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# A METHODOLOGY TO SEGMENT X-RAY TOMOGRAPHIC IMAGES OF MULTIPHASE POROUS MEDIA: APPLICATION TO BUILDING STONES.

by

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## ABSTRACT

An image analysis technique based on mathematical morphology tools dedicated to the segmentation of X-ray tomographic images of porous media is presented in this article. It consists in an efficient denoising using alternate sequential filters and a watershed operation using an original starting marker. The image is transformed into a mosaic that is straightforward to segment. An application to building stones of heritage monuments illustrates the potentialities of this technique.

## INTRODUCTION

Exposed to their climatic environment, the building stones of heritage monuments are often altered and eventually destroyed. This phenomenon called weathering is visible throughout the world and many studies in this field, led with architects and restorers, aimed at finding processes to slowing down, controlling or ultimately avoiding this decay (Amoroso and Fassina, 1983; Tiano *et al.*, 2006; Torraca, 1976). A way to achieve such a goal is to understand the weathering mechanisms of building stones, i.e. to relate the microscopic mechanisms occurring at the pore scale (dissolution of minerals, transport, precipitation, etc.) to their consequences at the macro-scale (desquamation, powdering, etc.) (Amoroso and Fassina, 1983; Camuffo, 1995; Trk, 2002). Some studies comparing weathered stones with unweathered stones were performed. The chemical and mineralogical composition, as well as the porosity were analysed (Rozenbaum *et al.*, 2007; Maravelaki-Kalaitzaki *et al.*, 2002; Galan *et al.*, 1999). The main processes of weathering were thus qualitatively inferred from the differences identified. However, a more quantitative understanding of these weathering mechanisms (fluid flow, dissolution, mass transport, crystallization) and their consequences is to simulate them via a computerized model. This requires in turn a quantitative, realistic description of the three dimensional structure of the porous medium (Dullien, 1992; Adler, 1992; Anguy *et al.*, 2001). Such a goal can be achieved with a promising and increasingly developing technique: X-ray tomography. Tomography designates the generic technique of constructing a 3-d image of a sample given several projections recorded at various angles (Kak and Slaney, 2001). It is a non-invasive method that enables the visualization of the inner structure of the stone. By using a X-ray light source, the resulting 3-d grey level image is a map of the X-ray absorption coefficient of the various phases constituting the sample. The synchrotron X-ray radiation source, compared to the more conventional X-ray tube, brings several crucial advantages such as beam stability, high flux, monochromaticity, high coherence and parallelism of the beam, that lead to high quality and high resolution images. It is a key technology enabling to measure accurately the inner structure of a

material.

However the segmentation of a raw tomographic image is seldom a trivial process, highly dependent on the starting image and the objects to extract from it. Segmentation is the process of partitioning billions of grey-level voxels of a 3-d image into distinct objects or phases. The goal, in the context of building stones, will be to separate the void phase (here actually filled with resin) from some distinct solid phases (two for the stone under study). Most of the segmentation complexity is related to the presence of noise (voxels with the same grey value can actually belong to two different phases) and blur (the borders between the phases are not well defined). Moreover, because the images are big and three-dimensional, the analysis cannot be done by hand (e.g. by marking the objects of interests) and must be as automated as possible. The main techniques found in the literature are:

- Thresholding the grey levels histogram, with (Kaestner *et al.*, 2006) or without (Appoloni *et al.*, 2007) a former filtering, with automatically (Sezgin and Sankur, 2004) or manually (Appoloni *et al.*, 2007) determined thresholds. The thresholded images sometimes have to undergo a binary post-treatment to adjust the results of these approaches. It is most of the time a reconstruction of the connected components of interest (du Roscoat *et al.*, 2005; Lambert *et al.*, 2005; Kaestner *et al.*, 2006; Erdogan *et al.*, 2006).
- Active contours on the image considered as a level set (Ramlau and Ring, 2007; Chung and kin Ho, 2000; Maksimovic *et al.*, 2000; Qatarneh *et al.*, 2001). These techniques are mostly used in medical applications and usually require a marking of the objects to be extracted.
- Watershed-based techniques (Videla *et al.*, 2007; Malcolm *et al.*, 2007; Benouali *et al.*, 2005; Carminati *et al.*, 2006).
- Combined techniques, e.g. (Sheppard *et al.*, 2004).

The segmentation step of the images of the stone under study, which falls in the third above category, is the subject of this contribution. It will be shown that the characteristics of these images lead toward a sophisticated de-noising technique based on a watershed mosaic-like operator (Beucher, 1990), using a carefully and automatically chosen marker. Following this introduction, section 2 presents the stone used in this study that serves as model stone, the sample preparation, and the images obtained on the ID-19 tomographic beamline at the ESRF (Grenoble, France). Section 3 details the image analysis procedure, based on mathematical morphology tools, used to segment the images. It also presents some preliminary results. Section 4 concludes this contribution.

## X-RAY MICRO-TOMOGRAPHY OF TUFFEAU SAMPLE

← insert Fig. 1

← insert Fig. 2

Most heritage monuments (châteaux, churches, cathedrals or houses) constituting the cultural heritage of the Loire valley, that is registered to the World Heritage list of the UNESCO (UNESCO, ???), are made with tuffeau, a highly porous limestone (porosity  $\approx 45\%$ ) originating from this valley. Previous studies (Dessandier, 1995; Brunet-Imbault, 1999; Rozenbaum *et al.*, 2007) showed that minerals are essentially sparitic (large grains) or micritic (small grains) calcite ( $\approx 50\%$ ), silica ( $\approx 45\%$ ) in the form of opal cristobalite-tridymite spheres and quartz crystals, and some secondary minerals such as clays and micas in much smaller proportion (a few %). The scanning electron microscopic (SEM) image in figure 1 illustrates the structural complexity of the main phases of tuffeau.

X-ray tomography (Kak and Slaney, 2001) is a choice technology to extract the structure of samples of various porous materials: rocks (Lindquist and Venkatarangan, 1999; Sheppard *et al.*, 2004; Appoloni *et al.*, 2007; Betson *et al.*, 2004; 2005; Videla *et al.*, 2007), cements and ceramics (Erdogan *et al.*, 2006; Maire *et al.*, 2007), soils (Gryze *et al.*, 2006; Carminati *et al.*, 2006) and others (Jones *et al.*, 2004; Mendoza *et al.*, 2007; du Roscoat *et al.*, 2005; Prodanović *et al.*, 2005). The objective is usually to characterize

the medium or to simulate some physical processes in a realistic geometry. Our ultimate objective pertains to both categories. The typical sizes of the structural components of tuffeau relevant to fluid flow, like micritic calcite grains (a few  $\mu\text{m}$  in size) and opal spheres (10 to 20  $\mu\text{m}$  in size), suggest the use of a high resolution tomograph, which leads toward synchrotron radiation facilities. However the smallest structures such as those related to the opal spheres roughness or phyllosilicates will not be accessible as their size is far below the best resolution any X-ray tomographic facility can achieve nowadays.

The microtomographic images presented in this study were collected at the ID-19 beamline of the ESRF (European Synchrotron Radiation Facility, Grenoble, France) (Salvo *et al.*, 2003; Baruchel *et al.*, 2006) at the smallest possible pixel size: 0.28  $\mu\text{m}$ . The energy used was 14.7 keV and 1500 successive rotations of the sample corresponding to 1500 angular positions ranging between 0 and 180 were acquired by the FReLoN camera with  $2048 \times 2048$  pixels image size. In order to stay in the field of view of the detector and avoid supplementary artifacts, the samples have to measure less than 700  $\mu\text{m}$  in diameter. They were prepared as cylindrical cores of that diameter and were mounted on a vertical rotator on a goniometric cradle. Preparation of a tuffeau sample of such a size requires particular care. Samples were impregnated with a resin in order to make a 700  $\mu\text{m}$  thin section. This latter was cut into matches of square section and finally trimmed to obtain quasi-cylinders of diameter  $\approx 700\mu\text{m}$ . Imaging time was approximately 45 minutes and the 2048 horizontal slices (0.28  $\mu\text{m}$  thick) were reconstructed from the projections with a dedicated filtered back-projection algorithm. The outputs of the tomographic process are then images of  $2048 \times 2048 \times 2048$  voxels with 256 level grey level values (one uncompressed image is then 8 GB in size). The grey level value of a voxel is linked to the X-ray absorption of the sample at the voxel position (Baruchel *et al.*, 2000). Thus, the pores appear in dark grey, the silica compounds in medium grey and the calcite compounds in light grey in figure 2. The different phases are easily distinguishable to the naked-eye and it is clear that the sample size is sufficient to catch the wide scale range of the different structural components. Calcite is present in the form of large irregular grains (sparitic calcite) or small grains that look like crumble (micritic calcite). Silica has

the form of large quartz crystals or small spheres of opal.

Hence it is not possible to rely on some shape or size criteria to identify the phases and only the grey level is relevant. The problem is although looking smooth naked eye, the images are in fact noisy as shown in figure 3-(a). This noise randomly affects the grey value of the voxels, preventing to label them solely from their grey values. In other words a mere threshold on such an image would yield a blatantly incorrect result. This noise effect is also visible on the image histogram: it is smoothed (see the histogram of the original image in figure 4). Theoretically, a perfect image of tuffeau (without noise) would contain only voxels with three precise grey values, one for each phase (resin, silica, calcite). Its histogram would then consist of only three peaks at these values. On the other hand, the voxel values of a noisy (i.e. real) image are randomly disrupted, given then intermediate values. The histogram is then smoothed and the peaks corresponding to the three phases are difficult to separate. Since it can only rely on the grey level to distinguish the phases, the segmentation technique will actually consist in an efficient denoising of the images: enough noise must be removed to identify the phases, without blurring which leads to losing the small structures of the images (e.g. micritic calcite). Some basic smoothing filters (e.g. a mean filter) have been found unable to fulfil both these requirements, hence the idea to turn towards morphological tools.

## IMAGES TREATMENT METHOD

The problematic is then to segment the images, i.e. to label each voxel as belonging to one of the three main phases: calcite, silica or resin. In order to achieve a quantitative and controlled segmentation, some assumptions will be made on the images and then, on this basis, a suitable segmentation approach will be proposed. It is a more reliable method than just do some trial-and-error until an acceptable, yet very subjective result emerges. The theoretical framework of the method presented in this paper lean on mathematical morphology. Mathematical morphology is a set-oriented image analysis theory formulated



in the first place by Matheron and Serra (Matheron, 1975; Serra, 1982; 1988). Rather than starting within the euclidian (continuous) space to build tools such as convolution or fourier analysis that are then discretised on the digital grid, the components of an image are considered as sets on which basic transformations are applied using a probe, called the structuring element (erosion, dilation), and geodesic operations (reconstruction, watershed). An exhaustive explanation of these concepts is far beyond the scope of this contribution, the reader should refer to the classical textbooks (Serra, 1982; 1988) for an in-depth presentation of this theory and its wide application field.

## PRESENTATION OF THE METHOD

The most efficient and widely used tool for segmentation in this field is the watershed transform applied to the gradient of the image (Beucher and Lantuejoul, 1979; Vincent and Soille, 1991), which contains the information about the borders of the objects in the original image. Given some markers, that shall be a subset of the local minima of the gradient (see below), the watershed transform identifies the zones of influence (in the sense of catchment basins) of each marker. The result is an assemblage of zones, one per marker, whose borders lie on the higher values of the gradient, i.e. on the borders of the image objects. However the major problem brought by this method is over-segmentation. A noisy image has a noisy gradient and, by using all the local minima of the gradient as markers, too many zones are created, most of them being irrelevant. One typical answer to this issue is to filter either the starting image or the gradient image with an alternate sequential filter (ASF), i.e. a sequence of opening and closing with a family of structuring elements of increasing size (Serra, 1982). On the one hand, filtering the gradient image is difficult to justify: it might lead to the loss of actual borders between the phases without control. On the other hand, using an ASF on the starting image reduces the noise without blurring but has two main undesirable side effects: (i) it destroys all the structures of the image smaller than the last structuring element used in the filter; (ii) it creates a lot of flat zones in the image (a connected set of voxels with the same grey-level), which in turn lead to a lot of zero-valued gradient zones, increasing the number of local minima of the

gradient and hence an over-segmentation.

This last problem is solved by making the following assumption: in each phase, each connected component to extract contains at least one local minima or local maxima. This local extrema might come from a residue of noise or be a real extrema (e.g. a small connected pore would induce a local minima; a small grain of calcite would induce a local maxima). As the filtered image contains a lot of flat zones, these extrema are almost always flat, i.e. correspond to a local minima of the gradient. The original idea presented here is to use as starting markers for the watershed operation the intersection of the local minima of the gradient with the local extrema of the filtered image.

← insert Fig. 3

## MATHEMATICAL DEVELOPMENT

A 3-d image  $\mathbf{f}$  is considered as a set of  $N \times N \times N$  voxels,  $N \in \mathbb{N}$ , on a cubic grid with 26-neighboring, each having an integer value (its grey level), in the range  $[0, 255]$ .

$$\mathbf{f} = \{v_{ijk}\}, v_{ijk} \in [0, 255], (i, j, k) \in [0, N]. \quad (1)$$

The image is here considered cubic for the sake of simplicity. Each voxel can be located in the image with a unique triplet of numbers (coordinates).

$$\mathbf{f}(\mathbf{x}) = v_{ijk}, \mathbf{x} = \{i, j, k\}. \quad (2)$$

On a grey level image, the erosion  $\varepsilon$  and the dilation  $\delta$  by a structuring element  $B$  are defined at every point  $\mathbf{x}$  by

$$\delta_B(\mathbf{f})(\mathbf{x}) = \vee \{f(\mathbf{x} - \mathbf{y}), \mathbf{y} \in B(\mathbf{x})\} \quad (3)$$

$$\varepsilon_B(\mathbf{f})(\mathbf{x}) = \wedge \{f(\mathbf{x} - \mathbf{y}), -\mathbf{y} \in B(\mathbf{x})\} \quad (4)$$

where  $\vee$  is the supremum (or maximum) operator and  $\wedge$  the infimum (minimum) operator and  $B(\mathbf{x})$  is the structuring element centered at point  $\mathbf{x}$ . The opening  $\gamma$  and closing  $\phi$  are

defined by the adjunctions

$$\varphi_B = \delta_B \varepsilon_B \quad (5)$$

$$\gamma_B = \varepsilon_B \delta_B \quad (6)$$

As the family of structuring elements, digital balls  $B_\lambda$ , with radius  $\lambda$ , are used

$$B_\lambda(\mathbf{x}) = \{\mathbf{y}, d(\mathbf{x}, \mathbf{y}) \leq \lambda\}, \lambda \in \mathbb{N} \quad (7)$$

where  $d(\mathbf{x}, \mathbf{y})$  is the euclidian distance between the digital points  $\mathbf{x}$  and  $\mathbf{y}$ . (Note that on the cubic digital grid with 26-neighbors for each voxels,  $B_1$  is a cube of 3 voxels side.)

The operation of sequential alternate filtering are brought up to  $\lambda = 3$ , yielding the filtered image  $\mathbf{h}$

$$\mathbf{h} = \gamma_{B_3} \varphi_{B_3} \gamma_{B_2} \varphi_{B_2} \gamma_{B_1} \varphi_{B_1}(\mathbf{f}). \quad (8)$$

The intermediate steps and the result of this filtering operation are shown in figure 3-(a) to (d).

An ASF up to a structuring element of size  $n$  removes the noise with characteristic length smaller than  $n$  but, as a counter part, destroys any component of the image smaller than that size. Hence the more the ASF is pushed towards bigger sizes, the more the image is denoised but the more structural components of the image are lost. A compromise has to be done. One crucial advantage of such a morphological filter is the knowledge of what kind of structure is lost: everything smaller than the structuring element. In this particular approach, everything bigger than a ball with a diameter of 7 voxels is kept (which is the typical size of micritic calcite grains). An ASF up to a smaller structuring element appeared to leave too much noise.

With the filtered image  $\mathbf{h}$  the marker image is constructed as the intersection of the local extrema of the image with the local minima of the gradient. The morphological gradient  $\mathbf{g}$  of the filtered image is obtained in the following way

$$\mathbf{g} = \delta_{B_1}(\mathbf{h}) - \varepsilon_{B_1}(\mathbf{h}). \quad (9)$$

The marker is then

$$\mathbf{m} = (\max(\mathbf{h}) \vee \min(\mathbf{h})) \wedge \min(\mathbf{g}) \quad (10)$$

where the function min is defined for every voxel of the image at location  $\mathbf{x}$  by

$$\min(\mathbf{h})(\mathbf{x}) = \begin{cases} 255 & \text{if } \mathbf{h}(\mathbf{x}) \text{ belongs to a local minimum} \\ 0 & \text{otherwise} \end{cases} \quad (11)$$

with an equivalent definition for max. A local minimum (resp. maximum) is a set of connected voxels (possibly one single voxel) that has no neighbor with a strictly lower (resp. higher) value. Note that because the min and max functions return binary images, the supremum and infimum in equation 10 are equivalent to union and intersection respectively.

The marker  $\mathbf{m}$  has non-zero values only at some selected gradient local minima, it can be used to start a watershed invasion of the gradient image

$$\mathbf{w} = \text{watershed}(\mathbf{g}, \mathbf{m}) \quad (12)$$

The watershed identifies the zones of influence (catchment basin) of each minima in the gradient image marked with an extrema in the filtered image. During the process, when such a zone is identified, the mean value of the image  $\mathbf{h}$  over this zone is computed and affected to all the pixels belonging to this zone in the resulting image  $\mathbf{w}$ . As a result a mosaic of flat zones is obtained which is much simpler than the starting image as illustrated in figure 3 (Beucher, 1990). Using the histogram (figure 4) the threshold levels are easily identified (as the minimum values between the peaks). The results of the thresholding of the mosaic image are presented in figures 5, 6 and 7.

All the computations were conducted in 3-d with a self-developped C++ code.

← insert Fig. 4

← insert Fig. 5

← insert Fig. 6

← insert Fig. 7

## CONCLUSION

In this contribution an efficient technique enabling to denoise and to segment X-ray tomographic images of porous media stones was presented and applied to building stone. It allows a very strong noise removal without blurring, at the price of losing the smaller structural components of the image. This loss is however controlled: the size of the structuring element of the last ASF step gives the size of the smallest structural components kept. As the method makes no a priori strong assumption about the images to segment, it should then be easily generalized to tomographic images of various materials and even to images from other imaging techniques.

The perspectives of this work are now to perform the geometrical and topological analysis of each identified phase and simulate fluid and mass transport in order to characterize the weathering effects of building stones.

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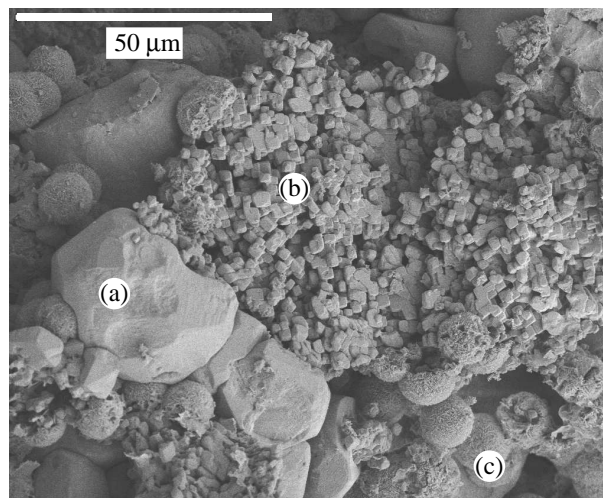


Fig. 1: SEM image of a tuffeau sample with (a) sparitic calcite (large grains), (b) micritic calcite (small grains of a few  $\mu\text{m}$ ), (c) opal spheres of 10 to 20  $\mu\text{m}$  diameter.

