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Dynamical evolution of the Gliese 581 planetary system

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ABSTRACT

Context. The M dwarf Gliese 581 has recently been found to harbour two super Earths in addition to an already known close-in Neptune-mass planet. Interestingly, these two planets are considered as potentially habitable, and recent theoretical works give further credit to this hypothesis, in particular for the outermost planet (Gl 581 d).

Aims. In this paper, we address the issue of the dynamical stability evolution of this planetary system. This is important because the basic stability ensures that a 3-planet model is a physically adequate description of the radial-velocity (RV) data. It is also crucial when considering the planets' habitability because the secular evolution of the orbits may regulate their climate, even in the case where the system is stable.

Methods. We have numerically integrated the planetary system over 108 yrs, starting from the present fitted solution. We also performed additional simulations where i) we vary the inclination of the system relative to the line of sight, ii) assume eccentricities at the upper limit of the error bars in the radial velocity fit and where iii) we consider additional (yet undetected) outer planets. We also compute Lyapunov exponents to quantify the level of dynamical chaos in the system.

Results. In all cases, the system appears dynamically stable, even in close to pole-on configurations. The system is actually chaotic, but nevertheless stable. The semi-major axes of the planets are extremely stable, and their eccentricities undergo small amplitude variations. The addition of potential outer planets does not affect this result.

Conclusions. Consequently, from the dynamical point-of-view, a 3-planet model is an adequate description of the present RV-data set. Only a limited range of inclinations can be excluded for coplanar orbits ($i < 10^{\circ}$). The climate on the planets is expected to be secularly stable, thus not precluding the development of life. Gl 581 remains the best candidate for a planetary system with planets that potentially bear primitive forms of life.

Key words. Planetary systems – Methods: N-body simulations – Celestial mechanics – Stars: Gliese 581 – Astrobiology – Stars: low-mass, brown dwarfs

1. Introduction

The M dwarf Gliese 581 has been the subject of a recent investigation with the identification of its 3-planet system. One of the planets (Gl 581 b), a Neptune-mass object orbiting the ≼ star on a 5.4-day orbit, has already been known for two years (Bonfils et al. 2005). Recently, Udry et al. (2007) have reported the discovery of two additional super Earths (Gl 581 c and d), revolving around the star in 12.9 and 83 days (see details in Table 1). Considering Gl581's luminosity, Udry et al. (2007) inferred the equilibrium temperature of both planets and conclude they may lie within the habitable zone of the star.

Detailed further modeling by von Bloh et al. (2007) and Selsis et al. (2007) addresses the habitability of the planets. Likewise, von Bloh et al. (2007) find that the greenhouse effect increases Gl 581 c temperature so much that they no longer consider the planet to be in the habitable zone. For similar rea-

sons, Selsis et al. (2007) find that GI 581 c's surface temperature is very likely higher than the equilibrium temperature calculated by Udry et al. (2007). However, they do not rule out habitability for this planet, as a large cloud coverage (> 75%) would cool down the planet enough. Conversely, both studies agree that the outermost planet (Gl 581 d) is a good candidate for habitability (although close to the outer edge of the habitable zone) and actually consider it as the better of the two candidates.

An important and unsettled issue about this system concerns its dynamical behaviour. It is first important to know whether the planetary system is dynamically stable and for which range of orbital inclinations. If verified, the basic stability of the system ensures that the model used (3 planets) is a physically adequate description of the observations (the radialvelocity measurements). If not verified, the planet detections are not necessarily invalidated (as RV periodogrammes clearly show that three coherent signals sum up at specific periods). It would instead mean that either not enough data were collected

Table 1. Orbital parameters of the Gl 581 planetary system, as derived from the fit of Udry et al. (2007)

Planet	Period (days)	Semi-major axis (AU)	Eccentricity	ω (deg)	$t_{\rm p}~({\rm JD}-2400000)$	Mass (M_{\oplus})
Gl 581 b	5.36843 ± 0.00031	$0.04061 \pm 0.16 \times 10^{-6}$	0.01374 ± 0.01405	273.21195 ± 60.54198	52998.74631 ± 0.90393	15.82 ± 0.25
Gl 581 c	12.92648 ± 0.00723	$0.07295 \pm 2.7 \times 10^{-4}$	0.15926 ± 0.05981	257.41189 ± 24.37209	52993.40770 ± 1.00130	5.073 ± 0.31
Gl 581 d	83.22730 ± 0.65845	0.2525 ± 0.013	0.12118 ± 0.12034	317.01021 ± 41.79575	52946.80339 ± 11.49888	7.804 ± 0.69

to converge toward the "true" parameters of the system or that the model (3 planets) is not complex enough to describe the data. Further varying the orbital inclination, we expect to find that below a given value – or, equivalently, above given masses for the planets – the system becomes unstable. Not valid physically, this range of inclinations should be rejected among the possible solutions. This partially constrains the sin *i* degeneracy inherent to radial-velocity detections.

Beyond the basic stability, the secular evolution of the orbits may play an important role regarding planets' habitability. All climate calculations (von Bloh et al. 2007; Selsis et al. 2007) have been done with the currently determined orbits. The secular evolution of the orbits has the potential of affecting the climate on the planets. A given planet may lie within the habitable zone but, if subject to significant eccentricity changes, it can undergo strong climate variations that eventually preclude life development. The presently determined eccentricities (Table 1) are small enough to ensure climate stability. But one needs to know which maximum values they reach due to secular perturbations.

In the present paper, we numerically investigate the secular evolution of the Gl 581 system, starting from the solution of Table 1. In Sect. 2, we study this solution (that we subsequently refer to as the nominal case). In Sect. 3, we perform other integrations, assuming different inclinations from edgeon and letting the initial eccentricities of the planets reach their maximum values within their error bars. In order to quantify the dynamical chaos in this system, we compute Lyapunov exponents for all these solutions in Sect. 4. In Sect. 5, we investigate the perturbing action of potentially additional outer planets that have not been detected yet, provided their contribution to the radial velocity signal is small enough compared to the residuals of the 3-planets fit. Our conclusions are presented in Sect. 6.

2. The nominal case

The best 3-planet orbital fit for GI 581 is explained in Table 1. This solution with the assumptions of coplanarity and $\sin i = 1$ ($i = 90^{\circ}$, an edge-one system) will constitute our nominal case. We numerically integrate this system taking $0.31\,M_{\odot}$ for the mass of GI 581. The integration is performed using the symplectic N-body code SyMBA (Duncan et al. 1998), which handles close encounters. The initial timestep is fixed to $2\times 10^{-4}\,\mathrm{yr} = 0.18\,\mathrm{day}$, i.e. 1/30 of the smallest orbital period. Symplectic integration schemes usually ensure energy conservation with 10^{-6} relative accuracy as soon as the timestep is taken to $\sim 1/20$ of the smallest orbital period (Levison & Duncan 1994). The integration is carried out over $10^8\,\mathrm{yr}$. On more limited timespans, we checked that taking a significantly

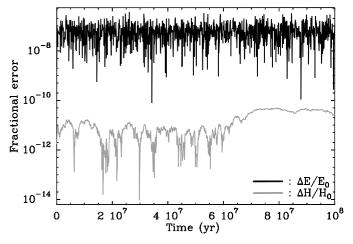


Fig. 1. Fractional errors on the total energy E with respect to the initial one E_0 (black curve), and on the total angular momentum H with respect to the initial one H_0 (grey curve), as a function of time over the 10^8 yr integration

Table 2. Precession frequencies for the nominal solution, as computed from the linear secular theory

Name	Frequency ("/yr)	Period (yr)
g_1	3300.9	392.62
g ₂ g ₃	539.04 38.199	2404.2 33945.

smaller timestep does not change the result. In Fig. 1, we display the fractional errors on the total energy and angular momentum over the 10⁸ yr integration. The energy is preserved to less than 10^{-7} relative accuracy. Hence we are confident in our integration. Figure 2 shows the first 10⁴ years of the integration. We see that the secular variations of the 3 planetary orbits are very regular. The eccentricities undergo quasi-periodic modulations, while the longitudes of periastra precess regularly. This solution is in fact very close to the one we can compute with a linear secular theory (Laplace – Lagrange), such as described the one by Bretagnon (1974, 1990). In the linear approximation, the secular evolution of the eccentricity vectors of the 3 planets is a combination of sine and cosine terms with 3 characteristic frequencies $(g_i, i = 1, 2, 3)$ that are listed in Table 2. These frequencies are obtained by solving the linear secular equations for their eigenvalues. We obviously see these characteristic frequencies in Fig. 2. An interesting outcome is that these precession frequencies are much higher than in the Solar System, which do not exceed 25''/yr, and g_1 is basically the main precession frequency of the periastron of Gl 581 b

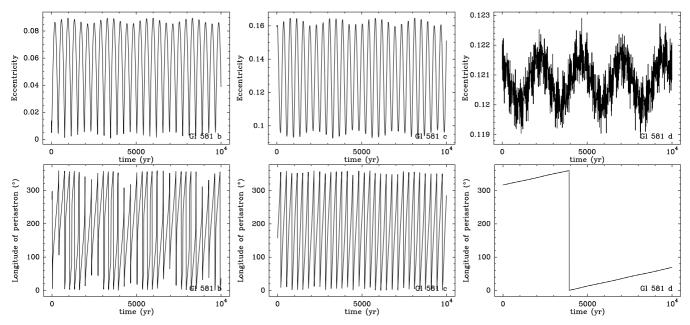


Fig. 2. The 10^4 first years of the integration of the nominal solution. The upper plots show the temporal evolution of the eccentricity of the three planets Gl 581 b,c, and d, from left to right, respectively; the lower plots are the same for the longitude of periastron ϖ

Table 3. Variation ranges for some orbital parameters fo the 3 planets over the 10^8 yr integration.

Planet	Semi-major axis (AU)	Eccentricity	Periastron (AU)	Apoastron (AU)
Gl 581 b	0.040609 - 0.046185	0.01 - 0.095	0.0368 - 0.0402	0.041 - 0.0445
Gl 581 c	0.072885 - 0.073	0.07 - 0.16	0.0614 - 0.0678	0.078 - 00846
Gl 581 d	0.2522 - 0.2528	0.1200 - 0.1246	0.2207 - 0.2227	0.2823 - 0.2843

and Gl 581 c. This is obviously due to the much smaller size of the system. Given the error bar on the fits of the arguments of periastra (ω_1, ω_2) , the secular motion should be detectable within ~ 30 years, and probably less if the orbital fits get more constrained in the near future thanks to further monitoring.

In Table 3, we list the maximum evolution ranges for the orbital elements of the three planets. The semi-major axes are extremely stable, revealing a regular dynamics out of any meanmotion resonance configuration. The evolution ranges of the eccentricities are narrow, so that we may claim than the system is stable with a high level of confidence. While the time span of the integration is 10^8 yr, most of the characteristic features of the secular evolution of the orbital parameters occur on a 10^4 yr-time scale. Therefore, even if the star is believed to be older than 2×10^9 yr, the current integration clearly explores all the dynamical possible outcomes of the system. Actually, due to the short orbital periods of the planets (and to the high precession frequencies), integrating the Gl 581 over 10^8 yr is basically equivalent to integrating the Solar System over ~ 100 Gyr

Interestingly, the present-day eccentricity of Gl 581 c roughly corresponds to its maximum values along its secular evolution, and the eccentricity of Gl 581 d only has small variations. Hence we expect the climate of both outer planets to be secularly stable.

3. Other solutions

The nominal solution corresponds to an inclination $i = 90^{\circ}$ (so the lowest possible planetary masses) and to the orbital parameters of the discovery paper (Table 1). Lower inclinations and/or parameter's values slightly outside the best solution may lead to different dynamical behaviours that are worth investigating.

In a first set of additional simulations, we assume various inclinations ranging from 0 (pole on) to 90° (edge on), but still holding the initial eccentricities to their nominal values. The mass of each planet is augmented by a factor $1/\sin i$ with respect to the nominal case. In a second set of simulations we assume different inclinations and, moreover investigate the impact of eccentricities larger than in the nominal case (as less stability is only expected if the eccentricity is larger). For that set, we take the initial eccentricities for the three planets at the upper limit of their error bars (we add 1σ to the eccentricities) For both sets of integrations, we plot the width of the evolution ranges obtained over the 10^5 yr integration for both the semimajor axis and the eccentricities of the three planets (Fig. 3).

As can be seen from Fig. 3, when the inclination decreases, the dynamical interactions increase accordingly and we expect the system to become unstable below a given inclination. As for the nominal case, the integrations are carried out over 10^5 yr. They naturally show that both the semi-major axis and

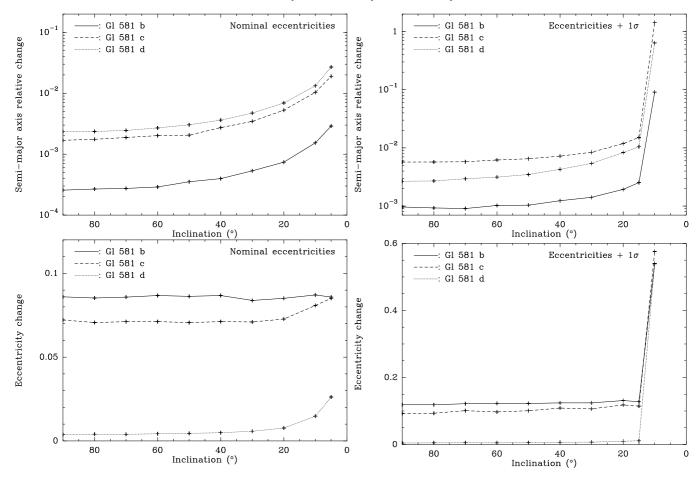


Fig. 3. Stability of the three-planet system in various configurations. The maximum variation range for the semi-major axes (upper plots) and for the eccentricities (lower plots) is displayed as a function of the assumed viewing inclination of the system with respect to pole-on. Each cross corresponds to a single simulation. The left plots correspond to simulations with the nominal eccentricities as initial conditions, and the right plots to simulations with eccentricities increased by 1σ relative to the error bars given in Table 1.

the eccentricity take a wider range of values than in the nominal case with decreasing inclinations. In the first set of integrations (nominal initial eccentricities), the system nonetheless remains stable down to $i=10^\circ$. Almost pole-on configurations ($i<10^\circ$) are unstable and should be rejected from possible solutions. Although, such low inclinations are very improbable, and from the statistical point-of-view, the actual masses of the planets are probably close to those listed in Table 1.

In the second set of simulations (1σ augmented initial eccentricities), the dynamical interactions are slightly enhanced and the semi-major axis and the eccentricity take a wider range of values than for the first set of additional simulations. The system is therefore found unstable below larger inclinations ($< 20^{\circ}$).

In all cases, the instability appears very unlikely. If we assume that the rotation axis of the system is randomly distributed in space, $i > 20^{\circ}$ occurs with a probability of 0.94. In conclusion, irrespective of its actual inclination, the Gl 581 planetary system is very probably stable.

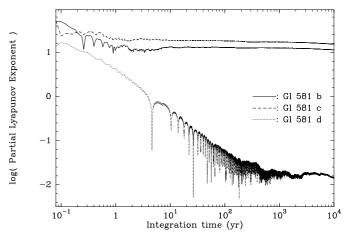


Fig. 4. Progress of the calculation of the partial Lyapunov exponents as a function of the integration time, in the nominal case for Gl 581 (zero inclination, nominal eccentricities). At $t = 10^4$ yr, the three exponents have stabilised.

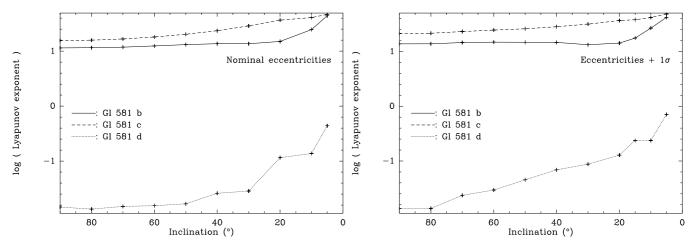


Fig. 5. Lyapunov exponents as a function of the inclination i, computed for all the simulations described in Fig. 3. Left plot: simulations with nominal eccentricities; **Right plot**: simulations with 1σ increased eccentricities.

4. Lyapunov exponents

Looking for variation ranges for the orbital elements is a basic tool for investigating the stability of a planetary system. A more sophisticated way for quantifying chaos is to compute Lyapunov exponents. For all simulations decribed above, we compute the maximum Lyapunov exponents (MLE) for the three planets, following the technique by Benettin et al. (1978) (see also Morbidelli 2002). The exponents are computed by integrating fictitious bodies having initial conditions that are very close to those of the planets and estimating their exponential diverge rate. We coupled this algorithm with the SyMBA integrator.

When we start integrating the bodies with initial coordinate vector p_0 (holding for the positions and velocities of all the bodies), we also integrate another system of bodies with identical masses, but with initial coordinate vector $p_0 + \delta p_0$, where $\|\delta p_0\| \ll \|p_0\|$. After a fixed normalization time t_{norm} , we compute the error vector $\delta p(t_{\text{norm}})$ as the difference at $t = t_{\text{norm}}$ (after integration) between the coordinate vector of the fictitious bodies and of the regular bodies. We then compute

$$s_1 = \frac{\|\delta p(t_{\text{norm}})\|}{\|\delta p_0\|}$$
 and $\delta p_1 = \frac{\delta p(t_{\text{norm}})}{s_1}$ (1)

We then use δp_1 as a new initial error vector for the fictitious bodies relative to the coordinates vector of the regular bodies at t_{norm} , and we iterate the above process. Each t_{norm} , the error vector is renormalized this way, and we obtain a sequence s_1, s_2, \ldots of renormalization factors. Benettin et al. (1978) proved that the MLE \mathcal{L} can be computed as

$$\mathcal{L} = \lim_{n \to +\infty} \frac{1}{n \, t_{\text{norm}}} \sum_{i=1}^{n} s_i \equiv \lim_{n \to +\infty} L_n \qquad . \tag{2}$$

The result is independent of the choice of t_{norm} , provided it is chosen small enough to avoid too large an exponential divergence. During the integration, we compute $\log L_n$ for every t_{norm} , and we try to derive an asymptotic behaviour. Two cases can occur: i) $\log L_n$ converges towards a finite limit. Then the system is chaotic and we have reached $\mathcal{L} > 0$ within our integration time. ii) Or $\log L_n$ keeps decreasing monotonically

at the end of the integration. This means that the orbit is very probably regular or, more precisely, less chaotic than a given level that depends on the integration time.

In practice we compute MLEs for all the individual bodies in the integration: for each orbit we compute the associated (partial) error vector, and perform individual renormalizations. Each body has its own sequence of s_i 's. Note that more than the absolute values of the MLE derived, the comparison between the values derived for the individual bodies and between different integrations is more relevant. This shows clearly which orbits are the most chaotic.

In our example applications, we integrate over 10^4 yr to compute the MLEs. t_{norm} has been fixed to 0.02 yr, i.e., 100 times the timestep. The progress of the computation of the MLEs in the nominal case for the three planets is plotted as a function of the integration time in Fig. 4. We see that they have all converged towards finite limits at $t = 10^4$ yr, showing that the orbits are actually chaotic.

The global result of MLE calculation is shown in Fig. 5, where we have computed the MLEs for the three planets for all the simulations described in Fig. 3 (stopping at $t = 10^4$ yr). In all cases, we obtain non-zero exponents, showing that the system is actually chaotic.

We see that the MLEs slowly increase with decreasing inclinations, showing as expected that solutions at smaller inclinations are more chaotic, due to higher planetary masses. We nevertheless note that the variation is small except for $i < 20^{\circ}$. The system is not much more chaotic at $i = 20^{\circ}$ than at $i = 90^{\circ}$. This confirms that there is no real dynamical constraint on the inclination. We also note that solutions with 1σ increased eccentricities are not more chaotic than those with nominal eccentricities. As a result the dynamical stability does not put any additional constraint on the planet eccentricities other than those derived from the radial velocity analysis.

From Fig. 5, it also becomes clear that the two inner planets (Gl 581 b and c) are much more chaotic than the outer one (Gl 581 d) (the exponent is smaller). In fact, the two inner planets are significantly chaotic. This does not prevent them from being stable. Actually, chaos does not necessarily mean insta-

Table 4. Semi-major axis and eccentricity variation ranges for the 3 known planet of Gl 581, plus additional outer planets (see text), computed over 10^5 yr integrations

Planet	Semi-major axis (AU)	Eccentricity		
With a 1 M	I _J planet at 5 AU:			
Gl 581 b	0.04060120 - 0.04061199	0.00367502 - 0.0895939		
Gl 581 c	0.07286312 - 0.0729903	0.09259277 - 0.164875		
Gl 581 d	0.25222823 - 0.25281971	0.11884516 - 0.1228305		
With a 29.	$6 M_{\oplus}$ planet at $5 \mathrm{AU}$:			
Gl 581 b	0.04060139 - 0.04061188	0.00347993 - 0.0895106		
Gl 581 c	0.07286522 - 0.0729892	0.09258738 - 0.1647922		
Gl 581 d	0.25222915 - 0.2528203	0.11887163 - 0.1226443		
With a 26.	5 M _⊕ planet at 4 AU:			
Gl 581 b	0.04060141 - 0.04061174	0.00354749 - 0.08949917		
Gl 581 c	0.07286447 - 0.07298892	0.09258812 - 0.16479787		
Gl 581 d	0.25222689 - 0.25282013	0.11884819 - 0.1226468		
With a 22.9 M_{\oplus} planet at 3 AU:				
Gl 581 b	0.04060137 - 0.04061170	0.00372438 - 0.0895144		
Gl 581 c	0.07286369 - 0.07298806	0.09258945 - 0.16479738		
Gl 581 d	0.25222659 - 0.25281951	0.11884226 - 0.12267108		
With a 18.7 M_{\oplus} planet at 2 AU :				
Gl 581 b	0.04060140 - 0.04061177	0.00405747 - 0.08955927		
Gl 581 c	0.07286632 - 0.07298852	0.09259499 - 0.16492574		
Gl 581 d	0.25222099 - 0.25281587	0.11886586 - 0.12266511		
With a 13.	2 M _⊕ planet at 1 AU:			
Gl 581 b	0.04060131 - 0.04061176	0.00475611 - 0.08969945		
Gl 581 c	0.07286289 - 0.07298820	0.09258994 - 0.16491917		
Gl 581 d	0.25222239 - 0.25280011	0.11882570 - 0.12246267		

bility. The Solar System is known to be chaotic (but on longer timescales), yet it is nevertheless stable.

5. Other planets

Our simulations were made with the three known planets orbiting Gl 581. However, the system may harbour additional, unknown planets. The presence of these planets may affect the stability of the whole system. There are upper limits to the presence of additional (mainly outer) planets. The maximum amplitude of the residuals in the 3-planet fits of Udry et al. (2007) is $\pm 2.1 \,\mathrm{m\,s^{-1}}$. Any additional planet should not generate a radial velocity with a larger amplitude, otherwise it would have already been detected. Assuming $i=90^{\circ}$ and a circular orbit, this puts severe constraints on the mass m and distance d of the unseen planet. We derive

$$\frac{m}{1\,M_{\oplus}} \le 13.227 \times \sqrt{\frac{d}{1\,\text{AU}}} \qquad . \tag{3}$$

This constraint holds if the unseen planet generates full-amplitude variations within the timespan of the radial velocity data, i.e., ~ 1000 days (Udry et al. 2007). This means that the orbital period of the unseen planet must not exceed ~twice

this time span to account for this constraint, i.e. an orbital distance $d \le 5.5$ AU. For more distant planets, the constraint is much weaker. In fact, this upper limit is probably already too large. Dynamically speaking, we do no expect any hypothetical planet orbiting at 5.5 AU to significantly affect the dynamics of the inner system located inside 0.25 AU. We are thus confident in the conclusions we derive below, as all potentially destabilizing configurations have been explored.

