accretion rate. In order to avoid this type of un-physical solutions, an inequality constraint optimization is implemented: if negative accretion rates occur, the time base is forced to remain slightly positive (dotted line).

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

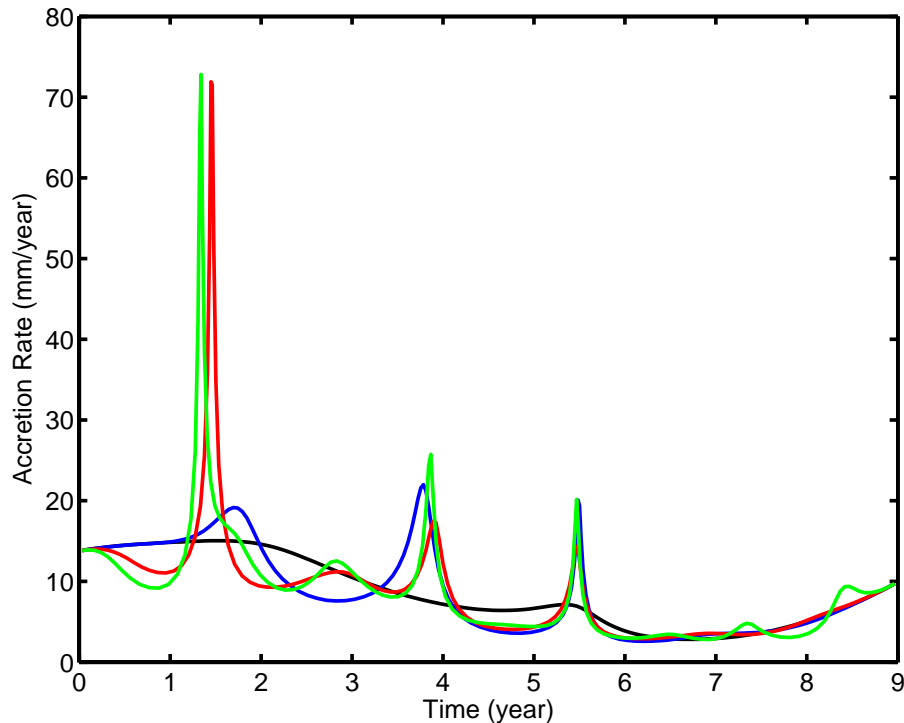


Fig. 4. The accretion rates are shown for different sets of model complexity (all matched on clam 1 (vide infra)): in black ($h=1$, $b=5$), in blue ($h=2$, $b=10$), in red ($h=3$, $b=15$) and in green ($h=4$, $b=20$). The variations increase with increasing complexity, but so far, we are not able to tell which of these accretion rates describes best reality. Note that the accretion rate of about 70 mm/year for the two most complex models is fixed at these levels due to the constraints, which have become active.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

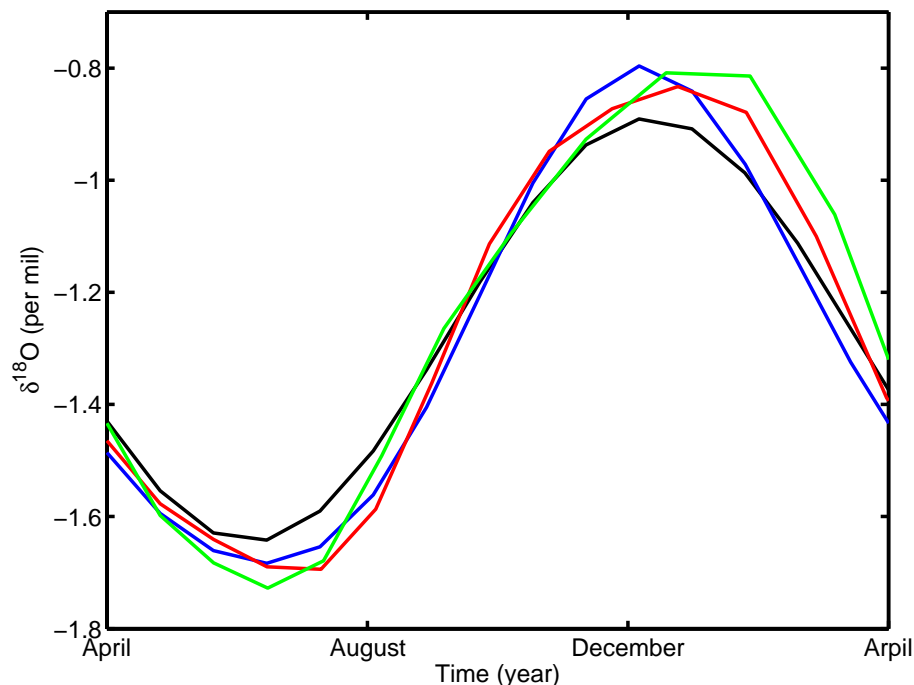


Fig. 5. One period of the periodic signals is shown (matched on clam 1 (vide infra)): in black ($h=1$, $b=5$), in blue ($h=2$, $b=10$), in red ($h=3$, $b=15$) and in green ($h=4$, $b=20$). Note that the amplitude of the black signal is different from that of the green signal. Further, the minima of the signals correspond quite well (June), but the maxima changes with about one month. Which of these models is closed to reality?

