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The adsorption enthalpy of nitrogen oxides on crystalline ice

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Abstract. The partitioning of nitrogen oxides between ice and air is important to the ozone budget in the upper troposphere. In the present study, the adsorption of nitrogen oxides on ice was investigated at atmospheric pressure using a chromatographic technique with low concentrations of radioactively labelled nitrogen oxides. The measured retentions solely depended on molecular adsorption and were not influenced by dimerisation, formation of encapsulated hydrates on the ice surface, dissociation of the acids, nor by migration into a quasi-liquid layer or grain boundaries. Based on the chromatographic retention and the model of thermochromatography, the adsorption enthalpies of -20 kJ mol^{-1} for NO, -22 kJ mol^{-1} for NO₂, -30 kJ mol^{-1} for peroxyacetyl nitrate, -32 kJ mol^{-1} for HONO and -44 kJ mol^{-1} for HNO3 were calculated. To assess the adsorption enthalpies, standard adsorption entropies were calculated based on statistical thermodynamics. In this work, the use of two different standard states was demonstrated. Consequently different values of the standard adsorption entropy, of either between $-39 \,\mathrm{J}\,(\mathrm{K}\,\mathrm{mol})^{-1}$ and $-45 \,\mathrm{J}\,(\mathrm{K}\,\mathrm{mol})^{-1}$, or $-164 \,\mathrm{J}\,(\mathrm{K}\,\mathrm{mol})^{-1}$ and $-169 \,\mathrm{J}\,(\mathrm{K}\,\mathrm{mol})^{-1}$ for each nitrogen oxide were deduced. The adsorption enthalpy derived from the measurements, was independent of the choice of standard state. A brief outlook on environmental implications of our findings indicates that adsorption on ice might be an important removal process of HNO₃. In addition, it might be of some importance for HONO and peroxyacetyl nitrate and irrelevant for NO and NO2.

1 Introduction

In the early 70's Crutzen (1970) stressed that nitrogen oxides play a critical role in the atmospheric ozone budget, e.g. in the upper troposphere where an increase in the NO_x con-

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centration leads to higher ozone levels (Jaeglé et al., 1998). Therefore, detailed knowledge of the sources and sinks of nitrogen oxides in the atmosphere is of paramount importance in the understanding of the observed increase of ozone in the free troposphere (Wang et al., 1993) and to model the future composition of the atmosphere. Ice surfaces, which are one of the main condensed substrates in the upper troposphere and lower stratosphere (Winkler and Trepte, 1998; Heymsfield and Sabin, 1998), may be a powerful sink for NO_v. During the SUCCESS campaign, Weinheimer et al. (1998) measured 10% to 20% of the gas-phase NO_v concentration in wave-cloud ice particles. Yet, for whatever uptake process of gas species on ice surfaces, the first step is adsorption on the surface. This study aims to evaluate the thermodynamics of adsorption for the reactive nitrogen species NO and NO₂ and the reservoir species HONO, HNO₃ and peroxyacetyl nitrate (PAN) on ice surfaces. The thermodynamics of adsorption are rarely discussed in literature, as many of the previous studies have focused on uptake kinetics. To our knowledge, only few studies on NO, HONO and HNO₃ adsorption enthalpies on ice have been published (Sommerfeld et al., 1992; Rieley et al., 1996; Thibert and Dominé, 1998; Tabazadeh et al., 1999; Chu et al., 2000). We introduce here a method to simultaneously evaluate the adsorption properties of several NO_v species in synthetic air on ice surfaces. The method combines the advantage of high sensitivity of a radioactive tracer technique with a chromatographic approach, thus enabled us to measure at atmospheric pressure and with a surface coverage of a fraction of a formal mono layer. Briefly, radioactively labelled nitrogen oxides in a flow of air or N₂ are fed to a chromatographic column packed with ice spheres. A negative temperature gradient along the column leads to an increasing retention of each species as they are transported in the column. After the experiment, their migration distance in the column is determined by measuring the distribution of radioactivity along the column. If the model of mobile adsorption is applied, the adsorption en-

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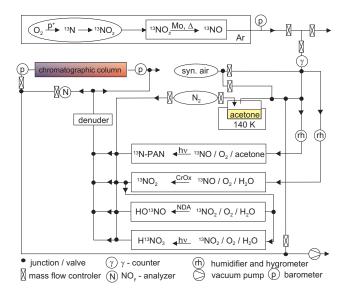


Fig. 1. Experimental set-up: gas target to produce ¹³N, photolysis cells to oxidize the nitrogen oxides and chromatographic column.

thalpy can be calculated. Eichler et al. (2000, 1995) have shown the feasibility of this approach to derive the adsorption enthalpy of NO_y on different surfaces and of radon on ice surfaces in previous studies. We will show here that the migration of the nitrogen oxides through the column is neither influenced by dimerisation, migration into a quasi-liquid layer or the grain boundaries, formation of encapsulated hydrates, nor by dissociation of the acids.

2 Experimental

2.1 Gas phase synthesis

Figure 1 shows the experimental set-up, which consists of the production of the radioactive nitrogen isotope ^{13}N ($t_{1/2} =$ 10 min), the synthesis of various NO_v species in designated reaction chambers, and the evaluation of their adsorption properties in the chromatographic apparatus. Details of the ¹³N-production at Paul Scherrer Institute's Philips Cyclotron and the gas phase synthesis of ¹³NO₂, HO¹³NO and H¹³NO₃ are described in detail elsewhere (Ammann, 2001). Briefly, a proton beam (1 μ A, 11.1 MeV) irradiated a 5 cm³ s⁻¹ flow of 20% O2 (99.9995%, Carbagas AG) in He (99.9999%, Carbagas AG). This ${}^{16}{\rm O}({\rm p},\alpha)^{\bar{13}}{\rm N}$ reaction formed various oxidized ¹³N-species inside the gas target, which were reduced to ¹³NO by passing them over a molybdenum foil at 300 - 500°C. A 80 m long polyethylene tube (2 mm in diameter) delivered the gas flow to the laboratory. This complete system was placed in a protective argon atmosphere (99.999% Carbagas AG) to prevent diffusion of impurities into the gas flow. In the laboratory, the gas flow passed a γ counter to constantly evaluate the input of ¹³N. Afterwards a fraction of the gas flow was diluted with N2 (99.9995%, Carbagas AG) or synthetic air and fed to the experiments and a chemiluminescence NO analyzer (CLD, Germany). A molybdenum converter for reduction of NO_v to NO was attached to the chemiluminescence analyzer to measure impurities of ¹⁴NO_y, which come from irradiation of traces of ¹⁴N₂ in the He- and O₂-gas by the proton beam. All tubing in the laboratory was kept at room temperature and consisted of perfluoro-alkoxy copolymer (PFA) 4 mm i.d. without any protective gas surrounding them. The diffusion of impurities into the gas flow through PFA, as well as losses and memory effects of the various nitrogen oxides through the column walls are minimal compared to Teflon or polyethylene tubing (Neuman et al., 1999). The experiments were done at atmospheric pressure, and gas flows were controlled by mass flow controllers (Brooks Instruments, The Netherlands) with 1% full scale accuracy.

¹³NO₂ was synthesized by passing the ¹³NO over CrO₃ on firebrick support at 30% relative humidity. HO¹³NO was synthesized by passing the ¹³NO₂ through a filter impregnated with 100 µl of 1% N-(1-naphthyl)ethylenediamine dihydrochloride (NDA) in methanol-water (10/90) at 30% relative humidity. H¹³NO₃ was produced by photolysis of a $^{13}NO_2/H_2O/O_2$ mixture in N_2 at 172 nm. $^{13}N - PAN$ was produced through photolysis of acetone at 253 nm in the presence of ¹³NO and O₂ (Warneck and Zerbach, 1992). The acetone was dosed to the gas phase by passing a gentle flow of air over solid acetone at 140 K. This saturated gas flow was further diluted prior to entering the photolysis cell. It is very important to work with low acetone concentrations, as in experiments with higher acetone concentrations, the acetone condensed on the ice and column walls, trapping the $^{13}N - PAN$, and consequently hindering its migration. This condensation, which is visible with the naked eyes, was not observed in the experiments described here with the low acetone concentration.

Most syntheses produced a mixture of several 13 NO_y which, when fed to a column, yielded the adsorption properties of several 13 NO_y species simultaneously. To carry out experiments with only one 13 NO_y species in the gas phase, a series of selective gas traps were used to scrub all but one species from the gas phase, where possible. The traps, which were designed as cylindrical denuders, were coated with Na₂CO₃ for absorbing HONO or PAN, a mixture of NDA and KOH ($^{1/1}$) for NO₂, NaCl for HNO₃ and Co₂O₃ for NO (see Kalberer et al., 1996, 1999, for details). Those denuders, in combination with γ -detectors and the chemiluminescence NO_y analyzer, were also used to identify and quantify the various 13 NO_y species (Ammann, 2001). In addition, PAN was identified in the gas flow with a GC-ECD (Schrimpf et al., 1995).

2.2 Ice preparation and characterization

Deionized water was purified with a Millipore Milli-Q water system to a resistivity $< 0.054 \,\mu\text{S cm}^{-1}$ and degassed in an ultra-sonic bath. Small droplets, 0.3 - 0.7 mm in diameter, were rapidly frozen in liquid nitrogen. The surface area of the ice spheres was evaluated based on the weight of 100 droplets and an ice density of $0.85 \,\mathrm{g \, cm^{-3}}$. This low ice density was chosen to account for any air inclosure during the rapid freezing. The spheres were annealed in air for at least 12 h at 258 K in a cold room to allow them to crystallize. To prepare a column, the ice spheres were sieved with calibrated sieves (Retsch, Germany) with a grain size of $400 \,\mu m$ and $630 \,\mu\text{m}$. The spheres were filled in quartz, Teflon or PFA tubes, which were sealed at each end and stored at 258 K. From the mass of the ice filling and the surface area per gram, the surface area per centimeter of the column was calculated, which varied between 4 and 10.9 cm² cm⁻¹ for the different experiments. During transport to the laboratory, the ice columns were cooled to 190 K with solid CO2. Additionally, a BET methane adsorption isotherm of the ice spheres was measured (Legagneux et al., 2002). In brief, approximately 66 g of the ice spheres, between 400 μ m and 500 μ m in diameter, were put in a sample holder in the cold room at 253 K. The sample holder was placed in a cooled dewar, connected to the instrument in the laboratory at room temperature and immediately immersed in liquid nitrogen. The sample holder was then evacuated and subsequently dosed with methane at relative pressures between 0.007 and 0.22 to derive the adsorption isotherm. The relative pressure is equal to p_i/p^{sat} where p_i [Pa] is the absolute pressure and p^{sat} [Pa] is the saturation pressure. The free volume of the filled sample holder was measured with He prior to the measurement.

2.3 Thermo-chromatography

The main feature of thermo-chromatography is a negative temperature gradient along the packed ice chromatography column. The apparatus is set up to maintain a stable and negative temperature gradient as shown in Fig. 2. It consists of a copper tube (10 mm i.d.), the two ends of which were kept at different temperatures. One end, from which the gas flow exits the apparatus, was immersed in liquid nitrogen. The other end was cooled to a variable temperature between 218 K and 250 K with a cryostat. We used a Haake Phoenix P2-C50P thermostat or a Julabo FP88 with pure ethanol (Merck, 99%) as cooling liquid. The cooling liquid was pumped through a copper tubing (8 mm i.d.), which was wound around the warmer end of the central copper tube bearing the ice column. The temperature at any position in the column was stable (\pm 1 K) after 1 h of operation. Prior to each experiment the temperature gradient was measured with a Pt-100 thermo element (MTS, Switzerland) in an empty column. The temperature gradient measurement in an empty column and a packed column showed good agreement. Depending

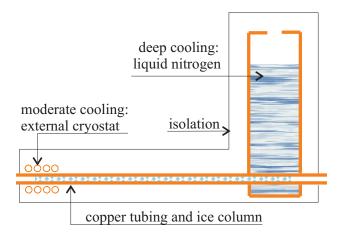


Fig. 2. Thermo-chromatography apparatus to maintain a negative temperature gradient along the column.

on the temperature at the column entrance and the length of the copper tube, a temperature gradient between $-4\,\mathrm{K\,cm^{-1}}$ and $-8\,\mathrm{K\,cm^{-1}}$ was measured. A typical temperature profile in the column is shown in Fig. 5. It is characterized by a flat temperature gradient at the beginning and at the end of the tube and by a steep gradient in the center part of the column. Only the slope of the central gradient, which is linear with a regression coefficient above 0.99, was considered in our analysis. This is justified by the strong temperature dependence of the partition coefficient. For the error analysis, the slope of the temperature gradient was deduced only a few centimeters in front of a peak (see Sect. 3.3). Both gradients differed typically by 0.5 K cm⁻¹.

To start an experiment the packed columns were placed in the temperature gradient. First, the carrier gas passed through the column for 30 min. to allow the temperature equilibrium to be reached at any place in the ice column. Then, a small gas flow containing the ¹³N-nitrogen oxides was added to the carrier gas. The concentration of nitrogen oxides was varied between 3 ppb and 47 ppb. The flow through the column was controlled with a mass flow controller at the column exit and varied between $75 \,\mathrm{cm}^3 \,\mathrm{min}^{-1}$ and $360 \,\mathrm{cm}^3 \,\mathrm{min}^{-1}$. After a variable time of 14, 30 or 31 min the experiment was stopped. The column was sealed and immersed in an open bath of liquid nitrogen to stop any further migration of nitrogen oxides in the column. The distribution of the ¹³N-nitrogen oxides in the column was measured, usually exhibiting distinct, symmetric peaks for each NO_v species. The migration distance, or more precisely, the temperature at this position (denoted as deposition temperature) is the primary observable of the experiment.

2.4 Detection

To deduce the distribution of nitrogen oxides along the column, a coincident γ -counter scanned each column three

times. The coincident γ -counter consisted of two Bismuth-Germanate-detectors, 3 cm in diameter, mounted face to face with a gap of 35 mm. Coincident γ -counting leads to optimum counting efficiency and low background counting rates (less than 1 cts s⁻¹), because each decay of ¹³N results in two γ -rays in opposite directions to each other. The activity in the column was calculated based on the measured coincident counts and the radioactive decay after the experiment.

