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Global 2-D intercomparison of sectional and modal aerosol modules

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Abstract. We present an intercomparison of several aerosol modules, sectional and modal, in a global 2-D model in order to differentiate their behavior for tropospheric and stratospheric applications. We model only binary sulfuric acidwater aerosols in this study. Three versions of the sectional model and three versions of the modal model are used to test the sensitivity of background aerosol mass and size distribution to the number of bins or modes and to the prescribed width of the largest mode. We find modest sensitivity to the number of bins (40 vs. 150) used in the sectional model. Aerosol mass is found to be reduced in a modal model if care is not taken in selecting the width of the largest lognormal mode, reflecting differences in sedimentation in the middle stratosphere. The size distributions calculated by the sectional model can be better matched by a modal model with four modes rather than three modes in most but not all situations. A simulation of aerosol decay following the 1991 eruption of Mt. Pinatubo shows that the representation of the size distribution can have a significant impact on modelcalculated aerosol decay rates in the stratosphere. Between 1991 and 1995, aerosol extinction and surface area density calculated by two versions of the modal model adequately match results from the sectional model. Calculated effective radius for the same time period shows more intermodel variability, with a 20-bin sectional model performing much better than any of the modal models.

1 Introduction

Aerosols are important to the radiative balance and chemistry of the atmosphere, and can modify cloud properties. In the stratosphere, aerosol particles provide surfaces for heterogeneous chemistry, modifying the ratio of active NO_x , HO_x , CIO_x , and BrO_x radicals to reservoir species (Fahey et al., 1993; Wennberg et al., 1994) and thus modifing ozone concentrations following volcanic eruptions (Hofmann and Solomon, 1989). In the troposphere, aerosol particles can act as cloud condensation nuclei, influencing cloud droplet number density and size (Penner et al., 2001), and thus cloud albedo. They also have direct radiative effects (Haywood and Ramaswamy, 1998) and can modify atmospheric circulation (Labitzke and McCormick, 1992; McCormick, et al., 1995) and temperature (Hansen et al., 2002).

This study was motivated by the requirements of the Global Modeling Initiative (GMI) 3-D chemical-transport model (Rotman et al., 200). The GMI model was created to be modular and permit intercomparisons between different process modules as a way of studying model sensitivity. It uses a variety of wind fields, from both assimilation systems and GCM simulations (Douglass et al., 1999; Strahan and Douglass, 2004). It can also use a variety of chemical schemes and parameterizations (Considine et al., 2000; Douglass et al., 2004). Sulfur chemistry and aerosol microphysics from the University of Michigan 3-mode model have been added to the tropospheric version of GMI (Liu et al., 2005). Eventually the GMI will operate with aerosol microphysics in a version which will span both troposphere and stratosphere, and can run with either a sectional or modal aerosol representation. This study tests and contrasts these two representations of aerosol size distribution in a 2-D model of the troposphere and stratosphere for both accuracy and computational efficiency.

Tropospheric aerosol models must deal with many types of aerosols, including sulfate, dust, sea salt, organics, and black carbon. Because of the computational requirements of 3-D tropospheric models, the prediction of aerosol mass was often considered adequate and fixed size distributions were assumed to evaluate radiative effects (Penner et al., 2001, 2002). More recent models have added the prediction of number density and size distribution using efficient

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methods such as modal representations (Wilson et al., 2001; Liu et al., 2005; Stier et al., 2005) or the method of moments (Wright et al., 2001). Regional tropospheric models have employed more detailed sectional representations (Jacobson, 2001; Zhang et al., 2004) to predict particle size distributions without imposing an a priori shape on the distribution.

Stratospheric aerosol models generally differ from tropospheric aerosol models because resolving the size distribution of aerosol particles becomes more important at altitudes above the tropopause. In the troposphere, only particles larger than $\sim 1 \,\mu m$ settle appreciably, whereas the thinner air in the stratosphere causes sedimentation rates to be a strong function of both particle radius and air density. Even particles of 0.01 μ m radius have significant sedimentation rates at 30 km. Resolving the size distribution of aerosol particles is crucial to predicting the correct sedimentation rate and therefore the lifetime and vertical distribution of particles in the stratosphere. Thus stratospheric models have generally used the sectional approach to resolve size distributions (Weisenstein et al., 1997; Timmreck, 2001; Pitari et al., 2002). Yet the sectional approach leads to numerical diffusion in size space, which may be excessive for a coarse resolution sectional model. The computational expense of a sectional model is mitigated for stratospheric studies because non-sulfate particles are not important in much of the stratosphere and therefore are generally omitted.

Many of the sulfur source gases are short-lived and have localized emissions, such as industrial sources. Rapid transport in convective cells is believed to play an important role in moving sulfur source gases from the boundary layer to the upper troposphere, where they may interact with clouds. Transport by diabatic ascent, cloud outflow, and horizontal motion moves sulfur from the troposphere into the stratosphere. Thus detailed modeling of tropospheric transport, cloud interactions, and microphysics is important to predicting the sulfur entering the stratosphere. For these reasons, we believe it important to model tropospheric and stratospheric aerosols together in a 3-D model like the GMI.

The University of Michigan aerosol module, referred to as UMaer, is described in Herzog et al. (2004). That paper applied the aerosol module within a zero-dimensional box model and compared results with the Atmospheric and Environmental Research (AER) sectional model using 40 or 150 bins. In that intercomparison, both models were thoroughly tested until the only remaining differences were due to the representation of the size distribution; differences in microphysical parameterizations were removed. Here that intercomparison is extended to two dimensions so that the impact of the different representations of size distribution will be seen in the model transport and sedimentation as well. The 2-D study is performed prior to implementation of aerosol microphysics in the stratosphere-troposphere GMI for efficiency. While details of tropospheric chemistry and transport are missing here, the stratospheric results in 2-D should not differ appreciably from stratospheric results in 3-D. Thus we focus most of our intercomparisons and comparisons with observations on the stratosphere. We have performed simulations of sulfate aerosol under background nonvolcanic conditions and a time dependent simulation from 1991 to 1999 including the Mt. Pinatubo eruption.

This paper presents descriptions of the 2-D model framework used as the intercomparison tool and the two aerosol modules in Sect. 2. In Sect. 3 we describe the intercomparison approach and model versions tested (three sectional, three modal). Section 4 provides results of a background atmosphere calculation in the troposphere and stratosphere, showing how differences in aerosol representation affect model results. Section 5 shows results of a volcanic simulation and the differences in aerosol removal rates with the different approaches. A summary and discussion is provided in Sect. 6.