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[I◀](#)[▶I](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

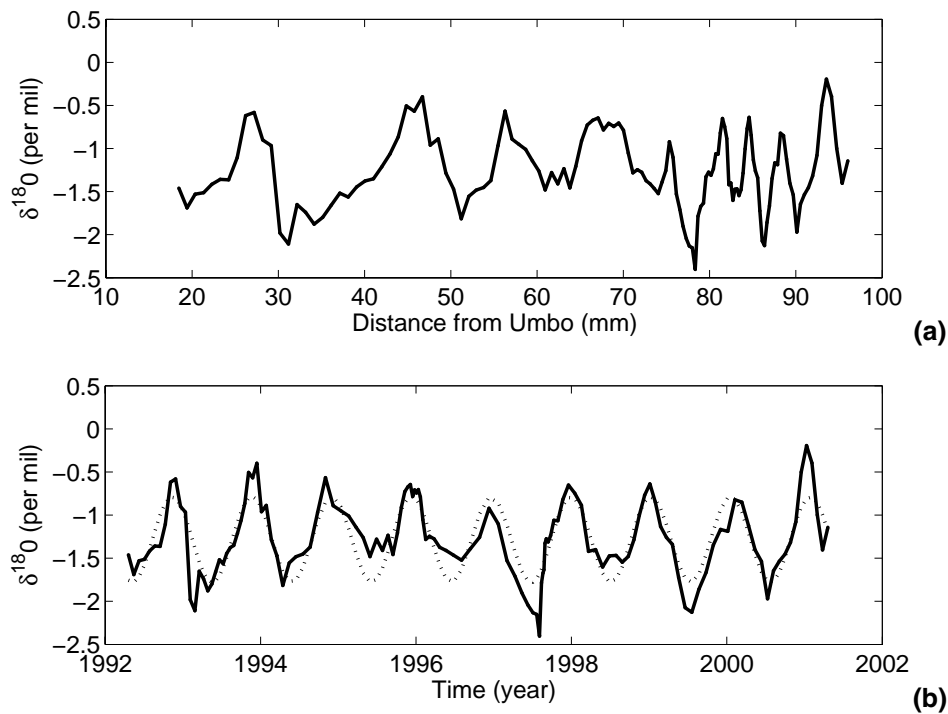


Fig. 6. Clam 1: **(a)** raw data and **(b)** signal on the constructed time base (full line) and the signal model (dotted line).