To determine the optimum step size of the detectors, the resolution and absolute efficiency of the system, a column was spiked with point- and broader sources of a $^{18}F^-$ solution of known activity and scanned. The optimum step size turned out to be 0.5 cm, which yielded an accuracy in detection of the peak maximum position of ≤ 0.5 cm. The resolution of this arrangement was 3 cm, which led to a broadening of the peak base width to 4-6 cm of a point source of ≤ 0.5 cm in diameter. The absolute detector efficiency, which is defined as number of observed coincident counts per decay within 1 cm, was 0.0134. The efficiency of 0.0134 resulted in a detection limit of 1×10^5 molecules ^{13}N , or 8×10^{-14} mol of total NO_V ($^{13}N+^{14}N$) per centimeter column length.

2.5 Derivation of the adsorption enthalpy

The adsorption enthalpy was calculated based on the experimentally determined migration distance and the theory of thermo-chromatography (Eichler and Zvára, 1982). This theory is based on the model of linear chromatography, which requires reversibility of the partition equilibria in the column. This reversibility has been demonstrated by Eichler et al. (1995) by simulating the experimentally observed deposition zone of NO₂ by means of a Monte Carlo simulation exclusively based on a reversible equilibrium. A brief outline of the calculations, which were done with the Maple 6.0 software (Waterloo Maple), is given below. The detailed formulas and notations are given in the Appendix.

The model of linear chromatography (Eq. 1) describes the position of each species in the column, z [cm], as function of the time, t [min], the linear gas velocity, u [cm min⁻¹] and the partition function, k_i [–].

$$\frac{\mathrm{d}z}{\mathrm{d}t} = \frac{u}{1+k_i} \tag{1}$$

Substituting k_i with its thermodynamic definition and applying several simplifications (see Appendix B), Eq. (2) is obtained. It gives a relation between known experimental factors: t_e (experimental time), g (temperature gradient), u_0 (linear gas velocity at standard temperature), T_D (deposition temperature), T_S (starting temperature of gradient), v (open volume in the column), a (ice surface area in column) and the thermodynamic functions $\Delta H_{\rm ads}$ (adsorption enthalpy), $\Delta S_{\rm ads}^0$ (standard adsorption entropy), T_0 (standard temperature), V/A (standard volume to standard surface area), R

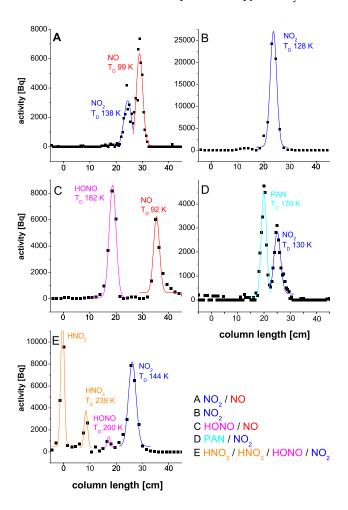


Fig. 3. Distribution of different nitrogen oxide species in columns packed with ice spheres at different experimental settings. Zero column length denotes the beginning of the ice spheres in the column. The activity is a measure for the concentration of NO_y species along the column. The lines are Gaussian peak fits to our data by Origin 6.1. They are a help to visualize the results more easily. The spontaneous signals visible at the column entrance in chromatogram D are due to detector noise, and their decreasing relative contribution derives from the calculation of the activity based on the observed counts.

(gas constant).

$$\left(t_{e} + \frac{T_{0}}{g \cdot u_{0}} \cdot \ln \frac{T_{D}}{T_{S}}\right) \cdot \frac{v \cdot g \cdot u_{0}}{a \cdot T_{0} \cdot \frac{V}{A} \cdot \exp\left(\frac{\Delta S_{\text{ads}}^{0}}{R}\right)}$$

$$= \int_{T_{S}}^{T_{D}} \frac{1}{T} \cdot \exp\left(\frac{-\Delta H_{\text{ads}}}{RT}\right) \tag{2}$$

For each set of experimental parameters, ΔH_{ads} was calculated by means of an iteration process with a given ΔS_{ads}^0 . ΔS_{ads}^0 was calculated based on statistical thermodynamics and the model of mobile adsorption using Eq. (3) with h (Planck constant), k_B (Boltzmann constant), N_A (Loschmidt's number), m (molar mass) and ν (vibrating fre-

quency) of the adsorbed species on the surface (see Appendix D). This frequency was assumed to be identical to the phonon frequency of ice. As to our knowledge no experimental data about the phonon frequency ν of the solid state of water at temperatures of our experiment exist, a rounded value of $3 \times 10^{13} \, \mathrm{s}^{-1}$ based on the relations of Madelung and Einstein, Lindemann and Debye and data in Hobbs (1974, p. 388) was used (Eichler et al., 2000).

$$\Delta S_{\text{ads}}^{0} = R \left[ln \left[\frac{A}{V} \sqrt{\frac{N_{\text{A}} h^{2}}{2 \pi m k_{\text{B}} T_{\text{D}}}} \right] - 0.5 \right]$$

$$+ R \left[\frac{h \nu}{k_{\text{B}} T_{\text{D}} \left(e^{\frac{h \nu}{k_{\text{B}} T_{\text{D}}}} - 1 \right)} \right]$$
(3)

3 Results and discussion

Figure 3 shows the chromatograms of various nitrogen oxides at low ppb concentrations in ice columns at different experimental settings. Chromatogram A results from exposure of the ice column to NO₂ (peak at 24 cm) and NO (29 cm), B from exposure NO₂ (24 cm) with some traces of HONO (13 cm), C from HONO (18 cm) and NO (35 cm), D from PAN (20 cm) and NO₂ (25 cm), and E from HNO₃ (0 cm and 8 cm), HONO (18 cm) and NO₂ (26 cm). It can be clearly seen that each nitrogen oxide species is uniquely retarded in the ice column leading to well defined chromatographic peaks, even if several species are fed to the column simultaneously. The surface concentration of NO_v was always at least one order of magnitude below a mono layer even after accumulation for 30 min. For example, a typical experiment with 4 ppb of NO₂ and HONO at a flow rate of 95 ml min⁻¹ yielded a surface coverage of 1% of a formal mono layer for each nitrogen oxide at the end of an experiment. The experimental time of this run was 30 min, the surface area per centimeter in the column was 10.9 cm² cm⁻¹ and the deposition temperature was 139 K and 184 K, respectively. Peak base widths of 2 cm for the NO₂ and 1 cm for the HONO peak and a formal mono layer of 1×10^{15} molecules cm² were assumed. Even at concentrations of 47 ppb NO_v, surface coverage did not exceed 13% of a formal mono layer at a flow rate of $27 \,\mathrm{ml}\,\mathrm{min}^{-1}$. Hence, condensation was very unlikely in the column. In addition, a concentration dependence of the migration distance between 3 ppb and 47 ppb NO_v in the gas phase was not observed, as expected for condensational processes.

3.1 Mechanistic considerations of the uptake at experimental conditions

To evaluate chromatographic experiments, it is absolutely mandatory to know which processes occur in the column and

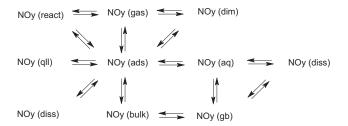


Fig. 4. Overview of equilibria of nitrogen oxides in the gas and ice phase, such as dimerisation (dim), e.g. $NO_2 \rightleftharpoons N_2O_4$; adsorption (ads); reaction (react), e.g. $NO_2 + NO \rightleftharpoons N_2O_3$; solvation into the quasi-liquid layer (qll), bulk or grain boundaries (gb); formation of encapsulated hydrates (aq); and dissociation (diss), e.g. of HNO_2 and HNO_3 .

determine the retention behavior. The mechanistical aspects of uptake on ice are still under some debate (see Girardet and Toubin, 2001, for a detailed overview). Several possible mechanisms that can be advanced to describe the processes in the chromatographic column are summarized in Fig. 4. As the experimental set-up used in this work can not address the elementary processes in the column, in the following, published data were used to evaluate which process might determine the retention. The importance of such analysis has been shown by Huthwelker et al. (2001), who reanalyzed data of Lamb and Clapsaddle (1989) and Conklin et al. (1993). In this reanalysis the authors found, in contrast to the original publications, that the retention of SO₂ in these experiments on adsorption on ice was not due to adsorption, but to diffusion into the grain system of the polycrystalline ice.

The first question is, whether NO_2 is dimerized, as it tends to at low temperatures, or reacted with NO to form N_2O_3 either in the gas phase or on the surface. For the following discussion, it was assumed that the adsorption equilibrium constant describes the partitioning of NO_2 in the column, and a typical gas phase concentration of 3 ppb NO_2 and flow rate of 5 cm³ s⁻¹ were chosen. The concentration of NO_2 first increases due to the temperature decrease at constant pressure up to its maximum value of about 1.3×10^{11} molecules cm⁻³ at 140 K, before it decreases rapidly due to the increasing residence time on the surface. Under these conditions (Atkinson et al., 1999), the extrapolated apparent first order forward rate constant for formation of N_2O_4 in the gas phase (Eq. 4) constantly increases from 5×10^{-2} s⁻¹ at 250 K to 1.4×10^{-1} s⁻¹ at 140 K and decreases again to 10^{-2} s⁻¹ at 120 K.

$$2 \operatorname{NO}_{2}(gas) \rightleftharpoons \operatorname{N}_{2}\operatorname{O}_{4}(gas) \tag{4}$$

Obviously, the formation of N_2O_4 is much slower than the transport of NO_2 in the carrier gas flow, which is almost constant at $0.02\,\mathrm{s}$ per cm column length from the column entrance to a position in the column at $140\,\mathrm{K}$. Thus, under the non-steady-state conditions of this chromatographic system the dimerisation is very unlikely.

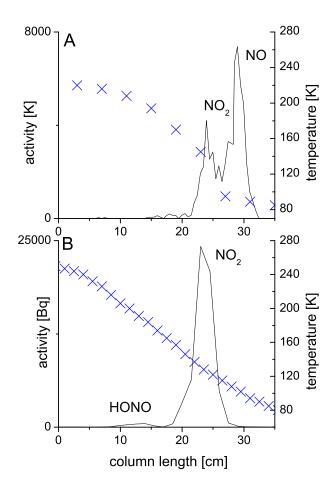


Fig. 5. Comparison of two chromatograms with different experimental conditions. The activity is given on the left axis (solid line) and the temperature along the column at the right axis (crosses). In experiment A the temperature was always too low for a quasi-liquid layer to form, whereas in chromatogram B a quasi liquid layer might have evolved. Note that the two NO_2 peaks should be compared; the NO in experiment A was added on purpose, without any relation to this comparison.

Dimerisation on the surface can be ruled out under the chosen experimental conditions, based on the symmetry of the chromatographic peaks. A NO_2 -dimer should have stronger adsorption energies compared to NO_2 on the ice surface. Thus dimerisation of NO_2 on the surface would result in a fronting of the chromatographic peaks. From the absence of such fronting (see Fig. 3), we conclude that the nitrogen oxides did not dimerize on the surface, nor react to N_2O_3 . And from the calculations above, we conclude that NO_2 did not dimerize in the gas phase and thus the adsorption properties of NO_2 -monomers were investigated.

Secondly, which are the processes that determined the retention of the nitrogen oxides in the column? For HNO_3 , HONO and PAN, the retention of which is increased at temperatures above $160 \, \text{K}$, a metastable, molecular adsorbed state of these adsorbates on the ice surface $(NO_v(ads))$

is assumed. Such a molecular adsorbed state has been proposed for HCl by Svanberg et al. (2000) based on molecular dynamics simulations. In a subsequent step, the adsorbates may form encapsulated hydrates (NO_v (aq)) within the outermost water bilayer (Delzeit et al., 1997), which in the case of the acids facilitates dissociation (Packer and Clary, 1995). Recent molecular dynamic simulations by Bolton and Pettersson (2000) confirmed that the ice surface is highly dynamic at temperatures above 180 K and indicated that water molecules rapidly exchange between the upper surface layers. The time scale of water molecule exchange is in the order of ns, and thus much faster than the species' residence time on the surface, which is in the order of ms. Hence, we presume that in our experiments not the hydrate formation and dissociation, but the adsorption equilibrium of the molecular species is rate limiting the transport of HNO₃, HONO and PAN through the column. The dissociation of acids on ice surfaces, the products of which have been experimentally observed for HNO₃ by Zondlo et al. (1997), may also rapidly and reversibly occur directly on the surface (Svanberg et al., 2000; Clary and Wang, 1997), and thus again not contribute to the retention of HNO3 and HONO in the column.

In contrast, we assume that NO and NO₂ are exposed to a rather rigid ice surface, as their retention is only enhanced at temperatures below 140 K, and consequently both are not encapsulated by water molecules. Indeed, Uras et al. found molecular HCl at low coverage at 125 K (1998) and showed in a monte carlo simulation that at 110 K, NH₃ stays on the ice surface at low coverage and only builds a hydrate capsule within a surface bilayer at high coverage (Uras et al., 2000).

A quasi-liquid layer has been observed at ice surfaces above −24 °C (Bluhm and Salmeron, 1999; Döppenschmidt et al., 1998), and has been used to explain an increased uptake at temperatures approaching the melting point of chemically different species such as NO (Sommerfeld et al., 1992), HNO₃ (Diehl et al., 1998) and SO₂ (Lamb and Clapsaddle, 1989). Although in some of the experiments presented here the nitrogen oxides were exposed to ice at temperatures above -24° C at the column entrance, the retention is not influenced by diffusion in the quasi-liquid layer. This is illustrated in Fig. 5, which shows two chromatograms under different experimental conditions. Similar migration distances of NO₂ were recorded, even when the column entrance was kept at a temperature too low for a quasi-liquid layer to evolve (Fig. 5a). Obviously, the equilibrium NO_v (ads) \rightleftharpoons NO_v (qll) shifts so rapidly that the rate limiting factor for transport of the species along the column remains the adsorption equilibrium NO_y (gas) $\rightleftharpoons NO_y$ (ads). The very small fraction taken up into the quasi-liquid layer, which has not been detected within the relatively short duration of the experiments, did not affect the retention of the molecules. Nevertheless, uptake into the quasi-liquid layer might influence the long-term fate of these species.