2 Model descriptions

The AER 2-D model is used as the framework for this intercomparison, with transport, sulfur chemistry, and aerosol microphysics performed for the global domain from the surface to 60 km. Grid resolution is 9.5° in latitude and 1.2 km in the vertical. Transport is effected by the residual circulation and by horizontal and vertical diffusion. We use transport parameters from Fleming et al. (1999) which are calculated from observed ozone, water vapor, zonal wind, and temperature for climatological conditions. Wave driving is provided by forcing from six planetary waves and the effects of gravity wave breaking. Diabatic heating rates are computed following Rosenfield et al. (1974), with tropospheric latent heating from Newell et al. (1974). The calculation of horizontal diffusion coefficients follows Randel and Garcia (1994).

Since we are modeling sulfate aerosols for this intercomparison, we model only sulfur chemistry and use necessary radical concentrations from other model simulations. Sulfur source gases include DMS, H₂S, CS₂, OCS, and SO₂. Surface fluxes are 25 MT sulfur per year from DMS, 1 MT sulfur from CS₂, 8.7 MT sulfur from H₂S, and 78 MT sulfur from SO₂. In addition, we assume a surface mixing ratio for OCS of 500 pptv which provides a stratospheric source of sulfur. Photolysis and reactions with OH, O, O₃, and NO₃ convert sulfur source gases to sulfuric acid. Concentrations of these reactants are taken from a present-day simulation with the AER 2-D chemical-transport model and vary seasonally. Details of the chemical scheme can be found in Weisenstein et al. (1997). Reaction rates are taken from the JPL 2002 compendium (Sander et al., 2003). Homogeneous nucleation of sulfuric acid vapor occurs chiefly in the tropical upper troposphere due to low temperatures and high relative humidity. Subsequently, condensation increases the size of particles, while coagulation limits their number density. Evaporation occurs in the 30-40 km altitude region, yielding H₂SO₄ vapor, and, after photolysis, SO₂.

The University of Michigan aerosol module (UMaer) is capable of treating the nucleation and growth of sulfuric acidwater aerosols, as well as their coagulation with nonsulfate particles (Herzog et al., 2004). Aerosol size distributions, defined by N(r), particle number concentration at radius r, are treated by predicting two moments (mass and number) of the two or more lognormal distributions

$$\frac{dN(r)}{dr} = \frac{N_0}{\sqrt{2\pi}r_g \ln \sigma_g} \exp(-\frac{1}{2}\frac{\ln^2(r/r_g)}{\ln^2 \sigma_g})$$
(1)

each of which is defined by a mode radius r_g and a distribution width σ_g . The distribution width is specified. As mass is added to each mode and the particles grow, a merging process shifts mass from mode to mode, keeping the mode radii within defined bounds. The module performs dynamic time stepping without operator splitting such that all aerosol processes interact with each other during each time step. It can be applied to both tropospheric and stratospheric conditions, but to date has been used only in the troposphere and lowermost stratosphere.

The AER 2-D sulfate aerosol model was described in Weisenstein et al. (1997, 1998). The aerosol module uses a sectional representation of the particle size distribution and can represent any arbitrary distribution shape. Particle number density in 40 bins between 0.4 nm and $3.2 \,\mu$ m by volume doubling is predicted, though the bin number, smallest bin radius, and volume ratio between bins are adjustable parameters. The model is intended for stratospheric applications and includes only sulfuric acid-water particles. Aerosol composition, or weight fractions of sulfate and water, is adjusted continuously based on ambient temperature and relative humidity according to Tabazadeh et al. (1997). Particle sizes are based on both sulfate and water fractions, so that particles grow or shrink when either temperature or water vapor concentration changes in a grid box. The microphysical solution uses operator splitting with a time step of one hour for transport, chemistry, and microphysics, but 20 substeps for the condensation and nucleation processes to prevent one process from dominating the gas-to-particle exchange rate.

Our goal in this intercomparison, and our previous box model intercomparison (Herzog et al., 2004) was to compare microphysical modules which are identical except in the way that the size distribution is represented. To that end, we have compared each aerosol process carefully and ensured that initial tendencies are identical. We use the Vehkamaeki et al. (2002) nucleation parameterization, which is in agreement with more detailed calculations of hydrated clusters for temperatures greater than 190 K. The parameterization calculates the radius, composition, and production rate of new particles. The UMaer module adds the new particle number and mass to the smallest aerosol mode, exactly preserving the calculated number density. The AER module requires that the nucleated mass be added to a single bin with a fixed radius, so particle number is adjusted to preserve the calculated nucleation mass.

The condensation and evaporation process is treated as described in Herzog et al. (2004). The condensational growth or evaporation in each bin or mode depends of the difference in the gas phase H_2SO_4 concentration, N_{gas} , and the equilibrium concentration of H_2SO_4 above the particle surface, N_{gas}^{equ} , and is described by

$$\frac{\partial}{\partial t}N_{\rm gas} = -4\pi\beta D(N_{\rm gas} - N_{\rm gas}^{\rm equ})r_p N_p \tag{2}$$

where β is a term correcting for noncontinuum effects and imperfect surface accomodation, *D* is the diffusion coefficient for H₂SO₄ molecules in air, and N_p is the number density of particles in the bin or mode. For the sectional model, r_p is the bin radius. For the modal model, the appropriate radius r_p depends on the volume mean wet radius, $\overline{r_{vol}}$, and the width of the lognormal distribution, σ_g ,

$$r_p = \overline{r_{\text{vol}}} \exp(-\ln^2 \sigma_g). \tag{3}$$

Wet radius is calculated using the Tabazadeh et al. (1997) parameterization for aerosol composition. The Kelvin effect is included in the calculation of N_{gas}^{equ} and depends upon particle radius. The modal model uses volume mean radius in this calculation, and for calculation of the Knudsen number when calculating β . Condensation doesn't change the number of particles, only the mass in each mode for the modal model. In the sectional model, condensational growth shifts particles to larger bin sizes. Evaporation does the opposite, shifting particles to smaller sizes, but net number density is only reduced for evaporation from the smallest bin size or mode.

The coagulation process reduces number concentration and shifts aerosol mass into larger particles. A coagulation kernel defines the collision probability of two paticles of different radii, and depends on the radius of each particle and the particle diffusion coefficients. The modal model uses volume mean wet radius for this calculation. In the sectional model, when two particles of radii r_i and r_j collide, where $r_i < r_i$, a particle is removed from bin *i* and a new particle with size intermediate to bin *j* and bin j+1 is created. We apportion the particle mass between the two bins but this process results in numerical diffusion in size space. If the ratio of adjacent bin volumes is 2.0, then coagulation of two particles in bin *j* results in a particles of exactly radius r_{i+1} . In the modal model, coagulation within a mode results in a reduction in number in that mode. Coagulation between modes results in a reduction in mass and number of the smaller mode and an increase of mass in the larger mode.

The sedimentation process affects the vertical distribution of aerosol sulfate, particularly in the middle stratosphere, and reduces the residence time of particles. The gravitational settling velocity of a particle with radius r_p is given by

$$v_{\text{grav}} = \frac{2}{9} \frac{g}{\eta_{\text{air}}} r_p^2 \rho_p \left[1 + Kn [1.257 + 0.4 \exp(-1.1Kn^{-1})] \right]$$
(4)

Module	Label	Bin ratios by volume	Time step	Run time rel. to AER40
AER 150 bins	AER150	V _{rat} =1.2	15 min	20
AER 40 bins	AER40	V _{rat} =2.0	1 h	1.0
AER 20 bins	AER20	V _{rat} =4.0	1 h	0.25
Module	Label	Distribution width σ_g	Merge radii	Run time rel. to AER40
UMaer 3 modes	UMaer-3mA	1.2/1.514/1.77623	0.005/0.05	0.7
	UMaer-3mB	1.2/1.514/1.6	0.005/0.05	0.7

Table 1. Model versions used in 2-D intercomparison study.

with

$$Kn = \frac{\lambda_{\text{air}}}{r_p} \tag{5}$$

according to Stokes law with the Cunningham slip correction factor (Seinfeld and Pandis, 1997). Here λ_{air} is the mean free path of air and η_{air} is the viscosity of air. The sectional model applies the above settling velocity for each bin. The modal model applies one settling velocity per mode, replacing r_p with an effective radius appropriate for sedimentation of aerosol number

$$r_p^{\text{num}} = \overline{r_{\text{vol}}} \exp(-0.5 \ln^2 \sigma_g) \tag{6}$$

or for sedimentation of aerosol mass

$$r_p^{\text{mass}} = \overline{r_{\text{vol}}} \exp(2.5 \ln^2 \sigma_g). \tag{7}$$

Since settling velocity is quite sensitive to particle radius for submicron particles at altitudes above about 25 km, we expect that the difference in a modal and a sectional model may be pronounced above 25 km.

The box model intercomparison between these two aerosol modules (Herzog et al., 2004) showed that the modal model was capable of predicting both aerosol number concentration and surface area to within a factor of 1.2 (4 modes) or 1.3 (2 modes) on average as compared to the sectional model. Prediction of accumulation mode particle number concentration was not as accurate but still generally within a factor of 2.1. This intercomparison is performed within a 2-D model in order to compare differences due to transport and sedimentation over seasonal and decadal time scales. In the sectional model, transport occurs independently for each size bin. In the modal model, transport modifies the number and mass for each mode. Sedimentation in the modal model is a function of the assumed distribution width, since the larger tail of the distribution is much more sensitive to settling, yet the entire modal distribution is given the same settling velocity. Sedimentation not only removes particles from a given grid box, it also moves particles from higher to lower altitudes, affecting local size distributions and vertical mass profiles. We expect sedimentation to contribute to much of the difference between model-calculated aerosol distributions, and therefore we perform some calculations with and without sedimentation.

3 Intercomparison approach

Our intercomparison approach is to apply the different aerosol modules within the same 2-D chemical-transport model. Thus transport and chemistry are treated identically insofar as possible. We use the AER sectional model with 20, 40 bins, or 150 bins. The 40-bin version is our standard treatment. The 150-bin version is computationally expensive, but reduces the numerical diffusion inherent in a sectional model. We treat this version as the most accurate model numerically, thus allowing us to analyze deficiencies in the AER 40-bin model. A low-resolution 20-bin model is also used. The UMaer modal model is run with three modes and with four modes. We present two 3-mode versions differing in the width, σ_g , of the largest mode. For each modal model, we specify the distribution width and size limits of the modes. The model versions and their defining parameters are listed in Table 1. Also shown in Table 1 are the time steps used in the sectional models and the runtime of each model relative to the AER40 version. Each model is run to steadystate for a background atmosphere case without volcanic influence. The final state is independent of the initial condition. Most of these cases are also run in time-dependent mode for a Pinatubo-like injection of volcanic SO₂ in the tropical stratosphere, so that we can compare the volcanic aerosol decay rates over an eight year period. These calculations are initialized with the steady-state background condition for the respective model.

Each model version covers the diameter range from subnanometer to about $3 \mu m$. In the sectional model, the bin spacing is described by the parameter V_{rat} which is the ratio



Fig. 1. Model calculated aerosol parameters from the AER 2-D model using the 150-bin sectional aerosol module AER150. Shown are annual average (a) mass density in μ g/m³, (b) surface area density in μ m²/cm³, (c) effective radius in μ m, and (d) number density of particles with radius greater than 0.05 μ m in cm⁻³.

of particle volumes between adjacent bins. Typical stratospheric aerosol sectional models (see Bekki and Pyle, 1992; Mills et al., 1999; Timmreck, 2001) employ V_{rat} values of 2.0, as does our 40-bin model. Our 150-bin model uses a V_{rat} of 1.2 to cover the same radius space. Numerical stability demands smaller time steps as the number of bins increases. We use a 15 min time step for the 150-bin model and a one hour time step for the 40-bin and 20-bin models, in each case applying 20 substeps for condensation and nucleation.

The modal model specifies the width of each mode, σ_g . In addition, merge radii are required which specify when aerosol mass is shifted to the next larger mode as the mean radius of the mode increases. This process is invoked when 2.5% of all particles in a mode are larger than the specified merge radius. See Herzog et al. (2004) for details of this process. The modal version UMaer-3mA uses mode definitions which were tuned to calculate tropospheric aerosols. UMaer-3mB has an adjustment of the largest mode for better stratospheric performance. UMaer-4m is a 4-mode version which can better represent the details of the size distribution under varying conditions. The computational requirements of the 3-mode model are about 70% that of the 40-bin model. The 4-mode model requires about 110% of the computational resources of the 40-bin model. The 150-bin model increases the computational cost by a factor of 20 over the 40-bin model, is not practical for global calculations in 2-D, and is prohibitive for 3-D. The 20-bin model proved the most efficient, only 25% the CPU time of the 40-bin model, but with significant degradation in accuracy.

4 Nonvolcanic atmosphere intercomparison

We use the AER model with 150 bins (designated AER150) as the best numerical solution for the background atmosphere simulation. We define the background atmosphere for sulfate aerosol as an atmosphere with biogenic and anthropogenic sulfur emissions appropriate to the year 2000, but without volcanic influence. We omit aerosol types other than sulfate for simplicity in our intercomparison. The modeled tropospheric aerosol is not realistic without dust, sea salt, organic



Fig. 2. Percent difference in annual average aerosol extinction at (a) $1.02 \,\mu$ m and (b) $0.525 \,\mu$ m between the AER150 model simulation and SAGE II version 6.1 observations for 2001–2002.



Fig. 3. Calculated size distributions from the AER 2-D model using the 150-bin sectional aerosol module AER150 (black lines), the 40-bin sectional aerosol module AER40 (red lines), and the 20-bin sectional aerosol module AER20 (yellow lines) in April at (**a**) the equator and 10 km, (**b**) the equator and 20 km, (**c**) the equator and 30 km, and (**d**) 55° N and 20 km.

carbon, and black carbon and cannot be compared with observations. The stratospheric aerosol is realistic a few kilometers away from the tropopause, and will be compared with global observations from the SAGE II satellite. In Fig. 1 we show calculated annual average aerosol properties from the AER150 model version for the global domain from the surface to 40 km (the top of the aerosol layer). Aerosol mass density in μ g/m³, including both sulfuric acid and water in particulate form, is shown in Fig. 1a, and surface area density in μ m²/cm³ in Fig. 1b. These integrated aerosol quantities



Fig. 4. Percent change in model-calculated aerosol parameters from the AER 2-D model using the 40-bin sectional aerosol module AER40 versus the 150-bin sectional aerosol module AER150. Shown are annual average differences in (**a**) mass density, (**b**) surface area density, (**c**) effective radius, and (**d**) number density of particles with radius greater than $0.05 \,\mu$ m.

are important for mass balance and heterogeneous chemistry affecting ozone, respectively. Shown in Fig. 1c is the effective radius, defined as

$$R_{\rm eff} = \frac{\int r^3 \frac{dN}{dr} dr}{\int r^2 \frac{dN}{dr} dr}$$
(8)

and in Fig. 1d the number density of particles with radii greater than $0.05 \,\mu$ m.

SAGE II version 6.1 observations of aerosol extinction at 1.02 and 0.525 μ m are compared with AER150 extinctions, calculated by applying a Mie scattering code to the model-generated size distributions, in Fig. 2. The SAGE II data represent an average with gap-filling over the 2001–2002 period, as detailed in the SPARC aerosol assessment report (Thomason and Peter, 2006). The AER150 model produces calculated 1.02 μ m extinctions well below the SAGE II observations in the troposphere and tropopause region due to omission of non-sulfate aerosols, but within 30% of SAGE II observations in the stratosphere below 30 km. Calculated extinctions above 30 km are significantly below observations,

and represent a combination of observational uncertainty and perhaps a poor representation of the evaporation process in the model. The comparison with 0.525 μ m SAGE II extinction also shows agreement within 30% in the midstratosphere, but a different spatial pattern than the 1.02 μ m extinction, indicating errors in model-representation of the size distribution. Uncertainties in model transport are also a factor in these comparisons. But the general agreement between the model and observations in the mid-stratosphere indicates a reasonable representation of sulfur sources and aerosol microphysics. Differences between the model versions reported here are in many cases no greater than other model uncertainties, though these differences, caused by the representation of the size distribution, are shown to produce biases.

We compare the AER sectional modules with 40 bins (AER40) and 20 bins (AER20) with the sectional model using 150 bins (AER150) to assess their accuracy relative to numerical diffusion in radius. Figure 3 shows calculated aerosol size distributions in April at several latitudes and



Fig. 5. Percent change in model-calculated aerosol parameters from the AER 2-D model using the 20-bin sectional aerosol module AER20 versus the 150-bin sectional aerosol module AER150. Shown are annual average differences in (a) mass density, (b) surface area density, (c) effective radius, and (d) number density of particles with radius greater than $0.05 \,\mu$ m.



Fig. 6. Percent change in annual average model-calculated aerosol mass density with sedimentation versus without sedimentation in the AER40 model (panel **a**). Percent difference in annual average model-calculated aerosol mass density between the UMaer-3mA model without sedimentation and the AER40 model without sedimentation (panel **b**).

altitudes for the AER150 model, the AER40 model, and the AER20 model. The size distributions are very similar, but

lower resolution in size space produces more large particles and more small particles due to the size broadening effect гò

40

30

20

10

90°S

60°S

30°S

ΕQ

Latitude

(a)

Altitude (km)





Fig. 7. Percent change in model-calculated annual average aerosol parameters from the AER 2-D model using the UMaer 3-mode aerosol module UMaer-3mA versus the 150-bin sectional aerosol module AER150. Shown are annual average differences in (a) mass density, (b) surface area density, (c) effective radius, and (d) number density of particles with radius greater than 0.05 μ m.

of numerical diffusion. At the equator and 20 km, shown in Fig. 3b, a nucleation mode is evident along with an accumulation mode. Size broadening in the AER40 and AER20 models leads to significantly more particles between the two modes.

Figure 4 shows percent differences between AER40 and AER150 in aerosol mass density, surface area density, effective radius, and number density. Aerosol mass density between AER40 and AER150 is identical in the troposphere, but in the stratosphere AER40 is reduced by 1% at the tropopause to 10-15% at 30 km relative to the AER150 model. The reduction in aerosol mass density with altitude is caused by greater sedimentation in AER40 with its slightly broader size distributions. AER40 also shows less surface area density than AER150, by 4-14% between the surface and 30 km. Reductions in the troposphere are seen due to differences in the size distributions between the two models, even though their mass densities are the same. Effective radius is increased by 0-6% in AER40, consistent with the increase in large particles which leads to increased sedimentation. Number density for particles greater than $0.05 \,\mu m$ radius is decreased by 8-12% throughout most of the troposphere and stratosphere. Figure 5 shows similar plots for the AER20 model relative to the AER150 model. Mass density of the AER20 model is 5–30% smaller than the AER150 model in the stratosphere. Surface area density is 15-30% smaller. Effective radius is increased by 2-18%, and number density decreased by 25–30%.

We have run the AER40, AER20, UMaer-3mA, UMaer-3mB, and UMaer-4m models without sedimentation, since we expect that sedimentation will play a major role in differences between these models. Figure 6a shows the impact of sedimentation on aerosol mass density in the AER40 model. Sedimentation reduces aerosol mass by a few percent at the tropopause, up to 40% at 15 km, and up to 90% at 30 km. In the tropics below 25 km, aerosol mass is increased by sedimentation, since particles sediment from above into this region, and the upwelling circulation causes some particles to stagnate here. Figure 6b shows a comparison of aerosol mass density calculated by the UMaer-3mA model



Fig. 8. Calculated size distributions from the AER 2-D model using the 150-bin sectional aerosol module AER150 (black lines), the 3-mode UMaer-3mA aerosol module (blue lines), the 3-mode UMaer-3mB aerosol module (green lines), and the 4-mode UMaer-4m aerosol module (cyan lines) in April at (**a**) the equator and 10 km, (**b**) the equator and 20 km, (**c**) the equator and 30 km, and (**d**) 55° N and 20 km.

without sedimentation versus the AER40 model without sedimentation. In all of our comparisons, we adjust the radii of modal distributions to include condensed water, since the sectional model size distributions include both water and sulfate. Differences between the models without sedimentation are 0-20% within the stratosphere below 35 km, and less than 5% in the troposphere. Over most of the model domain, the UMaer-3mA model without sedimentation calculated more aerosol mass density than the AER40 model without sedimentation. The UMaer-3mB model does not differ substantially from the Umaer-3mA model without sedimentation. The UMaer-4m model differs from the Umaer-3mA model by 2% or less in aerosol mass density in the lower stratosphere when sedimentation is omitted. The AER20 model without sedimentation does not differ from the AER40 model below 35 km.

When sedimentation is included in the calculations, differences between the modal and sectional models become considerably larger. Figure 7a shows percent differences in aerosol mass density between models UMaer-3mA and AER150. The models don't differ in the troposphere, but the UMaer-3mA model calculates less aerosol mass in most of the middle stratosphere, by as much as 40%. In the tropical lower stratosphere, the UMaer-3mA model calculates up to 20% more aerosol mass, and near the tropopause at high latitudes up to 10% more aerosol mass. In the comparison

without sedimentation, the UMaer-3mA model showed an increase of 5-10% in aerosol mass over most of the stratosphere relative to AER40. Sedimentation is removing more aerosol mass in the middle stratosphere of the UMaer-3mA model than in the AER150 model, and the excess sedimentation is increasing aerosol mass in parts of the lower stratosphere. Since an entire mode sediments at one rate, the modal model behaves differently than a low-resolution sectional model. Changes in surface area density between Umaer-3mA and AER150 are show in Fig. 7b. Surface area changes in both the troposphere and stratosphere, with differences within 20% everywhere except at high latitudes and high altitudes. Figure 7c shows differences in effective radius, which is lower than AER150 by up to 30% at 30 km, and greater by up to 20% in the tropical upper troposphere and lower stratosphere. Number density, shown in Fig. 7d, is lower than AER150 by 10-20% in most of the stratosphere and up to 30% in the troposphere, but greater by 10% in the tropical lower stratosphere.

The aerosol size distributions generated by the modal models are shown in Fig. 8 for several latitudes and altitudes and compared with size distributions generated by the AER150 model. The blue lines represent the UMaer-3mA model and the green lines the UMaer-3mB model. These are both 3-mode models and differ only in the width of the third and largest mode. As seen in the figures, UMaer-3mA



Fig. 9. Percent change in model-calculated annual average aerosol parameters from the AER 2-D model using the UMaer 3-mode aerosol module UMaer-3mB versus the 150-bin sectional aerosol module AER150. Shown are annual average differences in (a) mass density, (b) surface area density, (c) effective radius, and (d) number density of particles with radius greater than $0.05 \,\mu$ m.

always produces more large particles than UMaer-3mB and both produce more large particles than AER150 for the locations shown. The 4-mode UMaer-4m model results are shown with cyan lines. The size distributions that the modal model is capable of reproducing accurately depend on the imposed number of modes and widths of those modes. The distribution shown in Fig. 8b for 20 km at the equator in April is a lognormal distribution of aged aerosol particles centered at about 0.1 μ m with a secondary peak below 0.001 μ m due to nucleation. The 3-mode models reproduce this distribution well. The 4-mode model calculates too many particles in the 0.001 to 0.004 μ m size range. The distribution shown in Fig. 8a for the tropical upper troposphere contains large numbers of particles from 0.0005 μ m to 0.1 μ m and results from continual nucleation. The 3-mode models cannot reproduce this distribution over the full range of radii, but capture the distribution well for particles greater than 0.01 μ m. The 4-mode model more accurately captures the particle distributions for radii less than 0.01 μ m. The distributions shown in Figs. 8c and d represent an aerosol population that may have been subjected to evaporation or mixing of air masses with different histories. Both the 3-mode and 4-mode models have difficulty reproducing the lower size cutoff of these distributions, with the 3-mode models performing better. However, since integrated aerosol properties depend most strongly on the larger particles in the distribution, this failure may not be significant for many applications.

Figure 9 shows percent changes in integrated aerosol properties for the UMaer-3mB model relative to the AER150 model. This figure can be compared with Fig. 7 to evaluate how the width of the large mode in the 3-mode model affects quantities such as aerosol mass density and effective radius. The narrower width of the large mode in UMaer-3mB does lead to an aerosol mass density above 25 km which is closer to the AER150 mass density than the UMaer-3mA model. Mass density is still 10–30% less than AER150, but not 20–40% less as was UMaer-3mA. In the lower stratosphere and up to 25 km in the tropics, the aerosol mass density is greater than in AER150 and up to 10% greater than with UMaer-3mA. Narrowing the large mode of the 3-mode



Fig. 10. Percent change in model-calculated annual average aerosol parameters from the AER 2-D model using the UMaer 4-mode aerosol module UMaer-4m versus the 150-bin sectional aerosol module AER150. Shown are annual average differences in (a) mass density, (b) surface area density, (c) effective radius, and (d) number density of particles with radius greater than 0.05 μ m.

model improved the simulation of mass density in the middle stratosphere but made the results somewhat worse in the lower stratosphere and tropics. The same is true for surface area density, where in addition the tropospheric values became somewhat worse. Effective radius, however, is improved in the entire stratosphere, but not in the troposphere. Calculated number density is improved in most of the troposphere but becomes worse in the tropical stratosphere.

The same comparisons for the 4-mode model are shown in Fig. 10. The maximum difference between UMaer-4m and AER150 is only 20% in aerosol mass density or surface area density below 30 km. Large differences above that altitude are not significant in terms of stratospheric aerosol mass, but reflect differences in how the models simulate evaporation of aerosols at the top of the aerosol layer. Overall, the simulation of effective radius is quite good between 5 and 30 km. Number density simulations are also improved over the 3-mode models, with only 10% differences in the stratosphere below 25 km, but with differences of 10–40% in the lower and middle troposphere.

Table 2 gives the global aerosol burdens of the six simulations discussed, along with tropospheric and stratospheric burdens. The AER150 model predicts 165 kilotons of aerosol sulfur in the troposphere and 138 kilotons of sulfur in the stratosphere. The AER40 and AER20 models predicts 1% less in the troposphere and 6% less in the stratosphere. The modal models all predict 162 kilotons of sulfur in the troposphere, but stratospheric burdens range from 130 to 146 kilotons. The UMaer-4m model predicts 141 kilotons of sulfur in the stratosphere, only 2% higher than the AER150 model. The UMaer-3mA model predicts 6% low and the UMaer-3mB model 6% high. Table 2 also shows a breakdown in stratospheric aerosol between that above and below 25 km. The AER150 model produces a stratospheric aerosol mass distribution with 16% above 25 km. The AER40, UMaer-3mB and UMaer-4m models have 15% of the stratospheric sulfate aerosol above 25 km, the AER20 model only 13%, and the UMaer-3mA only 12%. Though the global aerosol mass in the UMaer-4m model is closer to the AER150 model than is AER40, the AER40 model has smaller deviations

Model version	Global burden	Trop burden	Strat burden	Strat <25 km	Strat >25 km
AER150	303	165	138	116	22
AER40	294	164	130	110	20
AER20	283	163	130	113	17
UMaer-3mA	292	162	130	114	16
UMaer-3mB	308	162	146	124	22
UMaer-4m	303	162	141	120	21

Table 2. Aerosol burdens in kilotons of sulfur calculated by each model version.

from AER150 at most latitudes and altitudes (see Figs. 4 and 10) in mass, surface area density, effective radius, and number density. We find that a 4-mode model in general does a better job than a 3-mode model, but in some situations a 3-mode model simulates the size distributions better. The low resolution sectional model AER20 generally does a worse job than UMaer-4m and UMaer-3mB in our background atmosphere simulations, though its differences from AER150 are more consistent spatially.

5 Volcanic perturbation intercomparison

We have simulated the Mt. Pinatubo volcanic eruption in the Phillipines in order to compare the different model formulations under very high aerosol loading and to compare the rates of aerosol decay. Our simulations are performed by injecting 20 megatons of SO₂ (Bluth et al., 1992; McCormick et al., 1995) on 14 June 1991 into the tropical stratosphere between 5°S and 15° N at 16–29 km altitude (Read et al., 1993). The simulations cover the 8 year period from the beginning of 1991 until the end of 1998. Simulations are performed with the AER40 model, the AER20 model, and the UMaer-3mA, UMaer-3mB, and UMaer-4m models. The AER40 model is used here as the benchmark model, since running the AER150 model for 8 years is not practical. Observations of aerosol extinction and surface area density derived from the SAGE II satellite are available during the growth and decay of Pinatubo aerosols, though the tropical lower stratosphere experienced instrument saturation in the early months and observatons there are lacking.

Figure 11 shows model results of the evolution of $1.02 \,\mu\text{m}$ extinction from 1991 until 1999, as well as the SAGE II version 6.1 extinction observations. All models yield similar peak extinction values 2–3 months after the eruption in the tropics. This similarity is not unexpected, as the chemical transformation of SO₂ to H₂SO₄ is independent of the microphysical scheme, and thermodynamics dictate that all gas phase H₂SO₄ in the lower and middle stratosphere will condense into particles, though the condensation rate depends somewhat on the existing particle size distribution. Between 1992 and 1996, the AER40, AER20, UMaer-3mB, and UMaer-4m models match observations adequately



Fig. 11. Aerosol extinction at $1.02 \,\mu\text{m}$ in km⁻¹ for 1991 to 1999 at (a) the equator and 26 km, and (b) 55° N and 20 km. SAGE II data version 6.1 are shown by black symbols with error bars, model results by colored lines.

at the equator and 26 km. The UMaer-3mA model results are much too low between 1992 and 1996, a results of the excessive width of the largest mode which leads to excess sedimentation. The two sectional models and UMaer-4m match each other closely, with UMaer-3mB yielding somewhat lower values of extinction between 1992 and 1996. The



Fig. 12. Aerosol surface area density in $\mu m^2/cm^3$ for 1991 to 1999 at (a) the equator and 26 km, and (b) 55° N and 20 km. SAGE II data version 6.1 are shown by black symbols with error bars, model results by colored lines.

UMaer-3mB model matches observations best in late 1992 and early 1993, but AER40, AER20, and UMaer-4m match more closely between mid-1993 and 1997. After 1997, the modal model results are higher than the sectional model results and the observations. Results at 55° N and 20 km are also shown in Fig. 11. The SAGE II observations have larger error bars here, and the models show larger differences due to the transport time from the tropics and the differences in sedimentation and size evolution during this period. Peak extinction in early to mid 1992 differs among the models, with the UMaer-3mA model reaching only 1/3 the maximum of the AER40 model. We find that the UMaer-3mA model matches observations most closely in 1992, and UMaer-3mB matches most closely in 1994 and 1995. The sectional models are significantly higher than observations in these years, perhaps due to a poor representation of the initial SO₂ distribution from the eruption or to inadequacies in the model transport.



Fig. 13. Aerosol effective radius in μ m for 1991 to 1999 at (a) the equator and 26 km, and (b) 55° N and 20 km from simulations with the AER40, AER20, UMaer-3mA, UMaer-3mB, and UMaer-4m models.

The evolution of modeled aerosol surface area density at the equator and 26 km and at 55° N and 20 km is shown in Fig. 12. Surface area density derived from SAGE II version 6.1 extinction observations, as described in Thomason and Peter (2006), is also shown. Surface area density appears less sensitive to model formulation than extinction or mass density, with all models except UMaer-3mA showing almost coincident results which match observations well between 1992 and 1994 at the equator and 26 km. After 1995, the sectional models calculate lower surface area densities than do any of the UMaer models. At 55° N and 20 km, UMaer-3mA results lie significantly below those of the other models and match the observations most closely during 1992 and 1993, while UMaer-4m produces the highest reslts, sometimes well above observations. The AER20 model produces the lowest surface area density after 1995, though error bars in the observations eliminate only the UMaer-3mB and UMaer-4m models. We have not found a single model version which best match observations at all latitudes, altitudes, and times,



Fig. 14. Calculated size distributions from simulations of the Mt. Pinatubo eruption using the AER 2-D model with the 40-bin sectional aerosol module AER40 (red lines), the UMaer-3mA module (blue lines), the UMaer-3mB module (green lines) and the UMaer-4m module (cyan lines) at (a) the equator and 26 km in January 1992, (b) the equator and 26 km in January 1994, (c) 55° N and 20 km in January 1994, and (d) 55° N and 20 km in January 1994.

illustrating that uncertainties in model dynamics may dwarf the accuracy of the microphysics scheme.

The time evolution of aerosol effective radius is shown in Fig. 13. This parameter is sensitive to the full particle size spectrum, unlike extinction and surface area density which depend mostly on the larger particles which contain the majority of the aerosol mass. The effect of a large increase in gas phase sulfur in the stratosphere is to produce a burst of nucleation, seen here as a drop in effective radius at the time of the eruption, and then to increase particle sizes over several months, from about $0.15 \,\mu\text{m}$ to about $0.45 \,\mu\text{m}$, as the vast majority of sulfur condenses onto existing particles and increases their diameters. As shown in Fig. 14, the AER40 model calculates a narrower size distribution than the modal models in the post-Pinatubo period. The modal models have aerosol mass mainly in the largest mode whose width is specified and wider than that calculated by AER40. The AER40 size distributions are not symmetrical in January 1992 or January 1994, peaking at $0.4-0.5 \,\mu\text{m}$ and dropping faster on the high radius side than on the low radius side. The modal models generate far more particles below $0.1 \,\mu\text{m}$ radius, and thus produce a smaller effective radius. Distributions from the AER20 model are very similar to but slightly wider than AER40 and are not shown in the figure. Effective radius at the equator and 26 km is up to 40% low in UMaer-3mA relative to AER40 in 1994 and 1995, and falls back to background levels 2 years sooner than AER40. UMaer-3mB does a somewhat better jobs than UMaer-3mA but still calculates much lower effective radii and an earlier return to background conditions. The UMaer-4m model does a better job of simulating effective radius, but is still 17% low in 1994. The AER20 model simulates effective radius quite accurately between 1992 and 1996, much better than any of the modal models.

The rate at which the particulate matter is removed from the stratosphere is a function of sedimentation rate, which depends on the amount of aerosol mass in larger particles. Thus the different microphysical schemes calculate somewhat different rates of aerosol decay following this simulated volcanic injection. Models UMaer-3mA and UMaer-3mB differ only in the width of the largest lognormal mode, and show aerosol decay at very different rates, confirming the what faster than for AER40, but the UMaer-3mA model decays much too fast. The UMaer-4m model gives decay rates close to the AER40 model for the 1992–1995 period. The AER20 low-resolution sectional model also performs well during the post-Pinatubo period, and calculates effective radius much better than any of the modal models. This highlights the deficiency of a modal model, which forces sedimentation of all mass in an aerosol mode at the same rate.

6 Conclusions

We have performed global 2-D model calculations with three versions of a sectional model and three versions of a modal model. The sectional model with 40 bins has numerical diffusion compared to the sectional model with 150 bins, resulting in somewhat greater sedimentation and 6% less stratospheric aerosol mass, with maximum differences of 15% at 30 km. We tested two three-mode model versions and found a 12% difference between them in stratospheric aerosol mass as a function of the prescribed width of the largest lognormal mode. Differences in aerosol mass between these models and the 150-bin sectional model are as high as 40% at 30 km. A four-mode version was found to perform better than the three-mode version under some, but not all, conditions. A low-resolution sectional model with 20 bins was found to be very efficient but roughly comparable in accuracy to the UMaer-3mB model for a background atmosphere calculation. Effective radius was more sensitive to model formulation than mass density or surface area density.

Our 8-year calculations of the Pinatubo eruption period have been compared with SAGE-II observations of aerosol extinction at $1.02 \,\mu$ m and show that the UMaer-3mA version indeed has sedimentation which removes aerosol mass too quickly. The AER40, AER20, UMaer-3mB and UMaer-4m versions are all generally consistent with observations between 1992 and 1996, but the sectional models better match observations after 1996 when background aerosol levels are approached. We have not found a single model version which best match observations at all latitudes, altitudes, and times, indicating the importance of other model uncertainties. Calculated effective radius shows the clearest distinction between model versions during the 1992–1996 period, and the AER20 model is found to match the more accurate AER40 model quite well for this quantity.

Based on the model performances documented here and the computational efficiency, we recommend that the AER40 and UMaer-3mB model versions should be incorporated into the GMI stratosphere-troposphere chemistry-transport model. In addition, the low-resolution AER20 sectional model could be useful for certain applicatons. Developing a modal model which can prognostically determine mode width would likely be more efficient computationally and at least as accurate as a 4-mode scheme without this feature.

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References

- Bekki, S. and Pyle, J. A.: 2-D assessment of the impact of aircraft sulphur emissions on the stratospheric sulphate aerosol layer, J. Geophys. Res., 97, 15 839–15 847, 1992.
- Bluth, G. J. S., Doiron, S. D., Schnetzler, C. C., Krueger, A. J., and Walter, L. S.: Global tracking of the SO₂ clouds from the June 1991 Mount Pinatubo eruptions, Geophys. Res. Lett., 19, 151–154, 1992.
- Carslaw, K. S., Luo, B., and Peter, Th.: An analytic expression for the composition of aqueous HNO₃-H₂SO₄ stratospheric aerosol including gas phase removal of HNO₃, Geophys. Res., Lett., 22, 1877–1880, 1995.
- Considine, D. B., Douglass, A. R., Connell, P. S., Kinnison, D. E., and Rotman, D. A.: A polar stratospheric cloud parameterization for the three-dimensional model of the global modeling initiative and its response to stratospheric aircraft emissions, J. Geophys. Res., 105, 3955–3975, 2000.
- Douglass, A. R., Prather, M. J., Hall, T. M., Strahan, S. E., Rasch, P. J., Sparling, L. C., Coy, L., and Rodriguez, J. M.: Choosing meteorological input for the global modeling initiative assessment of high-speed aircraft, J. Geophys. Res., 104, 27545–27564, 1999.
- Douglass, A. R., Connell, P. S., Stolarski, R. S., and Strahan, S. E.: Radicals and reservoirs in the GMI chemistry and transport model: comparison to measurements, J. Geophys. Res., 109, D16302, doi:10.1029/2004JD004632, 2004.
- Fahey, D. W., Kawa, S. R., Woodbridge, E. L., et al.: In situ measurements constraining the role of sulphate aerosols in midlatitude ozone depletion, Nature, 363, 509–514, 1993.
- Fleming, E. L., Jackman, C. H., Stolarski, R. S., and Considine, D. B., Simulation of stratospheric tracers using an improved empirically-based two-dimensional model transport formulation, J. Geophys. Res., 104, 23 911–23 934, 1999.
- Hall, T. M., Waugh, D. W., Boering, K. A., and Plumb, R. A.: Evaluation of transport in stratospheric models, J. Geophys. Res., 104, 18815–18839, 1999.
- Hansen, D., Sato, M., Nazarenko, L., et al.: Climate forcings in the Goddard Institute for Space Studies SI2000 simulations, J. Geophys. Res., 107, D17, 4347, doi:10.1029/2001JD001143, 2002.
- Haywood, J. and Ramaswamy, V.: Global sensitivity studies of the direct radiative forcing due to anthropogenic sulphate and black carbon aerosols, J. Geophys. Res., 103, 6043–6058, 1998.
- Herzog M., Weisenstein, D. K., and Penner, J. E.: A dynamic aerosol module for global chemical transport models: Model description, J. Geophys. Res., 109, D18202, doi:10.1029/2003JD004405, 2004.
- Hofmann, D. J. and Solomon, S.: Ozone destruction through heterogeneous chemistry following the eruption of El Chichon, J. Geophys. Res., 94, 5029–5041, 1989.