We thus performed new simulations, each of them with the nominal conditions, but to which we add an additional planet orbiting the star on a circular orbit at an arbitrary distance d, and with the maximum mass allowed by Eq.(3). All the integrations were carried out over 10⁵ yr. We did 5 simulations with d = 5, 4, 3, 2, and 1 AU. This gives masses of 29.6, 26.5, 22.9, 18.7, and 13.2 M_{\oplus} , respectively. We also added a simulation with a 1 Jupiter mass (M_J) planet orbiting the star at 5 AU, as the constraint (3) is less severe at this distance. Note that this case is by far the worst possible disturbing configuration that is still compatible with the constraints. More distant companions, even massive, are less destabilizing. In a first-order approximation, the perturbing effect of a distant planet of mass m orbiting at distance d on an inner planet orbiting at distance r scales as the tidal stripping effect on the orbit, i.e. $\propto mr/d^3$. Hence a 1 $M_{\rm J}$ planet at 5 AU is as disturbing as a 8 $M_{\rm J}$ planet at 10 AU and a 32 $M_{\rm I}$ brown dwarf at 20 AU. The AO surveys would likely have already detected such a massive companion.

In all cases, the whole system appears just as stable as without any additional planet. The result concerning the stability is summarised in Table 4 where we give the semi-major axis and eccentricity variation ranges for the three known planets. The results are very similar among the 6 different integrations, even in the case of a Jovian planet, showing that the additional planet has little influence on the stability of the inner system. Moreover, Table 4 is easily compared to Table 3. The varation ranges are very similar. Therefore, we may stress that any additional outer planet that fits into the constraint of the radial velocity residuals does not affect the stability of the 3-planet system. Note that the maximum eccentricity values in Table 4 are actually slightly lower than those in Table 3. This could appear surprising, since the integration in Table 3 is made without any additional perturber. Recall, however, that it extends over 10⁸ yr instead of 10⁵ for those in Table 4. This shows conversely that if we were entending the integrations of Table 4 up to 10⁸ yr, we should expect slightly wider variation ranges. The basic conclusion nevertheless remains: the stability of the system is not affected.

6. Discussion

We have computed the secular evolution of the Gl 581 planetary system in various possible configurations. The main conclusion is that the system is almost always stable. It is stable for inclinations as low as $\sim 20^\circ$ and even if the initial eccentricities are augmented by their 1- σ error bars.

As expected for any planetary system with regular dynamics, the semi-major axes vary very little and the three planets are expected to remain at their current location with respect to the star. Meanwhile, the eccentricities of the two outer plan-

ets (both considered for habitability) reach values that are significantly above the Earth's value. Concerning Gl 581 c, the present-day eccentricity is close to its maximum value. This planet is not expected to get much farther away from its parent star and, to maintain a surface temperature cool enough to allow the presence of liquid water, a high water-cloud coverage (~75%) would be required at any time. Regarding Gl 581 d, the nominal eccentricity is non negligible (~ 0.12) and also found to be very stable. It is significantly above the maximum value reached by the Earth throughout its secular evolution (~ 0.06 , see e.g. Laskar 1988) and corresponds to a 24% variation of the radiation flux received from the star between apoastron and periastron. The anomalistic season effects should therefore be strong, if not damped by the short orbital period (83 days). If we compare the periastron and apoastron values of GI 581 d to the habitable zone calculations by Selsis et al. (2007) and von Bloh et al. (2007), we see that Gl 581 d is outside the habitable zone at apoastron but well inside at periastron. As pointed out by Selsis et al. (2007), the average stellar flux received by an eccentric orbit is enhanced by a factor $1/\sqrt{1-e^2}$ with respect to a circular orbit with the same semi-major axis. This can help maintaining Gl 581 d in the habitable zone. What we show here is that this effect is secularly permanent.

Now, if the obliquity of the rotation axis of this planet is non-zero, this should combine with the obliquity's seasonal effect and lead to climate differences between the hemispheres of this planet, much like Mars presently. The obliquity of Gl 581 d is of course unknown, but Selsis et al. (2007) and von Bloh et al. (2007) agree in claiming that, given the estimated age of the star (>2 Gyrs), the rotation of Gl 581 d should already be tidally locked with the orbital motion. In that case, we would expect the obliquity to have been set to zero by tidal effects, and there should instead be climate differences between the night and day hemispheres. This could help in maintaining the day hemisphere habitable. Selsis et al. (2007) also show that tidal locking does not contradict the non-zero eccentricity of the orbit. Tides usually tend to both synchronize the rotation and circularize the orbit. The circularization time is almost always longer than the synchronization time (Hut 1981). For Gl 581 d, Selsis et al. (2007) estimate the synchronization time to 10 Myrs and the circularization time to 10 Gyrs, i.e. well above the present age of the system.

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