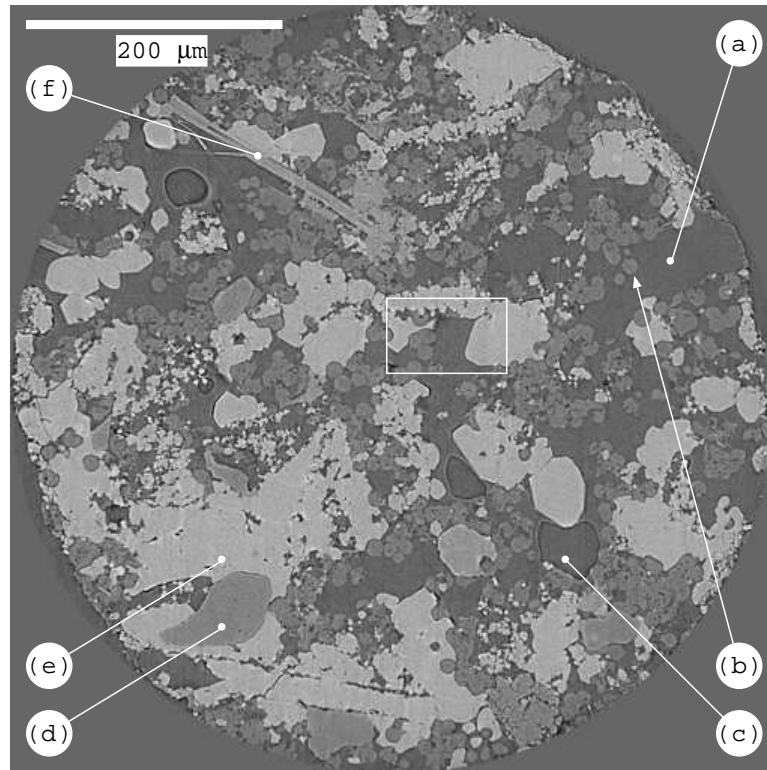


Fig. 2: One slice extracted from a 3-d tomographic image of a tuffeau sample. The image is  $2048 \times 2048$  pixels, pixel size is  $0.28\text{m}$  (the radius of the sample is  $\approx 600\text{m}$ ) with (a) resin, (b) silica (opal sphere), (c) air bubble in the resin (caused by the impregnation process), (d) silica (quartz crystal), (e) calcite and (f) phyllosilicate. The rectangle marks the location of the zoomed image that appears in figure 3-(a).

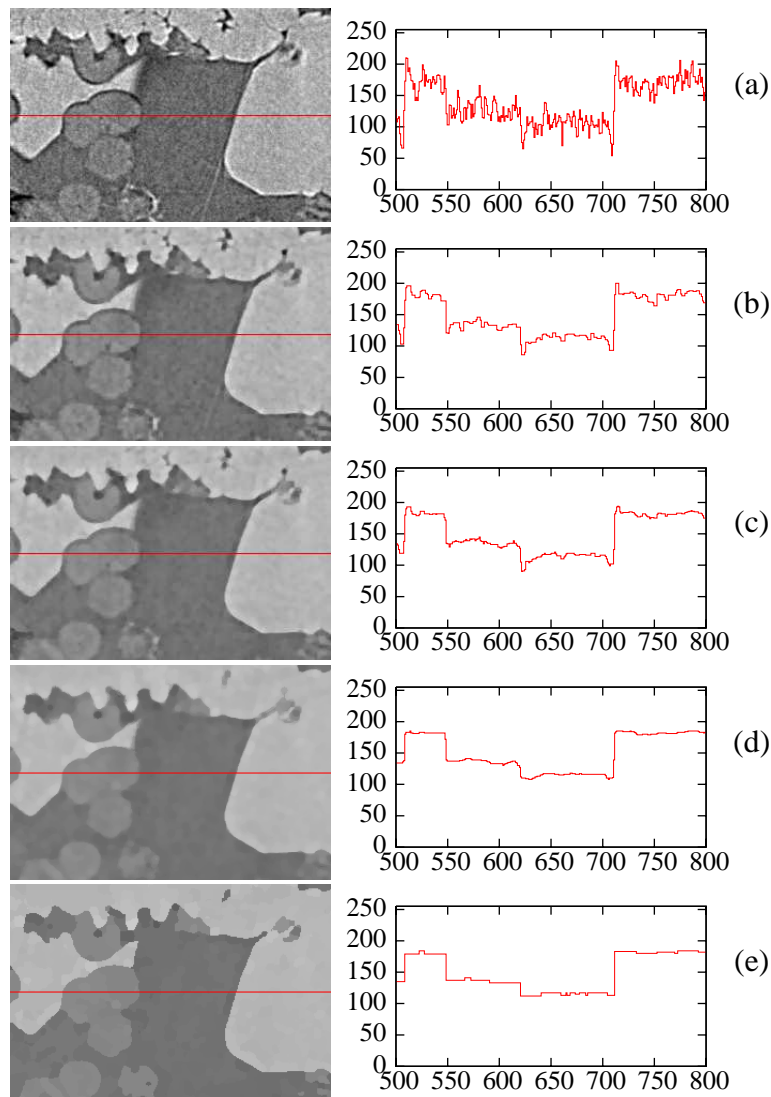


Fig. 3: *Illustration of the image processing. In the left column a 2-d zoom in the sample (white rectangle in figure 2) undergoes the image treatment. The images are  $300 \times 200$  pixels with pixel size  $0.28\mu\text{m}$ . In the right column, a line of the zoomed image (noted in red in the left column) is plotted (pixel coordinate in abscissa, grey level in ordinate). From top to bottom: (a) the original image; (b) after step 1 of the ASF; (c) after step 2, (d) after step 3, (e) after the computation of the mosaic. The histograms of the whole 3-d image at each steps are visible on figure 4. The ASF clearly removes the noise in the image without blurring the borders between the phases. The watershed operation flattens more the image, yielding a very simple image to threshold.*