- Jackman, C. H., Douglass, A. R., Brueske, K. F., and Klein, S. A.: The influence of dynamics on two-dimensional model results: Simulations of ¹⁴C and stratospheric aircraft NO_x injections, J. Geophys. Res., 96, 22 559–22 572, 1991.
- Jacobson, M. Z.: Global direct radiative forcing due to multicomponent anthropogenic and natural aerosols, J. Geophys. Res., 106, 1551–1568, 2001.
- Kalnay, E., Kanamitsu, M., Kistler, R., et al.: The NCEP/NCAR 40year reanalysis project, Bull. Am. Meteorol. Soc., 77, 437–471, 1996.
- Kinnison, D. E., Connell, P. S., Rodriguez, J. M., et al.: The Global Modeling Initiative assessment model: Application to high-speed civil transport perturbation, J. Geophys. Res., 106, 1693–1711, 2001.
- Labitzke, K. and McCormick, M. P.: Stratospheric temperature increases due to Pinatubo aerosols, Geophys. Res. Lett., 19, 207– 210, 1992.
- Liu X., Penner, J. E., and Herzog, M.: Global modeling of aerosol dynamics: Model description, evaluation, and interactions between sulfate and nonsulfate aerosols, J. Geophys. Res., 110, D18206, doi:10.1029/2004JD005674, 2005.
- McCormick, M. P., Thomason, L. W., and Trepte, C. R.: Atmospheric effects of the Mt. Pinatubo eruption, Nature, 373, 399– 404, 1995.
- Mills, M. J., Toon, O. B., Solomon, S. S.: A two-dimensional microphysical model of the polar stratospheric CN layer, Geophys. Res. Lett., 26, 1133–1136, 1999.
- Newell, R. E., Kidson, J. W., Vincent, D. G., and Boer, G. J.: The General Circulations of the Tropical Atmosphere, vol. 2, MIT Press, Cambridge, Mass., 1974.
- Penner, J. E., Andreae, M., Annegarn, H., et al.: Aerosols: Their direct and indirect effects, in: Climate Change 2001: The Scientific Basis, edited by: Houghton, H. T., Ding, Y., Griggs, D. J., et al., pp. 289–348, Cambridge Univ. Press, New York, 2001.
- Penner, J. E., Zhang, S. Y., Chin, M., et al.: A comparison of model and satellite-derived aerosol optical depth and reflectivity, J. Atmos. Sci., 59, 441–460, 2002.
- Pitari, G., Mancini, E., Rizi, V., and Shindell, D. T.: Impact of future climate and emission changes on stratospheric aerosols and ozone, J. Atmos. Sci., 59, 414–440, 2002.
- Randel, W. J. and Garcia, R. R.: Application of a planetary wave breaking parameterization to straospheric circulation statistics, J. Atmos. Sci., 51, 1157–1168, 1994.
- Read, W. G., Froidevaux, L., and Waters, J. W.: Microwave limb sounder measurements of stratospheric SO₂ from the Mt. Pinatubo volcano, Geophys. Res. Lett., 20, 1299–1302, 1993.
- Rosenfield, J. E., Newman, P. A., and Schoeberl, M. R.: Computation of diabatic descent in the stratospheric polar vortex, J. Geophys. Res., 99, 16 677–16 689, 1994.
- Rotman, D. A., Tannahill, J. R., Kinnison, D. E., et al.: The Global Modeling Initiative Assessment Model: Model description, integration and testing of the transport shell, J. Geophys. Res., 106, 1669–1691, 2001.
- Sander, S. P., Friedl, R. R., DeMore, W. B., et al.: Chemical kinetics and photochemical data for use in stratospheric modeling, Supplement to evaluation 12: Update of key reactions, Evaluation Number 13, JPL Publication 00-3, Jet Propulsion Laboratory, NASA, 2000.

- Seinfeld, J. H. and Pandis, S. N.: Atmospheric Chemsitry and Physics, John Wiley, Hoboken, N.J., 1997.
- Smolarkiewicz, P. K.: A simple positive definite advection scheme with small implicit diffusion, Mon. Wea. Rev., 111, 479–487, 1984.
- Stier, P., Feichter, J., Kinne, S., et al.: The aerosol-climate model ECHAM5-HAM, Atmos. Chem. Phys., 5, 1125–1156, 2005, http://www.atmos-chem-phys.net/5/1125/2005/.
- Strahan, S. E. and Douglass, A. R.: Evaluating the credibility of transport processes in simulations of ozone recovery using the Global Modeling Initiative three-dimensional model, J. Geophys. Res., 109, D05110, doi:10.1029/2003JD004238, 2004.
- Tabazadeh, A., Toon, O. B., Clegg, S. L., and Hamill, P.: A new parameterization of H₂SO₄/H₂O aerosol composition: Atmospheric implications, Geophys. Res., Lett., 24, 1931–1934, 1997.
- Thomason, L. and Peter, Th. (Eds.): SPARC Assessment of Stratospheric Aerosol Properties, WCRP-124, WMO/TD NO. 1295, SPARC Report No. 4, Toronto, Canada, 2006.
- Timmreck, C.: Three-dimensional simulation of stratospheric background aerosol: First results of a multiannual general circulation model simulation, J. Geophys. Res., 106, 28 313–28 332, 2001.
- Vehkamäki, H., Kulmala, M., Napari, I., Lehtinen, K. E. J., Timmreck, C., Noppel, M., and Laaksonen, A.: An improved parameterization for sulfuric acid-water nucleation rates for tropospheric and stratospheric conditions, J. Geophys. Res., 107(D22), 4622, doi:10.1029/2002JD002184, 2002.
- Weisenstein, D. K., Yue, G. K., Ko, M. K. W., Sze, N. D., Rodriguez, J. M., and Scott, C. J.: A two-dimensional model of sulfur species and aerosol, J. Geophys. Res., 102, 13019–13035, 1997.
- Weisenstein, D. K., Ko, M. K. W., Dyominov, I. G., Pitari, G., Ricciardulli, L., Visconti, G., and Bekki, S.: The effects of sulfur emissions from HSCT aircraft: A 2-D model intercomparison, J. Geophys. Res., 103, 1527–1547, 1998.
- Wennberg, P. O., Cohen, R. C., Stimpfle, R. M., et al.: Removal of stratospheric O₃ by radicals: In situ measurements of OH, HO₂, NO, NO₂, ClO, and BrO, Science, 266, 398–404, 1994.
- Wilson, J., Cuvelier, C., and Raes, F.: A modeling study of global mixed aerosol fields, J. Geophys. Res., 106, 34081–34108, 2001.
- Wright, D. L., Kasibhatla, P. S., McGraw, R., and Schwartz, S. E.: Description and evaluation of a six-moment aerosol microphysical module for use in atmospheric chemical transport models, J. Geophys. Res., 106, 20275–20291, 2001.
- WMO: Scientific Assessment of Ozone Depletion: 1991, World Meteorological Organization Global Ozone Research and Monitoring Project Report No. 25, Geneva, 1992.
- Zhang, Y., Pun, B., Vijayaraghavan, K., Wu, S.-Y., Seigneur, C., Pandis, S. N., Jacobson, M. Z., Nenes, A., and Seinfeld, J. H.: Development and application of the model of aerosol dynamics, reaction, ionization, and dissolution (MADRID), J. Geophys. Res., 109, D01202, doi:10.1029/2003JD003501, 2004.