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

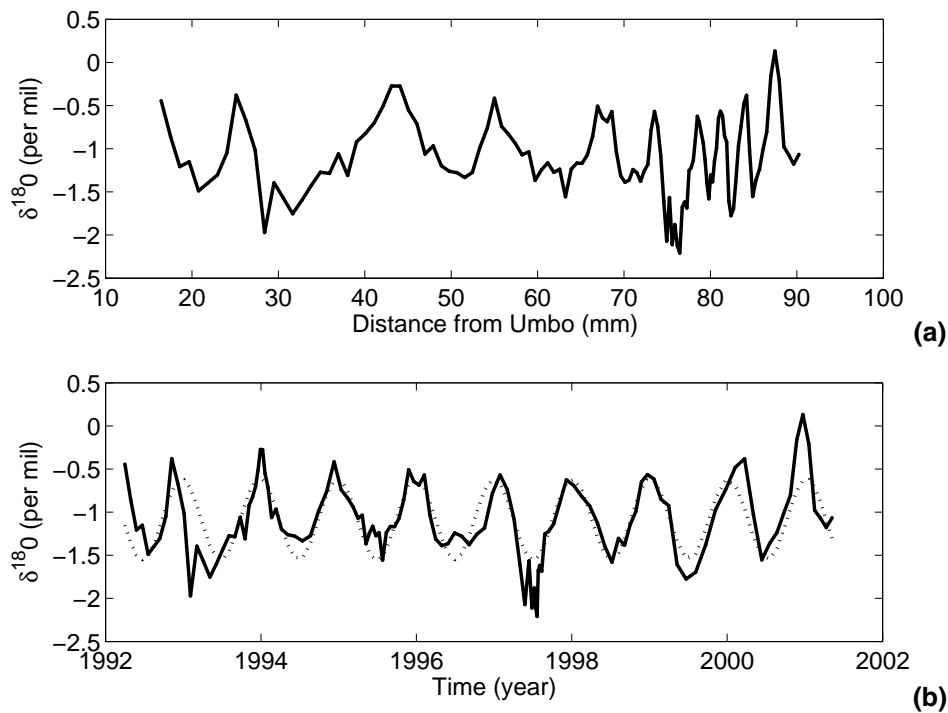
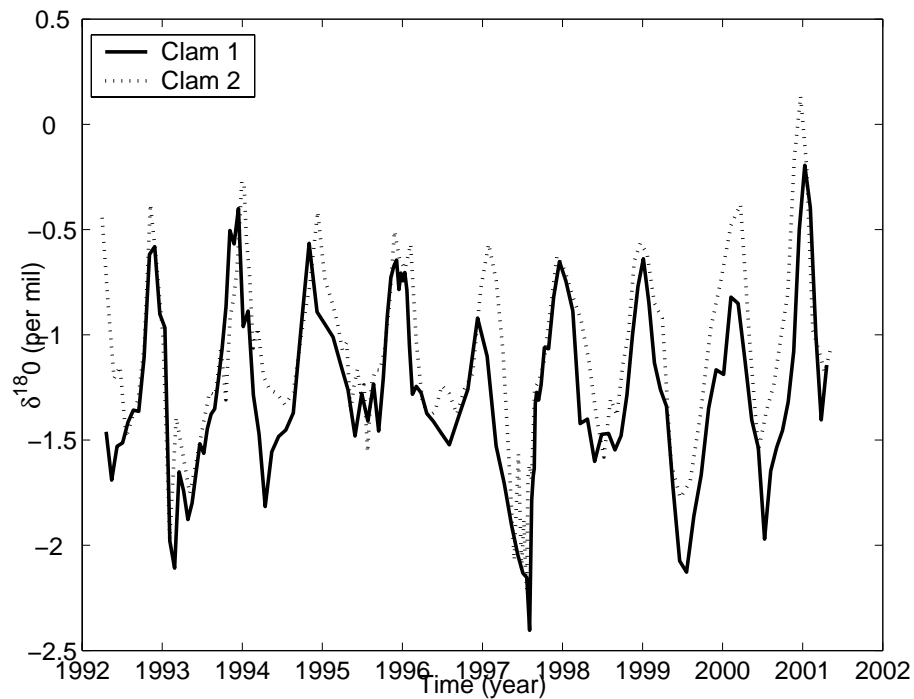


Fig. 7. Clam 2: **(a)** raw data and **(b)** signal on the constructed time base (full line) and the signal model (dotted line).

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[I◀](#)[▶I](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

**Dating annually
resolved archives**

F. De Ridder et al.

**Fig. 8.** $\delta^{18}\text{O}$ -records from the two clams after time base correction.[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[I◀](#)[▶I](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Dating annually resolved archives

F. De Ridder et al.

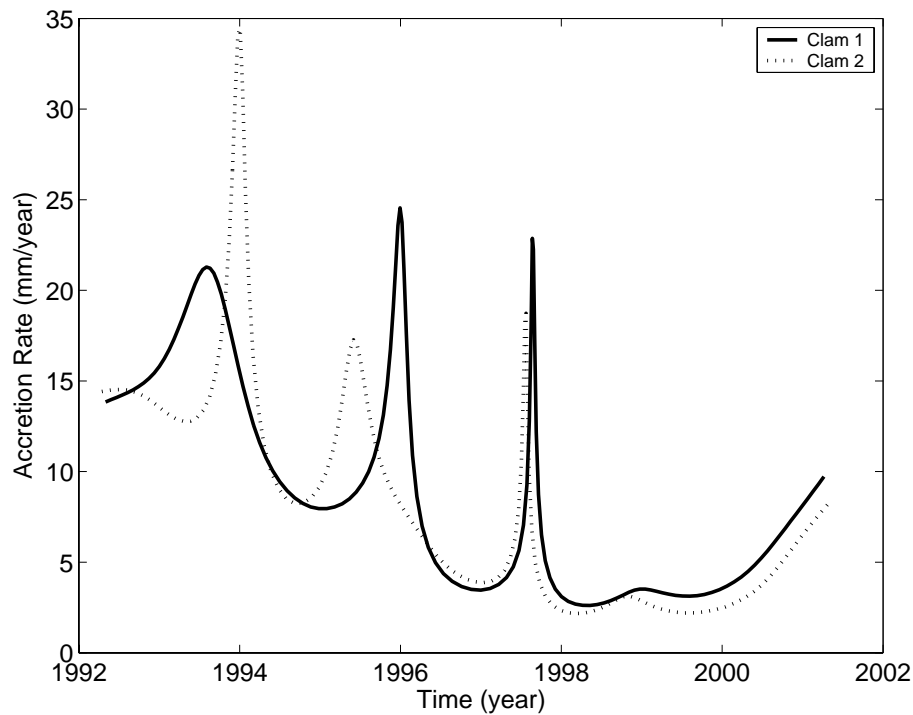


Fig. 9. Estimated accretion rate in both clams.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion