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# On Human Motion Imitation

Wael Suleiman\*, Eiichi Yoshida†, Jean-Paul Laumond\* and André Monin\*  
CNRS/STIC-AIST/ISRI Joint French-Japanese Robotics Laboratory (JRL)

\* LAAS - CNRS, university of Toulouse

7 Avenue du Colonel Roche, 31077 Toulouse, France

{suleiman, jpl, monin}@laas.fr

† Intelligent Systems Research Institute, National Institute  
of Advanced Industrial Science and Technology (AIST)

AIST Central 2, Umezono 1-1-1, Tsukuba, 305-8568 Japan

{e.yoshida}@aist.go.jp

**Abstract**—In this paper, the imitation of human recorded motions by a humanoid robot is considered. The main objective is to reproduce an imitated motion as closely as possible to the original human recorded motion. To achieve this goal, the imitation problem is formulated as an optimization problem and the physical limits of the humanoid robot is considered as constraints. The optimization problem is then solved recursively by using an efficient dynamics algorithm, which allows the calculation of the gradient function with respect to the control parameters analytically. The simulation results using OpenHRP platform, which is a dynamical simulator for humanoid robot motions, have pointed out that the imitated motions preserve the salient characteristics of the original human captured motion and the optimization procedure converges well thanks to the analytical calculation of gradient function.

**Index Terms**—Humanoid robot; Motion capture; Imitation; Recursive dynamics; Optimization

## I. INTRODUCTION

Imagining an humanoid robot collaborates with humans to execute some daily tasks is now reality. Actually, the ability of humanoid robots to execute complex tasks increases rapidly. In order to increase the autonomous behavior of humanoid robots as well as improving their reactivity, the humanoid robot should be able to imitate human motions.

In recent years, the imitation of human motions was an active research field. Pollard *et al* [1] have proposed a method to transform a dance captured motion to a motion that the humanoid robot can execute. Nakaoka *et al* [2] have realized a whole body control of humanoid robot to imitate Jongara-Bushi dance, which is a traditional Japanese folk dance. To maintain the dynamical stability of humanoid robot, they control the trajectory of Zero Moment Point (ZMP) [3] to be inside the polygon of support. Safonova *et al* [4] use also a pre-recorded human motion to generate optimal motion of the upper body of Sarcos humanoid robot. The function to be minimized is the difference between the recorded and executed motion by the robot. However, the previous methods do not consider some physical limits of humanoid robot, e.g. torques limits.

Ruchanurucks *et al* [5] have proposed a method to optimize upper body motion of humanoid robot in order to imitate a recorded human motion. Their optimization objective function

preserves the main characteristics of the original motion, and at the same time it respects the physical constraints of the humanoid robot. However, the authors have mentioned that the resulting trajectories would meet the latter limits while the former limits are often violated. This is because their method considers the velocity and force constraints separately.

In this paper, our objective is to generate a motion within the humanoid physical capabilities from an human captured motion. The physical limits are the angle, angular velocity and torques limits of humanoid robot's joints. We focus on the imitation of upper body motion. On the other hand, the motion of lower body can be efficiently generated using leg motion primitives [6], [7]. Concerning the dynamical stability of humanoid robot, it can be guaranteed by controlling the ZMP trajectory [8].

The main contribution of this paper is providing an unified optimization framework for generate upper body humanoid robot motions from human captured motions. The generated motions imitate the original human captured motion as closely as possible, and at the same time they respect the physical limits of humanoid robot.

The remainder of this paper is organized as follows. In Section II the imitation problem is formulated. An overview of the algorithm of recursive multibody dynamics is given in Section III. In Section IV the optimization problem is reformulated using the notations of recursive multibody algorithm which is explained in the previous section. In Section V discretizing the configuration space and solving the optimization problem are pointed out. Some experimental results are given in Section VI and Section VII concludes the paper.

## II. IMITATION PROBLEM FORMULATION

The kinematic structure of the humanoid robot HRP-2 [9] is given in Fig. 1. In this structure the degree of freedoms are presented by cylinders. The structure contains 30 degree of freedoms.

The inputs of the imitation procedure are human captured motions. These motions are provided by a motion capture system as a skeleton of virtual actor and a sequence of angular values of its joints.

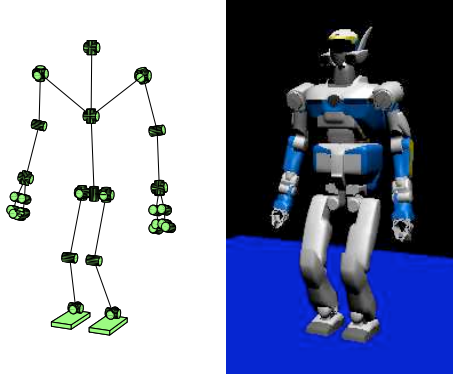


Fig. 1. Description of HRP-2 kinematic structure.

Generally, the virtual actor has more degree of freedoms than the humanoid robot and as well its links lengths are different from those of humanoid robot.

The imitation problem, from a kinematic point of view, is well known in computer graphics and it is called motion retargeting [10]. The motion retargeting problem is formulated as follows

$$\min_{\mathbf{q}_t} \int_{t_0}^{t_f} (\mathbf{q}_t - \mathbf{q}_t^c)^T (\mathbf{q}_t - \mathbf{q}_t^c) + \sigma (P_t - P_t^c)^T (P_t - P_t^c) dt$$

subject to

$$\begin{cases} \mathbf{q}_{t_0} = \mathbf{q}_0 \\ \mathbf{q}_{t_f} = \mathbf{q}_f \\ \mathbf{q}^- \leq \mathbf{q}_t \leq \mathbf{q}^+ \end{cases} \quad (1)$$

where  $\sigma$  is a user defined constant.  $\mathbf{q}_t$  and  $\mathbf{q}_t^c$  are the vectors of angular values of the humanoid robot's joints and the corresponding joints of virtual actor respectively.  $P_t$  and  $P_t^c$  are the Cartesian positions of the hands and head of humanoid robot and virtual actor in the pelvis frame, and it is defined as follows

$$P_t = \begin{bmatrix} P_{\text{head}} \\ P_{\text{right hand}} \\ P_{\text{left hand}} \end{bmatrix} \quad (2)$$

Note that if the lengths of the virtual actor's links are largely different from those of humanoid robot, the vector  $P_t^c$  can be scaled to fit the humanoid robot size.  $\mathbf{q}^-$  and  $\mathbf{q}^+$  denote the minimal and maximal values of vector  $\mathbf{q}_t$  respectively.

The retargeting problem has been extremely studied in computer graphics during the last years, and we have actually many commercial graphic softwares that can solve it efficiently.

However, in the motion imitation by a humanoid robot additional difficulties arise such as the joints angular velocity and torques limits.

By taking into account those additional constraints, the motion

imitation problem becomes

$$\min_{\mathbf{q}_t, \dot{\mathbf{q}}_t, \ddot{\mathbf{q}}_t} \int_{t_0}^{t_f} (\mathbf{q}_t - \mathbf{q}_t^c)^T (\mathbf{q}_t - \mathbf{q}_t^c) + \sigma (P_t - P_t^c)^T (P_t - P_t^c) dt$$

subject to

$$\text{Permanent constraints} \begin{cases} \mathbf{M}(\mathbf{q}_t) \ddot{\mathbf{q}}_t + \mathbf{C}(\mathbf{q}_t, \dot{\mathbf{q}}_t) = \boldsymbol{\tau}_t \\ \mathbf{q}_{t_0} = \mathbf{q}_0, \dot{\mathbf{q}}_{t_0} = \mathbf{0}, \ddot{\mathbf{q}}_{t_0} = \mathbf{0} \\ \mathbf{q}_{t_f} = \mathbf{q}_f, \dot{\mathbf{q}}_{t_f} = \mathbf{0}, \ddot{\mathbf{q}}_{t_f} = \mathbf{0} \\ \boldsymbol{\tau}^- \leq \boldsymbol{\tau}_t \leq \boldsymbol{\tau}^+ \\ \dot{\mathbf{q}}^- \leq \dot{\mathbf{q}}_t \leq \dot{\mathbf{q}}^+ \\ \mathbf{q}^- \leq \mathbf{q}_t \leq \mathbf{q}^+ \end{cases} \quad (3)$$

where  $\boldsymbol{\tau}_t$  is the vector of the applied torques on the humanoid robot's joints.  $\mathbf{M}(\mathbf{q}_t) \ddot{\mathbf{q}}_t + \mathbf{C}(\mathbf{q}_t, \dot{\mathbf{q}}_t) = \boldsymbol{\tau}_t$  is the dynamic equation of motion.

Solving the optimization problem (3) is generally difficult on account of the complicity of the dynamic equation of motion, and the implicit relation between the vector of applied torques  $\boldsymbol{\tau}_t$  and the vector of joints positions  $\mathbf{q}_t$ .

The objective of the following section is giving an overview of an efficient recursive algorithm for multibody dynamics, which allows the calculation of the gradient function of the dynamic equation analytically.

### III. RECURSIVE MULTIBODY DYNAMICS

Park *et al* [11] have proposed to write the recursive multibody dynamics for serial open or branched kinematic chains using Lie group and Lie algebra. The main advantage of this formulation is to relate the joint torques and joint angles explicitly. Therefore the differentiation of joint torques with respect to joint angles can be done analytically.

Let us define the Lie groups  $SO(3)$  and  $SE(3)$ , which denote the orthonormal matrix  $\Theta$  in  $R^{3 \times 3}$  and the homogeneous transformation group respectively. The Lie algebra of  $SO(3)$  and  $SE(3)$  are denoted  $so(3)$  and  $se(3)$  respectively. The operators defined on these groups are: skew, matrix exponential, adjoint map  $Ad_G(\cdot)$ , dual adjoint  $Ad_G^*(\cdot)$ , Lie bracket  $ad_g(\cdot)$  and dual Lie bracket  $ad_g^*(\cdot)$ . For more details on Lie group, Lie algebra and the operators definitions see Appendix.

#### A. Forward Kinematics

The kinematics of an open chain can be modeled as a sequence of homogeneous transformation between consecutive joint frames. Let  $T_{i-1,i} \in SE(3)$  be the transformation matrix between the frame of link  $i$  and the frame of link  $i-1$ . The matrix  $T_{i-1,i}$  can be written using matrix exponential notation as follows

$$T_{i-1,i} = M_i e^{S_i q_i} \quad (4)$$

where  $S_i \in se(3)$  is the joint screw written in the coordinate of link  $i-1$ ,  $q_i$  is the current position of joint  $i$  and  $M_i$  is the coordinate transformation between link  $i$  and link  $i-1$ .

Using the above definition of transformation matrix, the end-effector of a kinematic chain can be calculated by the product

$$\begin{aligned} T_{0,n} &= T_{0,1}T_{1,2}\cdots T_{n-1,n} \\ &= M_1e^{S_1q_1}M_2e^{S_2q_2}\cdots M_n e^{S_nq_n} \end{aligned} \quad (5)$$

Note that by expressing the matrix of transformation in exponential form, we can calculate its derivative with respect to  $q_i$  analytically.

### B. Recursive inverse dynamics of branched chains

Branched chains are serial open chains with two or more branches leading to two or more tip links [11], [12]. In the branched chains two definitions arise :

- *Parent link*: the link inward (towards the base) from a given link.
- *Child link*: the link or links which are outward (towards the tips) from a given link.

#### Spatial velocity of branched chains:

- **Initialization**: Given  $V_0$ .
- **Outward recursion**: loop over all links in depth manner:

$$\begin{aligned} T_{P,i} &= M_i e^{S_i q_i} \\ V_i &= Ad_{T_{P,i}^{-1}}(V_P) + S_i \dot{q}_i \\ a_i &= -ad_{S_i \dot{q}_i}(V_i) \\ b_i &= -ad_{V_i}^*(J_i V_i) \end{aligned} \quad (6)$$

where the index  $P$  denotes the parent link of link  $i$ ,  $T_{P,i}$  designs the mapping from the link  $i$  to its parent  $P$  and  $V_P$  denotes the spatial velocity of link  $P$ .

**Applied torques on the branched chains**: In order to calculate the inward recursion of forces and torques, we define the external forces applied on a link  $j$  by  $\hat{F}_j$ .

- **Initialization**: Given the external applied forces on each link  $\hat{F}_j$ ,  $\dot{V}_0$  and  $\hat{J}_j = 0$  for each tip link.
- **Inward recursion**: loop over all links in reversed breadth

$$\begin{aligned} \dot{V}_i &= Ad_{T_{P,i}^{-1}}(\dot{V}_P) + S_i \dot{q}_i + a_i \\ \hat{J}_i &= J_i + \sum_{j \in C} Ad_{T_{i,j}^*}^* \hat{J}_j Ad_{T_{i,j}^{-1}} \\ B_i &= b_i + \sum_{j \in C} Ad_{T_{i,j}^*}^* z_j \\ z_i &= \hat{J}_i (S_i \dot{q}_i + a_i) + B_i + \sum_{j \in C} Ad_{T_{i,j}^*}^* \hat{F}_j \\ F_i &= \hat{J}_i Ad_{T_{P,i}^{-1}}(\dot{V}_P) + z_i \\ \tau_i &= S_i^T F_i \end{aligned} \quad (7)$$

where  $C$  denotes the child links for link  $i$ , and  $\tau_i$  is the torque applied on the joint  $i$ .

The matrix  $J_i$  is called the spatial inertia and it is defined as follows

$$J_i = \begin{bmatrix} I_i - m_i [r_i]^2 & m_i [r_i] \\ -m_i [r_i] & m_i \mathbf{1} \end{bmatrix} \quad (8)$$

where  $I_i$  is the inertia of the link  $i$  about its centre of mass and  $m$  is its mass.  $r_i$  is the vector from the point of application of the force and the centre of mass of the link  $i$ . Recall that  $[r_i]$  is the skew operator see Appendix for more details.

## IV. OPTIMIZATION PROBLEM REFORMULATION

Using Eq. (7), the dynamic equation of motion  $\mathbf{M}(\mathbf{q}_t)\ddot{\mathbf{q}}_t + \mathbf{C}(\mathbf{q}_t, \dot{\mathbf{q}}_t) = \tau_t$  can be rewritten as follows

$$S^T F_t = \tau_t \quad (9)$$

where  $\tau_t$ ,  $F_t$  and  $S$  are defined as follows

$$\tau_t = \begin{bmatrix} \tau_{1,t} \\ \tau_{2,t} \\ \vdots \\ \tau_{n,t} \end{bmatrix}, F_t = \begin{bmatrix} F_{1,t} \\ F_{2,t} \\ \vdots \\ F_{n,t} \end{bmatrix}, S = \begin{bmatrix} S_1 & 0 & \cdots & 0 \\ 0 & S_2 & \cdots & 0 \\ \vdots & \ddots & \ddots & \vdots \\ 0 & \cdots & 0 & S_n \end{bmatrix} \quad (10)$$

$\tau_t$  and  $F_t$  are the vectors of the applied torques and forces on the humanoid robot's joints respectively.  $\tau_{i,t}$  and  $F_{i,t}$  denote the value of the applied torque and force on the joint  $i$  respectively.

In order to transform this optimization problem into a classical optimization problem, let us define

$$\begin{aligned} X_t &= [\mathbf{q}_t^T \quad \dot{\mathbf{q}}_t^T \quad \ddot{\mathbf{q}}_t^T]^T \\ L(X_t) &= \min_{X_t} \int_{t_0}^{t_f} (\mathbf{q}_t - \mathbf{q}_t^c)^T (\mathbf{q}_t - \mathbf{q}_t^c) + \cdots \\ &\quad \sigma (P_t - P_t^c)^T (P_t - P_t^c) dt \\ G(X_t) &= \begin{bmatrix} \tau_t - \tau^+ \\ -\tau_t + \tau^- \\ \dot{\mathbf{q}}_t - \dot{\mathbf{q}}^+ \\ -\dot{\mathbf{q}}_t + \dot{\mathbf{q}}^- \\ \mathbf{q}_t - \mathbf{q}^+ \\ -\mathbf{q}_t + \mathbf{q}^- \end{bmatrix}, H(X_t) = \begin{bmatrix} \tau_t - S^T F_t \\ \mathbf{q}_{t_0} - \mathbf{q}_0 \\ \dot{\mathbf{q}}_{t_0} \\ \ddot{\mathbf{q}}_{t_0} \\ \mathbf{q}_{t_f} - \mathbf{q}_f \\ \dot{\mathbf{q}}_{t_f} \\ \ddot{\mathbf{q}}_{t_f} \end{bmatrix} \end{aligned} \quad (11)$$

Thus the optimization problem (3) can be transformed into the following classical form

$$\begin{aligned} &\min_{X_t} L(X_t) \\ &\text{subject to} \\ &H(X_t) = 0 \\ &G(X_t) \leq 0 \end{aligned} \quad (12)$$

The above optimization problem has been extremely studied in the literature of optimization theory. To solve this optimization problem, one can use the augmented Lagrange multiplier method, which is a very efficient and reliable method [13]. Using the augmented Lagrange multiplier method transforms the optimization problem (12) to the minimization of the following function

$$\min_{X_t, \lambda} \tilde{L}(X_t, \lambda) = L(X_t) + \lambda_{\psi}^T \psi + \frac{1}{2} \sigma \psi^T \psi + \lambda_H^T H + \frac{1}{2} \sigma H^T H \quad (13)$$

where  $\lambda = [\lambda_{\psi}^T \quad \lambda_H^T]^T$ ,  $\psi = \max \{G(X_t), \frac{-1}{\sigma} \lambda_{\psi}\}$ . Then there exist  $\lambda^*$  such that  $X_t^*$  is an unconstrained local minimum of  $\tilde{L}(X_t, \lambda^*)$  for all  $\sigma$  larger than some finite  $\bar{\sigma}$ .

To solve the unconstrained optimization problem of  $\tilde{L}(X_t, \lambda)$  with respect to  $X_t$ , one can use Gauss-Newton method. Note that the function  $\tilde{L}(X_t, \lambda)$  is differentiable in  $X_t$  if and only if

$L(X_t)$ ,  $H(X_t)$  and  $G(X_t)$  are differentiable in  $X_t$ , and in this case we can write

$$\frac{\partial \tilde{L}(X_t, \lambda)}{\partial X_t} = \frac{\partial L(X_t)}{\partial X_t} + (\lambda_H + \sigma H)^T \frac{\partial H(X_t)}{\partial X_t} + \max\{0, \lambda_\psi + \sigma G(X_t)\}^T \frac{\partial G(X_t)}{\partial X_t} \quad (14)$$

As  $\lambda^*$  is unknown, an update rule is used

$$\begin{aligned} \lambda_H^{k+1} &= \lambda_H^k + \sigma H(X_t^k) \\ \lambda_\psi^{k+1} &= \lambda_\psi^k + \sigma \psi(X_t^k) \end{aligned} \quad (15)$$

where  $X_t^k$  is the unconstrained minimum of  $\tilde{L}(X_t, \lambda^k)$ . Such updating rule will generate a sequence  $\lambda^k$  converges to  $\lambda^*$  [14]. In practice, a good schedule is to choose a moderate  $\sigma^0$ , and increase it as follows

$$\sigma^{k+1} = \alpha \sigma^k \quad (16)$$

where  $\alpha$  is between 5 and 10. A threshold  $\bar{\sigma}$  is chosen and the update rule of  $\sigma$  stops when  $\sigma^k$  becomes higher than  $\bar{\sigma}$ .

For more details on the algorithm of augmented multiplier Lagrange method see [15], [13], [14].

Approximating the gradient function  $\frac{\partial \tilde{L}(X_t, \lambda)}{\partial X_t}$  by a numerical difference method is usually used in practice. However, this approach is not only a time consuming method on account of the evaluation of the gradient calculation, but also may not converge well because of the approximation.

As we have mentioned the main advantage of using the recursive dynamic algorithm explained in Section III-B is calculating the gradient function analytically in a recursive way.

#### A. Gradient calculation

The objective is to calculate the gradient of the dynamic quantities. By considering the vector of parameters  $X_t = [\mathbf{q}_t^T \quad \dot{\mathbf{q}}_t^T \quad \ddot{\mathbf{q}}_t^T]^T$ , let us start by calculating the derivatives of the operators with respect to an element  $x$  of  $X_t$

$$\begin{aligned} \frac{\partial T_{0,n}}{\partial x} &= T_{0,i} (S_i \delta_{x,q_i}) T_{i,n} \\ \frac{\partial Ad_{T_{i-1,i}}^{-1}(Y)}{\partial x} &= ad_{Ad_{T_{i-1,i}}^{-1}(Y)} (S_i \delta_{x,q_i}) + Ad_{T_{i-1,i}}^{-1} \left( \frac{\partial Y}{\partial x} \right) \\ \frac{\partial Ad_{T_{i,i+1}}^*(Y)}{\partial x} &= ad_{Ad_{T_{i,i+1}}^*(Y)} (S_{i+1} \delta_{x,q_{i+1}}) \left( Ad_{T_{i,i+1}}^*(Y) \right) + \dots \\ &\quad Ad_{T_{i,i+1}}^* \left( \frac{\partial Y}{\partial x} \right) \\ \frac{\partial ad_Z(Y)}{\partial x} &= ad_{\frac{\partial Z}{\partial x}}(Y) + ad_Z \left( \frac{\partial Y}{\partial x} \right) \\ \frac{\partial ad_Z^*(Y)}{\partial x} &= ad_{\frac{\partial Z}{\partial x}}^*(Y) + ad_Z^* \left( \frac{\partial Y}{\partial x} \right) \end{aligned} \quad (17)$$

where  $\delta_{x_1, x_2}$  is the Kronecker delta defined as follows

$$\delta_{x_1, x_2} = \begin{cases} 1 & \text{if } x_1 = x_2 \\ 0 & \text{otherwise} \end{cases} \quad (18)$$

The calculation of the gradient with respect to  $X_t$  can be done in a recursive way analogously to the recursive dynamic calculation.

#### Forward recursion:

- **Initialization:** Given  $\frac{\partial V_0}{\partial X_t}$ .
- loop over all links in depth manner:

$$\begin{aligned} \frac{\partial V_i}{\partial X_t} &= \frac{\partial Ad_{T_{P_i}}^{-1}(V_P)}{\partial X_t} + S_i \frac{\partial \dot{q}_i}{\partial X_t} \\ \frac{\partial a_i}{\partial X_t} &= - \frac{\partial ad_{S_i \dot{q}_i}(V_i)}{\partial X_t} \\ \frac{\partial b_i}{\partial X_t} &= - \frac{\partial ad_{V_i}^*(J_i V_i)}{\partial X_t} \end{aligned} \quad (19)$$

#### Backward recursion:

- **Initialization:** Given  $\frac{\partial \hat{F}_j}{\partial X_t}, \frac{\partial V_0}{\partial X_t}$ .
- loop over all links in reversed breadth

$$\begin{aligned} \frac{\partial \dot{V}_i}{\partial X_t} &= \frac{\partial Ad_{T_{P_i}}^{-1}(\dot{V}_P)}{\partial X_t} + S_i \frac{\partial \dot{q}_i}{\partial X_t} + \frac{\partial a_i}{\partial X_t} \\ \frac{\partial \hat{F}_i}{\partial X_t} &= \sum_{j \in C} \frac{\partial Ad_{T_{i,j}}^*}{\partial X_t} \hat{F}_j Ad_{T_{i,j}}^{-1} + \dots \\ &\quad Ad_{T_{i,j}}^* \hat{F}_j \frac{\partial Ad_{T_{i,j}}^*}{\partial X_t} + Ad_{T_{i,j}}^* \frac{\partial \hat{F}_j}{\partial X_t} Ad_{T_{i,j}}^{-1} \\ \frac{\partial B_i}{\partial X_t} &= \frac{\partial b_i}{\partial X_t} + \sum_{j \in C} \frac{\partial Ad_{T_{i,j}}^* z_j}{\partial X_t} \\ \frac{\partial z_i}{\partial X_t} &= \frac{\partial \hat{F}_i}{\partial X_t} (S_i \dot{q}_i + a_i) + \hat{F}_i \left( S_i \frac{\partial \dot{q}_i}{\partial X_t} + \frac{\partial a_i}{\partial X_t} \right) + \dots \\ &\quad \frac{\partial B_i}{\partial X_t} + \sum_{j \in C} \frac{\partial Ad_{T_{i,j}}^* \hat{F}_j}{\partial X_t} \\ \frac{\partial F_i}{\partial X_t} &= \frac{\partial \hat{F}_i}{\partial X_t} Ad_{T_{P_i}}^{-1}(\dot{V}_P) + \hat{F}_i \frac{\partial Ad_{T_{P_i}}^{-1}(\dot{V}_P)}{\partial X_t} + \frac{\partial z_i}{\partial X_t} \\ \frac{\partial \tau_i}{\partial X_t} &= S_i^T \frac{\partial F_i}{\partial X_t} \end{aligned} \quad (20)$$

where as we mentioned  $C$  denotes the child links for link  $i$ .

#### V. DISCRETIZATION OF CONFIGURATION SPACE

It is well known that the space of the admissible solutions of the minimization problem (3) is very large. In order to transform this infinite dimensional space to a finite one, we can use a basis of shape functions.

Let us consider a basis of shape functions  $B_t$  that is defined as follows

$$B_t = [B_t^1 \quad B_t^2 \quad \dots \quad B_t^l]^T \quad (21)$$

where  $B_t^i$  denotes the value of shape function number  $i$  at the instant  $t$ , the dimension of  $B_t$  is  $l$  defines the dimension of the basis of shape functions.

The projection of the vector of angular values  $\mathbf{q}_t$  into the basis of shape functions  $B_t$  can be given by the following formula

$$\mathbf{q}_t = Q_B B_t \quad (22)$$



where  $Q_B$  is a constant matrix.

The derivative  $\dot{\mathbf{q}}_t$  and  $\ddot{\mathbf{q}}_t$  can be written as follows

$$\begin{aligned}\dot{\mathbf{q}}_t &= Q_B \dot{B}_t \\ \ddot{\mathbf{q}}_t &= Q_B \ddot{B}_t\end{aligned}\quad (23)$$

In this case, the derivative with respect to each element  $Q_B(i, j)$  of the matrix  $Q_B$  can be computed using the following formula

$$\begin{aligned}\frac{\partial Y_t}{\partial Q_B(i, j)} &= \frac{\partial Y_t}{\partial X_t} \times \frac{\partial X_t}{\partial Q_B(i, j)} \\ &= \frac{\partial Y}{\partial X_t} \times e^i [B_t^j \quad \dot{B}_t^j \quad \ddot{B}_t^j]\end{aligned}\quad (24)$$

where

$$e^i = [0 \quad \dots \quad 0 \quad 1 \quad 0 \quad \dots \quad 0]^T$$

↑  
i

By using the discretization of the configuration space, the problem of optimization transforms into the problem of finding the optimal matrix  $Q_B$ , which minimizes the function  $\tilde{L}(X_t, \lambda)$  in Eq. (13).

It remains to define the shape functions  $B_t^i$ . In our case, the shape functions should verify the following properties:

- 1) They are continuous.
- 2) Their first and second derivatives are continuous.

Therefore, we use the *quartic B-spline functions*.

## VI. EXPERIMENTAL RESULTS

The motion that we have chosen to validate the proposed method is a boxing captured motion. This motion is a challenging motion to be imitated on account of the complexity of upper body movements. The vertical movement of the pelvis joint is also considered, and the movements of the lower body is calculated using inverse kinematic. Snapshots of the conducted motion using OpenHRP platform [16] are presented in Fig. 2. In order to assure the dynamical stability of humanoid robot, the trajectory of ZMP is controlled using the method of cart table model proposed by Kajita *et al* [8] as follows

- 1) the ZMP trajectory of the optimized motion is calculated.
- 2) the calculated ZMP trajectory is bounded to be inside the polygon of support feet and it is then filtered to have a smooth trajectory.
- 3) Once the filtered ZMP trajectory is available, we use the cart table model [8] to calculate the trajectory of the centre of mass.
- 4) The horizontal trajectory of the free flyer (pelvis joint) is then calculated using the trajectory of the centre of mass.

In Fig. 3 the angular position trajectories of the virtual actor's right elbow joint and the optimized trajectory are given. The optimized trajectory respects the physical limits of HRP-2 humanoid robot, which are not only the angle limits but also the angular velocity and torques limits.

However, the self collision problem is not considered in this work as shown in Fig. 4. Although, approximating the humanoid robot's links by cylinders and spheres, and then consider the distance between them as an additional constraint can solve the problem of self collision, this procedure may yield an imitated motion largely different from the original human captured motion on account of the approximation. Therefore, we believe that using efficient methods as those proposed in [17], [18], [19] which take into account the detailed geometry model of humanoid robot and collision pairs as many as possible can give better results.

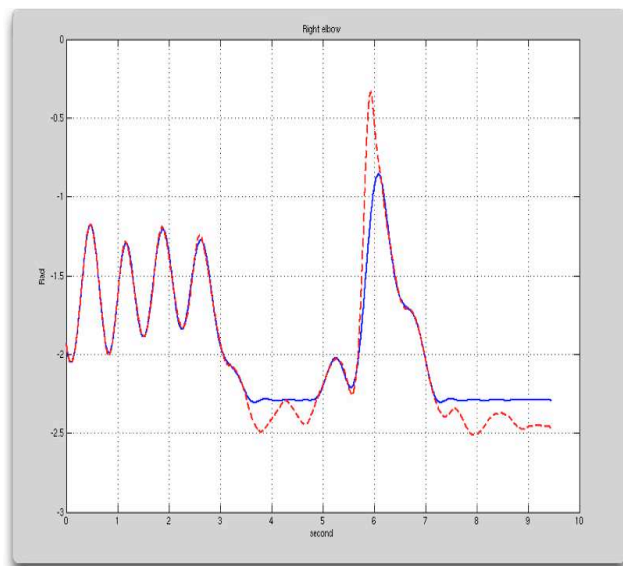


Fig. 3. Angular position of right elbow: the dashed line for the original motion of virtual actor and the solid line after the optimization and considering the physical limits of HRP-2 humanoid robot.

## VII. CONCLUSION

In this paper, the human motion imitation by a humanoid robot is considered. In order to generate an imitated motion within the humanoid robot capabilities, the imitation problem is formulated as an optimization problem. The physical limits of the humanoid robot are transformed into constraints of the optimization problem, and the objective function to be minimized is the integral of the difference between the angular values of humanoid robot's joints and the corresponding joints of virtual actor.

The experimental results have pointed out that the proposed method yields imitated motions that preserve the salient characteristics of the original human captured motion, and at the same time they respect the humanoid robot's physical limits.

Future work will focus on the integration of self collision avoiding into the optimization problem as an additional constraint.

## VIII. ACKNOWLEDGMENT

The human captured data used in this paper was obtained from mocap.cs.cmu.edu. The database was created with funding from NSF EIA-0196217.

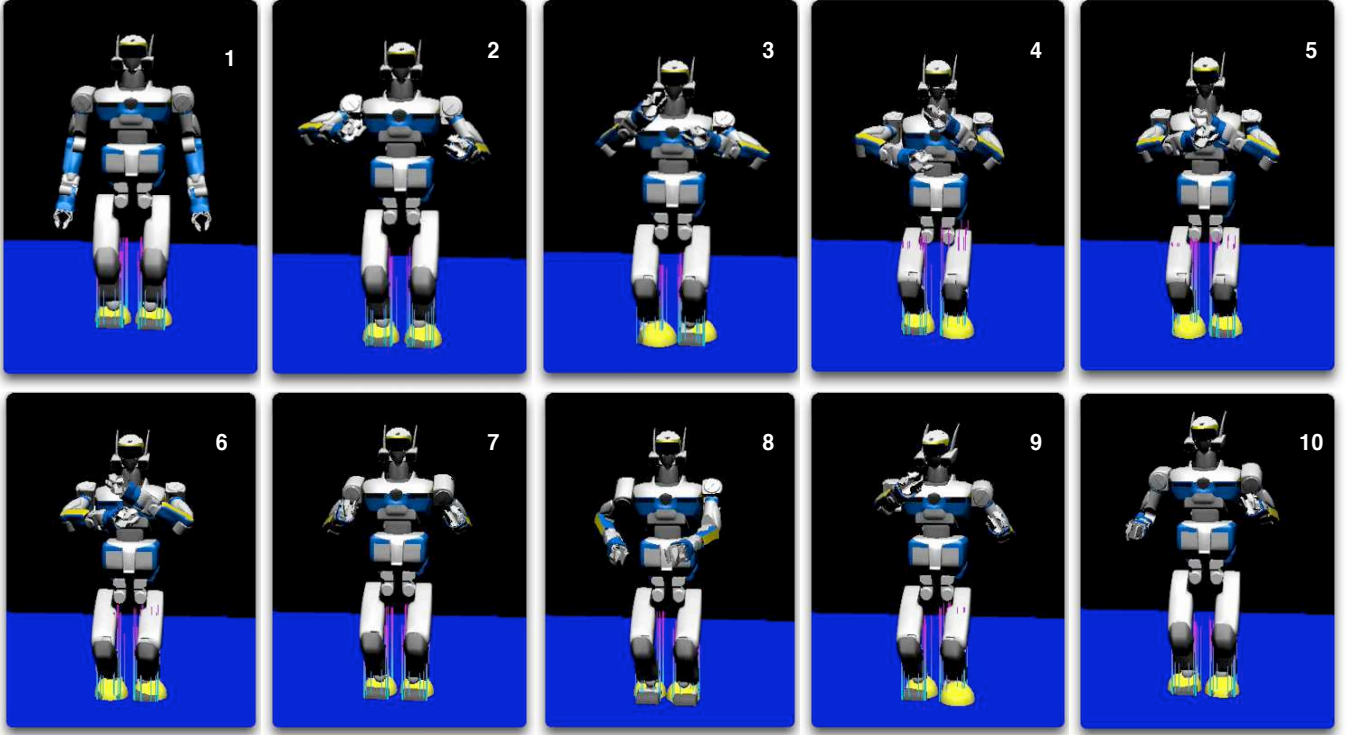


Fig. 2. Snapshots of the conducted motion.

## APPENDIX

A *Lie group* is a differentiable manifold. An example of Lie group is the orthonormal matrix  $\Theta$  in  $R^{3 \times 3}$ , which is called  $SO(3)$ . Note that this group consists of the rotation matrices in Euclidean space. Another example of Lie group is the group of homogeneous transformation which is the special Euclidean group or  $SE(3)$ . Given a rotation  $\Theta \in SO(3)$  and translation  $b \in R^3$ , the homogeneous matrix is defined as follows

$$G = \begin{bmatrix} \Theta & b \\ 0 & 1 \end{bmatrix} \quad (\text{A-1})$$

An important concept associated with each Lie group is the notation of *Lie algebra*. The tangent space at the identity element of a Lie group is called the Lie algebra for that group. The Lie algebra of  $SO(3)$  and  $SE(3)$  are denoted  $so(3)$  and  $se(3)$  respectively.

Let us define some notations and operations on Lie groups and Lie algebra:

1) Skew operator:

$$[\cdot] : \omega \in R^3 \rightarrow so(3)$$

$$[\omega] = \begin{bmatrix} 0 & -\omega_z & \omega_y \\ \omega_z & 0 & -\omega_x \\ -\omega_y & \omega_x & 0 \end{bmatrix} \quad (\text{A-2})$$

2)  $(\cdot, \cdot)$  operator:

$$(\cdot, \cdot) : \{\omega, v\} \in R^3 \rightarrow se(3)$$

$$(\omega, v) = \begin{bmatrix} [\omega] & v \\ 0 & 0 \end{bmatrix} \quad (\text{A-3})$$

3) Matrix exponential:

$$e^{(\omega, v)} = \exp \begin{bmatrix} [\omega] & v \\ 0 & 0 \end{bmatrix} = \begin{bmatrix} \exp([\omega]) & Av \\ 0 & 1 \end{bmatrix} \quad (\text{A-4})$$

where

$$\exp([\omega]) = I + \frac{\sin \phi}{\phi} [\omega] + \frac{1 - \cos \phi}{\phi^2} [\omega]^2, \phi = \|\omega\|$$

$$A = I + \frac{1 - \cos \phi}{\phi^2} [\omega] + \frac{\phi - \sin \phi}{\phi^3} [\omega]^2 \quad (\text{A-5})$$

4) Adjoint map on  $SE(3)$ :

$$Ad_G(h) : se(3) \rightarrow se(3)$$

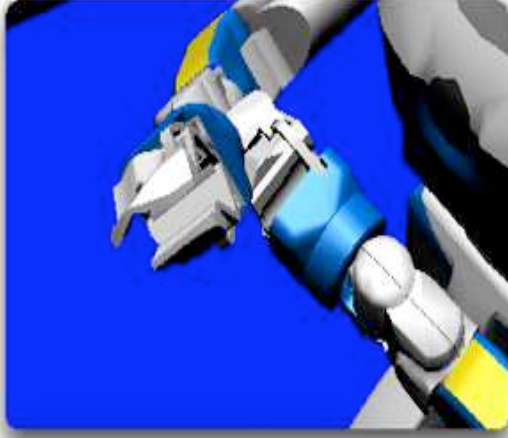
$$Ad_G(h) = \begin{bmatrix} \Theta & 0 \\ [b]\Theta & \Theta \end{bmatrix} \begin{bmatrix} h_\omega \\ h_v \end{bmatrix} \quad (\text{A-6})$$

where  $G \in SE(3)$  is defined as in (A-1), and  $h = (h_\omega, h_v) \in se(3)$ .

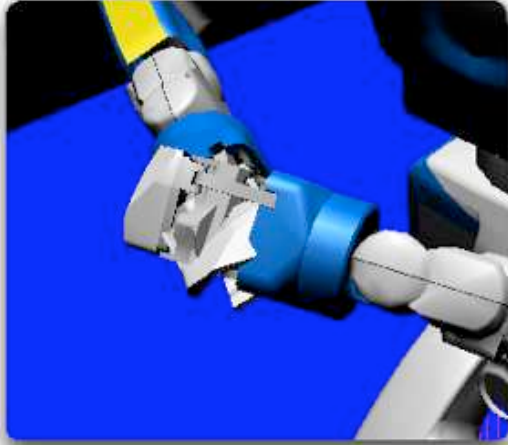
5) Dual adjoint operator:

$$Ad_G^*(h^*) : se(3)^* \rightarrow se(3)^*$$

$$Ad_G^*(h^*) = \begin{bmatrix} \Theta^T & \Theta^T [b]^T \\ 0 & \Theta^T \end{bmatrix} \begin{bmatrix} M \\ F \end{bmatrix} \quad (\text{A-7})$$



(a)



(b)

Fig. 4. Self collisions.

where  $G \in SE(3)$ , and  $h^* = (M, F) \in se(3)^*$ .

6) Lie bracket operator:

$$ad_g(h) = [g, h] = \begin{bmatrix} [g_\omega] & 0 \\ [g_v] & [g_\omega] \end{bmatrix} \begin{bmatrix} h_\omega \\ h_v \end{bmatrix} \quad (A-8)$$

where  $g, h \in se(3)$ .  $h = (h_\omega, h_v)$  and  $g = (g_\omega, g_v)$ .

7) Dual Lie bracket operator:

$$ad_g^*(h^*) = [g, h^*] = \begin{bmatrix} [g_\omega]^T & [g_v]^T \\ 0 & [g_\omega]^T \end{bmatrix} \begin{bmatrix} M \\ F \end{bmatrix} \quad (A-9)$$

where  $g = (g_\omega, g_v) \in se(3)$  and  $h^* = (M, F) \in se(3)^*$ .

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