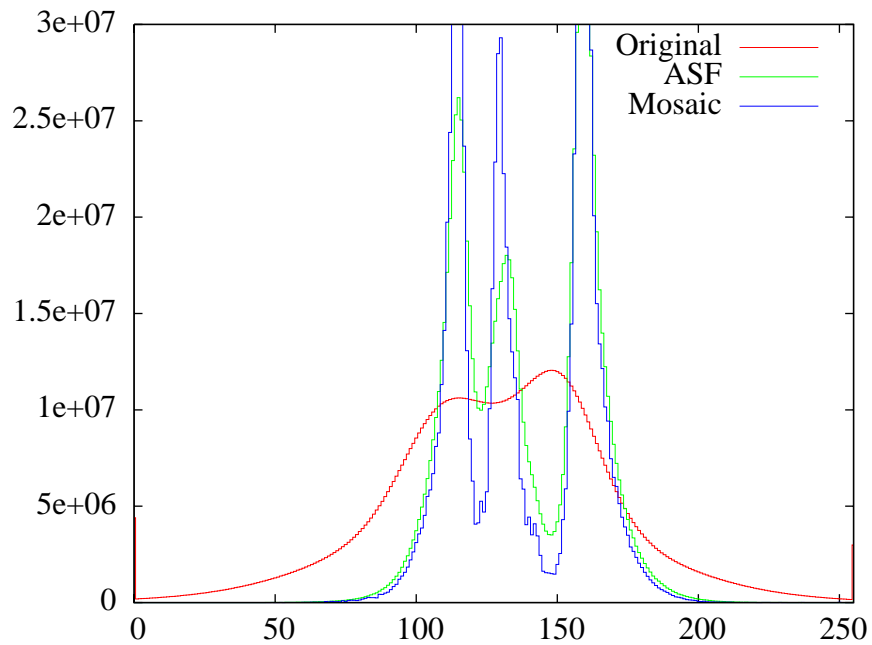


Fig. 4: *Evolution of the histogram of a  $1024 \times 1024 \times 1024$  voxels image during the image processing. The starting image is visible on figure 6. Original is the histogram of the original images (figure 3-(a)), ASF after the ASF (figure 3-(d)) and Mosaic after the watershed (figure 3-(e)). In the starting image, the noise precludes any thresholding, the peaks are not distinguishable. The ASF makes them become visible, the watershed operation provides an increased clean-up of the image, resulting in the last histogram where the threshold levels are straightforward.*