For polycrystalline ice, as used here, an increased uptake

Table 1. Adsorption enthalpy , ΔH_{ads} [kJ mol $^{-1}$], and standard adsorption entropies, ΔS_{ads}^0 [J/(K mol)], of various NO $_y$ species. Random errors, σ [kJ mol $^{-1}$]; number of measurements (in brackets) and the systematic error, δ_{sys} [kJ mol $^{-1}$], of ΔH_{ads} are given as well. For calculation of ΔS_{ads}^{01} a value of 1 cm $^{-1}$ for A/V was used and for ΔS_{ads}^{02} , A was set to 6.7×10^{10} cm 2 and V to 2.2×10^4 cm 3

	ΔH_{ads}	σ	$\delta_{ m sys}$	ΔS_{ads}^{01}	ΔS_{ads}^{02}	σ
HNO ₃	-44	2.3 (4)	13	-168	-44	0.1
HONO	-32	1.7 (9)	10	-166	-42	0.1
PAN	-30	1.2 (7)	7	-169	-45	0.5
NO_2	-22	1.0(21)	6	-165	-39	0.1
NO	-20	2.6 (7)	5	-164	-40	0.2

at warmer temperatures has been explained by diffusion into the grain boundaries (Huthwelker et al., 2001). In addition, strong acids are known to accumulate in the grain boundaries, as Mulvaney et al. (1988) has shown for H₂SO₄. This diffusive process is driven by a strong concentration gradient, and as equilibrium is only reached after hours (Mader, 1992), any nitrogen oxide that diffuses into the grain boundaries is trapped in the vein system, at least for the duration of the experiment and thus does not contribute to the peak formation. Furthermore, we note that the surface of the polycrystalline spheres not only consisted of crystalline facies but also of grain boundaries, so that the adsorption enthalpy derived represents an average over all facies, defect sites and grain boundaries exposed at the surface.

In conclusion, we suggest that the retention of each individual nitrogen oxide solely depends on molecular adsorption processes and thus the theory of thermo-chromatography can be applied to our results. We want to state that our current adsorption model does not include changes of the ice surface that are induced by the adsorbate such as restructuring of the ice lattice or vibrational changes (Delzeit et al., 1996).

3.2 Standard states

Table 1 shows the adsorption enthalpy of the nitrogen oxides examined. To determine the adsorption enthalpy based on the experimental findings, the standard adsorption entropy was calculated. The standard adsorption entropy calculations were done with two different standard states, which both resulted, as expected, in the same adsorption enthalpy. Recall, that the enthalpy does not depend on the choice of standard states (Carmichael, 1976). There have been two standard states applied for this work, because for adsorption processes there is no general agreement on the choice of a standard state as for pure gas phase processes. In the literature, two different approaches are usually considered. Eichler and Zvára (1982) arbitrarily set the ratio of A/V to the value 1 cm⁻¹. The advantage of this standard state is its

Table 2. Assessment of the absolute systematic error, δ_{sys} [kJ mol⁻¹]. The table lists the modification of a number of input values and the resulting change in ΔH_{ads} for each nitrogen oxide

	NO	NO_2	HONO	HNO ₃	PAN
$t_e \pm 1 \text{ min}$	0.1	0.0	0.1	0.1	0.1
$u_0 \pm 20 \text{ cm}^3 \text{ s}^{-1}$	0.1	0.3	0.3	0.1	0.3
$g \pm 0.5 K$	0.1	0.1	0.1	0.2	0.1
$v \pm 300 \%$	1.4	1.8	1.9	2.8	1.9
$a \pm 300 \%$	1.1	1.6	5.2	2.2	5.2
$T_S + 30 K$	0.0	0.0	0.1	3.0	0.0
$T_D \pm 10 K$	1.8	2.7	2.5	4.2	2.8
$m + 1 g mol^{-1}$	0.0	0.0	0.0	0.0	0.0

independence of temperature, particle size, and absolute values of V or A. Goss (1997) used a standard state introduced by de Boer (1968), treated the adsorbed species as a two dimensional gas and defined the standard state of that "gas" as a state where the average distance of two molecules is identical to the average distance of two molecules in a three dimensional gas phase at standard pressure and temperature. The two dimensional gas law with a two dimensional pressure f [N m⁻¹] was used to calculate a standard surface area of 6.7×10^{10} cm² (A) in analogy to the standard volume of the gas phase of 2.2×10^4 cm³ (V).

Note that the equilibrium constant K_p depends on the chosen standard state as well. Equation (5) gives the relation to transfer one into the other, where a/v is the actual surface to volume ratio in the experimental set-up; see Appendix B for further information.

$$\frac{a}{v} \cdot \frac{2.2 \times 10^4}{6.7 \times 10^{10}} \cdot K_p^{01} = \frac{a}{v} \cdot 1 \cdot K_p^{02}$$
 (5)

3.3 Error calculation

Typically, the resulting ΔH_{ads} of several experiments showed a standard deviation of about 1% to 3% distributed about the mean. From the experimental set-up presented above, it is evident that systematic errors are the main source of uncertainty. To assess this error, calculations based on one particular experiment have been repeated with all factors changed one by one to their possibly largest extent of uncertainty (Table 2). The resulting total difference in ΔH_{ads} to the mean value, which varies between 23% and 33%, is given in Table 1 as the total error. These total errors are similar to published uncertainties of experiments on adsorption in flow tubes (Fenter et al., 1996).

It can be clearly seen in Table 2 that the most critical input values are those relying on the determination of the deposition temperature and the ice surface (open volume and surface area). The error in the determination of the deposition temperature results mainly from installing the column manu-

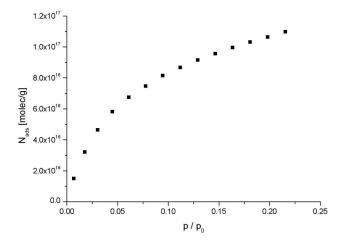


Fig. 6. Methane adsorption isotherm of ice spheres uses in this study.

ally onto the scanner and the resulting inaccuracy of the zero point alignment. Furthermore, the temperature measurement itself might include some error.

The surface areas calculated based on the weight of 100 droplets agreed well with the determination of the radius by sieving. BET measurements of the ice were done to evaluate whether the surface area that is available to adsorption, is of the same size as the geometric surface area. The geometric surface area is the area of a sphere with the same volume as the ice spheres used in our work. In the literature, a discrepancy of up to 8 times larger BET surface area per gram sample compared to the external surface area assessed via ESEM pictures has been observed for ice condensed from the vapor phase (Keyser and Leu, 1993). Figure 6 shows a plot of the methane adsorption isotherm of 66.3 g ice spheres, which where between 400 and 500 μ m in diameter. The ice spheres were produced in the same way as the spheres used in the chromatographic experiments. The BET surface area of $0.0186 \,\mathrm{m^2 g^{-1}}$ compares perfectly well with the geometric surface area between 0.0121 and 0.0188 m²g⁻¹. The geometric surface areas were calculated considering a radius of 400 microns and a density of 0.8 and 500 microns and a density of 0.99, respectively. Thus we conclude, that the ice spheres' surface area is not enlarged due to pores or additional microstructures on the surface, and the geometric surface area was used for calculations. Any defects that might have evolved due to the fast freezing of the ice, have probably vanished during the crystallization process at 258 K, or do not influence the adsorption properties of the ice surface. Nevertheless, a high error of 300% was introduced to account for the numerous unknowns such as bulk density of the produced ice, packing density of the column and the accuracy of the method to determine the weight of 100 droplets.

4 Discussion of the adsorption enthalpy

Both NO and NO₂ migrate to a temperature of below 140 K in the column and consequently small adsorption enthalpies of $-20 \,\mathrm{kJ} \,\mathrm{mol}^{-1}$ and $-22 \,\mathrm{kJ} \,\mathrm{mol}^{-1}$ are derived. In agreement with the experiments presented here, Saastad et al. (1993) did not detect any loss of NO in the gas phase above ice frozen from the liquid at temperatures down to 193 K. In contrast, Sommerfeld et al. (1992) found an adsorption enthalpy of -11 kJ mol^{-1} by measuring adsorption isotherms in packed columns down to 200 K using a chromatographic fronting technique. This discrepancy however might be due to the different experimental method and, as Sommerfeld et al. mentioned, a large uncertainty in their measured loss of NO to the ice, as the loss was small compared to the huge background loss of NO on the apparatus' walls. The results of NO₂ adsorption on ice again agree well with findings of Saastad et al. (1993), as in both cases NO₂ did not measurably adsorb on ice at temperatures down to 193 K. Rieley et al. (1996) measured a desorption enthalpy for N₂O₄ on ice of 39 kJ mol⁻¹, which is higher than the enthalpy of NO₂ presented here due to expected stronger binding interactions.

The adsorption of HONO on the ice surface begins to slow down the migration process at temperatures below 170 K, which qualitatively agrees well with a reversible adsorption of HONO at temperatures of 180-200 K published by Fenter and Rossi (1996). In addition, the HONO adsorption enthalpy of -32 kJ mol⁻¹ is in excellent agreement with an adsorption enthalpy of -33.8 kJ mol⁻¹ reported by Chu et al. (2000).

In all HNO₃ experiments in this work, two peaks evolved (see Fig. 3e). The first peak is assigned to an irreversible inclosure of HNO3 in the water rime. The riming was only observed in the experiments with HNO₃ because we had to work at higher relative humidity to generate HNO₃ from the reaction of NO2 with OH on-line. The deposition temperatures of the second peak, which were below 245 K, were taken to evaluate the HNO₃ adsorption enthalpy of $-44\,\mathrm{kJ}\,\mathrm{mol}^{-1}$. Tabazadeh et al. (1999) published a free enthalpy (ΔG) of $-59.4 \text{ kJ mol}^{-1}$ for HNO₃ adsorption and dissociation on ice based on experiments by Abbatt (1997). An adsorption enthalpy or entropy has not been published by the authors. If we expect the entropy to be negative due to the reduced degrees of freedom of the adsorbed state compared to the gas phase molecule, the enthalpy should be \leq -60 kJ mol⁻¹. This value agrees well with the sublimation enthalpy of HNO3 on ice measured by Thibert and Dominé (1998) of 68 kJ mol^{-1} . Both values are as expected more negative than our findings, as they describe enthalpy of both, adsorption and solvation.

The adsorption enthalpy of PAN on ice was determined to be $-30 \,\mathrm{kJ} \,\mathrm{mol}^{-1}$. To our knowledge the adsorption properties of PAN have been investigated for the first time.

The magnitude of the adsorption enthalpies for nitrogen oxides found point to the formation of one to two hydrogen

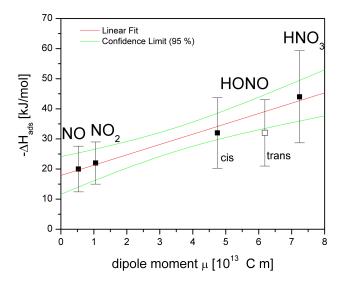


Fig. 7. Correlation of dipole moment (Lide, 2001-2002) and the experimentally found adsorption enthalpy for NO, NO₂, HONO and HNO₃.

bonds. The strength of a hydrogen bond depends on the capability of an ice surface to act as hydrogen bond donor and the dipole moment of the nitrogen oxide. The capability of the crystalline ice used in this study to form hydrogen bonds, which is determined by the number of free OH groups on the surface, should be sufficient for the coverage of nitrogen oxides below a mono layer in this work. First of all, FTIRAS measurements indicated a free OH coverage on crystalline ice to be approximately one-sixth of that on amorphous ice (Schaff and Roberts, 1996). And secondly, even after annealing at 258 K the polycrystalline character of the ice spheres used in our work, whose grain boundaries might posses free OH groups, is preserved. Finally, despite the annealing, surface defects facilitating free OH groups might be present on the surface. Assuming that hydrogen bonding is relevant for adsorption of nitrogen oxides on ice, the overall bond strength of the molecules to the surface should scale with the dipole moment. Figure 7 shows a correlation of dipole moments and the adsorption enthalpy determined in this study.

5 Atmospheric implications

Table 3 shows the partitioning of nitrogen oxides between ice and air at temperature and surface to volume ratios present in the environment. To calculate the partitioning coefficient (see Eq. A1) at environmental conditions, the standard Gibbs adsorption energy (ΔG_{ads}^0) was calculated at the temperature of interest based on the adsorption enthalpy and standard adsorption entropy from this study (see Eq. A4). The standard Gibbs adsorption enthalpy was in the following transferred to the partitioning coefficient using the actual surface to vol-

Table 3. Partitioning coefficient, k_i , of nitrogen oxides between ice and air under different atmospheric conditions. Note that the displayed partitioning coefficients describe the equilibrium of the gaseous and molecular adsorbed species. Any secondary equilibrium, such as dissociation, is not included in these calculations. See text for further explanation and references

	temperature	ice area	k _i	
	[K]	$[\mathrm{cm}^2\mathrm{cm}^{-3}]$	[-]	
		contrails		
NO	213	1×10^{-2}	2×10^{-6}	
NO ₂	213	1×10^{-2}	6×10^{-6}	
HONO	213	1×10^{-2}	2×10^{-3}	
PAN	213	1×10^{-2}	3×10^{-4}	
HNO ₃	213	1×10^{-2}	1	
	cirrus clouds			
		2		
NO	213	3×10^{-3}	7×10^{-7}	
NO_2	213	3×10^{-3}	2×10^{-6}	
HONO	213	3×10^{-3}	5×10^{-4}	
PAN	213	3×10^{-3}	1×10^{-4}	
HNO_3	213	3×10^{-3}	3×10^{-1}	
	snow pack (polar zone)			
			3	
NO	246	20	1×10^{-3}	
NO ₂	246	20	3×10^{-3}	
HONO	246	20	3×10^{-1}	
PAN	246	20	8×10^{-2}	
HNO_3	246	20	$9 \times 10^{+1}$	
	snow pack (temperate zone)			
NO	268	70	2×10^{-3}	
NO_2	268	70 70	3×10^{-3}	
HONO	268	70 70	3×10^{-1}	
PAN	268	70	7×10^{-2}	
HNO ₃	268	70	$4 \times 10^{+1}$	
	200	, ,	7/10	

ume ratio in the environment and the chosen standard state of the entropy calculation (see Eq. A3).

To illustrate the possible influence of adsorption of nitrogen oxides on the gas phase concentrations of NO_x (see Fig.4), these back-of-the-envelope calculations were performed with a wide range of environmental conditions. Namely, a high concentration of ice particles of up to $200\,\mathrm{cm}^{-3}$ typically found in contrails (Schröder et al., 2000), a huge surface area of freshly fallen snow in the arctic and temperate zone (Dominé et al., 2001) or the cold temperatures in the upper troposphere and the typical surface to volume ratio in the clouds (Schröder et al., 2000) were taken.

For a detailed description additional factors, such as gas phase and ice diffusion, or additional equilibria following the adsorption have to be included in a more precise model calculation, which is beyond the scope of this work. Nevertheless this basic estimation shows that HNO₃ significantly partitions to the ice phase where ice is abundant, whereas NO and NO₂ do not at all. HONO and PAN might not partition to the ice phase in clouds, but are expected to do so in the snow pack. As the partition coefficient strongly changes with temperature (e.g. for HONO $k_i \approx 1$ at 230 K and $k_i \approx 3 \times 10^{-1}$ at 250 K in an arctic environment) emission from or deposition to the snow pack may be expected after strong temperature changes. Be aware that these calculations might underestimate the total uptake on ice, as they do not account for additional processes, which follow the adsorption process and thus continuously shift the adsorption equilibrium.

6 Conclusions

The retention of nitrogen oxides fed to a chromatographic column filled with ice spheres in synthetic air or nitrogen was investigated at atmospheric pressure and submonolayer coverage. It was argued that the retention was exclusively determined by the equilibrium between a gas phase and a molecularly adsorbed species and not influenced by dimerisation, formation of an encapsulated hydrate on the ice surface, dissociation of the acids, nor by migration into a quasi-liquid layer or grain boundaries.

Based on the migration distance of each nitrogen oxide in the column, the enthalpy for molecular adsorption of $-20 \,\mathrm{kJ}\,\mathrm{mol}^{-1}$ for NO, $-22 \,\mathrm{kJ}\,\mathrm{mol}^{-1}$ for NO₂, $-30 \,\mathrm{kJ}\,\mathrm{mol}^{-1}$ for peroxyacetyl nitrate, $-32 \,\mathrm{kJ}\,\mathrm{mol}^{-1}$ for HONO and $-44 \,\mathrm{kJ}\,\mathrm{mol}^{-1}$ for HNO₃ was calculated. To perform these calculations, a standard state had to be chosen. The adsorption enthalpy values derived proved to be independent of that choice, and is thus an ideal value for comparison of adsorption energies with other groups. An error analysis revealed the actual surface area of the ice as major source of systematic uncertainty of the adsorption enthalpy calculations. Nevertheless, the total error associated with the reported adsorption enthalpy is less than 33%.

A brief outlook on environmental implications of our findings for exemplary conditions in contrails, cirrus clouds, as well as arctic and temperate zone snow packs indicated that adsorption on ice might be an important removal process of HNO₃, of some importance for HONO and peroxyacetyl nitrate and irrelevant for NO and NO₂.

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Appendix A: Notation

Symbol	Explanation	Unit		
S	entropy	$J(K \text{ mol}^{-1})$		
H	enthalpy	$J(K \text{ mol}^{-1})$		
U	inner energy	$J(K \text{ mol}^{-1})$		
U(0)	zero inner energy	$J(K \text{ mol}^{-1})$		
q	molecular partition	_		
	function			
Q	molar partition func-	_		
	tion			
T	temperature	K		
$T_{ m D}$	deposition tempera-	K		
	ture (temperature at			
	the position of the			
	peak)			
и	linear gas velocity	${\rm cmmin^{-1}}$		
u_0	linear gas velocity at	${\rm cmmin^{-1}}$		
	standard temperature			
a	surface area	cm^2		
v	volume	cm^3		
p	pressure	$ m Nm^{-2}$		
f	two dimensional	${ m Nm^{-1}}$		
	pressure			
\boldsymbol{A}	standard surface area	cm^2		
V	standard volume	cm^3		
p^0	standard pressure	$1 \times 10^5 \mathrm{N}\mathrm{m}^{-2}$		
f^0	standard two dimen-	$3.38 \times 10^{-2} \text{ N m}^{-1}$		
	sional pressure			
M	molecular mass	kg		
m	molar mass	$kg mol^{-1}$		
n	number of molecules	_		
ν	vibrating frequency	s^{-1}		
	- ,			
$N_{ m A}$	Loschmidt's number	$6.02285 \times 10^{23} \text{ mol}^{-1}$		
k_{B}	Boltzmann constant	$1.38066 \times 10^{-23} \mathrm{JK^{-1}}$		
h	Planck constant	$6.62618 \times 10^{-34} \mathrm{J}\mathrm{s}$		
R	gas constant	$8.31441 \text{ J (K mol)}^{-1}$		

Appendix B: Partitioning coefficient, adsorption equilibrium constant and standard states

At low concentrations the partitioning of each species in the chromatographic column, or in any two phase system, can be described by the partition coefficient (Eq. A1), which gives a relation of the total number of adsorbed and gaseous species.

$$k_i = \frac{n^{\text{ads}}}{n^{\text{gas}}} \left[- \right] \tag{A1}$$

This partition can be described by the adsorption equilibrium constant, which accounts for the influence of the actual surface to volume ratio on the column (Eq. A2).

$$K_{c} = \frac{n^{\text{ads}}/a}{n^{\text{gas}}/v} \text{ [cm]}$$

$$= k_{i} \cdot \frac{v}{a} \text{ [cm]}$$
(A2)

To perform thermodynamical calculations, the adsorption equilibrium constant (K_c) has to be transferred into the dimensionless standard equilibrium constant (K_p) , as can be seen in Eq. (A3).

$$K_{p} = \frac{f/f^{0}}{p/p^{0}} [-]$$

$$= \frac{n^{\text{ads}}/a \cdot RT \cdot p^{0}}{n^{\text{gas}}/v \cdot RT \cdot f^{0}} [-]$$

$$= k_{i} \cdot \frac{v}{a} \cdot \frac{A}{V} [-]$$
(A3)

The advantage of the standard adsorption equilibrium constant (K_p) is, that it can be expressed in terms of the standard adsorption entropy and adsorption enthalpy (Eq. A4), which both can be regarded as independent of temperature.

$$-RT \ln K_{\rm p} = \Delta H_{\rm ads} - T \ \Delta S_{\rm ads}^{0} \tag{A4}$$

Appendix C: The transport model and enthalpy calculations

The calculation of the adsorption enthalpy within the model of thermo-chromatography has been described by Eichler and Zvára (1982) in great detail. The transport of a species along the chromatographic column at low concentrations is given by Eq. (A5).

$$\frac{\mathrm{d}z}{\mathrm{d}t} = \frac{u}{1+ki} \tag{A5}$$

If a linear temperature gradient along the column (Eq. A6) is given,

$$T = T_{\rm S} - g \cdot z,\tag{A6}$$

Eq. (A5) yields

$$t = -\frac{1}{g} \int_{T_S}^{T_D} \frac{1 + \frac{a}{v} \cdot \frac{V}{A} K_p(T)}{u(T)} dT.$$
 (A7)

Neglecting the change in gas pressure along the column, we have

$$u(T) = \frac{u_0 \cdot T}{T_0} \ [cm \ s^{-1}]. \tag{A8}$$

Assuming that ΔH_{ads} and ΔS_{ads}^0 are independent of temperature, and substituting Eqs. (A3), (A4) and (A8) in Eq. (A7),

we obtain Eq. (A9), which can be solved by an iteration process, if ΔS_{ads}^0 is known.

$$\left(t + \frac{T_0}{g \cdot u_0} \cdot \ln \frac{T_D}{T_S}\right) \cdot \frac{v \cdot g \cdot u_0}{a \cdot T_0 \cdot \frac{V}{A} \cdot \exp\left(\frac{\Delta S_{\text{ads}}^0}{R}\right)}$$

$$= \int_{T_S}^{T_D} \frac{1}{T} \cdot \exp\left(\frac{-\Delta H_{\text{ads}}}{RT}\right) \tag{A9}$$

Appendix D: Entropy calculations

Statistical thermodynamics allow to very precisely calculate the absolute entropy based on the partition functions. In the following we will calculate the change in entropy during adsorption as the difference of the absolute entropy of a molecule in the gas phase and of the molecule in the adsorbed state (Eq. A10).

$$\Delta S_{\rm ads} = S_{\rm ads} - S_{\rm gas} \tag{A10}$$

Each entropy term can be calculated based on the molar partition function, Eq. (A11). Using Stirling's approximation and $R = k_{\rm B} \cdot N_{\rm A}$ the partition function can be written as the molecular partition function (Eq. A12) for the canonical ensemble (Eq. A13).

$$S = \frac{\{U - U(0)\}}{T} + k_{\rm B} \cdot \ln Q \tag{A11}$$

$$S = \frac{\{U - U(0)\}}{T} + nR \cdot \ln \{\ln q - \ln N_A + 1\}$$
 (A12)

$$Q = q^n / n! (A13)$$

The inner energy, U-U(0), can itself be calculated based on the partition functions (Eq. A14).

$$U - U(0) = -n \frac{\delta \ln q}{\delta kT}$$

$$= -n k_{\rm B} T^2 \frac{\delta \ln q}{\delta T}$$
(A14)

The partition function is simply calculated based on the molecule's translational (trans), rotational (rot), vibrational (vib) and electronical (el) degrees of freedom (Eq. A14).

$$q^{\text{tot}} = q^{\text{trans}} \cdot q^{\text{rot}} \cdot q^{\text{vib}} \cdot q^{\text{el}}$$
(A15)

The adsorbed state is defined by a large mobility of the adsorbed molecules on the surface and a vibrating mode perpendicular to the surface. The molecule only loses one translational degree of freedom and gains one vibrational degree of freedom during adsorption. As internal vibrations, rotations and the electronic configuration do not change and thus do not contribute to the adsorption entropy, we can calculate the partition function solely based on the translational and vibrational partition function. The translational partition function is calculated based on a particle-in-the-box as

$$q^{\text{trans}} = V \cdot \left(\frac{2\pi \, m \, k_{\text{B}} T}{h^2}\right)^{\frac{1}{2}} \tag{A16}$$

for the three dimensional state and as

$$q^{\text{trans}} = A \cdot \left(\frac{2\pi \, m \, k_{\text{B}} T}{h^2}\right) \tag{A17}$$

for the two dimensional (adsorbed) state. The vibrational partition function for one mode is given by

$$q^{\text{vib}} = \frac{e^{\frac{-h\nu}{2kT}}}{1 - e^{\frac{h\nu}{k_BT}}}.$$
(A18)

The vibrating frequency (ν) of the molecule in the adsorbed state is considered to be similar to the phonon frequency of ice. Since to our knowledge no experimental data about the vibrating frequency of the solid state of water exist at these temperatures, a rounded value of $3 \times 10^{13} \, \mathrm{s}^{-1}$ based on the relations of Madelung and Einstein, Lindemann and Debye and data in Hobbs (1974, p. 388) was used.

Using Eqs.(A14) and (A16) to calculate the contribution of the inner energy to the entropy yields

$$\frac{U - U(0)}{T} = \frac{3}{2} k_{\rm B} N_{\rm A} \tag{A19}$$

for the molecules in the gas phase. Similarly, for the adsorbed state based on Eqs. (A14), (A17) and (A18), we get

$$\frac{U - U(0)}{T} = k_{\rm B} N_{\rm A} + k_{\rm B} N_{\rm A} \cdot \frac{h \nu}{2 k_{\rm B} T} + \frac{N_{\rm A} k_{\rm B} \cdot h \nu}{k_{\rm B} T \cdot \left(e^{\frac{h \nu}{k_{\rm B} T}} - 1\right)}.$$
(A20)

Using Eqs. (A10), (A12), and (A16–A20), we finally get the standard adsorption entropy

$$\Delta S_{\text{ads}}^{0} = k_{\text{B}} N_{\text{A}} - \frac{3}{2} k_{\text{B}} N_{\text{A}} + k_{\text{B}} N_{\text{A}} \cdot \frac{h \nu}{2 k_{\text{B}} T} + \frac{N_{\text{A}} k_{\text{B}} \cdot h \nu}{k_{\text{B}} T \cdot \left(e^{\frac{h \nu}{k_{\text{B}} T}} - 1\right)} + N_{\text{A}} k_{\text{B}} \left[\ln \left(\frac{A}{V} \sqrt{\frac{N_{\text{A}} h^{2}}{2 \pi m k_{\text{B}} T}}\right) + \ln e^{-\frac{h \nu}{2 k_{\text{B}} T}} \right] - N_{\text{A}} k_{\text{B}} \ln \left(1 - e^{-\frac{h \nu}{k_{\text{B}} T}}\right)$$
(A21)

and with $\ln\left(1 - e^{-\frac{h\nu}{k_{\rm B}T}}\right)$ being approximately 0, Eq. (A21) finally yields Eq. (A22), which was used for calculations in this work.

$$\Delta S_{\text{ads}}^{0} = R \left[\ln \left[\frac{A}{V} \sqrt{\frac{N_{\text{A}} h^{2}}{2 \pi m k_{\text{B}} T_{\text{D}}}} \right] - 0.5 \right]$$

$$+ R \left[\frac{h \nu}{k_{\text{B}} T_{\text{D}} \left(e^{\frac{h \nu}{k_{\text{B}} T_{\text{D}}}} - 1 \right)} \right]$$
(A22)

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