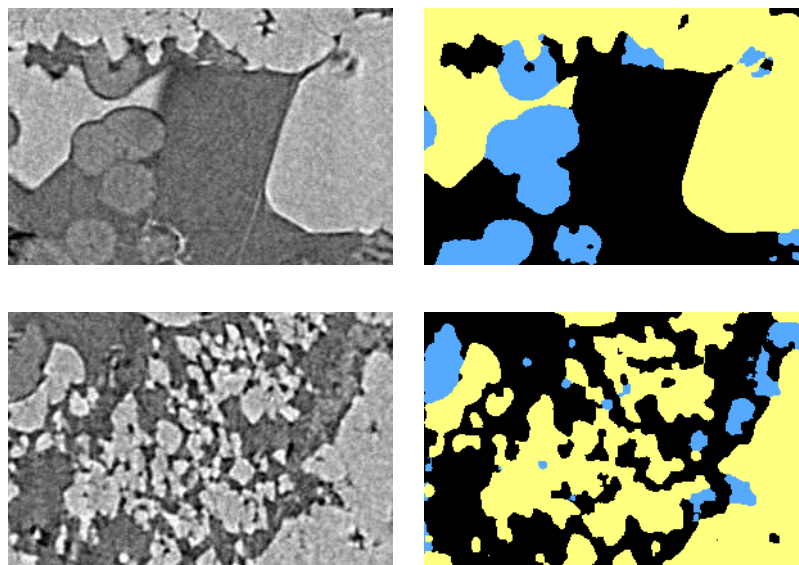


Fig. 5: *Illustration of the segmentation. In the left column two 2-d zooms ( $300 \times 200$  pixels) of the 3-d sample before image treatment. In the right column the thresholding of the mosaic, with levels selected using its histogram (minimum values between the three peaks); in black the porosity, in blue the silica, in yellow the calcite. In the top row, the image of figure 3, below a zone containing micritic calcite. This last example clearly shows that the smaller structures of the micritic calcite are lost, because of the ASF. However, some small zones appear in this image. It is due to the fact that the treatment of the image is fully 3-d while only a 2-d sample is here presented. These are small 2-d traces of a bigger 3-d structure.*

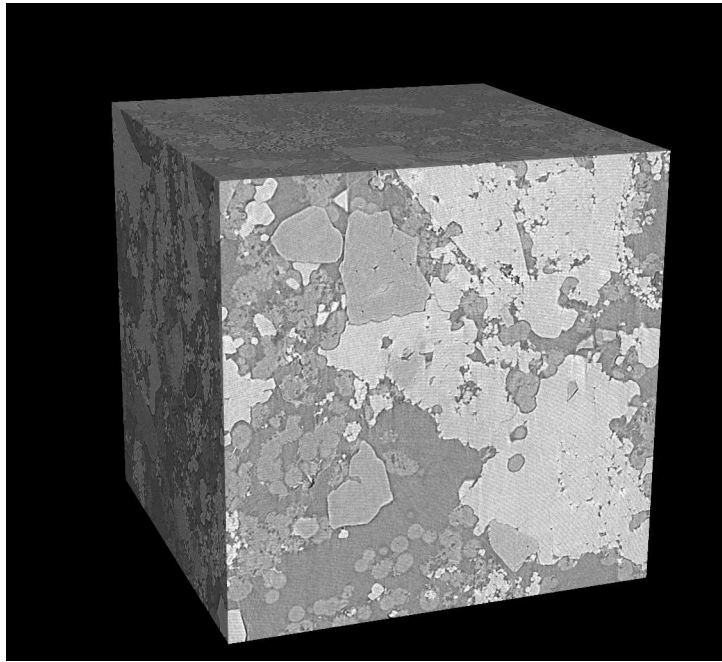


Fig. 6: 3-d illustration of the segmentation process: original image. The image is  $1024 \times 1024 \times 1024$  voxels. The segmented image is in figure 7.



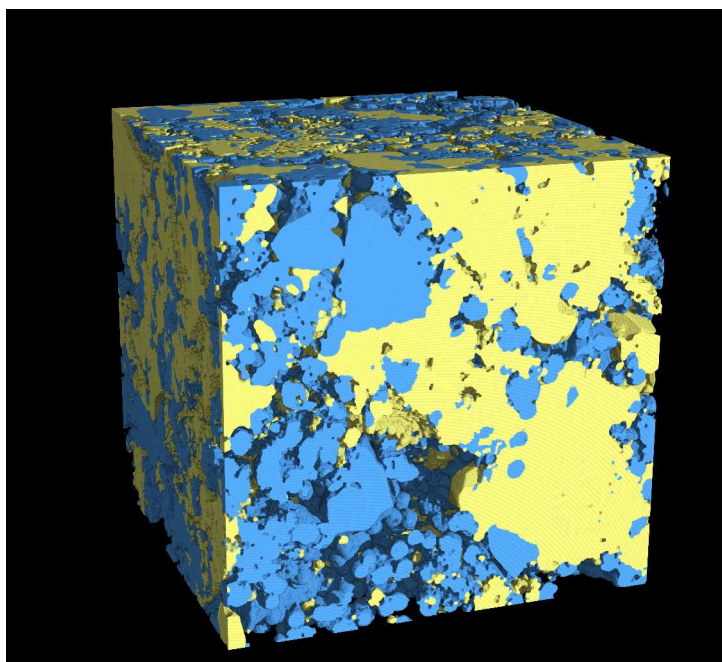


Fig. 7: 3-d illustration of the segmentation process: segmented version of the image in figure 6.